

K-means



Randomly initialize k centers

$$\square$$
 $\mu^{(0)} = \mu_1^{(0)}, ..., \mu_k^{(0)}$

■ Classify: Assign each point j∈{1,...N} to nearest center:

$$\square z^j \leftarrow \arg\min_i ||\mu_i - \mathbf{x}^j||_2^2$$

Recenter: μ_i becomes centroid of its point:

$$\square \mu_i^{(t+1)} \leftarrow \arg\min_{\mu} \sum_{i,j,j} ||\mu - \mathbf{x}^j||_2^2$$

 $\square \mu_i^{(t+1)} \leftarrow \arg\min_{\mu} \sum_{j:z^j=i} ||\mu - \mathbf{x}^j||_2^2 \qquad \qquad \mathbf{M} = \mathbf{Z}$ □ Equivalent to μ_i ← average of its points!

Case Study 2: Document Retrieval



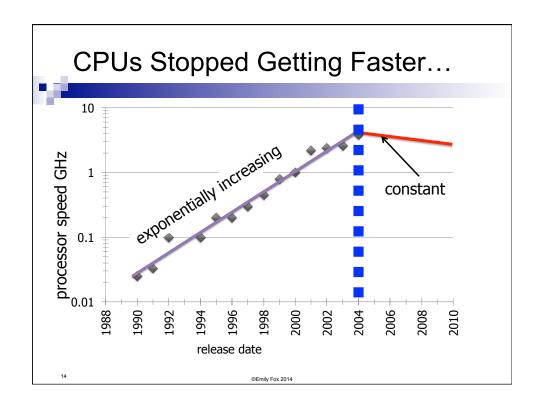
Machine Learning/Statistics for Big Data CSE547/STAT548, University of Washington

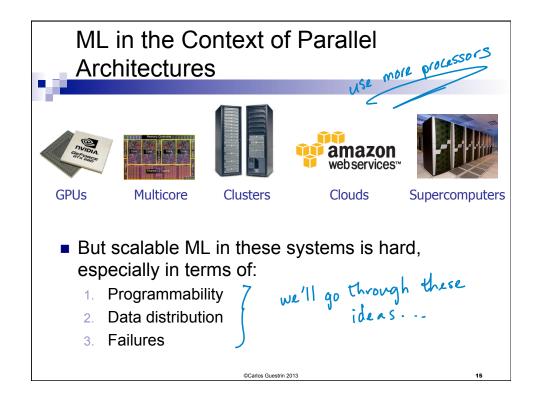
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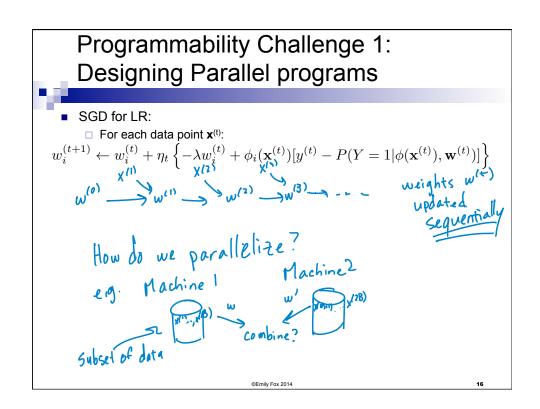
January 23rd, 2014

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Programmability Challenge 2: Race Conditions We are used to sequential programs: Read data, think, write data, read data, think, write data. But, in parallel, you can have non-deterministic effects: One machine reading data while other is writing Called a race-condition: Very annoying One of the hardest problems to debug in practice: because of non-determinism, bugs are hard to reproduce

Robustness to Failures Challenge



- From Google's Jeff Dean, about their clusters of 1800 servers, in first year of operation:
 - □ 1,000 individual machine failures
 - thousands of hard drive failures
 - one power distribution unit will fail, bringing down 500 to 1,000 machines for about 6 hours
 - □ 20 racks will fail, each time causing 40 to 80 machines to vanish from the network
 - □ 5 racks will "go wonky," with half their network packets missing in action
 - the cluster will have to be rewired once, affecting 5 percent of the machines at any given moment over a 2-day span
 - 50% chance cluster will overheat, taking down most of the servers in less than 5 minutes and taking 1 to 2 days to recover
- How do we design distributed algorithms and systems robust to failures?
 - It's not enough to say: run, if there is a failure, do it again... because you may never finish

