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**Robotics**  
**Spring 2023**  
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TAs: Yi Li, Srivatsa GS

# Recap: Course Overview

Filtering/Smoothing

Localization

Mapping

SLAM

Search

Motion Planning

TrajOpt

Stability/Certification

MDPs and RL

Imitation Learning

Off-Policy/MBRL

# Lecture Outline

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Recap + Policy Gradient

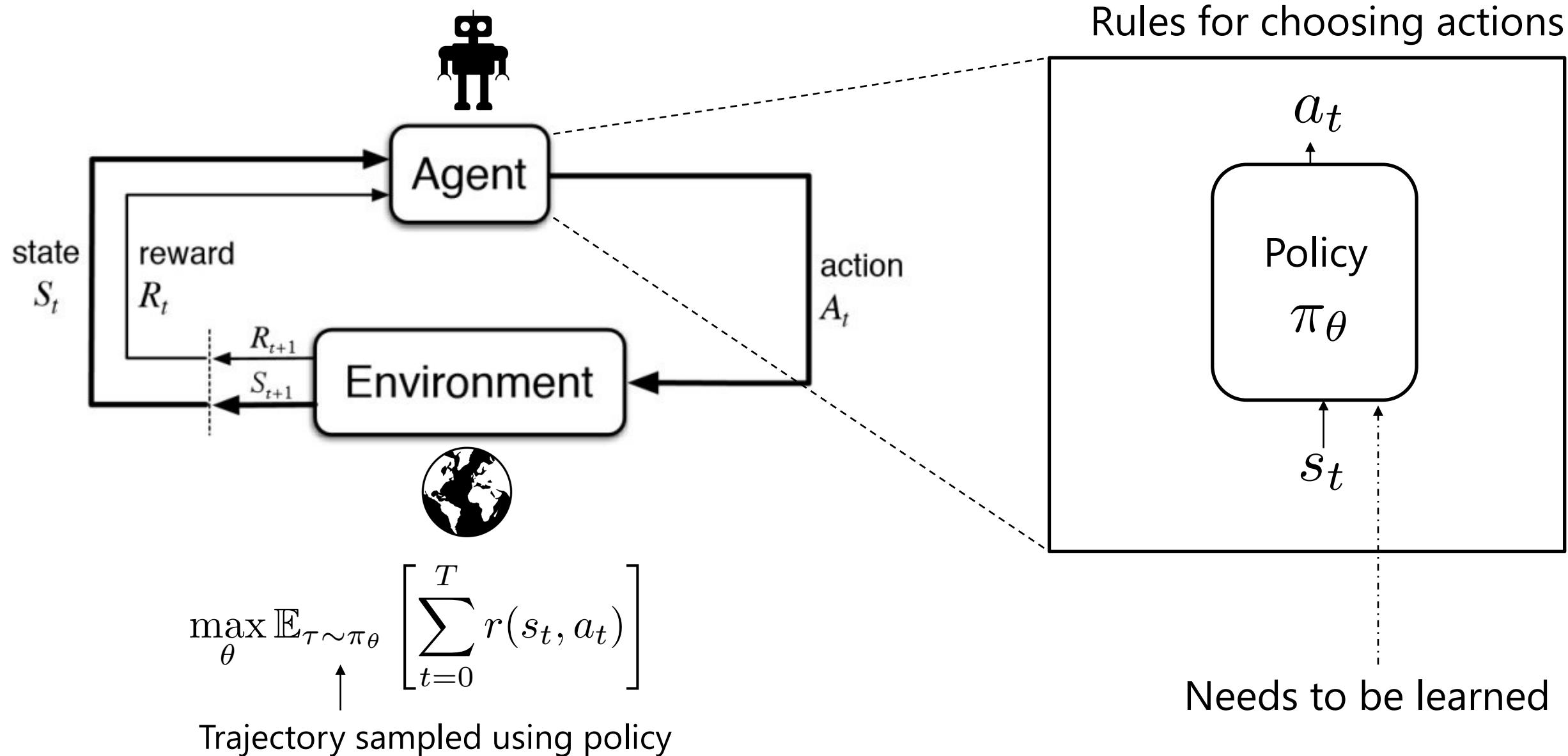


Basic Actor Critic Algorithms



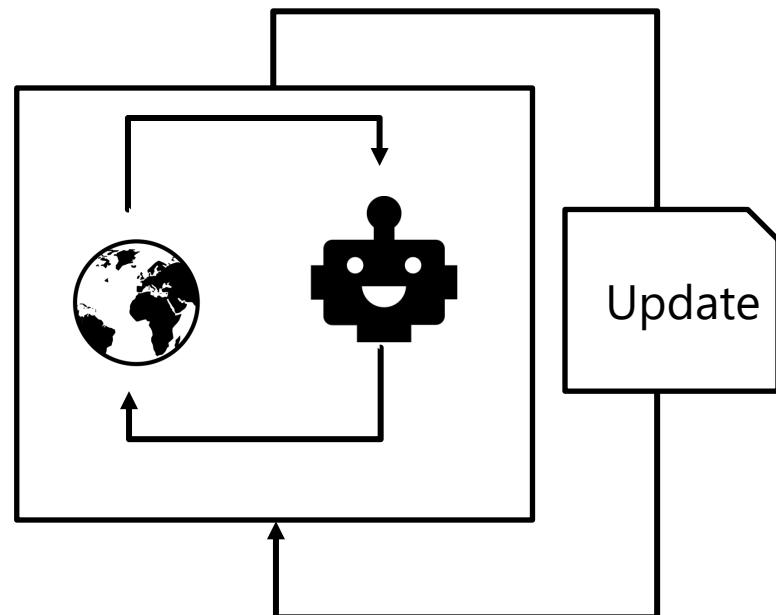
Making Actor-Critic Practical

# Reinforcement Learning Formalism



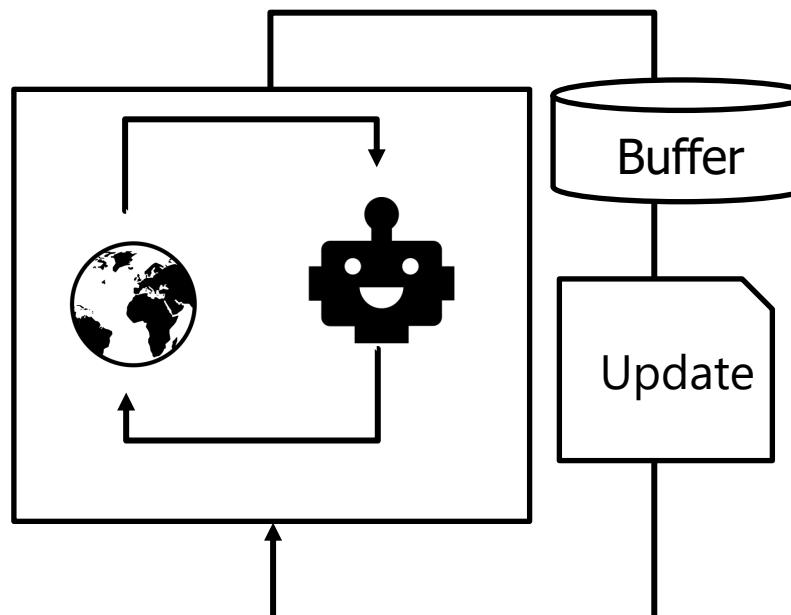
# Learning Algorithms for Robotics

## On-Policy Algorithms



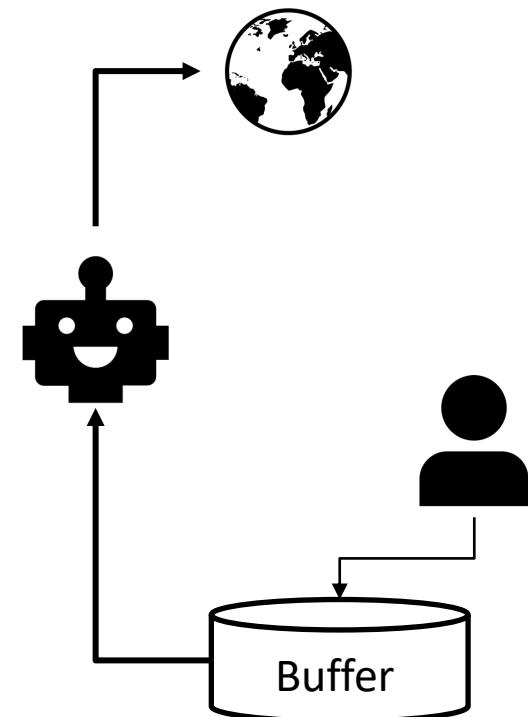
Simple, performant,  
Data inefficient

## Off-Policy Algorithms



Data-efficient,  
sometimes unstable

## Imitation Learning

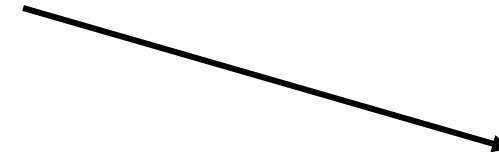


Performant, efficient, but  
compounding error and  
expensive data collection

# What if we just performed gradient ascent?

$$\max_{\theta} \mathbb{E}_{\tau \sim \pi_{\theta}} \left[ \sum_{t=0}^T r(s_t, a_t) \right]$$

$$= \int p_{\theta}(\tau) R(\tau) d\tau$$



Standard gradient descent (supervised learning)

$$\nabla_{\theta} \mathbb{E}_{x \sim g(x)} [f_{\theta}(x)]$$

REINFORCE gradient descent (RL)

$$\nabla_{\theta} \mathbb{E}_{x \sim p_{\theta}(x)} [f(x)]$$

Gradient wrt expectation variable, not of integrand!

# Taking the gradient of sum of rewards

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$$J(\theta) = \int p_\theta(\tau) R(\tau) d(\tau)$$

$$\begin{aligned} \nabla_\theta J(\theta) &= \nabla_\theta \int p_\theta(\tau) R(\tau) d(\tau) \\ &= \int \nabla_\theta p_\theta(\tau) R(\tau) d(\tau) \quad = \int \frac{p_\theta(\tau)}{p_\theta(\tau)} \nabla_\theta p_\theta(\tau) R(\tau) d(\tau) \\ &= \int p_\theta(\tau) \nabla_\theta \log p_\theta(\tau) R(\tau) d(\tau) \quad = \mathbb{E}_{p_\theta(\tau)} [\nabla_\theta \log p_\theta(\tau) R(\tau)] \end{aligned}$$

REINFORCE trick

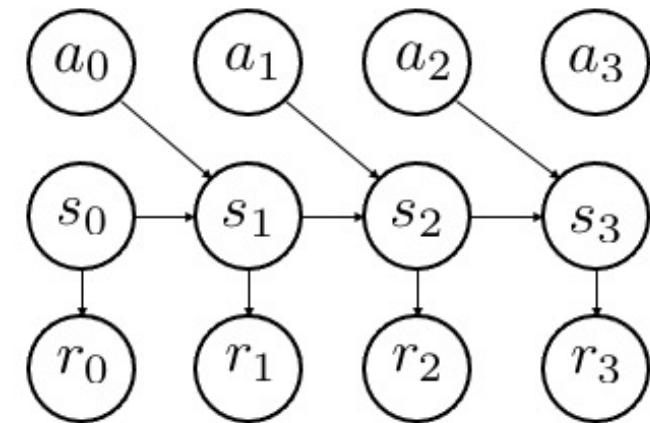
# Taking the gradient of return

Initial State

$$p_\theta(\tau) = p(s_0) \prod_{t=0}^{T-1} p(s_{t+1}|s_t, a_t) \pi(a_t|s_t)$$

Dynamics

Policy



$$\log p_\theta(\tau) = \log p(s_0) + \sum_{t=0}^{T-1} \log p(s_{t+1}|s_t, a_t) + \log \pi(a_t|s_t)$$

$$\nabla_\theta \log p_\theta(\tau) = \cancel{\nabla_\theta \log p(s_0)} + \sum_{t=0}^{T-1} \cancel{\nabla_\theta \log p(s_{t+1}|s_t, a_t)} + \nabla_\theta \log \pi(a_t|s_t)$$

$$\nabla_\theta \log p_\theta(\tau) = \sum_{t=0}^{T-1} \nabla_\theta \log \pi(a_t|s_t)$$

Model Free!!

