CSE-571 Robotics

Planning and Control:

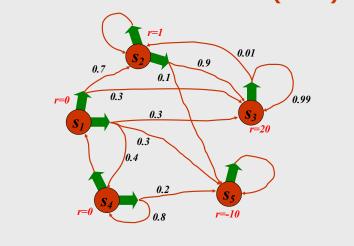
Markov Decision Processes

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Markov Decision Process (MDP)

- Given:
- States *x*
- Actions *u*
- Transition probabilities p(x'|u,x)
- Reward / payoff function r(x,u)
- Wanted:
- Policy $\pi(x)$ that maximizes the future expected reward

Markov Decision Process (MDP)



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Rewards and Policies

• Policy (general case):

$$\pi: z_{1:t-1}, u_{1:t-1} \to u_t$$

• Policy (fully observable case):

$$\pi: x_t \to u_t$$

• Expected cumulative payoff:

$$R_T = E \left[\sum_{\tau=1}^T \gamma^{\tau} r_{t+\tau} \right]$$

- T=1: greedy policy
- T>1: finite horizon case, typically no discount
- T=infty: infinite-horizon case, finite reward if discount < 1

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Policies contd.

• Expected cumulative payoff of policy:

$$R_T^{\pi}(x_t) = E \left[\sum_{\tau=1}^T \gamma^{\tau} r_{t+\tau} \mid u_{t+\tau} = \pi \left(z_{1:t+\tau-1} u_{1:t+\tau-1} \right) \right]$$

• Optimal policy:

$$\pi^* = \operatorname{argmax} R_T^{\pi}(x_t)$$

• 1-step optimal policy:

$$\pi_1(x) = \operatorname{argmax} r(x, u)$$

Value function of 1-step optimal policy:

$$V_1(x) = \gamma \max_{u} r(x, u)$$

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T-step Policies

• Optimal policy:

$$\pi_T(x) = \underset{u}{\operatorname{argmax}} \left[r(x,u) + \int V_{T-1}(x') p(x'|u,x) dx' \right]$$

• Value function:

$$V_T(x) = \gamma \max_{u} \left[r(x,u) + \int V_{T-1}(x') p(x'|u,x) dx' \right]$$

2-step Policies

• Optimal policy:

$$\pi_2(x) = \underset{u}{\operatorname{argmax}} \left[r(x,u) + \int V_1(x') p(x'|u,x) dx' \right]$$

• Value function:

$$V_2(x) = \gamma \max_{u} \left[r(x,u) + \int V_1(x') p(x'|u,x) dx' \right]$$

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Infinite Horizon

• Optimal policy:

$$V_{\infty}(x) = \gamma \max_{u} \quad \left[r(x,u) + \int V_{\infty}(x') p(x'|u,x) dx' \right]$$

- Bellman equation
- Fix point is optimal policy
- Necessary and sufficient condition

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Value Iteration

• for all x do

$$\hat{V}(x) \leftarrow r_{\min}$$

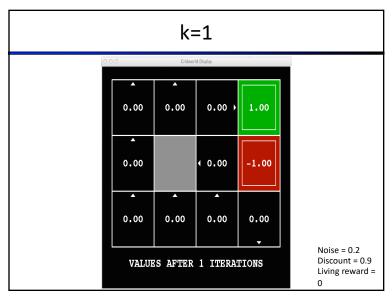
- endfor
- repeat until convergence
 - for all x do

$$\hat{V}(x) \leftarrow \gamma \max_{u} \left[r(x,u) + \int \hat{V}(x') p(x'|u,x) dx' \right]$$

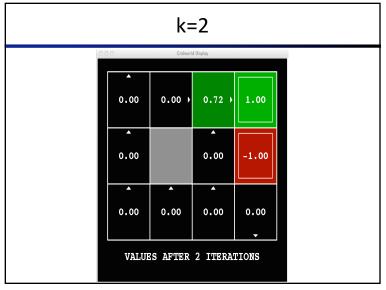
- endfor
- endrepeat

$$\pi(x) = \underset{u}{\operatorname{argmax}} \left[r(x,u) + \int \hat{V}(x') p(x'|u,x) dx' \right]$$