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Move Towards Higher-Level Abstraction



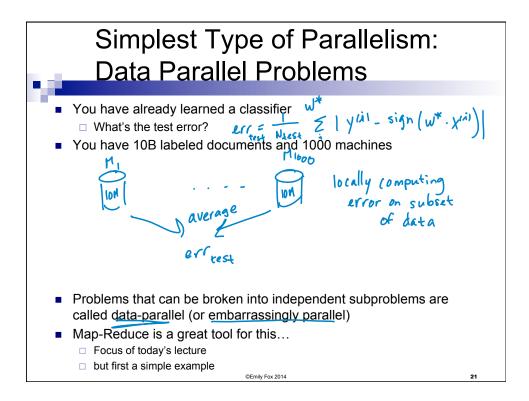
- Distributed computing challenges are hard and annoying!
 - Programmability
 - 2. Data distribution
 - 3. Failures

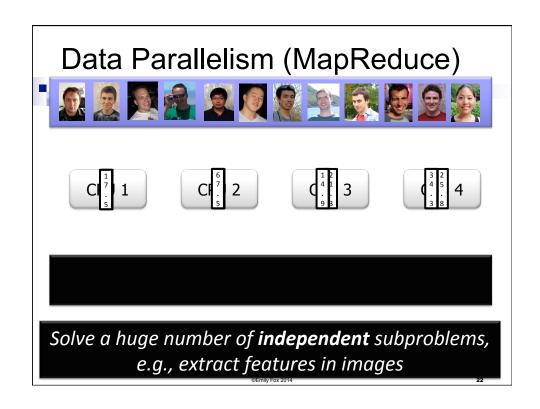


- High-level abstractions try to simplify distributed programming by hiding challenges:
 - □ Provide different levels of robustness to failures, optimizing data movement and communication, protect against race conditions...
 - □ Generally, you are still on your own WRT designing parallel algorithms
- Some common parallel abstractions:
 - Lower-level:
 - Pthreads: abstraction for distributed threads on single machine
 - MPI: abstraction for distributed communication in a cluster of computers
 - Higher-level:
 - Map-Reduce (Hadoop: open-source version): mostly data-parallel problems
 - GraphLab: for graph-structured distributed problems

7 this quarter

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Counting Words on a Single Processor



- (This is the "Hello World!" of Map-Reduce)
- Suppose you have 10B documents and 1 machine
- You want to count the number of appearances of each word on this
 - ☐ Similar ideas useful, e.g., for building Naïve Bayes classifiers and computing TF-IDF
- Code:

Naïve Parallel Word Counting



Simple data parallelism approach:

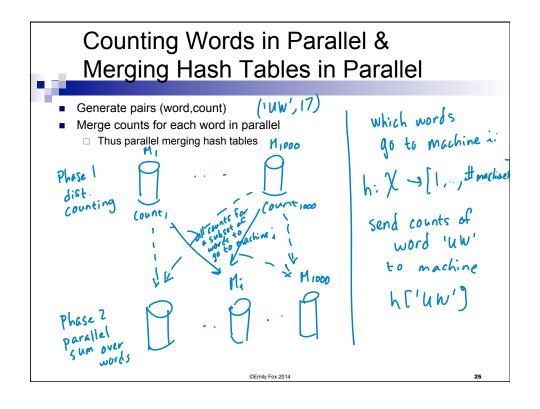


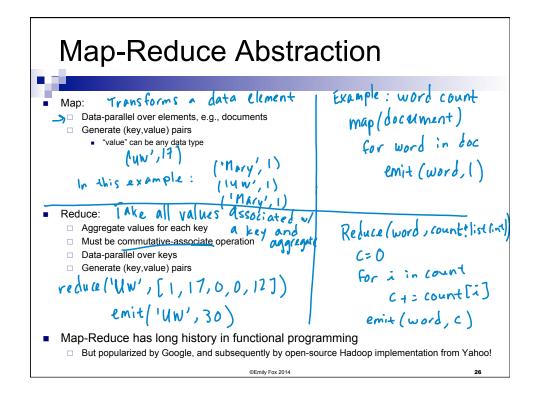


Count[word] = [Counta[word]

How do we do this for all words in the vocab?

