# CSE544 <br> Data Management 

## Lectures 4-6 <br> Query Execution

## Announcements

- HW1 due on Friday
- No lecture on Monday
- Review 2 due on Wednesday (Ch. 1\&2 only)
- Project groups by next Friday (email to me)


## Outline for the Next 3 Lectures

- Architecture of a DBMS
- Steps involved in processing a query
- Main Memory Operators
- Storage
- External Memory Operators


## Architecture of DBMS



## Warning: it will be confusing...

DBMS are monoliths: components cannot be isolated

- Good news:
- Hole system has rich functionality and is efficient
- Bad news:
- Hard to discuss components in isolation


## Multiple Processes



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## Why Multiple Processes

- DBMS listens to requests from clients
- Each request = one SQL command
- Handles multiple requests concurrently; multiple processes


## Process Models

- Process per DBMS worker
- Thread per DBMS worker
- Process pool

Next week's review:
Discuss pro/cons for each model

## Outline

- Architecture of a DBMS
- Steps involved in processing a query
- Main Memory Operators
- Storage
- External Memory Operators


## Query Optimization



## Lifecycle of a Query

SQL query
Parse \& Rewrite Query


# Example Database Schema 

View: Suppliers in Seattle
CREATE VIEW NearbySupp AS
SELECT sno, sname FROM Supplier
WHERE scity='Seattle' AND sstate='WA'

## Example Query

## - Find the names of all suppliers in Seattle who supply part number 2

## SELECT sno, sname FROM NearbySupp WHERE sno IN (SELECT sno <br> FROM Supply <br> WHERE pno = 2 )

## Lifecycle of a Query (1)

- Step 0: admission control
- User connects to the db with username, password
- User sends query in text format
- Step 1: Query parsing
- Parses query into an internal format
- Performs various checks using catalog: Correctness, authorization, integrity constraints
- Step 2: Query rewrite
- View rewriting, flattening, decorrelation, etc.


## View Rewriting, Flattening

## Original query:

SELECT sno, sname FROM NearbySupp<br>WHERE sno IN (SELECT sno FROM Supply WHERE pno = 2 )

View rewriting
= view inlining
= view expansion
Flattening
= unnesting

## View Rewriting, Flattening

## Original query:

SELECT sno, sname
FROM NearbySupp
WHERE sno IN (SELECT sno
FROM Supply
WHERE pno = 2 )

View rewriting
= view inlining
= view expansion
Flattening
= unnesting

## Rewritten query:

```
SELECT S.sno, S.sname
FROM Supplier S, Supply U
WHERE S.scity='Seattle' AND S.sstate='WA'
AND S.sno = U.sno
AND U.pno = 2;
```

Supplier(sno,sname,scity,sstate) Part(pno,pname,psize,pcolor)
Supply(sno,pno,price)

## Decorrelation

## Find all suppliers in 'WA' that supply only parts under $\$ 100$

## Supplier(sno,sname,scity,sstate)

Part(pno,pname,psize,pcolor)
Supply(sno,pno,price)

## Decorrelation

SELECT Q.sno
FROM Supplier Q
WHERE Q.sstate = 'WA' and not exists (SELECT*
FROM Supply P
WHERE P.sno = Q.sno and P.price > 100)

Find all suppliers in 'WA' that supply only parts under \$100

Supplier(sno,sname,scity,sstate)
Part(pno,pname,psize,pcolor)
Supply(sno,pno,price)

## Decorrelation



## Supplier(sno,sname,scity,sstate)

Part(pno,pname,psize,pcolor)
Supply(sno,pno,price)

## Decorrelation

## De-Correlation

SELECT Q.sno FROM Supplier Q WHERE Q.sstate = 'WA' and Q.sno not in<br>(SELECT P.sno<br>FROM Supply P<br>WHERE P.price > 100)

## Supplier(sno,sname,scity,sstate)

Part(pno,pname,psize,pcolor)
Supply(sno,pno,price)

## Decorrelation

> (SELECT Q.sno FROM Supplier Q WHERE Q.sstate = 'WA') EXCEPT (SELECT P.sno FROM Supply P WHERE P.price > 100)

## EXCEPT = set difference

## SELECT Q.sno FROM Supplier Q <br> WHERE Q.sstate = 'WA' and Q.sno not in <br> (SELECT P.sno <br> FROM Supply P <br> WHERE P.price > 100)

Supplier(sno,sname,scity,sstate)
Part(pno,pname,psize,pcolor)
Supply(sno,pno,price)

## Decorrelation

## (SELECT Q.sno FROM Supplier Q WHERE Q.sstate = 'WA') EXCEPT (SELECT P.sno FROM Supply P WHERE P.price > 100)

Finally...