# Taking the gradient of return

$$\nabla_{\theta} J(\theta) = \mathbb{E}_{\tau \sim p_{\theta}(\tau)} \left[ \nabla_{\theta} \log p_{\theta}(\tau) \sum_{t=0}^T r(s_t, a_t) \right]$$

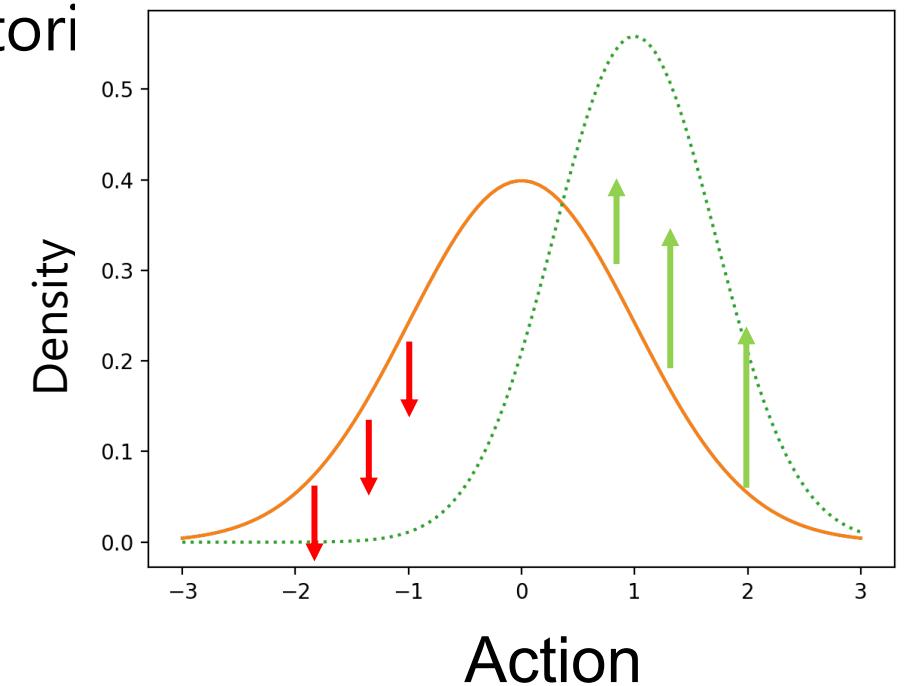
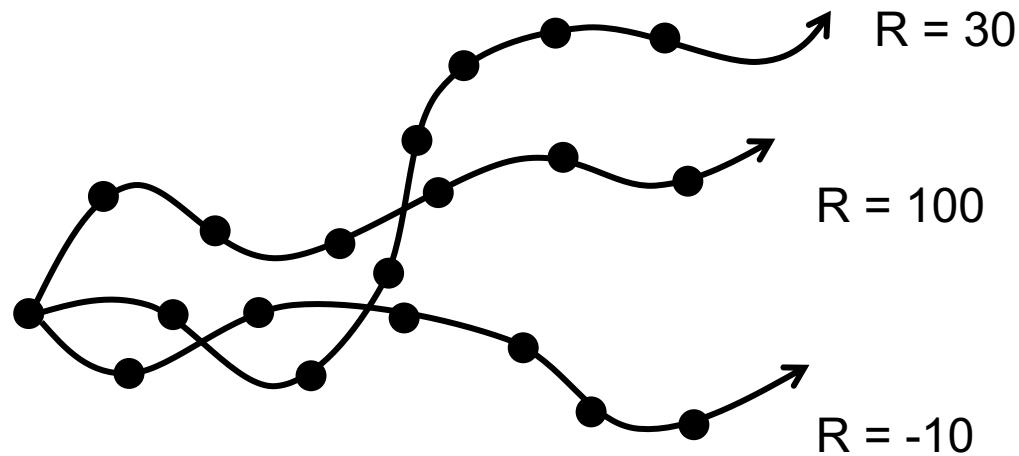
$$\nabla_{\theta} J(\theta) = \mathbb{E}_{\substack{s_0 \sim p(s_0) \\ s_{t+1} \sim p(s_{t+1}|s_t, a_t) \\ a_t \sim \pi(a_t|s_t)}} \left[ \sum_{t=0}^T \nabla_{\theta} \log \pi_{\theta}(a_t|s_t) \sum_{t'=0}^T r(s_t, a_t) \right]$$

$$\approx \frac{1}{N} \sum_{i=0}^N \sum_{t=0}^T \nabla_{\theta} \log \pi_{\theta}(a_t^i | s_t^i) \sum_{t'=0}^T r(s_{t'}^i, a_{t'}^i) \text{ (approximating using samples)}$$

# What does this mean?

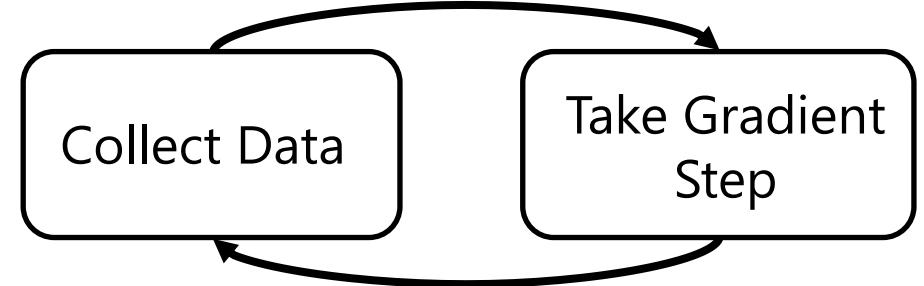
$$\nabla_{\theta} J(\theta) = \int p_{\theta}(\tau) \nabla_{\theta} \log p_{\theta}(\tau) d\tau \approx \frac{1}{N} \sum_{i=0}^N \sum_{t=0}^T \nabla_{\theta} \log \pi_{\theta}(a_t^i | s_t^i) \sum_{t'=0}^T r(s_{t'}^i, a_{t'}^i)$$

Increase the likelihood of actions in high return trajectories



# Resulting Algorithm (REINFORCE)

$$\nabla_{\theta} J(\theta) = \int p_{\theta}(\tau) \nabla_{\theta} \log p_{\theta}(\tau) d\tau$$



REINFORCE algorithm:

- On-policy →
1. sample  $\{\tau^i\}$  from  $\pi_{\theta}(\mathbf{a}_t | \mathbf{s}_t)$  (run it on the robot)
  2.  $\nabla_{\theta} J(\theta) \approx \sum_i (\sum_t \nabla_{\theta} \log \pi_{\theta}(\mathbf{a}_t^i | \mathbf{s}_t^i)) (\sum_t r(\mathbf{s}_t^i, \mathbf{a}_t^i))$
  3.  $\theta \leftarrow \theta + \alpha \nabla_{\theta} J(\theta)$

# REINFORCE Pseudocode

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**Algorithm 1** Vanilla Policy Gradient Algorithm
 

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- 1: Input: initial policy parameters  $\theta_0$ , initial value function parameters  $\phi_0$
- 2: **for**  $k = 0, 1, 2, \dots$  **do**
- 3:   Collect set of trajectories  $\mathcal{D}_k = \{\tau_i\}$  by running policy  $\pi_k = \pi(\theta_k)$  in the environment.
- 4:   Compute rewards-to-go  $\hat{R}_t$ .
- 5:   Compute advantage estimates,  $\hat{A}_t$  (using any method of advantage estimation) based on the current value function  $V_{\phi_k}$ .
- 6:   Estimate policy gradient as

$$\hat{g}_k = \frac{1}{|\mathcal{D}_k|} \sum_{\tau \in \mathcal{D}_k} \sum_{t=0}^T \nabla_{\theta} \log \pi_{\theta}(a_t | s_t) \Big|_{\theta_k} \hat{A}_t.$$

- 7:   Compute policy update, either using standard gradient ascent,

$$\theta_{k+1} = \theta_k + \alpha_k \hat{g}_k,$$

or via another gradient ascent algorithm like Adam.

- 8:   Fit value function by regression on mean-squared error:

$$\phi_{k+1} = \arg \min_{\phi} \frac{1}{|\mathcal{D}_k| T} \sum_{\tau \in \mathcal{D}_k} \sum_{t=0}^T \left( V_{\phi}(s_t) - \hat{R}_t \right)^2,$$

→ Sum up reward to go

→ Simply subtract baseline

typically via some gradient descent algorithm.

- 9: **end for**
- 

→ Regression to learn baseline

# How is this related to supervised learning?

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## Reinforcement Learning

$$\nabla_{\theta} J(\theta) = \int p_{\theta}(\tau) \nabla_{\theta} \log p_{\theta}(\tau) d\tau$$

$$\approx \frac{1}{N} \sum_{i=0}^N \sum_{t=0}^T \nabla_{\theta} \log \pi_{\theta}(a_t^i | s_t^i) \sum_{t'=0}^T r(s_{t'}^i, a_{t'}^i)$$

## Supervised Learning

$$\max_{\theta} \mathbb{E}_{(x,y) \sim \mathcal{D}} [\log p_{\theta}(y|x)]$$

$$\approx \frac{1}{N} \sum_i \nabla_{\theta} \log p_{\theta}(y^i | x^i)$$

PG = select good data + increase likelihood of selected data

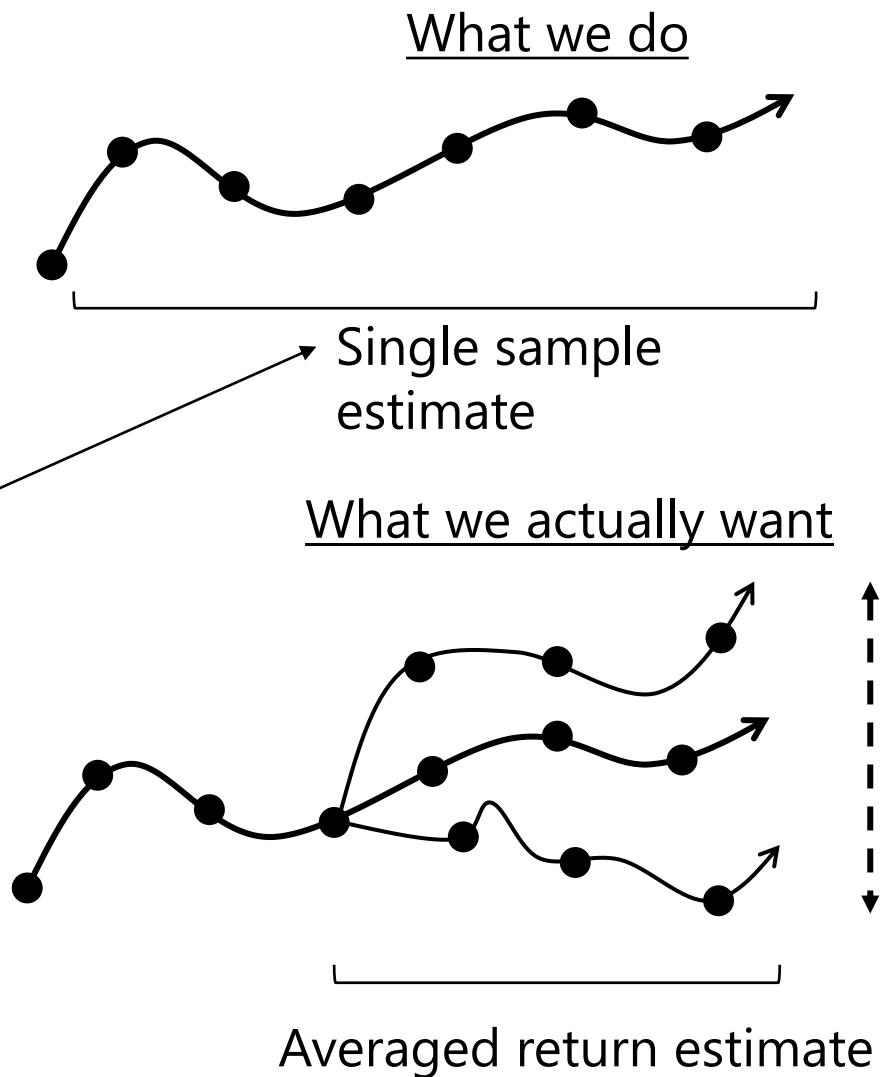
# What makes policy gradient challenging?

