## What is the neural code?



Sekuler lab, Brandeis

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Alan Litke, UCSD

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## What is the neural code?

Encoding: how does a stimulus cause a pattern of responses?

- what are the responses and what are their characteristics?
- neural models:
what takes us from stimulus to response;
descriptive and mechanistic models, and the relation between them.
Decoding: what do these responses tell us about the stimulus?
- Implies some kind of decoding algorithm
- How to evaluate how good our algorithm is?


## What is the neural code?



Single cells:
spike rate
spike times
spike intervals

## What is the neural code?



Single cells:
spike rate: what does the firing rate correspond to? spike times: what in the stimulus triggers a spike? spike intervals: can patterns of spikes convey extra information?

## What is the neural code?



Populations of cells:
population coding correlations between responses synergy and redundancy

## Receptive fields and tuning curves

Tuning curve: $r=f(s)$


Gaussian tuning curve of a cortical (V1) neuron

## Receptive fields and tuning curves

Tuning curve: $r=f(s)$


Cosine tuning curve of a motor cortical neuron

## Receptive fields and tuning curves



Sigmoid/logistic tuning curve of a "stereo" V1 neuron

Higher brain areas represent increasingly complex features


Quian Quiroga, Reddy, Kreiman, Koch and Fried, Nature (2005)





More generally, we are interested in determining the relationship:

> | P(response \| stimulus) encoding |
| :--- | :--- |

P(stimulus | response) decoding

Due to noise, this is a stochastic description.
Problem of dimensionality, both in response and in stimulus

## Reverse correlation

Fast modulation of firing by dynamic stimuli

Feature extraction


Use reverse correlation to decide what each of these spiking events stands for, and so to either:
-- predict the time-varying firing rate
-- reconstruct the stimulus from the spikes

## Reverse correlation

Basic idea: throw random stimuli at the system and collect the ones that cause a response

Typically, use Gaussian, white noise stimulus: an unbiased stimulus which samples all directions equally


## Reverse correlation



## Example: a neuron in the ELL of a fish

stimulus = fluctuating potential (generates electric field)


Spike-triggered Average


This can be done with other dimensions of stimulus as well
Spatio-temporal receptive field


## Modeling spike encoding

Given a stimulus, when will the system spike?
Decompose the neural computation into a linear stage and a nonlinear stage.


Simple example: the integrate-and-fire neuron

To what feature in the stimulus is the system sensitive?
Gerstner, spike response model; Aguera y Arcas et al. 2001, 2003; Keat et al., 2001

## Modeling spike encoding

spike-triggering<br>stimulus feature

decision function


The decision function is P (spike $\left.\mid \mathrm{x}_{1}\right)$.
Derive from data using Bayes' theorem:

$$
P\left(\text { spike } \mid x_{1}\right)=P(\text { spike }) P\left(x_{1} \mid \text { spike }\right) / P\left(x_{1}\right)
$$

$P\left(x_{1}\right)$ is the prior : the distribution of all projections onto $f_{1}$
$\mathrm{P}\left(\mathrm{x}_{1} \mid\right.$ spike $)$ is the spike-conditional ensemble :
the distribution of all projections onto $f_{1}$ given there has been a spike
P (spike) is proportional to the mean firing rate

## Models of neural function

spike-triggering<br>stimulus feature

decision function


Weaknesses

## Reverse correlation: a geometric view




## Functional models of neural response

spike-triggering stimulus features

multidimensional
decision function


## Functional models of neural response

spike-triggering stimulus features

decision function


## Functional models of neural response

spike-triggering<br>stimulus feature

decision function


## Covariance analysis

Let's develop some intuition for how this works: the Keat model
Keat, Reinagel, Reid and Meister, Predicting every spike. Neuron (2001)


- Spiking is controlled by a single filter
- Spikes happen generally on an upward threshold crossing of the filtered stimulus
$\rightarrow$ expect 2 modes, the filter $F(t)$ and its time derivative $F^{\prime}(\mathrm{t})$


## Covariance analysis



## Covariance analysis

Let's try a real neuron: rat somatosensory cortex
(Ras Petersen, Mathew Diamond, SISSA)


Record from single units in barrel cortex


## Covariance analysis

Spike-triggered average:


## Covariance analysis

Is the neuron simply not very responsive to a white noise stimulus?


## Covariance analysis



## Covariance analysis

Eigenspectrum
Leading modes


## Covariance analysis

Input/output relations wrt first two filters, alone:
and in quadrature:





## Covariance analysis

How about the other modes?

Next pair with +ve eigenvalues
Pair with -ve eigenvalues


## Covariance analysis

Input/output relations for negative pair


Firing rate decreases with increasing projection: suppressive modes

## Beyond covariance analysis

1. Single, best filter determined by the first moment
2. A family of filters derived using the second moment
3. Use the entire distribution: information theoretic methods
$\rightarrow$ Find the dimensions that maximize the mutual information between stimulus and spike

Removes requirement for Gaussian stimuli

## Limitations

Not a completely "blind" procedure: have to have some idea of the appropriate stimulus space

Very complex stimuli: does a geometrical picture work or make sense?

Rates vs spikes:
what is our model trying to do? What do we want to recover?

Adaptation:
stimulus representations change with experience!

