## Lecture 18

## Data Provenance

## Announcement

Project presentations:

- Tuesday, May 29, 8-1:30pm
- Presentation: 15'
- Presentation order on the Website
- Two Awards!
- Best Project: Diploma + Amazon Gift Certificate
- Best Presentation: Diploma + Amazon Gift Certificate
- Voting instructions to be sent by email

Next lecture:

- Friday, 5/25, 10:30am, CSE403


## Project Presentations Guidelines

What to include:

- A description of the problem: why is it important, why is it non-trivial
- An overview of prior approaches, and related work
- Your approach
- Your results (theoretical, empirical, experimental)
- A brief discussion on the significance of the results (do they work? do they solve the problem you set out to do ? do they improve over existing work ?)
- Conclusions

Rule of thumb: 1 slide / minute, then subtract slack You have $15 \rightarrow 12$ slides.

## Outline

## Sources:

- Karnouvarakis et al., Provenance Semirings, PODS 2007
- Cheney, Chiticariu,Tan, Provenance in Databases: Why, How, and Where, 2007
- Tannen, Tutorial on Provenance in EDBT 2010


## Data Provenance

Cheney, Chiticariu,Tan, Provenance in Databases: Why, How, and Where, 2007

- Provenance information describes the origins and the history of data in its life cycle. Such information (also called lineage) is important to many data management tasks.


## Data Provenance

- Provenance inside the DBMS
- Will discuss today
- Provenance outside of the DBMS
- Much more messy; there is a standard, OPM (Open Provenance Model)


## Provenance Annotations

- Some query produces an output table $T(A, B, C)$
- We store it over some period of time
- Later we ask: "where did

| A | B | C |
| :---: | :---: | :---: |
| a1 | b1 | c1 |
| a2 | b1 | c1 |
| a2 | b2 | c2 |
| a2 | b2 | c3 |

provenance1
provenance2
provenance3
provenance4 this tuple come from?"

- The "provenance annotation" answers this.


## Provenance Annotations

- Start by annotating each tuple in the original database with a unique identifier; can be the Tuple Id (TID)

| A | B |
| :---: | :---: |
| a1 | b1 |
| a2 | b1 |
| a2 | b2 |

- Next, compute the provenance expression inductively, based on the query plan


## Join Operator



## Projection Operator



## Union Operator



## Selection Operator

| $\sigma_{A=a 1}$ |  |
| :---: | :---: |
| A | B |
| a1 | b1 |
| a1 | b2 |
| a2 | b1 |
| a2 | b2 |
| a2 | b3 |


| A | B |
| :---: | :---: |
| a1 | b1 |
| a1 | b2 |

We could simply remove the tuples filtered out. But it's better to keep them around (we'll see why). What is their annotation?

## Selection Operator



| A | B |
| :---: | :---: |
| a1 | b1 |
| a1 | b2 |
| a2 | b1 |
| a2 | b2 |
| a2 | b3 |

We could simply remove the tuples filtered out. But it's better to keep them around (we'll see why). What is their annotation?

## Complex Example

$$
\sigma_{\mathrm{C}=\mathrm{e}} \prod_{\mathrm{AC}}\left(\prod_{\mathrm{AC}}(\mathrm{R}) \bowtie \prod_{\mathrm{BC}}(\mathrm{R}) \cup \prod_{\mathrm{AB}}(\mathrm{R}) \bowtie \prod_{\mathrm{BC}}(\mathrm{R})\right)=
$$

$\mathrm{R}=$

| A | B | C |
| :---: | :---: | :---: |
| a | b | c |
| d | b | e |
| f | g | e |


| A | $C$ |  |
| :---: | :---: | :--- |
| $a$ | $c$ | $(X \cdot X+X \cdot X) \cdot 0=2 \cdot X^{2}$ |
| $a$ | $e$ | $X \cdot Y \cdot 1=X \cdot Y$ |
| $d$ | $c$ | $Y \cdot X \cdot 0=0$ |
| $d$ | $e$ | $(Y \cdot Y+Y \cdot Z+Y \cdot Y) \cdot 1=2 \cdot Y^{2}+Y \cdot Z$ |
| $f$ | $e$ | $(Z \cdot Z+Z \cdot Y+Z \cdot Z) \cdot 1=2 \cdot Z^{2}+Y \cdot Z$ |

Discuss in class what these annotations mean

## K-Relations

Definition. A K-relation is a relation where each tuple is annotated with an element from the set K .