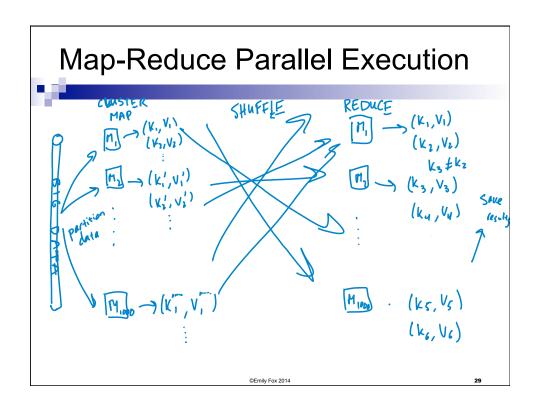
■ Merging hash tables: annoying, potentially not parallel → no gain from parallelism??? have to merge hash table

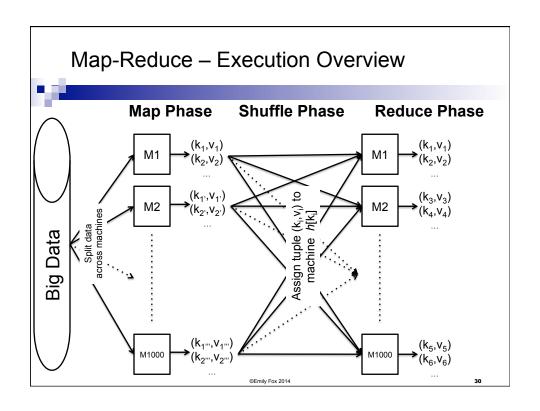


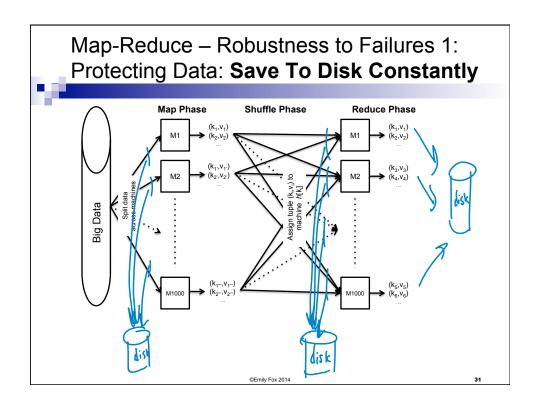


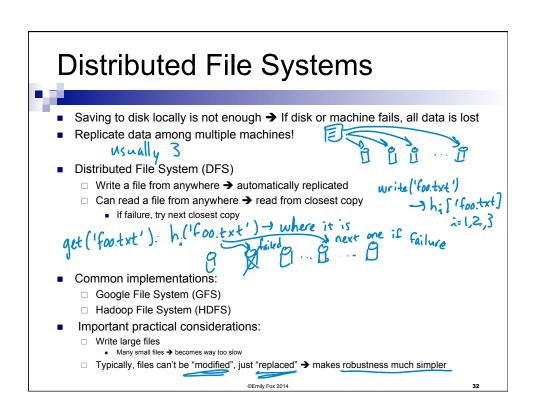
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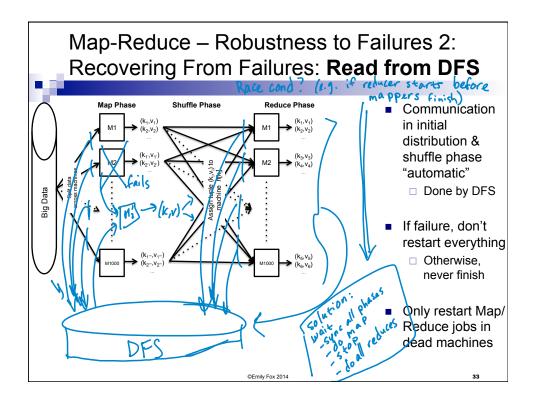
Reduce Code (Hadoop): Word Count

