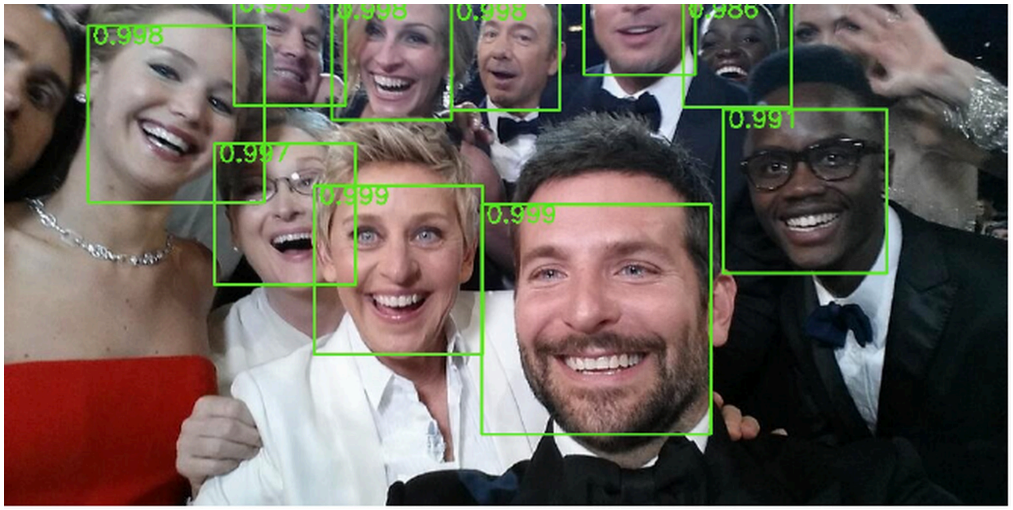
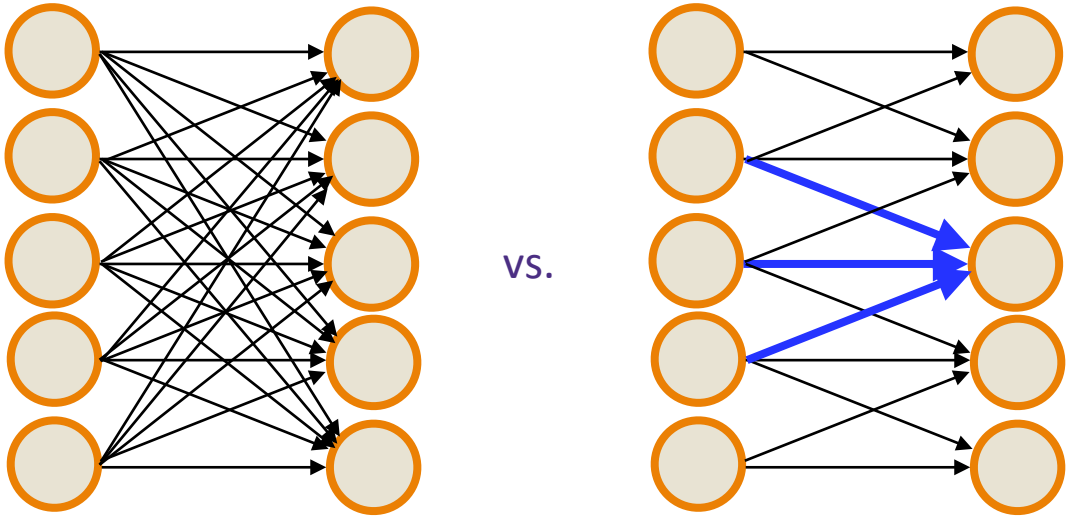
Convolutional Neural Networks

Neural Network Architecture

Objects are often **localized in space** so to find the faces in an image, not every pixel is important for classification—makes sense to drag a window across an image.

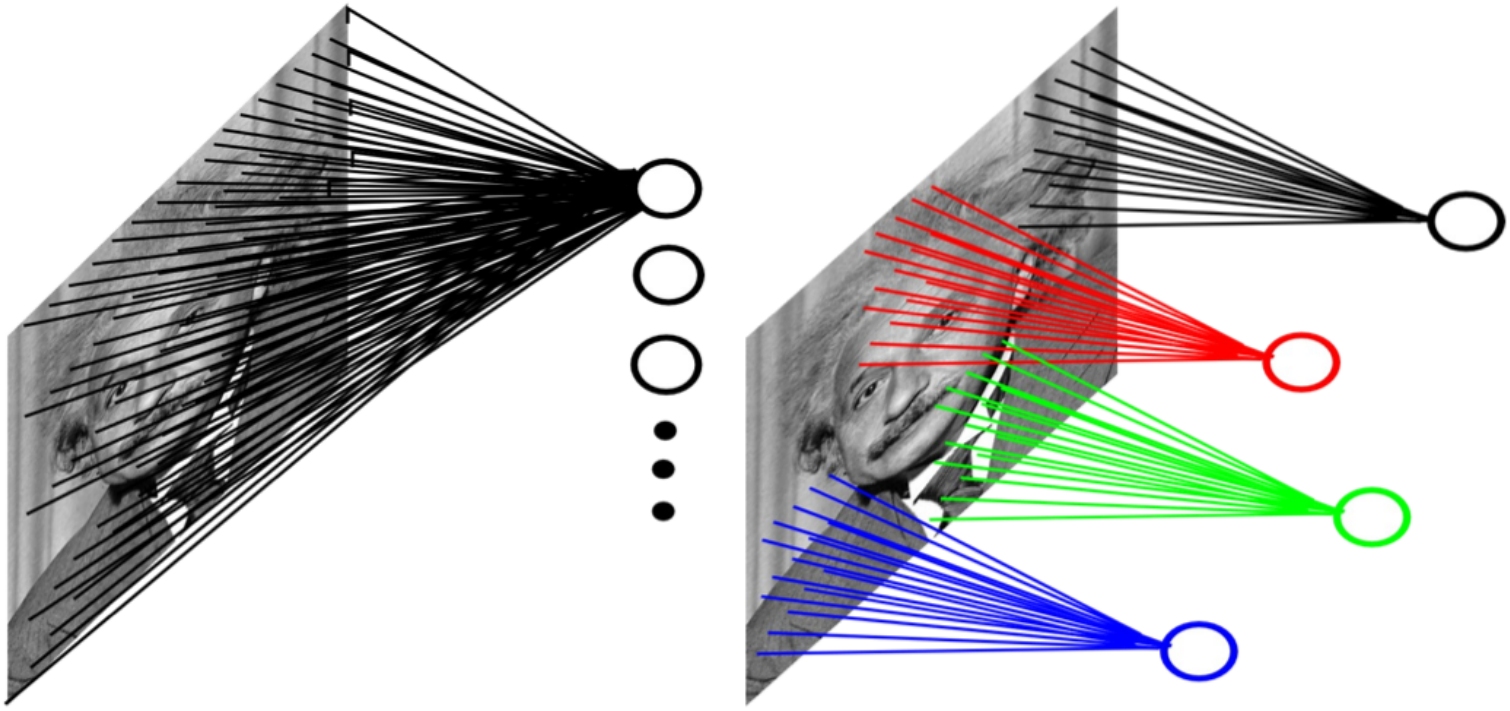


Similarly, to identify edges or other local structure, it makes sense to only look at **local information**



2d Convolution Layer

- **Example: 200x200 image**
  - Fully-connected, 400,000 hidden units = 16 billion parameters
  - Locally-connected, 400,000 hidden units 10x10 fields = 40 million params
  - Local connections capture local dependencies



Convolution of images (2d convolution)

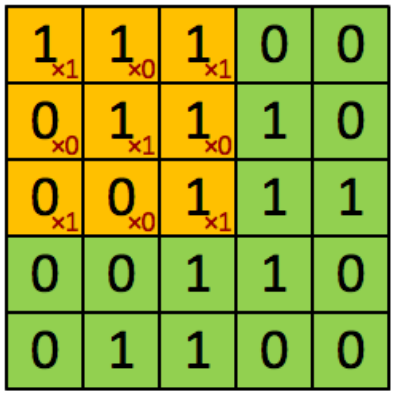
$$(I * K)(i,j) = \sum_m \sum_n I(i+m, j+n) K(m,n)$$

1	1	1	0	0
0	1	1	1	0
0	0	1	1	1
0	0	1	1	0
0	1	1	0	0

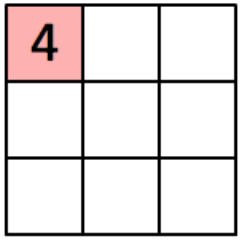
Image I

1	0	1
0	1	0
1	0	1

Filter K



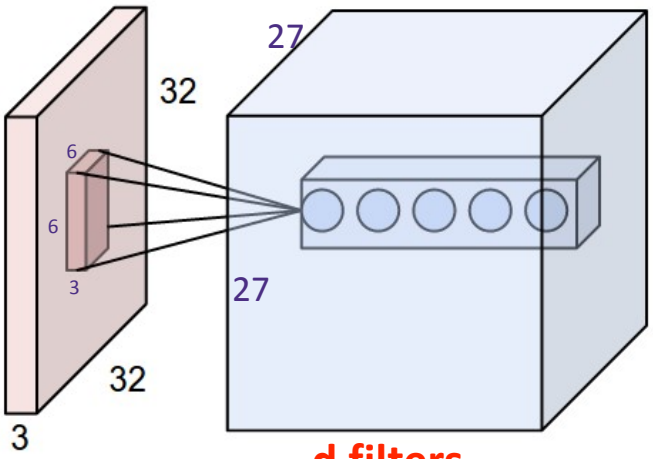
Image



Convolved Feature

$I * K$

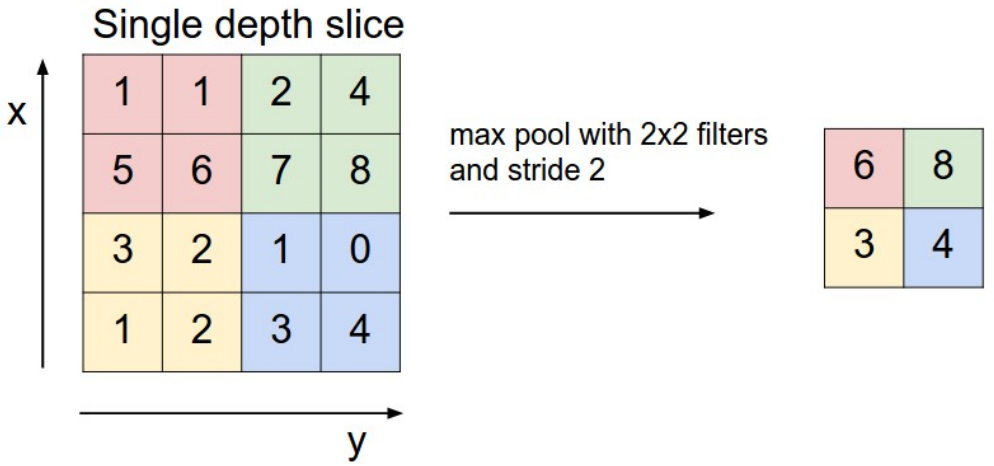
Stacking convolved images

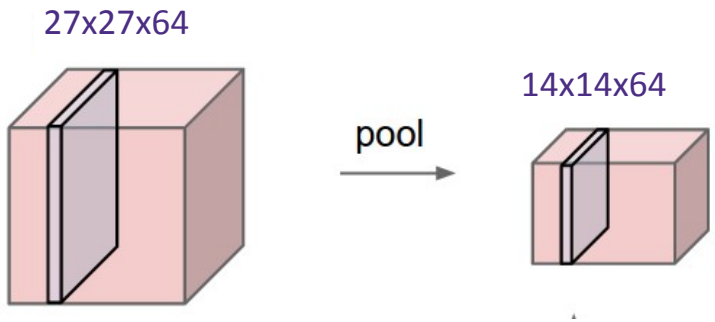


Repeat with d filters!

