CSE-571 Robotics

Planning and Control:

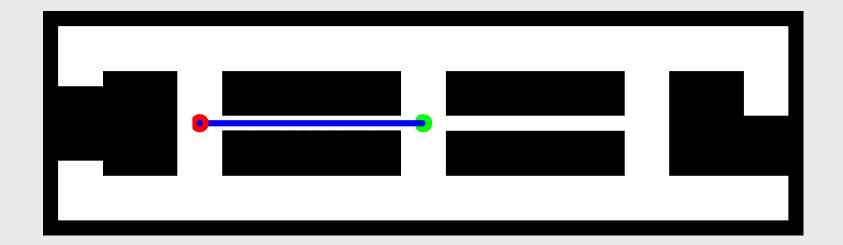
Markov Decision Processes

Problem Classes

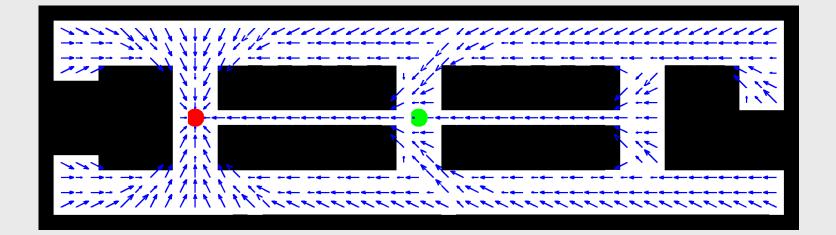
Deterministic vs. stochastic actions

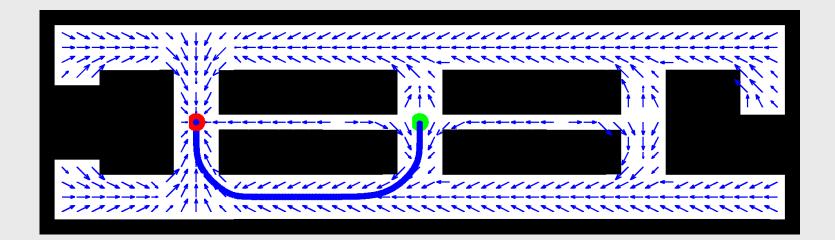
Full vs. partial observability

Deterministic, fully observable

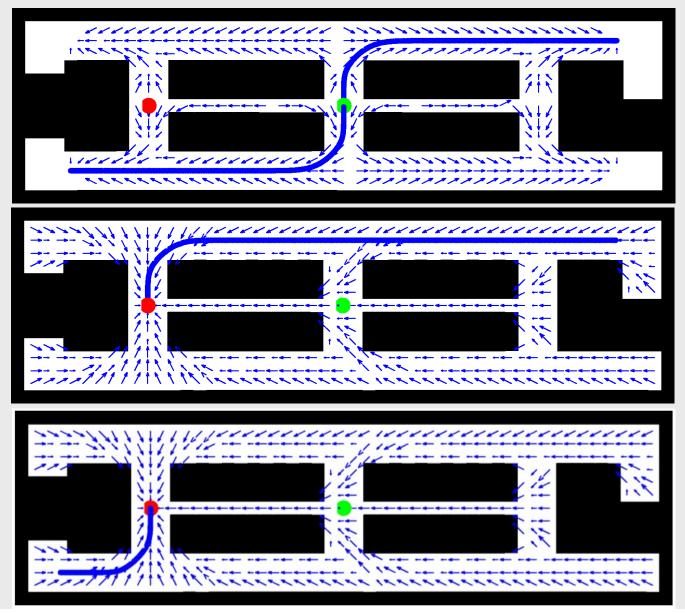


Stochastic, Fully Observable

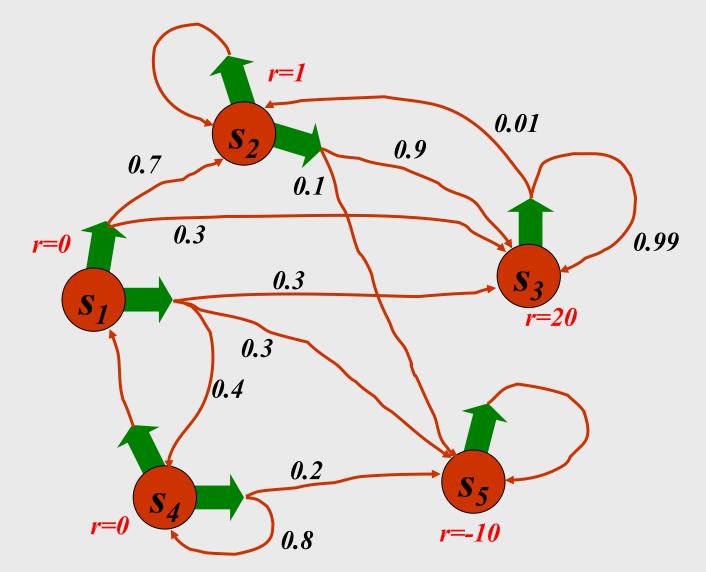




Stochastic, Partially Observable



Markov Decision Process (MDP)



Markov Decision Process (MDP)

• Given:

- States *x*
- Actions *u*
- Transition probabilities p(x'|u,x)
- Reward / payoff function r(x,u)

• Wanted:

Policy π(x) that maximizes the future expected reward

Rewards and Policies

• Policy (general case):

$$\pi: \quad z_{1:t-1}, u_{1:t-1} \rightarrow u_t$$

• Policy (fully observable case):

 $\pi: x_t \rightarrow u_t$

• Expected cumulative payoff:

$$R_{T} = E \quad \left[\sum_{\tau=1}^{T} \gamma^{\tau} r_{t+\tau}\right]$$

- T=1: greedy policy
- T>1: finite horizon case, typically no discount
- T=infty: infinite-horizon case, finite reward if discount < 1

Policies contd.

