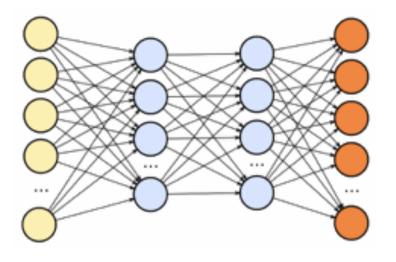
CSE 543/599I

Simon Du





CSE543/599I: Deep Learning

Instructor: Simon Du

Teaching Assistant: Prashant Rangarajan, Yuhao Wang

Course Website (contains all logistic information): https://courses.cs.washington.edu/

courses/cse543/22sp/

Piazza: https://piazza.com/washington/spring2022/cse543/home

Announcements: Canvas

Homework: Canvas

CSE543/599I: Deep Learning

What this class is:

- Fundamentals of DL: Neural network architecture, approximation properties, optimization, generalization, generative models, representation learning
- Preparation for further learning / research: the field is fastmoving, you will be able to apply the fundamentals and teach yourself the latest

What this class is not:

- An easy course: mathematically easy
- A survey course: laundry list of algorithms
- An application course: implementation of different architectures on different datasets

Prerequisites

- Working knowledge of:
 - Linear algebra
 - Vector calculus
 - Probability and statistics
 - Algorithms
 - Machine leanring (CSE 446/546)
- Mathematical maturity
- "Can I learn these topics concurrently?"

Lecture

- Time: Tuesday and Thursday 9:00 10:20AM
- CSE2 G10
- Slides + handwritten notes (e.g., proofs)
- Please ask questions
- Some lectures will be on Zoom
- Recording on Canvas
- Tentative schedule on course website

Homework (40%)

- 2 homework (20%+20%)
 - Each contains both theoretical questions and will have programming
 - Related to course materials
 - Collaboration okay but must write who you collaborated with. You must write, submit, and understand your answers and code
 - Submit on Canvas
 - Must be typed
 - □ Two late days
 - Tentative timeline:
 - □ HW 1 due: 4/22
 - □ HW 2 due: 5/6

Course Project (60%)

- Group of 1 2.
- Topic: literature review (state-of-the-art) or original research.
- Some potential topics are in listed on Canvas. OK to do a project on listed.
- You can work on a project related to your research.
- Proposal (due: 4/8): 5%
 - Format: NeurIPS Latex format, ~1 1.5 pages
- Presentations on (5/31 and 6/2 on Zoom): 20%
- Final report (due: 6/10): 35%
 - Format: NeurIPS Latex format, ~8 pages
- Submit on Canvas

Possible Topics

- Approximation properties
- Advanced optimization methods
- Optimization theory for deep learning
- Generalization theory for deep learning
- Deep reinforcement learning
- Implicit regularization
- Meta-learning algorithm / theory
- Robustness
- Lottery ticket hypothesis
- Deep learning application
- ...

Communication Chanels

- Announcements
 - Canvas
- questions about class, homework help
 - Piazza
 - Office hours:
 - □ Simon Du: Tu 10:30 11:30 AM (in person Gates 312 and Zoom)
 - Prashant Ranagarajan
 - Yuhao Wan
- Regrade requests / Personal concerns:
 - Email to instructor or TAs

Addcodes

 Email: Elle Brown (<u>ellean@cs.washington.edu</u>) for addcodes

Topic 1: Review (Today)

- ML Review: training, generalization
- Neural network basics: fully-connected neural network, gradient descent

Topic 2: Approximation Theory

- Why neural networks can express the (regression, classification, ...) function you want?
- Construction of such desired neural networks
- Universal approximation theorem

Topic 3: Optimization

- Review: Back-propagation
- Auto-differentiation
- Advanced optimizers: momentum (Nesterov acceleration), adaptive method (AdaGrad, Adam)
- Techniques for improving optimization
- Theory: global convergence of gradient of overparameterized neural networks
- Neural Tangent Kernel

Topic 4: Architecture

- Convolutional neural network
- Recurrent neural network
- Attention-based neural network
- General framework

Topic 5: Generalization

- Measures of generalization
- Double descent
- Techniques for improving generalization
- Generalization theory beyond VC-dimension
- Implicit regularization

