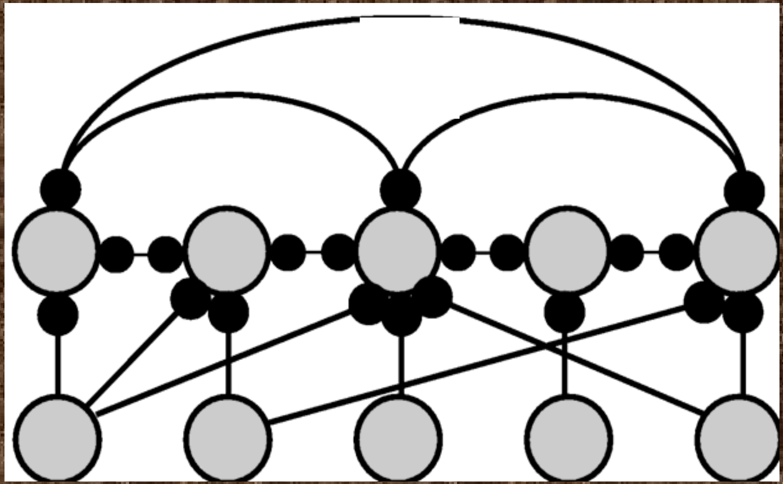
CSE/NB 528

Final Lecture: All Good Things Must…

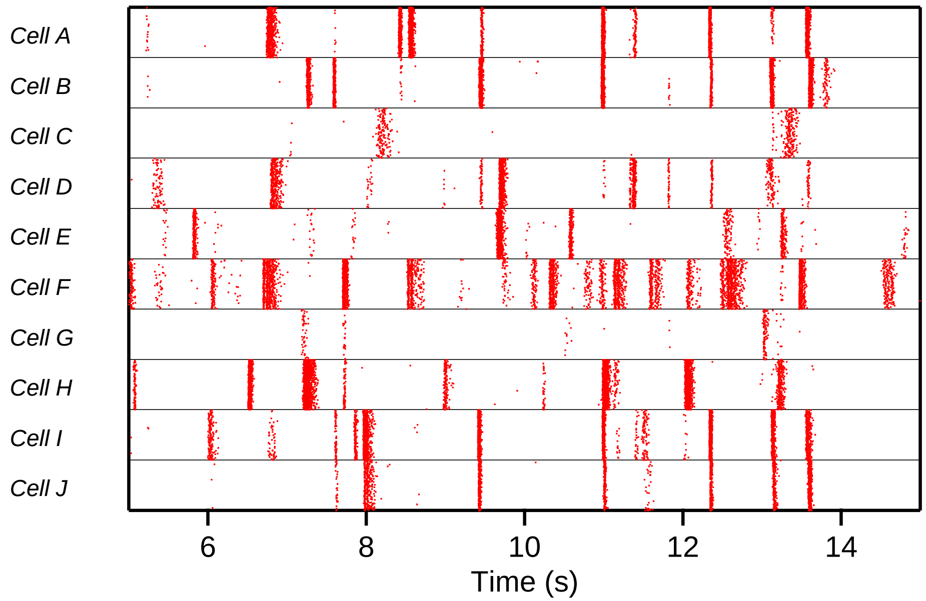


Lecture figures are from Dayan & Abbott's book
http://people.brandeis.edu/~abbott/book/index.html

Course Summary
(All good things must…come to an end)

- **Where have we been?**
  - Course Highlights
- **Where do we go from here?**
  - Challenges and Open Problems
- **Further Reading**

What *is* the neural code?



What is the nature of the code?

How should we represent the spiking output?

single cells vs populations

rates vs spike times vs intervals

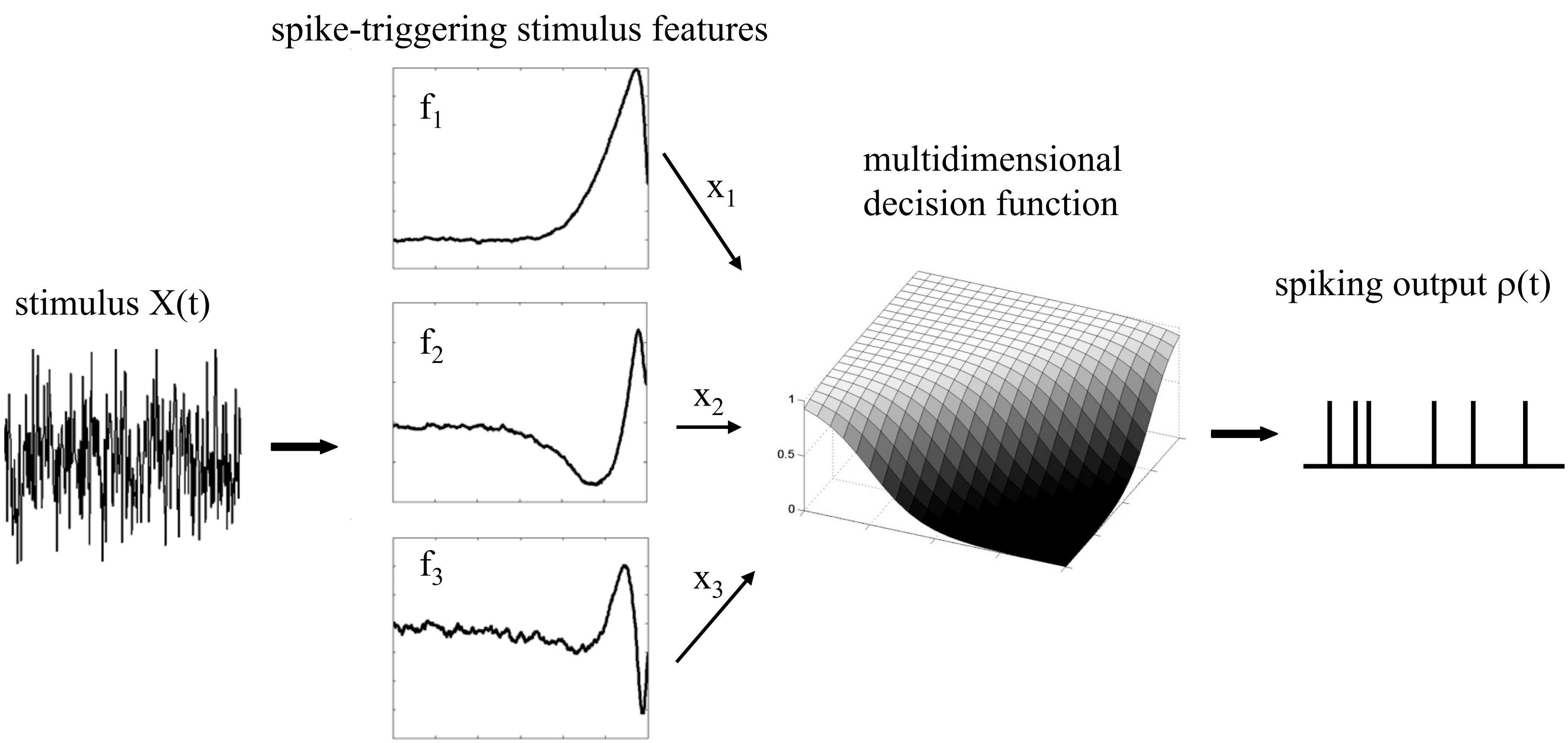
What features of the stimulus does the neural system represent?

