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# CSE 573: Artificial Intelligence

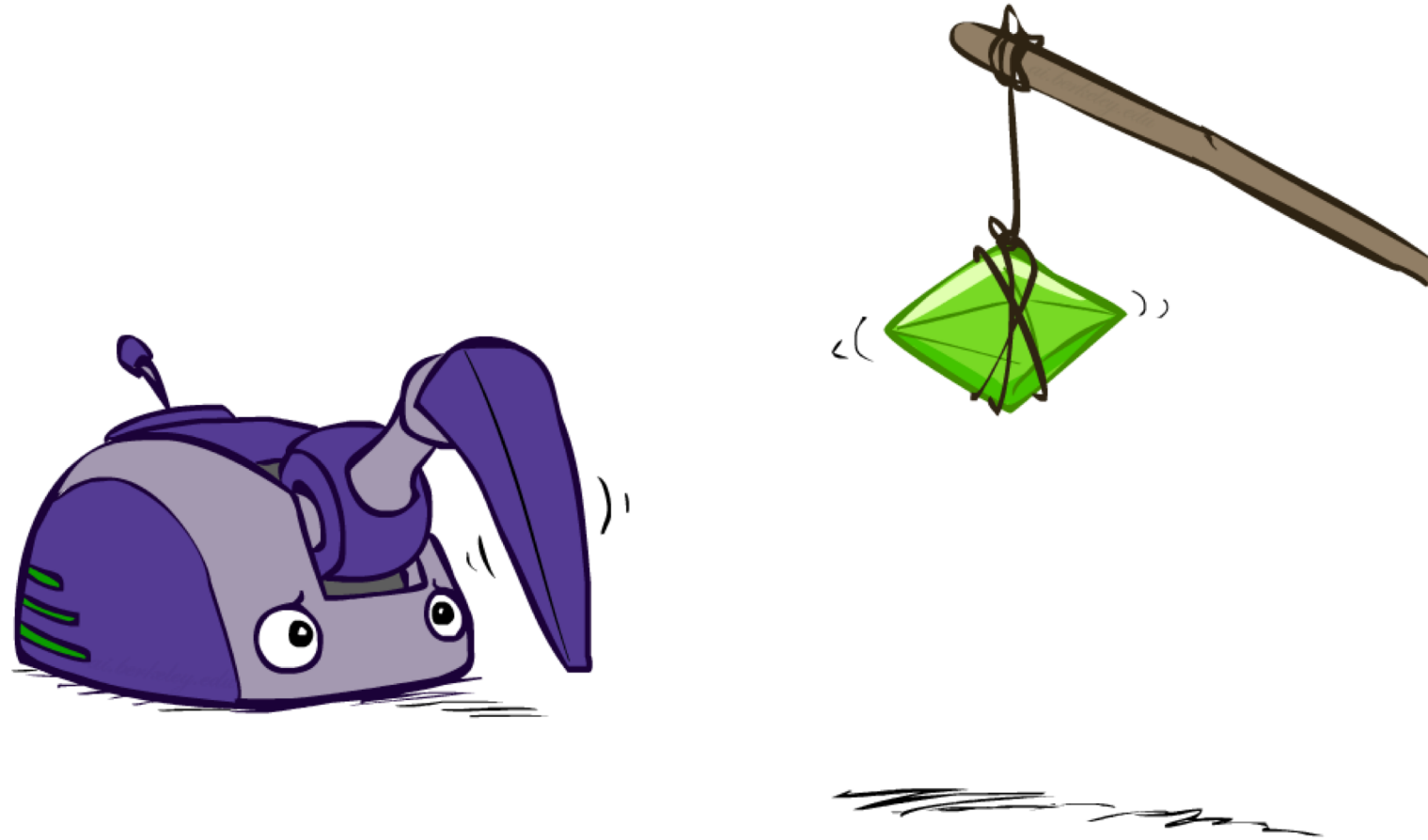
Hanna Hajishirzi  
Reinforcement Learning

slides adapted from  
Dan Klein, Pieter Abbeel [ai.berkeley.edu](http://ai.berkeley.edu)  
And Dan Weld, Luke Zettlemoyer



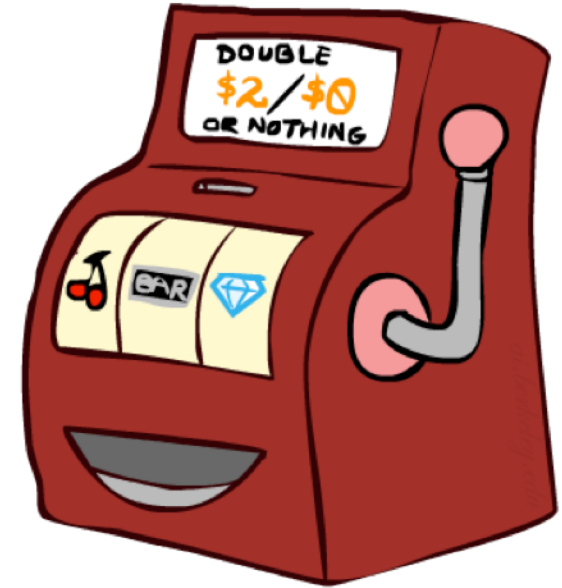
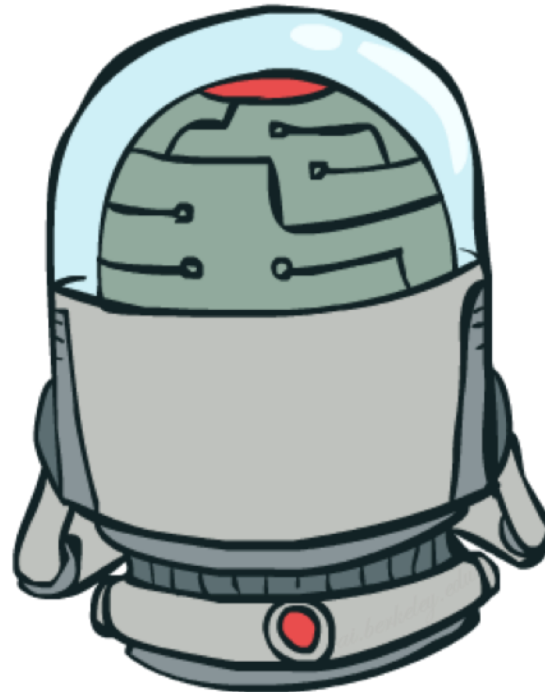
# Reinforcement Learning

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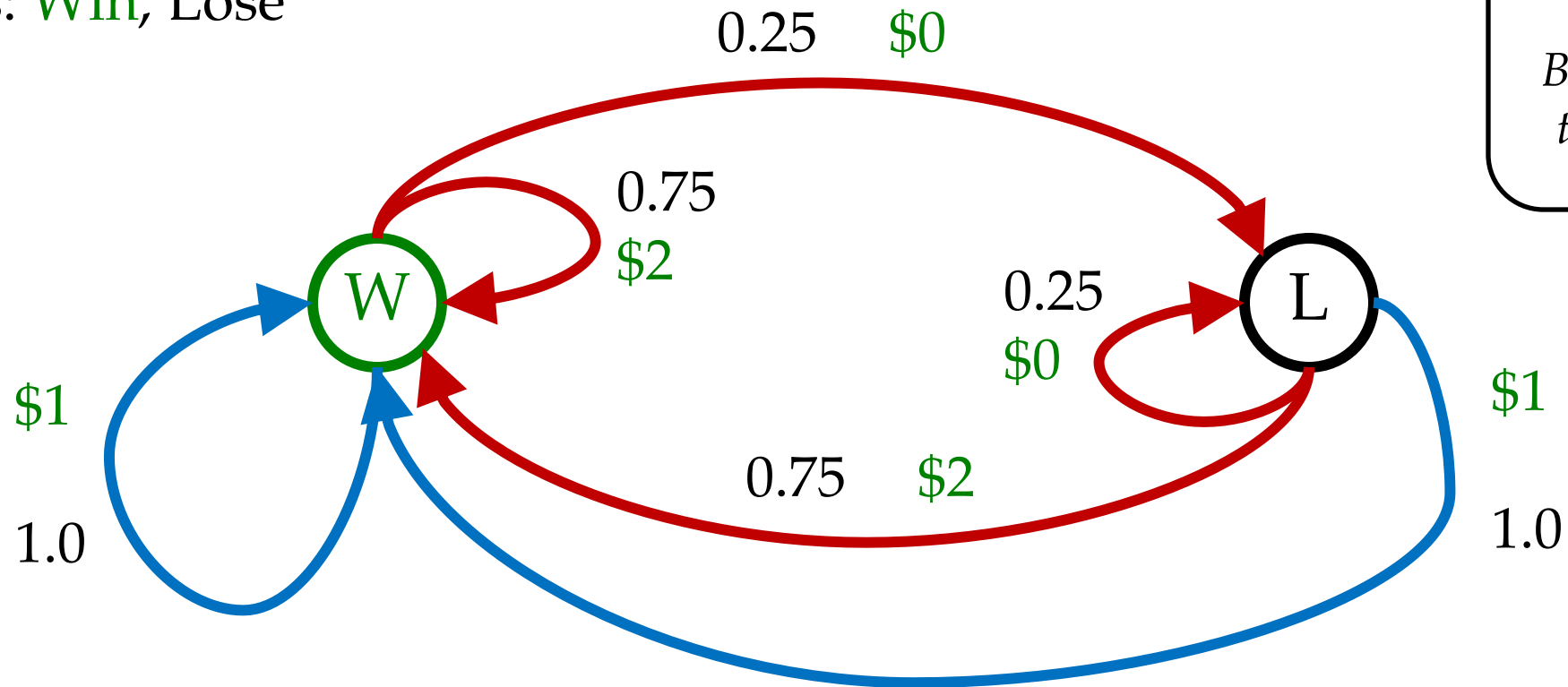
# Double Bandits