## Lifecycle of a Query (2)

- Step 3: Query optimization
- Find an efficient query plan for the query
- We will spend two lectures on this topic
- A query plan is
- Logical query plan: a relational algebra tree
- Physical query plan: add specific algorithms


## Five Basic Relational Operators

- Selection: $\sigma_{\text {condition }}(\mathrm{S})$
- Projection: $\pi_{\text {list-of-attributes }}(\mathrm{S})$
- Union (U)
- Set difference (-),
- Cross-product/cartesian product ( $\times$ ), Join: $R \bowtie_{\boldsymbol{\theta}} \mathrm{S}=\sigma_{\boldsymbol{\theta}}(\mathrm{R} \times \mathrm{S})$

Other operators: semi-join, anti-semijoin

## Extended Operators of Relational Algebra

- Duplicate elimination ( $\delta$ )
- Convert a bag to a set
- Can be expressed as a group-by $\gamma$
- Group-by/aggregate ( $\gamma$ )
- Example: $\quad \gamma_{\text {pcolor, } \max (\text { psize }) \rightarrow \mathrm{m}, \operatorname{avg}(\mathrm{psize}) \rightarrow \mathrm{s}}$ (Part)
- Min, max, sum, average, count
- Partitions tuples of a relation into "groups"
- Aggregates can then be applied to groups
- Sort operator $(\tau)$

Supplier(sno,sname,scity,sstate) Part(pno,pname,psize,pcolor) Supply(sno,pno,price)

## Logical Query Plan

SELECT x.sname FROM Supplier x, Supply y WHERE x.sno=y.sno and x.scity='Seattle’ and $x . s s t a t e=' W A ’$ and y.pno=2

Supplier(sno,sname,scity,sstate)
Part(pno,pname,psize,pcolor)
Supply(sno,pno,price)

## LoOiçi Purn Pr

$\pi$ sname
$\mid$
$\sigma$ sscity=‘Seattle' $\wedge$ sstate='WA' $\wedge$ pno=2
SELECT x.sname FROM Supplier x, Supply y WHERE x.sno=y.sno and $x . s c i t y=$ 'Seattle' and x.sstate='WA' and y.pno=2

## Supplier



Supplier(sno,sname,scity,sstate) Part(pno,pname,psize,pcolor)
Supply(sno,pno,price)

## LOOIC? (xuery Din



Supplier(sno,sname,scity,sstate)
Part(pno,pname,psize,pcolor)
Supply(sno,pno,price)

## Physical Query Plan

(On the fly)
$\pi$ sname
(On the fly) $\sigma_{\text {sscity }}=‘$ Seattle' $\wedge$ sstate $=' W A ' \wedge$ pno $=2$
(Nested loop)


Supplier
(File scan)
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Physical plan= Logical plan + choice of algorithms + choice of access path

## Final Step in Query Processing <br> - Step 4: Query execution

- Choice of algorithm
- How to pass data between operators, e.g. materialized, or pipelined


## Outline

- Architecture of a DBMS
- Steps involved in processing a query
- Main Memory Operators
- Storage
- External Memory Operators


## Multiple Processes



## Physical Operators

- For each operator, several algorithms
- Main memory or external memory

Supplier(sid, sname, scity, sstate) Supply(sid, pno, quantity)

## Main Memory Algorithms

Logical operator:
Supplier $\bowtie_{\text {sid=sid }}$ Supply

Three algorithms:

1. Nested Loops
2. Hash-join
3. Merge-join

Supplier(sid, sname, scity, sstate) Supply(sid, pno, quantity)

## 1. Nested Loop Join

Logical operator:
Supplier $\bowtie_{\text {sid=sid }}$ Supply

## for x in Supplier do for $y$ in Supply do if $x$.sid $=y . s i d$ then output $(x, y)$

Supplier(sid, sname, scity, sstate) Supply(sid, pno, quantity)

## 1. Nested Loop Join

Logical operator:
Supplier $\bowtie_{\text {sid=sid }}$ Supply

## for x in Supplier do for $y$ in Supply do if $x$.sid $=y . s i d$ then output( $\mathrm{x}, \mathrm{y}$ )

If $|\mathrm{R}|=|\mathrm{S}|=\mathrm{n}$,
what is the runtime?

Supplier(sid, sname, scity, sstate) Supply(sid, pno, quantity)

## 1. Nested Loop Join

Logical operator:
Supplier $\bowtie_{\text {sid=sid }}$ Supply

## for x in Supplier do

 for $y$ in Supply do if x .sid $=\mathrm{y}$.sid then output( $x, y$ )If $|R|=|S|=n$,
what is the runtime?
$O\left(n^{2}\right)$

## BRIEF Review of Hash Tables Separate chaining:



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A (naïve) hash function: 0 $h(x)=x \bmod 10$

Operations:
find $(103)=$ ?? insert(488) $=$ ??