Encoding and decoding neural information

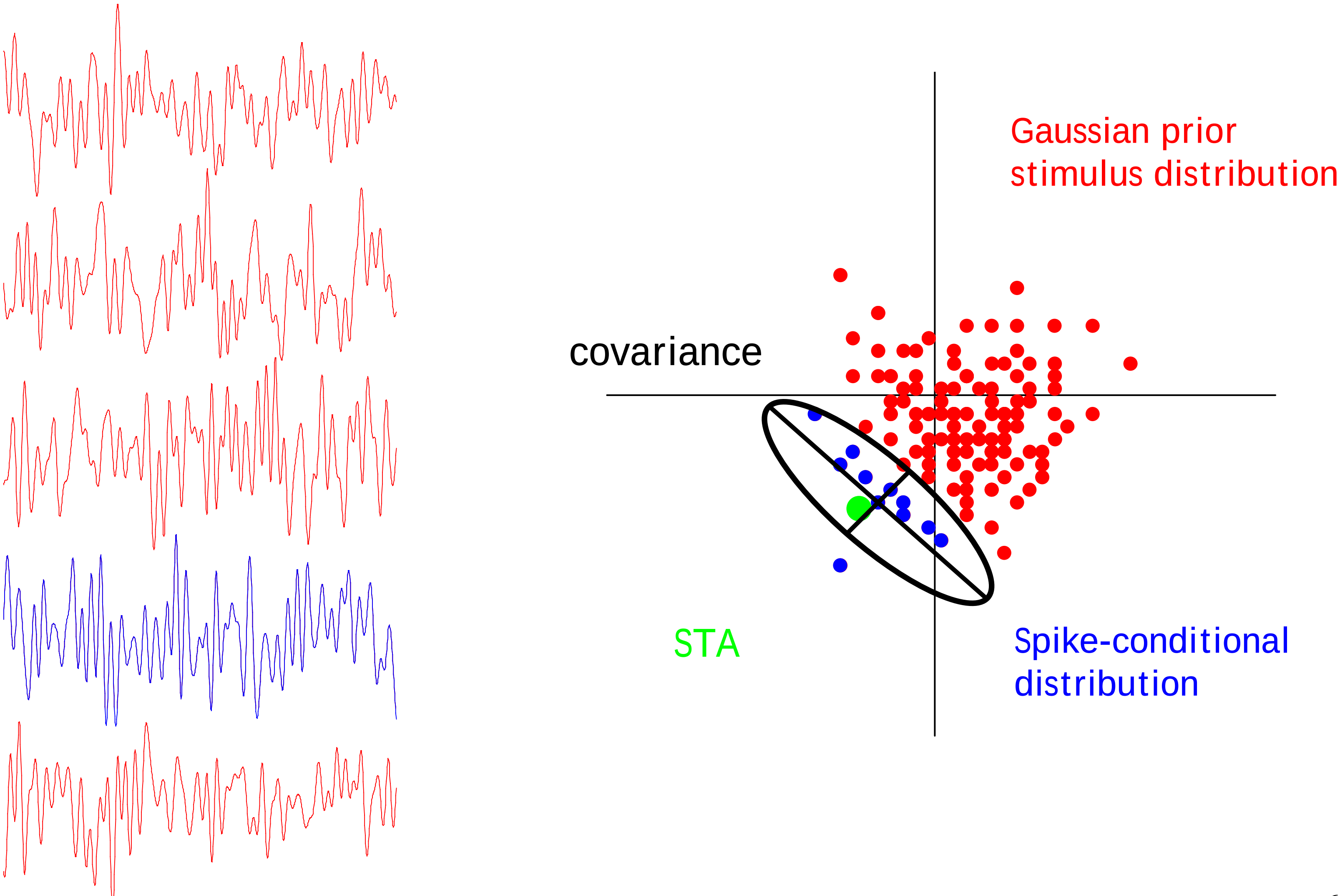
Encoding: building functional models of neurons/neural systems and predicting the spiking output given the stimulus

Decoding: what can we say about the stimulus given what we observe from the neuron or neural population?