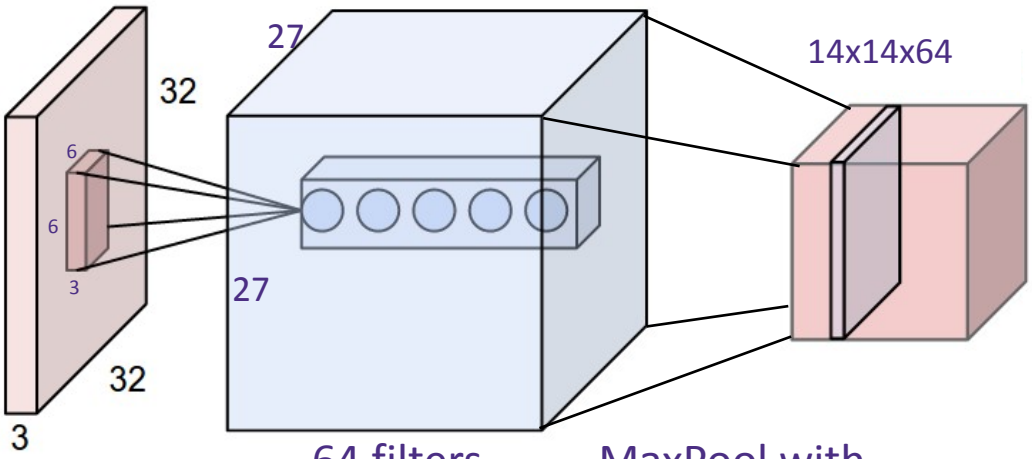
Pooling

Pooling reduces the dimension and can be interpreted as “This filter had a high response in this general region”





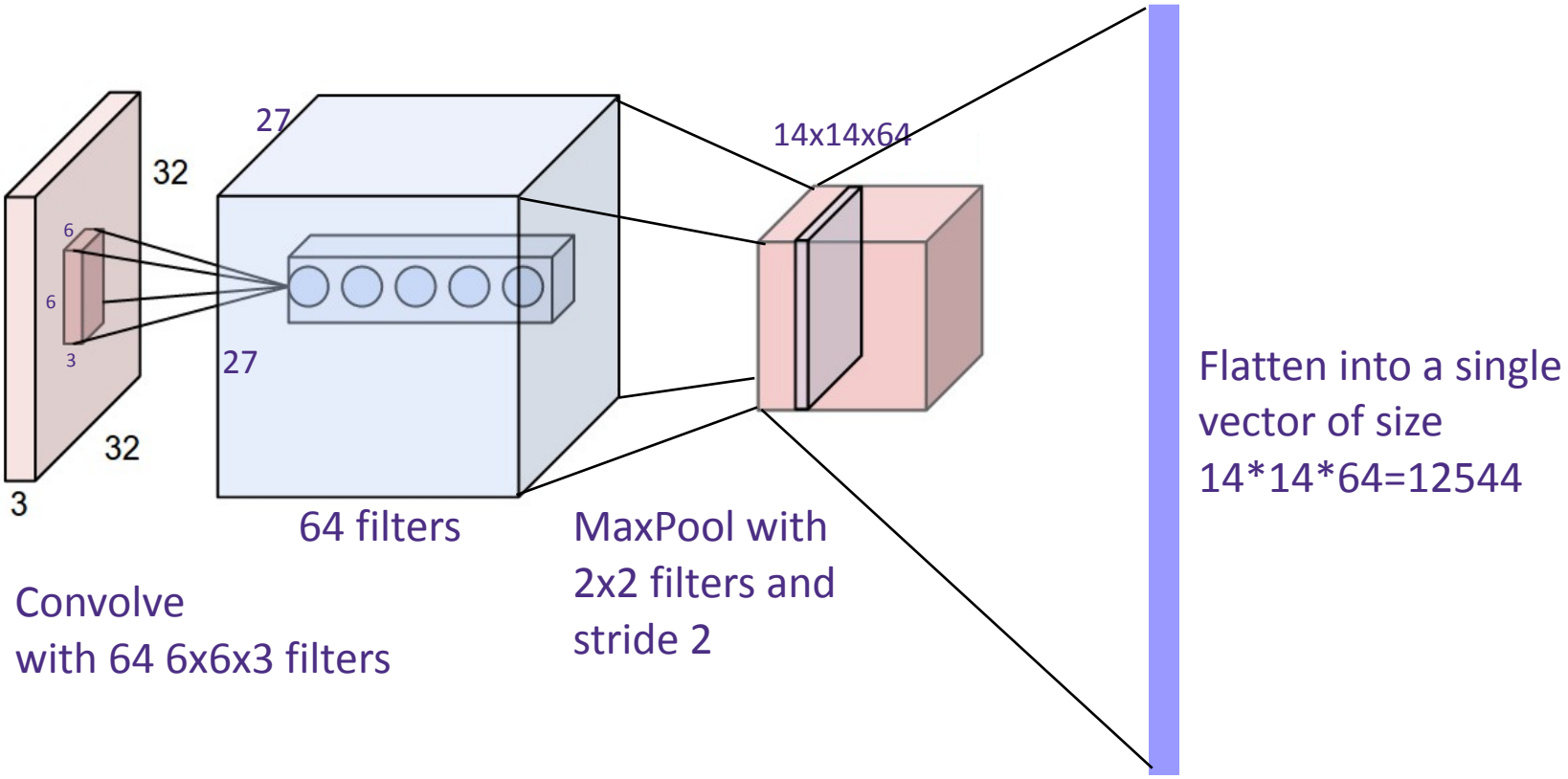
Pooling Convolution layer



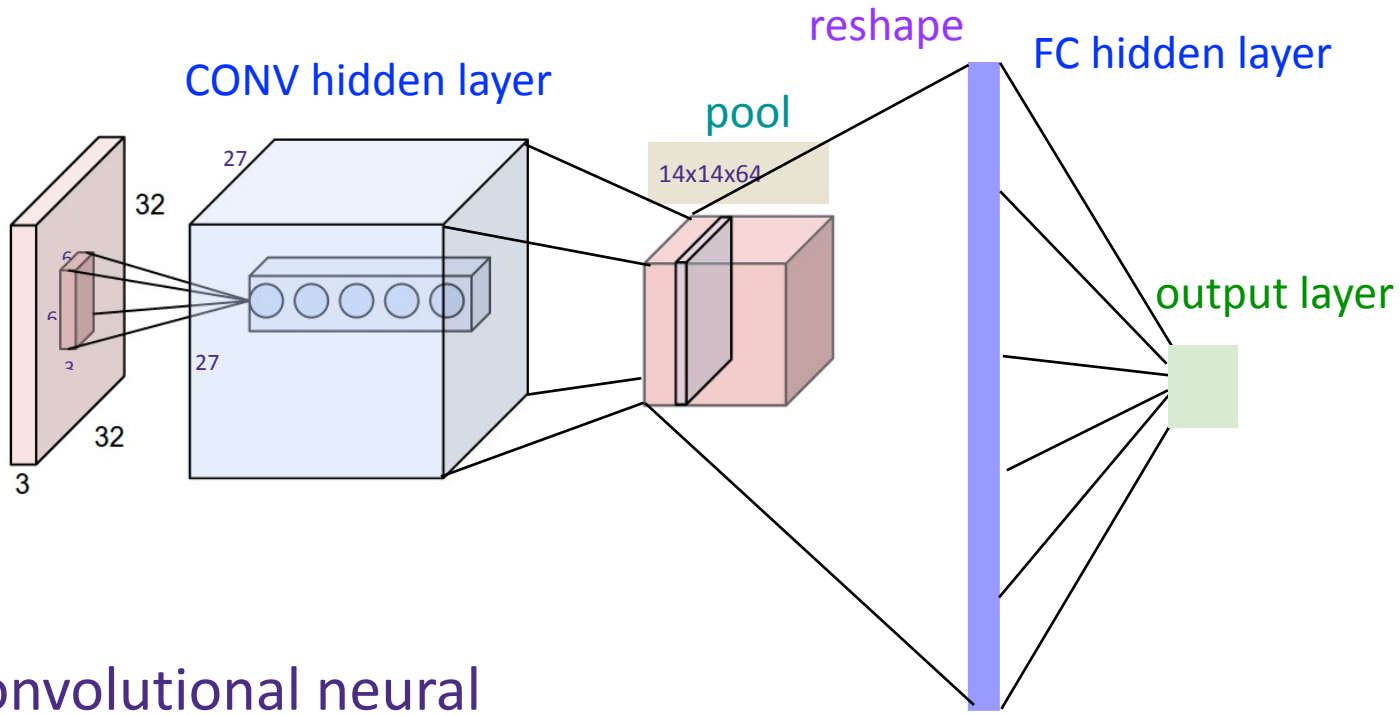
Convolve
with 64 6x6x3 filters

MaxPool with
2x2 filters and
stride 2

Flattening

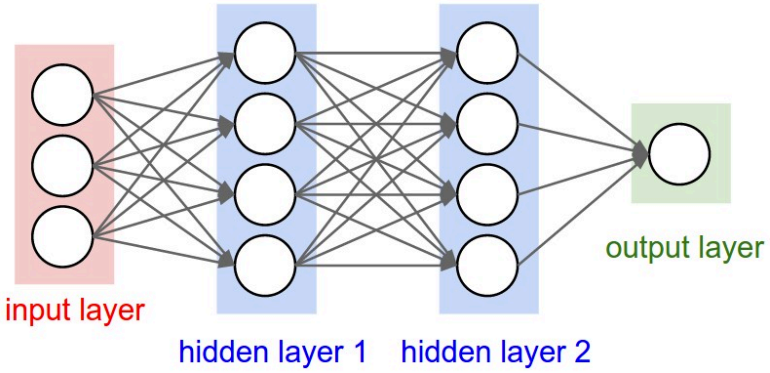

32
32
3
6
6
3
27
27
14x14x64
Convolve
with 64 6x6x3 filters
64 filters
MaxPool with
2x2 filters and
stride 2
Flatten into a single
vector of size
14*14*64=12544