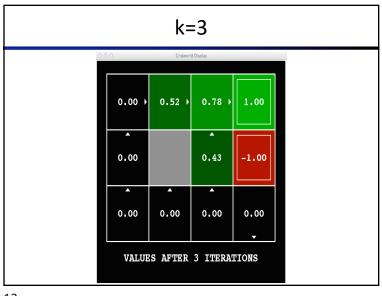
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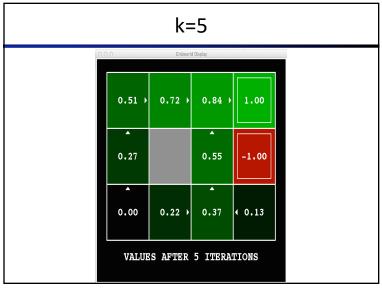
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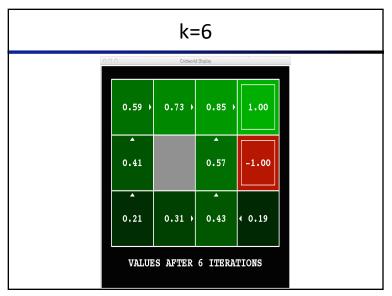


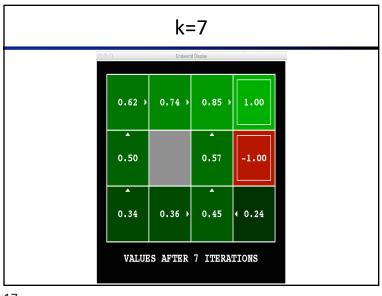
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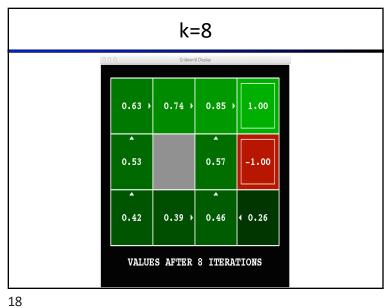


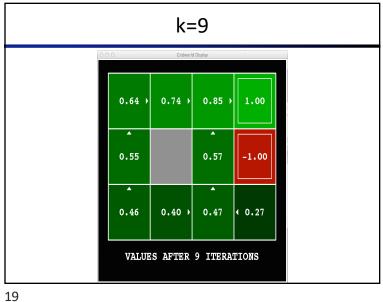
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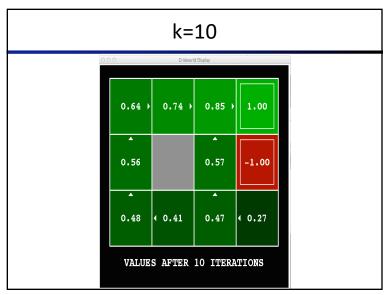


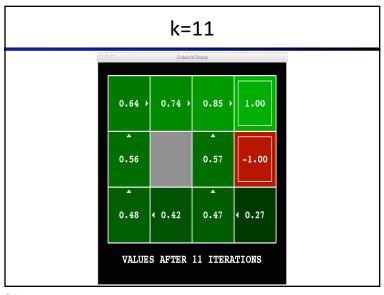










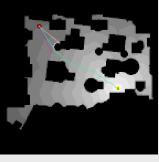


Value Function and Policy
Each step takes O(|A| |S| |S|) time.
Number of iterations required is polynomial in |S|, |A|, 1/(1-gamma)

Value Iteration for Motion Planning

(assumes knowledge of robot's location)





POMDPs

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- In POMDPs we apply the very same idea as in MDPs.
- Since the state is not observable, the agent has to make its decisions based on the belief state which is a posterior distribution over states.
- For finite horizon problems, the resulting value functions are piecewise linear and convex.
- In each iteration the number of linear constraints grows exponentially.
- Full fledged POMDPs have only been applied to very small state spaces with small numbers of possible observations and actions.
- Approximate solutions are becoming more and more capable.

Frontier-based Exploration

• Every unknown location is a target point.