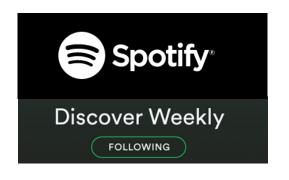
Topic 6: Unsupervised learning

- Explicit models
- Generative adversarial network
- Sampling

Topic 7: Representation Learning

- Transfer learning
- Domain adaptation
- Meta-learning
- Theory







ML uses past data to make predictions











Supervised Learning Process

Collect a dataset

Decide on a model

Find the function which fits the data best

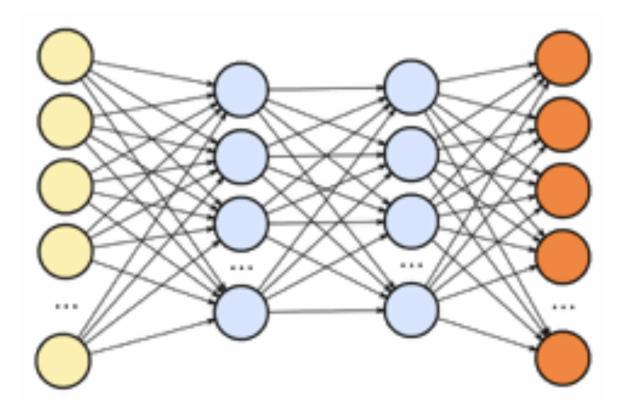
Choose a loss function

Pick the function which minimizes loss
on data

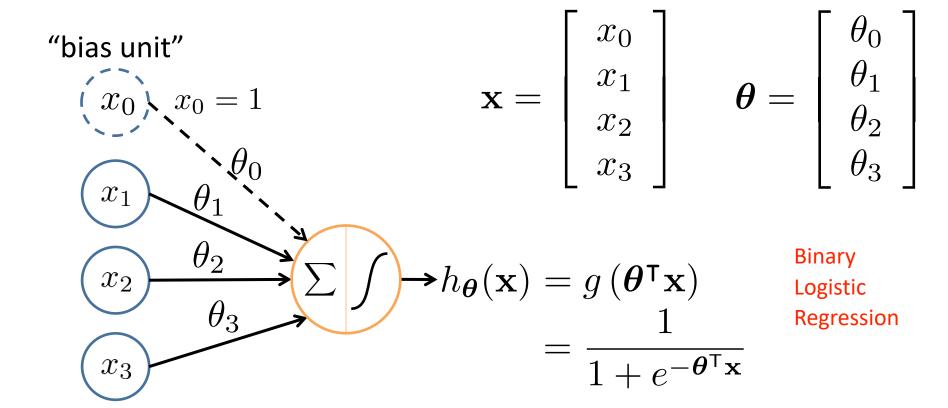
Use function to make prediction on new examples

Framework

Neural Networks

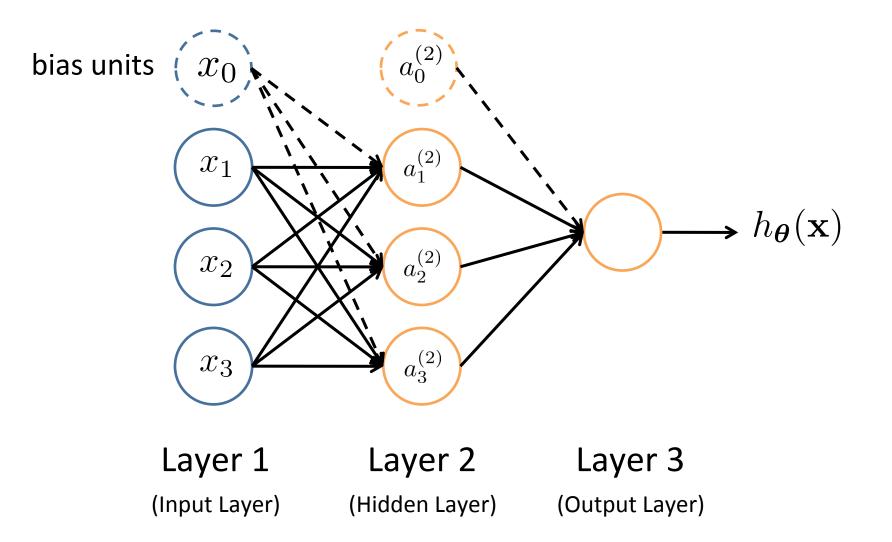


Single Node

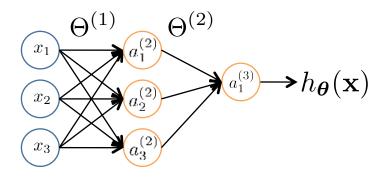


Sigmoid (logistic) activation function:
$$g(z) = \frac{1}{1 + e^{-z}}$$

Neural Network



Slide by Andrew Ng



 $a_i^{(j)}$ = "activation" of unit i in layer j

 $\Theta^{(j)}$ = weight matrix stores parameters from layer j to layer j + 1

$$a_{1}^{(2)} = g(\Theta_{10}^{(1)}x_{0} + \Theta_{11}^{(1)}x_{1} + \Theta_{12}^{(1)}x_{2} + \Theta_{13}^{(1)}x_{3})$$

