

Hidden Surfaces

1

Reading

- Foley *et al.*, Chapter 15

2

The Quest for 3D

- Construct a 3D hierarchical geometric model
- Define a virtual camera
- Map points in 3D space to points in an image

- produce a wireframe drawing in 2D from a 3D object

- Of course, there's more work to be done...

3

Introduction

- Not every part of every 3D object is visible to a particular viewer. We need an algorithm to determine what parts of each object should get drawn.
- Known as “hidden surface elimination” or “visible surface determination”.
- Hidden surface elimination algorithms can be categorized in three major ways:
 - Object space vs. image space
 - Object order vs. image order
 - Sort first vs. sort last
 - Still a very active research area
- Where would we use a hidden surface algorithm?

4

Object Space Algorithms

- Operate on geometric primitives
 - For each object in the scene, compute the part of it which isn't obscured by any other object, then draw.
 - Must perform tests at high precision
 - Resulting information is resolution-independent
- Complexity
 - Must compare every pair of objects, so $O(n^2)$ for n objects
 - Optimizations can reduce this cost, but...
 - Best for scenes with few polygons or resolution-independent output
- Implementation
 - Difficult to implement!
 - Must carefully control numerical error

5

Image Space Algorithms

- Operate on pixels
 - For each pixel in the scene, find the object closest to the COP which intersects the projector through that pixel, then draw.
 - Perform tests at device resolution, result works only for that resolution
- Complexity
 - Must do something for every pixel in the scene, so at least $O(R)$.
 - Easiest solution is so test projector against every object, giving $O(nR)$.
 - More reasonable version only does work for pixels belonging to objects: $O(nr)$, r is number of pixels per object
 - Often, with more objects, each is smaller, so we estimate $nr = O(R)$ in practice
- Implementation
 - Usually very simple!

6

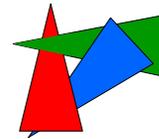
Object Order vs. Image Order

- Object order
 - Consider each object only once - draw its pixels and move on to the next object
 - Might draw the same pixel multiple times
- Image order
 - Consider each pixel only once - draw part of an object and move on to the next pixel
 - Might compute relationships between objects multiple times

7

Sort First vs. Sort Last

- Sort first
 - Find some depth-based ordering of the objects relative to the camera, then draw from back to front
 - Build an ordered data structure to avoid duplicating work
- Sort last
 - Sort implicitly as more information becomes available



8

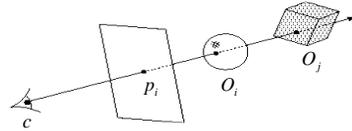
Important Algorithms

- Ray casting
- Z-buffer
- Binary space partitioning
- Back face culling

9

Ray Casting

- Partition the projection plane into pixels to match screen resolution
- For each pixel p_i , construct ray from COP through PP at that pixel and into scene
- Intersect the ray with every object in the scene, colour the pixel according to the object with the closest intersection



10

Aside: Definitions

- An algorithm exhibits *coherence* if it uses knowledge about the continuity of the objects on which it operates
- An *online* algorithm is one that doesn't need all the data to be present when it starts running
 - Example: insertion sort

11

Ray Casting Analysis

Categorization:

- Easy to implement?
- Hardware implementation?
- Coherence?
- Memory intensive?
- Pre-processing required?
- Online?
- Handles transparency?
- Handles refraction?
- Polygon-based?
- Extra work for moving objects?
- Extra work for moving viewer?
- Efficient shading?
- Handles cycles and self-intersections?

12

Z-buffer

- Idea: along with a pixel's red, green and blue values, maintain some notion of its *depth*
 - An additional channel in memory, like alpha
 - Called the depth buffer or Z-buffer

```
void draw_mode_setup( void ) {
    ...
    glEnable( GL_DEPTH_TEST );
    ...
}
```

- When the time comes to draw a pixel, compare its depth with the depth of what's already in the framebuffer. Replace only if it's closer
- Very widely used
- History
 - Originally described as "brute-force image space algorithm"
 - Written off as impractical algorithm for huge memories
 - Today, done easily in hardware

13

Z-buffer Implementation

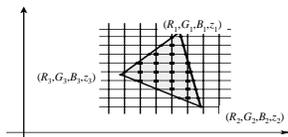
```
for each pixel  $p_i$ 
{
    Z-buffer[  $p_i$  ] = FAR
    Fb[  $p_i$  ] = BACKGROUND_COLOUR
}

for each polygon P
{
    for each pixel  $p_i$  in the projection of P
    {
        Compute depth  $z$  and shade  $s$  of P at  $p_i$ 
        if  $z < Z\text{-buffer}[ p_i ]$ 
        {
            Z-buffer[  $p_i$  ] =  $z$ 
            Fb[  $p_i$  ] =  $s$ 
        }
    }
}
```