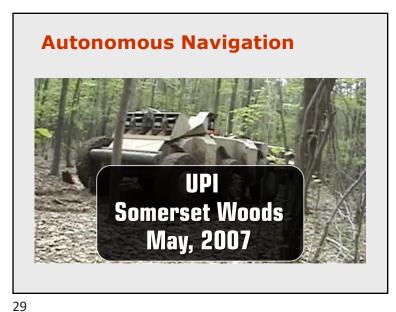


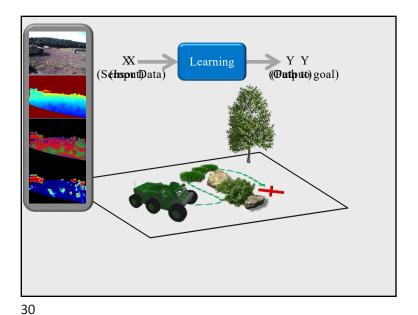
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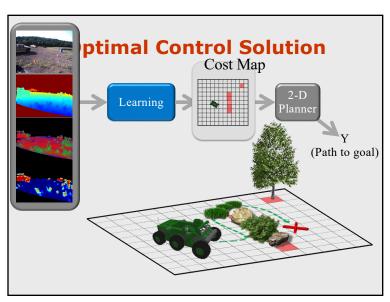
CSE 571
Inverse Optimal Control
(Inverse Reinforcement Learning)

Many slides by Drew Bagnell Carnegie Mellon University

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Mode 1: Training example

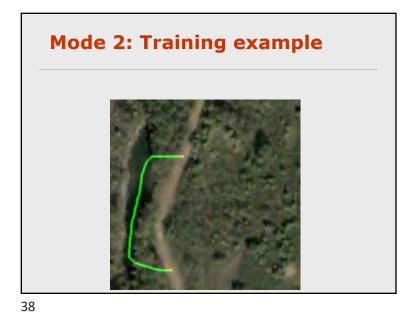






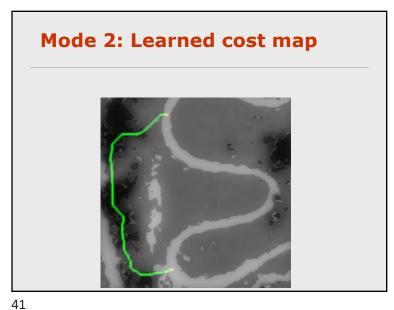
Mode 1: Learned cost map

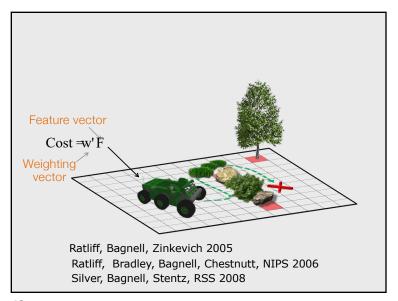


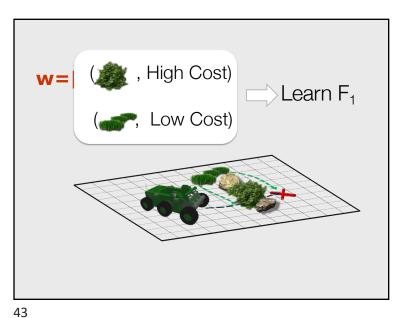


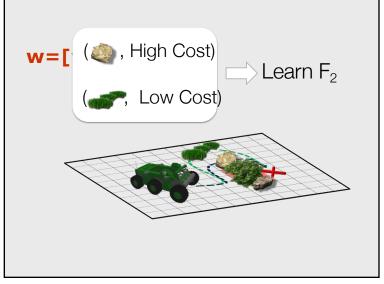














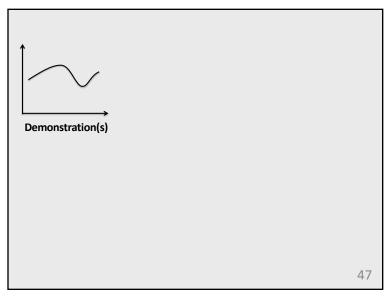
Learning Manipulation Preferences

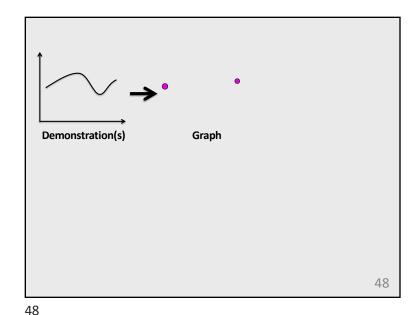
- Input: Human demonstrations of preferred behavior (e.g., moving a cup of water upright without spilling)
- Output: Learned cost function that results in trajectories satisfying user preferences

