

CSE544

Data Management

Lecture 6: Data Models, Relational Algebra

Announcements

- Project teams due Friday
- HW2 is posted
- Review of “What goes around...” today

Where We Are

- We are done with SQL; Please continue to read and learn on your own
- Today: data models, and why the relational model wins; then RA
- Next lectures: DBMS internals

References

- M. Stonebraker and J. Hellerstein. What Goes Around Comes Around. In "Readings in Database Systems" (aka the Red Book). 4th ed.

Outline

- Early data models
 - IMS
 - CODASYL
- Relational Model in some detail
- Data models that followed the relational model

Early Proposal 1: IMS*

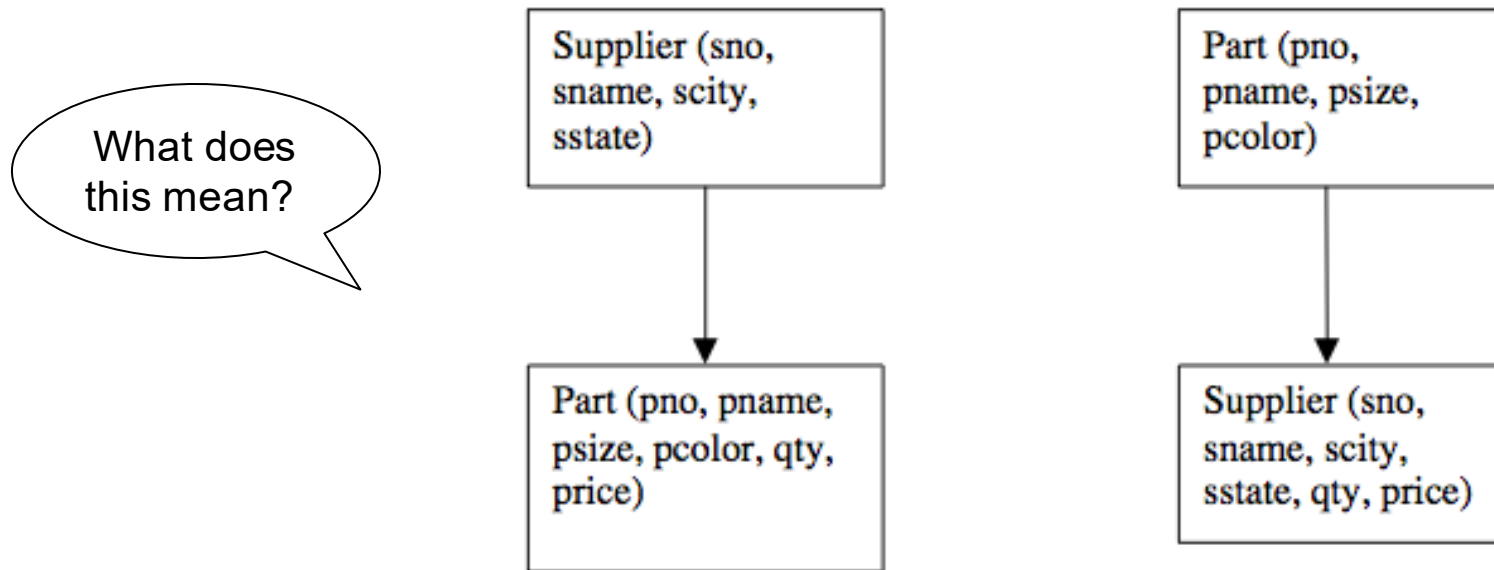
- What is it?

Early Proposal 1: IMS*

- **Hierarchical data model**
- **Record**
 - **Type**: collection of named fields with data types
 - **Instance**: must match type definition
 - Each instance has a **key**
 - Record types arranged in a **tree**
- **IMS database** is collection of instances of record types organized in a tree

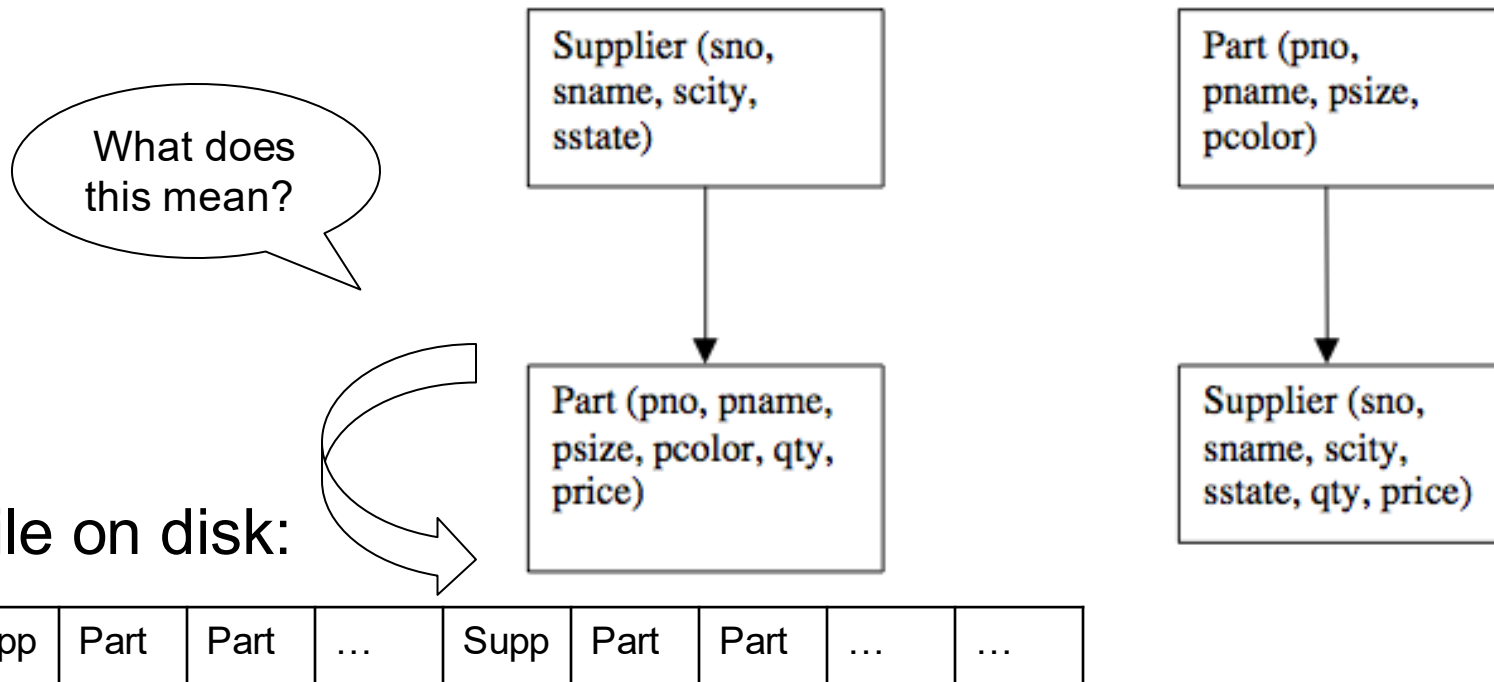
IMS Example

- Figure 2 from “What goes around comes around”



