

## Hierarchical Modeling

Brian Curless  
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## Reading

Optional:

- Angel, sections 8.1 – 8.6, 8.8

Further reading:

- *OpenGL Programming Guide*, chapter 3

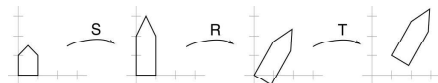
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## Symbols and instances

Most graphics APIs support a few geometric **primitives**:

- spheres
- cubes
- cylinders

These symbols are **instanced** using an **instance transformation**.



**Q:** What is the matrix for the instance transformation above?

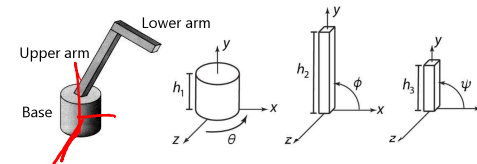
TRS

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## 3D Example: A robot arm

Let's build a robot arm out of a cylinder and two cuboids, with the following 3 degrees of freedom:

- Base rotates about its vertical axis by  $\theta$
- Upper arm rotates in its  $xy$ -plane by  $\phi$
- Lower arm rotates in its  $xy$ -plane by  $\psi$



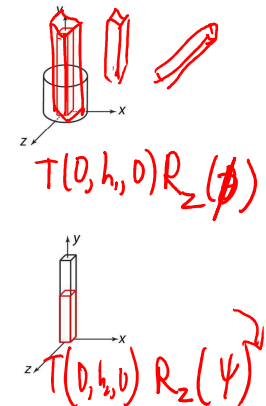
[Angel, 2011]

(Note that the angles are set to zero in the figures on the right; i.e., the parts are shown in their "default" positions.)

Suppose we have transformations  $R_x(\cdot)$ ,  $R_y(\cdot)$ ,  $R_z(\cdot)$ ,  $T(\cdot, \cdot, \cdot)$ .

**Q:** What matrix do we use to transform the base?

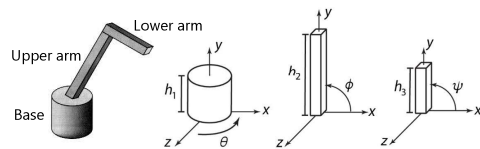
**Q:** What matrix product for the upper arm?



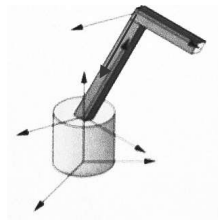
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### 3D Example: A robot arm

An alternative interpretation is that we are taking the original coordinate frames...

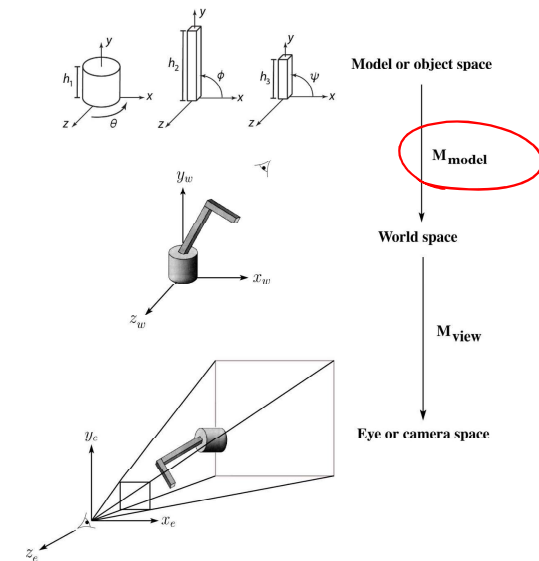


...and translating and rotating them into place:



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### From parts to model to viewer



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### Robot arm implementation

The robot arm can be displayed by keeping a global matrix and computing it at each step:

Matrix M, M\_model, M\_view;

```
main()
{
    . . .
    M_view = compute_view_transform();
    robot_arm();
    . . .
}
```

```
robot_arm()
{
    M_model = R_y(theta);
    M = M_view * M_model;
    base();
    M_model = R_y(theta) * T(0, h1, 0) * R_z(phi);
    M = M_view * M_model;
    upper_arm();
    M_model = R_y(theta) * T(0, h1, 0) * R_z(phi) * T(0, h2, 0) * R_z(psi);
    M = M_view * M_model;
    lower_arm();
}
```

*Transform for base*

*UA*

*LA*

Do the matrix computations seem wasteful?

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### Robot arm implementation, better

Instead of recalculating the global matrix each time, we can just update it *in place* by concatenating matrices on the right:

Matrix M\_modelview;

```
main()
{
    . . .
    M_modelview = compute_view_transform();
    robot_arm();
    . . .
}
```

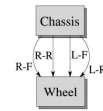
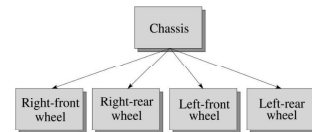
```
robot_arm()
{
    M_modelview *= R_y(theta);
    base();
    M_modelview *= T(0, h1, 0) * R_z(phi);
    upper_arm();
    M_modelview *= T(0, h2, 0) * R_z(psi);
    lower_arm();
}
```