• Expected cumulative payoff of policy:

$$R_{T}^{\pi}(x_{t}) = E \left[\sum_{\tau=1}^{T} \gamma^{\tau} r_{t+\tau} \mid u_{t+\tau} = \pi \left(z_{1:t+\tau-1} u_{1:t+\tau-1} \right) \right]$$

• Optimal policy:

$$\pi^* = \operatorname{argmax} R_T^{\pi}(x_t)$$

• 1-step optimal policy:

$$\pi_1(x) = \operatorname{argmax} r(x, u)$$

• Value function of 1-step optimal policy:

$$V_1(x) = \gamma \max_u r(x, u)$$

2-step Policies

• Optimal policy:

$$\pi_2(x) = \underset{u}{\operatorname{argmax}} \left[r(x,u) + \int V_1(x') p(x'|u,x) dx' \right]$$

• Value function:

$$V_2(x) = \gamma \max_{u} \left[r(x,u) + \int V_1(x') p(x'|u,x) dx' \right]$$

T-step Policies

• Optimal policy:

$$\pi_{T}(x) = \underset{u}{\operatorname{argmax}} \left[r(x,u) + \int V_{T-1}(x') p(x' | u, x) dx' \right]$$

• Value function:

$$V_T(x) = \gamma \max_{u} \left[r(x,u) + \int V_{T-1}(x') p(x'|u,x) dx' \right]$$

Infinite Horizon

• Optimal policy:

$$V_{\infty}(x) = \gamma \max_{u} \left[r(x,u) + \int V_{\infty}(x') p(x'|u,x) dx' \right]$$

- Bellman equation
- Fix point is optimal policy
- Necessary and sufficient condition

Value Iteration

• for all x do

$$\hat{V}(x) \leftarrow r_{\min}$$

- endfor
- repeat until convergence
 - for all x do

$$\hat{V}(x) \leftarrow \gamma \max_{u} \left[r(x,u) + \int \hat{V}(x') p(x'|u,x) dx' \right]$$

- endfor
- endrepeat

$$\pi(x) = \underset{u}{\operatorname{argmax}} \quad \left[r(x,u) + \int \hat{V}(x') p(x' | u, x) dx' \right]$$

00	0	Gridworl	d Display	
	^		^	
	0.00	0.00	0.00	0.00
			^	
	0.00		0.00	0.00
		^	^	
	0.00	0.00	0.00	0.00

VALUES AFTER O ITERATIONS

Noise = 0.2 Discount = 0.9 Living reward = 0

00	0	Gridworl	d Display		
		^			
	0.00	0.00	0.00 →	1.00	
	^				
	0.00		∢ 0.00	-1.00	
	^	^	^		
	0.00	0.00	0.00	0.00	
				•	
	VALUES AFTER 1 ITERATIONS				

Noise = 0.2 Discount = 0.9 Living reward = 0

00	0	Gridworl	d Display	
	0.00	0.00 →	0.72)	1.00
	^		^	
	0.00		0.00	-1.00
	^		^	
	0.00	0.00	0.00	0.00
				•

VALUES AFTER 2 ITERATIONS

$\begin{array}{ c c c c c c c c c c c c c c c c c c c$	0 0	0	Gridworl	d Display	
0.00 0.43 -1.00		0.00 >	0.52 →	0.78)	1.00
• • • 0.00 0.00 0.00 0.00					-1.00
		•	• 0.00	•	0.00

VALUES AFTER 3 ITERATIONS

00	0	Gridwor	d Display	-
	0.37)	0.66)	0.83)	1.00
	• 0.00		• 0.51	-1.00
	•	0.00)	• 0.31	∢ 0.00
	VALUE	S AFTER	4 ITERA	TIONS

00	0	Gridworl	d Display		
	0.51 →	0.72 →	0.84)	1.00	
	• 0.27		• 0.55	-1.00	
	• 0.00	0.22 ≯	• 0.37	∢ 0.13	
	VALUES AFTER 5 ITERATIONS				

000	Gridworl	d Display		
0.59)	0.73)	0.85)	1.00	
•		• 0.57	-1.00	
• 0.21	0.31)	▲ 0.43	∢ 0.19	
VALUI	VALUES AFTER 6 ITERATIONS			

000	Gridworl	d Display	-
0.62)	0.74 →	0.85)	1.00
^		•	
0.50		0.57	-1.00
▲ 0.34	0.36)	▲ 0.45	• 0.24
VALUES AFTER 7 ITERATIONS			

000	Gridworl	d Display	
0.63)	0.74)	0.85)	1.00
▲ 0.53		• 0.57	-1.00
• 0.42	0.39)	▲ 0.46	∢ 0.26
VALUES AFTER 8 ITERATIONS			

000	Gridworl	d Display	
0.64)	0.74 ≯	0.85)	1.00
0.55		• 0.57	-1.00
▲ 0.46	0.40 →	• 0.47	∢ 0.27
VALUES AFTER 9 ITERATIONS			

000)	Gridworl	d Display		
	0.64)	0.74)	0.85)	1.00	
	•		• 0.57	-1.00	
	▲ 0.48	∢ 0.41	• 0.47	◆ 0.27	
	VALUES AFTER 10 ITERATIONS				

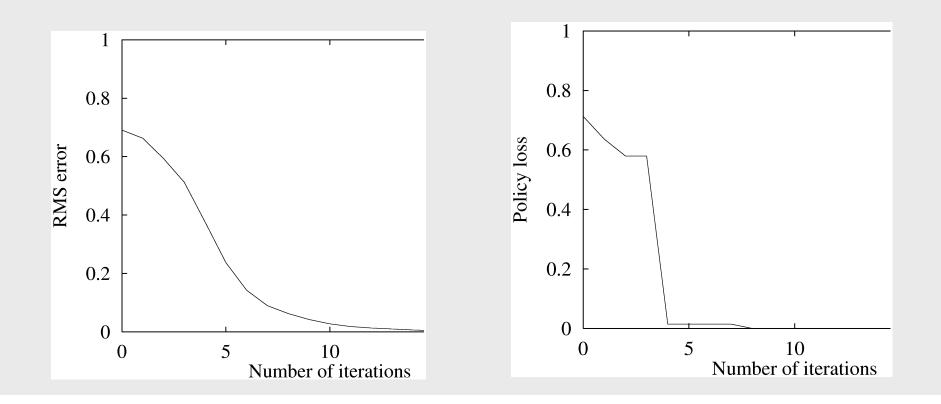
000	Gridworl	d Display	
0.64)	0.74 →	0.85)	1.00
•		•	
0.56		0.57	-1.00
▲ 0.48	∢ 0.42	• 0.47	∢ 0.27
VALUES AFTER 11 ITERATIONS			

Gridworld Display						
	0.64)	0.74 →	0.85)	1.00		
	•		•			
	0.57		0.57	-1.00		
	• 0.49	∢ 0.42	• 0.47	∢ 0.28		
	VALUES AFTER 12 ITERATIONS					