What we have described so far is an extension of the positive operations of the relational algebra to K-relations

We assumed that K has the operators +,

## Identities on Provenance Expressions

The problem:

- We have defined the provenance expressions for query plans P
- Given a query $Q$, we want the provenance of its answers to be the same, no matter what plan we use: P1, P2, ...
- What we need: if $\mathrm{P} 1=\mathrm{P} 2$, then the provenance expressions for P1 = the provenance expressions for P2


## Identities on Provenance Expressions

Definition. A structure $(\mathrm{K},+, \cdot, 0,1)$ is called a commutative semiring if: 1. $(K,+, 0)$ is a commutative monoid:
a. + is associative: $(x+y)+z=x+(y+z)$
b. + is commutative: $x+y=y+x$
c. 0 is the identity for $+: x+0=0+x=x$
2. ( $K, \cdot, 1$ ) is a commutative monoid:
a. ... (similar identities)
3. $\cdot$ distributes over + : $x \cdot(y+z)=x \cdot y+x \cdot z$
4. For all $x, x \cdot 0=0 \cdot x=0$

## Identities on provenance Expressions

Definition. A structure ( $K,+, \cdot, 0,1$ ) is called a commutative semiring if:

1. $(\mathrm{K},+, 0)$ is a commutative monoid:
a. + is associative: $(x+y)+z=x+(y+z)$
b. + is commutative: $x+y=y+x$
c. 0 is the identity for $+: x+0=0+x=x$
2. ( $K, \cdot, 1$ ) is a commutative monoid:
a. ... (similar identities)
3. distributes over $+: x \cdot(y+z)=x \cdot y+x \cdot z$
4. For all $x, x \cdot 0=0 \cdot x=0$

Theorem. The standard identities of the Bag algebra hold for K-relations iff ( $K,+, \cdot, 0,1$ ) is a commutative semiring.

# Identities on Provenance Expressions 

Discuss in class:

$$
q(x, y):=R(x, y), S(y, z), T(z, u)
$$

Given two plans, why are the annotations equal?

## Applications

$$
\sigma_{\mathrm{C}=\mathrm{e}} \prod_{\mathrm{AC}}\left(\prod_{\mathrm{AC}}(\mathrm{R}) \bowtie \prod_{\mathrm{BC}}(\mathrm{R}) \cup \prod_{\mathrm{AB}}(\mathrm{R}) \bowtie \prod_{\mathrm{BC}}(\mathrm{R})\right)=
$$

| $\mathrm{R}=$ |  |  |
| :---: | :---: | :---: |
| A | B | C |
| a | b | c |
| d | b | e |
| f | g | e |


| A | C |  |
| :---: | :---: | :---: |
| a | c | $2 \cdot{ }^{2}$ |
| a | e | X•Y |
| d | e | $2 \cdot Y^{2}+Y \cdot Z$ |
| f | e | $2 \cdot Z^{2}+Y \cdot Z$ |

Q: Suppose we delete the tuple ( $\mathrm{d}, \mathrm{b}, \mathrm{e}$ ) from R . Which tuple(s) disappear from the result?

## Applications

## $\sigma_{C=e} \Pi_{A C}\left(\Pi_{A C}(R) \bowtie \Pi_{B C}(R) \cup \Pi_{A B}(R) \bowtie \Pi_{B C}(R)\right)=$

| $\mathrm{R}=$ |  |  |
| :---: | :---: | :---: |
| A | B | C |
| a | b | c |
| d | b | e |
| f | g | e |


| A | C |  |
| :---: | :---: | :---: |
| a | C | $2 \cdot{ }^{2}$ |
| a | e | $X \cdot Y$ |
| d | e | $2 \cdot Y^{2}+Y \cdot Z$ |
| f | e | $2 \cdot Z^{2}+Y \cdot Z$ |


$=$| $A$ | $C$ |  |
| :--- | :--- | :--- |
| $a$ | $c$ | $2 \cdot X^{2}$ |
| $a$ | $e$ | 0 |
| $d$ | $e$ | 0 |
| $f$ | $e$ | $2 \cdot Z^{2}$ |

Q: Suppose we delete the tuple ( $\mathrm{d}, \mathrm{b}, \mathrm{e}$ ) from R.
A: Set $\mathrm{Y}=0$ Which tuple(s) disappear from the result?