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# Double-Bandit MDP

- Actions: *Blue*, *Red*
- States: *Win*, Lose



*No discount*  
*10 time steps*  
*Both states have*  
*the same value*

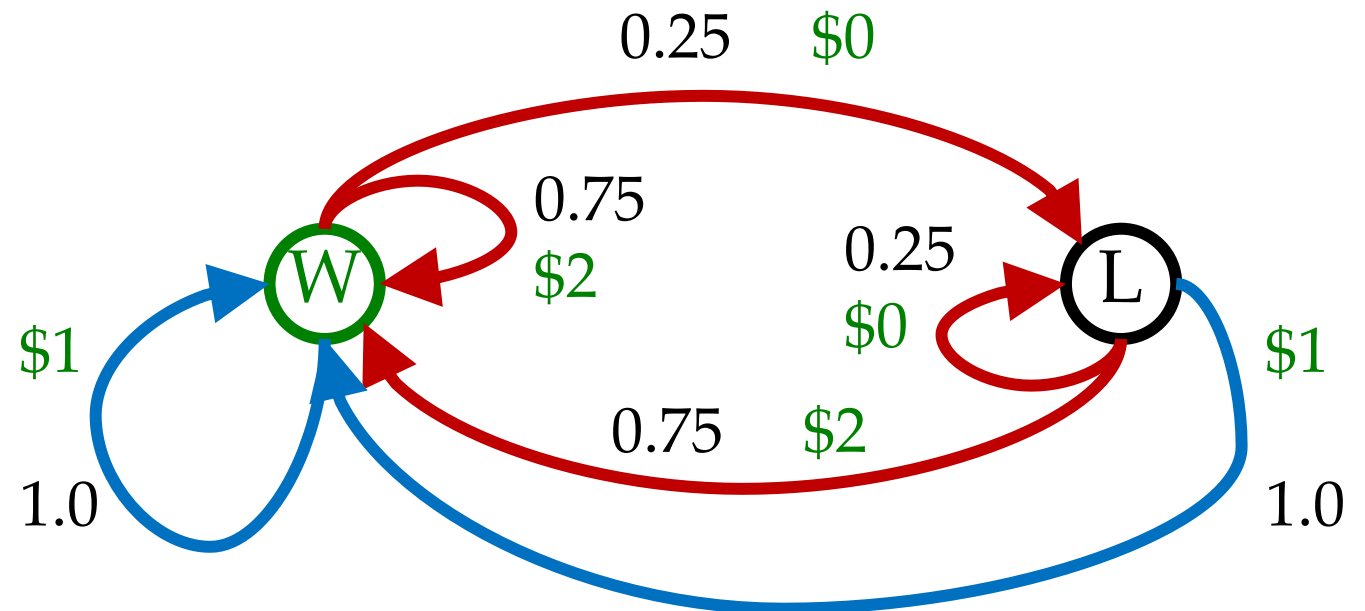


# Offline Planning

- Solving MDPs is offline planning
  - You determine all quantities through computation
  - You need to know the details of the MDP
  - You do not actually play the game!

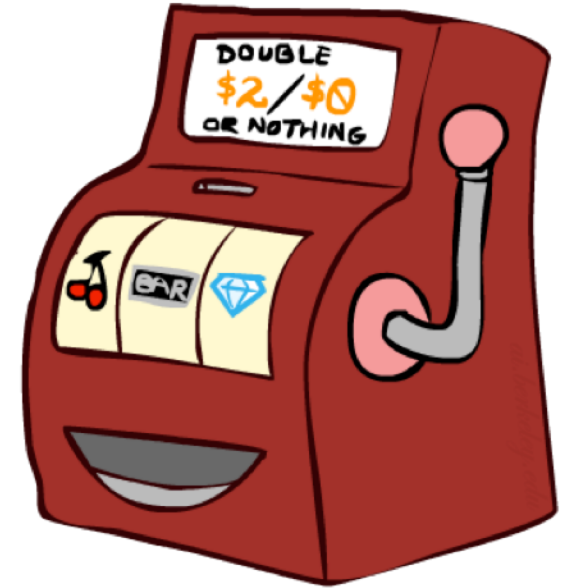
*No discount*  
*10 time steps*

	Value
Play Red	15
Play Blue	10



# Let's Play!

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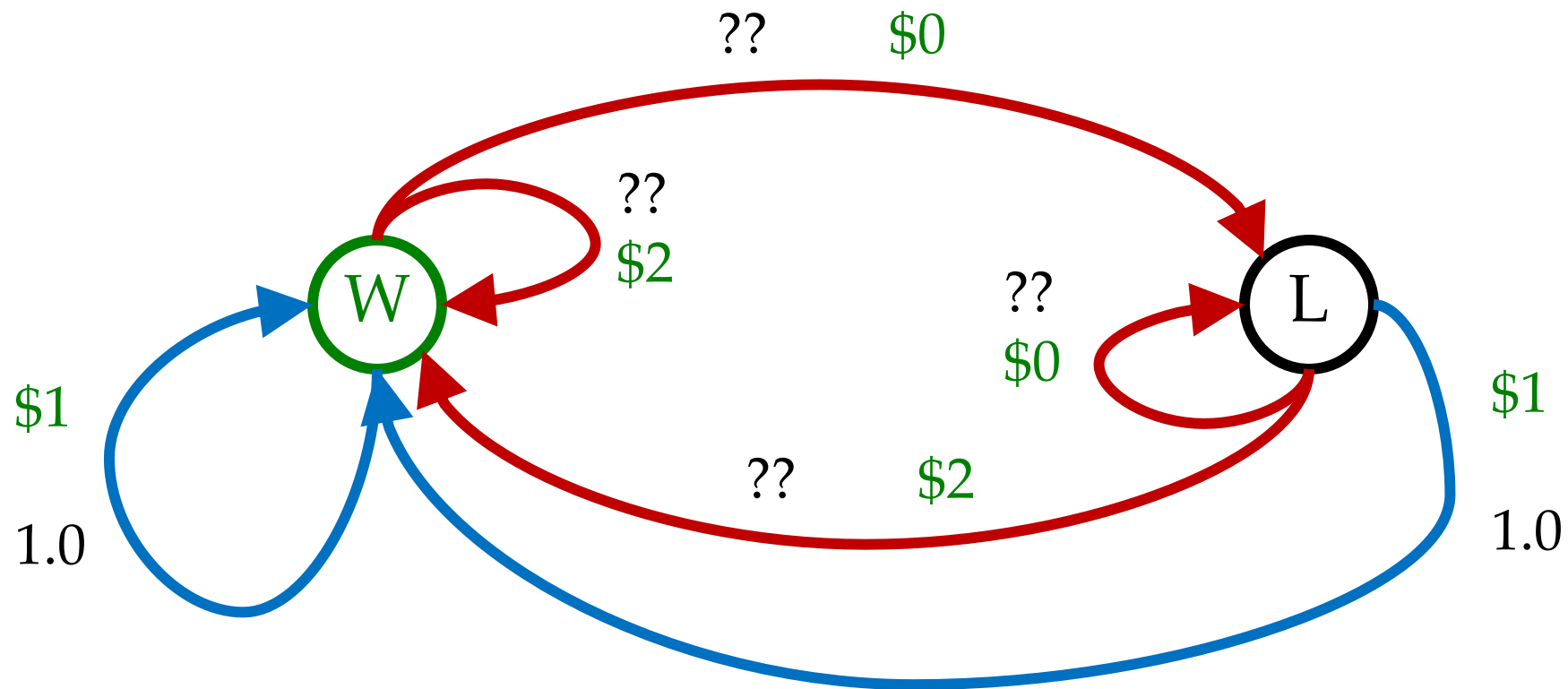


\$2 \$2 \$0 \$2 \$2

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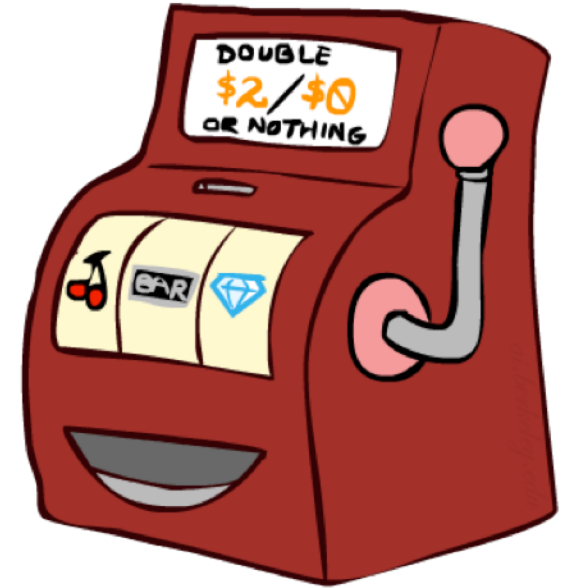
# Online Planning

- Rules changed! Red's win chance is different.