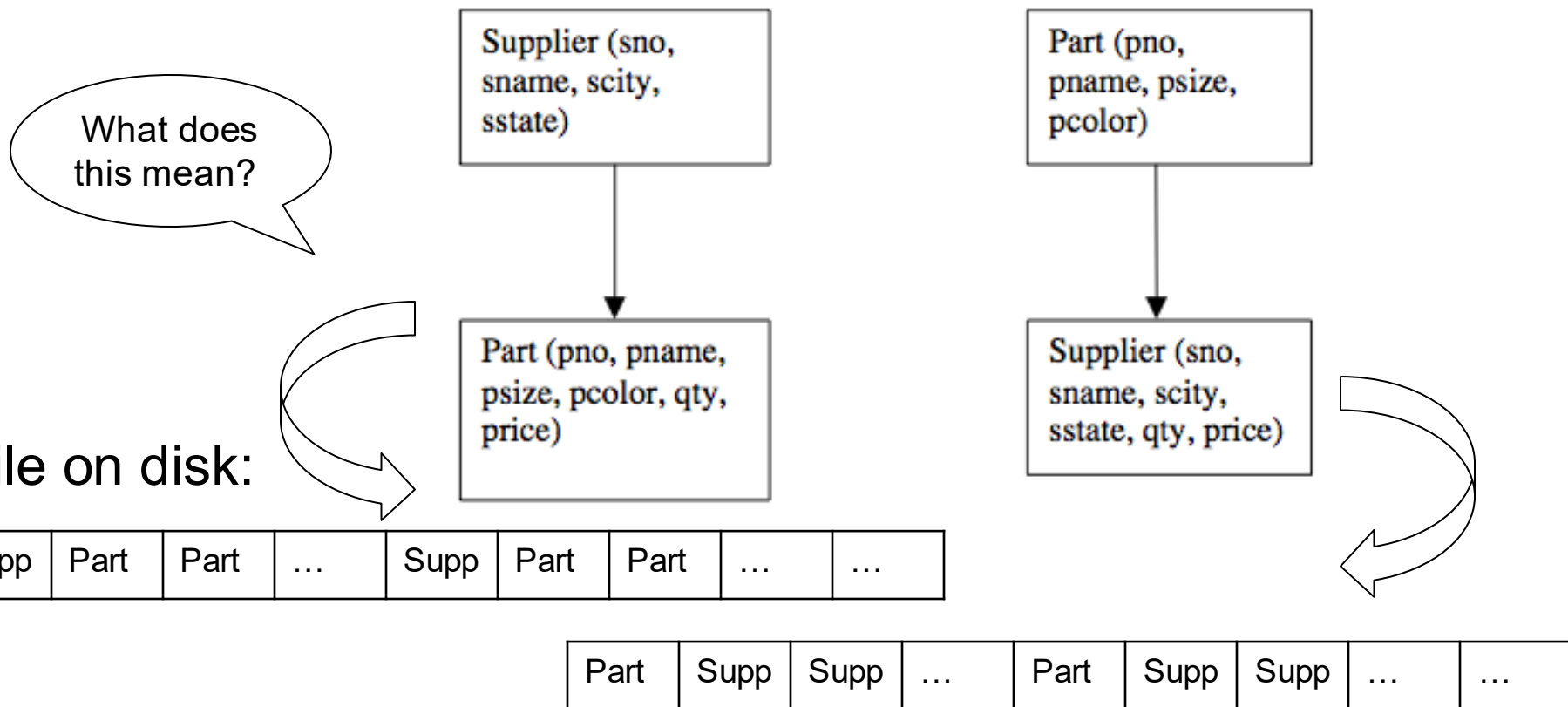
IMS Example

- Figure 2 from “What goes around comes around”



IMS Example

- Figure 2 from “What goes around comes around”



IMS Limitations

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- **Tree-structured data model**
 - Redundant data; existence depends on parent

IMS Limitations

- **Tree-structured data model**
 - Redundant data; existence depends on parent
- **Record-at-a-time** user interface
 - User must specify algorithm to access data

IMS Limitations

- **Tree-structured data model**
 - Redundant data; existence depends on parent
- **Record-at-a-time** user interface
 - User must specify algorithm to access data
- **Very limited physical independence**
 - Phys. organization limits possible operations
 - Application programs break if organization changes
- **Some logical independence but limited**

Data Manipulation Language: DL/1

How does a programmer retrieve data in IMS?

Data Manipulation Language: DL/1

How does a programmer retrieve data in IMS?

- Each record has a hierarchical sequence key (HSK)
- HSK defines semantics of commands:
 - `get_next`; `get_next_within_parent`
- **DL/1 is a record-at-a-time language**
 - Programmers construct algorithm, worry about optimization

Data storage

How is data physically stored in IMS?

Data storage

How is data physically stored in IMS?

- Root records
 - Stored sequentially (sorted on key)
 - Indexed in a B-tree using the key of the record
 - Hashed using the key of the record
- Dependent records
 - Physically sequential
 - Various forms of pointers
- Selected organizations restrict DL/1 commands
 - No updates allowed due to sequential organization
 - No “get-next” for hashed organization

Data Independence

What is it?

Data Independence

What is it?

- **Physical data independence**: Applications are insulated from changes in **physical storage details**
- **Logical data independence**: Applications are insulated from changes to **logical structure of the data**

Lessons from IMS

- Physical/logical data independence needed
- Tree structure model is restrictive
- Record-at-a-time programming forces user to do optimization

Early Proposal 2: CODASYL

What is it?

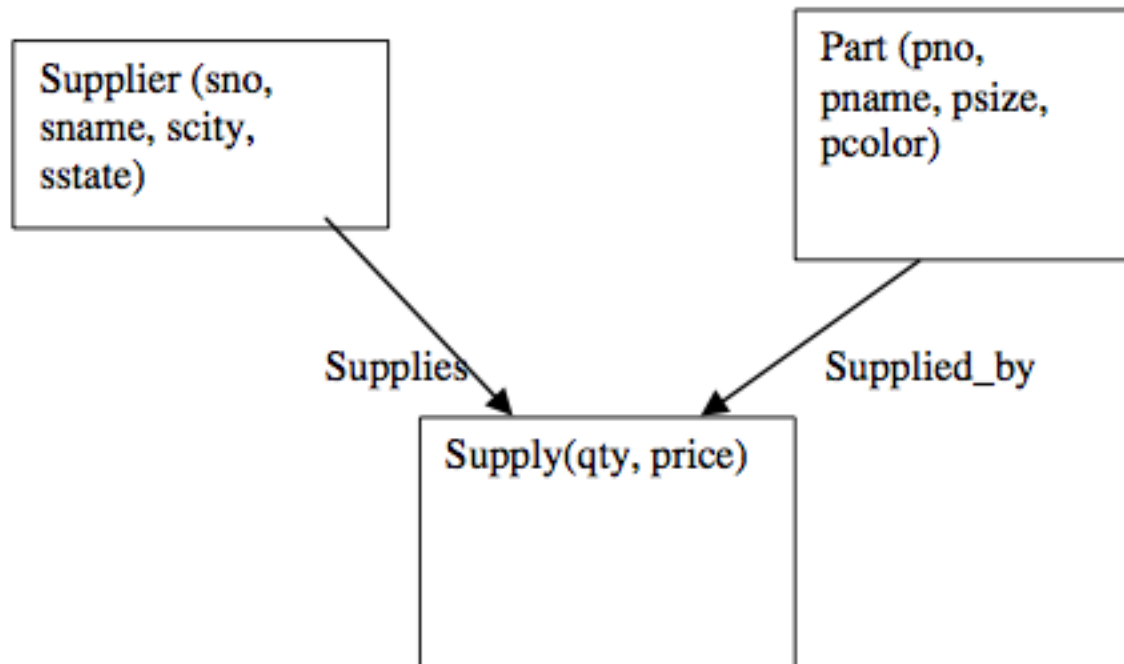
Early Proposal 2: CODASYL

What is it?

- **Networked data model**
- Primitives are also **record types** with **keys**
- Record types are organized into **network**
- Multiple parents; arcs = “sets”
- More flexible than hierarchy
- **Record-at-a-time** data manipulation language

CODASYL Example

- Figure 5 from “What goes around comes around”



CODASYL Limitations

- No data independence: application programs break if organization changes
- Record-at-a-time: “navigate the hyperspace”

The Programmer as Navigator

by Charles W. Bachman



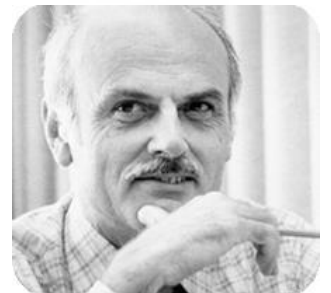
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- Relational Model in some detail
- Data models that followed the relational model

Relational Model Overview

Ted Codd 1970

- What was the motivation? What is the model?



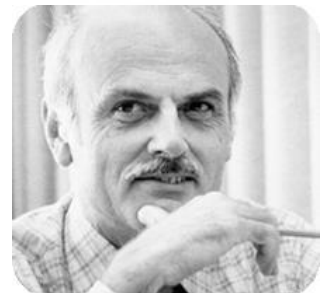
Relational Model Overview

Ted Codd 1970

- Motivation: **logical and physical data independence**
- Store data in a **simple data structure** (table)
- Access data through **set-at-a-time** language
- **No need for physical storage proposal**



Relational Database: A Practical Foundation for
Productivity



Great Debate

- Pro relational
 - What were the arguments?
- Against relational
 - What were the arguments?
- How was it settled?