## Applications

$$
\sigma_{\mathrm{C}=\mathrm{e}} \prod_{\mathrm{AC}}\left(\prod_{\mathrm{AC}}(\mathrm{R}) \bowtie \prod_{\mathrm{BC}}(\mathrm{R}) \cup \prod_{\mathrm{AB}}(\mathrm{R}) \bowtie \prod_{\mathrm{BC}}(\mathrm{R})\right)=
$$

| $\mathrm{R}=$ |  |  |
| :---: | :---: | :---: |
| A | B | C |
| a | b | c |
| d | b | e |
| f | g | e |


| A | C |  |
| :---: | :---: | :---: |
| a | c | $2 \cdot{ }^{2}$ |
| a | e | X•Y |
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Q: Suppose each tuple in $R$ occurs 3 times (bag semantics). How many times occurs each tuple in the answer?

## Applications

$$
\sigma_{C=e} \Pi_{A C}\left(\Pi_{A C}(R) \bowtie \Pi_{B C}(R) \cup \Pi_{A B}(R) \bowtie \Pi_{B C}(R)\right)=
$$

| $\mathrm{R}=$ |  |  |
| :---: | :---: | :---: |
| A | B | C |
| a | b | c |
| d | b | e |
| f | g | e |


| A | C |  |
| :---: | :---: | :---: |
| a | c | $2 \cdot{ }^{2}$ |
| a | e | X•Y |
| d | e | $2 \cdot Y^{2}+Y \cdot Z$ |
| f | e | $2 \cdot Z^{2}+Y \cdot Z$ |


| A | C |
| :---: | :---: |
| a | c |
| a | e |
| d | e |
| f | e |

Q: Suppose each tuple in $R$ occurs 3 times (bag semantics).
A. $\operatorname{Set} X=Y=Z=3$ How many times occurs each tuple in the answer?

## Lineage

## Lineage = set of contributing tuples

- Terminology alert: provenance and lineages are not used consistently in the literature
- The PODS'2007 paper calls this whyprovenance, Fig. 5; I will call it lineage


## Lineage

$\sigma_{C=e} \Pi_{A C}\left(\Pi_{A C}(R) \bowtie \Pi_{B C}(R) \cup \Pi_{A B}(R) \bowtie \Pi_{B C}(R)\right)=$

| $\mathrm{R}=$ |  |  |
| :---: | :---: | :---: |
| A | B | C |
| a | b | c |
| d | b | e |
| f | g | e |


| $A$ | $C$ |  |
| :---: | :---: | :--- |
| $a$ | $c$ | $2 \cdot X^{2}$ |
| $a$ | $e$ | $X \cdot Y$ |
| $d$ | $e$ | $2 \cdot Y^{2}+Y \cdot Z$ |
| $f$ | $e$ | $2 \cdot Z^{2}+Y \cdot Z$ |


| $A$ | $C$ |  |
| :---: | :---: | :--- |
| $a$ | $c$ | $X$ |
| $a$ | $e$ | $X, Y$ |
| $d$ | $e$ | $Y, Z$ |
| $f$ | $e$ | $Y, Z$ |

Lineage $=$ traces only the set of input tuples that contributed to an output tuple
This is also a semi-ring! Which one?