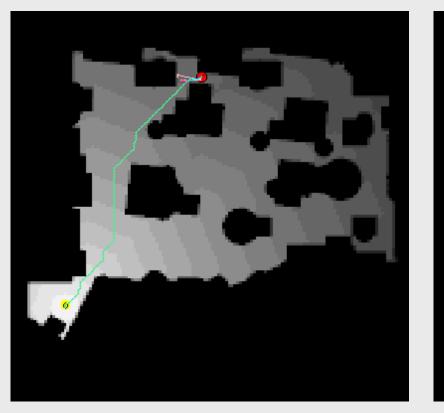
Gridworld Display					
0.64	▶ 0.74 ▶	0.85)	1.00		
^		•			
0.57		0.57	-1.00		
• 0.49	↓ 0.43	▲ 0.48	∢ 0.28		
VALUES AFTER 100 ITERATIONS					

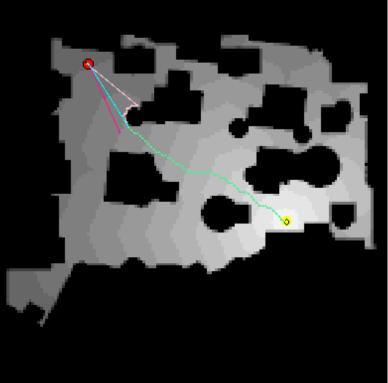
Value Function and Policy

- Each step takes O(|A| |S| |S|) time.
- Number of iterations required is polynomial in |S|, |A|, 1/(1-gamma)



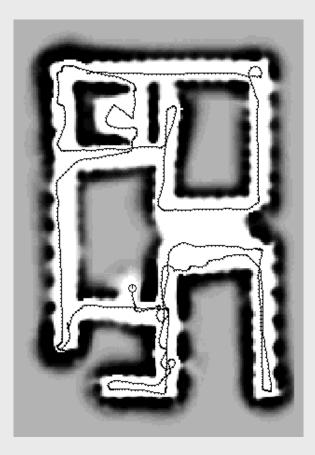
Value Iteration for Motion Planning (assumes knowledge of robot's location)

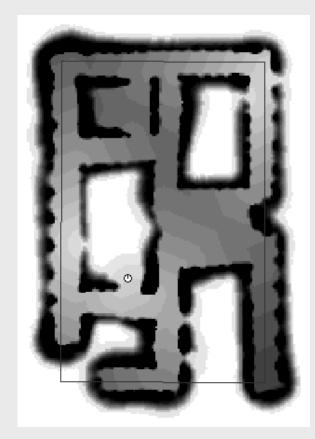




Frontier-based Exploration

• Every unknown location is a target point.





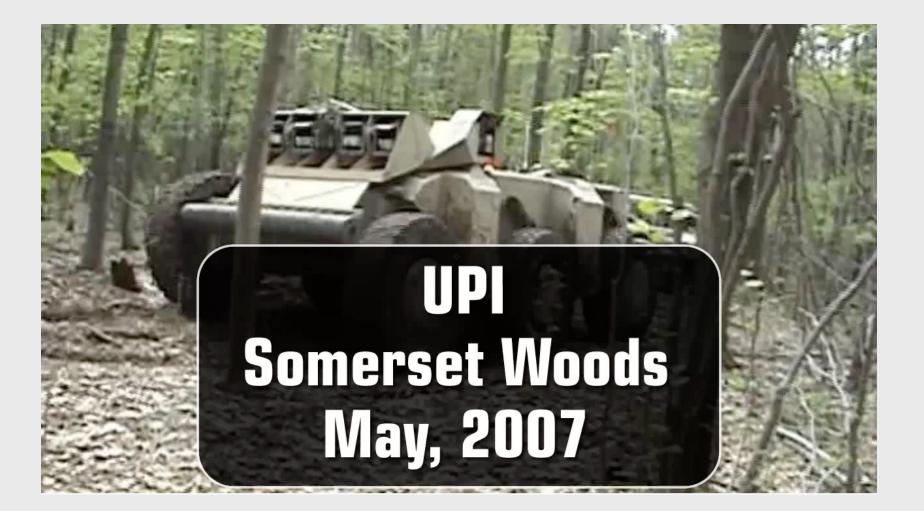
POMDPs

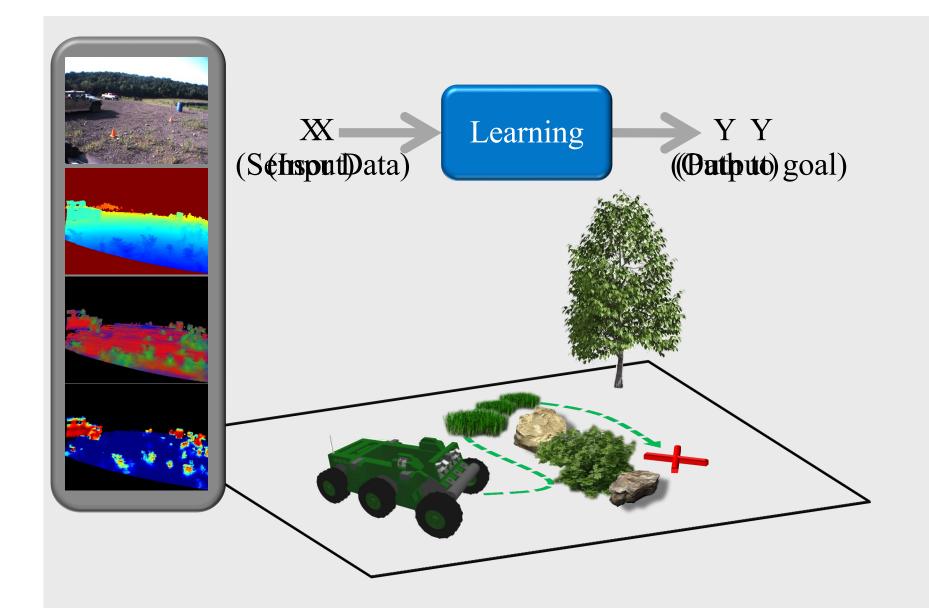
- In POMDPs we apply the very same idea as in MDPs.
- Since the state is not observable, the agent has to make its decisions based on the belief state which is a posterior distribution over states.
- For finite horizon problems, the resulting value functions are piecewise linear and convex.
- In each iteration the **number of linear constraints grows exponentially**.
- Full fledged POMDPs have only been applied to very small state spaces with small numbers of possible observations and actions.
- Approximate solutions are becoming more and more capable.