Training Convolutional Networks

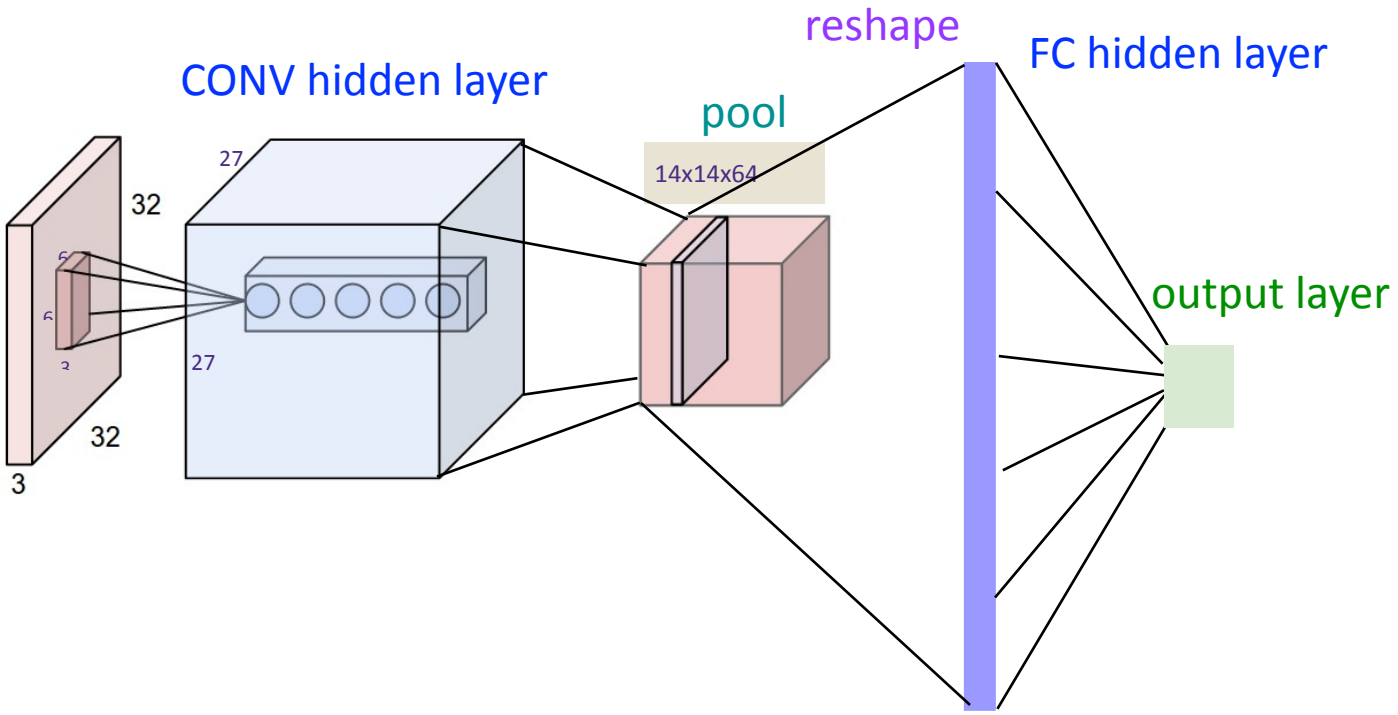


Recall: Convolutional neural networks (CNN) are just regular fully connected (FC) neural networks with some connections removed.

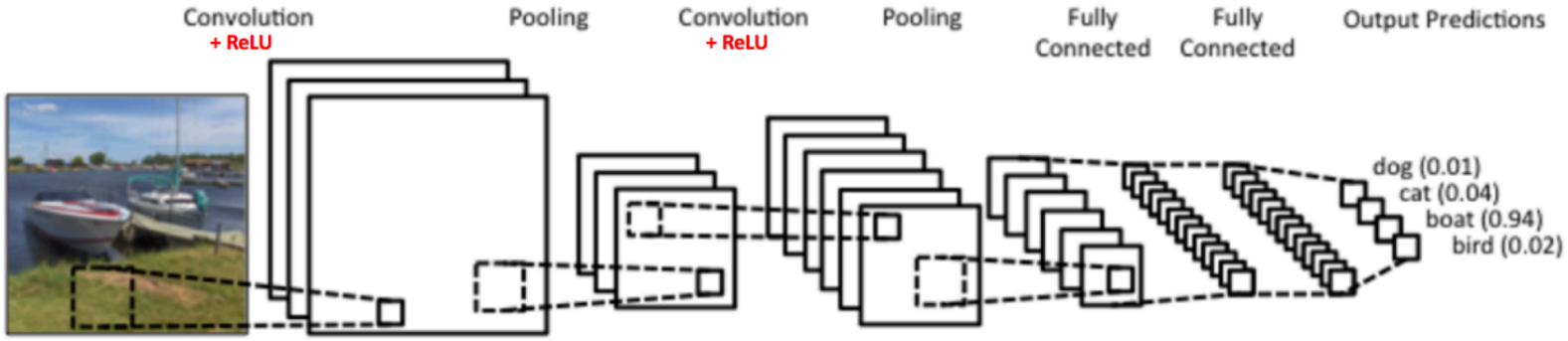
Train with SGD!

