#### CSE 521: Review

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# Complexity, I

Asymptotic Analysis Best/average/**worst** cases Upper/Lower Bounds Big O, Theta, Omega Analysis methods loops recurrence relations common data structures, subroutines

## Graph Algorithms

Graphs

- Breadth/depth first search
- Connected components
- Shortest paths/bipartitness/2-Colorability
- DAGS and topological ordering
- DFS/articulation points/biconnected components
- Strongly connected components

### **Design Paradigms**

#### Greedy

emphasis on correctness arguments, e.g. <u>exchange</u> Divide & Conquer

recursive solution, superlinear work, balanced subproblems, recurrence relations, solutions, Master Thm

#### **Dynamic Programming**

recursive solution, redundant subproblems, few

do all in careful order and tabulate; <u>OPT function</u> (usually far superior to "memoization")

#### **Powerful Subproblems**

Flow, Matching, Linear Programming

### Examples

Greedy

- Interval Scheduling Problems (3)
- Huffman Codes

Examples where greedy fails (stamps/change, scheduling, knap, RNA,...)

## Examples

Divide & Conquer

Merge sort

Closest pair of points

Integer multiplication (Karatsuba)

Matrix multiplication (Strassen)

Powering

FFT

#### Examples

Dynamic programming Fibonacci Making change/Stamps, Knapsack Weighted Interval Scheduling RNA String Alignment (code generation)



#### Examples & Concepts

Flow and matching

Residual graph, augmenting paths, max-flow/min-cut, Ford-Fulkerson and Edmonds-Karp algorithms, (preflowpush), integrality, reductions to flow, e.g. bipartite matching

## Complexity, II

#### P vs NP

Big-O and poly vs exponential growth

Definition of NP - hints/certificates and verifiers

Example problems from slides, reading & hw

SAT, 3-SAT, circuit SAT, vertex cover, clique, independent set, TSP, Hamilton cycle, coloring, max cut, knapsack

 $P \subseteq NP \subseteq Exp$  (and worse)

Definition(s) of (polynomial time) reduction

SAT  $\leq_p$  IndpSet, Knap examples (how, why correct, why  $\leq_p$ , implications)

Definition of NP-completeness

NP-completeness proofs

Asymmetry; SAT vs UNSAT, (polynomial hierarchy, PSPACE)

2x, I.5x approximations to Euclidean TSP

And see how relevant it is to your daily life! Classic Nintendo Games are (NP-)Hard

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March 9, 2012

Abstract

We prove NP-hardness results for five of Nintendo's largest video game franchises: Mario, Donkey Kong, Legend of Zelda, Metroid, and Pokémon. Our results apply to Super Mario Bros. 1, 3, Lost Levels, and Super Mario World; Donkey Kong Country 1– 3; all Legend of Zelda games except Zelda II: The Adventure of Link; all Metroid games; and all Pokémon role-playing games. For Mario and Donkey Kong, we show NP-completeness. In addition, we observe that several games in the Zelda series are **PSPACE-complete**.

#### **Final Exam Mechanics**

Closed book, 1 pg notes (8.5x11, 2 sides, handwritten)

(no bluebook needed; scratch paper may be handy; calculators unnecessary)

Comprehensive: All topics covered

assigned reading

slides

homework & solutions

## Some Typical Exam Questions

- Give O() bound on  $17n^*(n-3+\log n)$ , or on code {for i=1 ...}
- True/False: If X is  $O(n^2)$ , then it's rarely more than  $n^3 + 14$  steps.
- Explain why a given greedy alg is/isn't correct
- Give a run time recurrence for a recursive alg, or solve a simple one
- Simulate any of the algs we've studied
- Give an alg for problem X, maybe a variant of one we've studied, or prove it's in NP
- Understand parts of correctness proof for an algorithm or reduction Implications of NP-completeness
- Reductions
- NP-completeness proofs