$$a_{2}^{(2)} = g(\Theta_{20}^{(1)}x_{0} + \Theta_{21}^{(1)}x_{1} + \Theta_{22}^{(1)}x_{2} + \Theta_{23}^{(1)}x_{3})$$

$$a_{3}^{(2)} = g(\Theta_{30}^{(1)}x_{0} + \Theta_{31}^{(1)}x_{1} + \Theta_{32}^{(1)}x_{2} + \Theta_{33}^{(1)}x_{3})$$

$$h_{\Theta}(x) = a_{1}^{(3)} = g(\Theta_{10}^{(2)}a_{0}^{(2)} + \Theta_{11}^{(2)}a_{1}^{(2)} + \Theta_{12}^{(2)}a_{2}^{(2)} + \Theta_{13}^{(2)}a_{3}^{(2)})$$

If network has s_j units in layer j and s_{j+1} units in layer j+1, then $\Theta^{(j)}$ has dimension $s_{j+1} \times (s_j+1)$.

$$\Theta^{(1)} \in \mathbb{R}^{3 \times 4} \qquad \Theta^{(2)} \in \mathbb{R}^{1 \times 4}$$

Slide by Andrew Ng

Multi-layer Neural Network - Binary Classification

$$a^{(1)} = x$$

$$a^{(2)} = g(\Theta^{(1)}a^{(1)})$$

$$\vdots$$

$$a^{(l+1)} = g(\Theta^{(l)}a^{(l)})$$

$$\mathbf{a}^{(2)} = \mathbf{a}^{(3)}$$

$$\mathbf{a}^{(3)}$$

$$\widehat{y} = g(\Theta^{(L)}a^{(L)})$$

$$L(y, \widehat{y}) = y \log(\widehat{y}) + (1 - y) \log(1 - \widehat{y})$$

$$g(z) = \frac{1}{1 + e^{-z}}$$
Binary
Logistic
Regression

Multi-layer Neural Network - Binary Classification

$$a^{(1)} = x$$

$$a^{(2)} = \sigma(\Theta^{(1)}a^{(1)})$$

$$\vdots$$

$$a^{(l+1)} = \sigma(\Theta^{(l)}a^{(l)})$$

$$\mathbf{a}^{(2)} = \mathbf{a}^{(3)}$$

$$\mathbf{a}^{(4)}$$

$$\widehat{y} = g(\Theta^{(L)}a^{(L)})$$

$$L(y, \widehat{y}) = y \log(\widehat{y}) + (1 - y) \log(1 - \widehat{y})$$

$$\sigma(z) = \max\{0, z\} \quad g(z) = \frac{1}{1 + e^{-z}} \quad \text{Binary Logistic Regression}$$

Multiple Output Units: One-vs-Rest







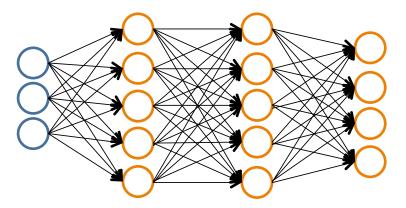


Pedestrian

Car

Motorcycle

Truck



$$h_{\Theta}(\mathbf{x}) \in \mathbb{R}^K$$

Multi-class Logistic Regression

We want:

$$h_{\Theta}(\mathbf{x}) pprox \begin{bmatrix} 1\\0\\0\\0 \end{bmatrix} \qquad h_{\Theta}(\mathbf{x}) pprox \begin{bmatrix} 0\\1\\0\\0 \end{bmatrix} \qquad h_{\Theta}(\mathbf{x}) pprox \begin{bmatrix} 0\\0\\1\\0 \end{bmatrix} \qquad h_{\Theta}(\mathbf{x}) pprox \begin{bmatrix} 0\\0\\1\\1 \end{bmatrix}$$

when pedestrian

$$h_{\Theta}(\mathbf{x}) \approx \begin{bmatrix} 0 \\ 1 \\ 0 \\ 0 \end{bmatrix}$$