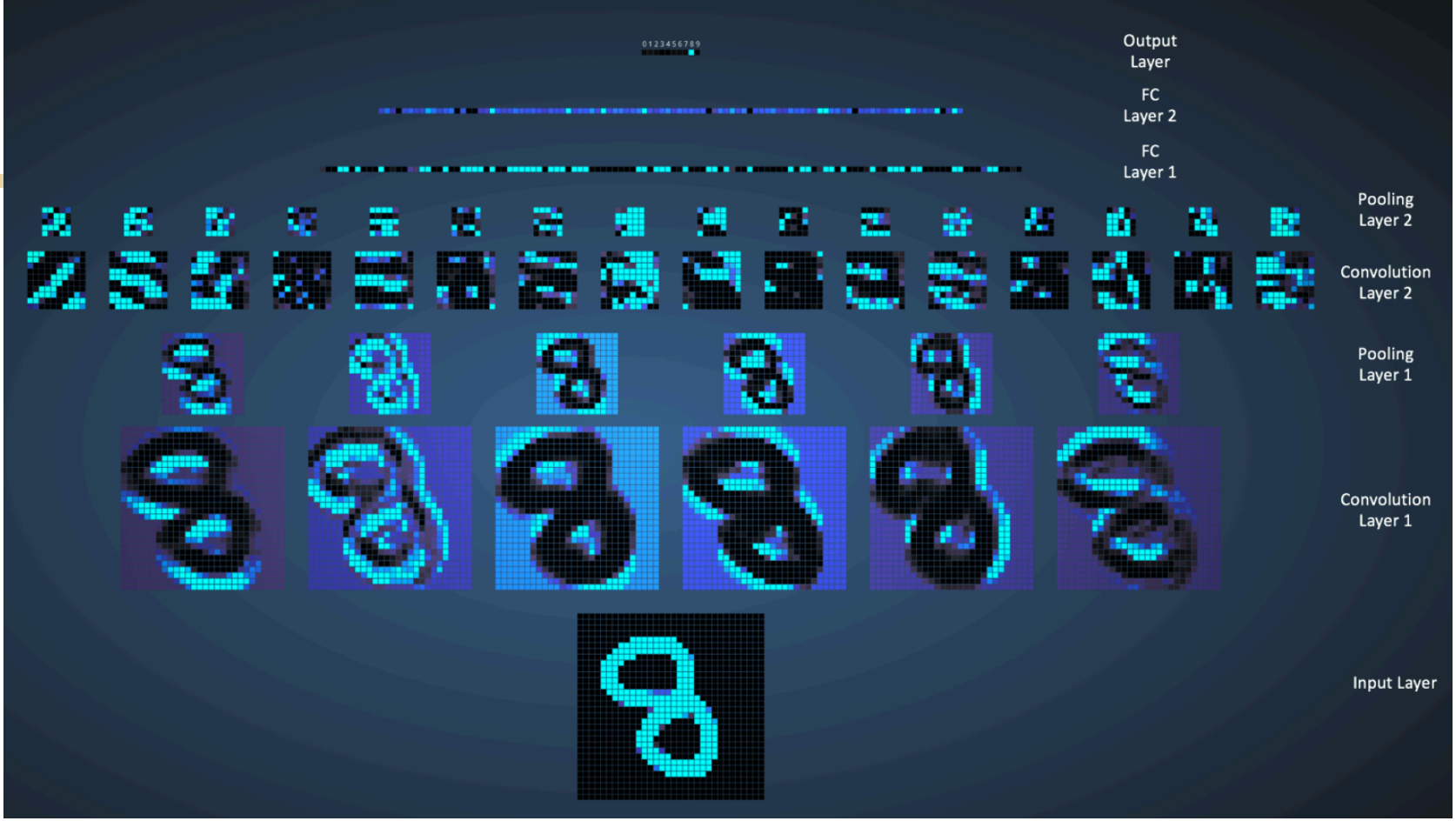


Training Convolutional Networks

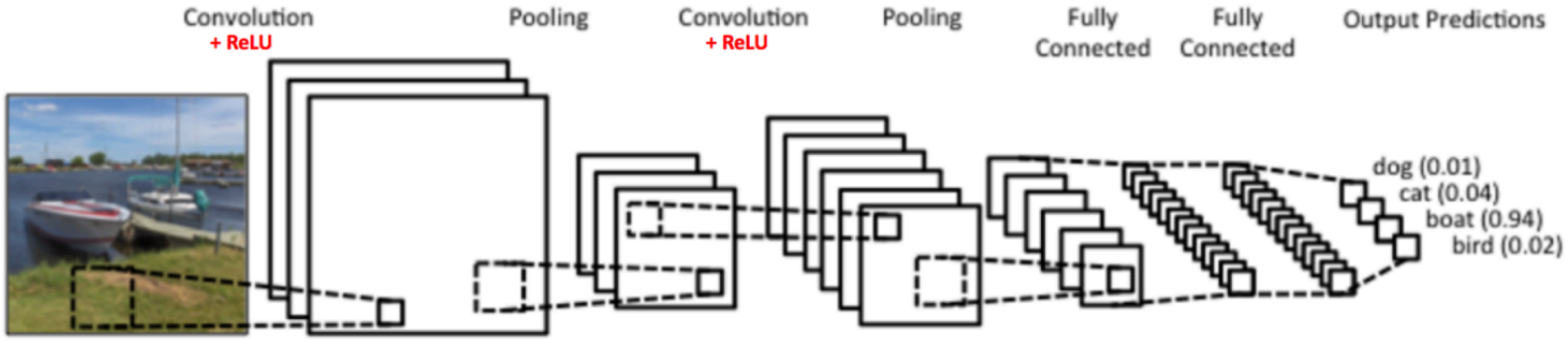


Real example network: LeNet





Real example network: LeNet



Famous CNNs

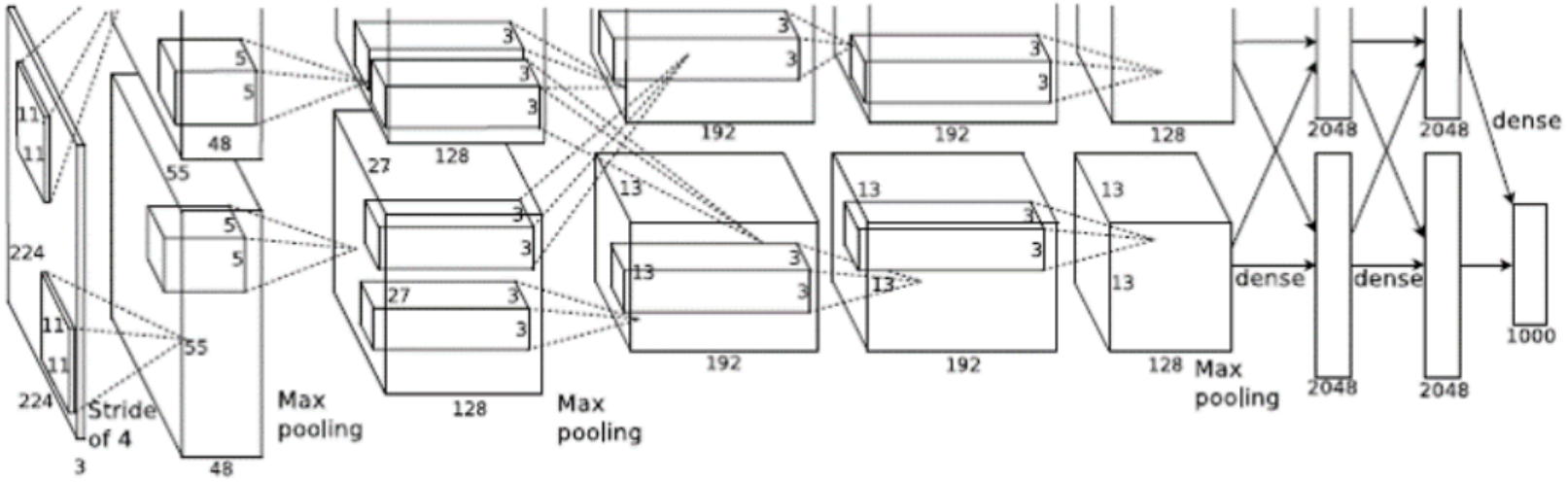
ImageNet Dataset

~14 million images, 20k classes

Deng et al. “Imagenet: a large scale hierarchical image database” ‘09

AlexNet

Breakthrough on ImageNet: ~the beginning of deep learning era



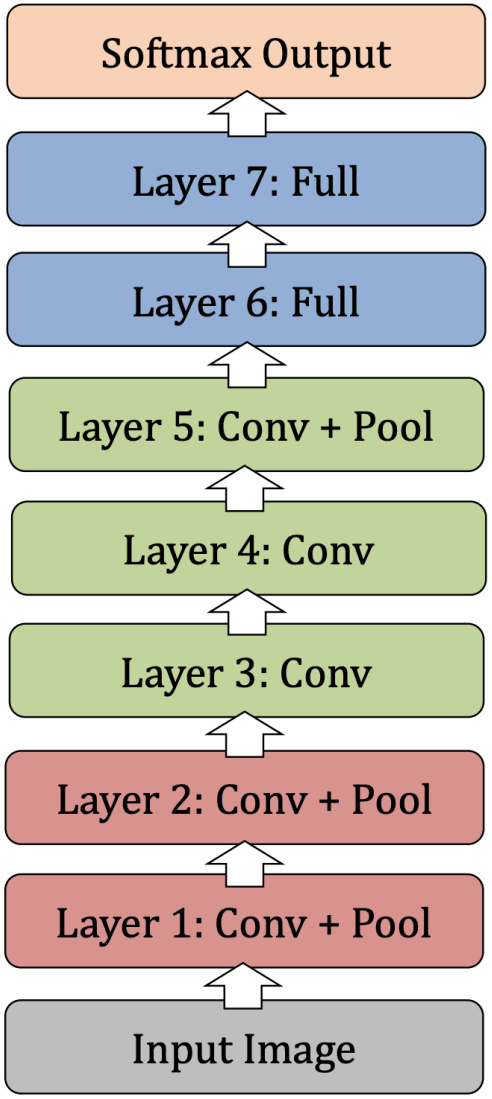
Krizhevsky, Sutskever, Hinton “ImageNet Claasification with Deep Convolutional Neural Networks”, NIPS 2012.

AlexNet

8 layers, ~60M parameters

Top5 error: 18.2%

Techniques used:
ReLU activation, overlapping pooling, dropout, ensemble (create 10 patches by cropping and average the predictions), data-augmentation (intensity of RGB channels)



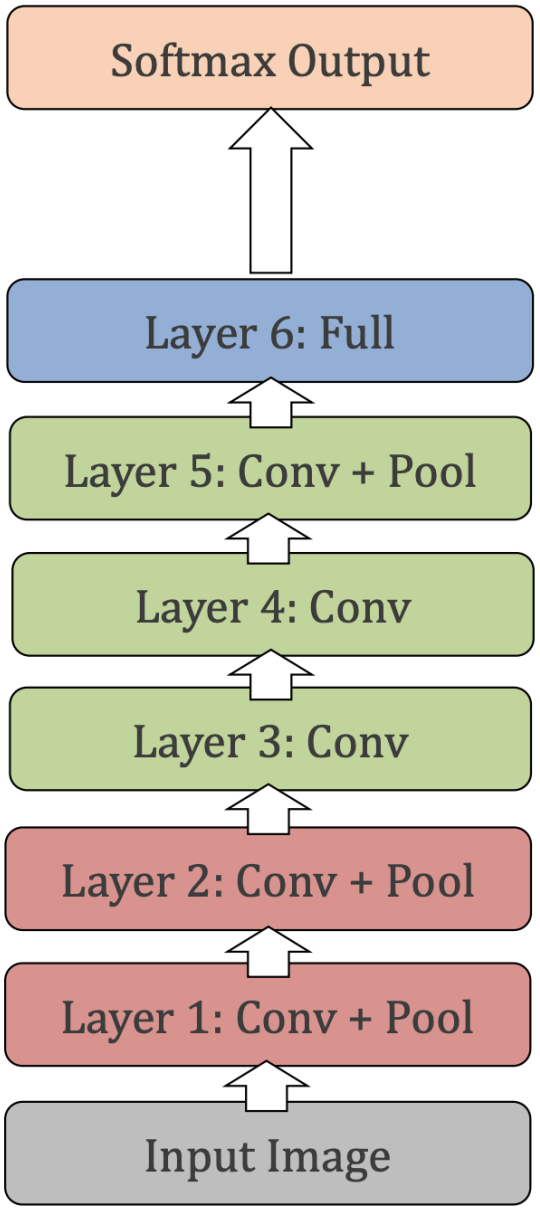
[From Rob Fergus' CIFAR 2016 tutorial]

AlexNet

Remove top fully-connected layer 7

Drop ~16 million parameters

1.1% drop in performance



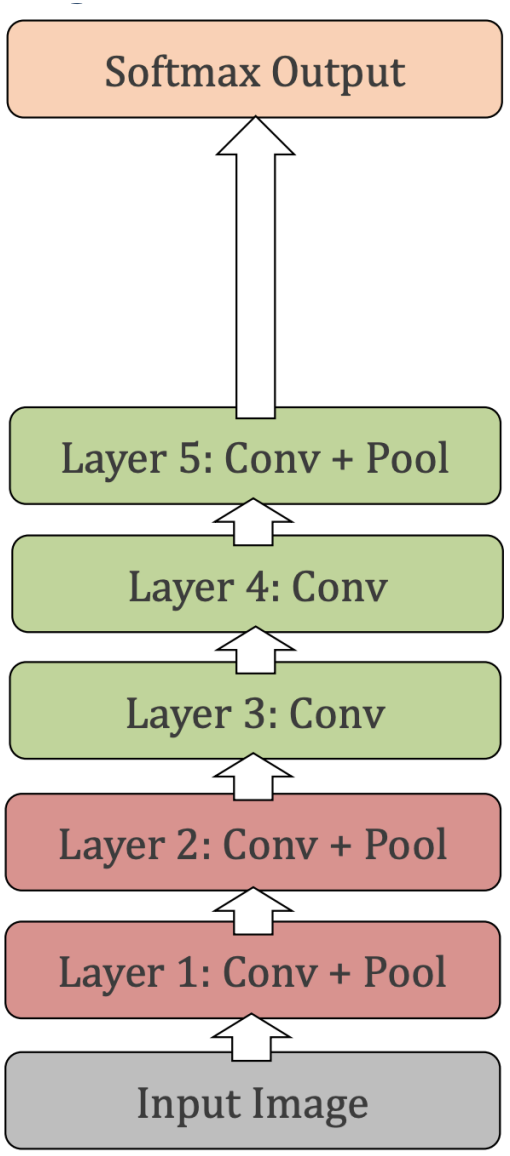
[From Rob Fergus' CIFAR 2016 tutorial]