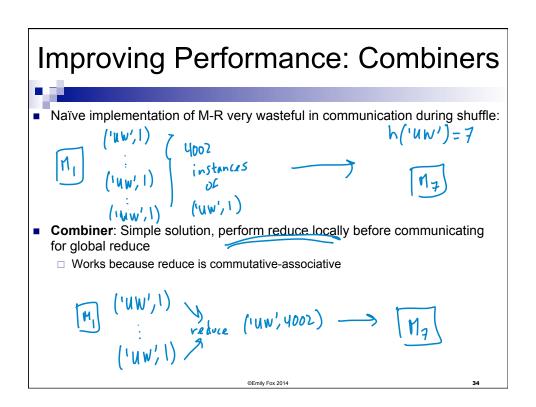


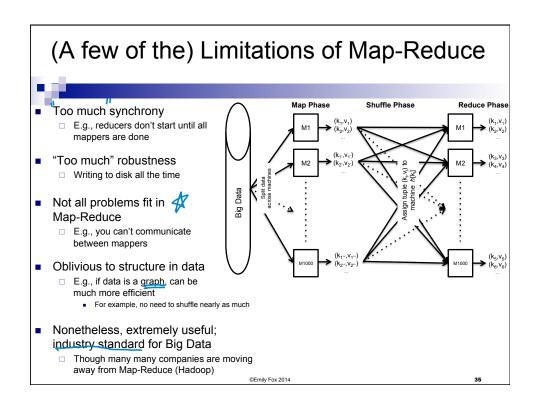


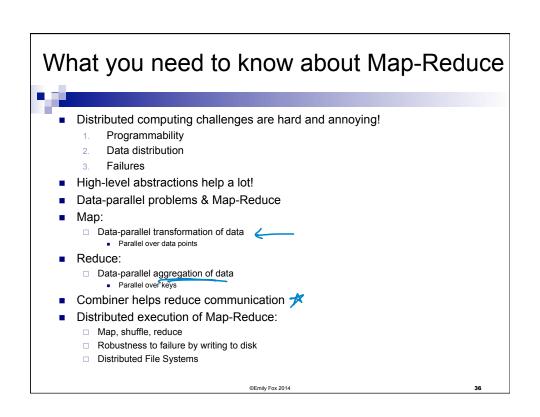


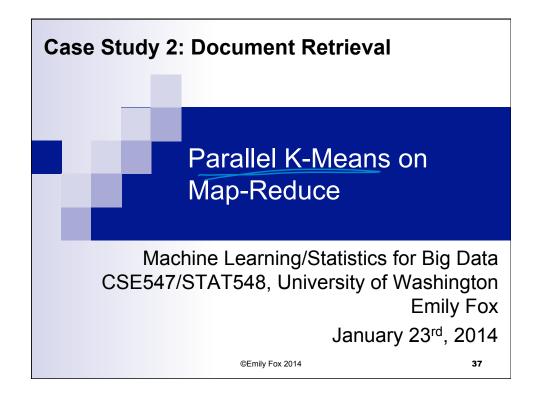


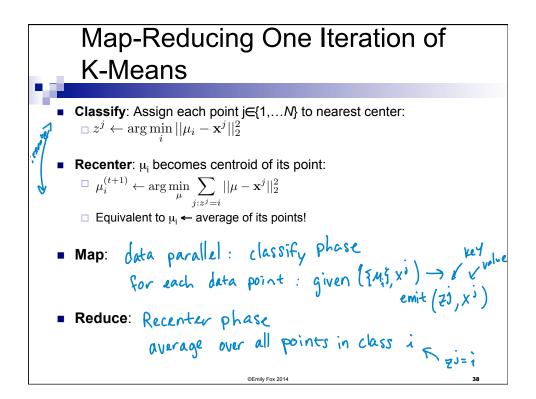












Classification Step as Map

- Classify: Assign each point j∈{1,...m} to nearest center: $\square z^j \leftarrow \arg\min||\mu_i - \mathbf{x}^j||_2^2$
- Map: map ([M, Mk], x)) Zi = argmin || Mi-xill2 emit (zi, xi) e.g. emit(2, (17,0,0,1,7,2))

Recenter Step as Reduce

- Recenter: μ_i becomes centroid of its point:
 - $\square \, \mu_i^{(t+1)} \leftarrow \arg \min_{\mu} \sum_{j:z^j=i} ||\mu \mathbf{x}^j||_2^2$
 - □ Equivalent to $\mu_i \leftarrow$ average of its points!

data assigned to class i Reduce (i, list-x: [x1, x2,....]) Reduce:

Some Practical Considerations



- K-Means needs an iterative version of Map-Reduce
 - Not standard formulation
- Mapper needs to get data point and all centers
 - ☐ A lot of data!
 - □ Better implementation: mapper gets many data points

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What you need to know about Parallel K-Means on Map-Reduce



- Map: classification step; data parallel over data point
- Reduce: recompute means; data parallel over centers

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