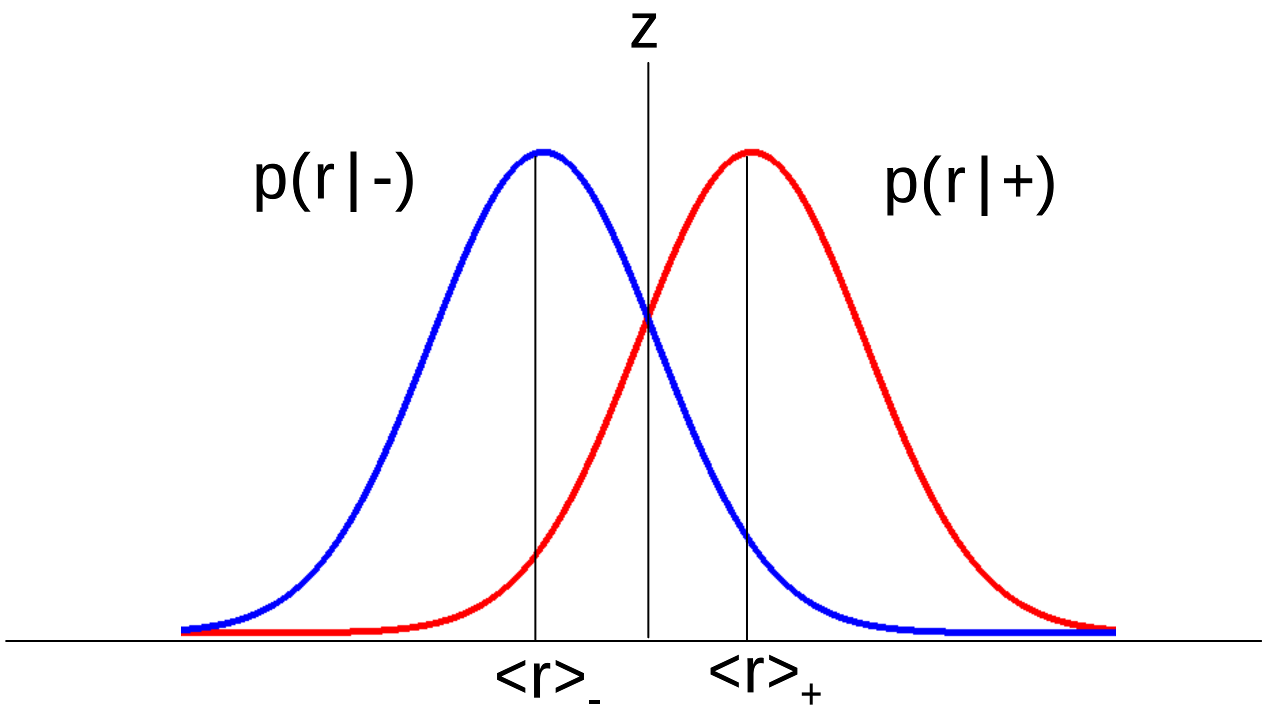
Highlights: Neural Encoding



Highlights: Finding the feature space of a neural system



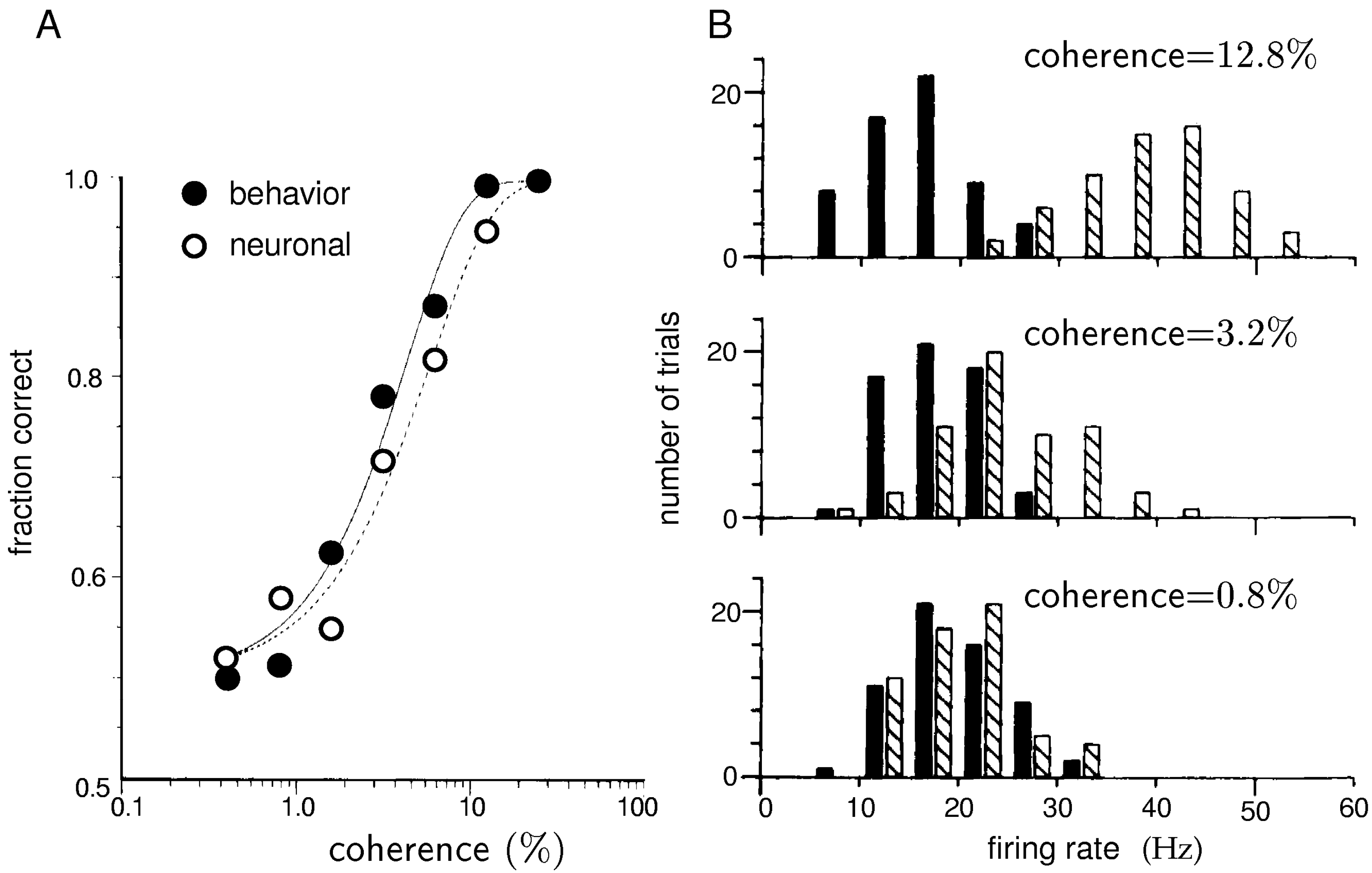
Decoding: Signal detection theory



Decoding corresponds to comparing test to threshold.

$\alpha(z) = P[\ r \geq z|-]$ false alarm rate, "size"

$\beta(z) = P[\ r \geq z|+]$ hit rate, "power"

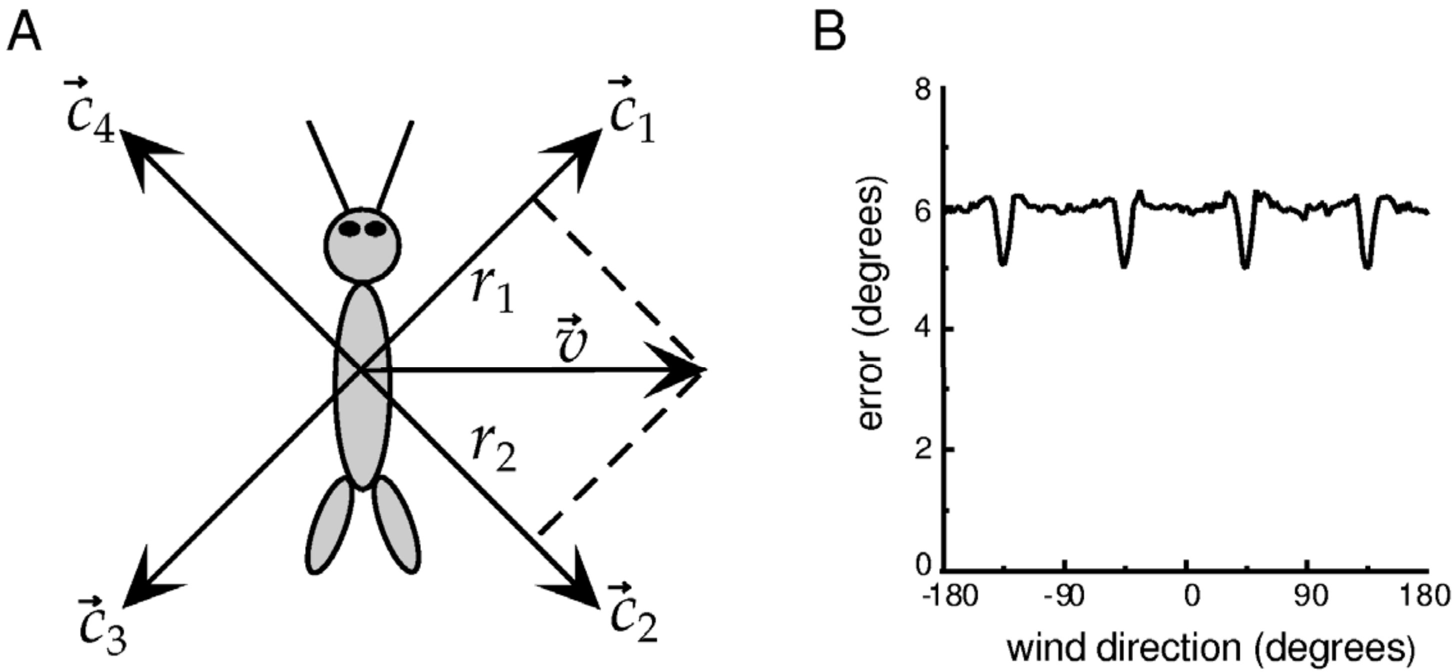


Close correspondence between neural performance and behaviour

Decoding from a population

e.g. cosine tuning curves

$$\vec{v}_{\text{pop}} = \sum_{a=1}^{4} \left(\frac{r}{r_{\max}} \right)_a \vec{c}_a$$



RMS error in estimate

Theunissen & Miller, 1991

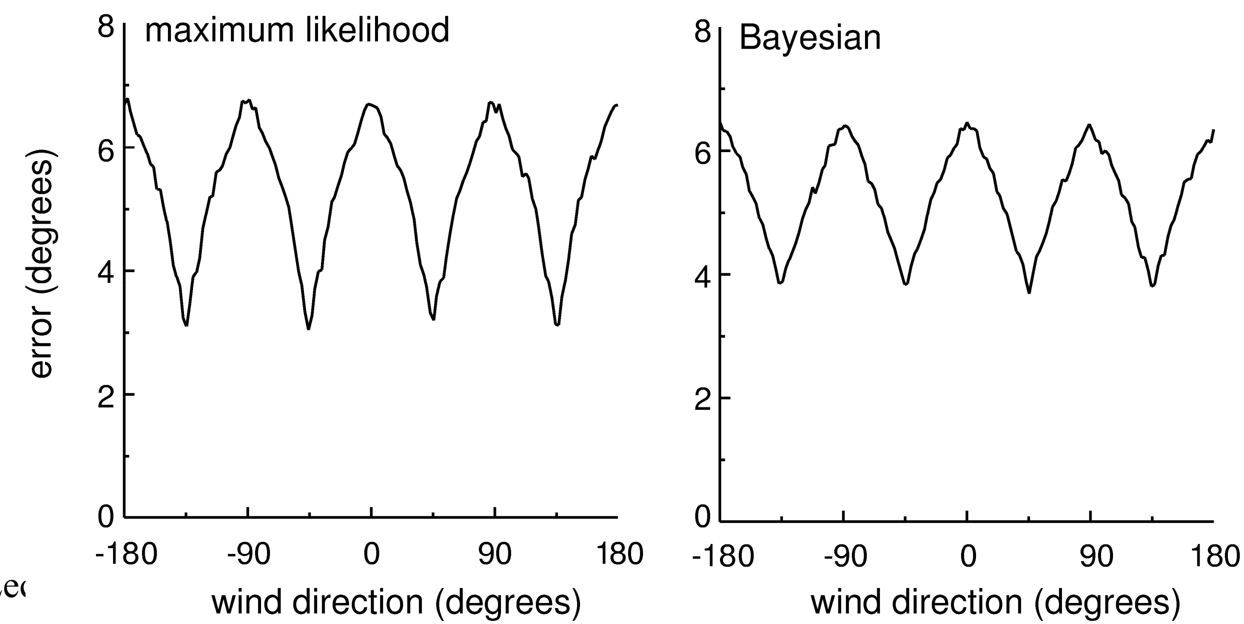
More general approaches: MAP and ML

MAP: s* which maximizes p[s|r]