$$\nabla_{\theta} J(\theta) = \int p_{\theta}(\tau) \nabla_{\theta} \log p_{\theta}(\tau) d\tau$$

$$\approx \frac{1}{N} \sum_{i=0}^N \sum_{t=0}^T \nabla_{\theta} \log \pi_{\theta}(a_t^i | s_t^i) \sum_{t'=0}^T r(s_{t'}^i, a_{t'}^i)$$

**High variance estimator!!**

Hard to tell what matters without many samples

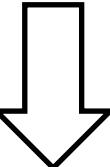


# Variance Reduction with Causality

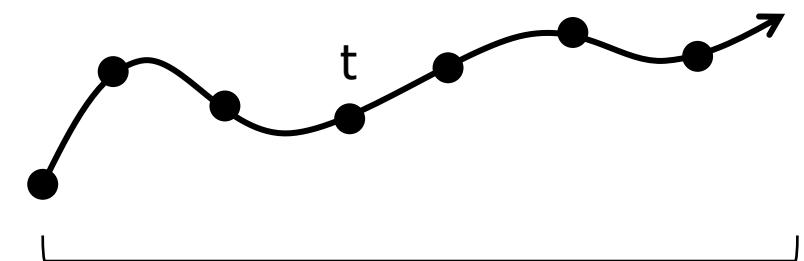
Idea: Trajectory returns depend on past and future, but we only care about the future, since actions cannot affect the past. Instead, consider **“return-to-go”**

$$\approx \frac{1}{N} \sum_{i=0}^N \sum_{t=0}^T \nabla_{\theta} \log \pi_{\theta}(a_t^i | s_t^i) \underbrace{\sum_{t'=0}^T r(s_{t'}^i, a_{t'}^i)}$$

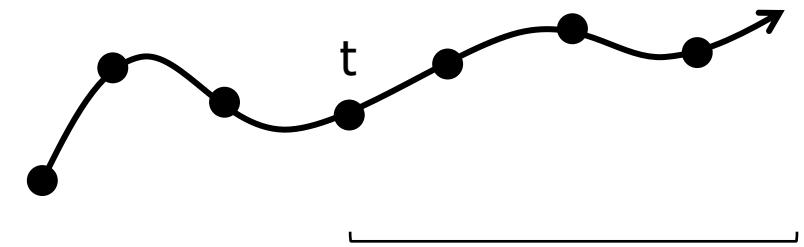
Includes  $t' < t$

Ignore past terms 

$$\frac{1}{N} \sum_{i=0}^N \sum_{t=0}^T \nabla_{\theta} \log \pi_{\theta}(a_t^i | s_t^i) \sum_{t'=t}^T r(s_{t'}^i, a_{t'}^i)$$

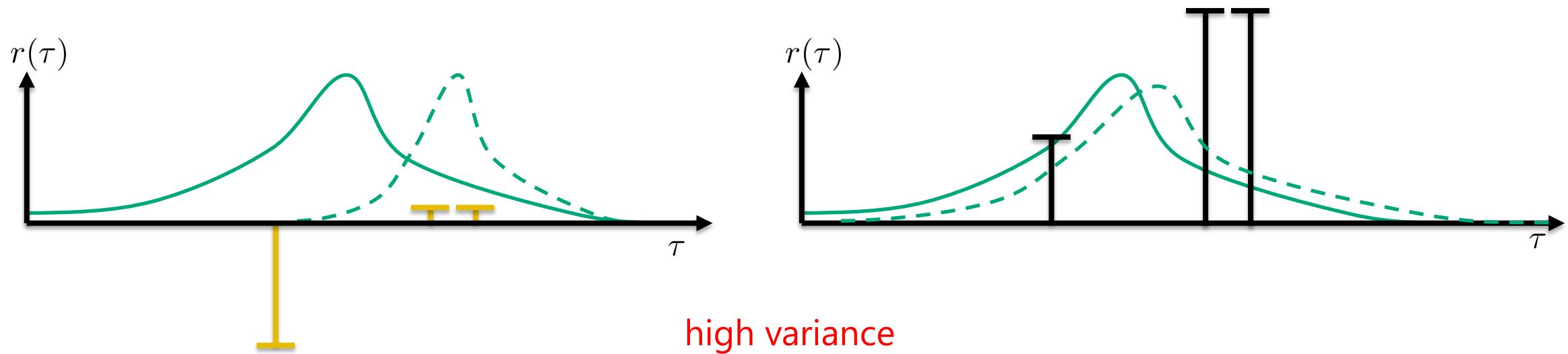


Full trajectory return



Return to go

# Can we reduce variance further?



Arbitrarily uncentered, scaled returns can lead to huge variance:

- Imagine all rewards were positive, every action would be pushed up, some more than others
- What if instead, we pushed down some actions and pushed up some others (even if rewards are positive)

# Variance Reduction with a Baseline

Idea: We can reduce variance by subtracting a current state dependent function from the policy gradient return

$$\frac{1}{N} \sum_{i=1}^N \sum_{t=0}^T \nabla_{\theta} \log \pi_{\theta}(a_t^i | s_t^i) \left[ \sum_{t'=t}^T r(s_{t'}^i, a_{t'}^i) - b(s_t) \right]$$

Baseline: Centers the returns, reduces variance

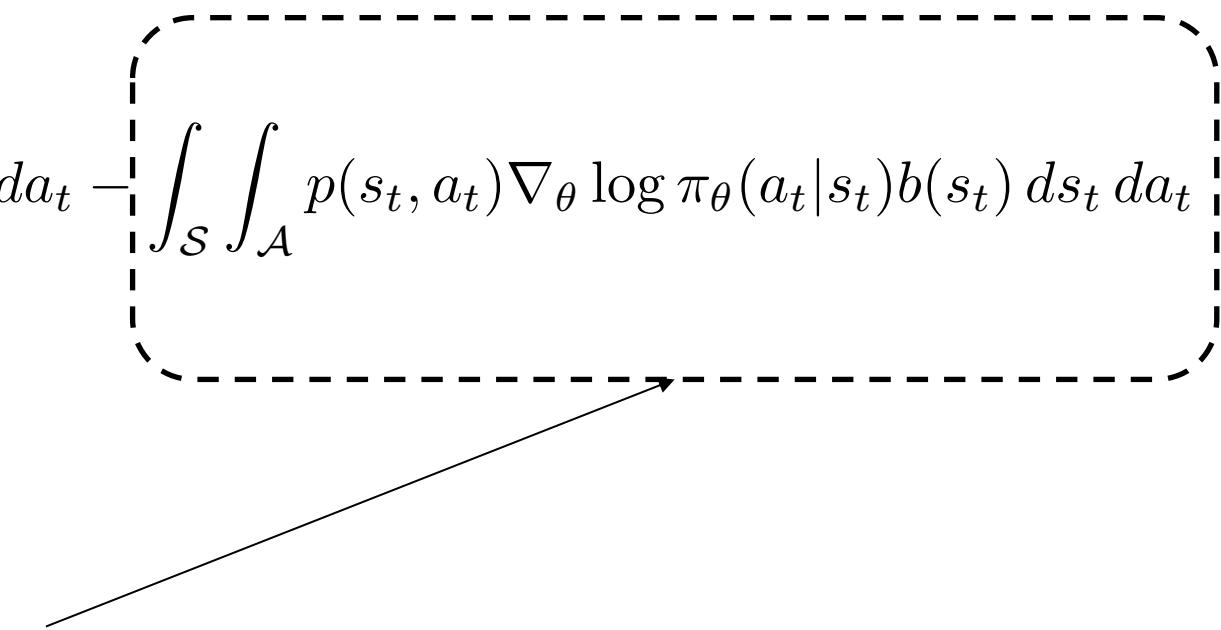
But does this increase bias??

# Variance Reduction with a Baseline

$$\int_{\mathcal{S}} \int_{\mathcal{A}} p(s_t, a_t) \nabla_{\theta} \log \pi_{\theta}(a_t | s_t) \left[ \sum_{t'=t}^T r(s_{t'}, a_{t'}) - b(s_t) \right] ds_t da_t$$

$$\int_{\mathcal{S}} \int_{\mathcal{A}} p(s_t, a_t) \nabla_{\theta} \log \pi_{\theta}(a_t | s_t) \left[ \sum_{t'=t}^T r(s_{t'}, a_{t'}) \right] ds_t da_t - \boxed{\int_{\mathcal{S}} \int_{\mathcal{A}} p(s_t, a_t) \nabla_{\theta} \log \pi_{\theta}(a_t | s_t) b(s_t) ds_t da_t}$$

Let us show this is 0!



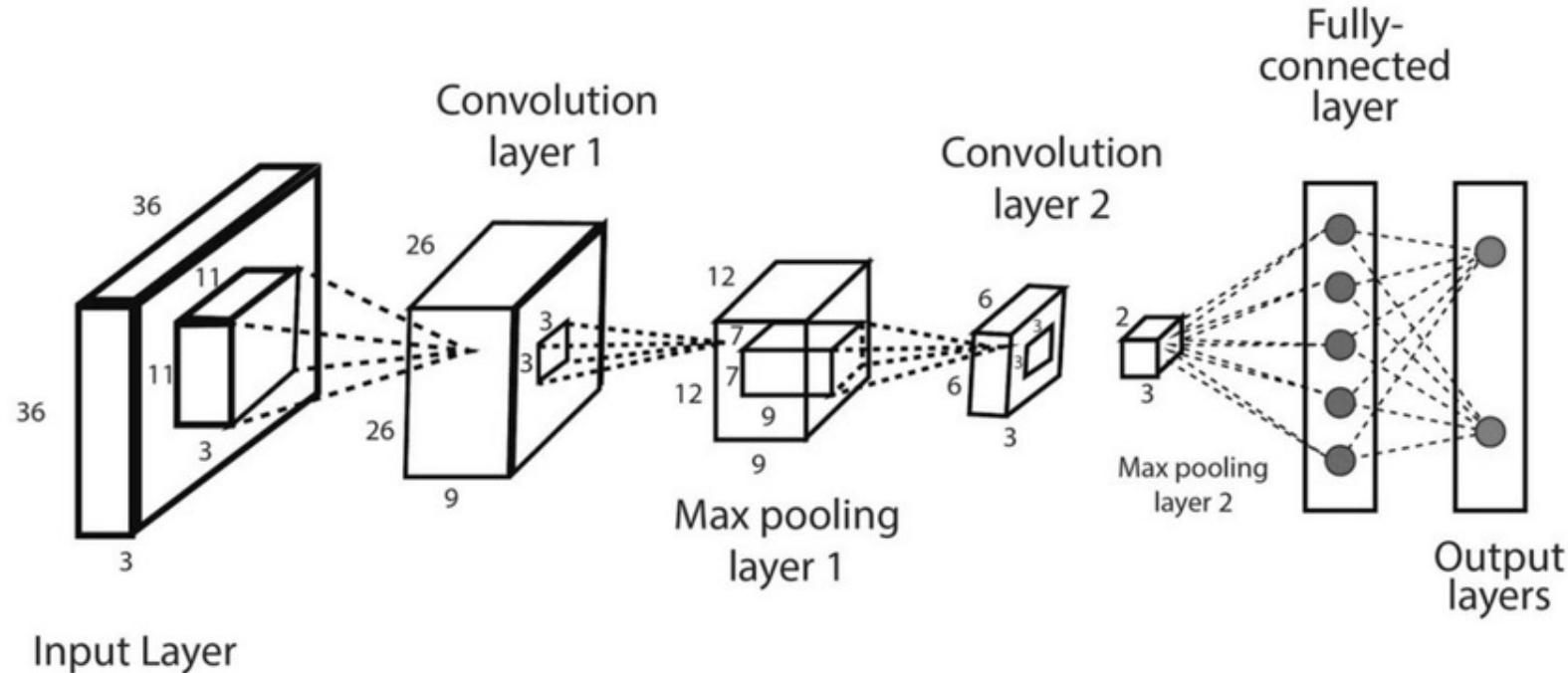
# Variance Reduction with a Baseline

$$\begin{aligned} \int \int p(s_t, a_t) \nabla_{\theta} \log \pi_{\theta}(a_t | s_t) [b(s_t)] ds_t da_t &= \int \int p(s_t) \pi_{\theta}(a_t | s_t) \nabla_{\theta} \log \pi_{\theta}(a_t | s_t) [b(s_t)] ds_t da_t \\ &= \int p(s_t) b(s_t) \int \pi_{\theta}(a_t | s_t) \nabla_{\theta} \log \pi_{\theta}(a_t | s_t) da_t ds_t \\ &= \int p(s_t) b(s_t) \int \nabla_{\theta} \pi_{\theta}(a_t | s_t) da_t ds_t \\ &= \int p(s_t) b(s_t) \nabla_{\theta} \int \pi_{\theta}(a_t | s_t) da_t ds_t = \int p(s_t) b(s_t) \nabla_{\theta}(1) ds_t = 0 \end{aligned}$$

Unbiased!