# Let's Play!

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\$0 \$0 \$2 \$0

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\$0

# What Just Happened?

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- That wasn't planning, it was learning!
  - Specifically, reinforcement learning
  - There was an MDP, but you couldn't solve it with just computation
  - You needed to actually act to figure it out
- Important ideas in reinforcement learning that came up
  - Exploration: you have to try unknown actions to get information
  - Exploitation: eventually, you have to use what you know
  - Regret: even if you learn intelligently, you make mistakes
  - Sampling: because of chance, you have to try things repeatedly
  - Difficulty: learning can be much harder than solving a known MDP



# Reinforcement Learning

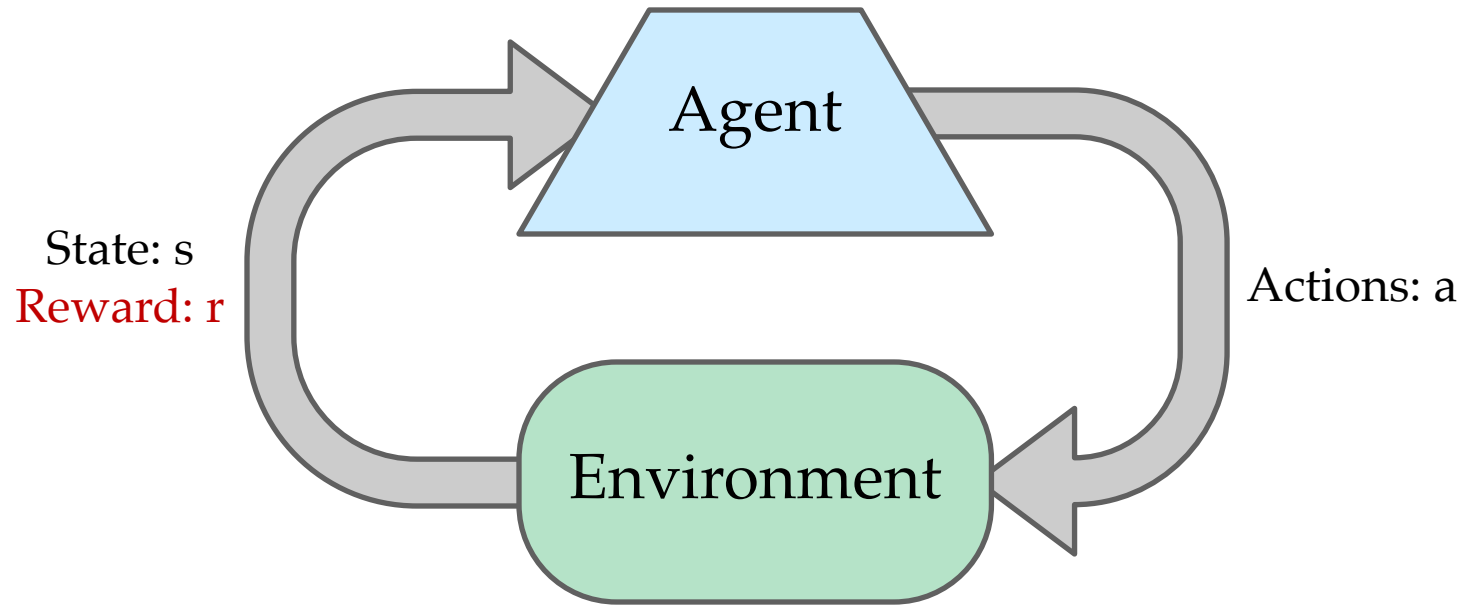
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- Still assume a Markov decision process (MDP):
  - A set of states  $s \in S$
  - A set of actions (per state)  $A$
  - A model  $T(s,a,s')$
  - A reward function  $R(s,a,s')$
- Still looking for a policy  $\pi(s)$
- New twist: don't know  $T$  or  $R$ 
  - I.e. we don't know which states are good or what the actions do
  - Must actually try actions and states out to learn



# Reinforcement Learning

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- Basic idea:
  - Receive feedback in the form of **rewards**
  - Agent's utility is defined by the reward function
  - Must (learn to) act so as to **maximize expected rewards**
  - All learning is based on observed samples of outcomes!

# Example: Learning to Walk

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Initial



A Learning Trial



After Learning [1K Trials]



# Example: Toddler Robot

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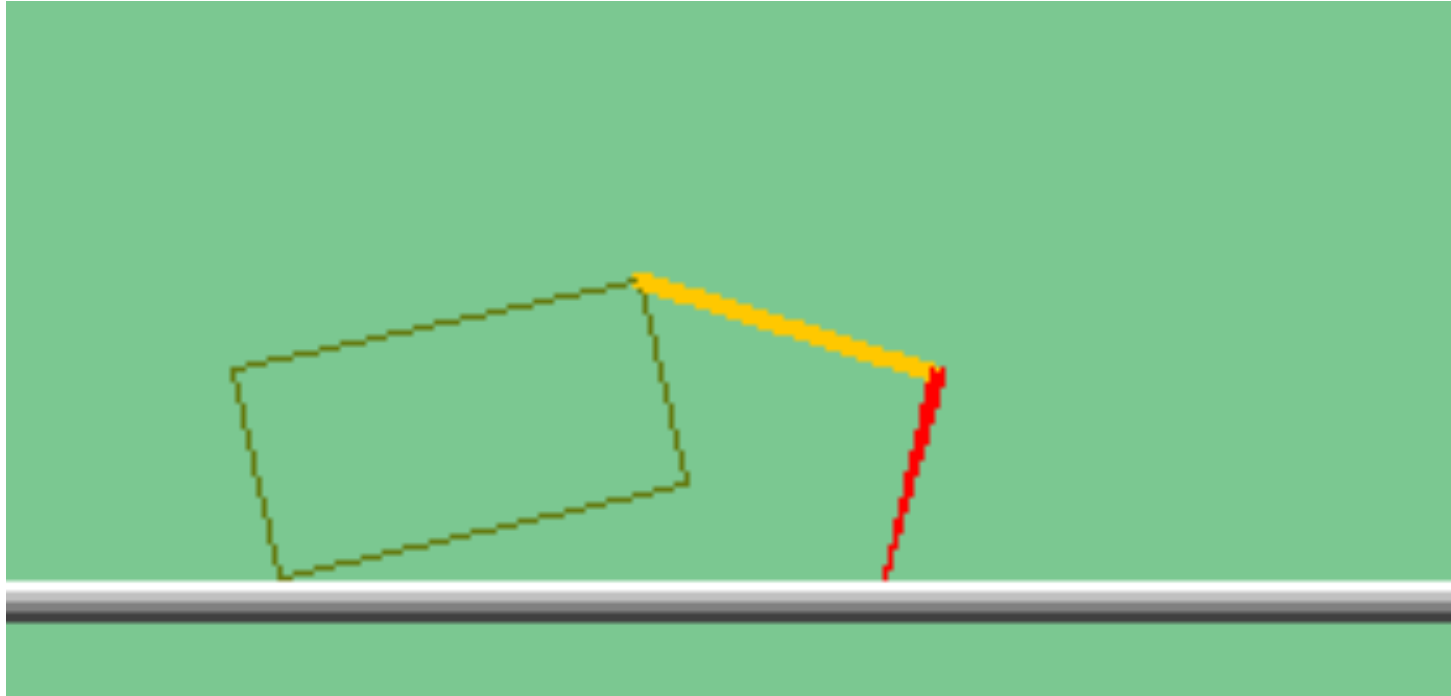
# Robotics Rubik Cub

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- <https://www.youtube.com/watch?v=x4O8pojMF0w>

# The Crawler!

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# Video of Demo Crawler Bot

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# Reinforcement Learning

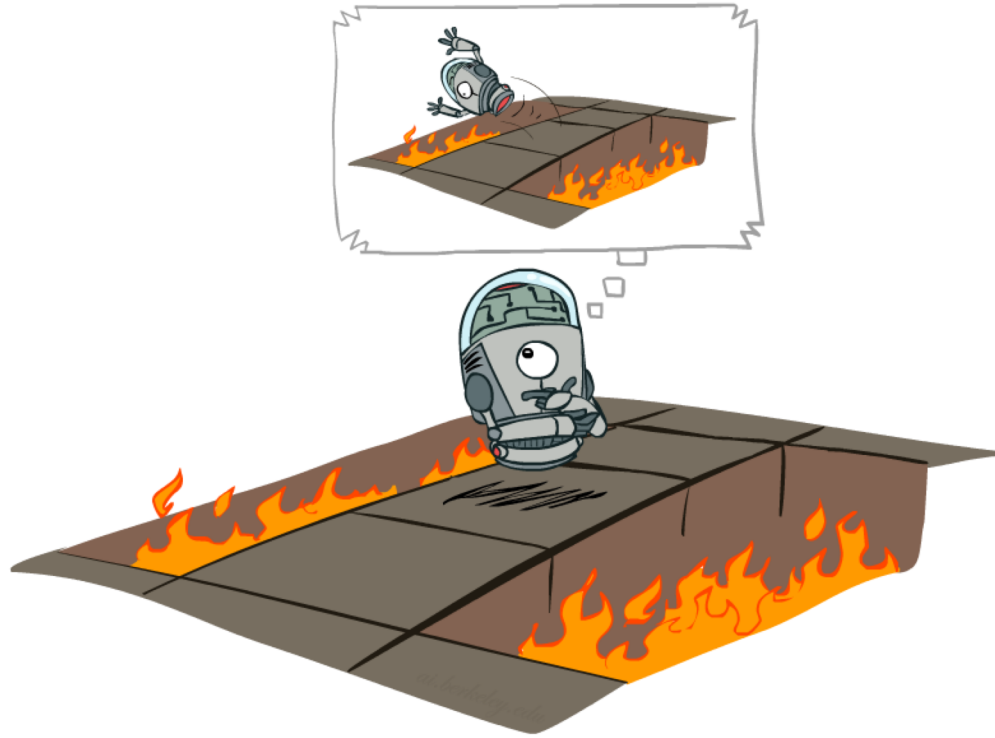
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- New twist: don't know  $T$  or  $R$ 
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  - Must actually try actions and states out to learn