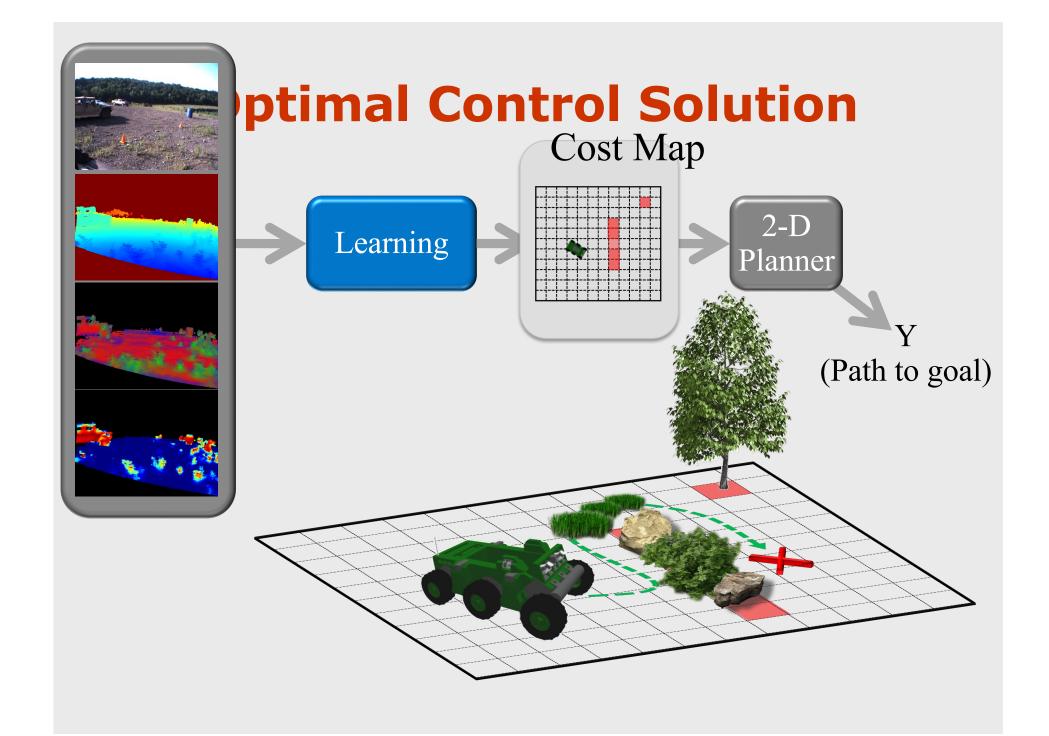
CSE 571 Inverse Optimal Control (Inverse Reinforcement Learning)