# Learning Baselines

Baselines are typically learned as deep neural nets from  $R^s \rightarrow R^1$



$$\frac{1}{N} \sum_{j=1}^N \|\hat{V}(s_t^j, a_t^j) - \sum_{t=1}^H r(s_t^j, a_t^j)\|$$

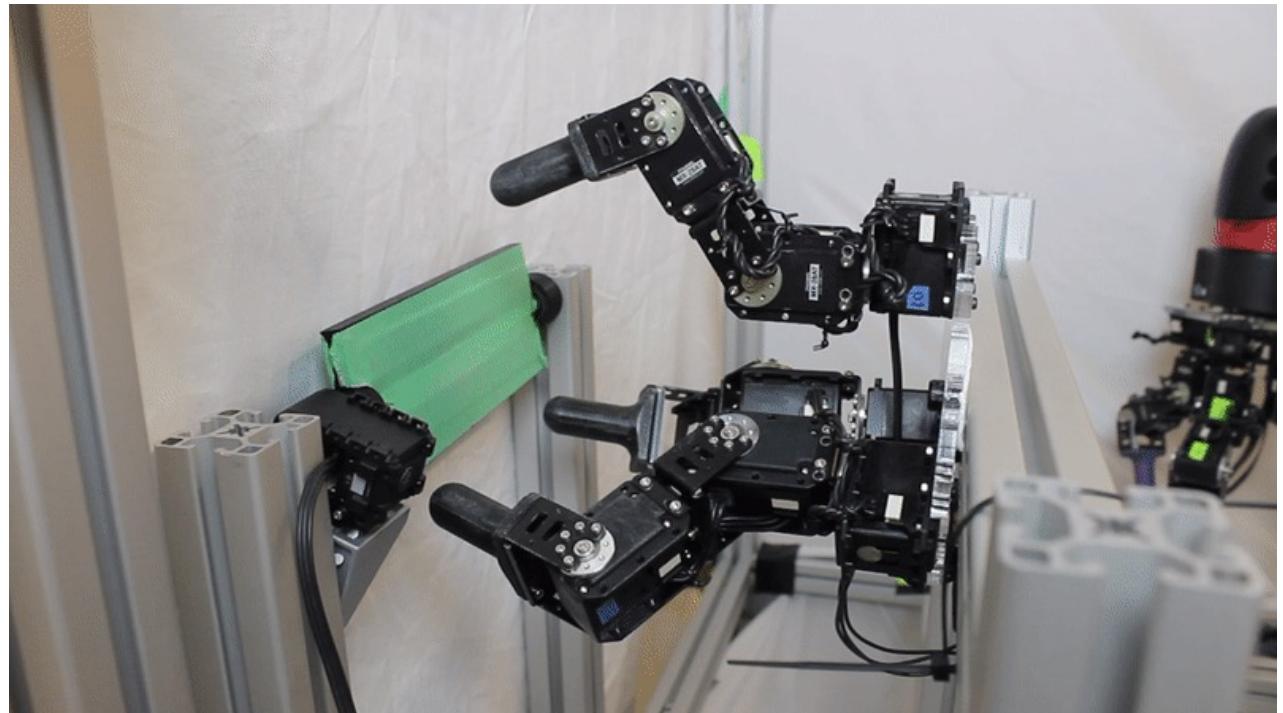
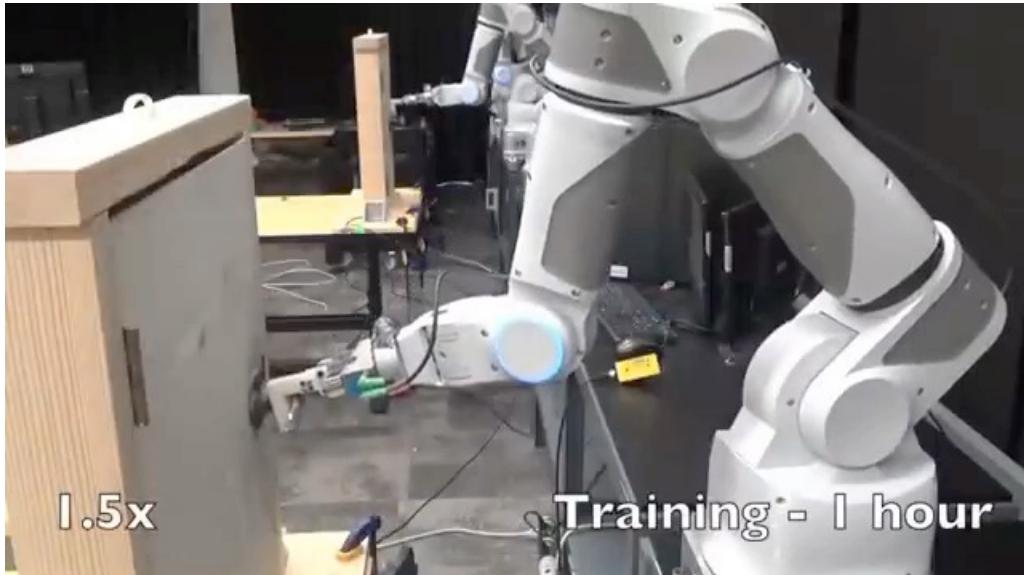
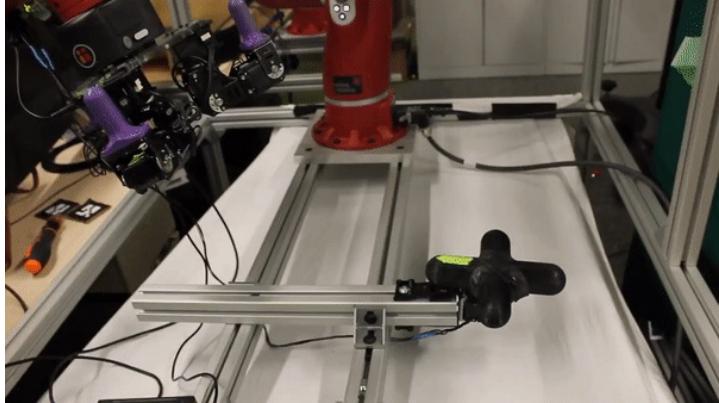
Minimize with Monte-carlo regression at every iteration, club with policy loss

$$A(s_t, a_t) = \sum_{t'=t}^T r(s'_t, a'_t) - V(s_t)$$

Allows us to define advantages

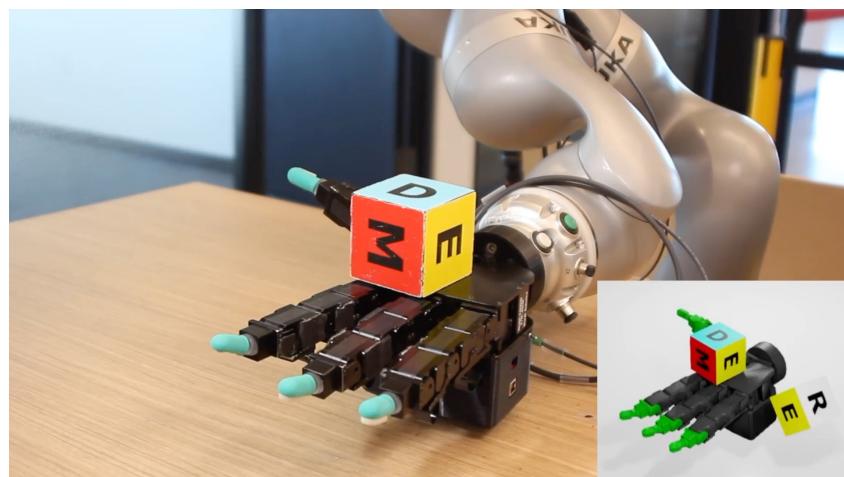
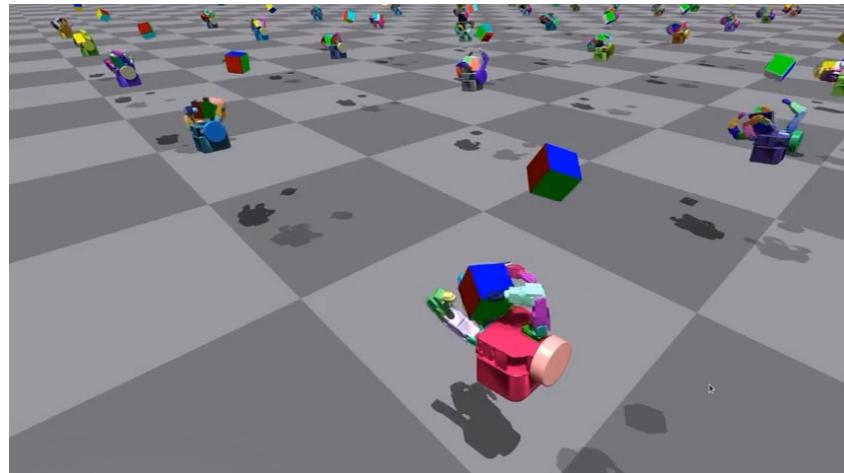
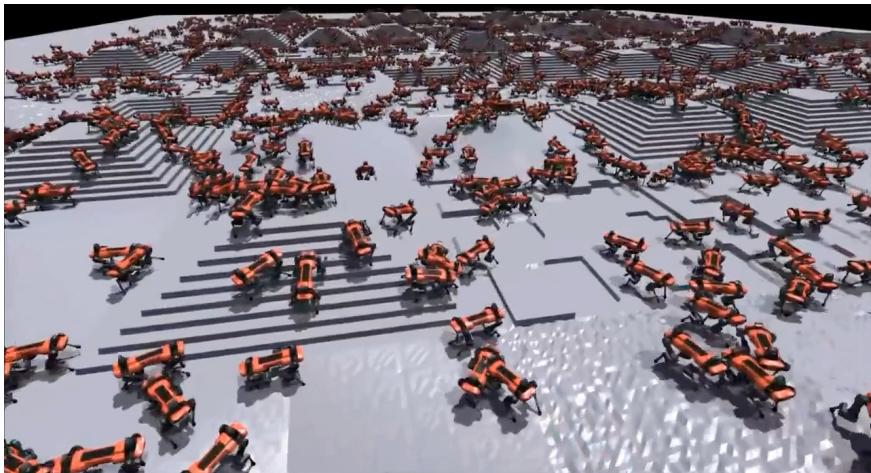
# How is this useful for robotics?

Can be used to train robots in the real world but only in limited settings



# How is this useful for robotics?

Largely useful for pretraining in simulation

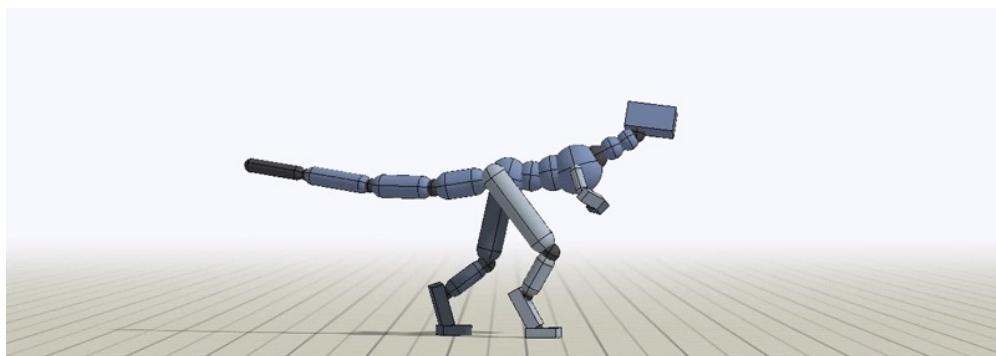
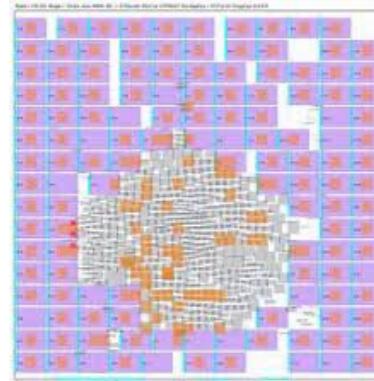


More in the sim2real lecture!