Great Debate

- Pro relational
 - CODASYL is too complex
 - No data independence
 - Record-at-a-time hard to optimize
 - Trees/networks not flexible enough
- Against relational
 - COBOL programmers cannot understand relational languages
 - Impossible to implement efficiently
- Ultimately settled by the market place

Outline

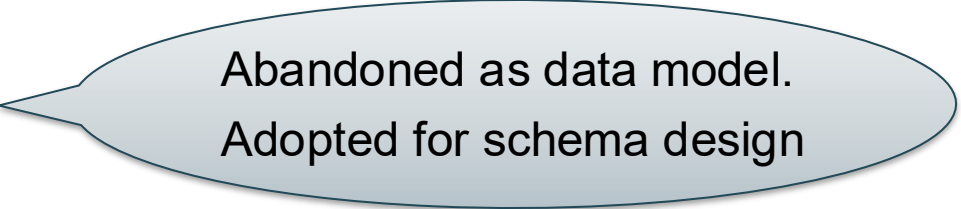
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Other Data Models

- Entity-relationship
- Object-relational
- Semistructured
- Key-value pairs

Other Data Models

- Entity-relationship

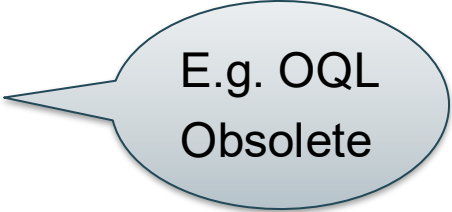


Abandoned as data model.
Adopted for schema design

- Object-relational
- Semistructured
- Key-value pairs

Other Data Models

- Entity-relationship
- Object-relational
- Semistructured
- Key-value pairs



E.g. OQL
Obsolete

Other Data Models

- Entity-relationship
- Object-relational
- Semistructured
- Key-value pairs



XML, Json, Protobuf
Nested data; tree-like

Other Data Models

- Entity-relationship
- Object-relational
- Semistructured
- Key-value pairs

NoSQL:

- GET(K), PUT(K,V)
- Great scalability
- Poor functionality

Data Independence in the Relational Model

Data Independence

- Logical data independence:
 - SQL views
- Physical data independence:
 1. Declarative query: FO or SQL
 2. Query plan: Relational Algebra
 3. Query optimization / execution

Data Independence

- Logical data independence:
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SQL Views

- `CREATE VIEW RedSuppliers AS ...`
- Creates a new relation name
- The content of that relation is defined by a `SELECT-FROM-WHERE` query

Supplier (sno, sname, scity, sstate)

Supply (sno, pno, qty, price)

Part (pno, pname, psize, pcolor)

SQL Views

```
CREATE VIEW RedSuppliers AS  
  SELECT DISTINCT x.*  
  FROM Supplier x, Supply y, Part z  
  WHERE x.sno=y.sno and y.pno=z.pno and z.pcolor='Red';
```

Supplier (sno, sname, scity, sstate)

Supply (sno, pno, qty, price)

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RedSuppliers is added to the database schema

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RedSuppliers is added to the database schema
Later we can use it, like any table:

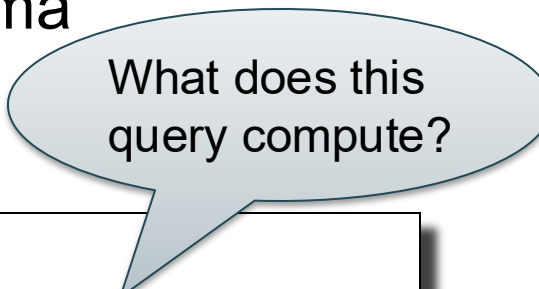
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Supplier (sno, sname, scity, sstate)
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SQL Views

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```

RedSuppliers is added to the database schema
Later we can use it, like any table:



What does this query compute?

```
SELECT DISTINCT x.*  
FROM RedSupplier x, Supply y, Part z  
WHERE x.sno=y.sno and y.pno=z.pno and z.pcolor='Blue';
```

Discussion

- **CREATE VIEW...**
 - Add view name permanently to the schema
 - To delete, type DROP VIEW ...
- **CREATE TEMPORAY VIEW...**
 - Supported in postgres
 - Add view name to the schema...
 - ...remove at the end of the session
- **WITH** Only local to one query

Virtual v.s. Materialized Views

- Virtual view – the default
 - The query defining the view is evaluated every time when it is used
 - The data is always up to date!
 - But we re-compute it every time: inefficient
- Materialized view
 - `CREATE MATERIALIZED VIEW ...`
 - Supported by some systems
 - Computed only once: efficient
 - But may not be up to date

Data Independence

- Logical data independence:
 - SQL views

- Physical data independence:
 1. Declarative query: FO or SQL
 2. Query plan: Relational Algebra
 3. Query optimization / execution

Data Independence

- Logical data independence:
 - SQL views

- Physical data independence:
 1. Declarative query: FO or SQL
 2. Query plan: Relational Algebra
 3. Query optimization / execution

We saw this

Next

Next lectures

Relational Algebra

Executing SQL Queries

- User writes in SQL
- System: SQL → Relational Algebra
- Query Plan: is optimized, then executed

Relational Algebra

Five operators:

- Selection σ
- Projection Π
- Join or cartesian product $\bowtie$, $\times$
- Union $\cup$
- Difference $-$

Selection

$\sigma_{condition}(T)$

Returns tuples in T
that satisfy the condition

```
SELECT *  
FROM T  
WHERE condition;
```

Selection

$\sigma_{condition}(T)$

Returns tuples in T
that satisfy the condition

$\sigma_{C=20 \wedge D \geq 66}(S) =$

```
SELECT *  
FROM T  
WHERE condition;
```

R=

A	B
1	10
1	20
2	20

S=

C	D
10	33
10	44
20	55
20	66
20	77
30	66

Selection

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C	D
20	66
20	77

S=

C	D
10	33
10	44
20	55
20	66
20	77
30	66

Projection

$$\Pi_{col1,col2,...}(T)$$

Return columns 1, 2, ...
from T; all rows

```
SELECT T.col1, T.col2,...  
FROM T  
WHERE condition;
```

R=

A	B
1	10
1	20
2	20

S=

C	D
10	33
10	44
20	55
20	66
20	77
30	66

Projection

$$\Pi_{col1, col2, \dots}(T)$$

Return columns 1, 2, ...
from T; all rows

$$\Pi_C(S) =$$

C
10
10
20
20
20
30

```
SELECT T.col1, T.col2,...  
FROM T  
WHERE condition;
```

R=

A	B
1	10
1	20
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S=

C	D
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10	44
20	55
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30	66

Bag semantics...

Projection

$$\Pi_{col1,col2,...}(T)$$

Return columns 1, 2, ...
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$$\Pi_C(S) =$$

C
10
10
20
20
20
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SELECT T.col1, T.col2,...  
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Projection

Bag semantics...

$$\Pi_{col1, col2, \dots}(T)$$

Return columns 1, 2, ...
from T; all rows

$$\Pi_C(S) =$$

C
10
10
20
20
20
30

or

C
10
20
30

...set semantics

```
SELECT T.col1, T.col2,...  
FROM T  
WHERE condition;
```

R=

A	B
1	10
1	20
2	20

S=

C	D
10	33
10	44
20	55
20	66
20	77
30	66

Join

$$T_1 \bowtie_{cond} T_2$$

Joins the two tables

```
SELECT *  
FROM T1, T2  
WHERE cond;
```

R=

A	B
1	10
1	20
2	20

S=

C	D
10	33
10	44
20	55
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Join

$$T_1 \bowtie_{cond} T_2$$

$$R \bowtie_{B=C} S =$$

Joins the two tables

```
SELECT *  
FROM T1, T2  
WHERE cond;
```

R=

A	B
1	10
1	20
2	20

S=

C	D
10	33
10	44
20	55
20	66
20	77
30	66

A	B	C	D
1	10	10	33
1	10	10	44
1	20	20	55
1	20	20	66
1	20	20	77
2	20	20	55
2	20	20	66
2	20	20	77

Join

$$T_1 \bowtie_{cond} T_2$$

Joins the two tables

$$R \bowtie_{x.B=y.B} R \bowtie y =$$

Disambiguate
attributes: various
conventions...

x.A	x.B	y.A	y.B
1	10	1	10
1	20	1	20
1	20	2	20
2	20	1	20
2	20	2	20

```
SELECT *  
FROM T1, T2  
WHERE cond;
```

R=

A	B
1	10
1	20
2	20

S=

C	D
10	33
10	44
20	55
20	66
20	77
30	66

Many Variants of Joins

- Eq-join: $R \bowtie_{B=C} S$
- Theta-join: $R \bowtie_{B \leq C \wedge A * D < 20} S$
- Cartesian product: $R \times S$
- Natural join: **next!**

Natural Join

- Joins on common column names
- Retains only one copy of the column

R=

A	B
1	10
1	20
2	20

S=

B	C
10	33
10	44
20	55
20	66
20	77
30	66

$R \bowtie S =$

Implicit: $R.B=S.B$

A	B	C
1	10	33
1	10	44
1	20	55
1	20	66
1	20	77
2	20	55
2	20	66
2	20	77

Quiz Time!