Many slides by Drew Bagnell Carnegie Mellon University

Autonomous Navigation







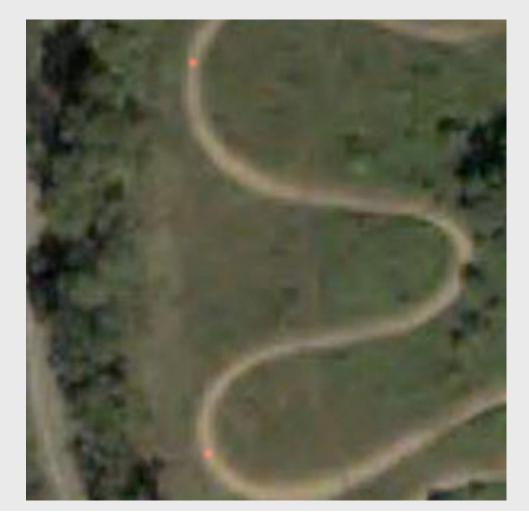
Mode 1: Training example



Mode 1: Training example



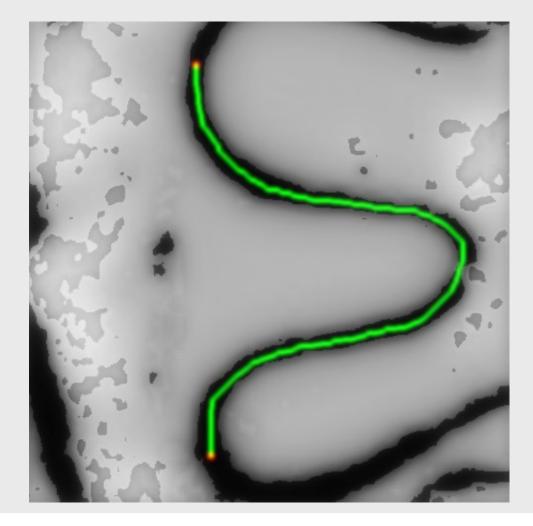
Mode 1: Learned behavior



Mode 1: Learned behavior



Mode 1: Learned cost map



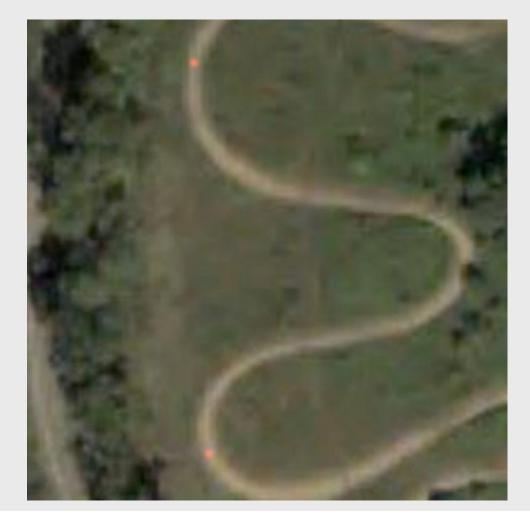
Mode 2: Training example



Mode 2: Training example



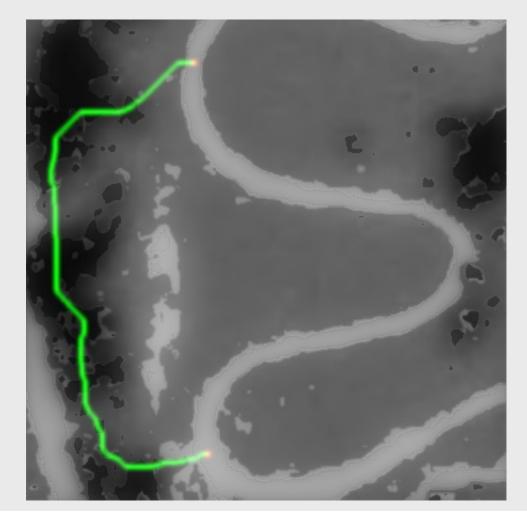
Mode 2: Learned behavior

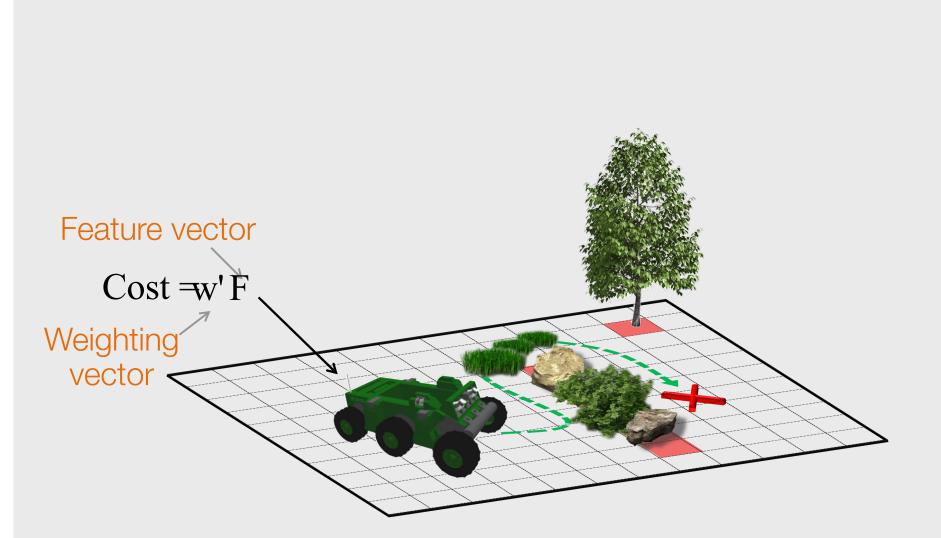


Mode 2: Learned behavior

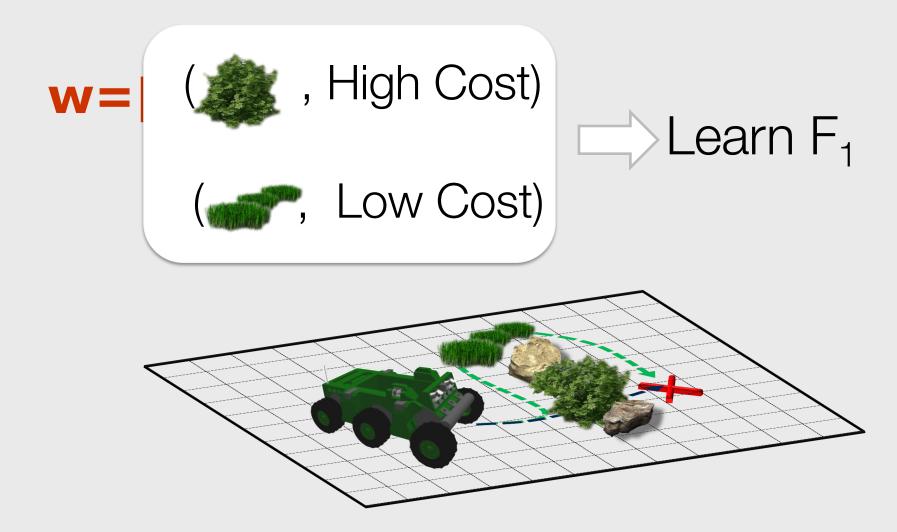


Mode 2: Learned cost map

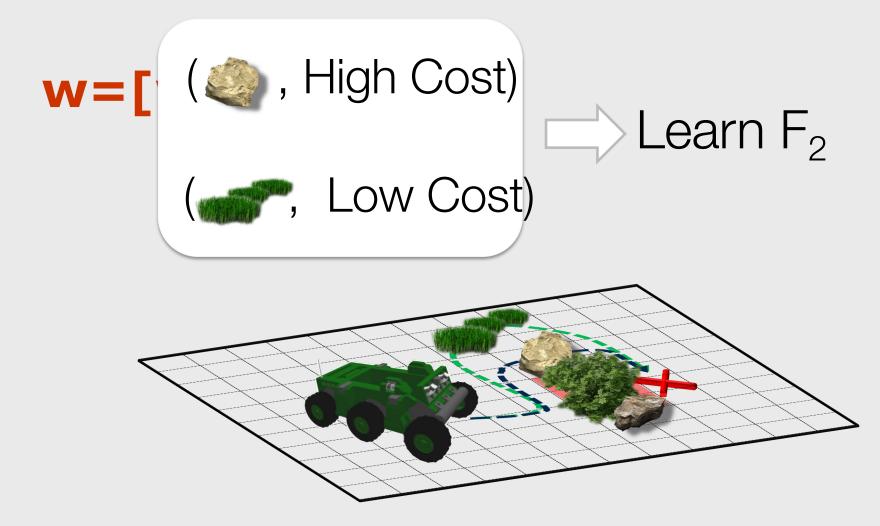




Ratliff, Bagnell, Zinkevich 2005 Ratliff, Bradley, Bagnell, Chestnutt, NIPS 2006 Silver, Bagnell, Stentz, RSS 2008



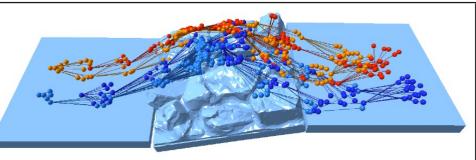
Ratliff, Bagnell, Zinkevich, ICML 2006 Ratliff, Bradley, Bagnell, Chestnutt, NIPS 2006 Silver, Bagnell, Stentz, RSS 2008