# Semirings for various models of provenance (1) <br> $R=$ <br> <div class="inline-tabular"><table id="tabular" data-type="subtable">
<tbody>
<tr style="border-top: none !important; border-bottom: none !important;">
<td style="text-align: center; border-left-style: solid !important; border-left-width: 1px !important; border-right-style: solid !important; border-right-width: 1px !important; border-bottom-style: solid !important; border-bottom-width: 1px !important; border-top-style: solid !important; border-top-width: 1px !important; width: auto; vertical-align: middle; ">A</td>
<td style="text-align: center; border-right-style: solid !important; border-right-width: 1px !important; border-bottom-style: solid !important; border-bottom-width: 1px !important; border-top-style: solid !important; border-top-width: 1px !important; width: auto; vertical-align: middle; ">B</td>
<td style="text-align: center; border-right-style: solid !important; border-right-width: 1px !important; border-bottom-style: solid !important; border-bottom-width: 1px !important; border-top-style: solid !important; border-top-width: 1px !important; width: auto; vertical-align: middle; ">C</td>
</tr>
<tr style="border-top: none !important; border-bottom: none !important;">
<td style="text-align: center; border-left-style: solid !important; border-left-width: 1px !important; border-right-style: solid !important; border-right-width: 1px !important; border-bottom-style: solid !important; border-bottom-width: 1px !important; border-top: none !important; width: auto; vertical-align: middle; ">a</td>
<td style="text-align: center; border-right-style: solid !important; border-right-width: 1px !important; border-bottom-style: solid !important; border-bottom-width: 1px !important; border-top: none !important; width: auto; vertical-align: middle; ">b</td>
<td style="text-align: center; border-right-style: solid !important; border-right-width: 1px !important; border-bottom-style: solid !important; border-bottom-width: 1px !important; border-top: none !important; width: auto; vertical-align: middle; ">c</td>
</tr>
<tr style="border-top: none !important; border-bottom: none !important;">
<td style="text-align: center; border-left-style: solid !important; border-left-width: 1px !important; border-right-style: solid !important; border-right-width: 1px !important; border-bottom-style: solid !important; border-bottom-width: 1px !important; border-top: none !important; width: auto; vertical-align: middle; ">d</td>
<td style="text-align: center; border-right-style: solid !important; border-right-width: 1px !important; border-bottom-style: solid !important; border-bottom-width: 1px !important; border-top: none !important; width: auto; vertical-align: middle; ">b</td>
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</tr>
<tr style="border-top: none !important; border-bottom: none !important;">
<td style="text-align: center; border-left-style: solid !important; border-left-width: 1px !important; border-right-style: solid !important; border-right-width: 1px !important; border-bottom: none !important; border-top: none !important; width: auto; vertical-align: middle; ">f</td>
<td style="text-align: center; border-right-style: solid !important; border-right-width: 1px !important; border-bottom: none !important; border-top: none !important; width: auto; vertical-align: middle; ">y</td>
<td style="text-align: center; border-right-style: solid !important; border-right-width: 1px !important; border-bottom: none !important; border-top: none !important; width: auto; vertical-align: middle; ">e</td>
</tr>
<tr style="border-top: none !important; border-bottom: none !important;">
<td style="text-align: center; border-left-style: solid !important; border-left-width: 1px !important; border-right-style: solid !important; border-right-width: 1px !important; border-bottom-style: solid !important; border-bottom-width: 1px !important; border-top: none !important; width: auto; vertical-align: middle; ">Z</td>
<td style="text-align: center; border-right-style: solid !important; border-right-width: 1px !important; border-bottom-style: solid !important; border-bottom-width: 1px !important; border-top: none !important; width: auto; vertical-align: middle; " class="_empty"></td>
<td style="text-align: center; border-right-style: solid !important; border-right-width: 1px !important; border-bottom-style: solid !important; border-bottom-width: 1px !important; border-top: none !important; width: auto; vertical-align: middle; " class="_empty"></td>
</tr>
</tbody>
</table>
<table-markdown style="display: none">| A | B | C |
| :---: | :---: | :---: |
| a | b | c |
| d | b | e |
| f | y | e |
| Z |  |  |</table-markdown></div> <br> Q = <br>  

Lineage [CuiWidomWiener 00 etc.]
Sets of contributing tuples
Semiring: $\left(\operatorname{Lin}(X), \cup, \cup^{*}, \varnothing, \varnothing^{*}\right)$

## Semirings for various models of

 provenance (2)$$
\mathrm{R}=
$$

| A | B | C |
| :---: | :---: | :---: |
| a | b | c |
| X | X |  |
| f | e | Y |
| y | Z |  |

(Witness, Proof) why-provenance
[BunemanKhannaTan 01] \& [Buneman+ PODS08]
Sets of witnesses (w. =set of contributing tuples)

Semiring: $(W h y(X), \cup, \cup, \varnothing,\{\varnothing\})$

\section*{Semirings for various models of provenance (3) <br> $R=$ <br> | A | B | C |
| :---: | :---: | :---: |
| a | b | c |
| d | b | e |
| f | g | e | <br> Q = <br> }

Minimal witness why-provenance
[BunemanKhannaTan 01]
Sets of minimal witnesses
Semiring: $(\operatorname{PosBool}(X), \Lambda, \vee, \tau, \perp)$

## Semirings for various models of

 provenance (4)$$
R=
$$

| A | B | C |
| :---: | :---: | :---: |
| a | b | c |
| d | b | e |
| f | y | e |
| Z |  |  |

Q =

Notation:
\{\} set
[] bag

$\square$

Trio lineage [Das Sarma+ 08]
Bags of sets of contributing tuples (of witnesses)
Semiring: (Trio $(X),+, \cdot, 0,1)$ (defined in [Green, ICDT 09])

## Semirings for various models of

 provenance (5)$\mathrm{R}=$

| A | B | C |
| :---: | :---: | :---: |
| a | b | c |
| X | X |  |
| d | b | e |
| y | Y |  |
| f | g | e |
| Z |  |  |

Q =

| A | C |
| :--- | :--- |
|  |  |
| d | e |
|  | $\{[\mathrm{Y}, \mathrm{Y}],[\mathrm{Y}, \mathrm{Z}]\}$ |
|  |  |