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Operations:
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Supplier(sid, sname, scity, sstate) Supply(sid, pno, quantity)

## 2. Hash Join

Logical operator:
Supply $\bowtie_{\text {sid=sid }}$ Supplier

for $x$ in Supplier do insert(x.sid, x)<br>for y in Supply do<br>$x=$ find(y.sid); output(x,y);

Supplier(sid, sname, scity, sstate) Supply(sid, pno, quantity)

## 2. Hash Join

Logical operator:
Supply $\bowtie_{\text {sid=sid }}$ Supplier

$$
\begin{aligned}
& \text { for } \mathrm{x} \text { in Supplier do } \\
& \text { insert(x.sid, } \mathrm{x}) \\
& \\
& \text { for } \mathrm{y} \text { in Supply do } \\
& \text { x = find(y.sid); } \\
& \text { output( } \mathrm{x}, \mathrm{y}) ; \\
& \hline
\end{aligned}
$$

If $|R|=|S|=n$,
what is the runtime?

Supplier(sid, sname, scity, sstate) Supply(sid, pno, quantity)

## 2. Hash Join

Logical operator:
Supply $\bowtie_{\text {sid=sid }}$ Supplier

## for $x$ in Supplier do insert(x.sid, x)

for $y$ in Supply do
$x=$ find( $\mathrm{y} . \mathrm{sid}$ ); output(x,y);

If $|\mathrm{R}|=|\mathrm{S}|=\mathrm{n}$, what is the runtime?
$\mathrm{O}(\mathrm{n})$

Supplier(sid, sname, scity, sstate) Supply(sid, pno, quantity)

## 2. Hash Join

Logical operator:
Supplier $\bowtie_{\text {sid=sid }}$ Supply

## Change join order

for y in Supply do insert(y.sid, y)
for x in Supplier do ????

Supplier(sid, sname, scity, sstate) Supply(sid, pno, quantity)

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## for y in Supply do insert(y.sid, y)

for x in Supplier do
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If $|\mathrm{R}|=|\mathrm{S}|=\mathrm{n}$, what is the runtime?
for $x$ in Supplier do
for $y$ in find(x.sid) do
$\mathrm{O}(\mathrm{n})$
But can be $\mathrm{O}\left(\mathrm{n}^{2}\right)$ why? output(x,y);

Supplier(sid, sname, scity, sstate) Supply(sid, pno, quantity)

## 2. Hash Join

Why would we change the order?
Logical operator:
Supplier $\bowtie_{\text {sid=sid }}$ Supply

If $|R|=|S|=n$,
what is the runtime?
for $x$ in Supplier do
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Supplier(sid, sname, scity, sstate) Supply(sid, pno, quantity)

## 2. Hash Join

Why would we change the order?
Logical operator:
Supplier $\bowtie_{\text {sid=sid }}$ Supply

## When |Supply| << |Supplier|

## for y in Supply do insert(y.sid, y)

If $|\mathrm{R}|=|\mathrm{S}|=\mathrm{n}$,
what is the runtime?
for x in Supplier do
for $y$ in find(x.sid) do
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Supplier(sid, sname, scity, sstate) Supply(sid, pno, quantity)

## 3. Merge Join

Logical operator:
Supplier $\bowtie_{\text {sid=sid }}$ Supply Sort(Supplier); Sort(Supply); x = Supplier.first();
y = Supply.first();

Supplier(sid, sname, scity, sstate) Supply(sid, pno, quantity)

## 3. Merge Join

Logical operator:
Supplier $\bowtie_{\text {sid=sid }}$ Supply
Sort(Supplier); Sort(Supply); x = Supplier.first();
y = Supply.first();
while y != NULL do
case:
x.sid < y.sid: ???
x.sid = y.sid: ???
x.sid > y.sid: ???

Supplier(sid, sname, scity, sstate) Supply(sid, pno, quantity)

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y = Supply.first();
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case:
x.sid < y.sid: x = x.next()
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x.sid = y.sid: output(x,y); y = y.next(); x.sid > y.sid: ???