Ratliff, Bagnell, Zinkevich, ICML 2006 Ratliff, Bradley, Bagnell, Chestnutt, NIPS 2006 Silver, Bagnell, Stentz, RSS 2008

example path



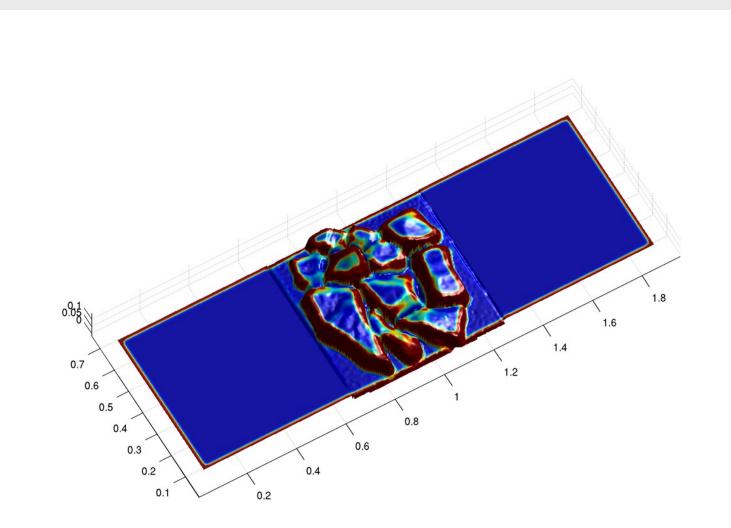




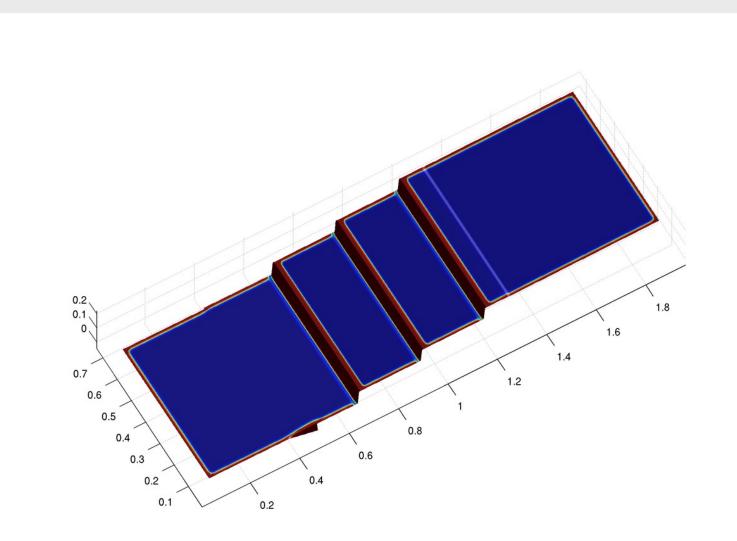
iff, Bradley, Che Bagnell 06

Zucker, Ratliff, Stolle, Chesnutt, Bagnell, Atkeson

Learned Cost Function Examples



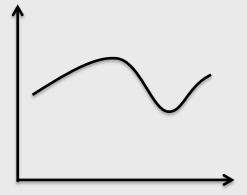
Learned Cost Function Examples



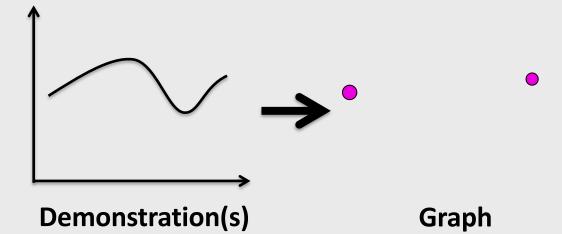
Learning Manipulation Preferences

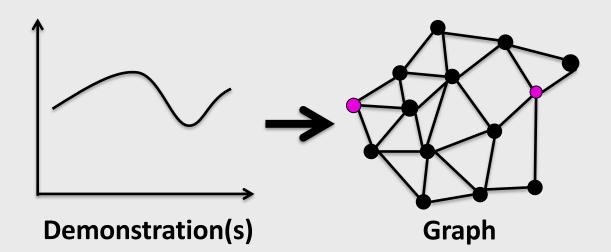
- Input: Human demonstrations of preferred behavior (e.g., moving a cup of water upright without spilling)
- Output: Learned cost function that results in trajectories satisfying user preferences