AlexNet

Remove both fully connected layers 6 and 7

Drop ~50 million parameters

5.7% drop in performance



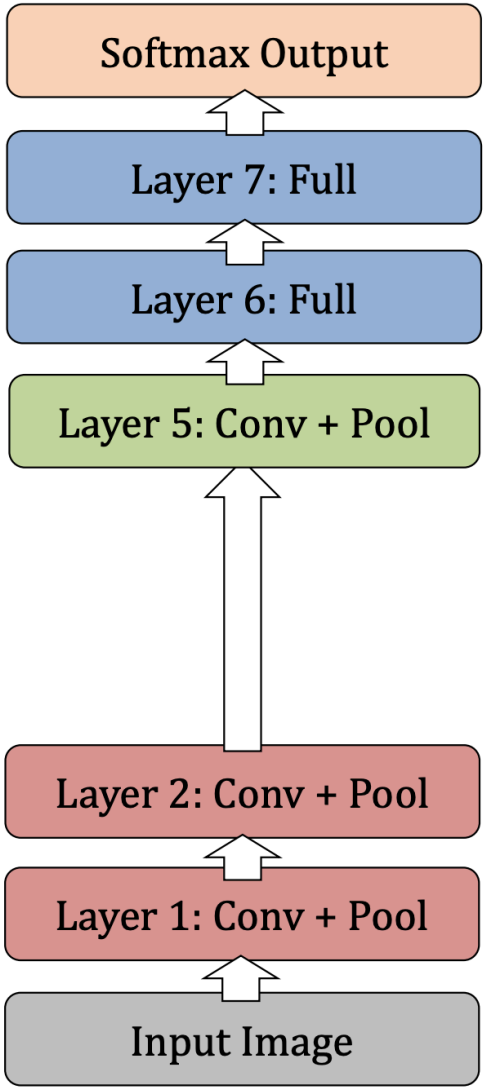
[From Rob Fergus' CIFAR 2016 tutorial]

AlexNet

Remove upper convolutio / feature extractor layers (layer 3 and 4)

Drop ~1 million parameters

3% drop in performance



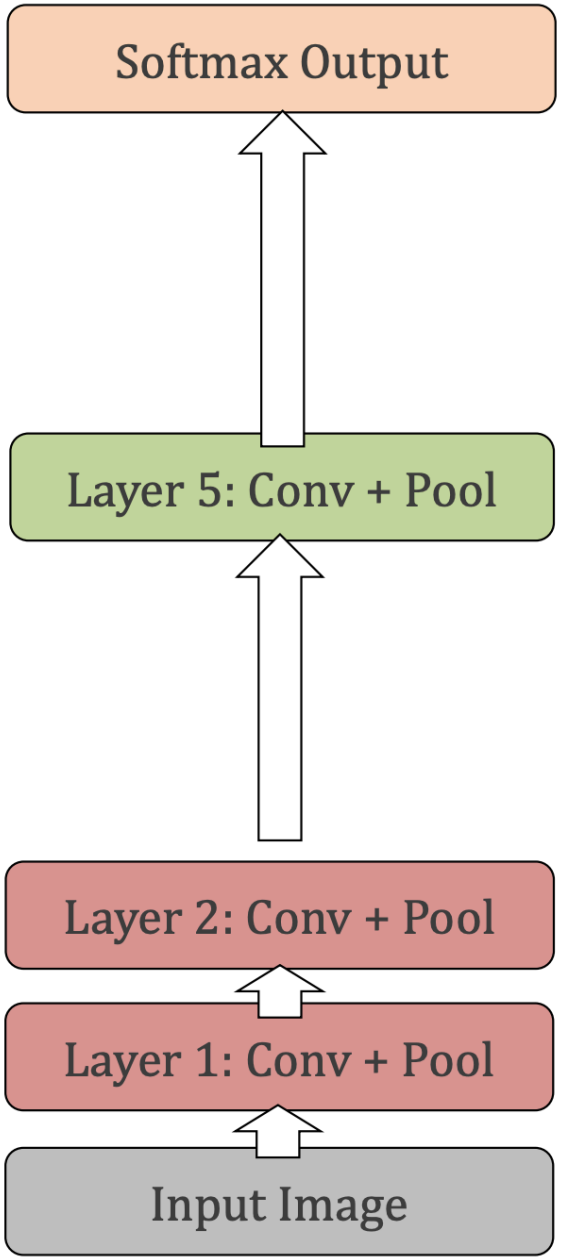
[From Rob Fergus' CIFAR 2016 tutorial]

AlexNet

Remove top fully connected layer 6,7 and upper convolution layers 3,4.

33.5% drop in performance.

Depth of the network is the key.



[From Rob Fergus' CIFAR 2016 tutorial]

GoogLeNet

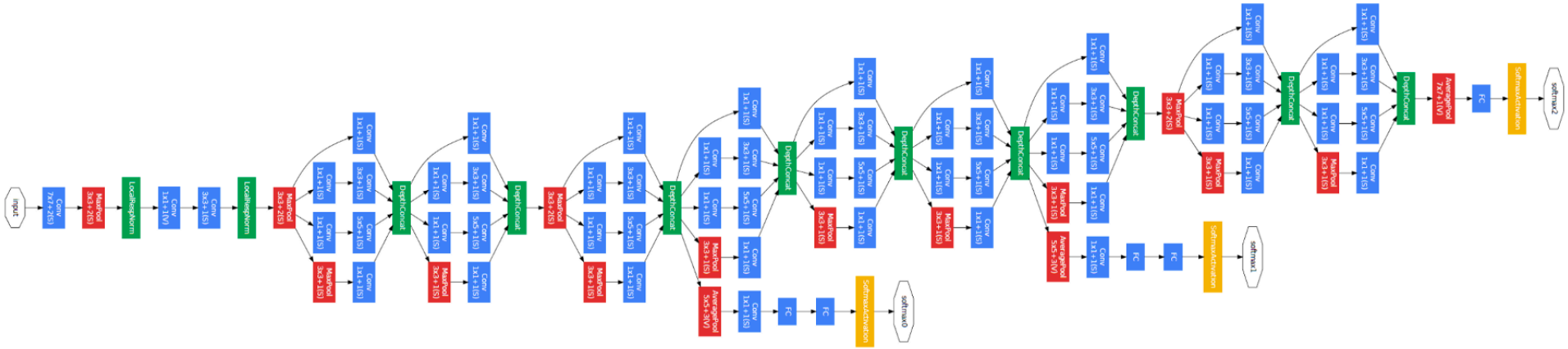
Motivation: multiscale nature of images

Large kernel for global features, and **smaller kernel** for local features.

Idea: have multiple different-size kernels at any layer.

[Going Deep with Convolutions, Szegedy et al. ’14]

GoogLeNet

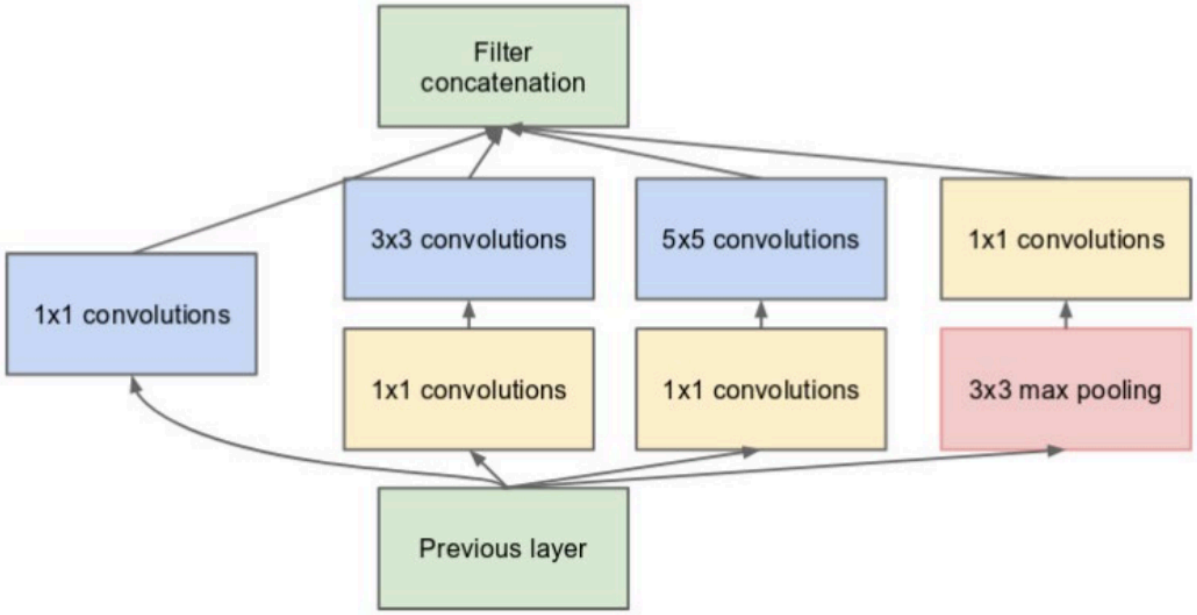


Large kernel for global features, and **smaller kernel** for local features.

Idea: have multiple different-size kernels at any layer.

[Going Deep with Convolutions, Szegedy et al. ’14]

Inception Module



Multiple filter scales at each layer

Dimensionality reduction to keep computational requirements down

[Going Deep with Convolutions, Szegedy et al. ’14]

Residual Networks

Motivation: extremely deep nets are hard to train (gradient explosion/ vanishing)