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$x . \operatorname{sid}>y . s i d: y=y . n e x t() ;$

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## Announcements

- Project teams due by Friday (email to me)
- HW2 posted, we use Snowflake
- Consider using Snowflake in your project!
- Architecture paper was due today


## Discuss Architecture Paper



## Recap: Main Memory Algorithms

- Join $\bowtie$ :
- Nested loop join
- Hash join
- Merge join
- Selection $\sigma$
- "on-the-fly"
- Index-based selection (next lecture)
- Group by $\gamma$
- Hash-based
- Merge-based

Briefly discuss
in class

## How Do We Combine Them?



## How Do We Combine Them?

The Iterator Interface

- open()
- next()

- close()

R

## Implementing Query Operators with the Iterator Interface

interface Operator \{

# Implementing Query Operators with the Iterator Interface 

```
interface Operator {
    // initializes operator state
    // and sets parameters
    void open (...);
```


## Implementing Query Operators with the Iterator Interface

```
interface Operator {
    // initializes operator state
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void open (...);
// calls next() on its inputs
// processes an input tuple
// produces output tuple(s)
// returns null when done
Tuple next ();
```


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```
// cleans up (if any)
```

// cleans up (if any)
void close ();
void close ();
}

```

\title{
Implementing Query Operators with the Iterator Interface
}

Example "on the fly" selection operator
```

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# Implementing Query Operators with the Iterator Interface 

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Tuple next ();
// cleans up (if any)
}
void close ();
        class Select implements Operator \{...
    void open (Predicate p,
                            Operator c) \{
        this.p = p; this.c = c; c.open();
        \}
    Tuple next () \{

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Tuple next ();
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void close ();

```
class Select implements Operator {...
    void open (Predicate p,
            Operator c) {
    this.p = p; this.c = c; c.open();
    }
    Tuple next () {
    boolean found = false;
    Tuple r = null;
    while (!found) {
        r = c.next();
        if (r == null) break;
        found = p(r);
    }
    return r;
    }

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    while (!found) {
        r = c.next();
        if (r == null) break;
        found = p(r);
    }
    return r;
}
void close () { c.close(); }
}
```


## Implementing Query Operators with the Iterator Interface

```
interface Operator {
```

    // initializes operator state
    // and sets parameters
    void open (...);
    // calls next() on its inputs
    // processes an input tuple
    // produces output tuple(s)
    // returns null when done
    Tuple next ();
    // cleans up (if any)
void close ();

## Query plan execution