# Offline (MDPs) vs. Online (RL)

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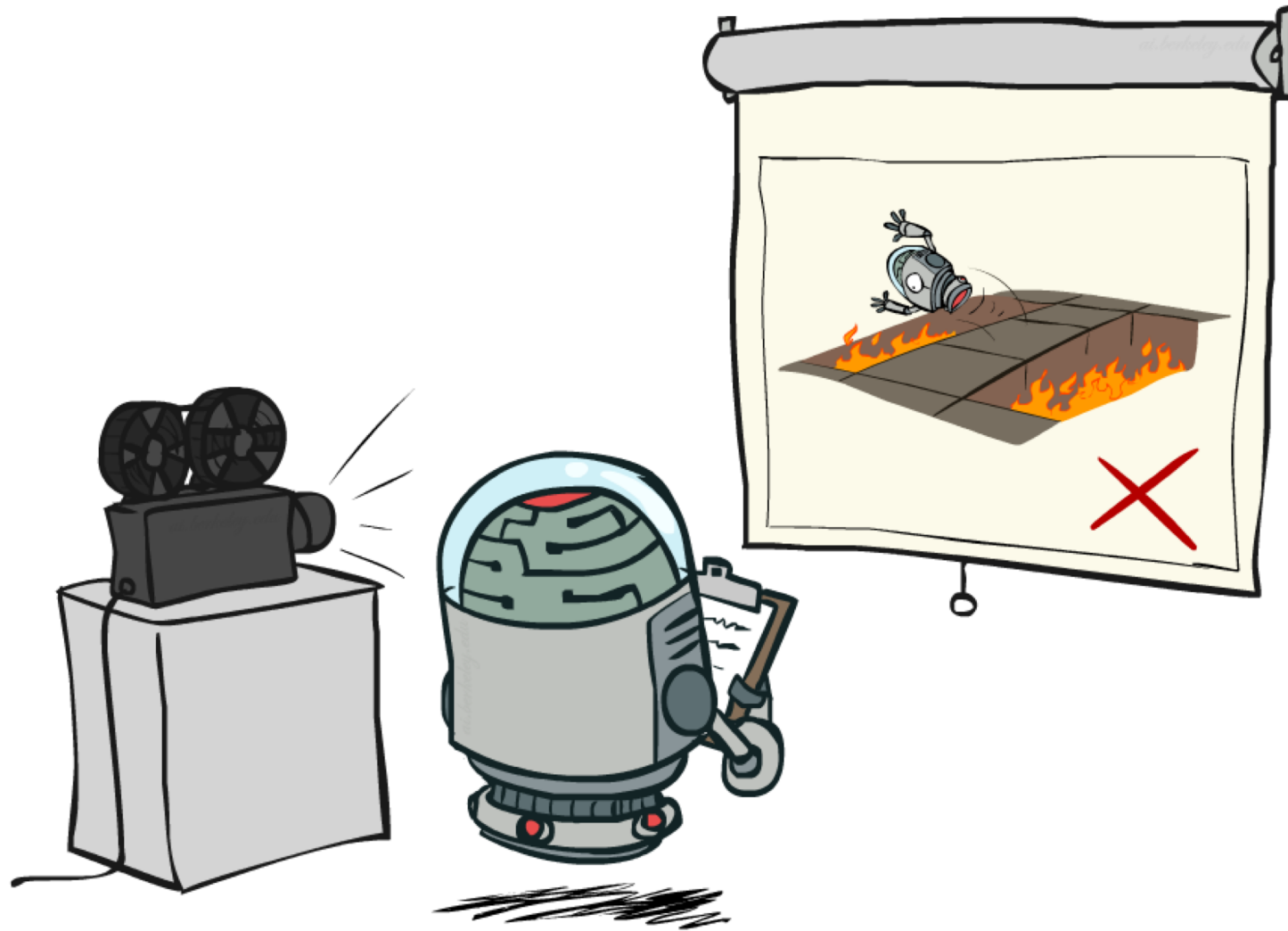
Offline Solution



Online Learning

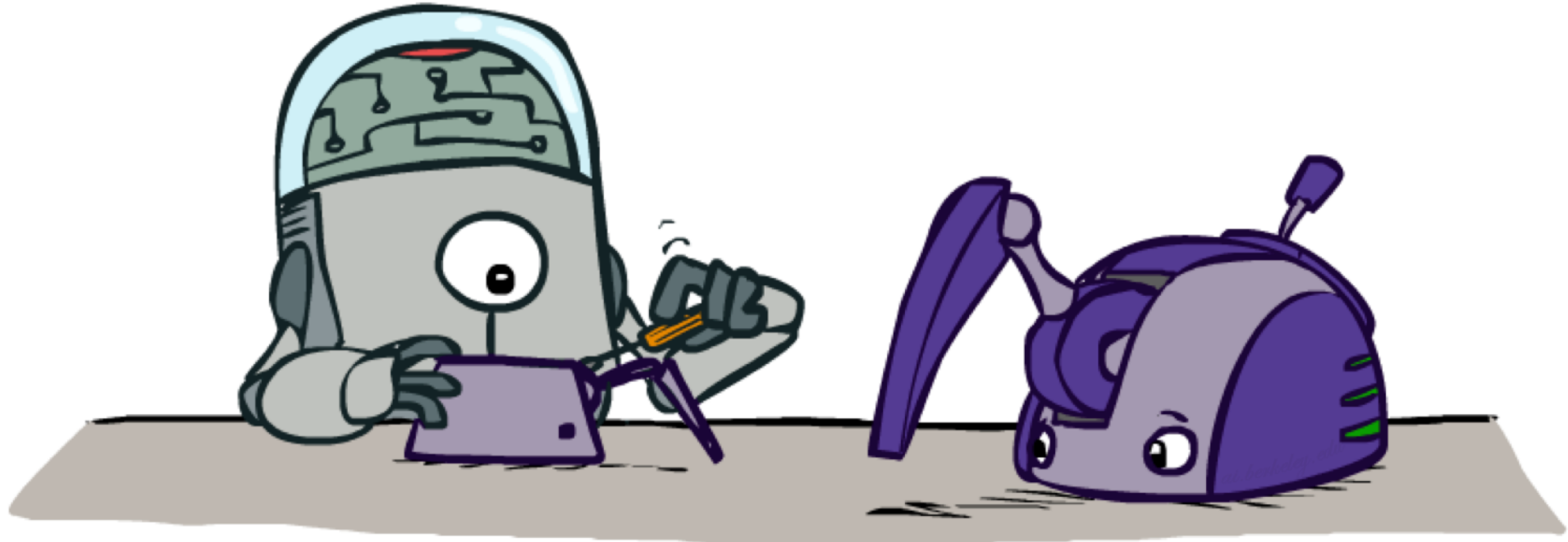
# Passive Reinforcement Learning

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# Model-Based Learning

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# Model-Based Learning

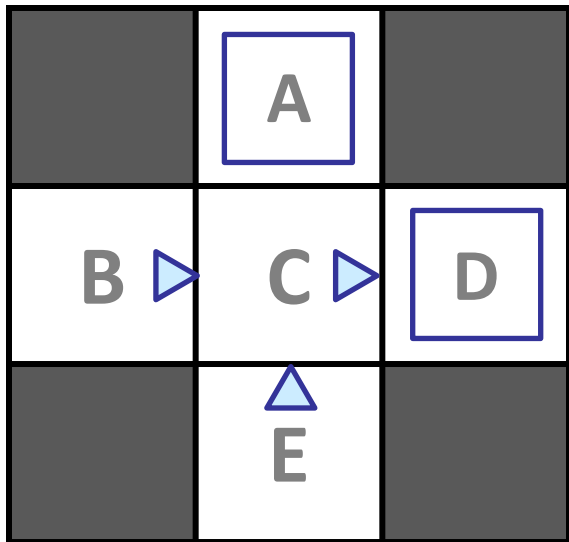
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- Model-Based Idea:
  - Learn an approximate model based on experiences
  - Solve for values as if the learned model were correct
- Step 1: Learn empirical MDP model
  - Count outcomes  $s'$  for each  $s, a$
  - Normalize to give an estimate  $\hat{T}(s, a, s')$
  - Discover each  $\hat{R}(s, a, s')$  when we experience  $(s, a, s')$
- Step 2: Solve the learned MDP
  - For example, use value iteration, as before



# Example: Model-Based Learning

## Input Policy $\pi$



Assume:  $\gamma = 1$

## Observed Episodes (Training)

### Episode 1

B, east, C, -1  
C, east, D, -1  
D, exit, x, +10

### Episode 2

B, east, C, -1  
C, east, D, -1  
D, exit, x, +10

### Episode 3

E, north, C, -1  
C, east, D, -1  
D, exit, x, +10

### Episode 4

E, north, C, -1  
C, east, A, -1  
A, exit, x, -10

## Learned Model

$$\hat{T}(s, a, s')$$

T(B, east, C) = 1.00  
T(C, east, D) = 0.75  
T(C, east, A) = 0.25  
...

$$\hat{R}(s, a, s')$$

R(B, east, C) = -1  
R(C, east, D) = -1  
R(D, exit, x) = +10  
...