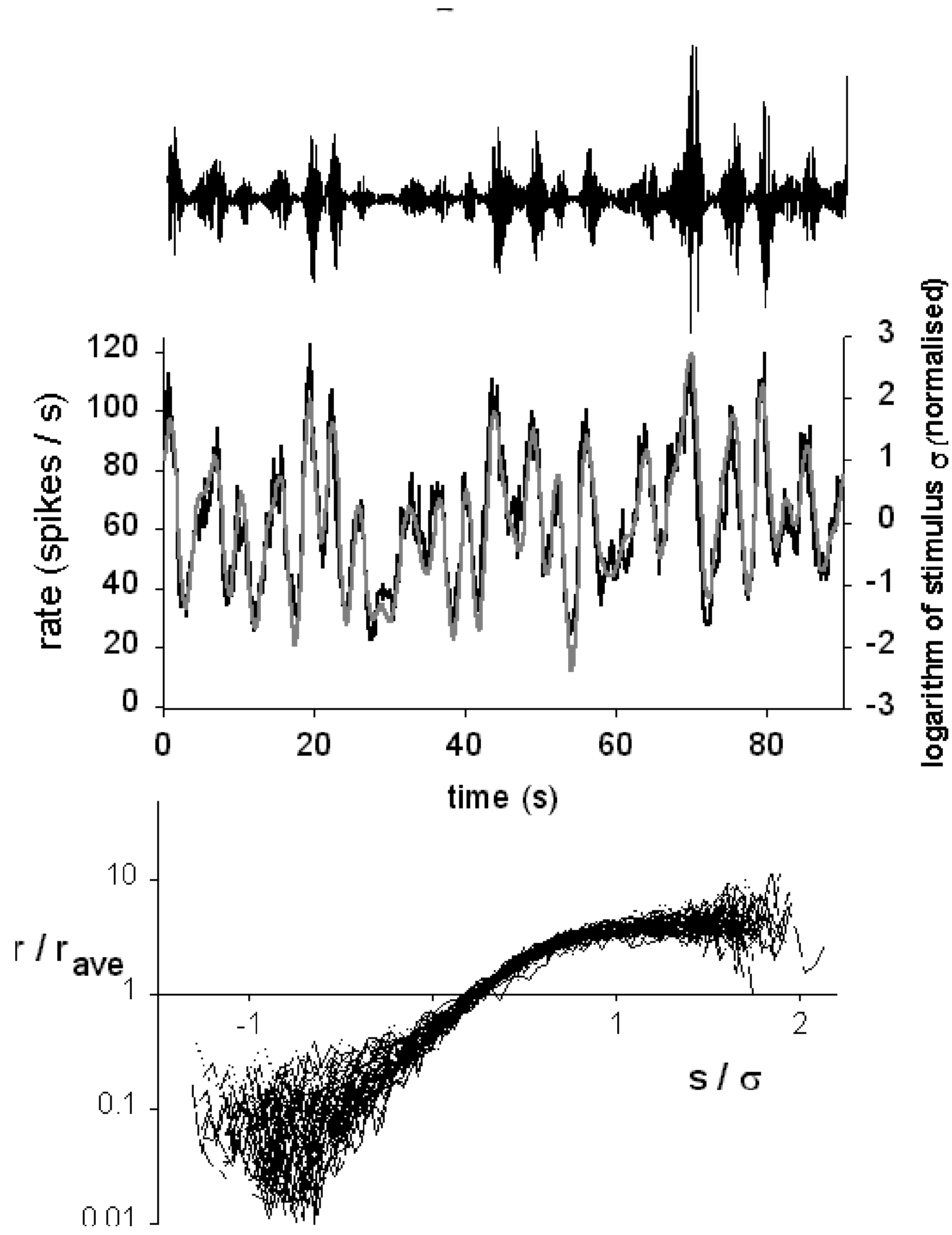
ML: s* which maximizes p[r|s]

Difference is the role of the prior: differ by factor p[s]/p[r]

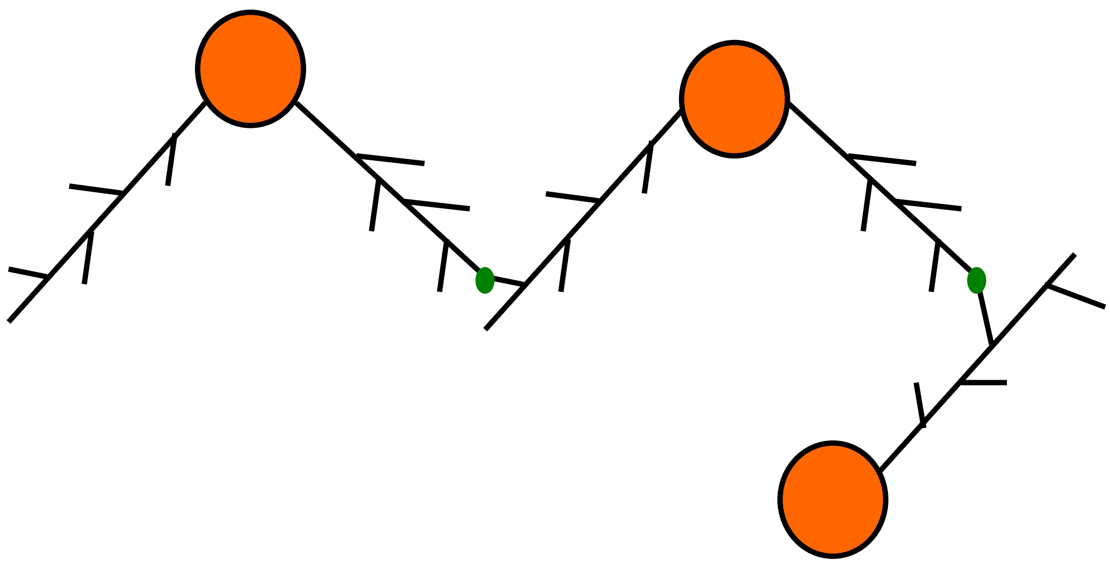
For cercal data:



Highlights:
Information maximization as a design principle of the nervous system

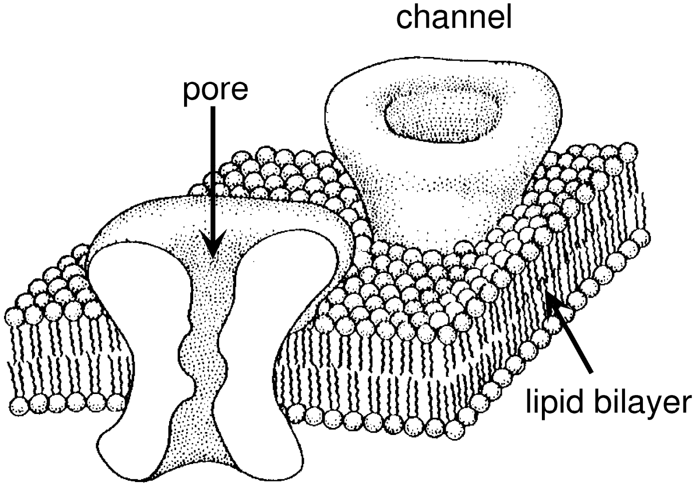


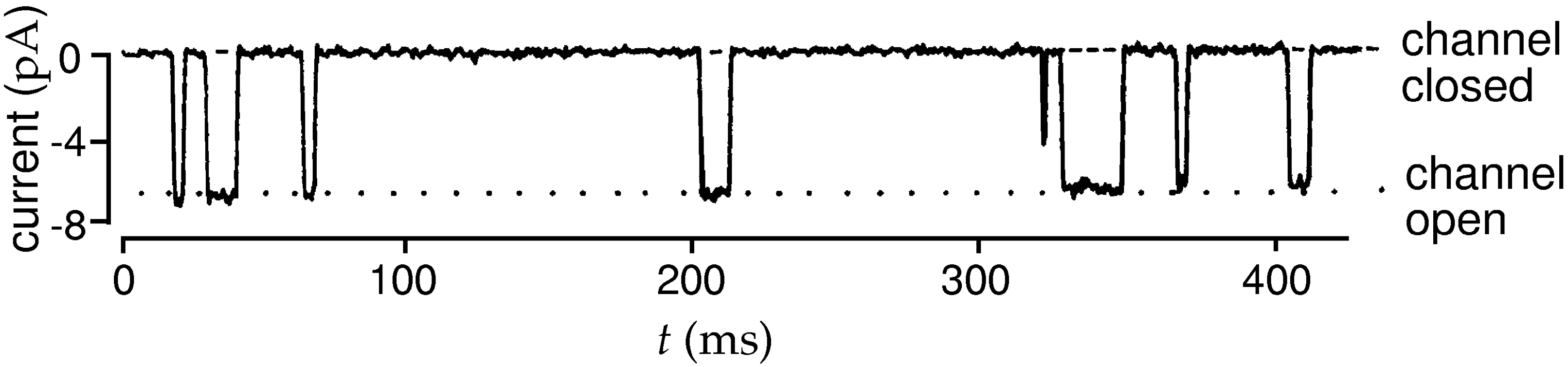
The biophysical basis of neural computation



