

CSE 571 Probabilistic Robotics

Boosting

Some slides taken from: Wolfram Burgard, Hongbo Deng, Antonio Torralba

Why boosting?

- A simple algorithm for learning robust classifiers
 - Freund & Shapire, 1995
 - Friedman, Hastie, Tibshirani, 1998
- Provides efficient algorithm for sparse feature selection
 - Tieu & Viola, 2000
 - Viola & Jones, 2003
- Easy to implement, doesn't require external optimization tools.

Motivation

- Indoor mapping is an important task in mobile robotics.



Motivation

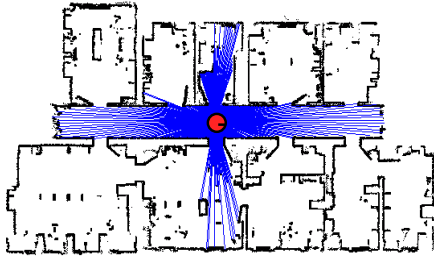
- Semantic mapping:



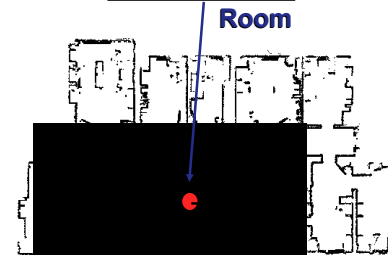
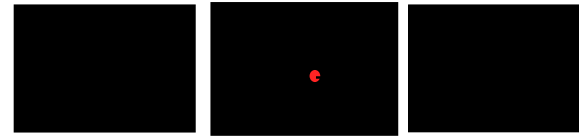
- Human-Robot interaction:
User: "Go to the corridor"

Goal

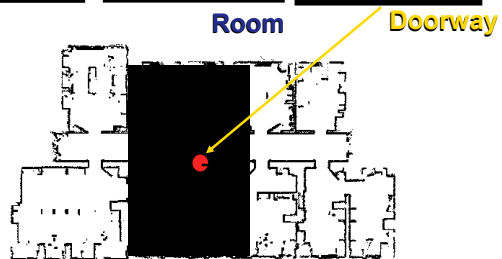
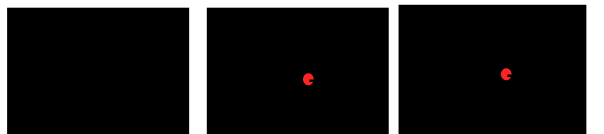
- Classification of the position of the robot using **one single observation**: a 360° laser range data.



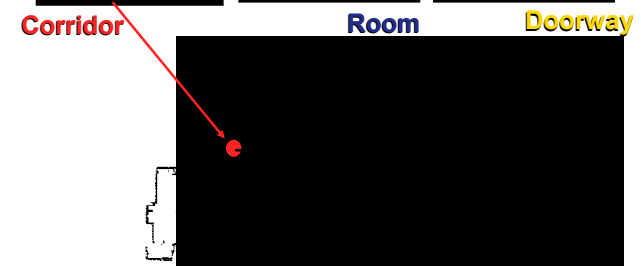
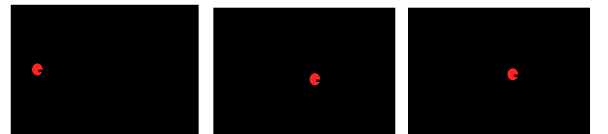
Observations



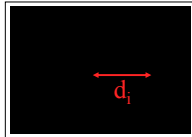
Observations



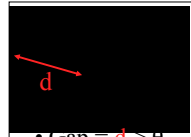
Observations



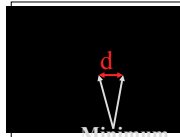
Simple Features



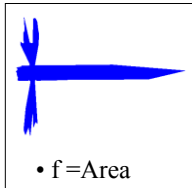
$$\bullet f = \frac{1}{N} \sum d_i$$



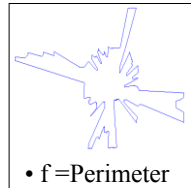
- Gap = $d > \theta$
- $f = \# \text{ Gaps}$