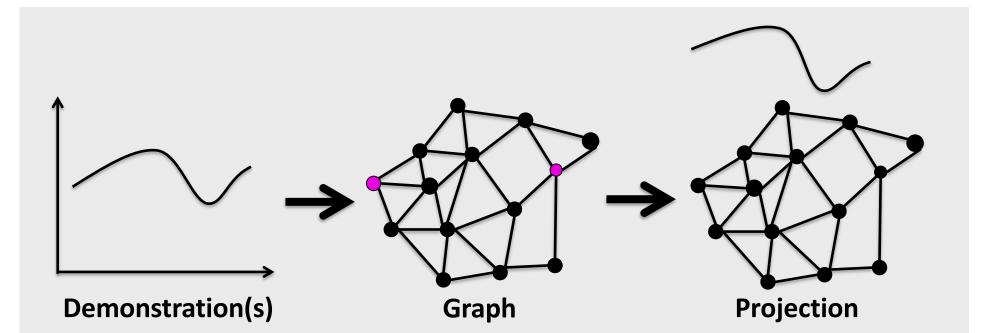


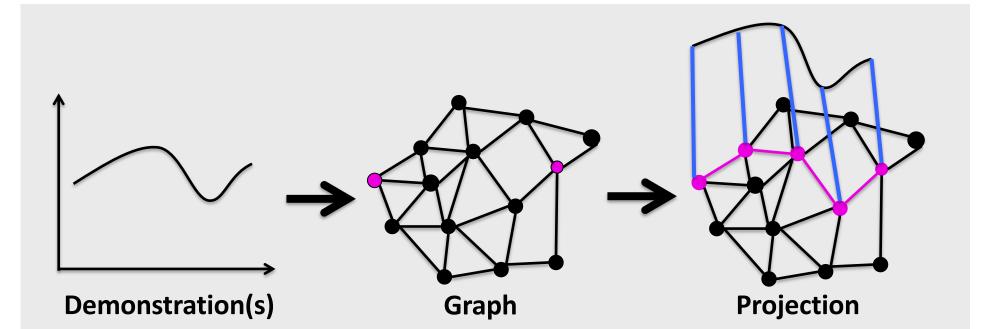


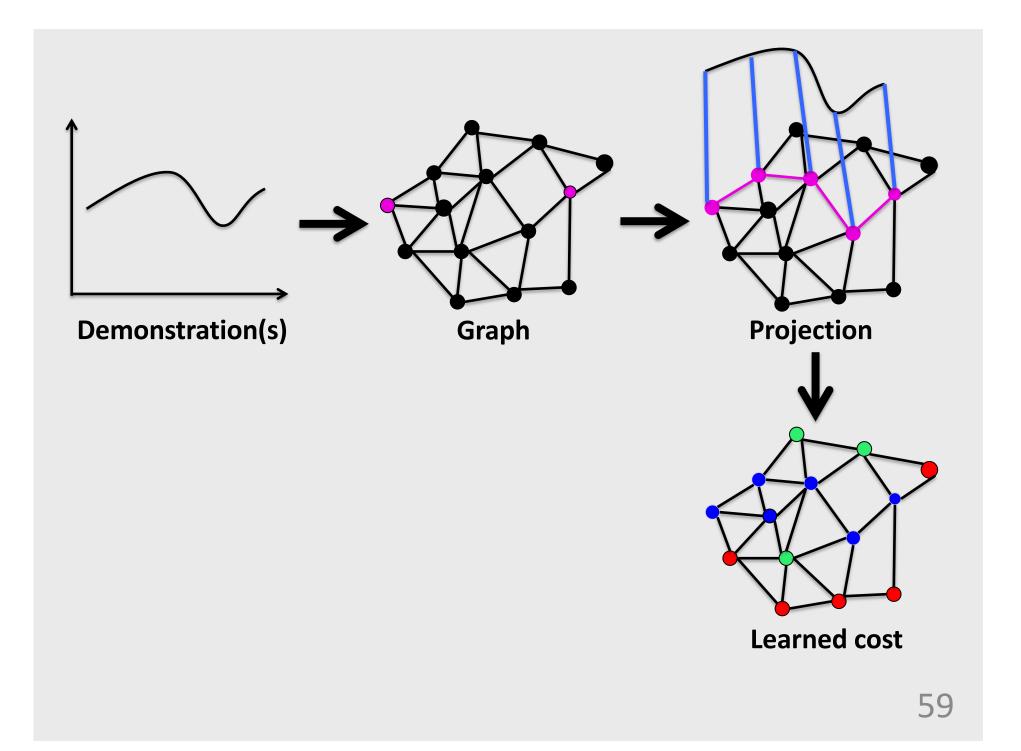
Demonstration(s)