# Pros/Cons of Policy Gradient Methods

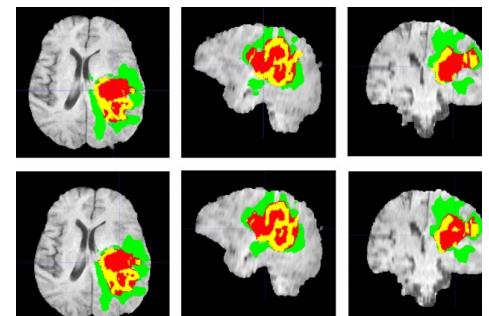
## Pros

- Conceptually simple, easy to implement
- Stable, good asymptotic performance
- Compatible with deep models
- Require minimal modeling



## Cons

- Sample inefficient
- Unable to reuse prior data effectively → on-policy
- Blackbox, can be hard to debug



# Lecture Outline

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**Recap + Policy Gradient**



Basic Actor Critic Algorithms



Making Actor-Critic Practical

# Why is Policy Gradient sample inefficient?

$$\begin{aligned}\nabla_{\theta} J(\theta) &= \int p_{\theta}(\tau) \nabla_{\theta} \log p_{\theta}(\tau) d\tau \\ &\approx \frac{1}{N} \sum_{i=1}^N \sum_t \nabla_{\theta} \log \pi_{\theta}(a_t^i | s_t^i) \sum_{t'=t}^T r(s_t^i, a_t^i)\end{aligned}$$



On-policy, unable to effectively use past data

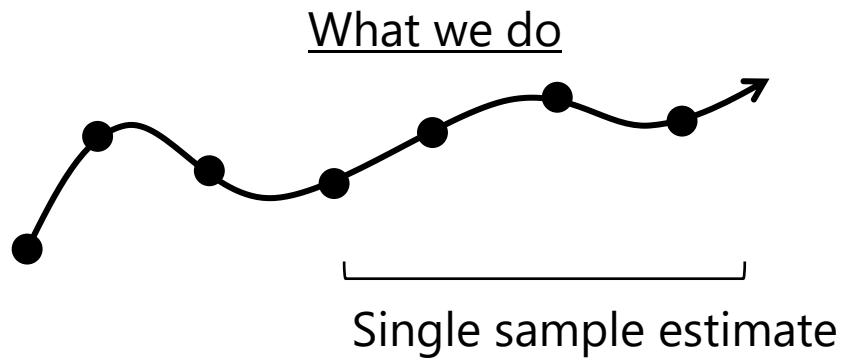
High Variance Estimator

Can we develop a **low variance off-policy** RL algorithm that can bootstrap from prior data?

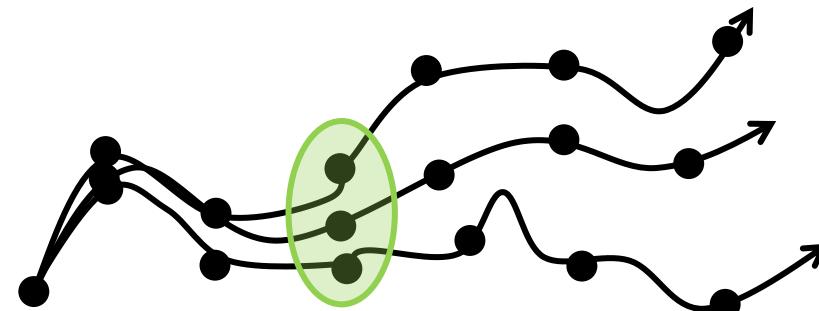
# What can we do to lower variance?

$$\begin{aligned}\nabla_{\theta} J(\theta) &= \int p_{\theta}(\tau) \nabla_{\theta} \log p_{\theta}(\tau) d\tau \\ &\approx \frac{1}{N} \sum_{i=1}^N \sum_t \nabla_{\theta} \log \pi_{\theta}(a_t^i | s_t^i) \sum_{t'=t}^T r(s_t^i, a_t^i)\end{aligned}$$

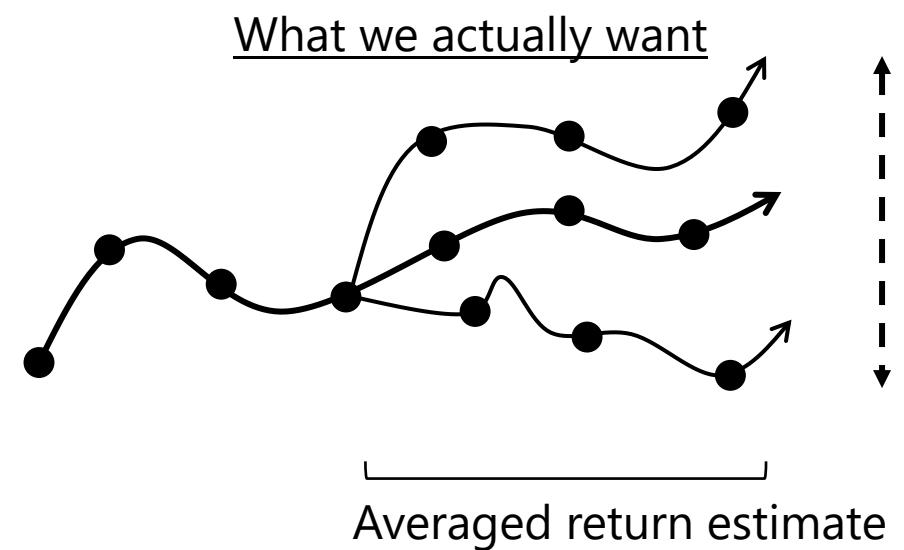




Idea: bundle this across many (s, a) with a function approximator

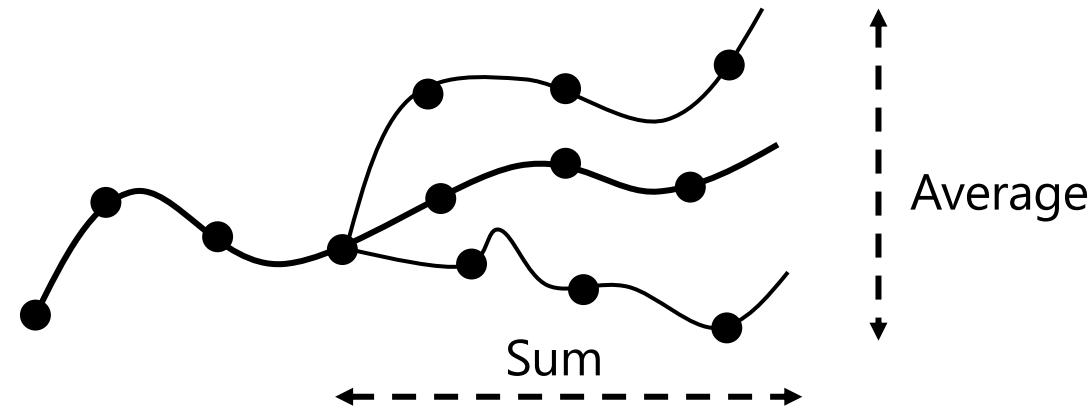


Function approximator bundles return estimates across states



# Notation: Q functions

$$\frac{1}{N} \sum_{i=1}^N \sum_t \nabla_\theta \log \pi_\theta(a_t^i | s_t^i) \sum_{t'=t}^T r(s_t^i, a_t^i)$$



Expected sum of rewards in the future, starting from  $(s, a)$  on first step, then  $\pi$

$$Q^\pi(s_t, a_t) = \mathbb{E}_{\pi_\theta} \left[ \sum_{t'=t}^T r(s'_t, a'_t) | s_t, a_t \right]$$

Bundles estimates across  $(s, a)$

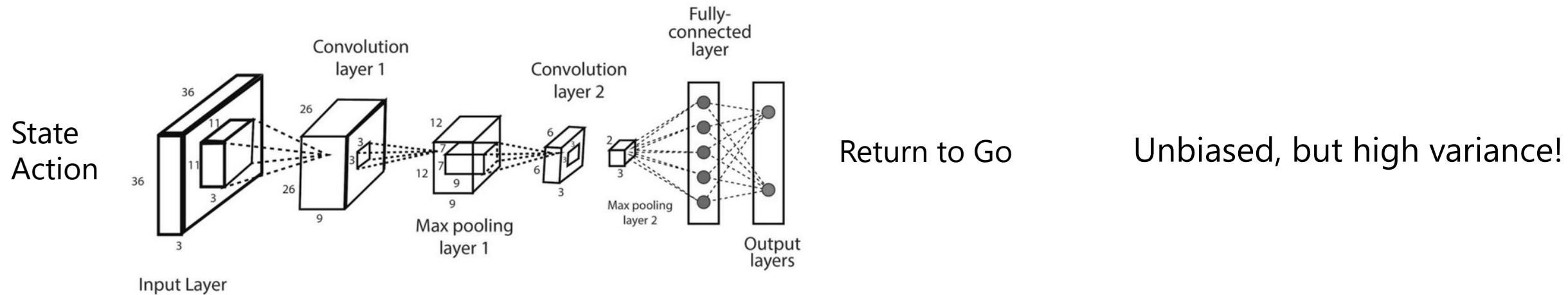
Use the magic of (deep) function approximation

# Estimation of Q-Functions

$$\frac{1}{N} \sum_{i=0}^N \sum_{t=0}^T \nabla_{\theta} \log \pi_{\theta}(a_t^i | s_t^i) Q^{\pi}(s_{t'}^i, a_{t'}^i)$$

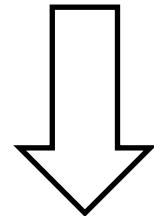
$$Q^{\pi}(s_t, a_t) = \mathbb{E}_{\pi_{\theta}} \left[ \sum_{t'=t}^T r(s'_t, a'_t) | s_t, a_t \right] \xleftarrow{\text{Monte-carlo approximation}}$$

Idea: Regression from (s, a) to Monte-Carlo estimate



# Can we do better?

$$\frac{1}{N} \sum_{i=1}^N \sum_t \nabla_{\theta} \log \pi_{\theta}(a_t^i | s_t^i) \sum_{t'=t}^T r(s_t^i, a_t^i)$$



Much lower variance if estimated well

$$\frac{1}{N} \sum_{i=0}^N \sum_{t=0}^T \nabla_{\theta} \log \pi_{\theta}(a_t^i | s_t^i) Q^{\pi}(s_{t'}^i, a_{t'}^i)$$

Can be learned off-policy!

Has special structure we can exploit!!