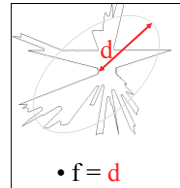
$$\bullet f = d$$



$$\bullet f = \text{Area}$$



$$\bullet f = \text{Perimeter}$$

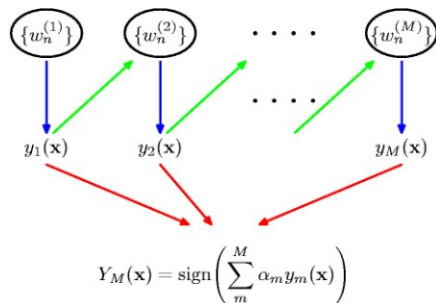


$$\bullet f = d$$

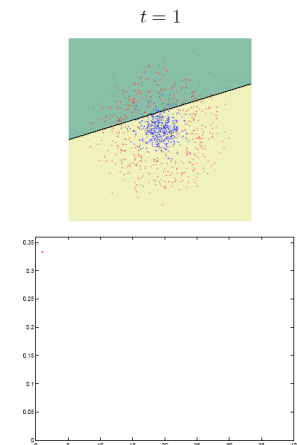
Combining Features

- **Observation:**
There are many simple features f_i .
- **Problem:**
Each single feature f_i gives poor classification rates.
- **Solution:**
Combine multiple simple features to form a final classifier using **AdaBoost**.

Idea

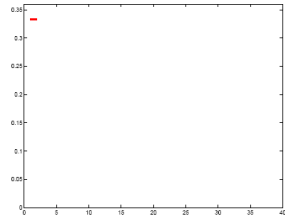
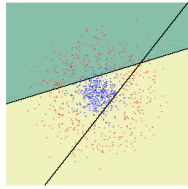


Example



Example

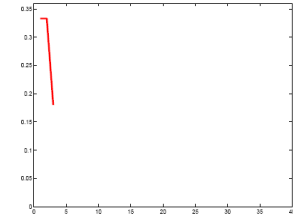
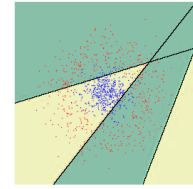
$t = 2$



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Example

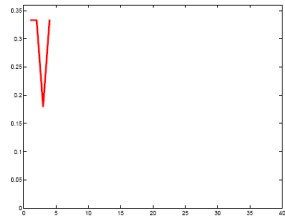
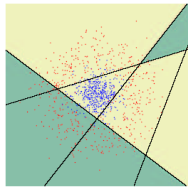
$t = 3$



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Example

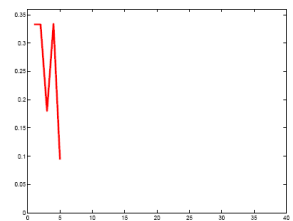
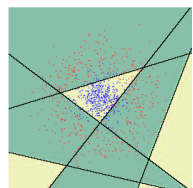
$t = 4$



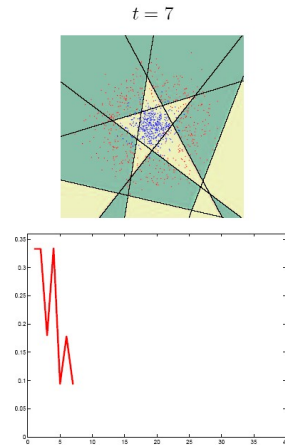
15

Example

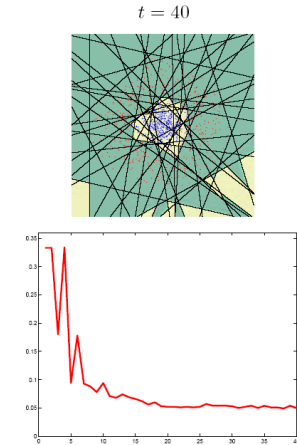
$t = 5$



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Example

17

Example

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AdaBoost Algorithm

1. Initialize data weights $w_n^{(1)} = 1/N$
2. For $m = 1, \dots, M$,
 - 2.1 Fit a classifier $y_m(x)$ by minimizing

$$J_m = \sum w_n^{(m)} I(y_m(\mathbf{x}_n) \neq t_n)$$
 - 2.2 Evaluate quantity ϵ_m (ratio of misclassified)

$$\epsilon_m = \frac{\sum_n w_n^{(m)} I(y_m(\mathbf{x}_n) \neq t_n)}{\sum_n w_n^{(m)}}$$
 Evaluate quantity α_m (weight for classifier m)

$$\alpha_m = \log\left(\frac{1-\epsilon_m}{\epsilon_m}\right)$$
 - 2.3 Update the data weighting coefficients

$$w_n^{(m+1)} = w_n^{(m)} e^{\alpha_m I(y_m(\mathbf{x}_n) \neq t_n)}$$
3. Make prediction by $Y_M(\mathbf{x}) = \text{sign}\left(\sum_{m=1}^M \alpha_m y_m(\mathbf{x})\right)$