# Analogy: Expected Age

Goal: Compute expected age of cse573 students

Known  $P(A)$

$$E[A] = \sum_a P(a) \cdot a = 0.35 \times 20 + \dots$$

Without  $P(A)$ , instead collect samples  $[a_1, a_2, \dots, a_N]$

Unknown  $P(A)$ : “Model Based”

$$\hat{P}(a) = \frac{\text{num}(a)}{N}$$
$$E[A] \approx \sum_a \hat{P}(a) \cdot a$$

Why does this work? Because eventually you learn the right model.

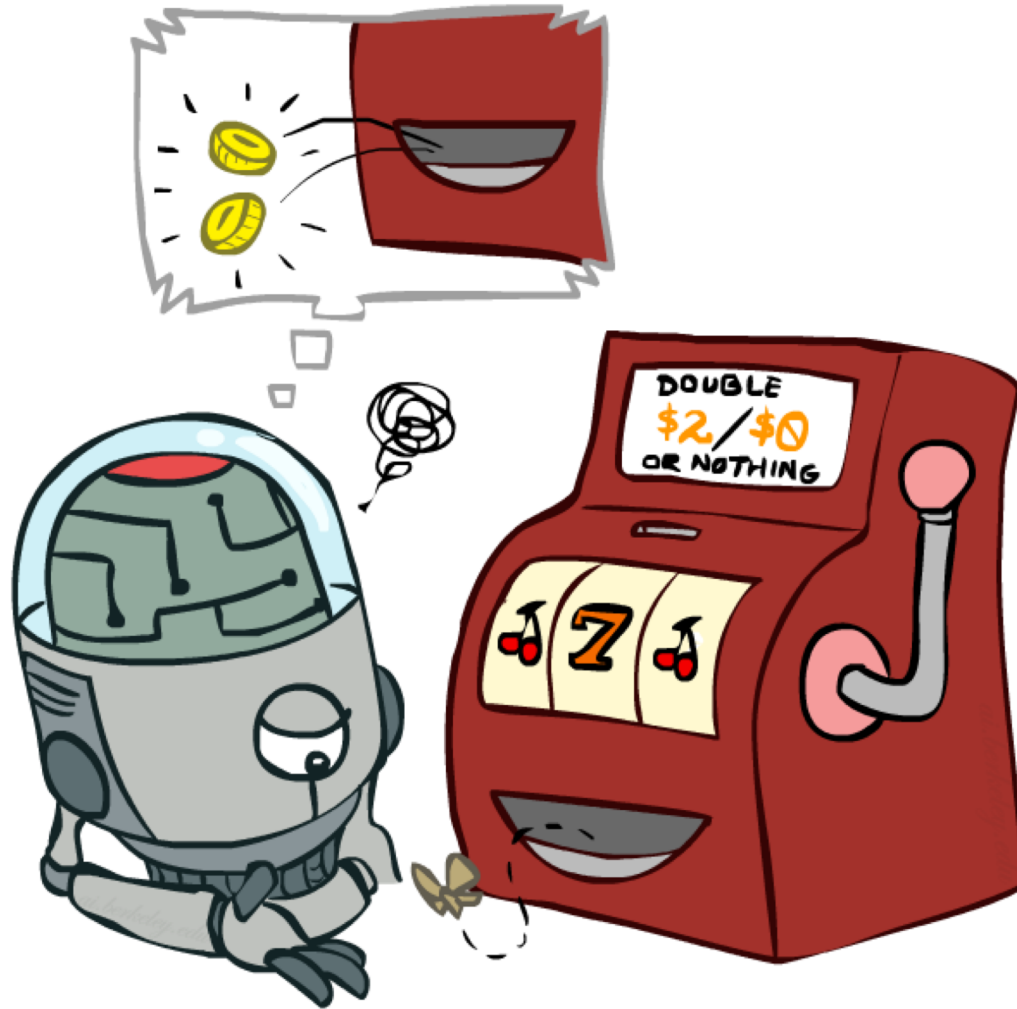
Unknown  $P(A)$ : “Model Free”

$$E[A] \approx \frac{1}{N} \sum_i a_i$$

Why does this work? Because samples appear with the right frequencies.

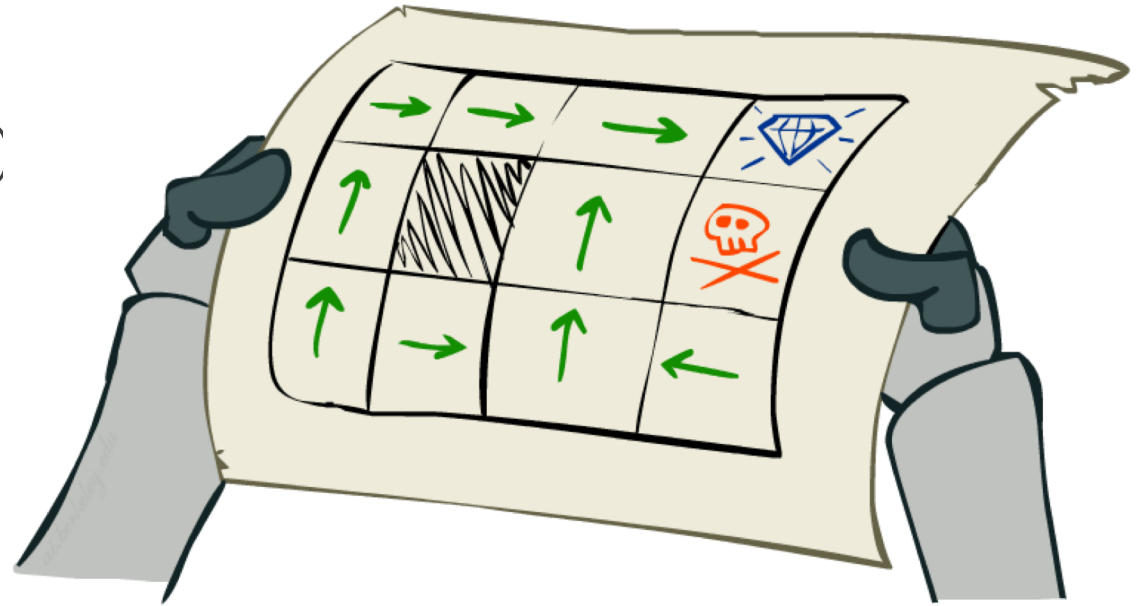
# Model-Free Learning

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# Passive Reinforcement Learning

- Simplified task: policy evaluation
  - Input: a fixed policy  $\pi(s)$
  - You don't know the transitions  $T(s,a,s')$
  - You don't know the rewards  $R(s,a,s')$
  - **Goal: learn the state values**
- In this case:
  - Learner is “along for the ride”
  - No choice about what actions to take
  - Just execute the policy and learn from experience
  - This is NOT offline planning! You actually take actions in the world.



# Direct Evaluation

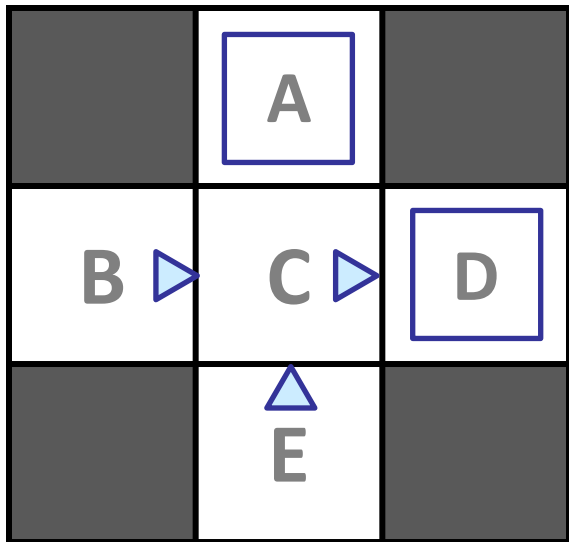
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- Goal: Compute values for each state under  $\pi$
- Idea: Average together observed sample values
  - Act according to  $\pi$
  - Every time you visit a state, write down what the sum of discounted rewards turned out to be
  - Average those samples
- This is called direct evaluation



# Example: Direct Evaluation

Input Policy  $\pi$



Assume:  $\gamma = 1$

Observed Episodes (Training)

Episode 1

B, east, C, -1  
C, east, D, -1  
D, exit, x, +10

Episode 2

B, east, C, -1  
C, east, D, -1  
D, exit, x, +10

Episode 3

E, north, C, -1  
C, east, D, -1  
D, exit, x, +10

Episode 4

E, north, C, -1  
C, east, A, -1  
A, exit, x, -10

Output Values

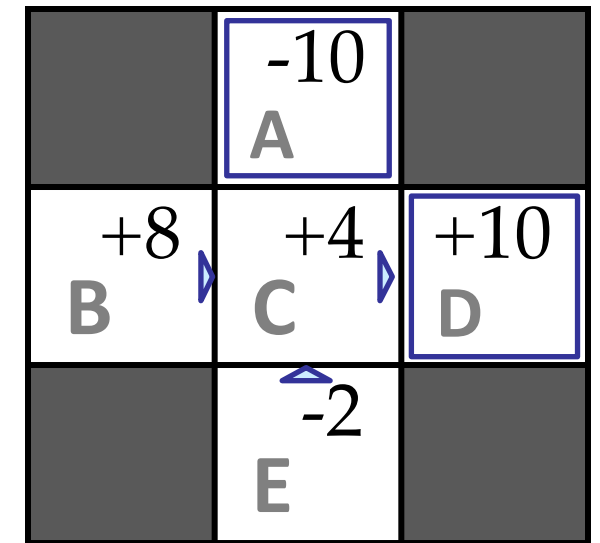
	-10 A	
+8 B	+4 C	+10 D
	-2 E	

*If B and E both go to C under this policy, how can their values be different?*

# Problems with Direct Evaluation

- What's good about direct evaluation?
  - It's easy to understand
  - It doesn't require any knowledge of  $T$ ,  $R$
  - It eventually computes the correct average values, using just sample transitions
- What bad about it?
  - It wastes information about state connections
  - Each state must be learned separately
  - So, it takes a long time to learn