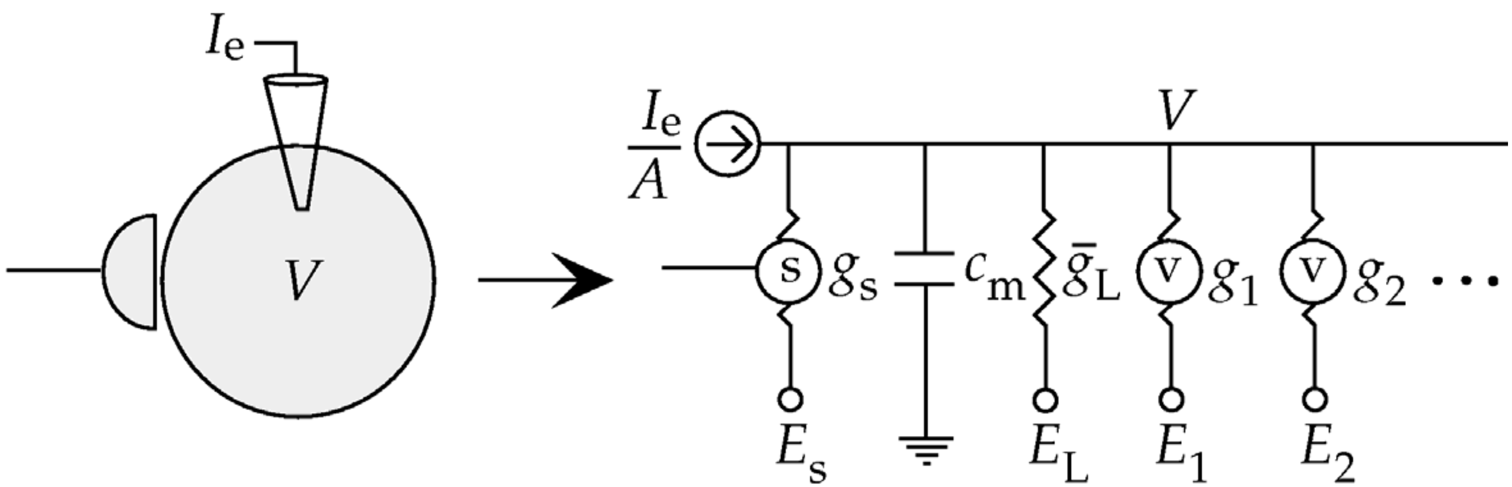
Excitability is due to the properties of ion channels

- Voltage dependent
- transmitter dependent (synaptic)
- Ca dependent





Highlights: The neural equivalent circuit



Ohm's law: $V = IR$ and Kirchhoff's law

$$\boxed{-C_m \frac{dV}{dt}} = \boxed{\sum_i g_i(V - E_i)} + \boxed{I_e}$$

Capacitive current

Ionic currents

Externally applied current

Simplified neural models

A sequence of neural models of increasing complexity that approach the behavior of real neurons

Integrate and fire neuron:

subthreshold, like a passive membrane
spiking is due to an imposed threshold at V_T

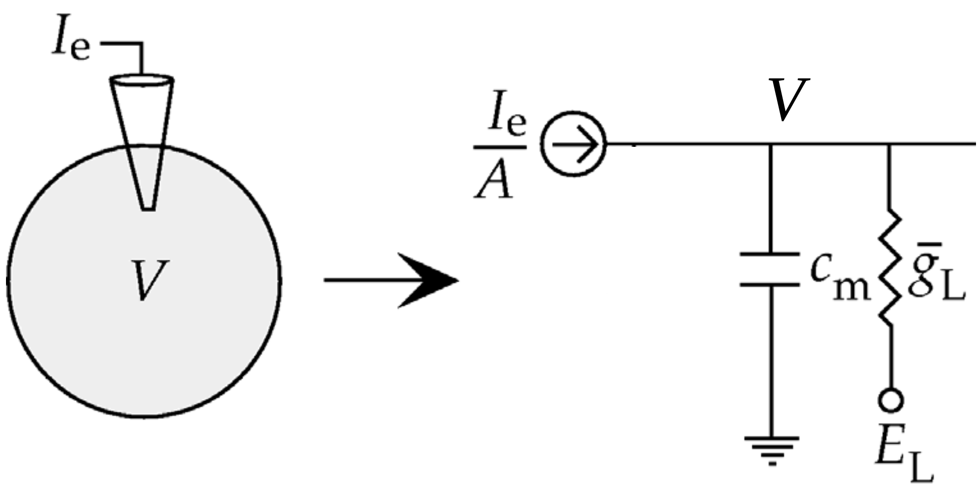
Spike response model:

subthreshold, arbitrary kernel
spiking is due to an imposed threshold at V_T
postspike, incorporates afterhyperpolarization

Simple model:

complete 2D dynamical system
spiking threshold is intrinsic
have to include a reset potential

Simplified Models: Integrate-and-Fire

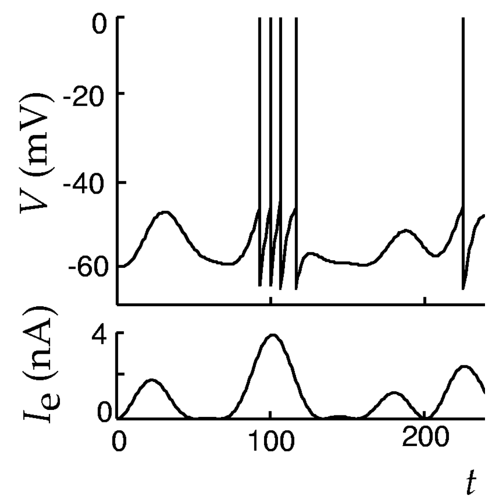


Integrate-and-Fire Model

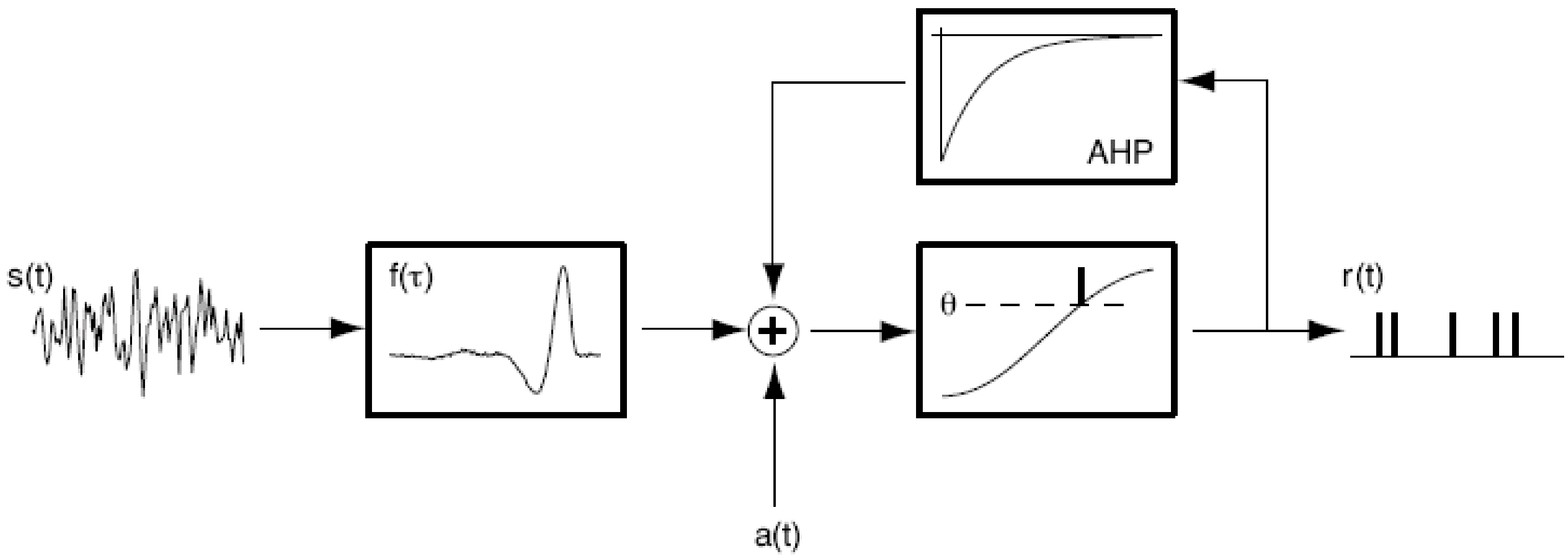
$$\tau_m \frac{dV}{dt} = -(V - E_L) + I_e R_m$$