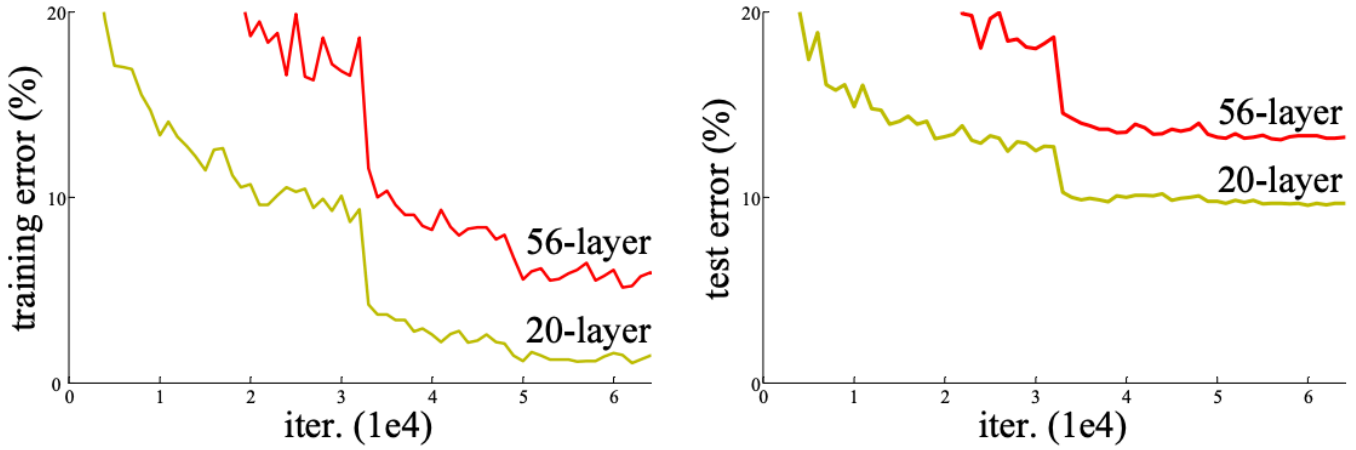


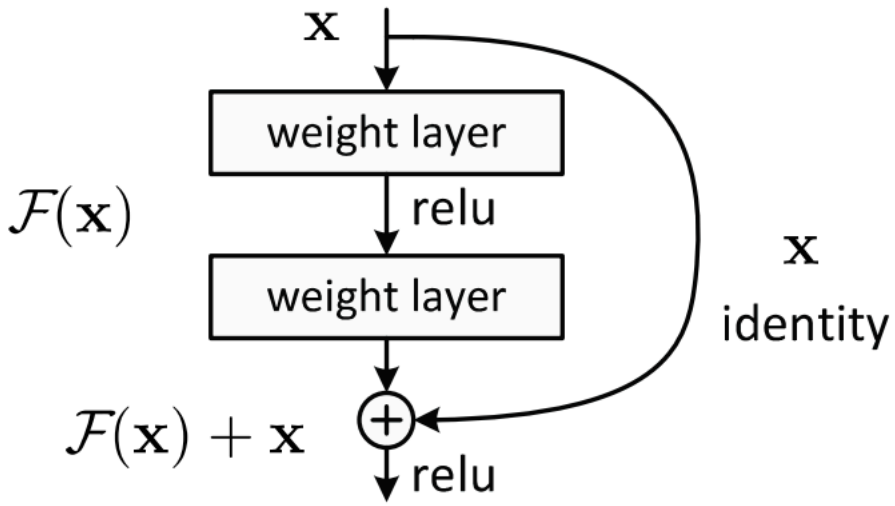
Figure 1. Training error (left) and test error (right) on CIFAR-10 with 20-layer and 56-layer "plain" networks. The deeper network has higher training error, and thus test error. Similar phenomena on ImageNet is presented in Fig. 4.

[He, Zhang, Ren, Sun, '16]

Residual Networks

Idea: identity shortcut, skip one or more layers.

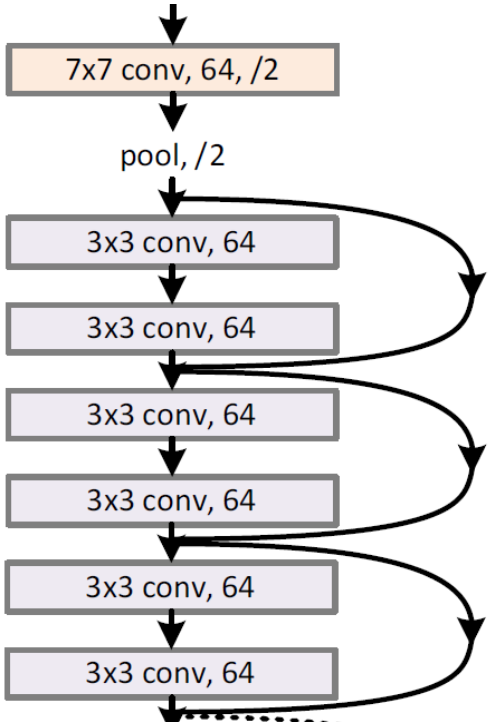
Justification: network can easily simulate shallow network ($F \approx 0$), so performance should not degrade by going deeper.

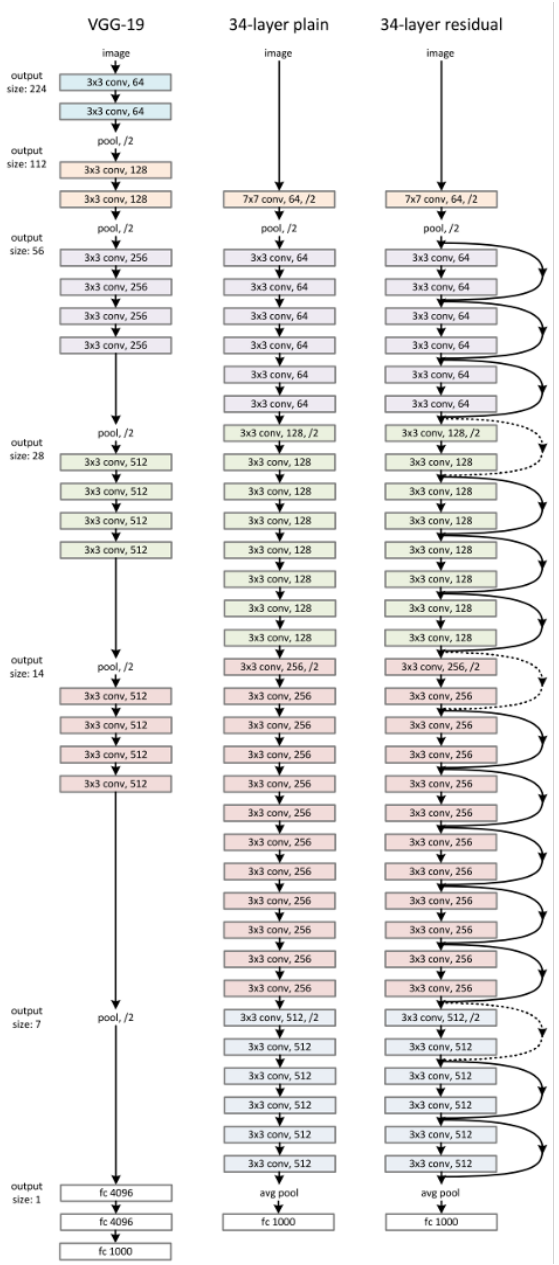


[He, Zhang, Ren, Sun, '16]

Residual Networks

- 3.57% top-5 error on ImageNet
- First deep network with > 100 layers.
- Widely used in many domains (AlphaGo)





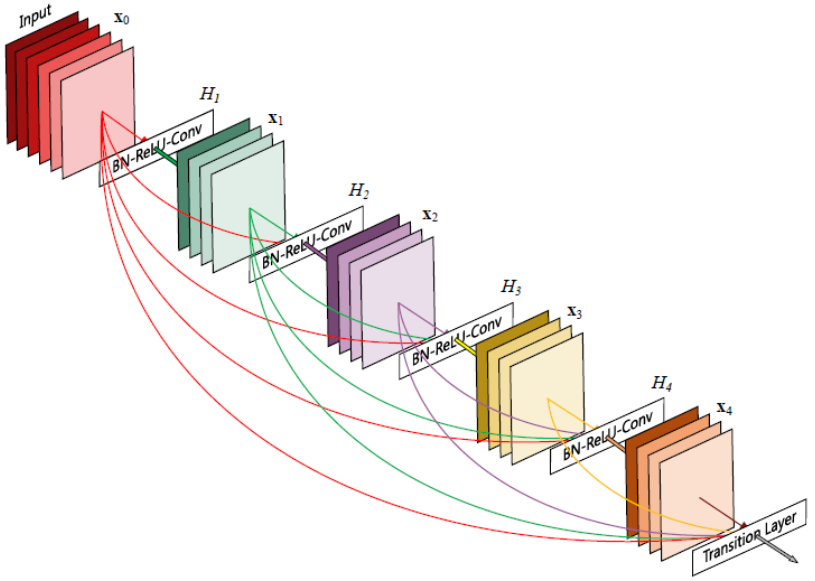
[He, Zhang, Ren, Sun, '16]

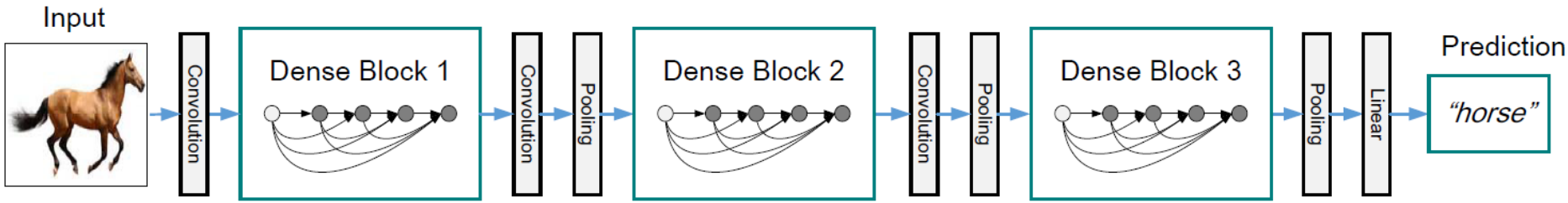
Densely Connected Network

Idea: explicit forward output of layer to all future layers (by concatenation)

Intuition: helps vanishing gradients, encourage reuse features (reduce parameter count)

Issues: network maybe too wide, need to be careful about memory consumption





[He, Zhang, Ren, Sun, '16]

Neural Architecture / Hyper-Parameter Search

Many design choices:

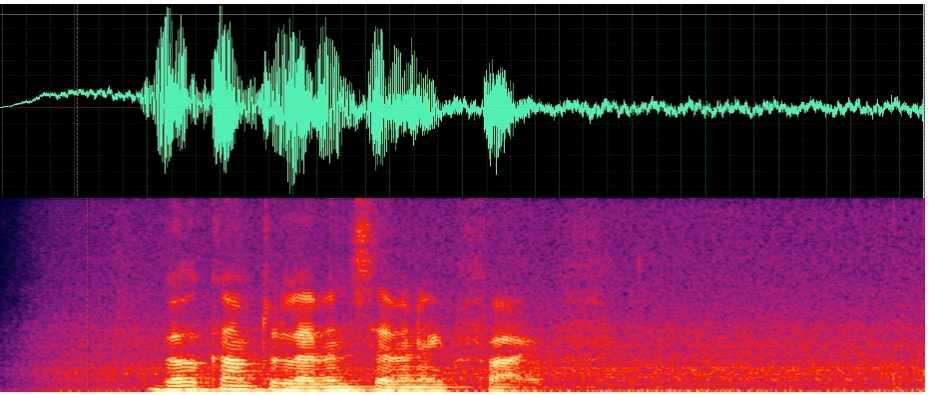
- Number of layers, width, kernel size, pooling, connections, etc.
- Normalization, learning rate, batch size, etc.