## Output Values



*If B and E both go to C under this policy, how can their values be different?*



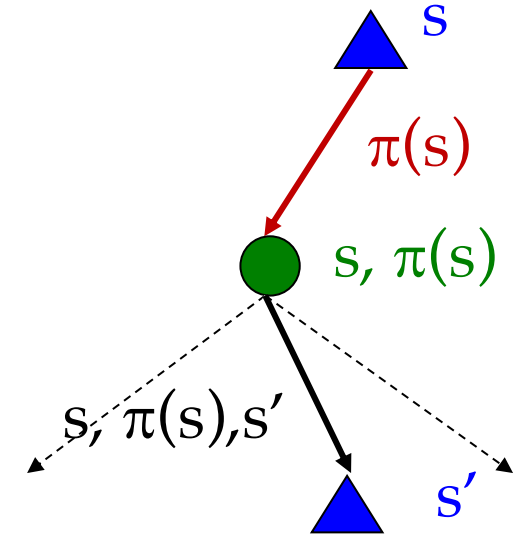
# Why Not Use Policy Evaluation?

- Simplified Bellman updates calculate  $V$  for a fixed policy:
  - Each round, replace  $V$  with a one-step-look-ahead layer over  $V$

$$V_0^\pi(s) = 0$$

$$V_{k+1}^\pi(s) \leftarrow \sum_{s'} T(s, \pi(s), s') [R(s, \pi(s), s') + \gamma V_k^\pi(s')]$$

- This approach fully exploited the connections between the states
  - Unfortunately, we need  $T$  and  $R$  to do it!
- Key question: how can we do this update to  $V$  without knowing  $T$  and  $R$ ?
  - In other words, how to we take a weighted average without knowing the weights?



# Sample-Based Policy Evaluation?

- We want to improve our estimate of  $V$  by computing these averages:

$$V_{k+1}^{\pi}(s) \leftarrow \sum_{s'} T(s, \pi(s), s') [R(s, \pi(s), s') + \gamma V_k^{\pi}(s')]$$

- Idea: Take samples of outcomes  $s'$  (by doing the action!) and average

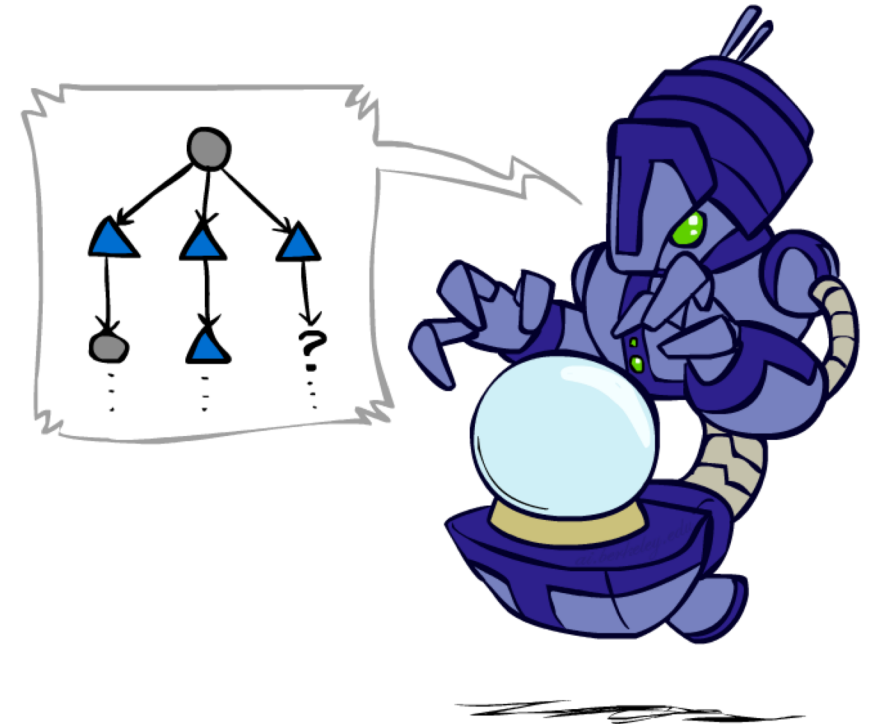
$$\text{sample}_1 = R(s, \pi(s), s'_1) + \gamma V_k^{\pi}(s'_1)$$

$$\text{sample}_2 = R(s, \pi(s), s'_2) + \gamma V_k^{\pi}(s'_2)$$

...

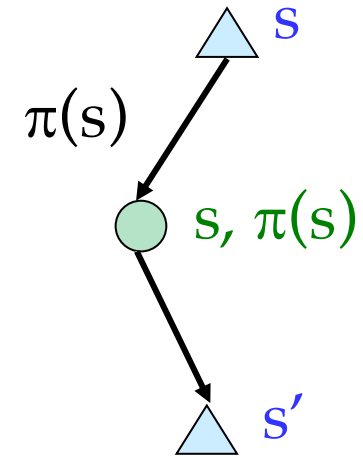
$$\text{sample}_n = R(s, \pi(s), s'_n) + \gamma V_k^{\pi}(s'_n)$$

$$V_{k+1}^{\pi}(s) \leftarrow \frac{1}{n} \sum_i \text{sample}_i$$



# Temporal Difference Learning

- Big idea: learn from every experience!
  - Update  $V(s)$  each time we experience a transition  $(s, a, s', r)$
  - Likely outcomes  $s'$  will contribute updates more often
- Temporal difference learning of values
  - Policy still fixed, still doing evaluation!
  - Move values toward value of whatever successor occurs: running average



Sample of  $V(s)$ :  $sample = R(s, \pi(s), s') + \gamma V^\pi(s')$

Update to  $V(s)$ :  $V^\pi(s) \leftarrow (1 - \alpha)V^\pi(s) + (\alpha)sample$

Same update:  $V^\pi(s) \leftarrow V^\pi(s) + \alpha(sample - V^\pi(s))$

# Exponential Moving Average

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- Exponential moving average
  - The running interpolation update:  $\bar{x}_n = (1 - \alpha) \cdot \bar{x}_{n-1} + \alpha \cdot x_n$
  - Makes recent samples more important
  - Forgets about the past (distant past values were wrong anyway)
- Decreasing learning rate (alpha) can give converging averages

# Example: Temporal Difference Learning

States

	A	
B	C	D
	E	

Assume:  $\gamma = 1$ ,  $\alpha = 1/2$

Observed Transitions

B, east, C, -2

	0	
0	0	8
	0	

C, east, D, -2

	0	
-1	0	8
	0	

	0	
-1	3	8
	0	

$$V^\pi(s) \leftarrow (1 - \alpha)V^\pi(s) + \alpha [R(s, \pi(s), s') + \gamma V^\pi(s')]$$

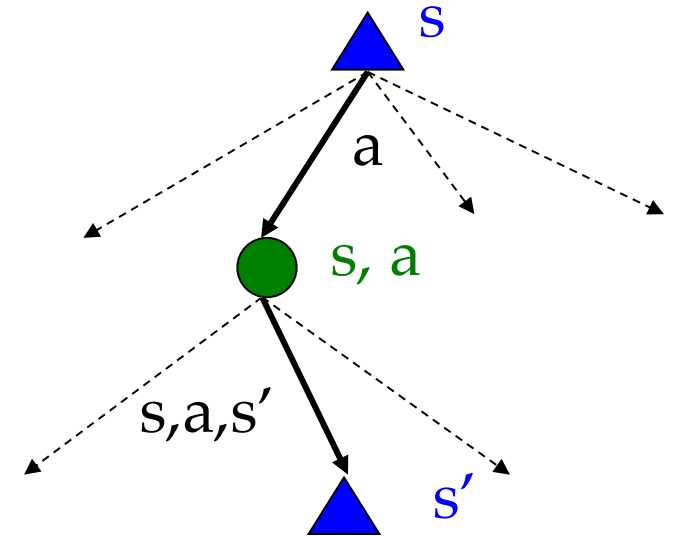
# Problems with TD Value Learning

- TD value learning is a model-free way to do policy evaluation, mimicking Bellman updates with running sample averages
- However, if we want to turn values into a (new) policy, we're sunk:

$$\pi(s) = \arg \max_a Q(s, a)$$

$$Q(s, a) = \sum_{s'} T(s, a, s') [R(s, a, s') + \gamma V(s')]$$

- Idea: learn Q-values, not values
- Makes action selection model-free too!