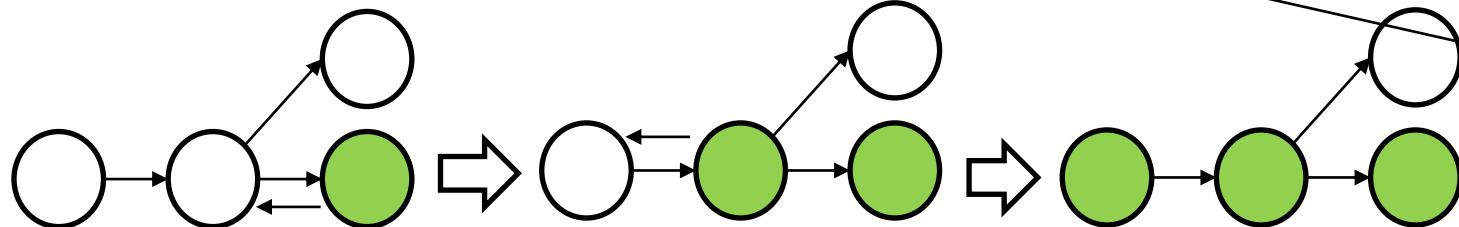
# Recursive structure in Q functions

Q functions have special recursive structure!

$$\begin{aligned}
 Q^\pi(s_t, a_t) &= \mathbb{E}_{\pi_\theta} \left[ \sum_{t'=t}^T r(s'_t, a'_t) | s_t, a_t \right] \\
 &= r(s_t, a_t) + \mathbb{E}_\pi \left[ \sum_{t'=t+1} \mathbb{E}_{s_{t+1} \sim p(\cdot | s_t, a_t)} [Q^\pi(s_{t+1}, a_{t+1})] \right]
 \end{aligned}$$

Bellman equation

$$Q^\pi(s_t, a_t) = r(s_t, a_t) + \mathbb{E}_{\substack{s_{t+1} \sim p(\cdot | s_t, a_t) \\ a_{t+1} \sim \pi_\theta(\cdot | s_{t+1})}} [Q^\pi(s_{t+1}, a_{t+1})]$$



Decompose temporally via dynamic programming

Can be from different policies

# Learning Q-functions via Dynamic Programming

Policy Evaluation: Try to minimize Bellman Error  
(almost)

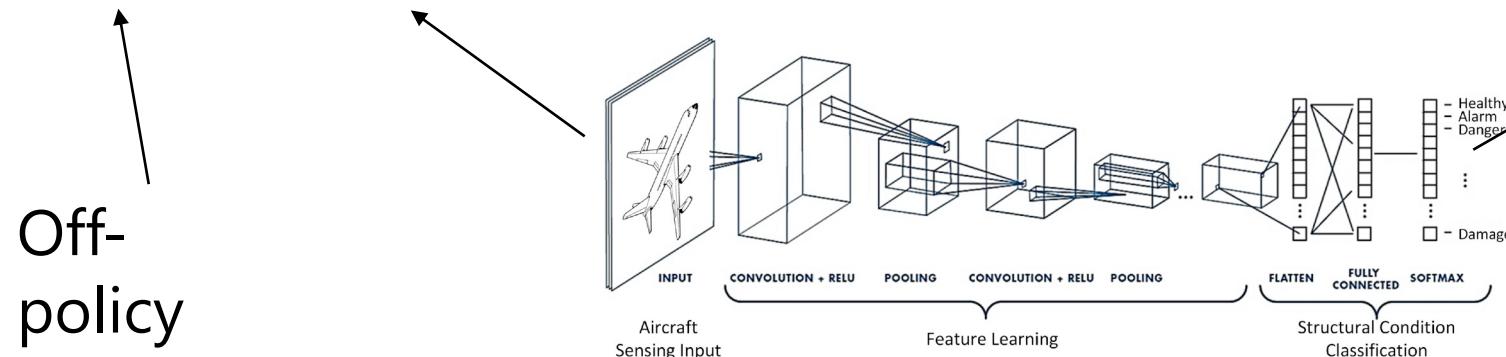
Bellman  
equation

$$Q^\pi(s_t, a_t) = r(s_t, a_t) + \mathbb{E}_{\substack{s_{t+1} \sim p(\cdot | s_t, a_t) \\ a_{t+1} \sim \pi_\theta(\cdot | s_{t+1})}} [Q^\pi(s_{t+1}, a_{t+1})]$$

Same function  
approximator

How can we convert this recursion into a learning  
objective?

$$\min_{\phi} \mathbb{E}_{(s_t, a_t, s_{t+1}) \sim \mathcal{D}} \left( Q_{\phi}^{\pi}(s_t, a_t) - (r(s_t, a_t) + \mathbb{E}_{a_{t+1} \sim \pi_\theta(a_{t+1} | s_{t+1})} [Q_{\hat{\phi}}^{\pi}(s_{t+1}, a_{t+1})]) \right)^2$$



Off-  
policy

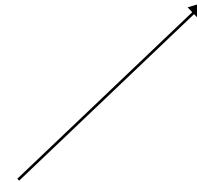
Can train via  
GD!

Note: this may look like gradient descent on Bellman error, it is not!

# Improving Policies with Learned Q-functions

Policy Improvement: Improve policy with **policy gradient**

$$\max_{\theta} \mathbb{E}_{s \sim \mathcal{D}, a \sim \pi_{\theta}(a|s)} [Q^{\pi_{\theta}}(s, a)]$$



Replace Monte-Carlo sum of rewards with learned Q function

Lowers variance compared to policy gradient!

# Policy Updates – REINFORCE or Reparameterization

Let's look a little deeper into the policy update

$$\max_{\theta} J(\theta) = \max_{\theta} \mathbb{E}_{s \sim \mathcal{D}} \mathbb{E}_{a \sim \pi_{\theta}(\cdot | s)} [Q^{\pi}(s, a)]$$

Likelihood Ratio/Score Function

Pathwise derivative/Reparameterization

$$\nabla_{\theta} J(\theta) = \mathbb{E}_{s \sim \mathcal{D}} \mathbb{E}_{a \sim \pi_{\theta}(\cdot | s)} [\nabla_{\theta} \log \pi_{\theta}(a | s) Q^{\pi}(s, a)]$$

$$\nabla_{\theta} J(\theta) = \mathbb{E}_{s \sim \mathcal{D}} \mathbb{E}_{z \sim p(z)} [\nabla_a Q^{\pi}(s, a)|_{a=\mu_{\theta}+z\sigma_{\theta}} \nabla_{\theta}(\mu_{\theta} + z\sigma_{\theta})]$$

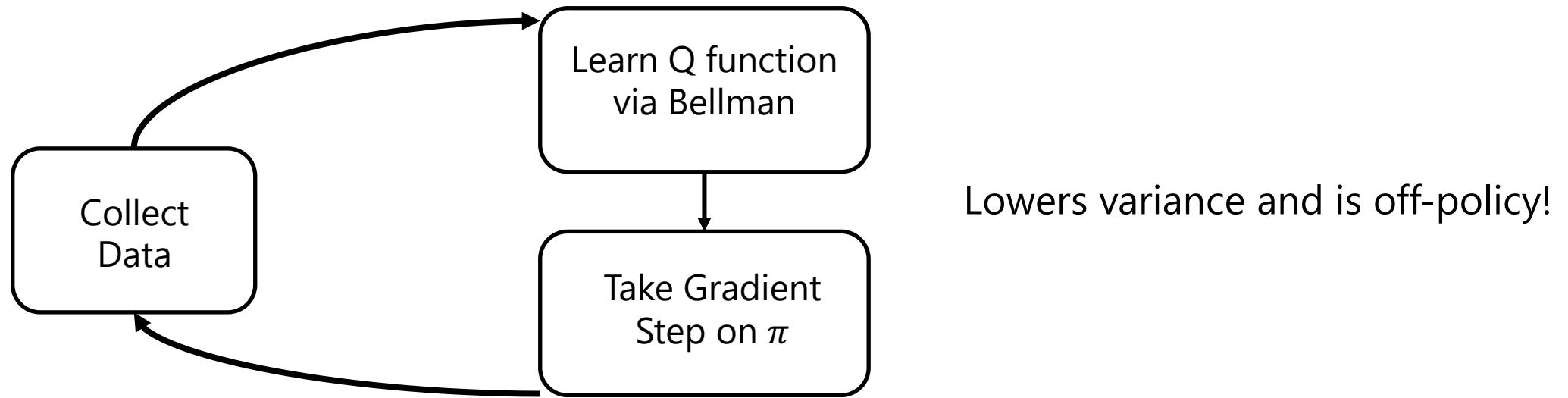
Easier to Apply to Broad Policy Class

Lower variance

# Actor-Critic: Policy Gradient in terms of Q functions

Critic: learned via the Bellman update (Policy Evaluation)

$$\min_{\phi} \mathbb{E}_{(s_t, a_t, s_{t+1}) \sim \mathcal{D}} [(Q_{\phi}^{\pi}(s_t, a_t) - (r(s_t, a_t) + \mathbb{E}_{a_{t+1} \sim \pi(\cdot | s_{t+1})} [Q_{\bar{\phi}}(s_{t+1}, a_{t+1})]))^2]$$

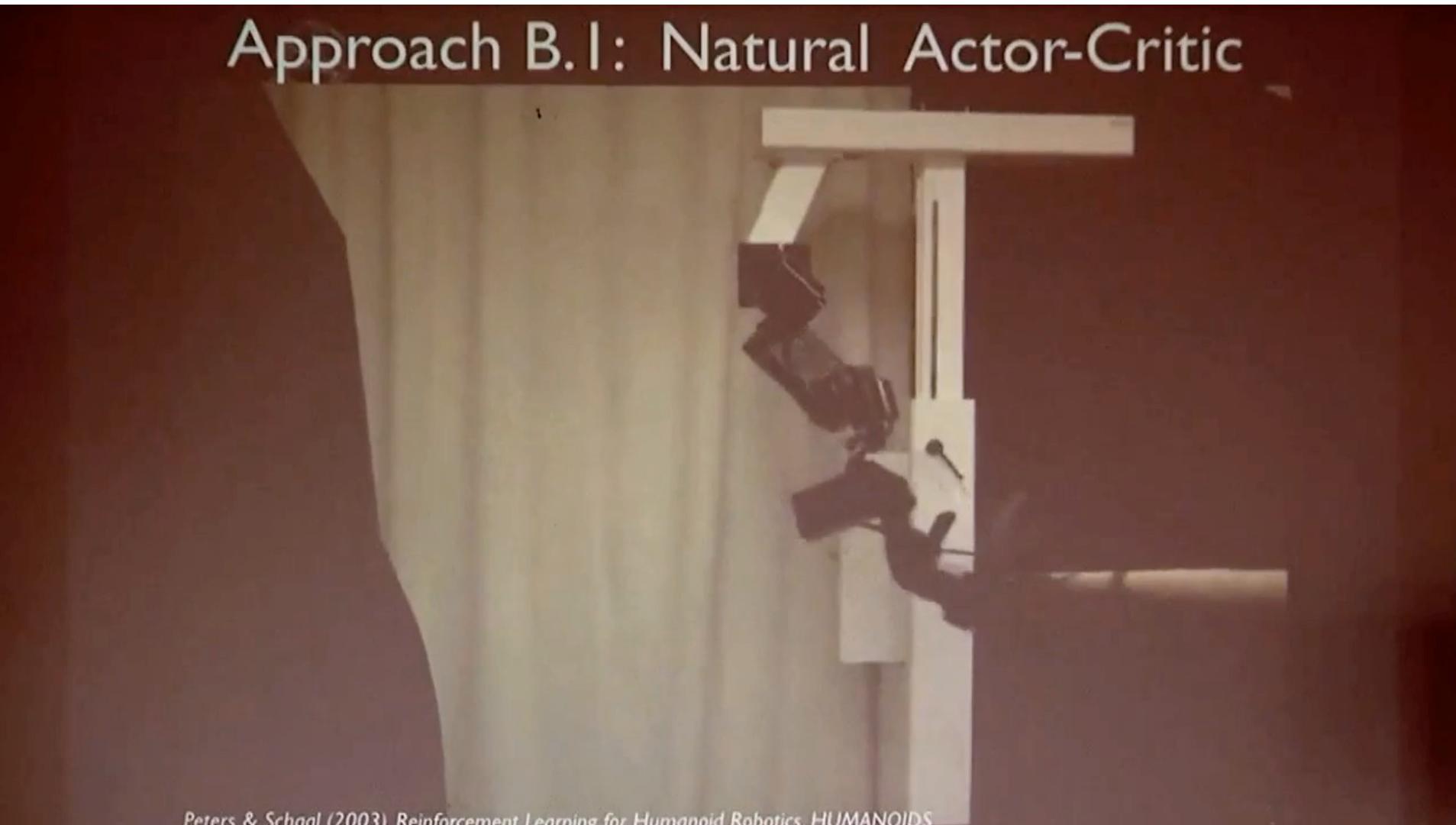


Actor: updated using learned critic (Policy Improvement)

$$\max_{\pi} \mathbb{E}_{s \sim \mathcal{D}} \mathbb{E}_{a \sim \pi(\cdot | s)} [Q^{\pi}(s, a)]$$

