

## Shading

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## Reading

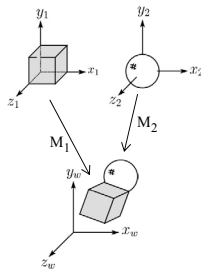
Required:

- ♦ Shirley, Chapter 10

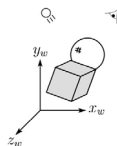
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## Basic 3D graphics

With affine matrices, we can now transform virtual 3D objects in their local coordinate systems into a global (world) coordinate system:



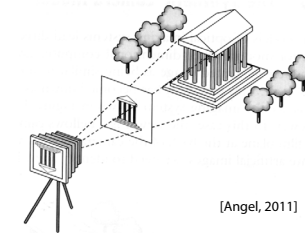
To synthesize an image of the scene, we also need to add light sources and a viewer/camera:



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## Pinhole camera

To create an image of a virtual scene, we need to define a camera, and we need to model lighting and shading. For the camera, we use a **pinhole camera**.



The image is rendered onto an **image plane** (usually in front of the camera).

Viewing rays emanate from the **center of projection** (COP) at the center of the pinhole.

The image of an object point **P** is at the intersection of the viewing ray through **P** and the image plane.

But is P visible? This is the problem of **hidden surface removal** (a.k.a., **visible surface determination**). We'll consider this problem later.

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## Shading

Next, we'll need a model to describe how light interacts with surfaces.

Such a model is called a **shading model**.

Other names:

- ♦ Lighting model
- ♦ Light reflection model
- ♦ Local illumination model
- ♦ Reflectance model
- ♦ BRDF

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## An abundance of photons

Given the camera and shading model, properly determining the right color at each pixel is *extremely hard*.

Look around the room. Each light source has different characteristics. Trillions of photons are pouring out every second.

These photons can:

- ♦ interact with molecules and particles in the air ("participating media")
- ♦ strike a surface and
  - be absorbed
  - be reflected (scattered)
  - cause fluorescence or phosphorescence.
- ♦ interact in a wavelength-dependent manner
- ♦ generally bounce around and around

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## Our problem

We're going to build up to a *approximations* of reality called the **Phong and Blinn-Phong illumination models**.

They have the following characteristics:

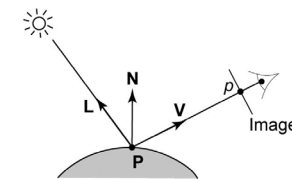
- ♦ *not* physically correct
- ♦ gives a "first-order" *approximation* to physical light reflection
- ♦ very fast
- ♦ widely used

In addition, we will assume **local illumination**, i.e., light goes: light source -> surface -> viewer.

No interreflections, no shadows.

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## Setup...



Given:

- ♦ a point **P** on a surface visible through pixel  $p$
- ♦ The normal **N** at **P**
- ♦ The lighting direction, **L**, and (color) intensity,  $I_L$ , at **P**
- ♦ The viewing direction, **V**, at **P**
- ♦ The shading coefficients at **P**

Compute the color,  $I$ , of pixel  $p$ .

Assume that the direction vectors are normalized:

$$\|\mathbf{N}\| = \|\mathbf{L}\| = \|\mathbf{V}\| = 1$$

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## “Iteration zero”

The simplest thing you can do is...

Assign each polygon a single color:

$$I = k_e$$

where

- ♦  $I$  is the resulting intensity
- ♦  $k_e$  is the **emissivity** or intrinsic shade associated with the object

This has some special-purpose uses, but not really good for drawing a scene.

[Note:  $k_e$  is omitted in Shirley.]

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## “Iteration one”

Let’s make the color at least dependent on the overall quantity of light available in the scene:

$$I = k_a + k_d I_{La}$$

- ♦  $k_a$  is the **ambient reflection coefficient**.
  - really the reflectance of ambient light
  - “ambient” light is assumed to be equal in all directions
- ♦  $I_{La}$  is the **ambient light intensity**.

Physically, what is “ambient” light?

[Note: Shirley uses  $c_a$  instead of  $I_{La}$ .]

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## Wavelength dependence

Really,  $k_a$ ,  $k_d$ , and  $I_{La}$  are functions over all wavelengths  $\lambda$ .

Ideally, we would do the calculation on these functions. For the ambient shading equation, we would start with:

$$I(\lambda) = k_a(\lambda) I_{La}(\lambda)$$

then we would find good RGB values to represent the spectrum  $I(\lambda)$ .