14

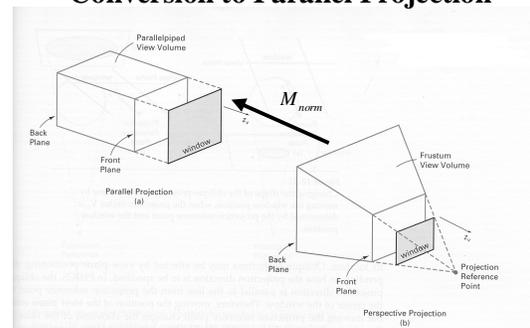
Z-buffer Tricks

- The shade of a triangle can be computed incrementally from the shades of its vertices
- Can do the same with depth



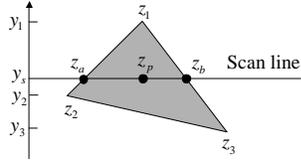
15

Depth Preserving Conversion to Parallel Projection



16

Z value interpolation



$$z_a = z_1 - (z_1 - z_2) \frac{y_1 - y_s}{y_1 - y_2}$$

$$z_b = z_1 - (z_1 - z_3) \frac{y_1 - y_s}{y_1 - y_3}$$

$$z_p = z_b - (z_b - z_a) \frac{x_b - x_p}{x_b - x_a}$$

17

Z-buffer Analysis

Categorization:

- Easy to implement?
- Hardware implementation?
- Coherence?
- Memory intensive?
- Pre-processing required?
- Online?
- Handles transparency?
- Handles refraction?
- Polygon-based?
- Extra work for moving objects?
- Extra work for moving viewer?
- Efficient shading?
- Handles cycles and self-intersections?

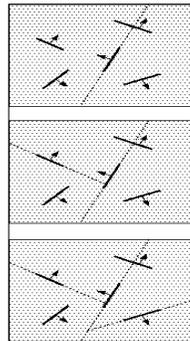
18

Binary Space Partitioning

- Goal: build a tree that captures some relative depth information between objects. Use it to draw objects in the right order.
 - Tree doesn't depend on camera position, so we can change viewpoint and redraw quickly
 - Called the binary space partitioning tree, or BSP tree
- Key observation: The polygons in the scene are painted in the correct order if for each polygon P ,
 - Polygons on the far side of P are painted first
 - P is painted next
 - Polygons in front of P are painted last

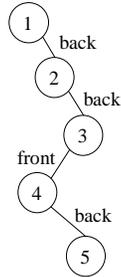
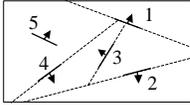
19

Building a BSP Tree (in 2D)



20

Alternate BSP Tree



21

BSP Tree Construction

```

BSPtree makeBSP( L: list of polygons )
{
    if L is empty
    {
        return the empty tree
    }

    Choose a polygon P from L to serve as root
    Split all polygons in L according to P
    return new TreeNode(
        P,
        makeBSP( polygons on negative side of P ),
        makeBSP( polygons on positive side of P ) )
}
    
```

- Splitting polygons is expensive! It helps to choose P wisely at each step.
 - Example: choose five candidates, keep the one that splits the fewest polygons

22

BST Tree Display

```

showBSP( v: Viewer, T: BSPtree )
{
    if T is empty then return

    P := root of T
    if viewer is in front of P
    {
        showBSP( back subtree of T )
        draw P
        showBSP( front subtree of T )
    } else {
        showBSP( front subtree of T )
        draw P
        showBSP( back subtree of T )
    }
}
    
```

23

BSP Tree Analysis

Categorization:

- Easy to implement?
- Hardware implementation?
- Coherence?
- Memory intensive?
- Pre-processing required?
- Online?
- Handles transparency?
- Handles refraction?
- Polygon-based?
- Extra work for moving objects?
- Extra work for moving viewer?
- Efficient shading?
- Handles cycles and self-intersections?

24

Back Face Culling

- Can be used in conjunction with polygon-based algorithms
- Often, we don't want to draw polygons that face away from the viewer. So test for this and eliminate (cull) back-facing polygons before drawing
- How can we test for this?

25

Summary

- Classification of hidden surface algorithms
- Understanding of Z-buffer
- Familiarity with BSP trees and back face culling

26