

## Hidden Surfaces

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## Reading

- Foley *et al.*, Chapter 15

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## The Quest for 3D

- Construct a 3D hierarchical geometric model
- Define a virtual camera
- Map points in 3D space to points in an image
  
- produce a wireframe drawing in 2D from a 3D object
  
- Of course, there's more work to be done...

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## Introduction

- Not every part of every 3D object is visible to a particular viewer. We need an algorithm to determine what parts of each object should get drawn.
- Known as “hidden surface elimination” or “visible surface determination”.
- Hidden surface elimination algorithms can be categorized in three major ways:
  - Object space vs. image space
  - Object order vs. image order
  - Sort first vs. sort last

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## Object Space Algorithms

- Operate on geometric primitives
  - For each object in the scene, compute the part of it which isn't obscured by any other object, then draw.
  - Must perform tests at high precision
  - Resulting information is resolution-independent
- Complexity
  - Must compare every pair of objects, so  $O(n^2)$  for  $n$  objects
  - Optimizations can reduce this cost, but...
  - Best for scenes with few polygons or resolution-independent output
- Implementation
  - Difficult to implement!
  - Must carefully control numerical error

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## Image Space Algorithms

- Operate on pixels
  - For each pixel in the scene, find the object closest to the COP which intersects the projector through that pixel, then draw.
  - Perform tests at device resolution, result works only for that resolution
- Complexity
  - Must do something for every pixel in the scene, so at least  $O(R)$ .
  - Easiest solution is so test projector against every object, giving  $O(nR)$ .
  - More reasonable version only does work for pixels belonging to objects:  $O(nr)$ ,  $r$  is number of pixels per object
  - Often, with more objects, each is smaller, so we estimate  $nr = O(R)$  in practice
- Implementation
  - Usually very simple!

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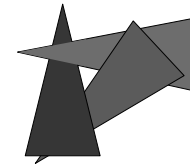
## Object Order vs. Image Order

- Object order
  - Consider each object only once - draw its pixels and move on to the next object
  - Might draw the same pixel multiple times
- Image order
  - Consider each pixel only once - draw part of an object and move on to the next pixel
  - Might compute relationships between objects multiple times

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## Sort First vs. Sort Last

- Sort first
  - Find some depth-based ordering of the objects relative to the camera, then draw from back to front
  - Build an ordered data structure to avoid duplicating work
- Sort last
  - Sort implicitly as more information becomes available



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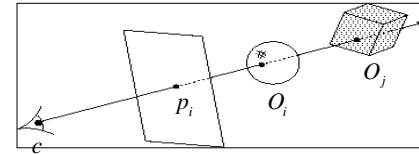
## Important Algorithms

- Ray casting
- Binary space partitioning
- Z-buffer
- Back face culling

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## Ray Casting

- Partition the projection plane into pixels to match screen resolution
- For each pixel  $p_i$ , construct ray from COP through PP at that pixel and into scene
- Intersect the ray with every object in the scene, colour the pixel according to the object with the closest intersection



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## Aside: Definitions

- An algorithm exhibits *coherence* if it uses knowledge about the continuity of the objects on which it operates
- An *online* algorithm is one that doesn't need all the data to be present when it starts running
  - Example: insertion sort

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## Ray Casting Analysis

### Categorization:

- Easy to implement?
- Hardware implementation?
- Coherence?
- Memory intensive?
- Pre-processing required?
- Online?
- Handles transparency?
- Handles refraction?
- Polygon-based?
- Extra work for moving objects?
- Extra work for moving viewer?
- Efficient shading?
- Handles cycles and self-intersections?

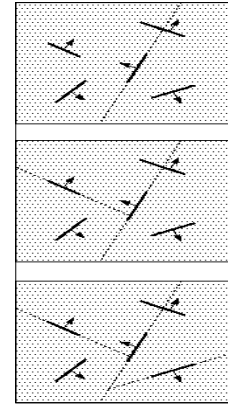
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## Binary Space Partitioning

- Goal: build a tree that captures some relative depth information between objects. Use it to draw objects in the right order.
  - Tree doesn't depend on camera position, so we can change viewpoint and redraw quickly
  - Called the binary space partitioning tree, or BSP tree
- Key observation: The polygons in the scene are painted in the correct order if for each polygon  $P$ ,
  - Polygons on the far side of  $P$  are painted first
  - $P$  is painted next
  - Polygons in front of  $P$  are painted last

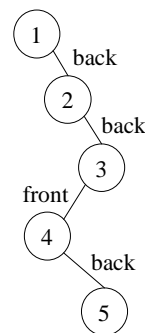
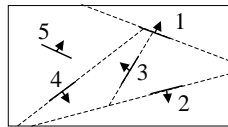
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## Building a BSP Tree (in 2D)