```
Operator q = parse("SELECT ...");
```

q = optimize(q);
q.open();
while (true) \{
Tuple t = q.next();
if (t == null) break;
else printOnScreen(t);
\}
q.close();

Supplier(sid, sname, scity, sstate) supply(sid, pno, quantity)Pipelining
(On the fly) $\Pi_{\text {sname }}$

Discuss: open/next/close for nested loop join
(On the fly $\phi_{\text {scity }}$ = 'Seattle' and sstate= 'WA' and pno=2
(Nested loop)


## Supply <br> (File scan)

Supplier
(File scan)

Supplier(sid, sname, scity, sstate) supply(sid, pno, quantity)Pipelining
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(On the fly , $_{\text {scity }}$ 'seate, next()
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Discuss: open/next/close for nested loop join
(On the fly , $_{\text {scity }}$ 'seate, next()
(On the $l y \phi_{\text {scity }}=$ 'Seattle' and sstate= 'WA' and pno=2
(Nested loop)


Supplier(sid, sname, scity, sstate) supply(sid, pno, quantity)Pipelining
(On the fly)

$\Pi_{\text {sname }}$

## Discuss hash-join in class

(On the fly $\phi_{\text {scity }}$ = 'Seattle' and sstate= 'WA' and pno=2
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## Supply <br> (File scan)

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(File scan)

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(File scan)

Supplier(sid, sname, scity, sstate)
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Supplier
(File scan)

## Pipeline v.s. Blocking

- Pipeline
- A tuple moves all the way through up the query plan
- Advantages: speed
- Disadvantage: need all hash tables in memory
- Blocking
- Compute and store on disk entire subplan
- Advantage: needs less memory
- Disadvantage: slower


## Outline

- Architecture of a DBMS
- Steps involved in processing a query
- Main Memory Operators
- Storage
- External Memory Operators


## Multiple Processes



## The Mechanics of Disk

Mechanical characteristics:
Cylinder

- Rotation speed (5400RPM) Disk head
- Number of platters (1-30)
- Number of tracks (<=10000)
- Number of bytes/track(105)

Unit of read or write: disk block
Once in memory: page
Typically: 4k or 8k or 16k

## Student

## Data Storage

- DBMSs store data in files

| ID | fName | IName |
| :--- | :--- | :--- |
| 10 | Tom | Hanks |
| 20 | Amy | Hanks |
| $\ldots$ |  |  |

- Most common organization is row-wise storage
- On disk, a file is split into blocks
- Each block contains a set of tuples

| 10 | Tom | Hanks |
| :--- | :--- | :--- |
| 20 | Amy | Hanks |
| block 1 |  |  |


| 50 | $\ldots$ | $\ldots$ |
| :--- | :--- | :--- |
| 200 | $\ldots$ |  | block 2


| 220 |  |  |
| :--- | :--- | :--- |
| 240 |  |  |

block 3

In the example, we have 4 blocks with 2 tuples each
Basic fact: disks always read/write an entire block at a time

## Disk Access Characteristics

- Disk latency
- Time between when command is issued and when data is in memory
- Equals = seek time + rotational latency
- Seek time = time for the head to reach cylinder
- $10 \mathrm{~ms}-40 \mathrm{~ms}$
- Rotational latency $=$ time for the sector to rotate
- Rotation time $=10 \mathrm{~ms}$
- Average latency $=10 \mathrm{~ms} / 2$
- Transfer time = typically $40 \mathrm{MB} / \mathrm{s}$


## Buffer Manager

 Page Requests from Higher Levels

- Data must be in RAM for DBMS to operate on it!
- Table of <frame\#, pageid> pairs is maintained


## Buffer Manager

Needs to decide on page replacement policy

- LRU
- Clock algorithm

Both work well in OS, but not always in DB
Enables the higher levels of the
DBMS to assume that the
needed data is in main memory.

## Arranging Pages on Disk

A disk is organized into blocks (a.k.a. pages)

- blocks on same track, followed by
- blocks on same cylinder, followed by
- blocks on adjacent cylinder

A file should (ideally) consists of sequential blocks on disk, to minimize seek and rotational delay.

For a sequential scan, pre-fetching several pages at a time is a big win!

## Storing Records On Disk

- Page format: records inside a page
- Record format: attributes inside a record
- File Organization


## Page Format

- 1 page = 1 disk block = fixed size (e.g. 8 KB )
- Records:
- Fixed length
- Variable length
- Record id = RID
- Typically RID = (PageID, SlotNumber)

Need RID's for indexes and for transactions

## Page Format Approach 1

Fixed-length records: packed representation
Divide page into slots. Each slot can hold one tuple Record ID (RID) for each tuple is (PageID,SlotNb)
Free space $\quad \mathrm{N}$

How do we insert a new record?
Number of records

## Page Format Approach 1

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Number of records
How do we delete a record?

## Page Format Approach 1

Fixed-length records: packed representation