# Detour: Q-Value Iteration

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- Value iteration: find successive (depth-limited) values
  - Start with  $V_0(s) = 0$ , which we know is right
  - Given  $V_k$ , calculate the depth  $k+1$  values for all states:

$$V_{k+1}(s) \leftarrow \max_a \sum_{s'} T(s, a, s') [R(s, a, s') + \gamma V_k(s')]$$

- But Q-values are more useful, so compute them instead
  - Start with  $Q_0(s,a) = 0$ , which we know is right
  - Given  $Q_k$ , calculate the depth  $k+1$  q-values for all q-states:

$$Q_{k+1}(s, a) \leftarrow \sum_{s'} T(s, a, s') [R(s, a, s') + \gamma \max_{a'} Q_k(s', a')]$$

# Q-Learning

- Q-Learning: sample-based Q-value iteration

$$Q_{k+1}(s, a) \leftarrow \sum_{s'} T(s, a, s') \left[ R(s, a, s') + \gamma \max_{a'} Q_k(s', a') \right]$$

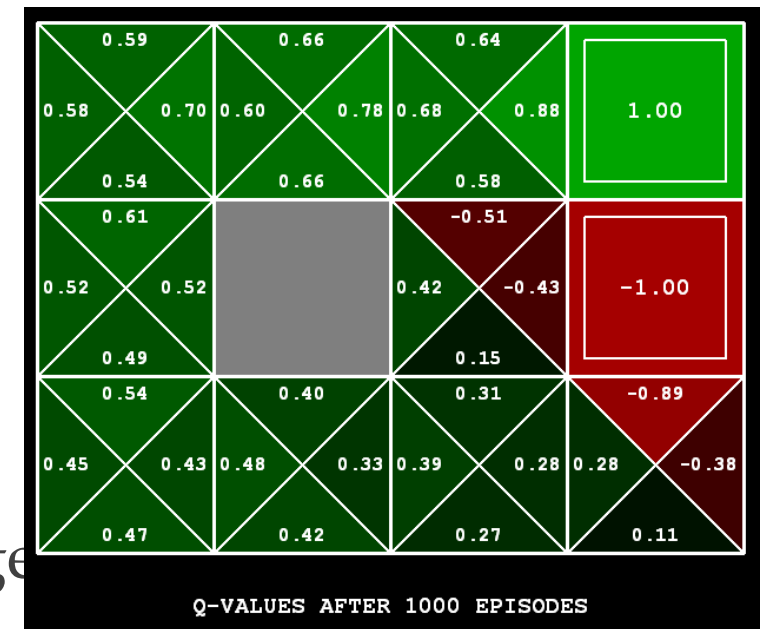
- Learn  $Q(s,a)$  values as you go

- Receive a sample  $(s,a,s',r)$
- Consider your old estimate  $Q(s, a)$
- Consider your new sample estimate:

$$sample = R(s, a, s') + \gamma \max_{a'} Q(s', a') \quad \text{no longer policy evaluation!}$$

- Incorporate the new estimate into a running average

$$Q(s, a) \leftarrow (1 - \alpha)Q(s, a) + (\alpha) [sample]$$

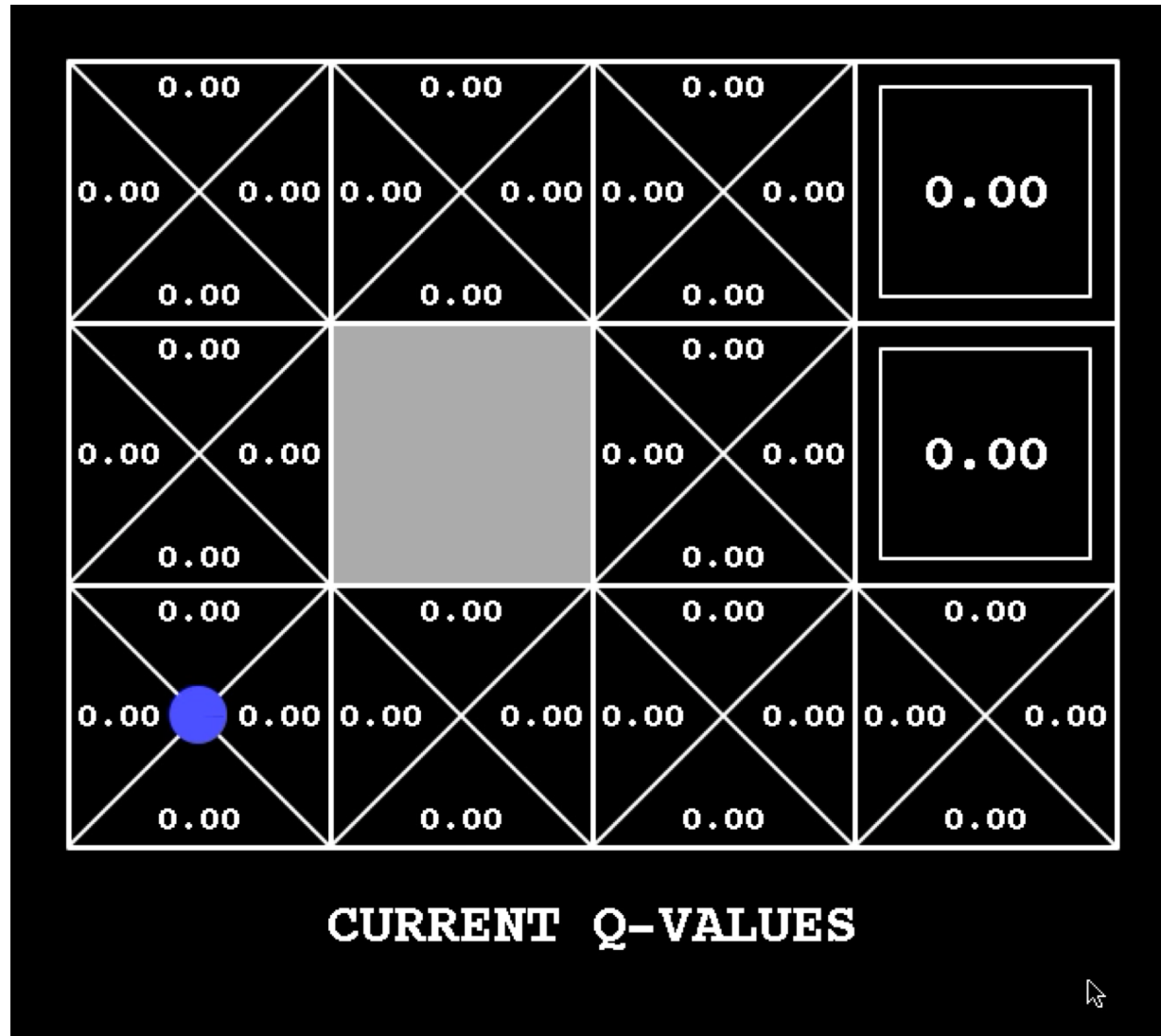


[Demo: Q-learning – gridworld (L10D2)]

[Demo: Q-learning – crawler (L10D3)]



# Q-Learning Demo



# Video of Demo Q-Learning -- Gridworld

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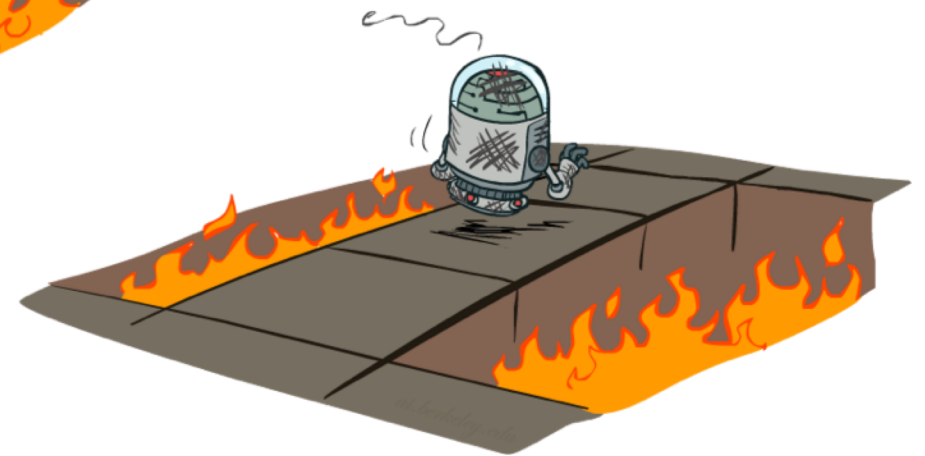
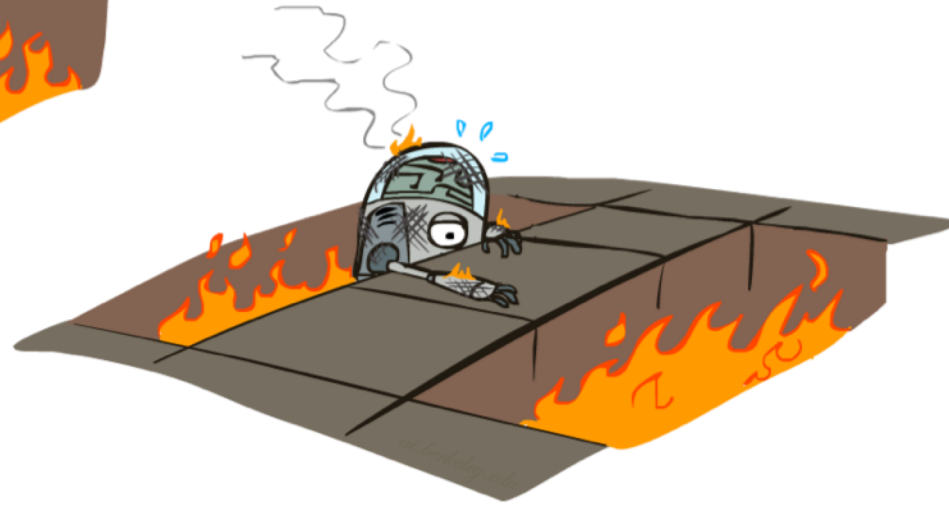
# Video of Demo Q-Learning -- Crawler