*M<sub>mv</sub> TR<sub>2</sub>*

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## Hierarchical modeling

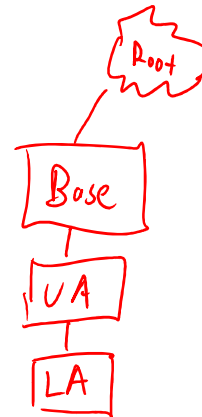
Hierarchical models can be composed of instances using trees or DAGs:



- edges contain geometric transformations
- nodes contain geometry (and possibly drawing attributes)

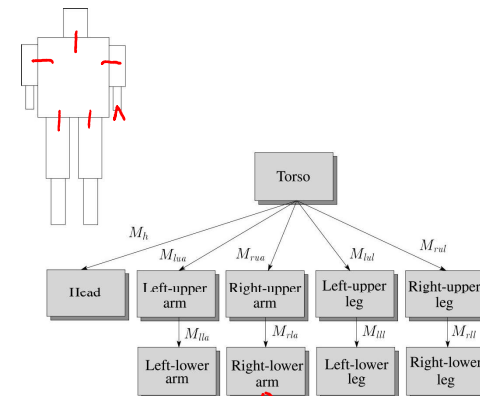
We will use trees for hierarchical models.

How might we draw the tree for the robot arm?



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## A complex example: human figure



Q: What's the most sensible way to traverse this tree?

*Depth first*

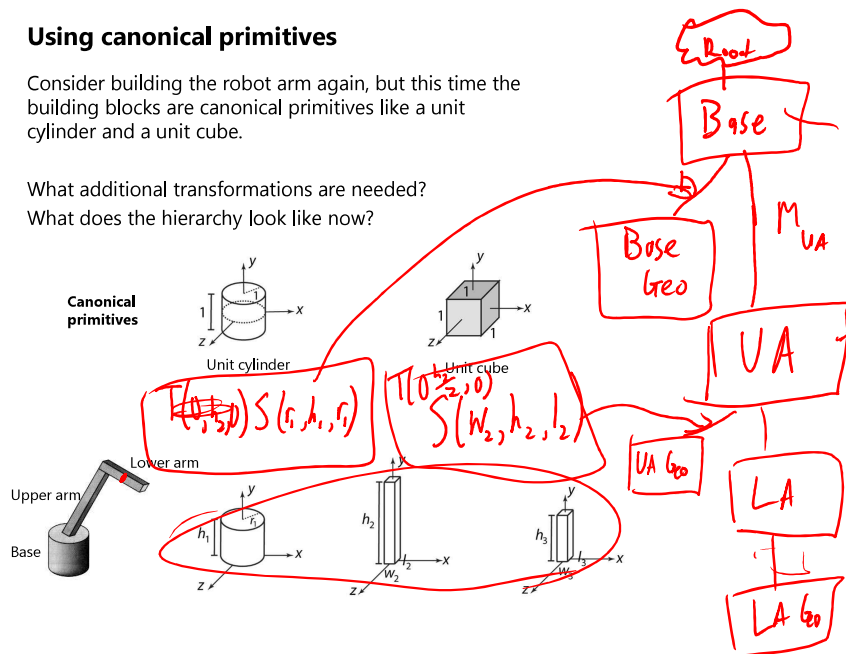
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## Using canonical primitives

Consider building the robot arm again, but this time the building blocks are canonical primitives like a unit cylinder and a unit cube.

What additional transformations are needed?

What does the hierarchy look like now?



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## Animation

The above examples are called **articulated models**:

- rigid parts
- connected by joints

They can be animated by specifying the joint angles (or other display parameters) as functions of time.

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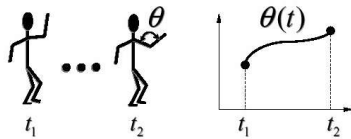
## Key-frame animation

The most common method for character animation in production is **key-frame animation**.

- ♦ Each joint specified at various **key frames** (not necessarily the same as other joints)
- ♦ System does interpolation or **in-betweening**

Doing this well requires:

- ♦ A way of smoothly interpolating key frames: **splines**
- ♦ A good interactive system
- ♦ A lot of skill on the part of the animator



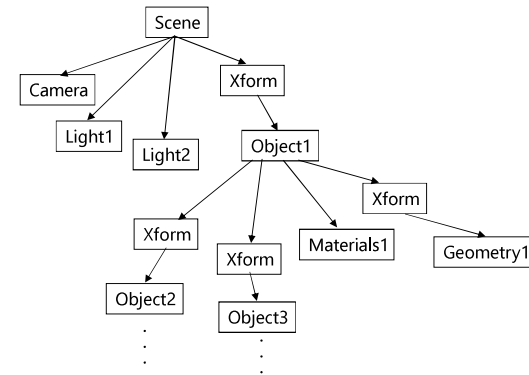
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## Scene graphs

The idea of hierarchical modeling can be extended to an entire scene, encompassing:

- ♦ many different objects
- ♦ lights
- ♦ camera position

This is called a **scene tree** or **scene graph**.



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## Summary

Here's what you should take home from this lecture:

- ♦ All the **boldfaced terms**.
- ♦ How primitives can be instanced and composed to create hierarchical models using geometric transforms.
- ♦ How the notion of a model tree or DAG can be extended to entire scenes.
- ♦ How OpenGL transformations can be used in hierarchical modeling.
- ♦ How keyframe animation works.

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