Divide page into slots. Each slot can hold one tuple
Record ID (RID) for each tuple is (PageID,SlotNb)


How do we insert a new record?
Number of records
How do we delete a record? Cannot remove record (why?) How do we handle variable-length records?

## Page Format Approach 2

 + Need to keep track of nb of slots

Slot directory

+ Also need to keep track of free space (F)
Can handle variable-length records
Can move tuples inside a page without changing RIDs RID is (PageID, SlotID) combination


## Record Formats

Fixed-length records => Each field has a fixed length (i.e., it has the same length in all the records)


Information about field lengths and types is in the catalog

## Record Formats

Variable length records


Remark: NULLS require no space at all (why ?)

## Announcements

- Project teams were due last week
- PAX paper review due on Wednesday
- HW2 Snowflake due on Friday


## Quick Review

- What is the unit of access for RAM*? What is the unit of access for disk? Why the difference?
- What is the Buffer Pool?
- Describe how a table is stored on disk
*RAM = Random Access memory = main memory


## Notes for the PAX paper

Memory hierarchies:


## File Organizations

- Heap (random order) files: Suitable when typical access is a file scan retrieving all records.
- Sequential file (sorted): Best if records must be retrieved in some order, or by a `range’
- Index: Data structures to organize records via trees or hashing.


## Index

- An additional file, that allows fast access to records in the data file given a search key


## Index

- An additional file, that allows fast access to records in the data file given a search key
- The index contains (key, value) pairs:
- Key = an attribute value (e.g., student ID or name)
- Value = a pointer to the record OR the record itself
- Could have many indexes for one table

Key = means here search key

## Actor

\section*{Example 1: Index on ID <br> | ID | fName | IName |
| :--- | :--- | :--- |
| 10 | Tom | Hanks |
| 20 | Amy | Hanks |
| $\ldots$ |  |  | <br> Data File Actor}

Index Actor_ID on Actor.ID


## Actor

Index Actor_fName on Actor.fName

\section*{Example 2: Index on fName <br> | ID | fName | IName |
| :--- | :--- | :--- |
| 10 | Tom | Hanks |
| 20 | Amy | Hanks |
| $\ldots$ |  |  |}



## B+ Tree Index by Example

$$
d=2
$$

Find the key 40


## Clustered vs Unclustered



Every table can have only one clustered and many unclustered indexes Why?

## Index Classification

- Clustered/unclustered
- Clustered = records close in index are close in data
- Option 1: Data inside data file is sorted on disk
- Option 2: Store data directly inside the index (no separate files)
- Unclustered = records close in index may be far in data


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- Meaning 1:
- Primary = is over attributes that include the primary key
- Secondary = otherwise
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- Meaning 2: means the same as clustered/unclustered
- Organization B+ tree or Hash table


## Discussion on Indices

- What they do: speed up disk access What they don't: speed up RAM algo.
- They benefit only SELECT queries that have some predicate $A=\ldots$ or $A<=\ldots$
- They hurt all INSERT/UPDATE/DELETE queries (why?)


## Outline

- Architecture of a DBMS
- Steps involved in processing a query
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- External Memory Operators


## Architecture



## Cost Parameters

- In database systems the data is on disk
- Parameters:
$-B(R)=\#$ of blocks (i.e., pages) for relation $R$
$-T(R)=\#$ of tuples in relation $R$
$-V(R, a)=\#$ of distinct values of attribute a
- M = \# pages available in main memory
- Cost = total number of I/Os
- Convention: writing the final result to disk is not included

Supplier(sid, sname, scity, sstate) Supply(sid, pno, quantity)

## Cost Parameters

Supplier(sid, sname, scity, sstate) Block size $=8 \mathrm{~KB}$

- B (Supplier) $=1,000,000$ blocks $=8 \mathrm{~GB}$
- T (Supplier) $=50,000,000$ records $\sim 50$ / block
- $V($ Supplier, sname) $=$
- $\mathrm{V}($ Supplier, scity $)=$
- V(Supplier, sstate) =

Supplier(sid, sname, scity, sstate) Supply(sid, pno, quantity)

## Cost Parameters

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~ 50 / block
why?

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- B (Supplier) $=1,000,000$ blocks
= 8GB
- T (Supplier) $=50,000,000$ records
- $V($ Supplier, sid $)=50,000,000$
- $\mathrm{V}($ Supplier, sname $)=40,000,000$
~ 50 / block
why?
meaning?

Supplier(sid, sname, scity, sstate) Supply(sid, pno, quantity)

## Cost Parameters

Supplier(sid, sname, scity, sstate) Block size $=8 \mathrm{~KB}$

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- T (Supplier) $=50,000,000$ records