If V > $V_{threshold}$ → Spike

Then reset: V = V_{reset}



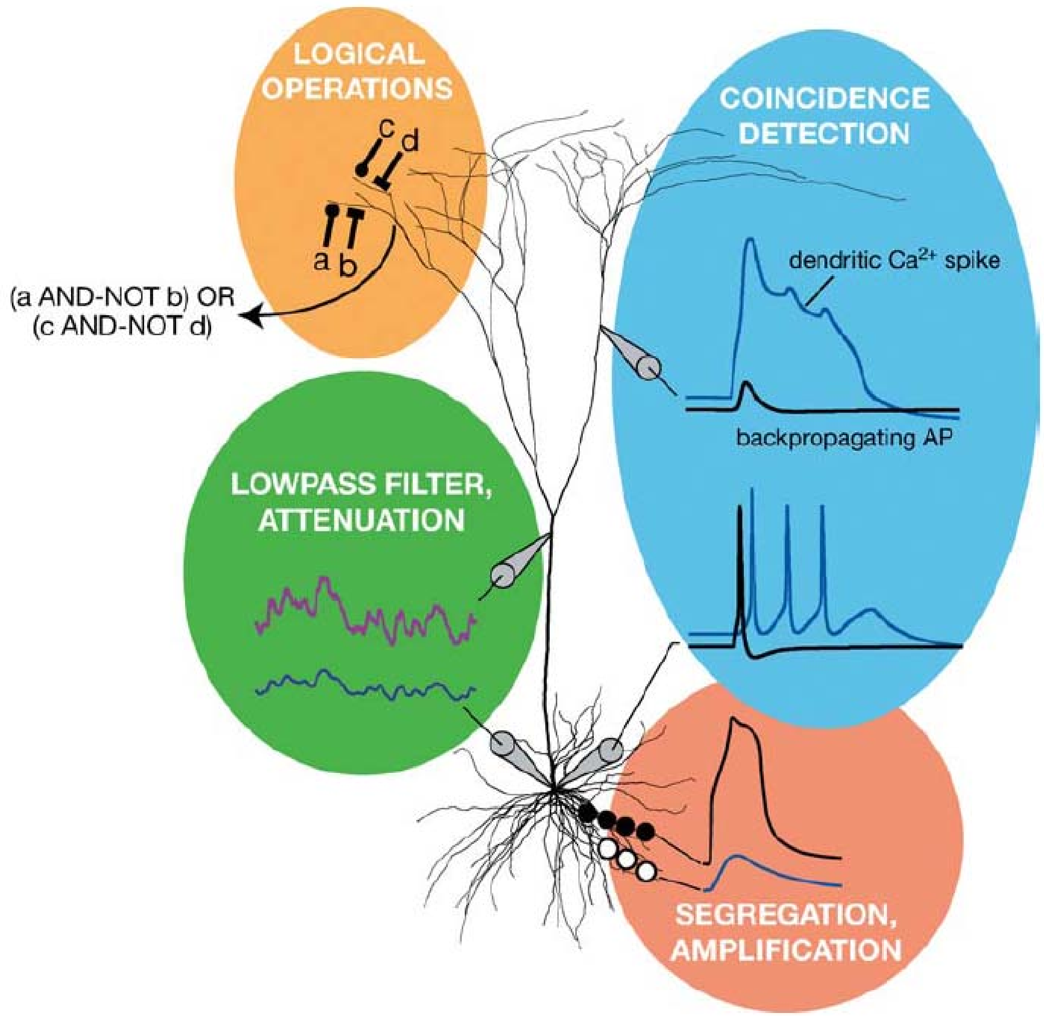
Simplified Models: Spike response model



Keat, Reinagel and Meister

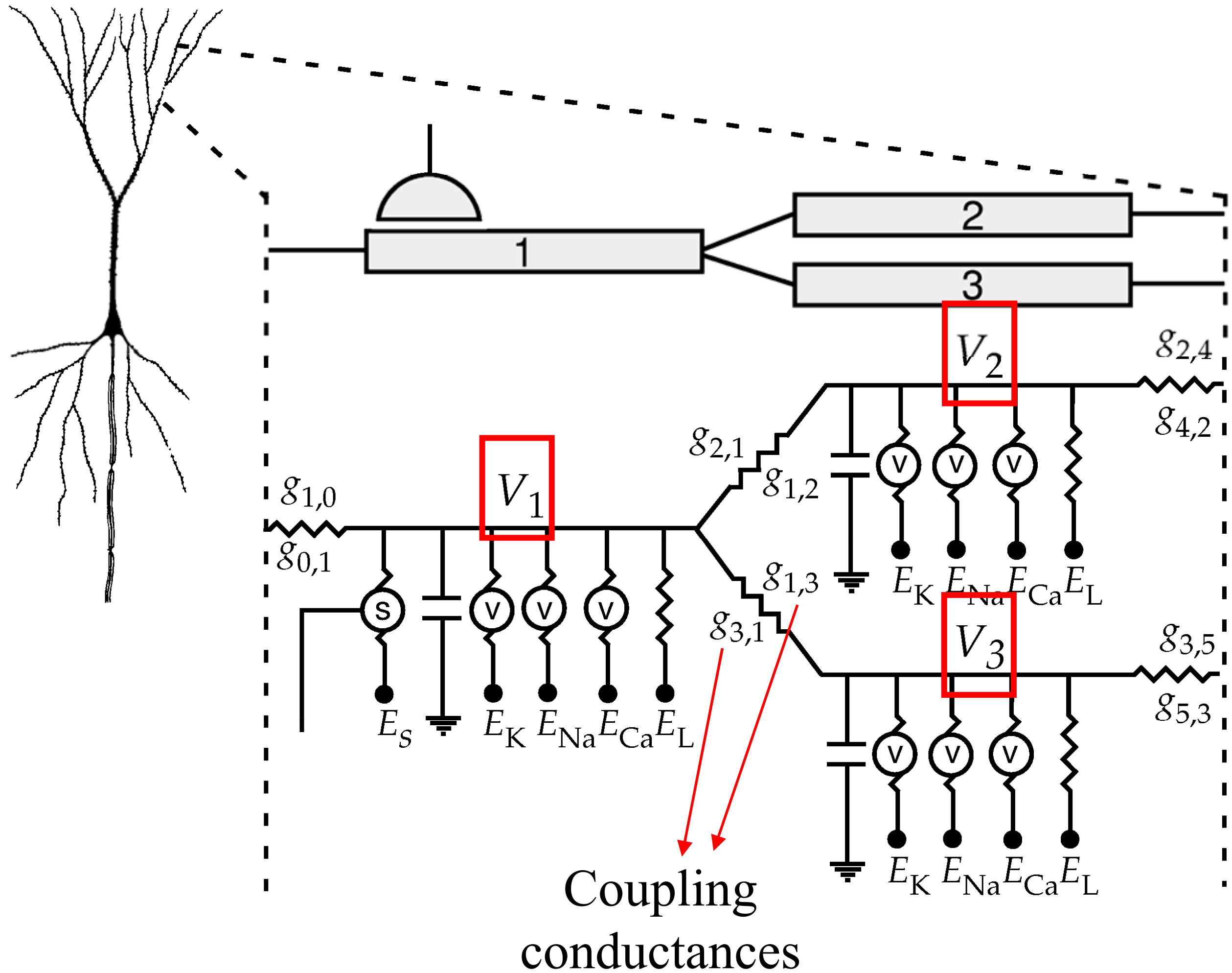
Highlights: Dendritic computation

Filtering
Shunting
Delay lines
Information segregation
Synaptic scaling
Direction selectivity