Strategies:

- Grid search
- Random search [Bergestra & Bengio ’12]
- Bandit-based [Li et al. ’16]
- Gradient-based (DARTS) [Liu et al. ’19]
- Neural tangent kernel [Xu et al. ’21]
- …

Recurrent Neural Networks

Sequence Data



检测语言 英语 中文 德语 中文（简体） 英语 日语

Deep learning is a popular area in AI.

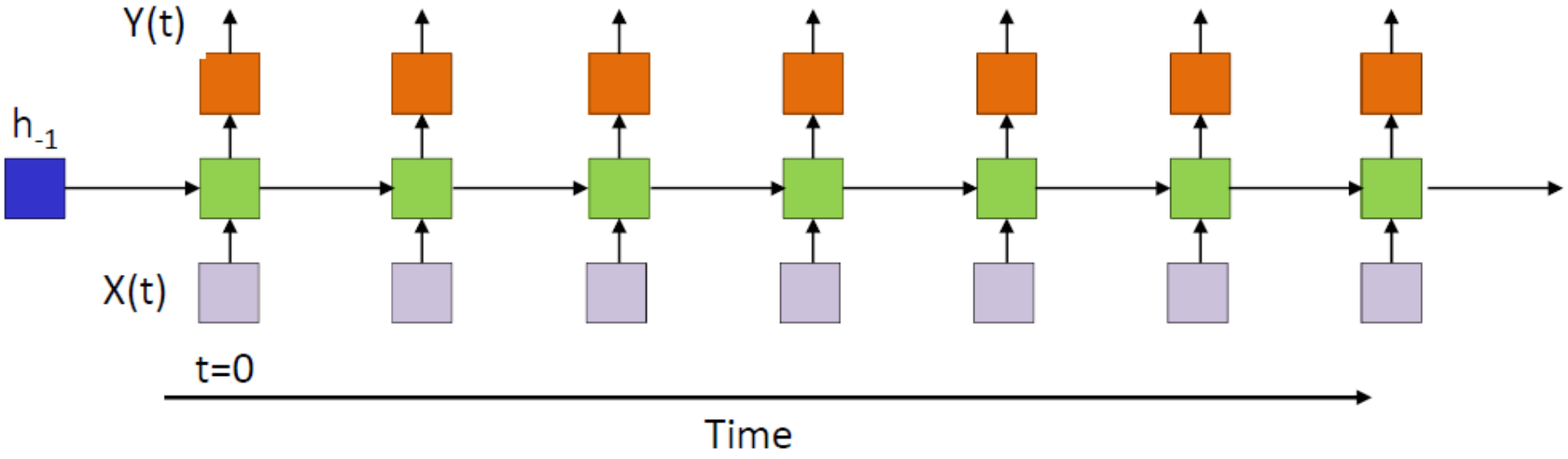
38 / 5000

深度学习是AI的热门领域。

Shēndù xuéxí shì AI de rèmén lǐngyù.

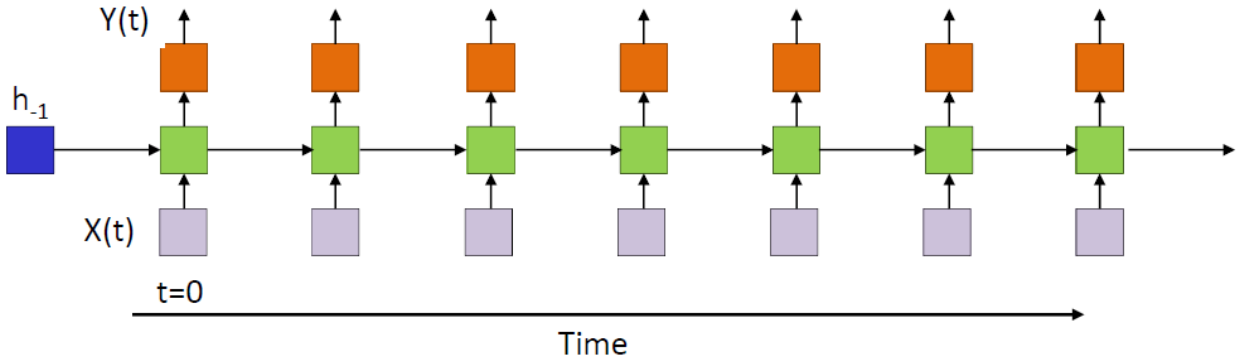
State-Space Model

- h_t: hidden state
- X_t: input
- Y_t: output
- $Y_t, h_t = f(h_{t-1}, X_t; \theta)$
- h_{-1}: initial state



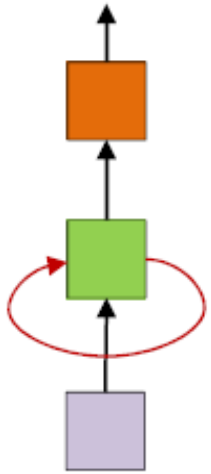
Recurrent Neural Network

- h_t: hidden state
- X_t: input
- Y_t: output
- $Y_t, h_t = f(h_{t-1}, X_t; \theta)$
- h_{-1}: initial state



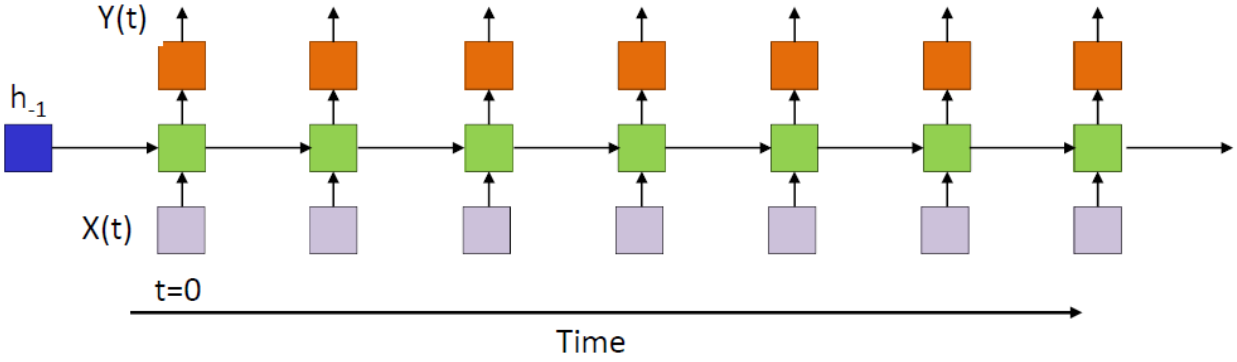
Fully-connect NN vs. RNN

- h_t: a vector summarizes all past inputs (a.k.a. "memory")
- h_{-1} affects the entire dynamics (typically set to zero)
- X_t affects all the outputs and states after t
- Y_t depends on $X_0, \ldots, X_t$



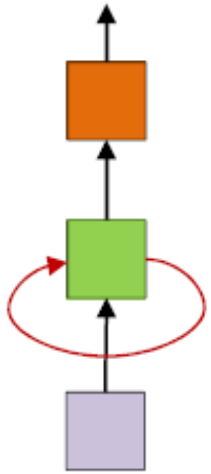
Recurrent Neural Network

- h_t: hidden state
- X_t: input
- Y_t: output
- $Y_t, h_t = f(h_{t-1}, X_t; \theta)$
- h_{-1}: initial state

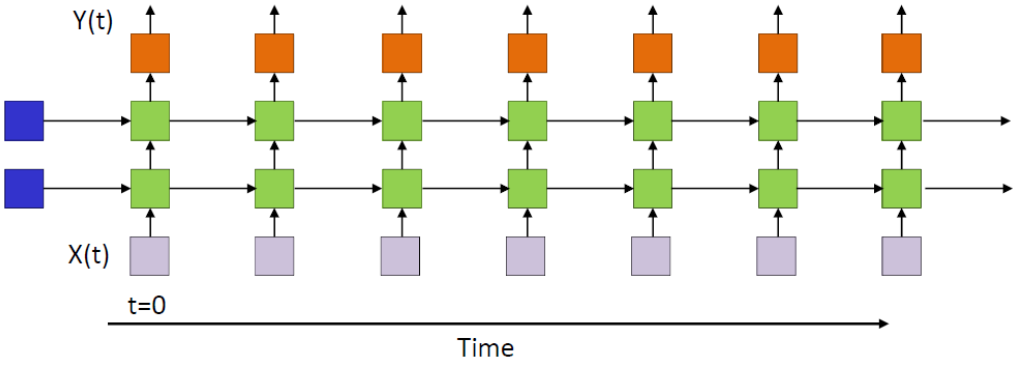


Fully-connect NN vs. RNN

- RNN can be viewed as repeated applying fully-connected NNs
- $h_t = \sigma_1(W^{(1)}X_t + W^{(11)}h_{t-1} + b^{(1)})$
- $Y_t = \sigma_2(W^{(2)}h_t + b^{(2)})$
- σ_1, σ_2 are activation functions (sigmoid, ReLU, tanh, etc)

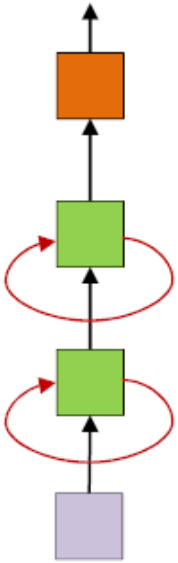


Recurrent Neural Network



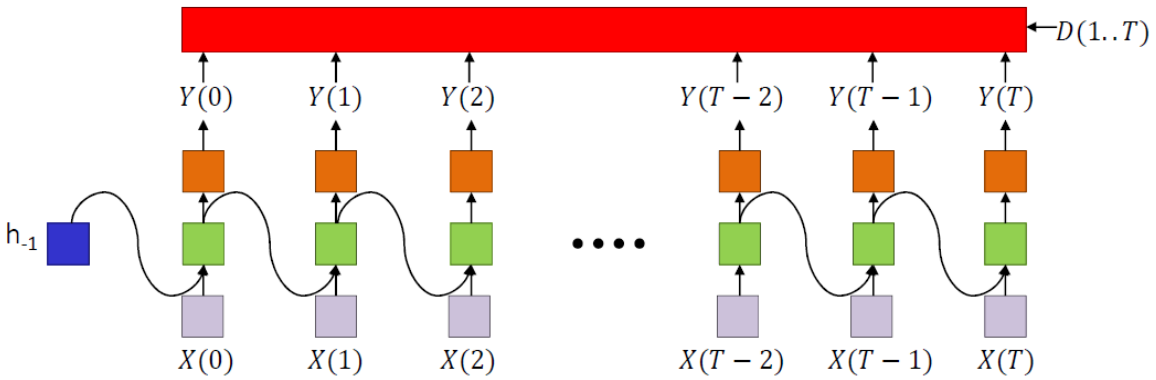
Stack *K* layers of fully-connected NN

- $h_t^{(k)}$: hidden state
- X_t: input
- Y_t: output
- $h_t^{(1)} = f_1^{(1)}(h_{t-1}^{(1)}, X_t; \theta)$
- $h_t^{(k)} = f_1^{(k)}(h_{t-1}^{(k)}, h_t^{(k-1)}; \theta)$
- $Y_t = f_2(h_t^{(K)}; \theta)$
- $h_{-1}^{(k)}$: initial states