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## Alternate BSP Tree



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## BSP Tree Construction

```

BSPtree makeBSP( L: list of polygons )
{
    if L is empty
    {
        return the empty tree
    }

    Choose a polygon P from L to serve as root
    Split all polygons in L according to P
    return new TreeNode(
        P,
        makeBSP( polygons on negative side of P ),
        makeBSP( polygons on positive side of P ) )
}
    
```

- Splitting polygons is expensive! It helps to choose  $P$  wisely at each step.
  - Example: choose five candidates, keep the one that splits the fewest polygons

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## BST Tree Display

```
showBSP( v: Viewer, T: BSPtree )
{
    if T is empty then return

    P := root of T
    if viewer is in front of P
    {
        showBSP( back subtree of T )
        draw P
        showBSP( front subtree of T )
    } else {
        showBSP( front subtree of T )
        draw P
        showBSP( back subtree of T )
    }
}
```

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## Z-buffer

- Idea: along with a pixel's red, green and blue values, maintain some notion of its *depth*
  - An additional channel in memory, like alpha
  - Called the depth buffer or Z-buffer

```
void draw_mode_setup( void ) {
    ...
    glEnable( GL_DEPTH_TEST );
    ...
}
```

- When the time comes to draw a pixel, compare its depth with the depth of what's already in the framebuffer. Replace only if it's closer
- Very widely used
- History
  - Originally described as "brute-force image space algorithm"
  - Written off as impractical algorithm for huge memories
  - Today, done easily in hardware

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## Z-buffer Implementation

```
for each pixel pi
{
    Z-buffer[ pi ] = FAR
    Fb[ pi ] = BACKGROUND_COLOUR
}

for each polygon P
{
    for each pixel pi in the projection of P
    {
        Compute depth z and shade s of P at pi
        if z < Z-buffer[ pi ]
        {
            Z-buffer[ pi ] = z
            Fb[ pi ] = s
        }
    }
}
```

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## Visibility tricks for Z-buffers

Z-buffering is *the* algorithm of choice for hardware rendering, so let's think about how to make it run as fast as possible...

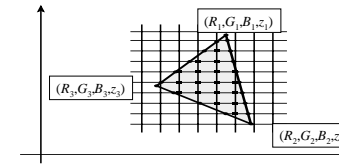
What is the complexity of the Z-buffer algorithm?

- What can we do to decrease the constants?

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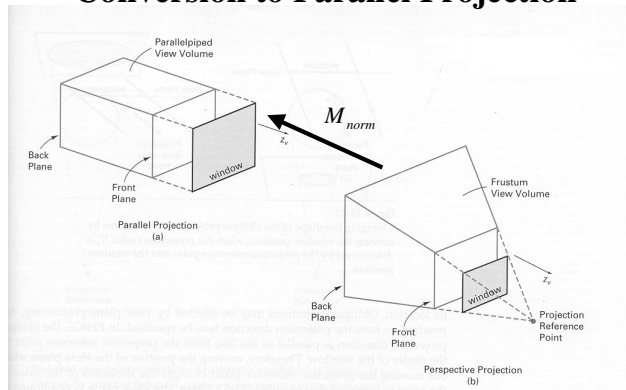
## Z-buffer Tricks

- The shade of a triangle can be computed incrementally from the shades of its vertices
- Can do the same with depth



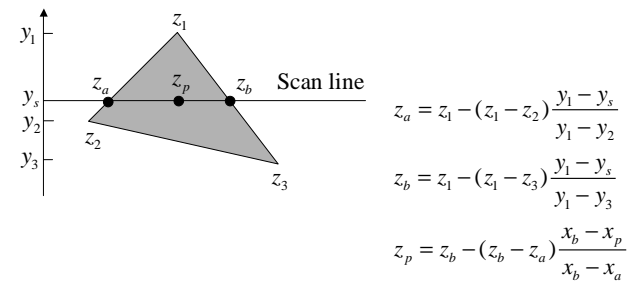
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## Depth Preserving Conversion to Parallel Projection



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## Z value interpolation



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## Z-buffer Analysis

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## Back Face Culling

- Can be used in conjunction with polygon-based algorithms
- Often, we don't want to draw polygons that face away from the viewer. So test for this and eliminate (cull) back-facing polygons before drawing
- How can we test for this?

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## Summary

- Classification of hidden surface algorithms
- Understanding of Z-buffer
- Familiarity with BSP trees and back face culling

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