Sequential Optimization

- Original motivation in learning theory
- Can be derived as sequential optimization of exponential error function

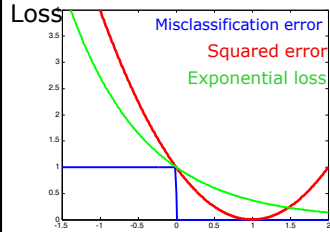
$$E = \sum_{n=1}^N \dots$$

with $n = \dots$

$$f_m(x) = \frac{1}{2} \sum_{l=1}^m \dots$$

- Fixing first $m-1$ classifiers and minimizing wrt m -th classifier gives AdaBoost equations!

Exponential loss



Squared error

$$J = \sum_{t=1}^N [y_t - F(x_t)]^2$$

Exponential loss

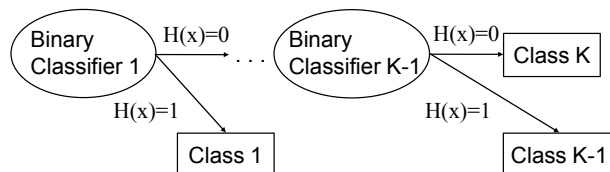
$$J = \sum_{t=1}^N e^{-y_t F(x_t)}$$

Further Observations

- Test error often decreases even when training error is already zero
- Many other boosting algorithms possible by changing error function
- Regression
- Multiclass

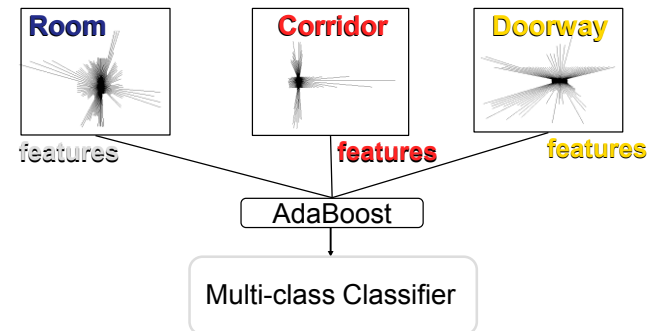
Multiple Classes

- Sequential AdaBoost for K different classes.



Summary of the Approach (1)

- **Training:** learn a strong classifier using previously labeled observations:

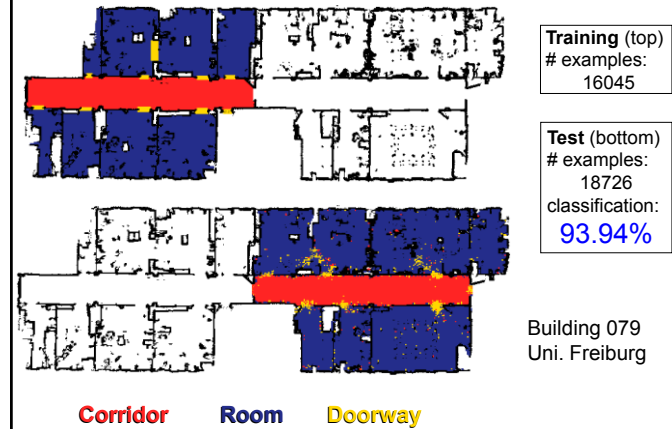


Summary of the Approach (2)