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# Active Reinforcement Learning

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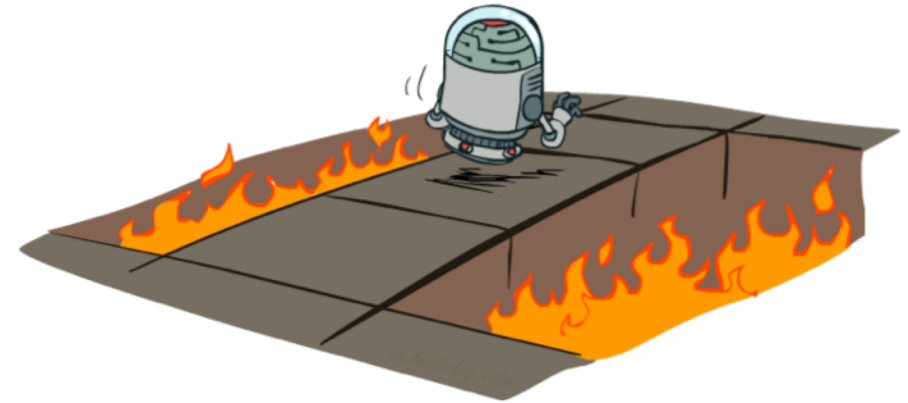


# Q-Learning:

act according to current optimal (and also explore...)

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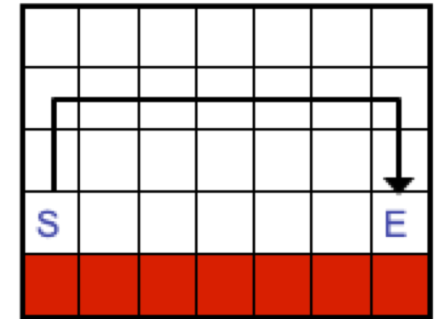
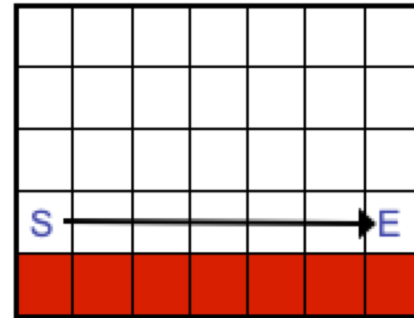
- Full reinforcement learning: optimal policies (like value iteration)
  - You don't know the transitions  $T(s,a,s')$
  - You don't know the rewards  $R(s,a,s')$
  - You choose the actions now
  - **Goal: learn the optimal policy / values**
- In this case:
  - Learner makes choices!
  - Fundamental tradeoff: exploration vs. exploitation
  - This is NOT offline planning! You actually take actions in the world and find out what happens...



# Q-Learning Properties

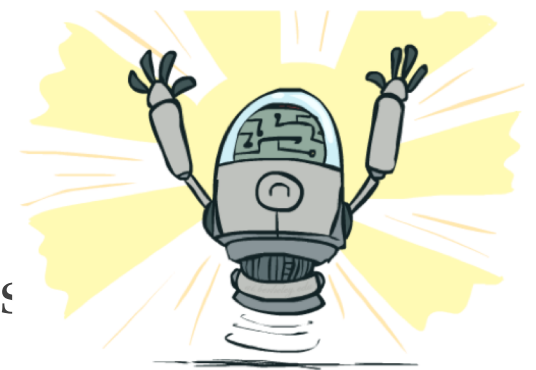
- Amazing result: Q-learning converges to optimal policy -- even if you're acting suboptimally!

- This is called **off-policy learning**



- Caveats:

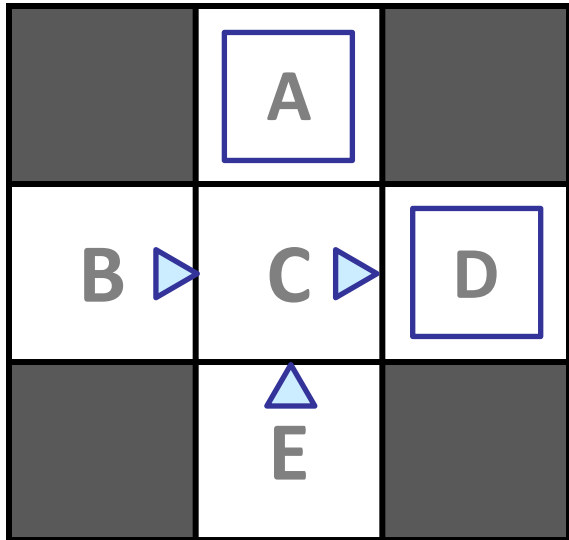
- You have to explore enough
- You have to eventually make the learning rate small enough
- ... but not decrease it too quickly
- Basically, in the limit, it doesn't matter how you select actions



# Model-Based Learning

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Input Policy  $\pi$



act according to current optimal  
also explore!

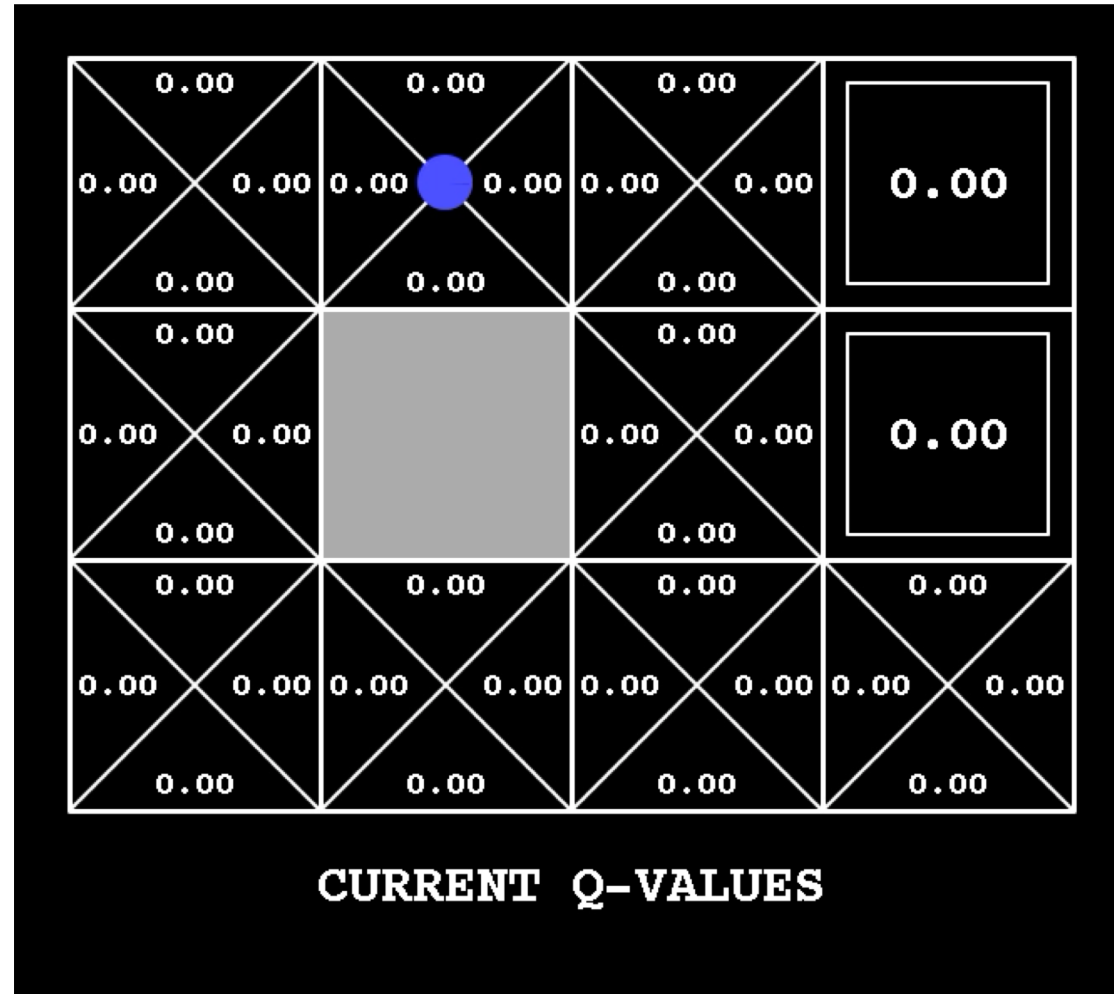
# How to Explore?

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- Several schemes for forcing exploration
  - Simplest: random actions ( $\epsilon$ -greedy)
    - Every time step, flip a coin
    - With (small) probability  $\epsilon$ , act randomly
    - With (large) probability  $1-\epsilon$ , act on current policy
  - Problems with random actions?
    - You do eventually explore the space, but keep thrashing around once learning is done
    - One solution: lower  $\epsilon$  over time
    - Another solution: exploration functions



# Q-Learn Epsilon Greedy



# Discussion: Model-Based vs Model-Free RL

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