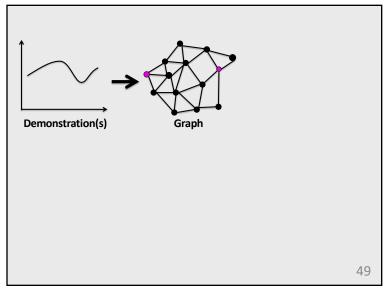


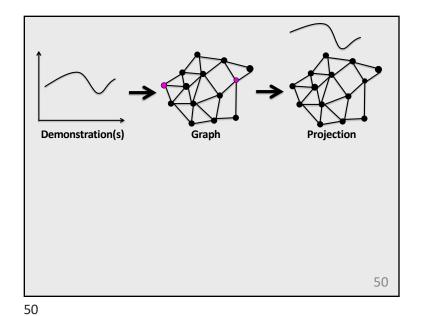
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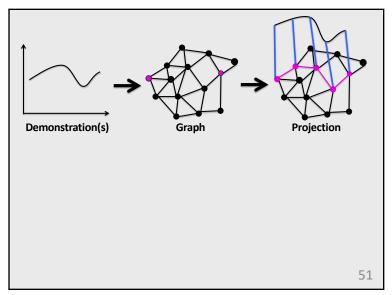
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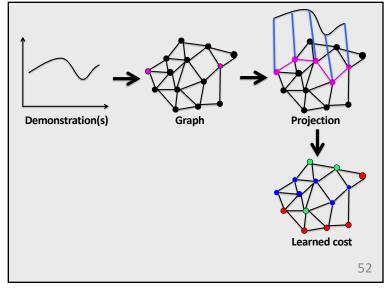


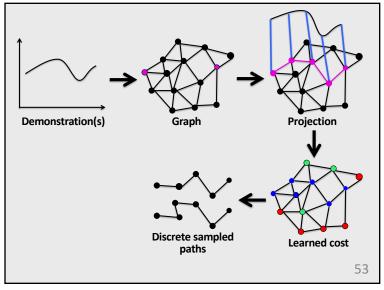


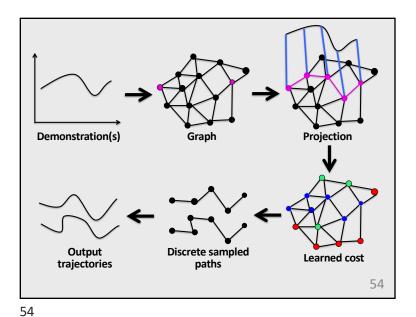


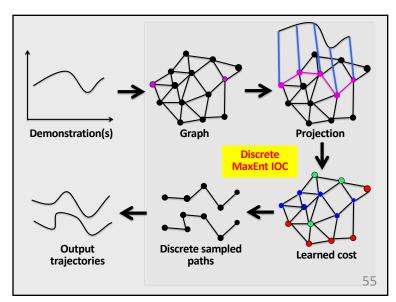


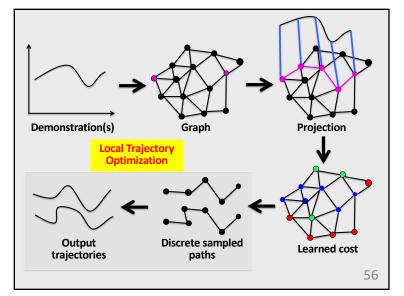












Setup

- **Binary** state-dependent features (~95)
 - Histograms of distances to objects
 - Histograms of end-effector orientation
 - Object specific features (electronic vs nonelectronic)
 - Approach direction w.r.t goal
- Task
 - Hold cup upright while not moving above electronics

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Laptop task: LTO + Smooth random path



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Laptop task: Demonstration (Not part of training set)



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Readings

- Max-Ent IRL (Ziebart, Bagnell): http://www.cs.cmu.edu/~bziebart/
- CIOC (Levine) <u>http://graphics.stanford.edu/projects/cioc/cioc.pdf</u>
- Manipulation (Byravan/Fox): https://rse-lab.cs.washington.edu/papers/graph-based-IOC-ijcai-2015.pdf
- Imitation learning (Ermon): https://cs.stanford.edu/~ermon/
- Human/manipulation (Dragan): https://people.eecs.berkeley.edu/~anca/research.html

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