$$h_{\Theta}(\mathbf{x}) \approx \begin{bmatrix} 0 \\ 0 \\ 1 \\ 0 \end{bmatrix}$$

$$h_{\Theta}(\mathbf{x}) \approx \begin{bmatrix} 0 \\ 0 \\ 0 \\ 1 \end{bmatrix}$$

when truck

17 Slide by Andrew Ng

Multi-layer Neural Network - Regression

$$a^{(1)} = x$$

$$a^{(2)} = \sigma(\Theta^{(1)}a^{(1)})$$

$$a^{(1)} = \sigma(\Theta^{(l)}a^{(l)})$$

$$a^{(2)} = \sigma(\Theta^{(l)}a^{(l)})$$

$$a^{(2)} = \sigma(\Theta^{(l)}a^{(l)})$$

$$a^{(2)} = \sigma(\Theta^{(l)}a^{(l)})$$

$$a^{(2)} = \sigma(\Theta^{(l)}a^{(l)})$$

$$\widehat{y} = \Theta^{(L)} a^{(L)}$$

$$L(y,\widehat{y}) = (y-\widehat{y})^2$$

$$\sigma(z) = \max\{0,z\}$$
 Regression

$$a^{(1)} = x$$

$$z^{(2)} = \Theta^{(1)}a^{(1)}$$

$$a^{(2)} = g(z^{(2)})$$

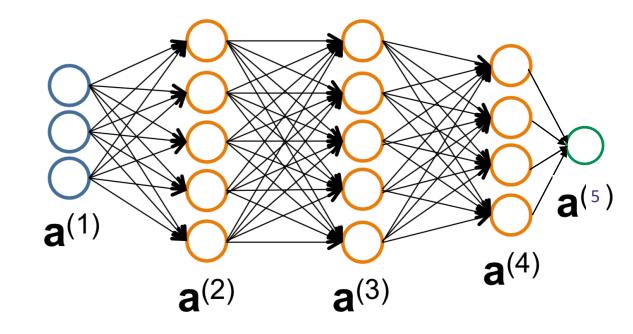
$$\vdots$$

$$z^{(l+1)} = \Theta^{(l)}a^{(l)}$$

$$a^{(l+1)} = g(z^{(l+1)})$$

$$\vdots$$

$$\widehat{y} = g(\Theta^{(L)}a^{(L)})$$



$$L(y, \hat{y}) = y \log(\hat{y}) + (1 - y)\log(1 - \hat{y})$$
$$g(z) = \frac{1}{1 + e^{-z}}$$

Gradient Descent: $\Theta^{(l)} \leftarrow \Theta^{(l)} - \eta \nabla_{\Theta^{(l)}} L(y, \widehat{y}) \qquad \forall l$

Gradient Descent:

$$\Theta^{(l)} \leftarrow \Theta^{(l)} - \eta \nabla_{\Theta^{(l)}} L(y, \widehat{y})$$

 $\forall l$

Seems simple enough, why are packages like PyTorch, Tensorflow, Theano, Cafe, MxNet synonymous with deep learning?

1. Automatic differentiation

2. Convenient libraries

3. GPU support

Gradient Descent:

Seems simple enough, Theano, Cafe, MxNet s

1. Automatic differ

2. Convenient libra

```
class Net(nn.Module):
    def __init__(self):
        super(Net, self).__init__()
        # 1 input image channel, 6 output channels, 3x3 square convolution
        # kernel
        self.conv1 = nn.Conv2d(1, 6, 3)
        self.conv2 = nn.Conv2d(6, 16, 3)
        # an affine operation: y = Wx + b
        self.fc1 = nn.Linear(16 \star 6 \star 6, 120) # 6\star6 from image dimension
        self.fc2 = nn.Linear(120, 84)
        self.fc3 = nn.Linear(84, 10)
    def forward(self, x):
        # Max pooling over a (2, 2) window
        x = F.max_pool2d(F.relu(self.conv1(x)), (2, 2))
        # If the size is a square you can only specify a single number
        x = F.max_pool2d(F.relu(self.conv2(x)), 2)
        x = x.view(-1, self.num_flat_features(x))
        x = F.relu(self.fc1(x))
        x = F.relu(self.fc2(x))
        x = self.fc3(x)
        return x
```

```
# create your optimizer
optimizer = optim.SGD(net.parameters(), lr=0.01)

# in your training loop:
optimizer.zero_grad() # zero the gradient buffers
output = net(input)
loss = criterion(output, target)
loss.backward()
optimizer.step() # Does the update
```