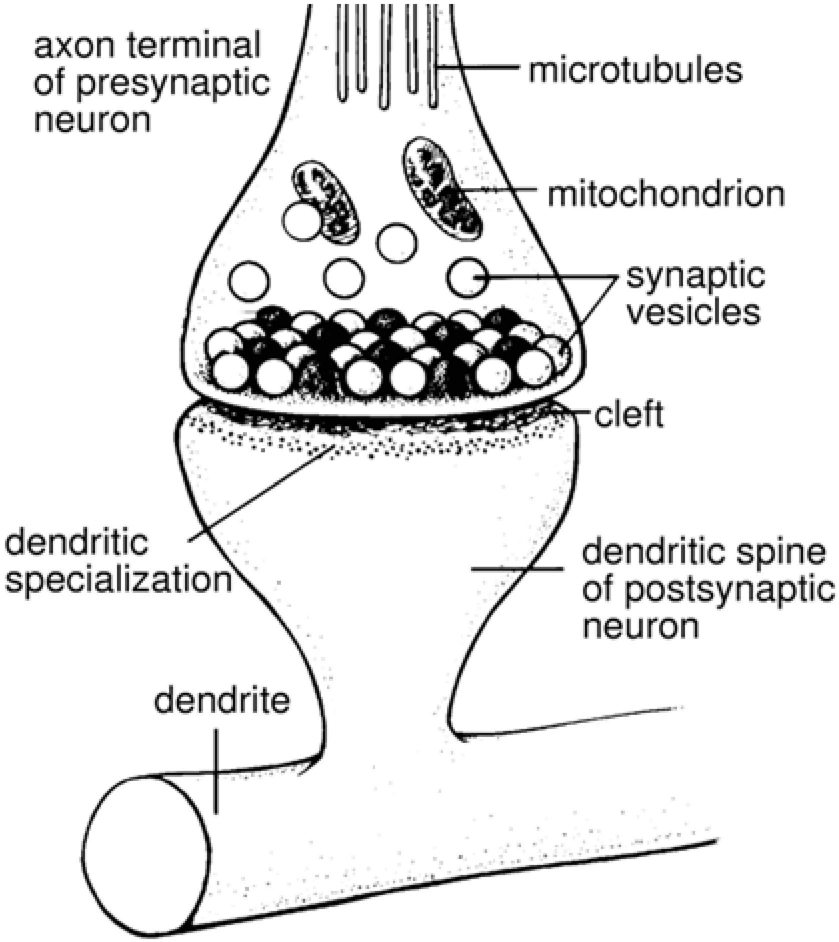


Highlights: Compartmental Models

Neuronal structure can be modeled using electrically coupled compartments



Connecting neurons: Synapses

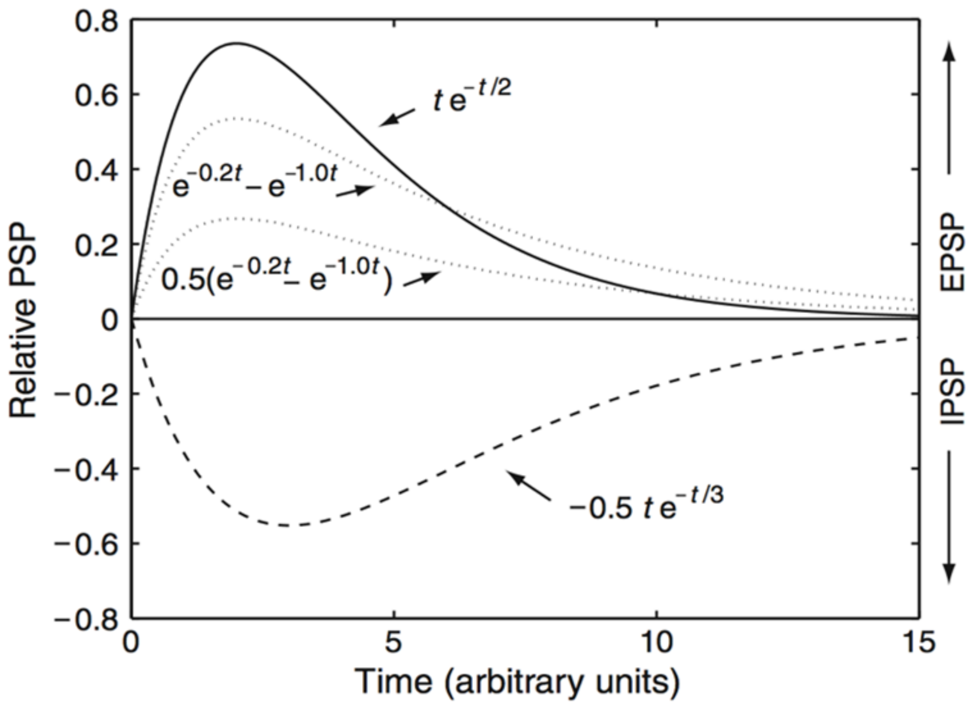


Presynaptic voltage spikes cause neurotransmitter to cross the cleft, triggering postsynaptic receptors allowing ions to flow in, changing postsynaptic potential

Glutamate: excitatory

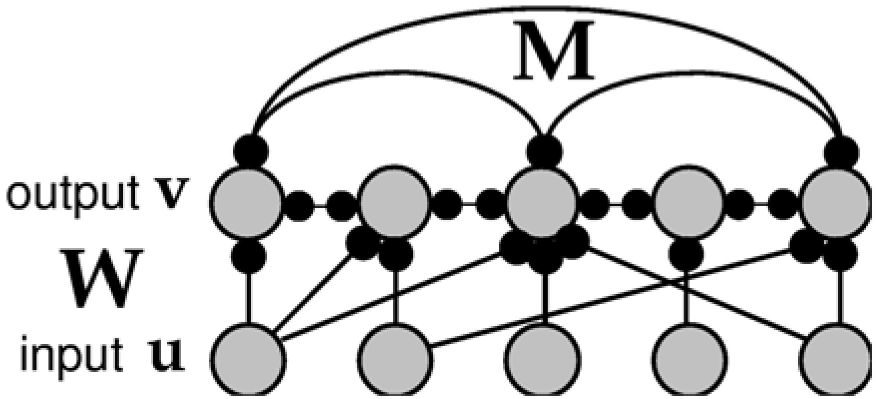
$GABA_A$: inhibitory

Synaptic voltage changes



Size of the PSP is a measure of synaptic strength.
Can vary on the short term due to input history
on the long term due to synaptic plasticity
.. one way to build circuits that learn

Modeling Networks of Neurons

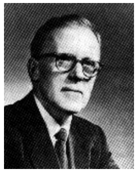


$$\tau \frac{d\mathbf{v}}{dt} = -\mathbf{v} + F(\mathrm{W}\mathbf{u} + \mathrm{M}\mathbf{v})$$

Output Decay Input Feedback

Highlights: Unsupervised Learning

- For linear neuron: $v = \mathbf{w}^T \mathbf{u} = \mathbf{u}^T \mathbf{w}$
- Basic Hebb Rule: $\tau_w \frac{d\mathbf{w}}{dt} = \mathbf{u}v$



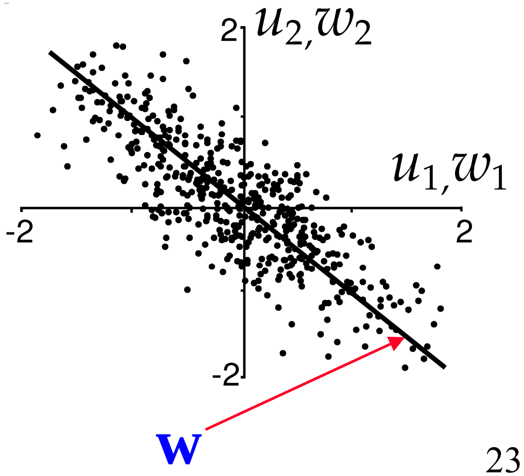
- Average effect over many inputs:

$$\tau_w \frac{d\mathbf{w}}{dt} = \langle \mathbf{u}v \rangle = Q\mathbf{w}$$

- Q is the input correlation matrix:

$$Q = \langle \mathbf{u}\mathbf{u}^T \rangle$$

Hebb rule performs principal component analysis (PCA)