# Actor-Critic in Action

Approach B.I: Natural Actor-Critic



Peters & Schaal (2003). Reinforcement Learning for Humanoid Robotics, HUMANOIDS

# Lecture Outline

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**Recap + Policy Gradient**



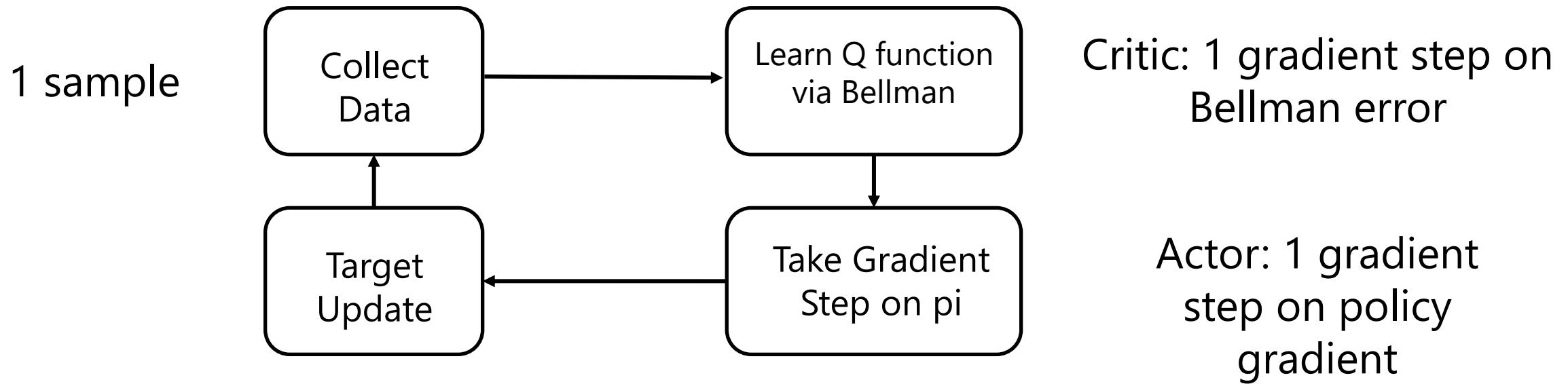
**Basic Actor Critic Algorithms**



Making Actor-Critic Practical

# Going from Batch Updates to Online Updates

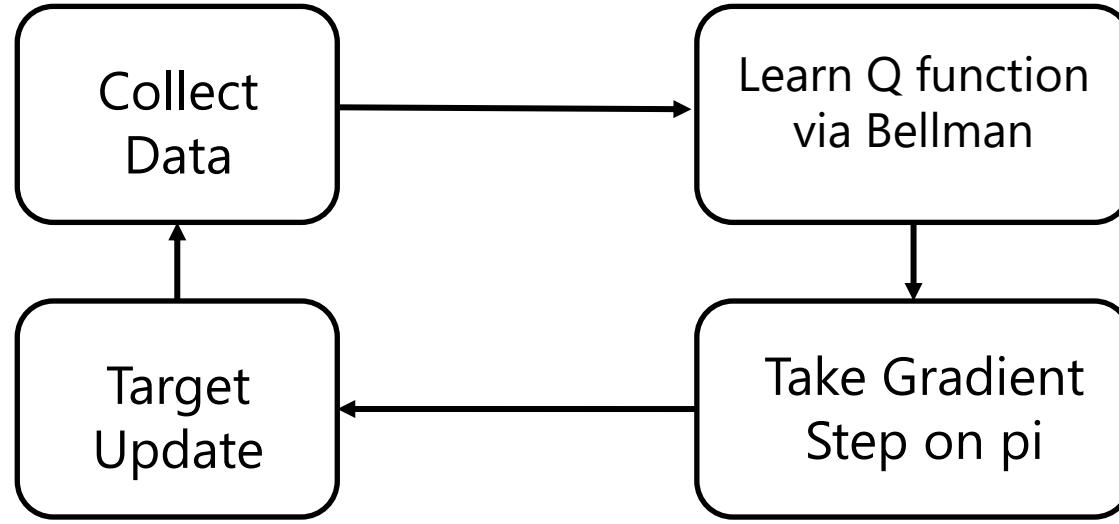
This algorithm can go from full batch mode to fully online updates



Allows for much more immediate updates

# Challenges of doing online updates

1 sample



Critic: 1 gradient step on Bellman error

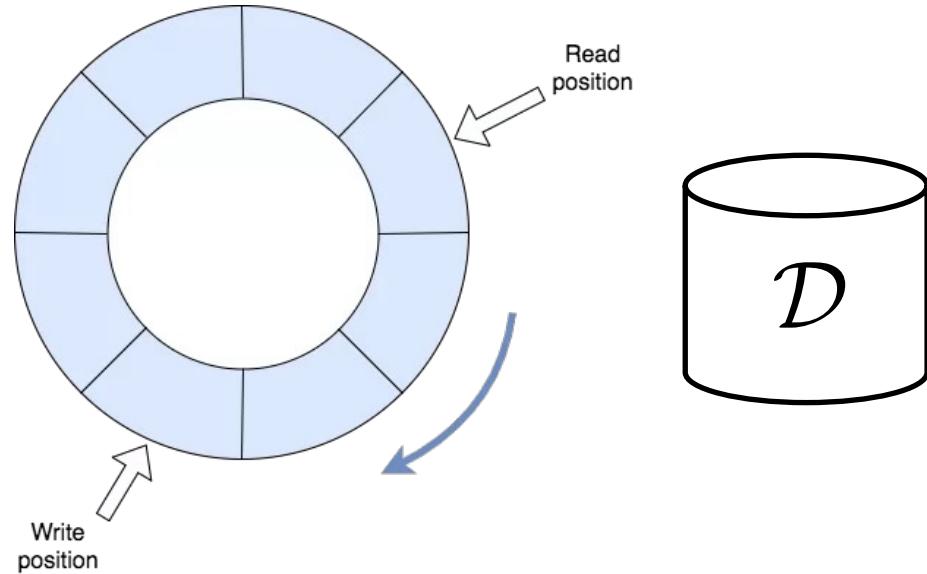
Actor: 1 gradient step on policy gradient

When updates are performed online, two issues persist:

1. Correlated updates since samples are correlated
2. Optimization objective changes constantly, unstable

# Decorrelating updates with replay buffers

Updates can be decorrelated by storing and shuffling data in a replay buffer



Sampled from replay buffer

$$\min_{\phi} \mathbb{E}_{(s,a,s') \sim \mathcal{D}} [Q_{\phi}^{\pi}(s_t, a_t) - (r(s_t, a_t) + \mathbb{E}_{a_{t+1} \sim \pi(\cdot | s_{t+1})} [Q_{\bar{\phi}}(s_{t+1}, a_{t+1})])]^2$$

$$\max_{\pi} \mathbb{E}_{s \sim \mathcal{D}} \mathbb{E}_{a \sim \pi(\cdot | s)} [Q^{\pi}(s, a)]$$

Instead of doing updates in order,  
sample batches from replay buffer

↓  
How?

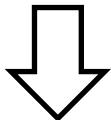
1. Sample uniformly
2. Prioritize by TD-error
3. Prioritize by target error
4. ... open area of research!

# Slowing moving targets with target networks

Continuous updates can be unstable since there is a churn of projection and backup

$$\min_{\phi} \mathbb{E}_{(s,a,s') \sim \mathcal{D}} \left[ Q_{\phi}^{\pi}(s_t, a_t) - (r(s_t, a_t) + \mathbb{E}_{a_{t+1} \sim \pi(\cdot | s_{t+1})} [Q_{\bar{\phi}}(s_{t+1}, a_{t+1})]) \right]^2$$

If we set  $\bar{\phi}$  to  $\phi$  every update, the update becomes very unstable

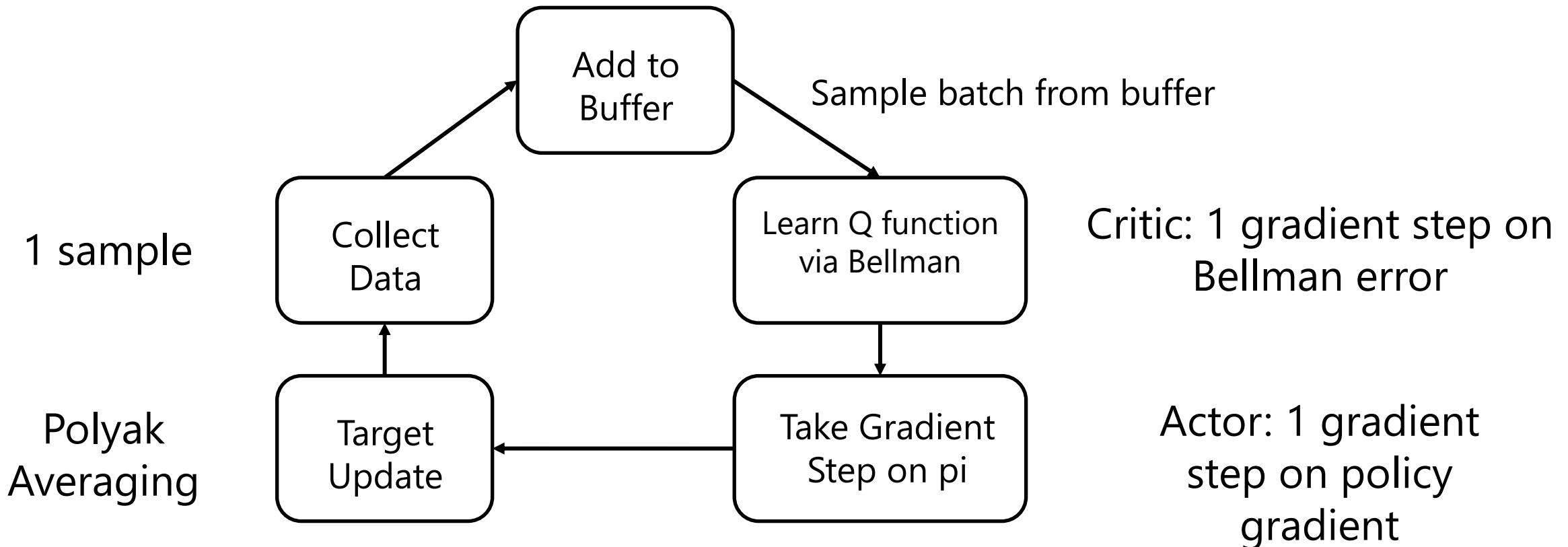


Move  $\bar{\phi}$  to  $\phi$  slowly!

$$\bar{\phi} = (1 - \tau)\phi + \tau\bar{\phi}$$

Polyak averaging

# A Practical Off-Policy RL Algorithm



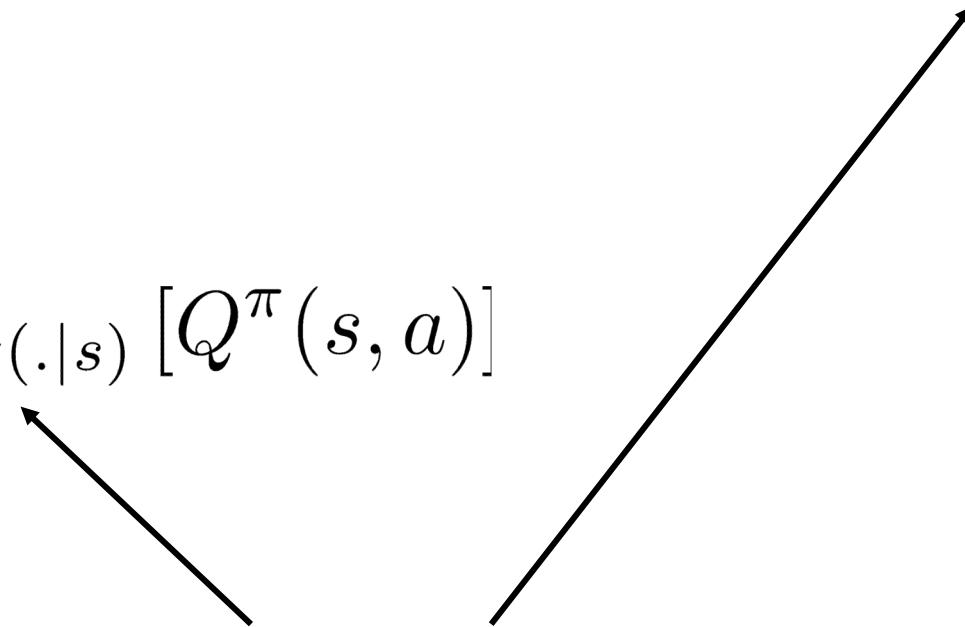
# Simplify -- Can we get rid of a parametric actor?