Training Recurrent Neural Network

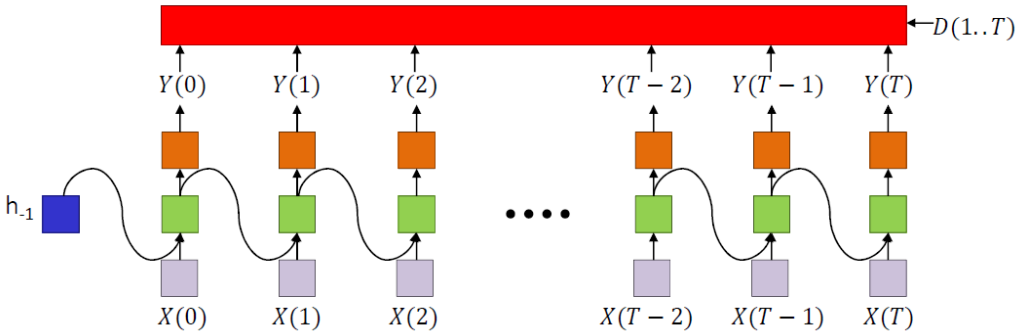
- h_t: hidden state
- X_t: input
- Y_t: output
- $Y_t, h_t = f(h_{t-1}, X_t; \theta)$
- h_{-1}: initial state



- Data: $\{(X_t, D_t)\}_{t=1}^{T}$ (RNN can handle more general data format)
- Loss $L(\theta) = \sum_{t=1}^{T} \ell(Y_t, D_t)$
- Goal: learn θ by gradient-based method
  - Back propagation

Back Propagation Through Time

- $h_t = \sigma_1(W^{(1)}X_t + W^{(11)}h_{t-1} + b^{(1)})$
- $Y_t = \sigma_2(W^{(2)}h_t + b^{(2)})$
- $Z_t^{(1)}$: pre-activation of hidden state ($h_t = \sigma_1(Z_t^{(1)})$)
- $Z_t^{(2)}$: pre-activation of output ($Y_t = \sigma_2(Z_t^{(2)})$)



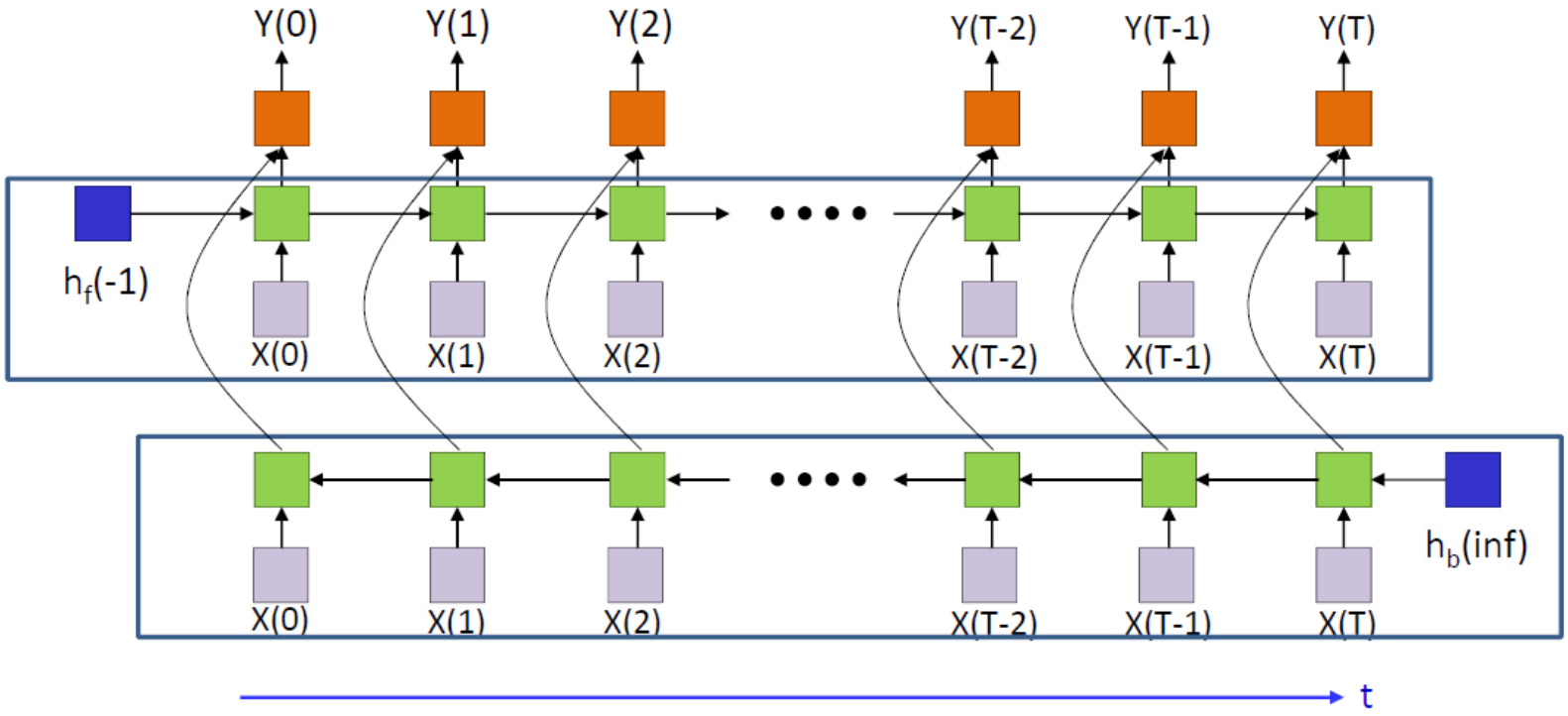
Back Propagation Through Time

Back Propagation Through Time

Extensions

What if Y_t depends on the entire inputs?

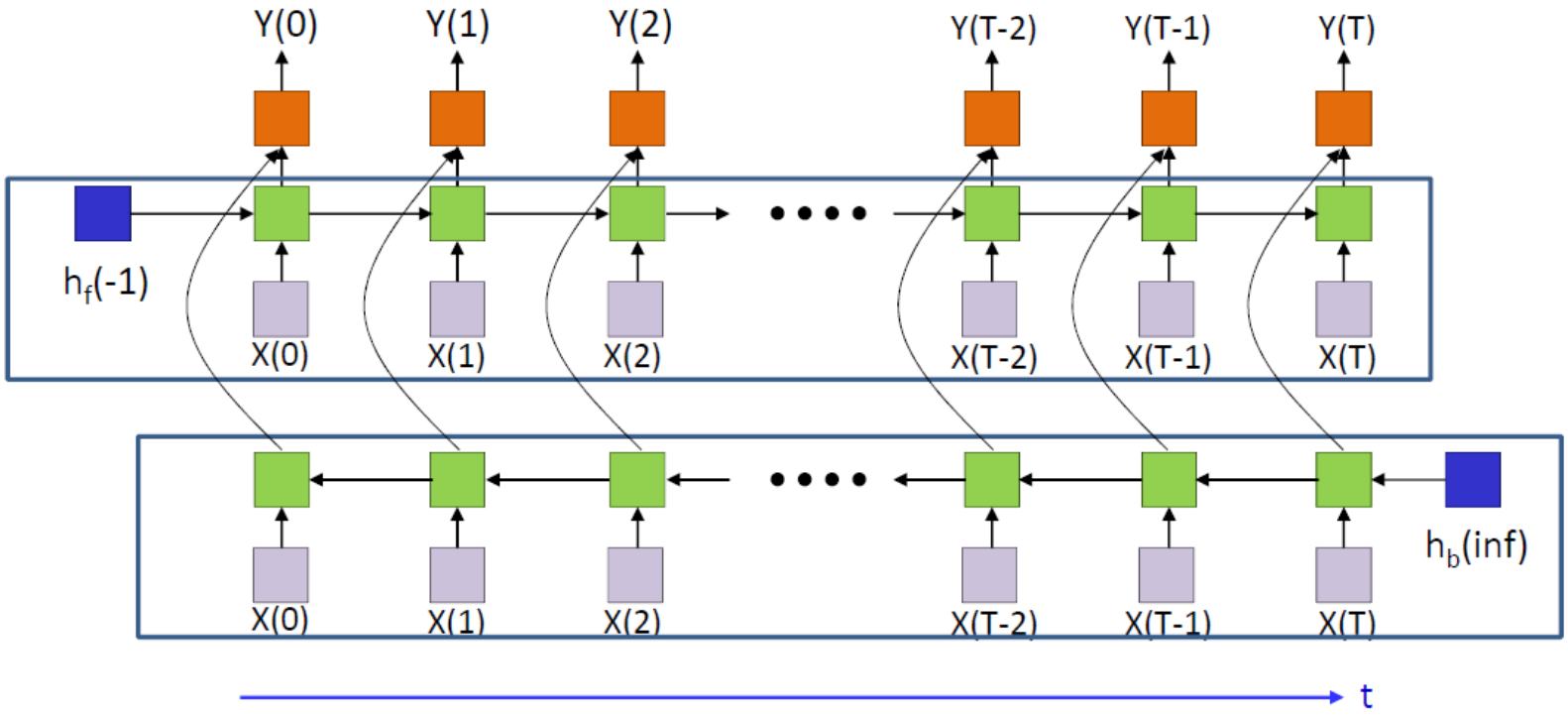
- Biredictional RNN:
  - AN RNN for forward dependencies: t= 0,…,T
  - An RNN for backward dependencies: t= T,…0
  - $Y_t = f_2(h_t^f, h_t^b; \theta)$



Extensions

RNN for sequence classification (sentiment analysis)

- $Y = \max_t Y_t$
- Cross-entropy loss



Practical issues of RNN

Linear RNN derivation

Practical issues of RNN: training

Gradient explosion and gradient vanishing

Techniques for avoiding gradient explosion

- Gradient clipping
- Identity initialization
- Truncated backprop through time
  - Only backprop for a few steps