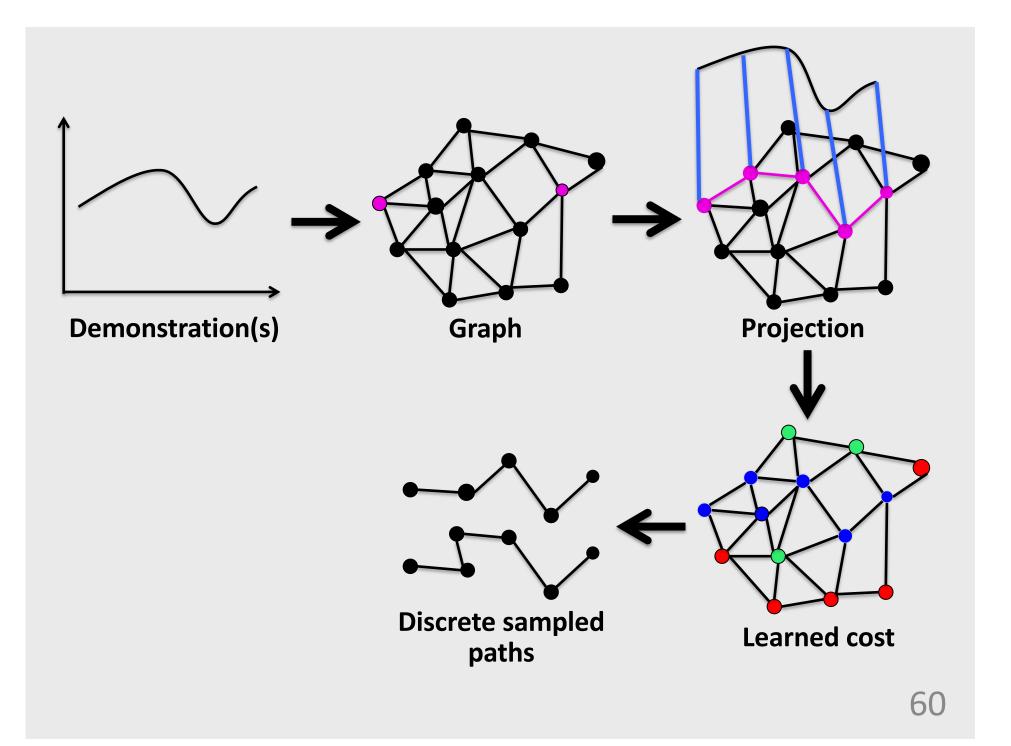


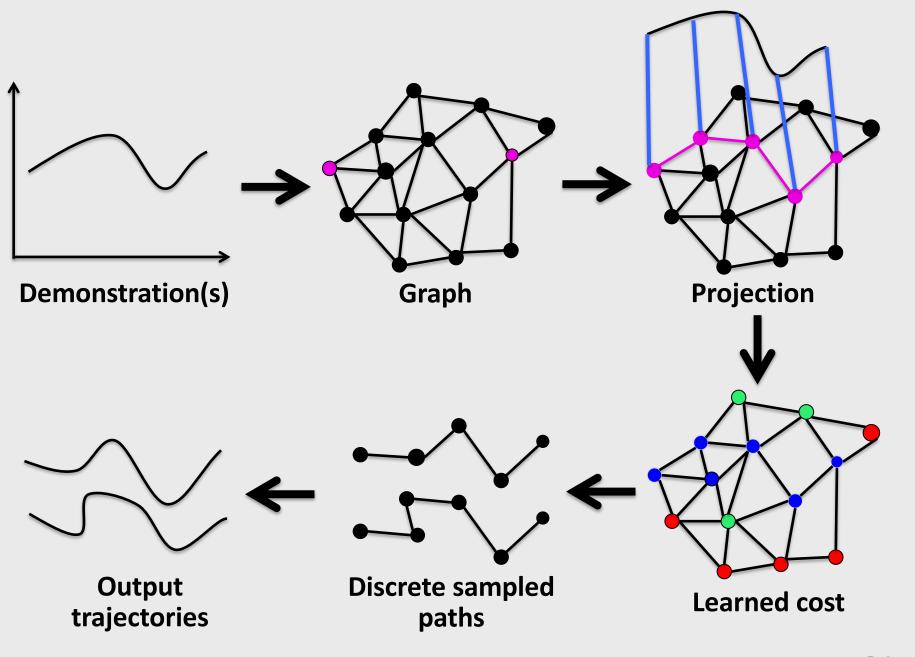


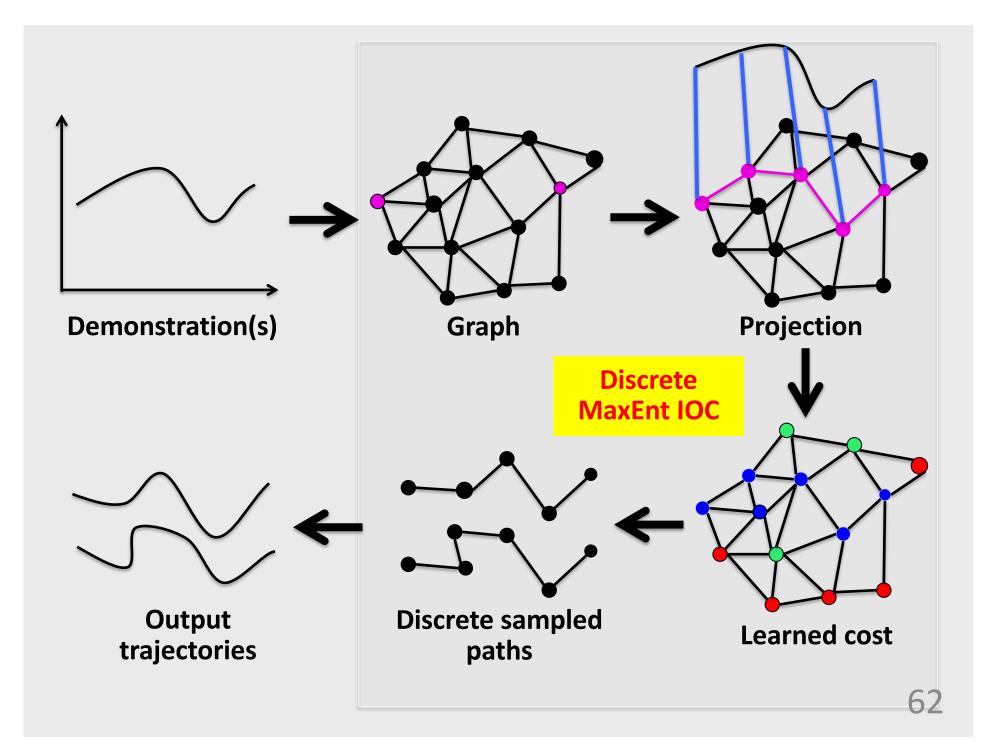


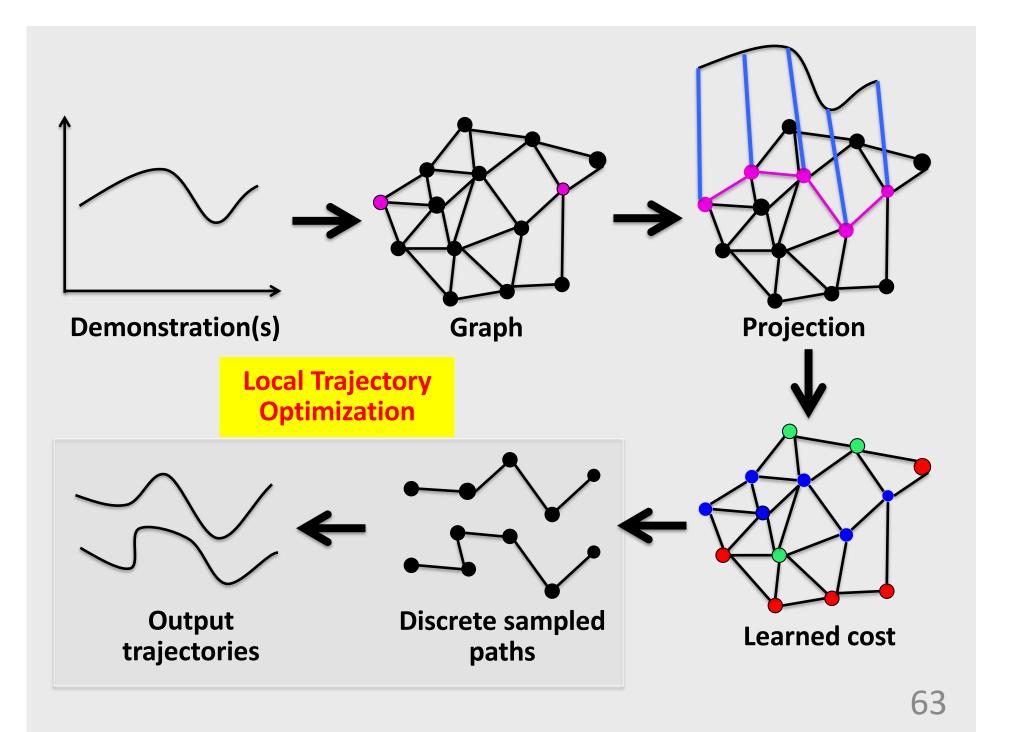












Setup

• **Binary** state-dependent features (~95)

- Histograms of distances to objects
- Histograms of end-effector orientation
- Object specific features (electronic vs nonelectronic)
- Approach direction w.r.t goal

• Task

 Hold cup upright while not moving above electronics

Laptop task: Demonstration (Not part of training set)



Laptop task: LTO + Smooth random path



Readings

- Max-Ent IRL (Ziebart, Bagnell): <u>http://www.cs.cmu.edu/~bziebart/</u>
- CIOC (Levine) <u>http://graphics.stanford.edu/projects/cioc/cioc.pdf</u>
- Manipulation (Byravan/Fox): <u>https://rse-</u> <u>lab.cs.washington.edu/papers/graph-based-IOC-</u> <u>ijcai-2015.pdf</u>
- Imitation learning (Ermon): <u>https://cs.stanford.edu/~ermon/</u>
- Human/manipulation (Dragan): <u>https://people.eecs.berkeley.edu/~anca/research.</u> <u>html</u>