What do these natural joins compute?

- $R(A, B) \bowtie S(B, C)$
- $R(A, B) \bowtie S(C, D)$
- $R(A, B) \bowtie S(A, B)$

Quiz Time!

What do these natural joins compute?

- $R(A, B) \bowtie S(B, C)$



Joins on B=B

- $R(A, B) \bowtie S(C, D)$

- $R(A, B) \bowtie S(A, B)$

Quiz Time!

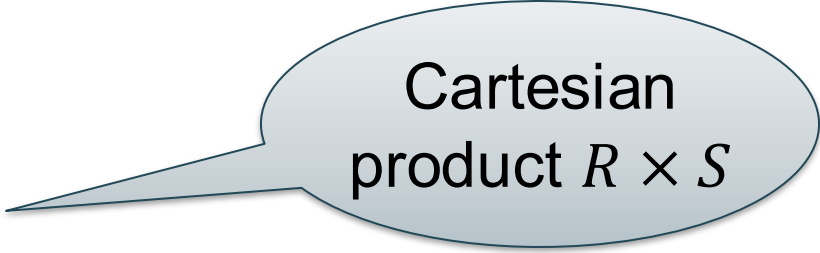
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Joins on $B=B$

- $R(A, B) \bowtie S(C, D)$



Cartesian
product $R \times S$

- $R(A, B) \bowtie S(A, B)$

Quiz Time!

What do these natural joins compute?

- $R(A, B) \bowtie S(B, C)$

Joins on $B=B$

- $R(A, B) \bowtie S(C, D)$

Cartesian
product $R \times S$

- $R(A, B) \bowtie S(A, B)$

Intersection $R \cap S$

Even More Joins

- Inner joins: $\bowtie$ (all variations)
- Left outer join: $\Join$
- Right-, full outer join: $\Join$, $\Join$
- Semi-join: $\ltimes$
- Anti-semi-join: $\triangleright$

People use various symbols

Semi-Join

$$R \bowtie S$$

A	B
1	20
1	30

Tuples in R that join with S

```
SELECT DISTINCT R.*  
FROM R, S  
WHERE join-cond;
```

R=

A	B
1	20
1	30
2	40

S=

B	C
10	33
10	44
20	55
20	66
20	77
30	66

Anti Semi-Join

$$R \triangleright S = R - R \bowtie S$$

A	B
2	40

Tuples in R that do not join with S

R=

A	B
1	20
1	30
2	40

S=

B	C
10	33
10	44
20	55
20	66
20	77
30	66

Finally: Union and Difference

- Set operations:

$$R \cup S, \quad R - S$$

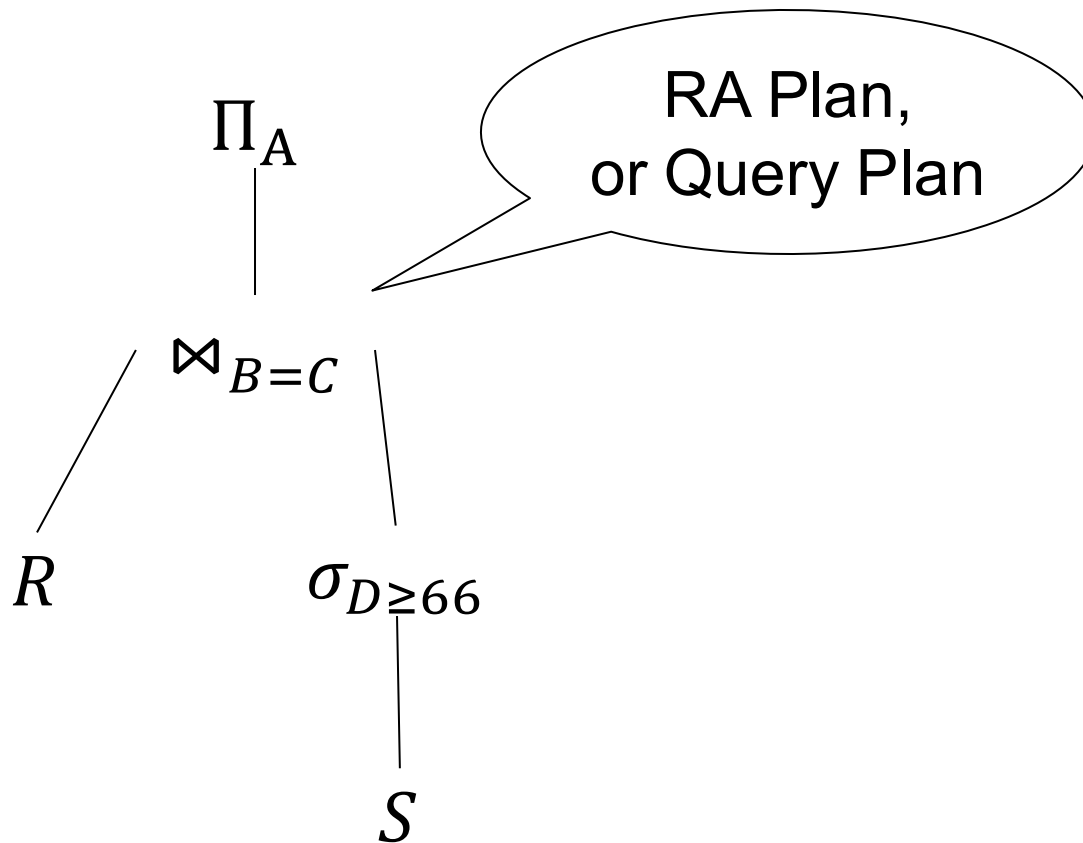
- R, S must have the same schema!

RA by Example

$$\Pi_A(R \bowtie_{B=C} \sigma_{D \geq 66}(S))$$

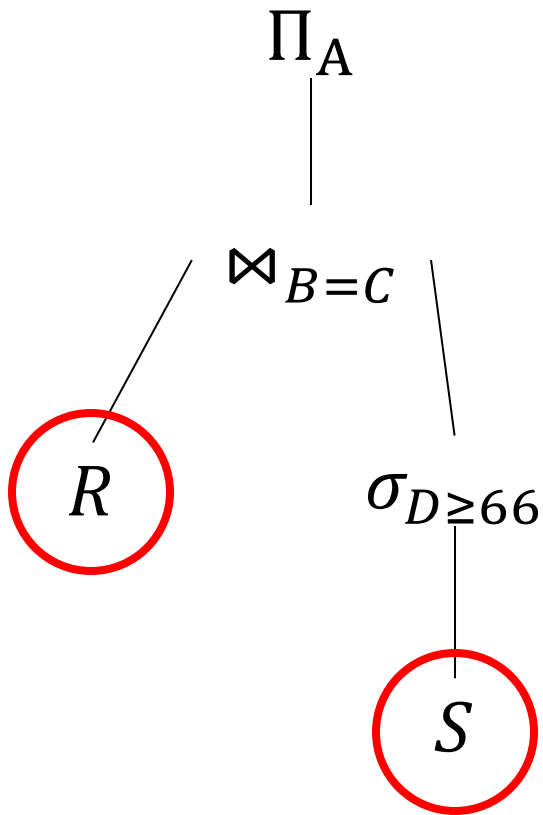
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RA by Example