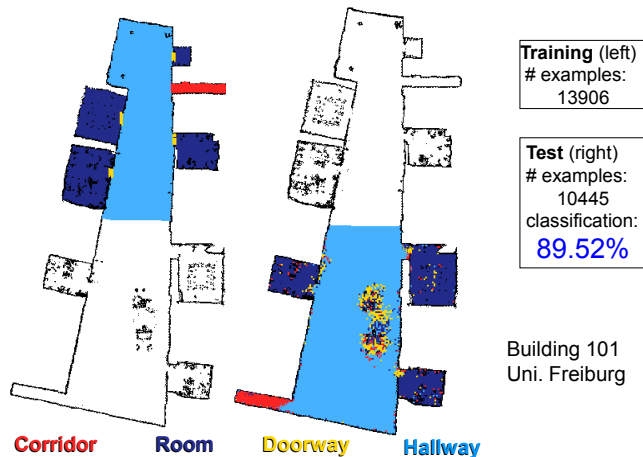
- **Test:** using the classifier to classify new observations:



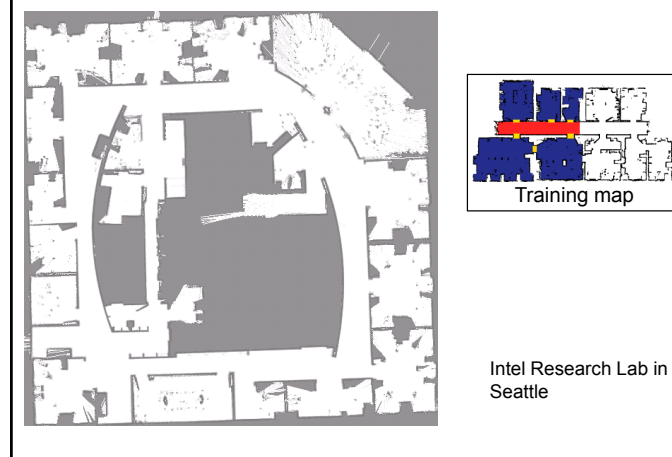
Experiments

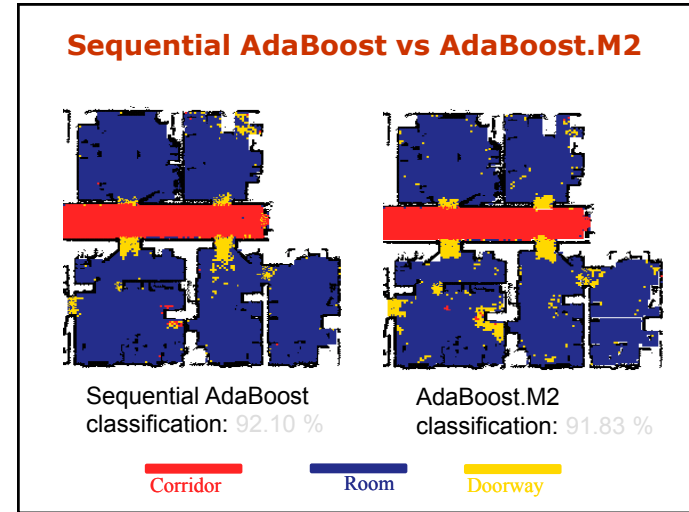
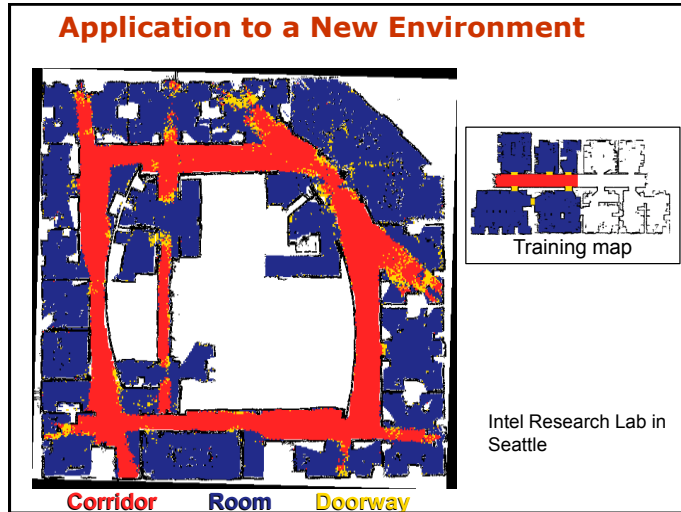


Experiments



Application to a New Environment





Boosting

- Extremely flexible framework
- Handles high-dimensional continuous data
- Easy to implement
- Limitation:
 - Only models local classification problems