Notation:
\{\} set
[] bag
Polynomials with boolean coefficients [Green, ICDT 09]
( $\mathrm{B}[X]$-provenance )
Sets of bags of contributing tuples
Semiring: $(B[X],+, \cdot, 0,1)$

## Semirings for various models of

 provenance (6)$$
\mathrm{R}=
$$

| A | B | C |
| :---: | :---: | :---: |
| a | b | c |
| d | b | e |
| f | g | e |

$$
Q=
$$



Provenance polynomials [GKT, PODS 07] ( $\mathrm{N}[\mathrm{X}]$-provenance )
Bags of bags of contributing tuples
Semiring: ( $N[X],+, \cdot, 0,1$ )

## Application

## Discretionary Access Control [LaPadula]

- Public $=P$
- Confidential = C
- Secret = S
- Top Secret = T
- No Such Thing... $=0$

$$
\begin{aligned}
& \mathrm{R}= \\
& \begin{array}{|c|c|c|}
\hline \mathrm{A} & \mathrm{~B} & \mathrm{C} \\
\hline \mathrm{a} & \mathrm{~b} & \mathrm{c} \\
\hline \mathrm{~d} & \mathrm{~b} & \mathrm{e} \\
\hline \mathrm{X}=\mathrm{C} \\
\mathrm{y} & \mathrm{Y}=\mathrm{P} \\
\mathrm{f} & \mathrm{~g} & \mathrm{e} \\
\mathrm{Z}=\mathrm{C}
\end{array}
\end{aligned}
$$

| $A$ | $C$ |  |
| :---: | :---: | :--- |
| $a$ | $c$ | $2 \cdot X^{2}=?$ |
| $a$ | $e$ | $X \cdot Y=?$ |
| $d$ | $e$ | $2 \cdot Y^{2}+Y \cdot Z=?$ |
| $f$ | $e$ | $2 \cdot Z^{2}+Y \cdot Z=?$ |

## Application

## Discretionary Access Control [LaPadula]

- Public = P
- Confidential $=\mathrm{C}$
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$$
\begin{aligned}
& \mathrm{R}= \\
& \begin{array}{|c|c|c|}
\hline \mathrm{A} & \mathrm{~B} & \mathrm{C} \\
\hline \mathrm{a} & \mathrm{~b} & \mathrm{c} \\
\hline
\end{array} \\
& \hline \mathrm{~d}
\end{aligned} \mathrm{~b}
$$

| $A$ | $C$ |  |
| :---: | :---: | :--- |
| $a$ | $c$ | $2 \cdot X^{2}=C$ |
| $a$ | $e$ | $X \cdot Y=C$ |
| $d$ | $e$ | $2 \cdot Y^{2}+Y \cdot Z=C$ |
| $f$ | $e$ | $2 \cdot Z^{2}+Y \cdot Z=T$ |

(A, min, max, 0, P), where $\mathrm{A}=\mathrm{P}<\mathrm{C}<\mathrm{S}<\mathrm{T}<0$

## But are there useful commutative semirings?

| $(\mathrm{B}, \wedge, \vee, \mathrm{T}, \perp)$ | Set semantics |
| :--- | :--- |
| $(\mathbb{N},+, \cdot, 0,1)$ | Bag semantics |
| $(\mathrm{P}(\Omega), \cup, \cap, \varnothing, \Omega)$ | Probabilistic events <br> [FuhrRölleke 97] |
| $($ BoolExp $(\mathrm{X}), \wedge, \vee, \mathrm{T}, \perp)$ | Conditional tables (c-tables) <br> [ImielinskiLipski 84] |
| $\left(\mathrm{R}_{+}^{\infty}, \min ,+, 1,0\right)$ | Tropical semiring <br> (cost/distrust score/confidence need) |
| $(\mathrm{A}$, min, max, $0, \mathrm{P})$ <br> where $\mathrm{A}=\mathrm{P}<\mathrm{C}<\mathrm{S}<\mathrm{T}<0$ | Access control levels <br> [PODS8] |

## A provenance hierarchy



## One semiring to rule them all... (apologies!)



A path downward from $K_{1}$ to $K_{2}$ indicates that there exists an onto (surjective) semiring homomorphism $h: K_{1} \rightarrow K_{2}$

## Using homomorphisms to relate models



Homomorphism?
$h(x+y)=h(x)+h(y) \quad h(x y)=h(x) h(y) \quad h(0)=0 \quad h(1)=1$
Moreover, for these homomorphisms $h(x)=x$