Traditionally, though,  $k_a$  and  $I_{La}$  are represented as RGB triples, and the computation is performed on each color channel separately:

$$\begin{aligned} I^R &= k_a^R I_{La}^R \\ I^G &= k_a^G I_{La}^G \\ I^B &= k_a^B I_{La}^B \end{aligned}$$

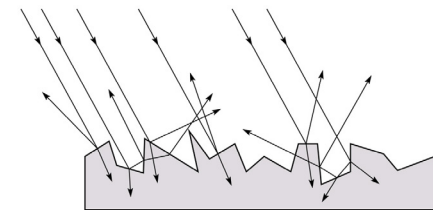
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## Diffuse reflectors

Diffuse reflection occurs from dull, matte surfaces, like latex paint, or chalk.

These **diffuse** or **Lambertian** reflectors reradiate light equally in all directions.

Picture a rough surface with lots of tiny **microfacets**.



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## Diffuse reflection

Let's examine the ambient shading model:

- ♦ objects have different colors
- ♦ we can control the overall light intensity
  - what happens when we turn off the lights?
  - what happens as the light intensity increases?
  - what happens if we change the color of the lights?

So far, objects are uniformly lit.

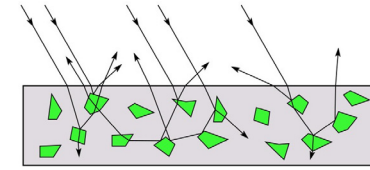
- ♦ not the way things really appear
- ♦ in reality, light sources are localized in position or direction

**Diffuse**, or **Lambertian** reflection will allow reflected intensity to vary with the direction of the light.

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## Diffuse reflectors

...or picture a surface with little pigment particles embedded beneath the surface (neglect reflection at the surface for the moment):



The microfacets and pigments distribute light rays in all directions.

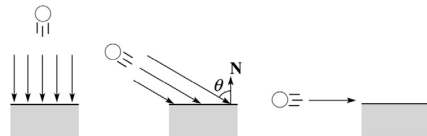
Embedded pigments are responsible for the coloration of diffusely reflected light in plastics and paints.

Note: the figures above are intuitive, but not strictly (physically) correct.

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## Diffuse reflectors, cont.

The reflected intensity from a diffuse surface does not depend on the direction of the viewer. The incoming light, though, does depend on the direction of the light source:



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## "Iteration two"

The incoming energy is proportional to \_\_\_\_\_, giving the diffuse reflection equations:

$$I = k_e + k_a I_{La} + k_d I_L B \text{ _____}$$

$$= k_e + k_a I_{La} + k_d I_L B( \quad )$$

where:

- ♦  $k_d$  is the **diffuse reflection coefficient**
- ♦  $I_L$  is the (color) intensity of the light source
- ♦  $\mathbf{N}$  is the normal to the surface (unit vector)
- ♦  $\mathbf{L}$  is the direction to the light source (unit vector)
- ♦  $B$  prevents contribution of light from below the surface:

$$B = \begin{cases} 1 & \text{if } \mathbf{N} \cdot \mathbf{L} > 0 \\ 0 & \text{if } \mathbf{N} \cdot \mathbf{L} \leq 0 \end{cases}$$

[Note: Shirley uses  $c_r$  and  $c_l$  instead of  $k_d$  and  $L$ .]

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## Specular reflection

**Specular reflection** accounts for the highlight that you see on some objects.

It is particularly important for *smooth, shiny* surfaces, such as:

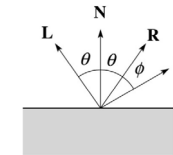
- ♦ metal
- ♦ polished stone
- ♦ plastics
- ♦ apples
- ♦ skin

Properties:

- ♦ Specular reflection depends on the viewing direction  $\mathbf{V}$ .
- ♦ For non-metals, the color is determined solely by the color of the light.
- ♦ For metals, the color may be altered (e.g., brass)

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## Specular reflection “derivation”



For a perfect mirror reflector, light is reflected about  $\mathbf{N}$ , so

$$I = \begin{cases} I_L & \text{if } \mathbf{V} = \mathbf{R} \\ 0 & \text{otherwise} \end{cases}$$

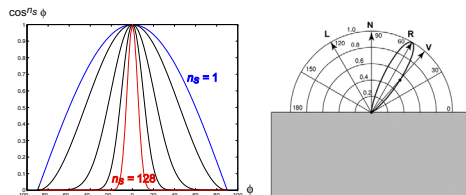
For a near-perfect reflector, you might expect the highlight to fall off quickly with increasing angle  $\phi$ .

Also known as:

- ♦ “**rough specular**” reflection
- ♦ “**directional diffuse**” reflection
- ♦ “**glossy**” reflection

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## Phong specular reflection



One way to get this effect is to take  $(\mathbf{R} \cdot \mathbf{V})$ , raised to a power  $n_s$ .

As  $n_s$  gets larger,

- ♦ the dropoff becomes {more,less} gradual
- ♦ gives a {larger,smaller} highlight
- ♦ simulates a {more,less} mirror-like surface

Phong specular reflection is proportional to:

$$I_{\text{specular}} \sim B(\mathbf{R} \cdot \mathbf{V})_+^{n_s}$$

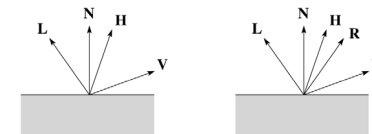
where  $(x)_+ \equiv \max(0, x)$ .

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## Blinn-Phong specular reflection

A common alternative for specular reflection is the **Blinn-Phong model** (sometimes called the **modified Phong model**.)

We compute the vector halfway between  $\mathbf{L}$  and  $\mathbf{V}$  as:



Analogous to Phong specular reflection, we can compute the specular contribution in terms of  $(\mathbf{N} \cdot \mathbf{H})$ , raised to a power  $n_s$ :

$$I_{\text{specular}} = B(\mathbf{N} \cdot \mathbf{H})_+^{n_s}$$

where, again,  $(x)_+ \equiv \max(0, x)$ .

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## “Iteration three”

The next update to the Blinn-Phong shading model is then:

$$I = k_e + k_a I_{La} + k_d I_L B(\mathbf{N} \cdot \mathbf{L}) + k_s I_L B(\mathbf{N} \cdot \mathbf{H})^{n_s}$$

$$= k_e + k_a I_{La} + I_L B \left[ k_d (\mathbf{N} \cdot \mathbf{L}) + k_s (\mathbf{N} \cdot \mathbf{H})^{n_s} \right]$$

where:

- $k_s$  is the **specular reflection coefficient**
- $n_s$  is the **specular exponent** or **shininess**
- $\mathbf{H}$  is the unit halfway vector between  $\mathbf{L}$  and  $\mathbf{V}$ , where  $\mathbf{V}$  is the viewing direction, and:

$$(\mathbf{N} \cdot \mathbf{H})^{n_s} = \begin{cases} (\mathbf{N} \cdot \mathbf{H})^{n_s} & \text{if } \mathbf{N} \cdot \mathbf{H} > 0 \\ 0 & \text{if } \mathbf{N} \cdot \mathbf{H} \leq 0 \end{cases}$$

[Note: Shirley uses  $\mathbf{e}$ ,  $\mathbf{r}$ ,  $\mathbf{h}$ , and  $\rho$  instead of  $\mathbf{V}$ ,  $\mathbf{R}$ ,  $\mathbf{H}$ , and  $n_s$ ]

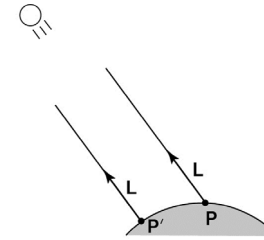
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## Directional lights

The simplest form of lights supported by renderers are ambient, directional, and point. Spotlights are also supported often as a special form of point light.

We’ve seen ambient light sources, which are not really geometric.

**Directional light** sources have a single direction and intensity associated with them.

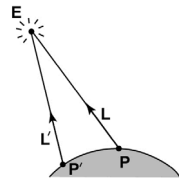


Using affine notation, what is the homogeneous coordinate for a directional light?

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## Point lights

The direction of a **point light** sources is determined by the vector from the light position to the surface point.



Physics tells us the intensity must drop off inversely with the square of the distance:

$$f_{\text{atten}} = \frac{1}{r^2}$$

Sometimes, this distance-squared dropoff is considered too “harsh.” A common alternative is:

$$f_{\text{atten}} = \frac{1}{a + br + cr^2}$$

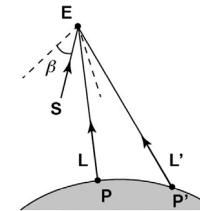
with user-supplied constants for  $a$ ,  $b$ , and  $c$ .

Using affine notation, what is the homogeneous coordinate for a point light?

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## Spotlights

We can also apply a *directional attenuation* of a point light source, giving a **spotlight** effect.



A common choice for the spotlight intensity is:

$$f_{\text{spot}} = \begin{cases} \frac{(\mathbf{L} \cdot \mathbf{S})^e}{a + br + cr^2} & \text{if } \mathbf{L} \cdot \mathbf{S} \leq \cos \beta \\ 0 & \text{otherwise} \end{cases}$$

where

- $\mathbf{L}$  is the direction to the point light.
- $\mathbf{S}$  is the center direction of the spotlight.
- $b$  is the cutoff angle for the spotlight
- $e$  is the angular falloff coefficient

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## “Iteration four”

Since light is additive, we can handle multiple lights by taking the sum over every light.

Our equation is now:

$$I = k_e + k_d I_{La} + \sum_j \frac{(\mathbf{L}_j \cdot \mathbf{S}_j)^{e_j}}{a_j + b_j r_j + c_j r_j^2} I_{L_j} B_j \left[ k_d (\mathbf{N} \cdot \mathbf{L}_j) + k_s (\mathbf{N} \cdot \mathbf{H}_j)^{n_s} \right]$$

This is the Blinn-Phong illumination model (for spotlights).

Which quantities are spatial vectors?

Which are RGB triples?

Which are scalars?

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## Choosing the parameters

Experiment with different parameter settings. To get you started, here are a few suggestions:

- Try  $n_s$  in the range [0,100]
- Try  $k_d + k_s < 1$
- Use a small  $k_d$  (~0.1)

|         | $n_s$  | $k_d$                    | $k_s$                 |
|---------|--------|--------------------------|-----------------------|
| Metal   | large  | Small, color of metal    | Large, color of metal |
| Plastic | medium | Medium, color of plastic | Medium, white         |
| Planet  | 0      | varying                  | 0                     |

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## BRDF

The diffuse+specular parts of the Blinn-Phong illumination model are a mapping from light to viewing directions:

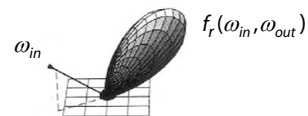
$$I = I_L B \left[ k_d (\mathbf{N} \cdot \mathbf{L}) + k_s \mathbf{N} \cdot \left( \frac{\mathbf{L} + \mathbf{V}}{\|\mathbf{L} + \mathbf{V}\|} \right)^{n_s} \right] = I_L f_r(\mathbf{L}, \mathbf{V})$$

The mapping function  $f_r$  is often written in terms of incoming (light) directions  $\omega_{in}$  and outgoing (viewing) directions  $\omega_{out}$ :

$$f_r(\omega_{in}, \omega_{out}) \quad \text{or} \quad f_r(\omega_{in} \rightarrow \omega_{out})$$

This function is called the **Bi-directional Reflectance Distribution Function (BRDF)**.

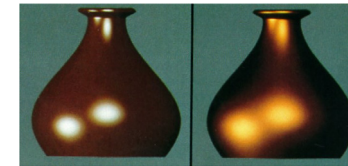
Here's a plot with  $\omega_{in}$  held constant:



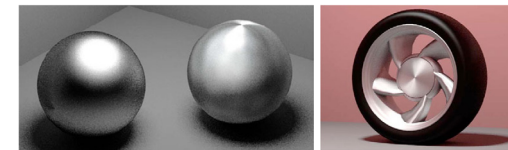
BRDF's can be quite sophisticated...

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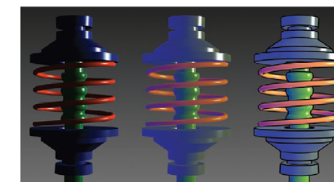
## More sophisticated BRDF's



[Cook and Torrance, 1982]



Anisotropic BRDFs [Westin, Arvo, Torrance 1992]



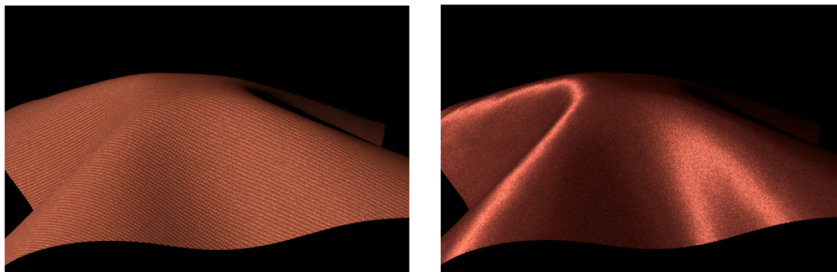
Artistics BRDFs [Gooch]

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### More sophisticated BRDF's (cont'd)



Hair illuminated from different angles [Marschner et al., 2003]



Wool and silk cloths [Irawan and Marschner, 2012]

### BSSRDFs for subsurface scattering



[Jensen et al. 2001]

### Shading the interiors of triangles

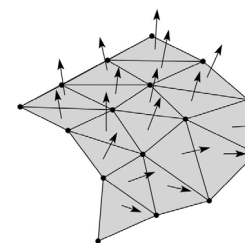
We will be computing colors using the Blinn-Phong lighting model.

Let's assume (as graphics hardware does) that we are working with triangles.

How should we shade the interiors of triangles?

### Shading with per-face normals

Assume each face has a constant normal:



For a distant viewer and a distant light source and constant material properties over the surface, how will the color of each triangle vary?



## Phong interpolation

To get smoother results, we can "hallucinate" normals that vary smoothly within a triangle, a process called **Phong interpolation**.

Here's how it works:

1. Compute normals at the vertices.
2. Interpolate normals and normalize.
3. Shade using the interpolated normals.