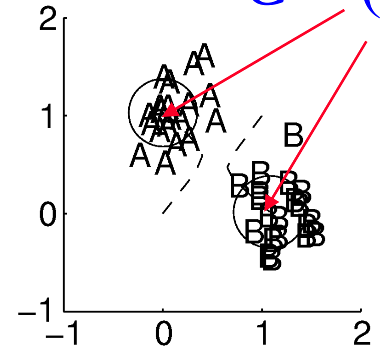
Highlights: The Connection to Statistics

Unsupervised learning = learning the *hidden causes* of input data

Causes $\mathbf{v}$ $\quad p[\mathbf{v}\,|\,\mathbf{u};G]$

(posterior)

$G = (\mu_{v,}\ \sigma_v)$



Causes of clustered data

Generative model

Recognition model

Use EM algorithm for learning

Data $\mathbf{u}$ $\quad p[\mathbf{u}\,|\,\mathbf{v};G]$

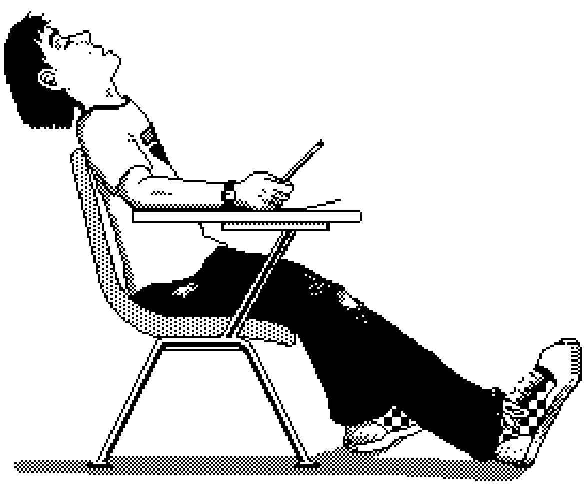
(data likelihood)

Highlights: Generative Models

Droning lecture

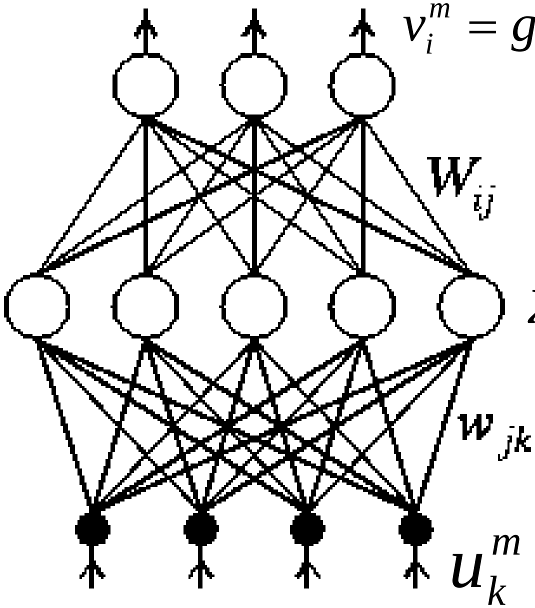
Lack of sleep

Mathematical derivations



Highlights: Supervised Learning

Backpropagation for Multilayered Networks



$$v_i^m = g\Big(\sum_j W_{ij}\, g\Big(\sum_k w_{jk} u_k^m\Big)\Big)$$

Goal: Find **W** and **w** that minimize errors:

$$E(W_{ij}, w_{jk}) = \frac{1}{2}\sum_{m,i}(d_i^m - v_i^m)^2$$

Desired output

Gradient descent learning rules:

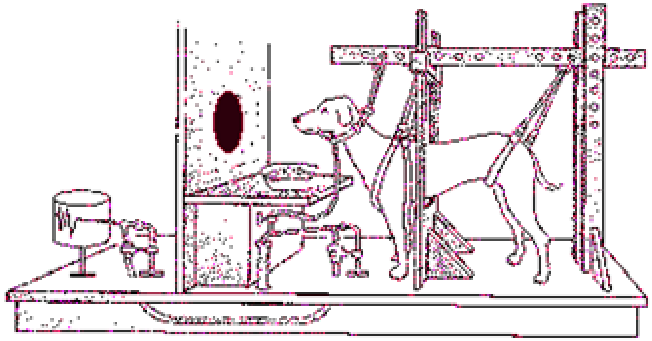
$$W_{ij} \rightarrow W_{ij} - \varepsilon \frac{\partial E}{\partial W_{ij}}$$ (Delta rule)

$$w_{jk} \rightarrow w_{jk} - \varepsilon \frac{\partial E}{\partial w_{jk}} = w_{jk} - \varepsilon \frac{\partial E}{\partial x_j^m} \cdot \frac{\partial x_j^m}{\partial w_{jk}}$$ (Chain rule)

Highlights: Reinforcement Learning

- Learning to predict rewards:

$$w \rightarrow w + \varepsilon(r - v)u$$

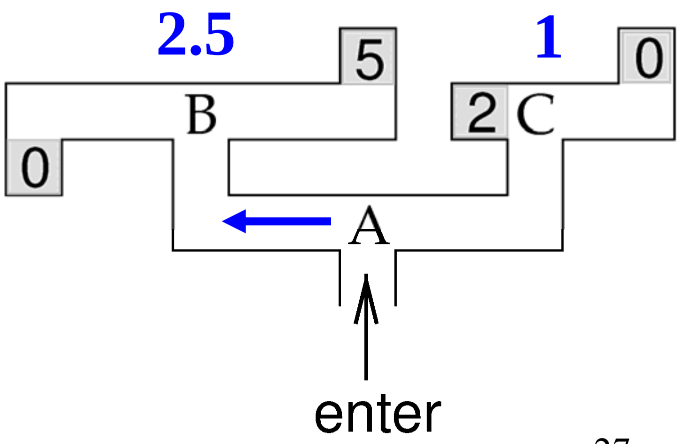


(http://employees.csbsju.edu/tcreed/pb/pdoganim.html)

- Learning to predict **delayed rewards** (TD learning):

$$w(\tau) \rightarrow w(\tau) + \varepsilon\,[r(t) + v(t+1) - v(t)]\,u(t-\tau)$$

- Actor-Critic Learning:
  - Critic learns value of each state using TD learning
  - Actor learns best actions based on value of next state (using the TD error)



The Future: Challenges and Open Problems

- How do neurons encode information?
  - **Topics**: Synchrony, Spike-timing based learning, Dynamic synapses
- Does a neuron's structure confer computational advantages?
  - **Topics**: Role of channel dynamics, dendrites, plasticity in channels and their density
- How do networks implement computational principles such as efficient coding and Bayesian inference?
- How do networks learn "optimal" representations of their environment and engage in purposeful behavior?
  - **Topics**: Unsupervised/reinforcement/imitation learning

Further Reading (for the summer and beyond)

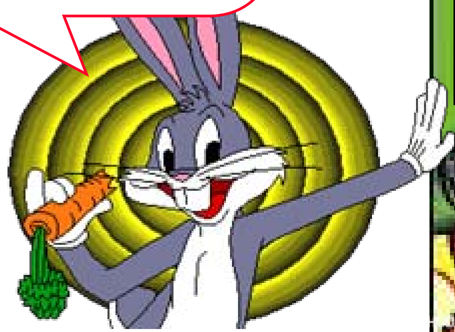
- *Spikes: Exploring the Neural Code,* F. Rieke et al., MIT Press, 1997
- *The Biophysics of Computation,* C. Koch, Oxford University Press, 1999
- *Large-Scale Neuronal Theories of the Brain*, C. Koch and J. L. Davis, MIT Press, 1994
- *Probabilistic Models of the Brain*, R. Rao et al., MIT Press, 2002
- *Bayesian Brain*, K. Doya et al., MIT Press, 2007
- *Reinforcement Learning: An Introduction*, R. Sutton and A. Barto, MIT Press, 1998

Next meeting: Project presentations!

- Project presentations will be on **Monday, June 8 (10:30am-12:20pm) in the same classroom**
- Keep your presentation short: **~6-8 slides, 8 mins/group**
- Slides:
  - Email Raj your powerpoint (or other) slides **before 8am on Monday, June 8** to use the class laptop

  OR
  - Bring your own laptop if you want to show videos etc.
- Projects reports (10-15 pages) due **June 10** (by email to both Raj and Adrienne before midnight)

Have a great summer!



Au revoir!