Critic Update

$$\min_{\phi} \mathbb{E}_{(s,a,s') \sim \mathcal{D}} [Q_{\phi}^{\pi}(s_t, a_t) - (r(s_t, a_t) + \mathbb{E}_{a_{t+1} \sim \pi(\cdot | s_{t+1})} [Q_{\bar{\phi}}(s_{t+1}, a_{t+1})])^2]$$

Actor Update

$$\max_{\pi} \mathbb{E}_{s \sim \mathcal{D}} \mathbb{E}_{a \sim \pi(\cdot | s)} [Q^{\pi}(s, a)]$$



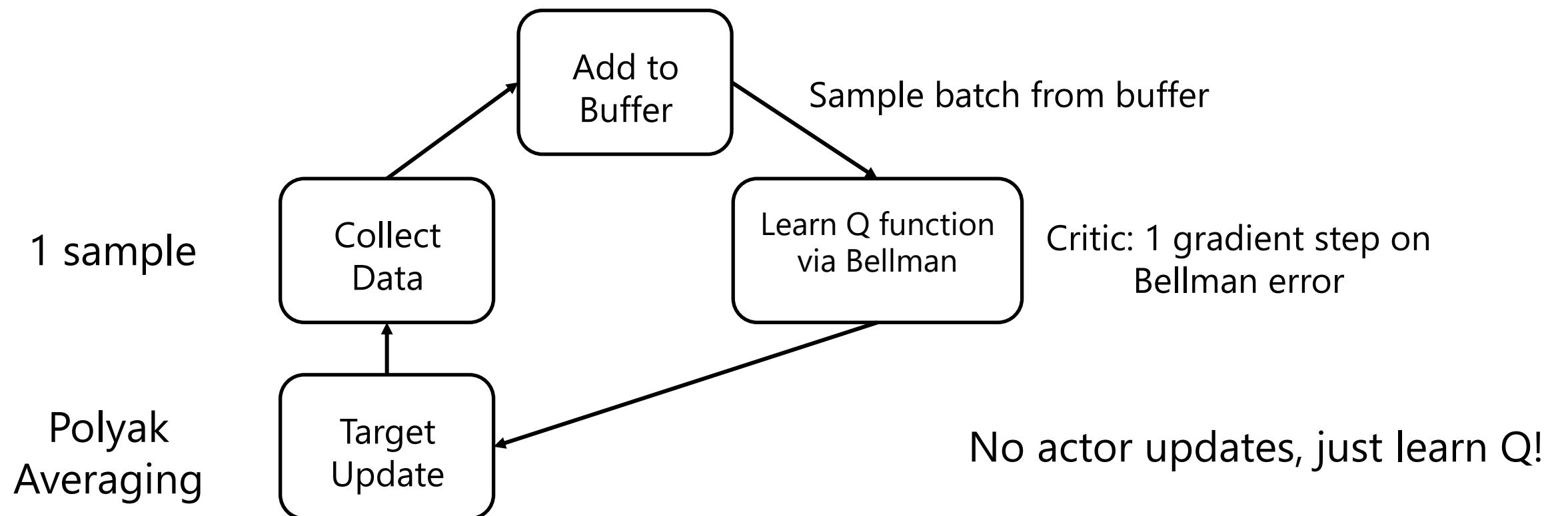
What if we removed this explicit actor completely?

# Directly Learning Q\*

$$\min_{\phi} \mathbb{E}_{(s,a,s') \sim \mathcal{D}} \left[ \left[ Q_{\phi}^{\pi}(s_t, a_t) - (r(s_t, a_t) + \max_{a_{t+1}} [Q_{\bar{\phi}}(s_{t+1}, a_{t+1})]) \right]^2 \right]$$

$$\pi(a|s) = \max_a Q(s, a)$$

Directly do max in the Bellman update



# How can we maximize w.r.t a?

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$$\pi(a|s) = \max_a Q(s, a)$$



Analytic maximization can be very difficult to perform in continuous action spaces  
Much easier in discrete spaces! → just do categorical max!

Some ideas to do maximization:

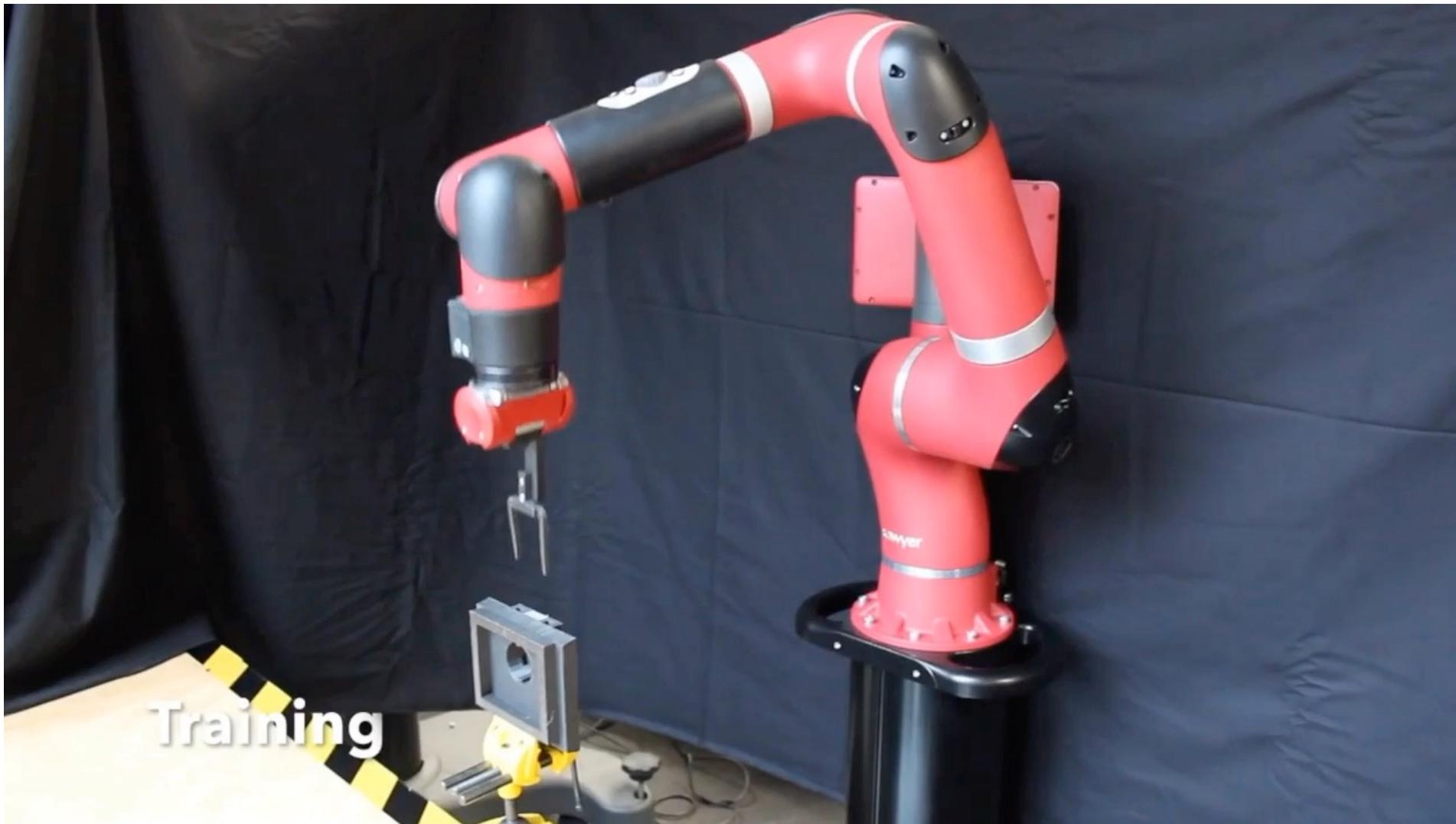
1. Sampling based (QT-opt (Kalashnikov et al))
2. Optimization based (NAF, Gu et al)

# Practical Actor-Critic in Action



Trained using QT-Opt

# Practical Actor-Critic in Action



Trained using DDPG

# What makes off-policy RL hard?

Deadly triad:

1. Function Approximation
2. Bootstrapping
3. Off-policy learning

$$\min_{\phi} \mathbb{E}_{(s,a,s') \sim \mathcal{D}} \left[ \left[ Q_{\phi}^{\pi}(s_t, a_t) - (r(s_t, a_t) + \max_{a_{t+1}} [Q_{\bar{\phi}}(s_{t+1}, a_{t+1})]) \right]^2 \right]$$

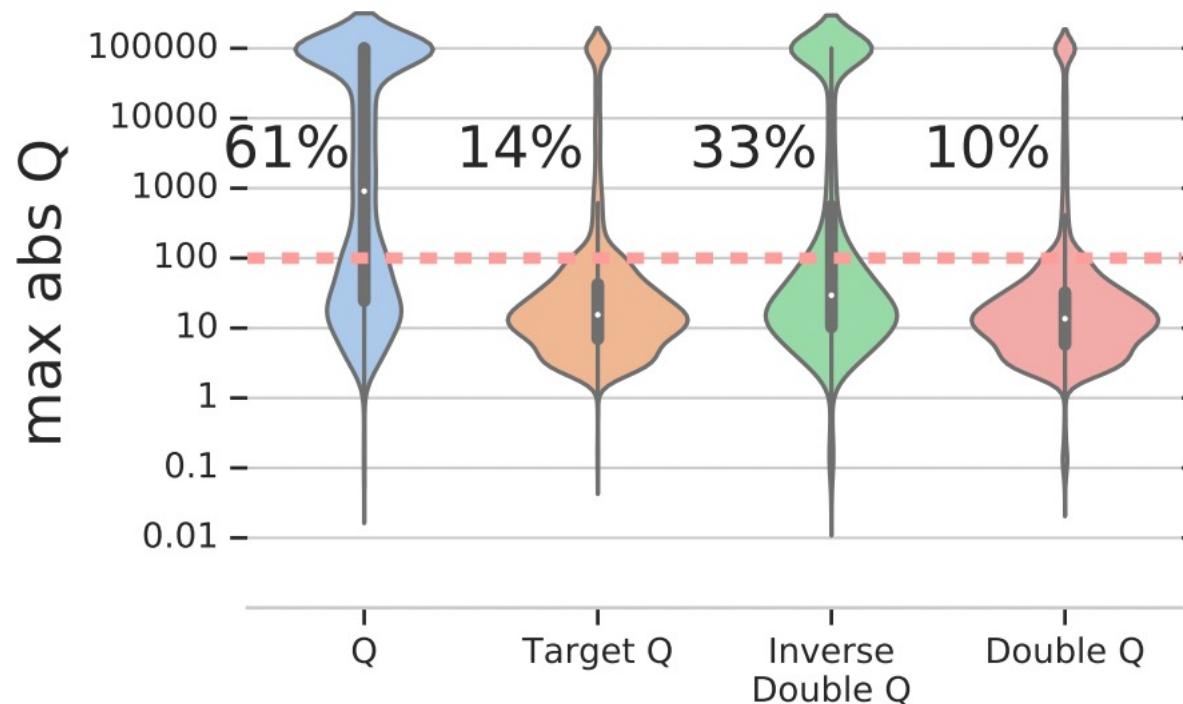
These in combination lead to many of the difficulties in stabilizing off-policy RL with function approximation

# Zooming out – what makes off-policy RL hard?

Deadly triad:

1. Function Approximation
2. Bootstrapping
3. Off-policy learning

61% of runs show divergence of Q-values



Diverges even with linear function approximation,  
when off-policy + bootstrapping

# Lecture Outline

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**Recap + Policy Gradient**



**Basic Actor Critic Algorithms**



**Making Actor-Critic Practical**

# Recap: Course Overview

Filtering/Smoothing

Localization

Mapping

SLAM

Search

Motion Planning

TrajOpt

Stability/Certification

MDPs and RL

Imitation Learning

Off-Policy/MBRL