- $V($ Supplier, sid $)=50,000,000$
- $\mathrm{V}($ Supplier, sname $)=40,000,000$
~ 50 / block
why?
meaning?
- $\mathrm{V}($ Supplier, scity $)=860$

Supplier(sid, sname, scity, sstate) Supply(sid, pno, quantity)

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~ 50 / block
why?
meaning?
- $\mathrm{V}($ Supplier, scity $)=860$
- $\mathrm{V}($ Supplier, sstate $)=50$
why?


## Cost Parameters

Supplier(sid, sname, scity, sstate) Block size $=8 \mathrm{~KB}$

- $B($ Supplier $)=1,000,000$ blocks
- $T$ (Supplier) $=50,000,000$ records
- $V($ Supplier, sid $)=50,000,000$
- $V($ Supplier, sname $)=40,000,000$
- $\mathrm{V}($ Supplier, scity $)=860$
- $\mathrm{V}($ Supplier, sstate $)=50$
- $M=10,000,000=80 G B$
= 8GB
~ 50 / block
why?
meaning?
why?
why so little?


## SELECT *

## ndex Based Selection

Selection on equality: $\quad \sigma_{a=v}(R)$
$V(R, a)=\#$ of distinct values of attribute a

Cost of index-based selection:

- Clustered index on a:
- Unclustered index on a:


## ndex Based Selection

Selection on equality: $\quad \sigma_{a=v}(R)$
$\mathrm{V}(\mathrm{R}, \mathrm{a})=$ \# of distinct values of attribute a
Assumptions:

- Values are uniformly distributed
- Ignore the cost of reading the index (why?)

Cost of index-based selection:

- Clustered index on a:
- Unclustered index on a:


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$\mathrm{V}(\mathrm{R}, \mathrm{a})=$ \# of distinct values of attribute a
Assumptions:

- Values are uniformly distributed
- Ignore the cost of reading the index (why?)

Cost of index-based selection:

- Clustered index on a:

$$
\begin{aligned}
& \text { cost }=B(R) / V(R, a) \\
& \text { cost }=T(R) / V(R, a)
\end{aligned}
$$

- Unclustered index on a:


## SELECT *

## Index Based Selection

- Example:

$$
\begin{aligned}
& B(R)=2000 \\
& T(R)=100,000 \\
& V(R, a)=20
\end{aligned}
$$

- Table scan (assuming $R$ is clustered)
- Index based selection
- If index is clustered:
- If index is unclustered:


## SELECT *

## ndex Based Selection

- Example:

$$
\begin{aligned}
& B(R)=2000 \\
& T(R)=100,000 \\
& V(R, a)=20
\end{aligned}
$$

- Table scan (assuming $R$ is clustered)
- $\mathrm{B}(\mathrm{R})=2,000 \mathrm{I} / \mathrm{Os}$
- Index based selection
- If index is clustered:
- If index is unclustered:


## ndex Based Selection

- Example:

$$
\begin{aligned}
& \mathrm{B}(\mathrm{R})=2000 \\
& \mathrm{~T}(\mathrm{R})=100,000 \\
& \mathrm{~V}(\mathrm{R}, \mathrm{a})=20
\end{aligned}
$$

- Table scan (assuming $R$ is clustered)
- $\mathrm{B}(\mathrm{R})=2,000 \mathrm{I} / \mathrm{Os}$
- Index based selection
- If index is clustered: $B(R) / V(R, a)=1001 / O s$
- If index is unclustered:


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- Example:

$$
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$$

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- $\mathrm{B}(\mathrm{R})=2,000 \mathrm{I} / \mathrm{Os}$
- Index based selection
- If index is clustered: $B(R) / V(R, a)=1001 / O s$
- If index is unclustered: $T(R) / V(R, a)=5,000$ I/Os


## ndex Based Selection

- Example:

$$
\begin{aligned}
& B(R)=2000 \\
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$$

- Table scan (assuming $R$ is clustered)


## The 2\% rule!

$-B(R)=2,000$ I/Os

- Index based selection
- If index is clustered: $B(R) / V(R, a)=1001 / O s$
- If index is unclustered: $T(R) / V(R, a)=5,000$ I/Os
- Lesson
- Don't build unclustered indexes when $\mathrm{V}(\mathrm{R}, \mathrm{a})$ is small!


## To Cluster or Not

Remember:

- Rule of thumb: Random reading 1-2\% of file $\approx$ sequential scan entire file;

Range queries benefit mostly from clustering because they may read more than 1-2\%


Percentage tuples retrieved


Percentage tuples retrieved


Percentage tuples retrieved


Percentage tuples retrieved

## External Memory Joins

- Nested loop join
- Index join, a.k.a. index nested loop join
- Partitioned hash-join, a.k.a. grace join
- Merge-join


## Nested Loop Joins

- $R \bowtie S$
- Naïve nested loop joint: $T(R)$ * $B(S)$ I/Os? WHY? Of course, can switch order: $B(R)$ * $T(S)$
- We can be much cleverer by using the available main memory: M
- Assume $|\mathrm{R}| \gg|\mathrm{S}|$. (Outer relation is bigger than inner relation)


## Block Nested Loop Join

- Group of (M-2) pages of $S$ is called a "block"
for each (M-2) pages ps of S do for each page pr of R do
for each tuple s in ps
for each tuple $r$ in pr do
if $r$ and $s$ join then output $(r, s)$


## Block Nested Loop Join



## Nested Loop Joins

Cost of block-based nested loop join

- Read S once:

$$
B(S)
$$

- Outer loop runs $B(S) /(M-2)$ times, each iteration reads the entire $R$ : $\quad B(S) B(R) /(M-2)$