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R=

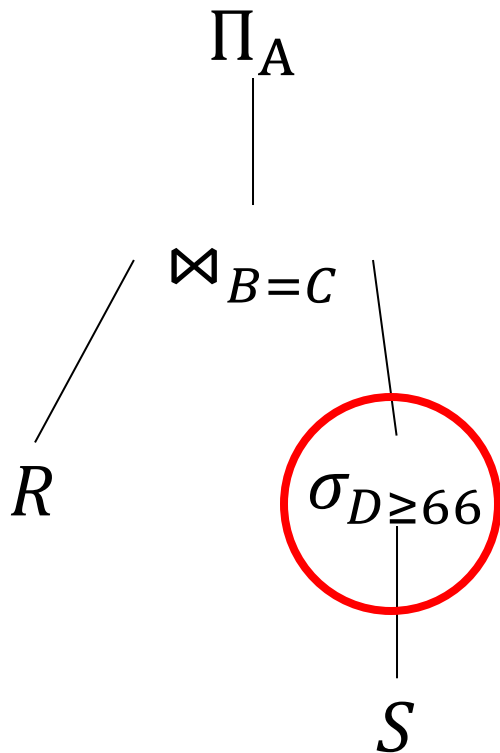
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RA by Example

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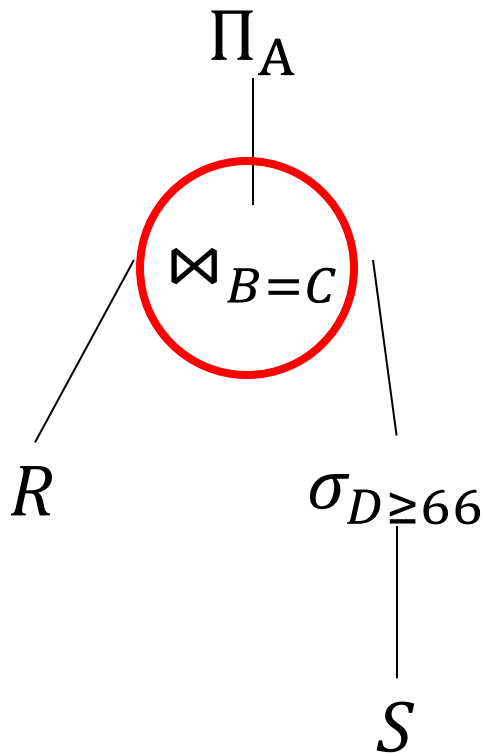
S=

C	D
20	66
20	77
30	66

C	D
10	33
10	44
20	55
20	66
20	77
30	66

RA by Example

$$\Pi_A(R \bowtie_{B=C} \sigma_{D \geq 66}(S))$$



A	B	C	D
1	20	20	66
1	20	20	77
2	20	20	66
2	20	20	77

C	D
20	66
20	77
30	66

R=

A	B
1	10
1	20
2	20

S=

C	D
10	33
10	44
20	55
20	66
20	77
30	66

RA by Example

A
1
2

Final output

A	B	C	D
1	20	20	66
1	20	20	77
2	20	20	66
2	20	20	77

C	D
20	66
20	77
30	66

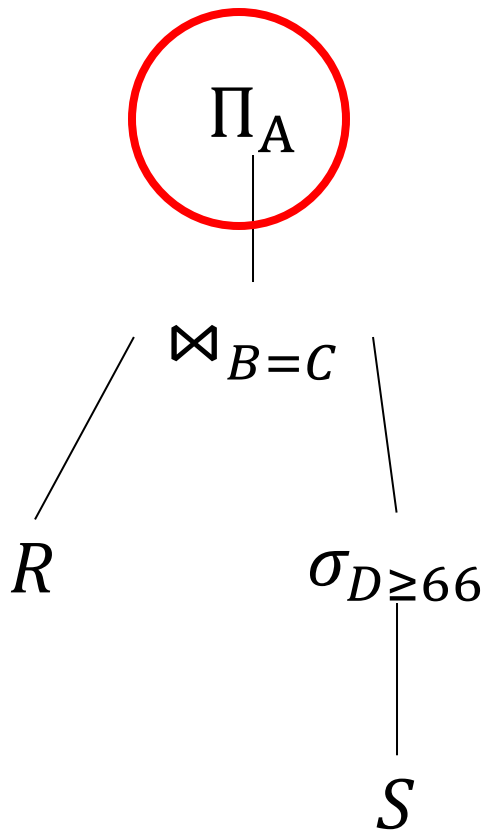
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Relational Algebra

Five operators:

- Selection σ
- Projection Π
- Join or cartesian product $\bowtie$, $\times$
- Union $\cup$
- Difference $-$

Relational Algebra

Which operations
are monotone?

Five operators:

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Relational Algebra

Which operations are monotone?

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Monotone

Non-monotone

Extended Relational Algebra

- Group-by and aggregate: γ
- Duplicate elimination: δ
- Sorting: τ



We only
discuss this

Group-by and Aggregates

$\gamma_{col1,col2,...,agg1,...}(T)$

Standard group-by:

```
SELECT col1,...,agg1(..),agg2(..)
FROM T
GROUP-BY condition;
```

$\gamma_{C,sum(D)}(S) =$

C	D
10	77
20	196
30	66

S=

C	D
10	33
10	44
20	55
20	66
20	77
30	66

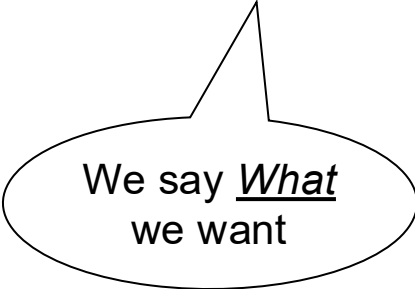
Translation

Every SQL query can be translated into an expression in the Extended RA

Product(pid, name, price)
Purchase(pid, cid, store)
Customer(cid, name, city)

SQL...

```
SELECT DISTINCT x.name, z.name  
FROM Product x, Purchase y, Customer z  
WHERE x.pid = y.pid and y.cid = y.cid and  
      x.price > 100 and z.city = 'Seattle'
```

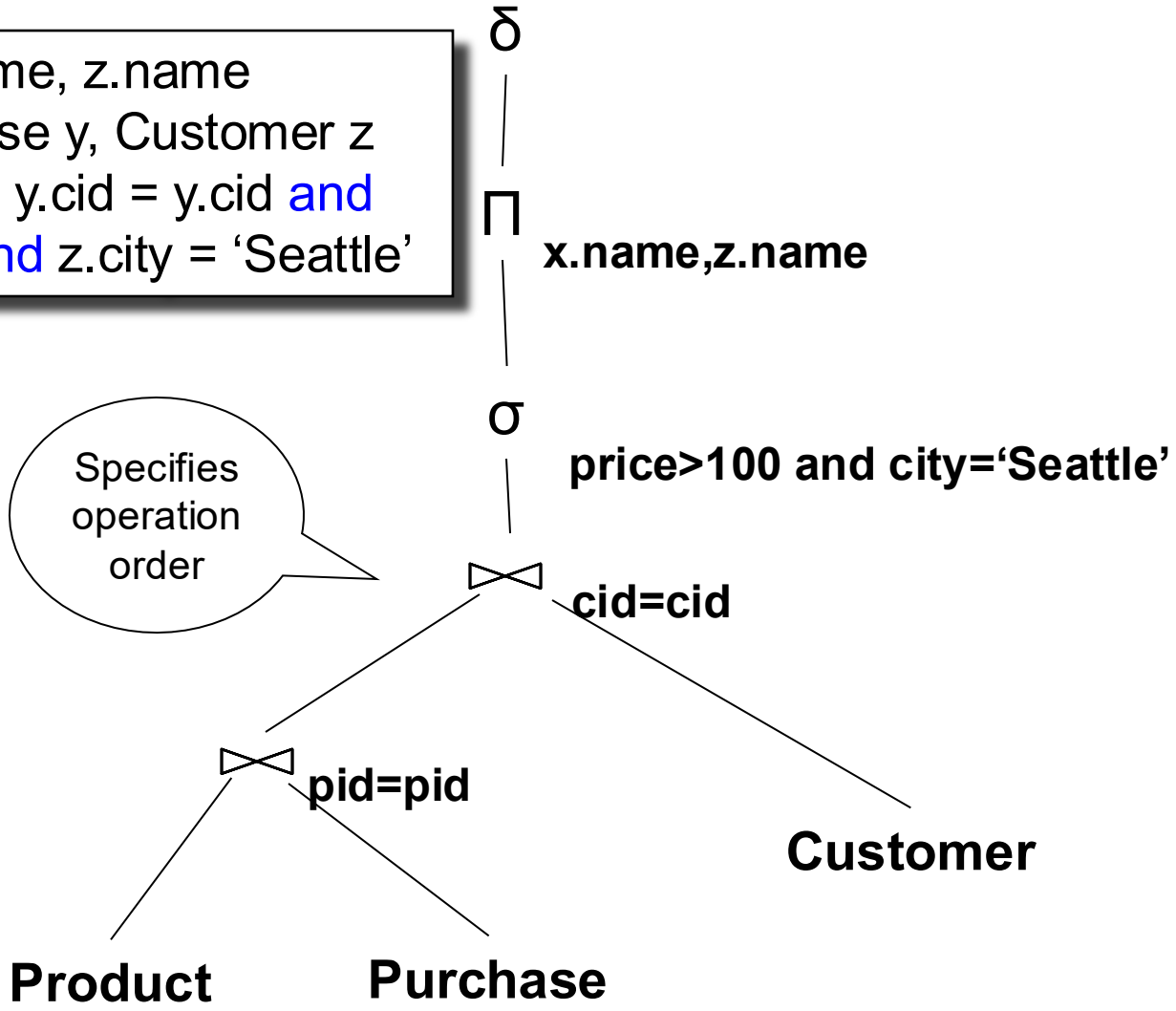


We say What
we want

Product(pid, name, price)
Purchase(pid, cid, store)
Customer(cid, name, city)

...to RA

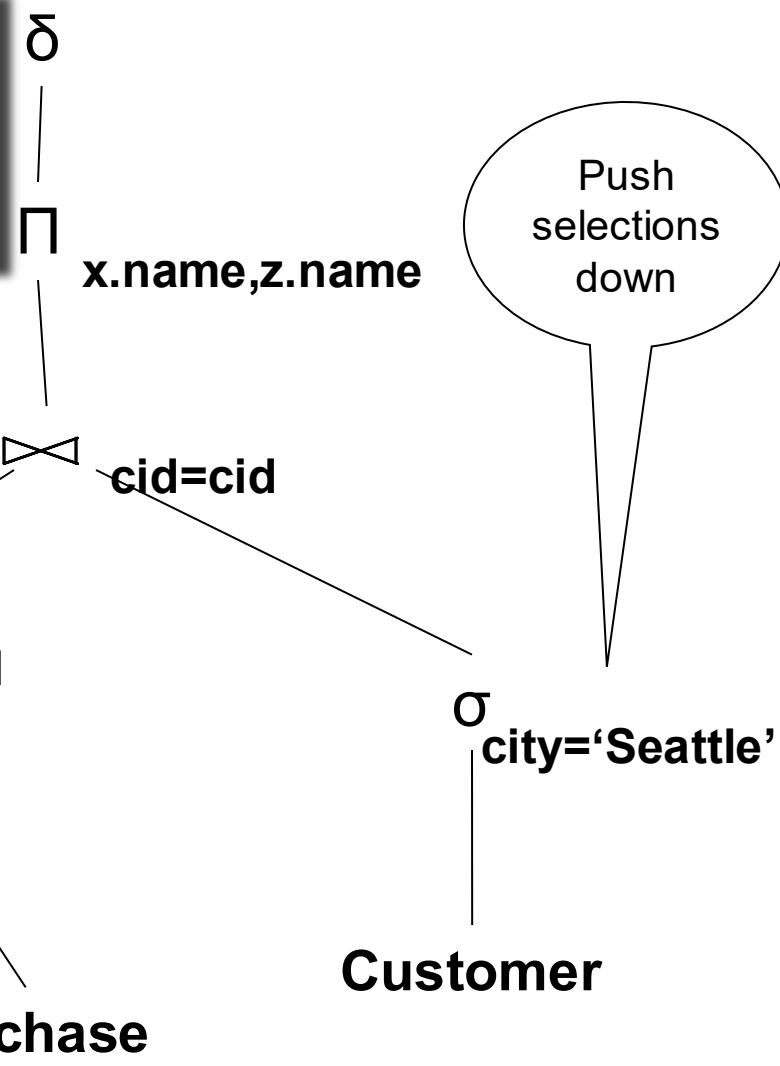
SELECT DISTINCT x.name, z.name
FROM Product x, Purchase y, Customer z
WHERE x.pid = y.pid **and** y.cid = y.cid **and**
 x.price > 100 **and** z.city = 'Seattle'



Product(pid, name, price)
Purchase(pid, cid, store)
Customer(cid, name, city)

Optimization

```
SELECT DISTINCT x.name, z.name  
FROM Product x, Purchase y, Customer z  
WHERE x.pid = y.pid and y.cid = z.cid and  
      x.price > 100 and z.city = 'Seattle'
```

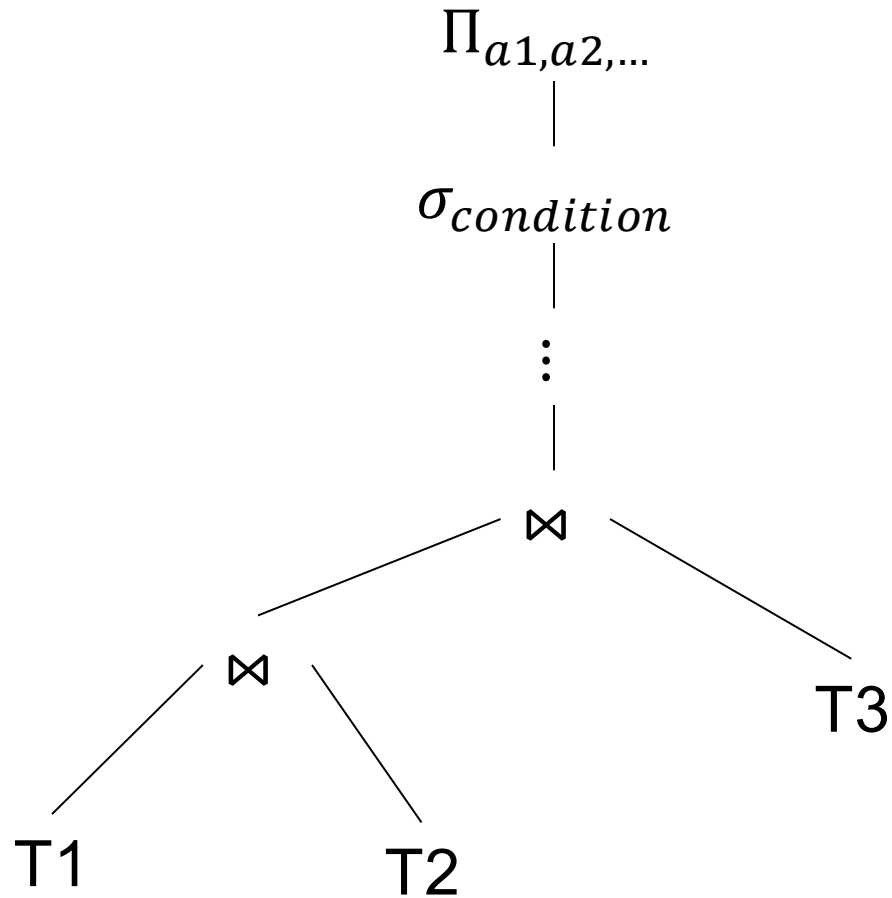


This is a quick preview!
More about this
next lectures

SQL to RA

Simple SFW

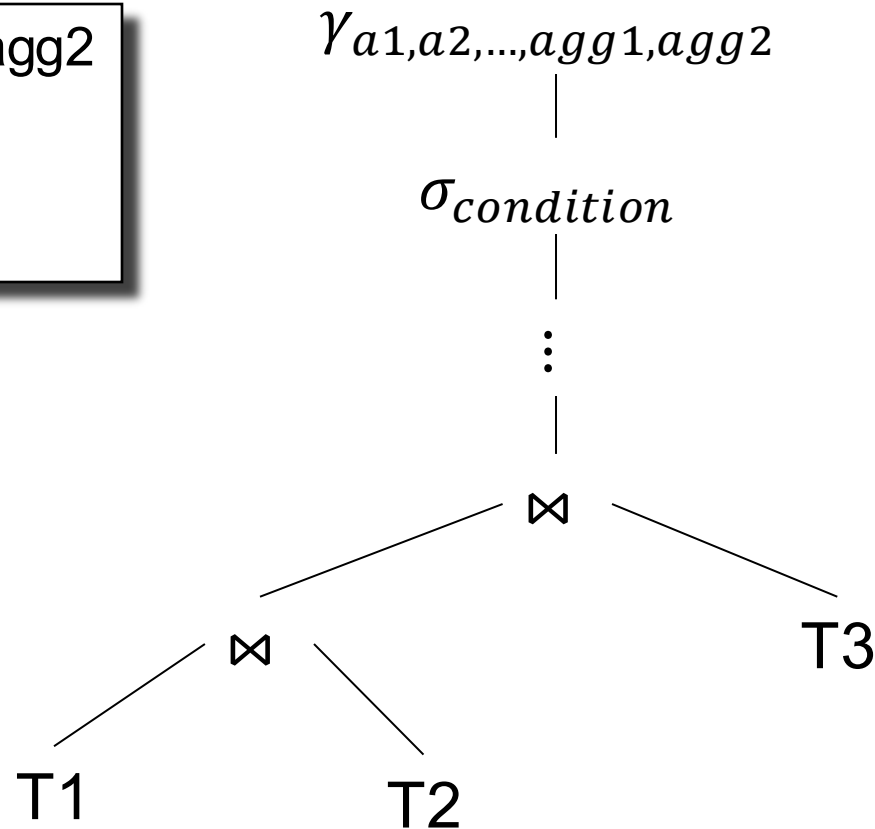
```
SELECT a1,a2,...  
FROM T1, T2, ...  
WHERE condition
```



SQL to RA

...add GROUP-BY

```
SELECT a1,a2,...,agg1,agg2  
FROM T1, T2, ...  
WHERE condition  
GROUP BY a1,a2,...
```



SQL to RA

$\Pi_{\text{only-what-we-need}}$

Both HAVING and
WHERE use σ

...add HAVING

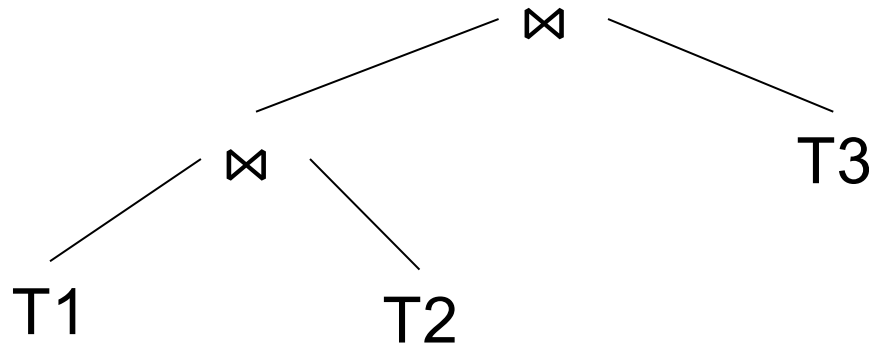
```
SELECT a1,a2,...,agg1,agg2  
FROM T1, T2, ...  
WHERE condition1  
GROUP BY a1,a2,...  
HAVING condition2
```

$\sigma_{\text{condition2}}$

$\gamma_{a1,a2,...,agg1,agg2,agg3,...}$

$\sigma_{\text{condition1}}$

$\vdots$



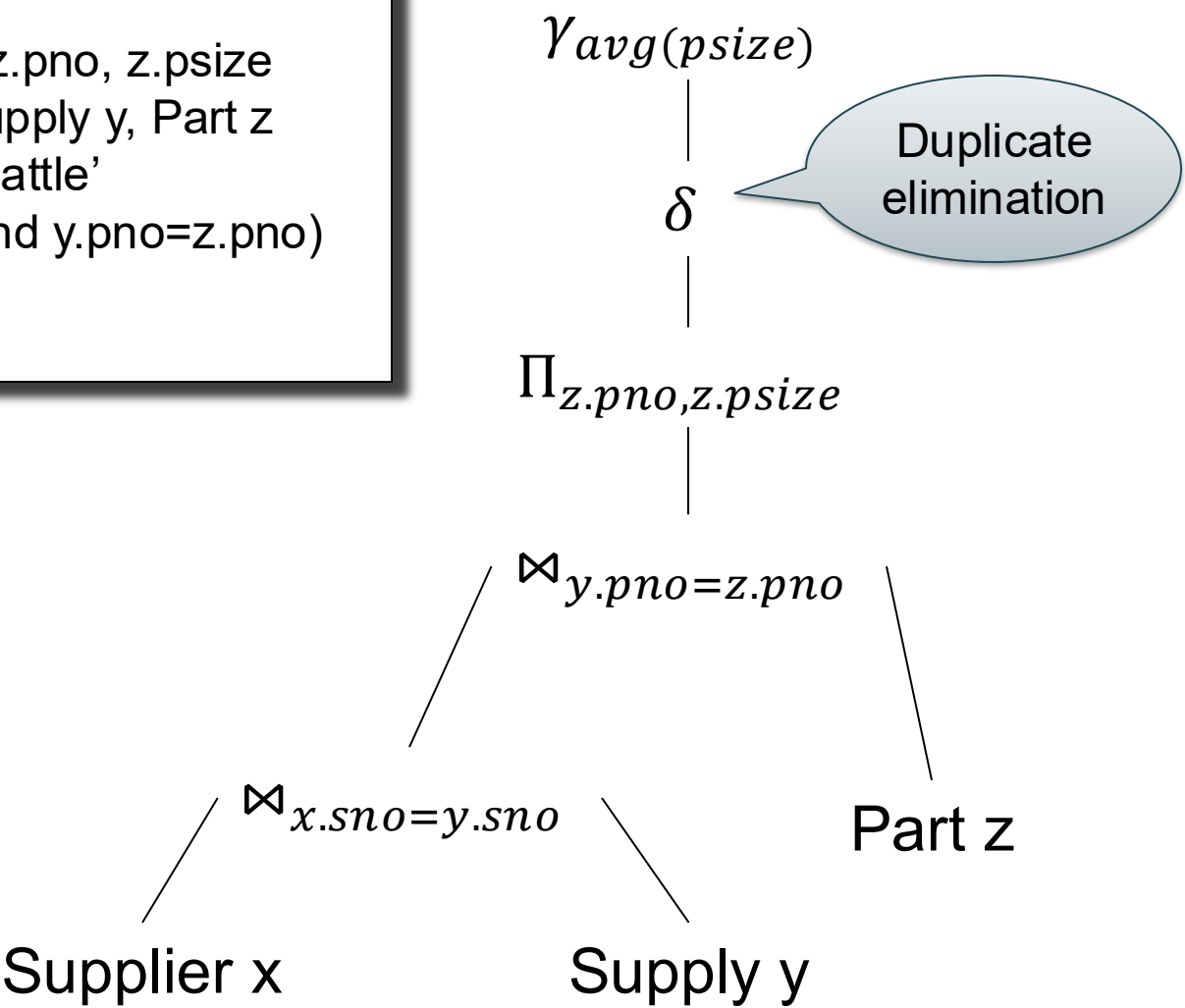
SQL to RA

- SQL queries without subqueries are straightforward to translate
- Subqueries may need to be flattened, then translated to SQL -- next

Supplier (sno, sname, scity, sstate)
Supply (sno, pno, qty, price)
Part (pno, pname, psize, pcolor)

Subqueries

```
WITH Tmp AS (  
    SELECT DISTINCT z.pno, z.psize  
    FROM Supplier x, Supply y, Part z  
    WHERE x.scity = 'Seattle'  
           and x.sno=y.sno and y.pno=z.pno)  
SELECT avg(psize)  
FROM Tmp;
```



Supplier (sno, sname, scity, sstate)

Supply (sno, pno, qty, price)

Part (pno, pname, psize, pcolor)

Subqueries

Find all suppliers in 'WA'
that supply only parts
under \$100

Supplier(sno, sname, scity, sstate)

Supply(sno, pno, qty, price)

Part(pno, pname, psize, pcolor)

Subqueries

```
SELECT x.sno
FROM Supplier x
WHERE x.sstate = 'WA'
      and not exists
      (SELECT *
       FROM Supply y
       WHERE x.sno = y.sno
        and y.price > 100)
```

Find all suppliers in 'WA'
that supply only parts
under \$100

Supplier (sno, sname, scity, sstate)
Supply (sno, pno, qty, price)
Part (pno, pname, psize, pcolor)

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SELECT x.sno
FROM Supplier x
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       FROM Supply y
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```

Find all suppliers in 'WA'
that supply only parts
under \$100

Translate to RA

Supplier(sno, sname, scity, sstate)
Supply(sno, pno, qty, price)
Part(pno, pname, psize, pcolor)

Subqueries

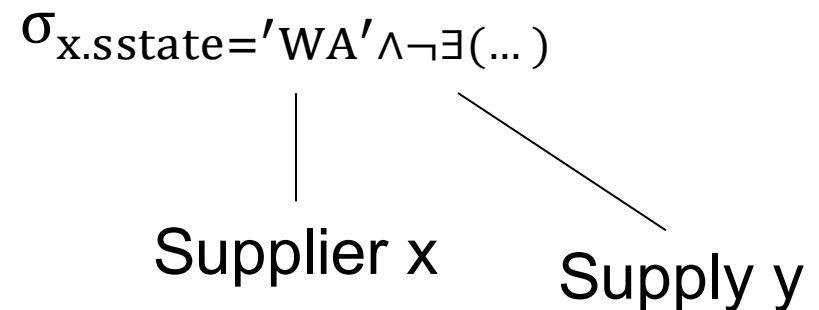
```
SELECT x.sno
FROM Supplier x
WHERE x.sstate = 'WA'
      and not exists
      (SELECT *
       FROM Supply y
       WHERE x.sno = y.sno
            and y.price > 100)
```

Supplier x

Supplier(sno, sname, scity, sstate)
Supply(sno, pno, qty, price)
Part(pno, pname, psize, pcolor)

Subqueries

```
SELECT x.sno
FROM Supplier x
WHERE x.sstate = 'WA'
    and not exists
    (SELECT *
     FROM Supply y
     WHERE x.sno = y.sno
          and y.price > 100)
```



Supplier(sno, sname, scity, sstate)
Supply(sno, pno, qty, price)
Part(pno, pname, psize, pcolor)

Subqueries

```
SELECT x.sno
FROM Supplier x
WHERE x.sstate = 'WA'
    and not exists
    (SELECT *
     FROM Supply y
     WHERE x.sno = y.sno
          and y.price > 100)
```

$\sigma_{x.sstate='WA' \wedge \neg \exists (...)}$

Supplier x

Supply y

Totally wrong!!

Supplier(sno, sname, scity, sstate)
Supply(sno, pno, qty, price)
Part(pno, pname, psize, pcolor)

Subqueries

```
SELECT x.sno
FROM Supplier x
WHERE x.sstate = 'WA'
    and not exists
    (SELECT *
     FROM Supply y
     WHERE x.sno = y.sno
        and y.price > 100)
```

Need to unnest

Totally wrong!!

$\sigma_{x.sstate='WA' \wedge \neg \exists (...)}$

Supplier x

Supply y

Supplier (sno, sname, scity, sstate)
Supply (sno, pno, qty, price)
Part (pno, pname, psize, pcolor)

Subqueries

```
SELECT x.sno
FROM Supplier x
WHERE x.sstate = 'WA'
    and not exists
    (SELECT *
     FROM Supply y
     WHERE x.sno = y.sno
        and y.price > 100)
```

Need to unnest

Correlation !

Supplier (sno, sname, scity, sstate)
Supply (sno, pno, qty, price)
Part (pno, pname, psize, pcolor)

Subqueries

```
SELECT x.sno
FROM Supplier x
WHERE x.sstate = 'WA'
      and not exists
      (SELECT *
       FROM Supply y
       WHERE x.sno = y.sno
              and y.price > 100)
```

De-Correlation

```
SELECT x.sno
FROM Supplier x
WHERE x.sstate = 'WA'
      and x.sno not in
      (SELECT y.sno
       FROM Supply y
       WHERE y.price > 100)
```

Supplier (sno, sname, scity, sstate)
Supply (sno, pno, qty, price)
Part (pno, pname, psize, pcolor)

Subqueries

Un-nest

```
(SELECT x.sno  
FROM Supplier x  
WHERE x.sstate = 'WA')  
EXCEPT  
(SELECT y.sno  
FROM Supply y  
WHERE y.price > 100)
```

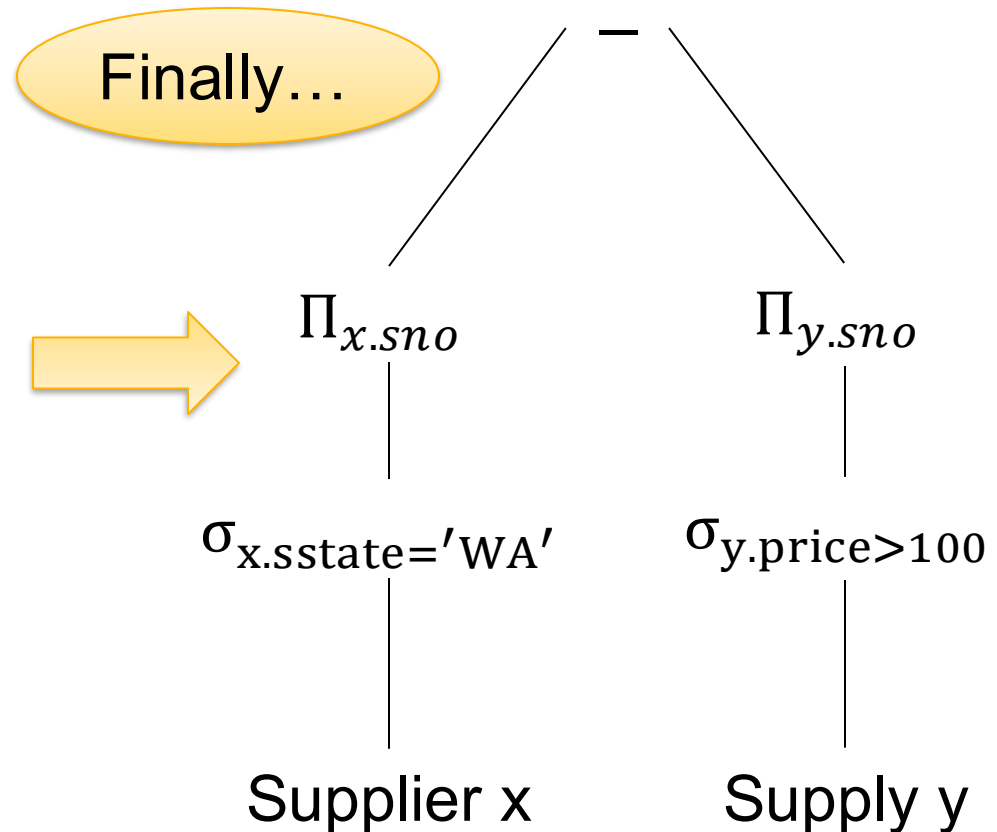
```
SELECT x.sno  
FROM Supplier x  
WHERE x.sstate = 'WA'  
and x.sno not in  
      (SELECT y.sno  
FROM Supply y  
WHERE y.price > 100)
```

EXCEPT = set difference

Supplier(sno, sname, scity, sstate)
Supply(sno, pno, qty, price)
Part(pno, pname, psize, pcolor)

Subqueries

```
(SELECT x.sno
FROM Supplier x
WHERE x.sstate = 'WA')
EXCEPT
(SELECT y.sno
FROM Supply y
WHERE y.price > 100)
```



Summary

- User writes in SQL
 - Declarative language
 - Users say WHAT they want
- System: SQL $\rightarrow$ Relational Algebra
 - Explicit operation order: HOW to compute
 - RA expression a.k.a. Query Plan
- Query Plan: is optimized, then **executed**