- Total cost:

$$
B(S)+B(S) B(R) /(M-2)
$$

## Nested Loop Joins

Cost of block-based nested loop join

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- Total cost:

$$
B(S)+B(S) B(R) /(M-2)
$$

Iterate over the smaller relation first!

## Index Nested Loop Join

$R \bowtie S$

- Assume $S$ has an index on the join attribute
- Iterate over R, for each tuple fetch corresponding tuple(s) from $S$
- Cost:
- If index on $S$ is clustered: $\quad B(R)+T(R) B(S) / V(S, a)$
- If index on $S$ is unclustered: $\quad B(R)+T(R) T(S) / V(S, a)$


## Two Pass Algorithms

- Idea: partition a relation R into buckets, on disk



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- Each bucket has size approx. $B(R) / M$



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- Each bucket has size approx. $B(R) / M$



## Partitioned (Grace) Hash Join

$R \bowtie S$

- Step 1:
- Hash S into M-1 buckets
- Send all buckets to disk
- Step 2
- Hash R into M-1 buckets
- Send all buckets to disk
- Step 3
- Join every pair of buckets


## Partition R using hash fn h

$R \bowtie S$


## Partition S using hash fn h

$R \bowtie S$


## Partitioned Hash Join

## $R \bowtie S$

- Read in partition of S, hash it using h2 ( $\neq$ h)
- Scan same partition of $R$, search for matches



## Partitioned Hash Join

- Cost: 3B(R) + 3B(S)
- Assumption: $\min (B(R), B(S)) \leq M^{2}$


## Hybrid Hash Join Algorithm

- Assume we have extra memory available
- Partition S into k buckets $t$ buckets $S_{1}, \ldots, S_{t}$ stay in memory
k-t buckets $\mathrm{S}_{\mathrm{t}+1}, \ldots, \mathrm{~S}_{\mathrm{k}}$ to disk
- Partition R into k buckets
- First t buckets join immediately with S
- Rest k-t buckets go to disk
- Finally, join k-t pairs of buckets:

$$
\left(R_{t+1}, S_{t+1}\right),\left(R_{t+2}, S_{t+2}\right), \ldots,\left(R_{k}, S_{k}\right)
$$

## Hybrid Hash Join Algorithm

How to choose k and t ?

- The first t buckets must fin in $M$ : $t / k * B(S) \leq M$


## Hybrid Hash Join Algorithm

How to choose k and t ?

- The first t buckets must fin in $M$ : $\quad t / k * B(S) \leq M$
- Need room for k-t additional pages: k-t $\leq \mathrm{M}$


## Hybrid Hash Join Algorithm

How to choose $k$ and $t$ ?

- The first t buckets must fin in $M$ : $\quad t / k * B(S) \leq M$
- Need room for k-t additional pages: k-t $\leq \mathrm{M}$
- Thus:
$t / k$ * $B(S)+k-t \leq M$


## Hybrid Hash Join Algorithm

How to choose k and t ?

- The first t buckets must fin in $M$ : $\quad t / k * B(S) \leq M$
- Need room for k-t additional pages: k-t $\leq \mathrm{M}$
- Thus:
$t / k$ * $B(S)+k-t \leq M$

Assuming t/k * $\mathrm{B}(\mathrm{S}) \gg \mathrm{k}-\mathrm{t}$ :
$t / k=M / B(S)$

## Hybrid Hash Join Algorithm

- How many I/Os?
- Cost of partitioned hash join: $3 B(R)+3 B(S)$
- Hybrid join saves $2 \mathrm{I} / \mathrm{Os}$ for a $\mathrm{t} / \mathrm{k}$ fraction of buckets
- Hybrid join saves $2 t / k(B(R)+B(S)) \quad I / O s$

Cost: $(3-2 t / k)(B(R)+B(S))=(3-2 M / B(S))(B(R)+B(S))$

## External Sorting

- Problem: Sort a file of size B with memory M
- Where we need this:
- ORDER BY in SQL queries
- Several physical operators
- Bulk loading of B+-tree indexes.
- Will discuss only 2-pass sorting, for when $\mathrm{B} \leq \mathrm{M}^{2}$


## External Merge-Sort: Step 1

- Phase one: load M pages in memory, sort



## External Merge-Sort: Step 2

- Merge $\mathrm{M}-1$ runs into a new run
- Result: runs of length $M(M-1) \approx M^{2}$


Assuming $\mathrm{B} \leq \mathrm{M}^{2}$, we are done

## External Merge-Sort

- Cost:
- Read+write+read $=3 B(R)$
- Assumption: $B(R)<=M^{2}$
- Other considerations
- In general, a lot of optimizations are possible


## Two-Pass Algorithms Based on Sorting

Grouping: $\gamma_{\mathrm{a}, \operatorname{sum}(\mathrm{b})}(\mathrm{R})$

Sort, then compute the sum(b) for each group of a's

- Step 1: sort chunks of size M, write
- cost 2B(R)
- Step 2: merge M-1 runs, combining groups by addition
- cost $B(R)$
- Total cost: $3 B(R)$, Assumption: $B(R) \leq M^{2}$


## Two-Pass Algorithms Based on Sorting

Join $R \bowtie S$

- Start by creating initial runs of length $M$, for $R$ and $S$ :
- Cost: 2B(R)+2B(S)
- Merge (and join) $M_{1}$ runs from $R, M_{2}$ runs from $S$ :
- Cost: $\mathrm{B}(\mathrm{R})+\mathrm{B}(\mathrm{S})$
- Total cost: $3 \mathrm{~B}(\mathrm{R})+3 \mathrm{~B}(\mathrm{~S})$
- Assumption:
- $R$ has $M_{1}=B(R) / M$ runs, $S$ has $M_{2}=B(S) / M$ runs
- $\mathrm{M}_{1}+\mathrm{M}_{2} \leq \mathrm{M}$
- Hence: $B(R)+B(S) \leq M^{2}$


## Summary of External Join Algorithms

- Block Nested Loop Join: $B(R)+B(R) * B(S) / M$
- Index Nested Loop Join: $B(R)+T(R) B(S) / V(S, a)$
- Hash Join: Hybrid Hash Join:
- Sort-Merge Join:

