

Trees & Graphs

Nathalie Henry Riche, Microsoft Research



About

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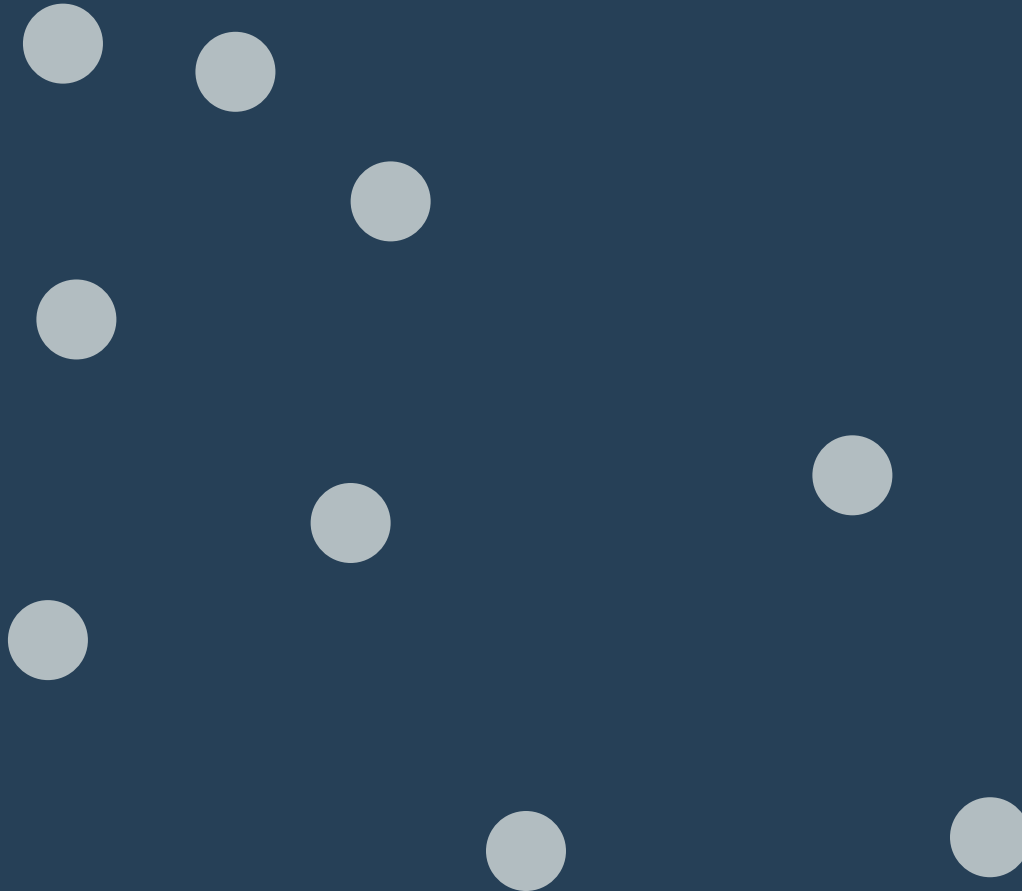
Today:

- Overview of techniques to visualize trees & graphs
- Their strengths & weaknesses
- Areas for future research

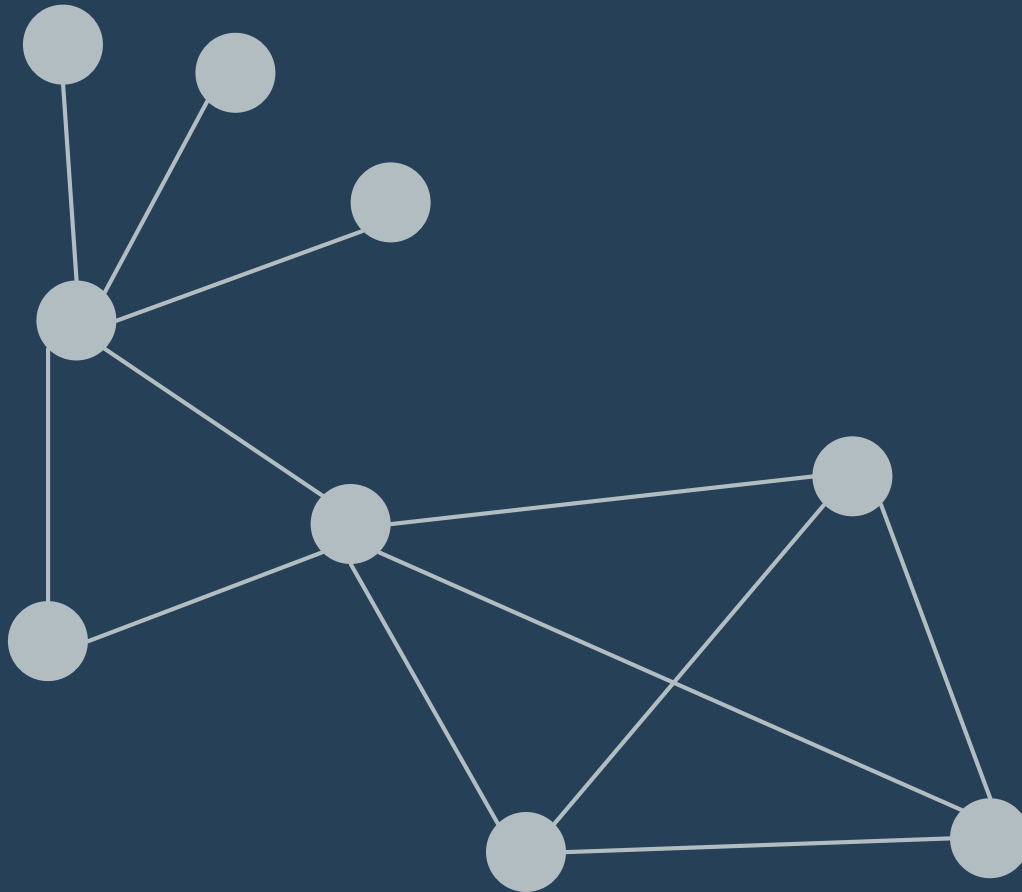
What's in a graph?



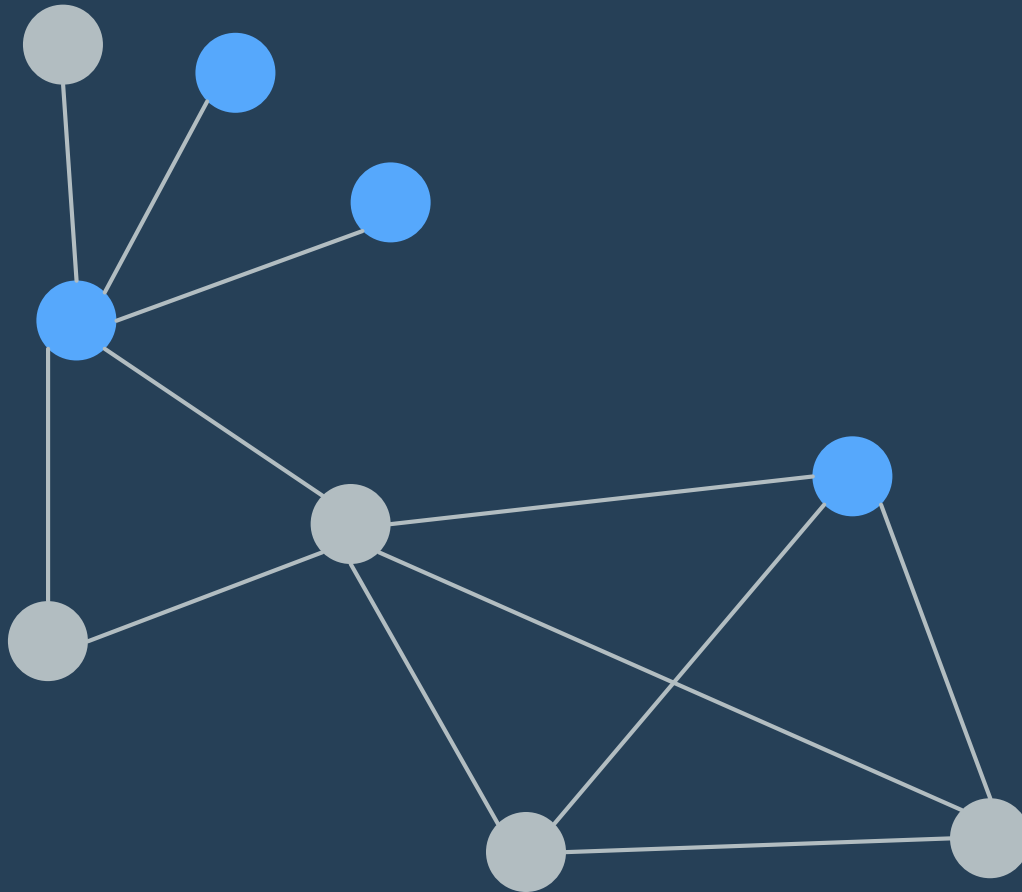
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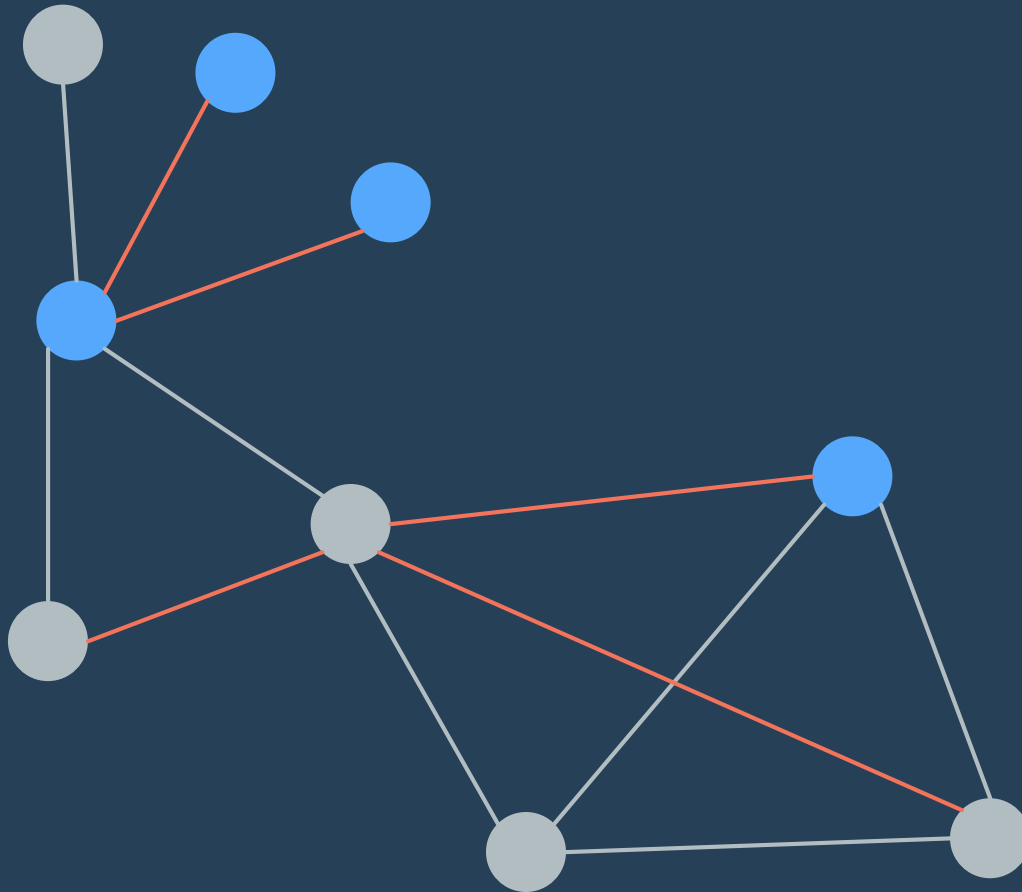
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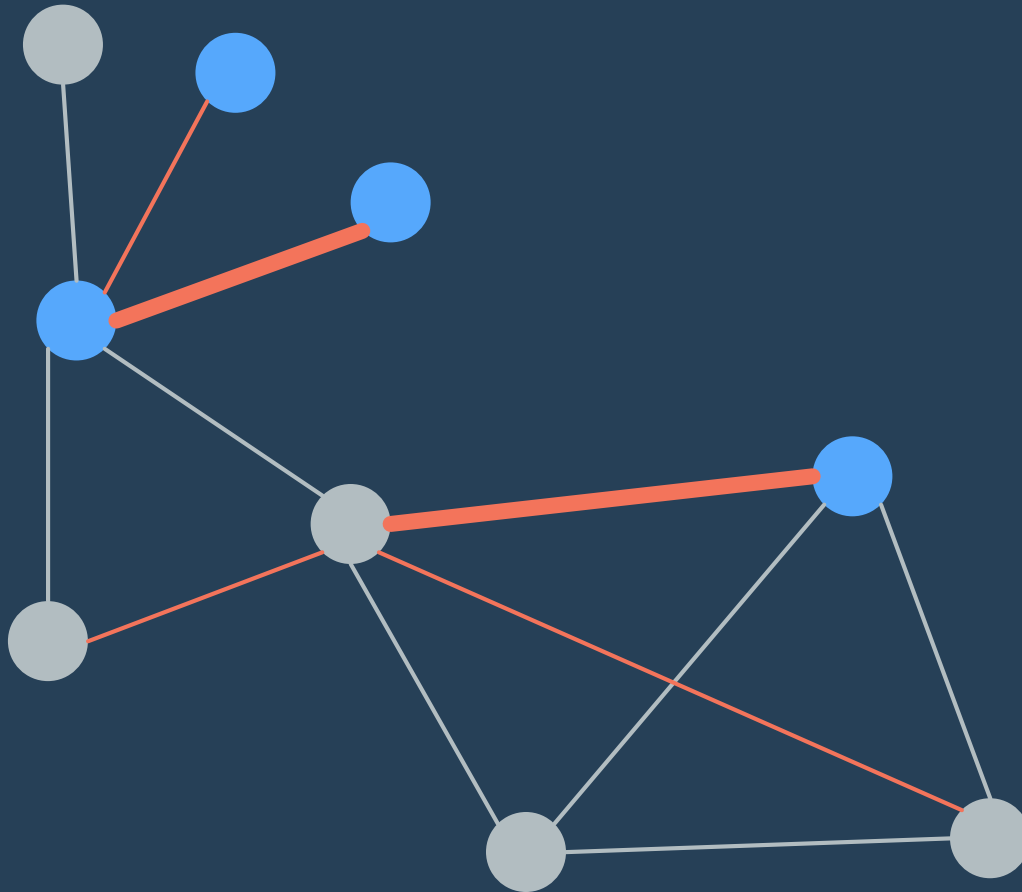
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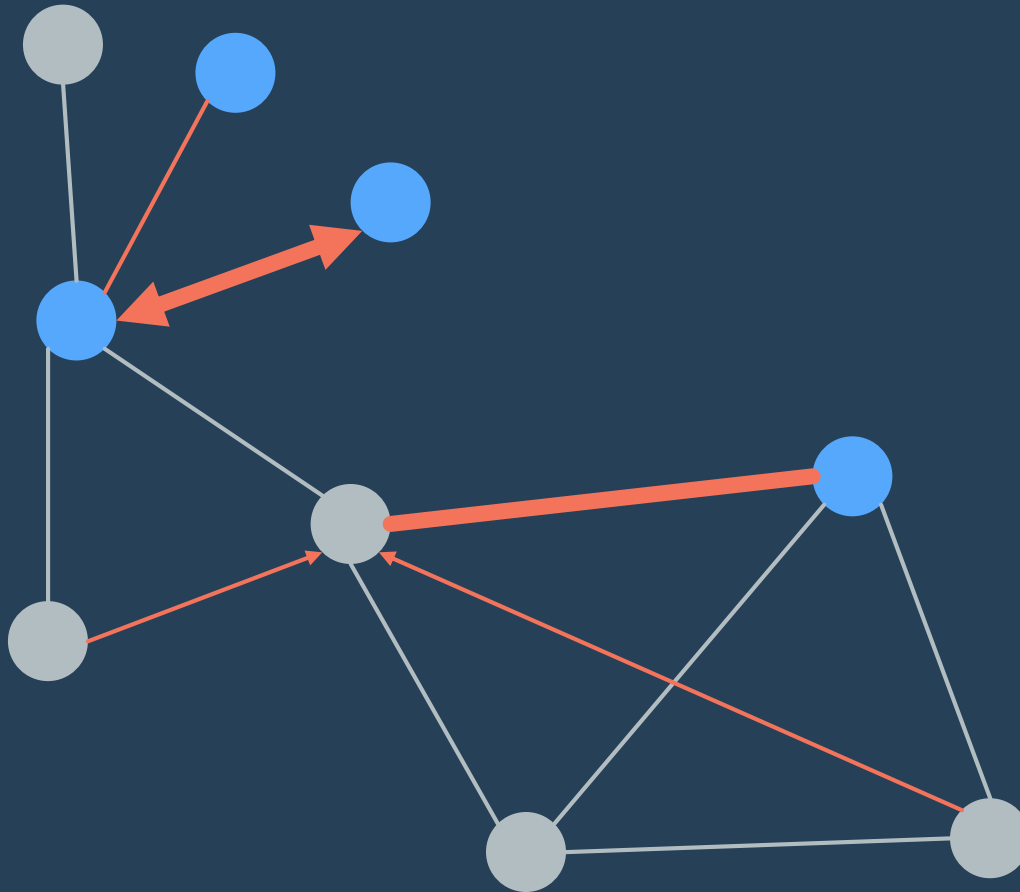
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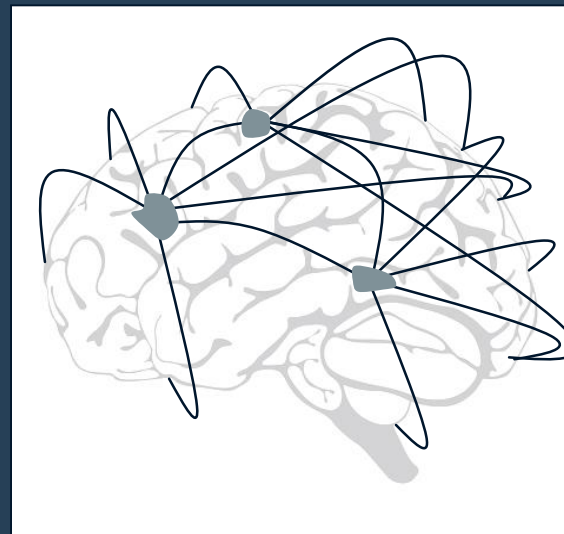
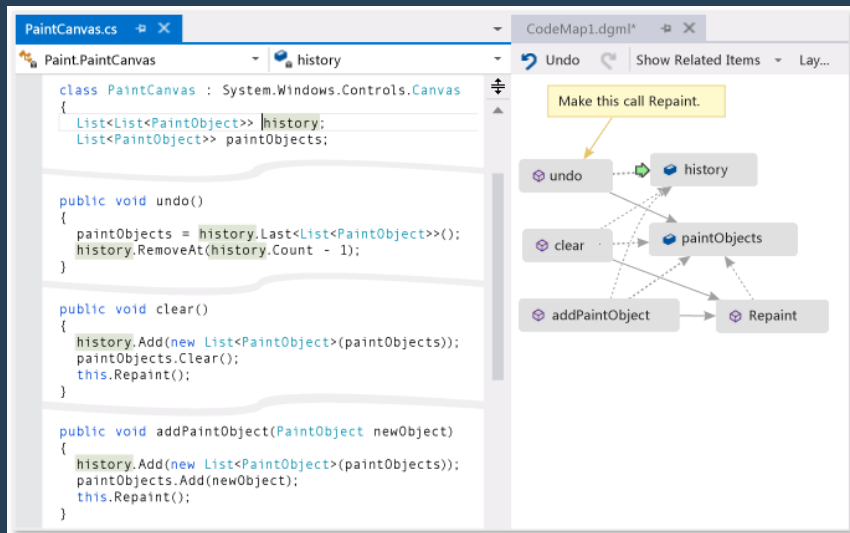
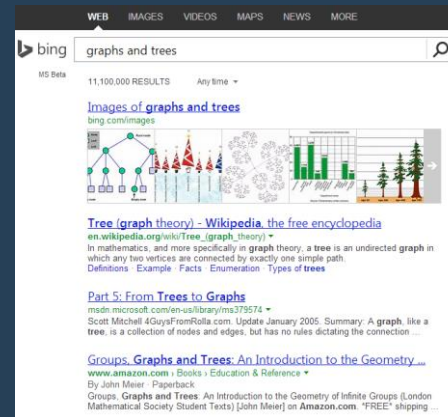
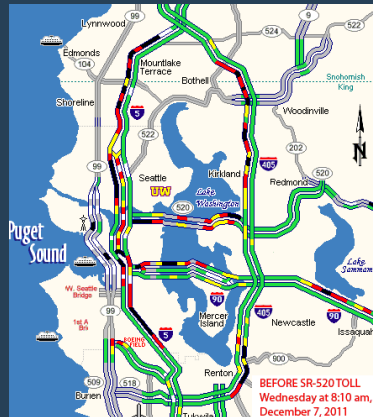
What's in a graph?



A vertical banner with a dark blue background. It features several stylized snowflake patterns. There are five prominent white snowflakes and several faint, light blue ones. The snowflakes are of various sizes and orientations, scattered across the banner. The overall aesthetic is clean and modern, suitable for a winter-themed event.



Everything can be a graph!



What questions might we ask?

- How does the brain organize itself to achieve a function?
- How does knowledge disseminate in online communities?
- How are two graphs similar?
- Which entities in a social network might be terrorists?

Graph Drawing

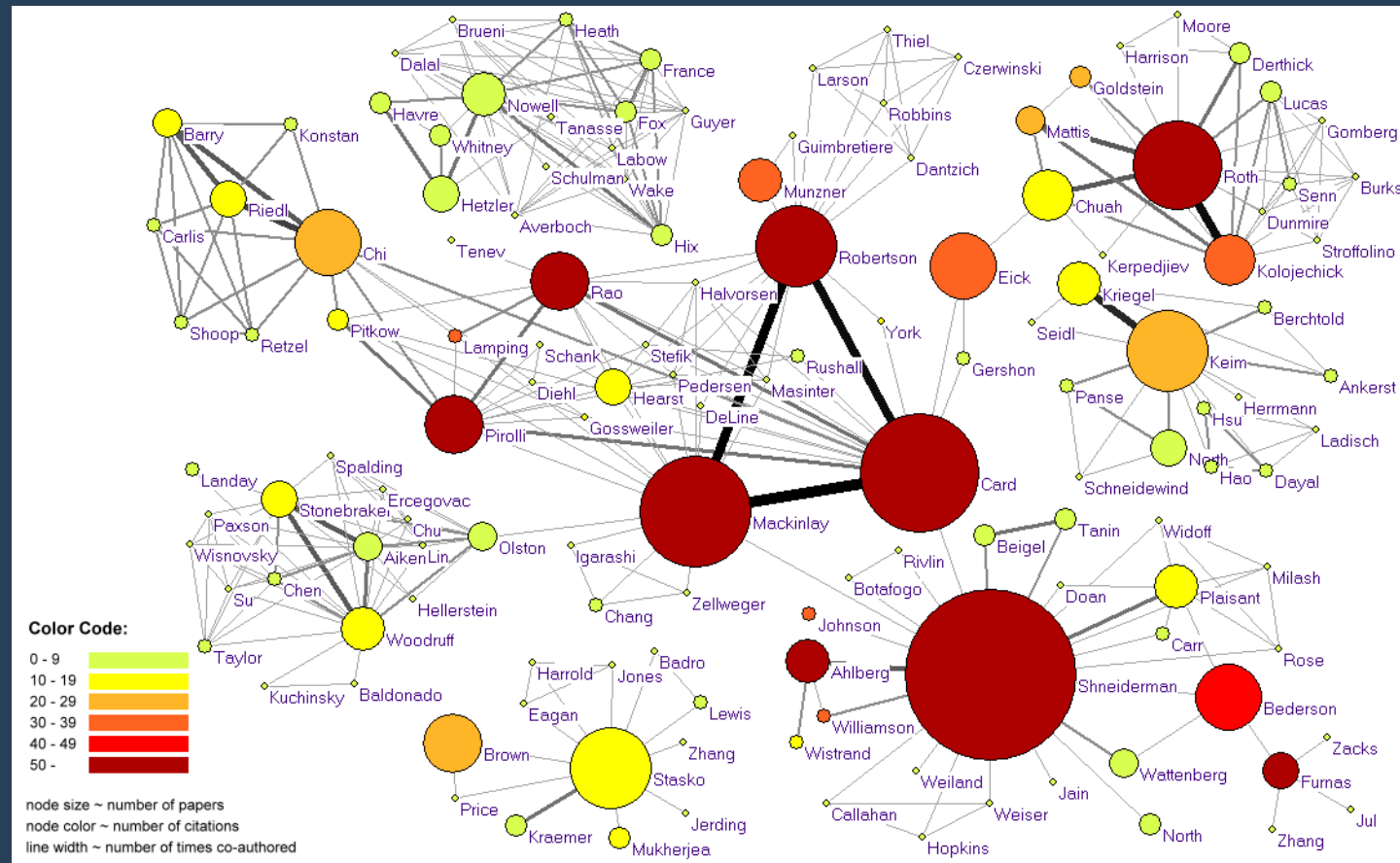
The primary concern of graph drawing is the spatial arrangement of nodes and links

Often (but not always) the goal is to effectively depict the graph structure:

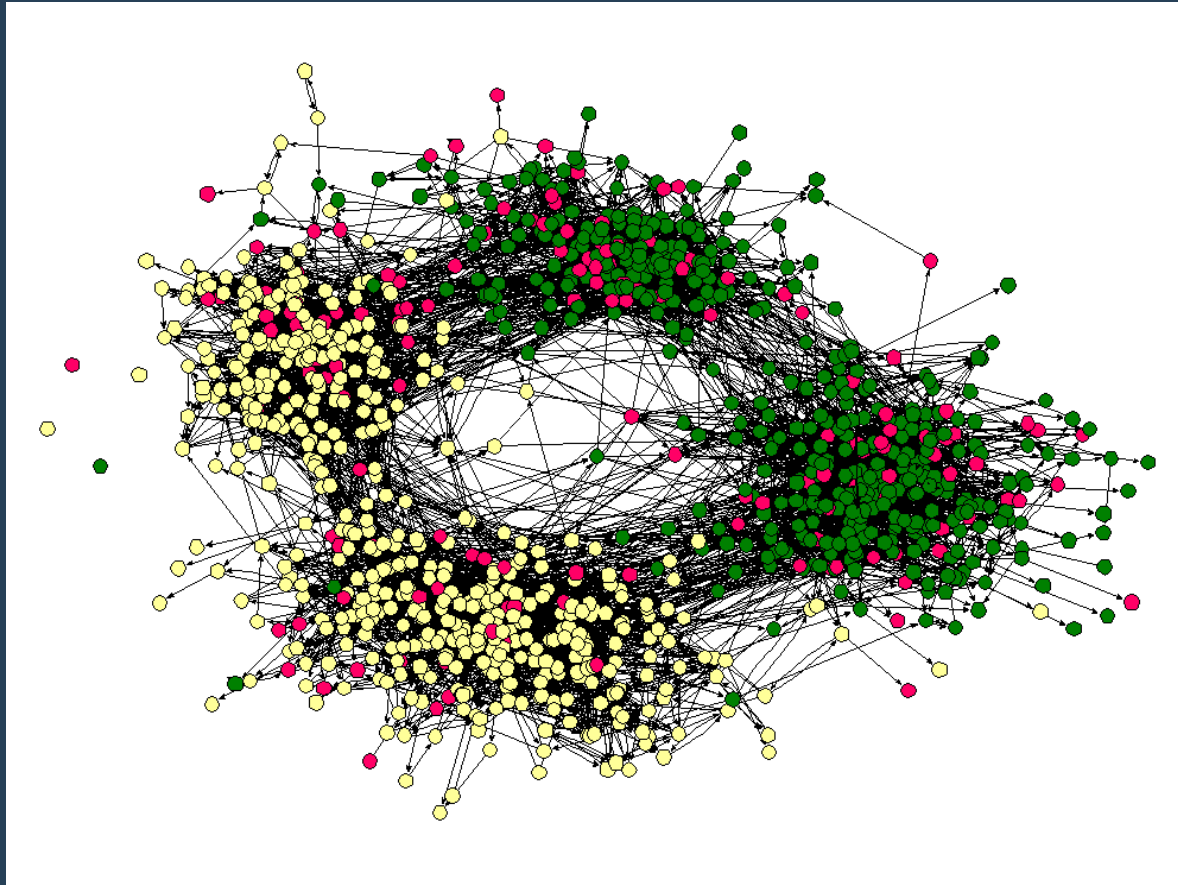
- Connectivity patterns
- Partitions / Clusters
- Outliers



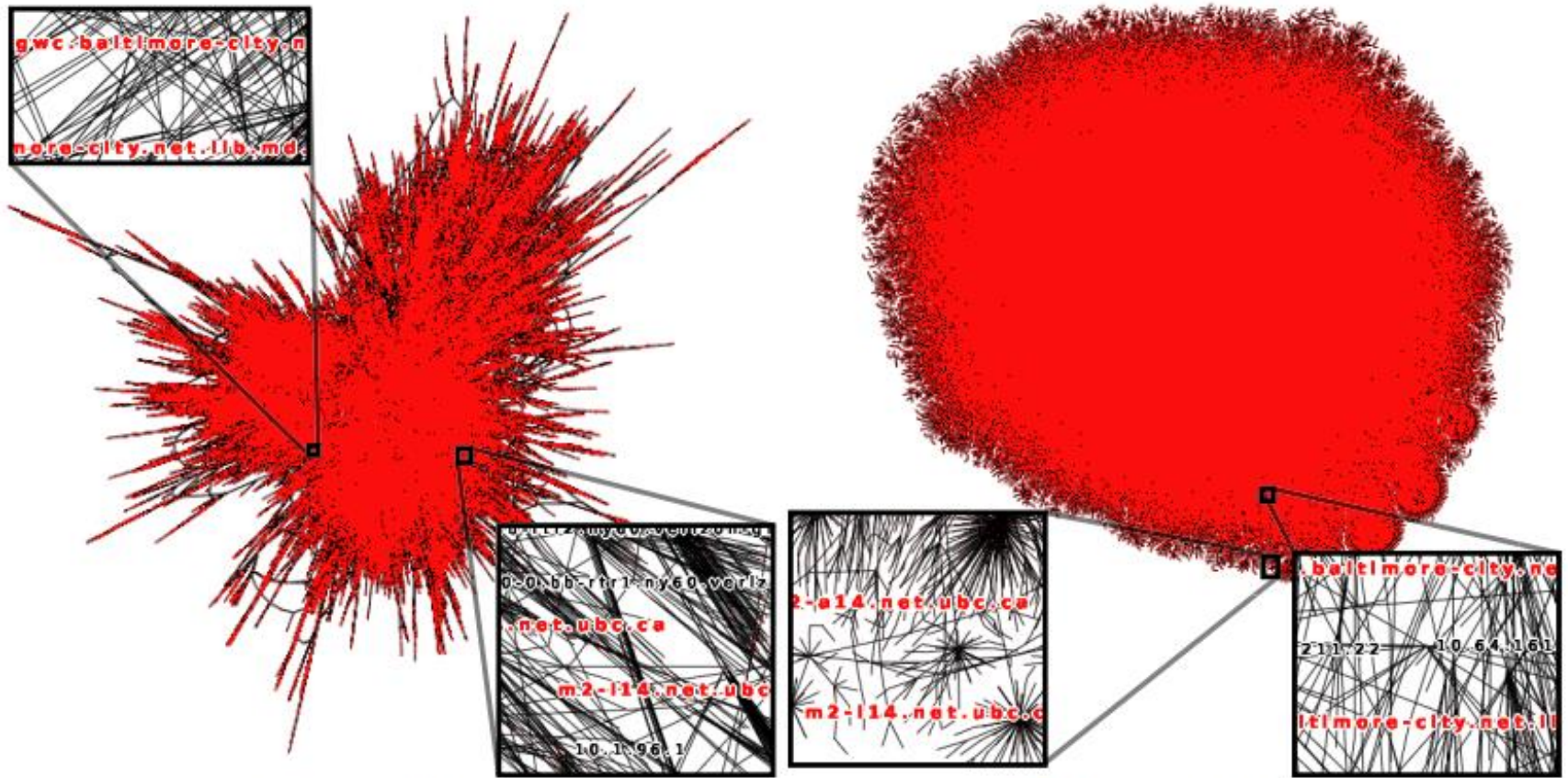
Putting things into perspective



Putting things into perspective



Putting things into perspective



(a) FM³: 11 Minutes

(b) LGL: 12 Hours

Outline

Tree visualization

Graph visualization

- node-link diagrams
- matrices

Recent research topics



Trees



4 Major tree visualizations

Indented lists



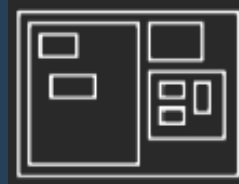
Node-link trees



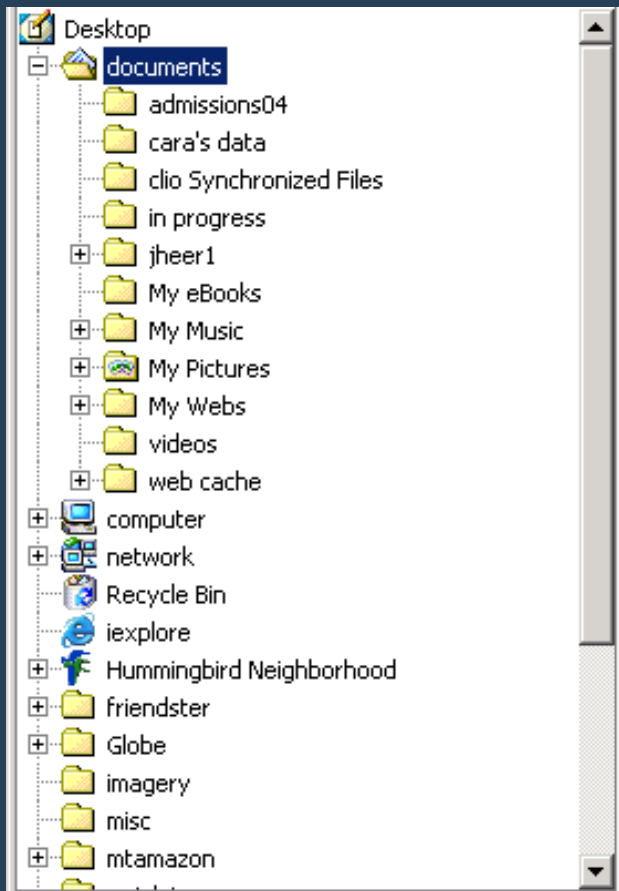
Layered diagrams



Treemaps



Indented List



Places all items along vertically spaced rows

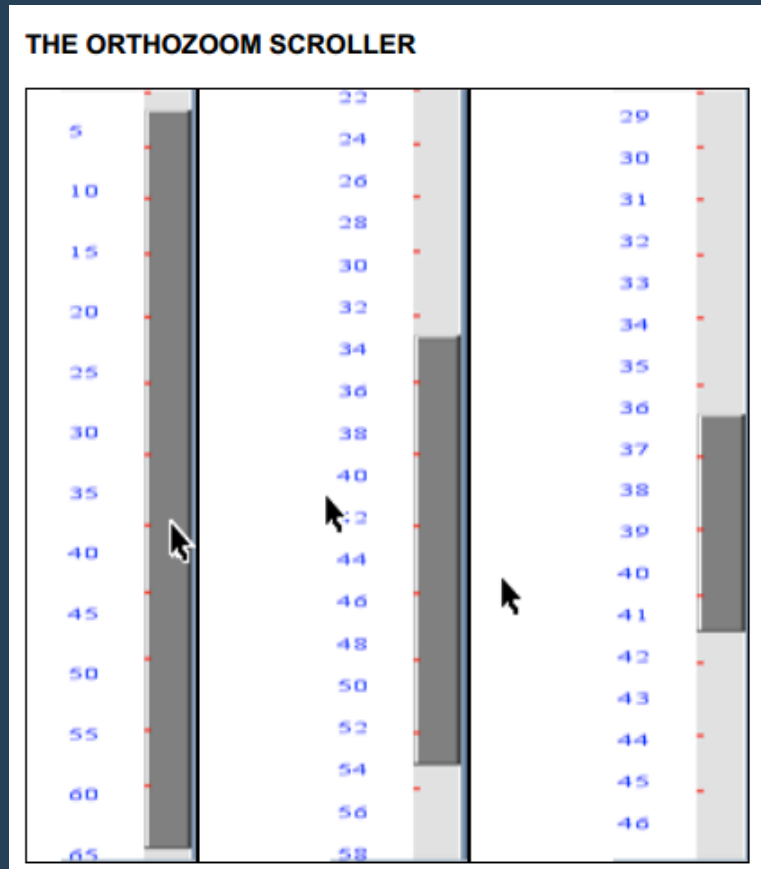
Indentation used to show parent/child relationships

Commonly used as a component in an interface

Breadth and depth contend for space

Often requires a great deal of scrolling

Interaction can help



OrthoZoom, *Appert et al.*, CHI 2006

<http://www.lri.fr/~appert/website/orthozoom/orthozoom.html>

king, nor the queen: and therefore, Peter, have at thee with a downright blow!

YORK

Dispatch: this knave's tongue begins to double.

Sound, trumpets, alarum to the combatants!

Alarum. They fight, and PETER strikes him down

HORNER

Hold, Peter, hold! I confess, I confess treason.

Dies

YORK

Take away his weapon. Fellow, thank God, and the good wine in thy master's way.

PETER

O God, have I overcome mine enemy in this presence?

O Peter, thou hast prevailed in right!

KING HENRY VI

Go, take hence that traitor from our sight;

For his death we do perceive his guilt:

And God in justice hath revealed to us

The truth and innocence of this poor fellow,

Which he had thought to have murder'd wrongfully.

Come, fellow, follow us for thy reward.

Sound a flourish. Exeunt

SCENE IV. A street.

Enter GLOUCESTER and his Servingmen, inmourning cloaks

GLOUCESTER

Thus sometimes hath the brightest day a cloud;

And after summer evermore succeeds

Barren winter, with his wrathful nipping cold:

So cares and joys abound, as seasons fleet.

Sirs, what's o'clock?

Servants

Ten, my lord.

GLOUCESTER

Ten is the hour that was appointed me

To watch the coming of my punish'd duchess:

Uneath may she endure the flinty streets,

To tread them with her tender-feeling feet.

Sweet Nell, ill can thy noble mind abrook

The abject people gazing on thy face,

With envious looks, laughing at thy shame,

That erst did follow thy proud chariot-wheels

When thou didst ride in triumph through the streets.

But, soft! I think she comes; and I'll prepare

My tear-stain'd eyes to see her miseries.

Enter the DUCHESS in a white sheet, and a taperburning in her hand; with

STANLEY, the Sheriff, and Officers

Servant

So please your grace, we'll take her from the sheriff.

GLOUCESTER

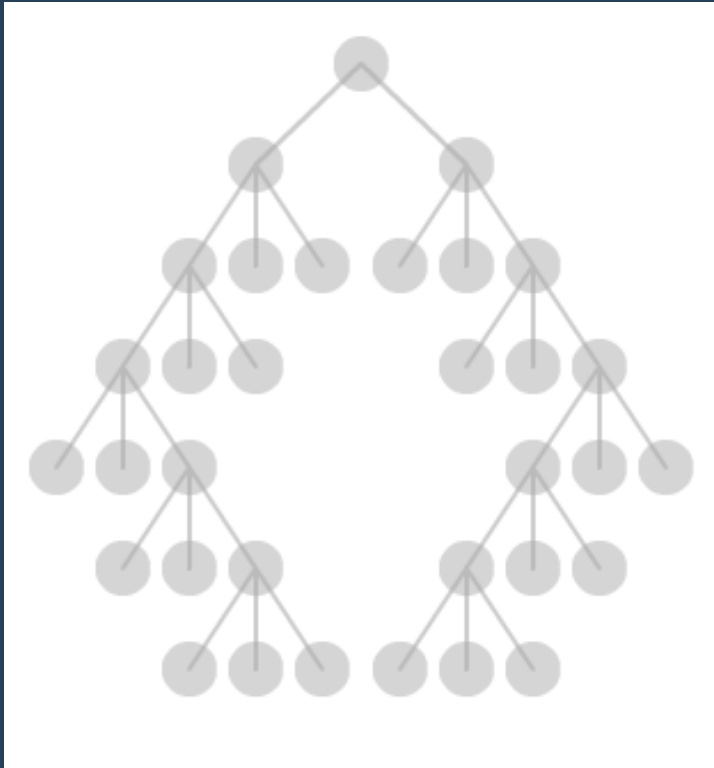
No, stir not, for your lives; let her pass by.

1108

Zoom: 1.0



Node-Link Trees

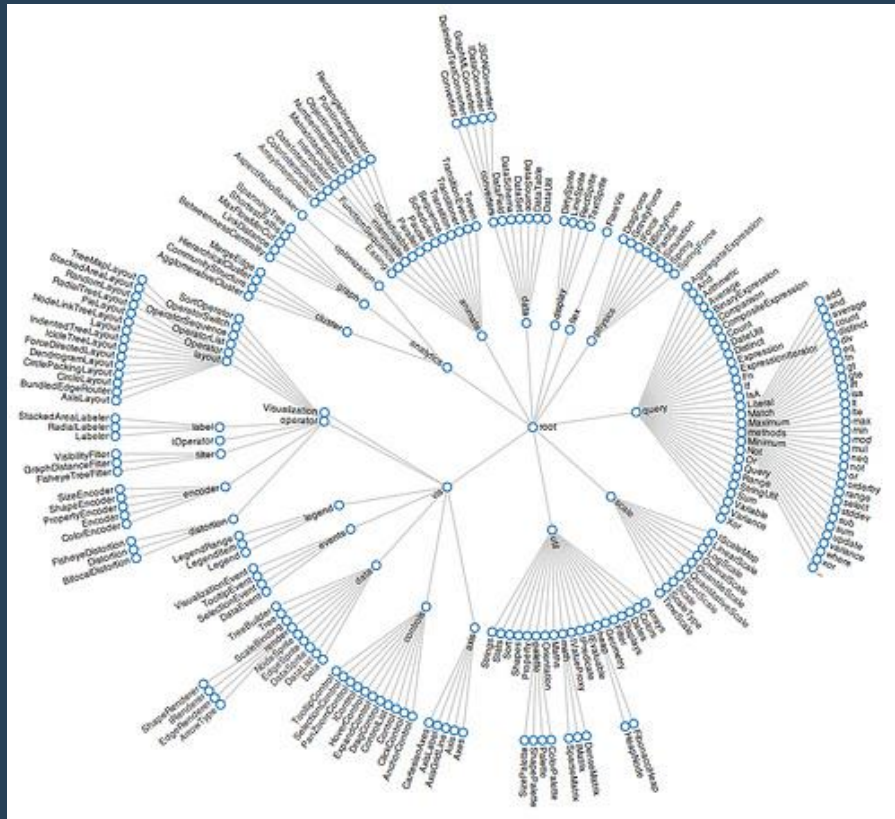


Nodes are distributed in space, connected by straight or curved lines.

Typical approach is to use 2D space to break apart breadth and depth.

Reingold-Tilford algorithm achieves linear time

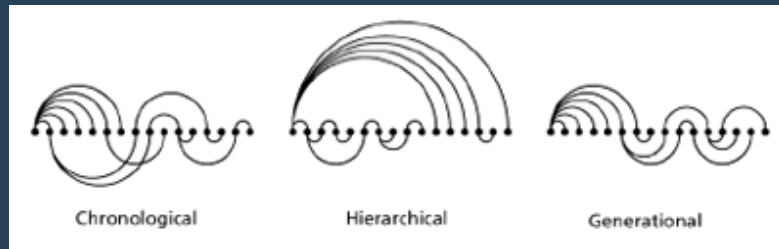
Node-Link Trees



Radial layout places the root in the center.

The radius encodes the depth.

Other node-Link trees



ThreadArcs,
Kerr,
2003



PhylloTrees,
Neumann et al.,
Eurovis 2006

Layered diagrams

Signify tree structure using

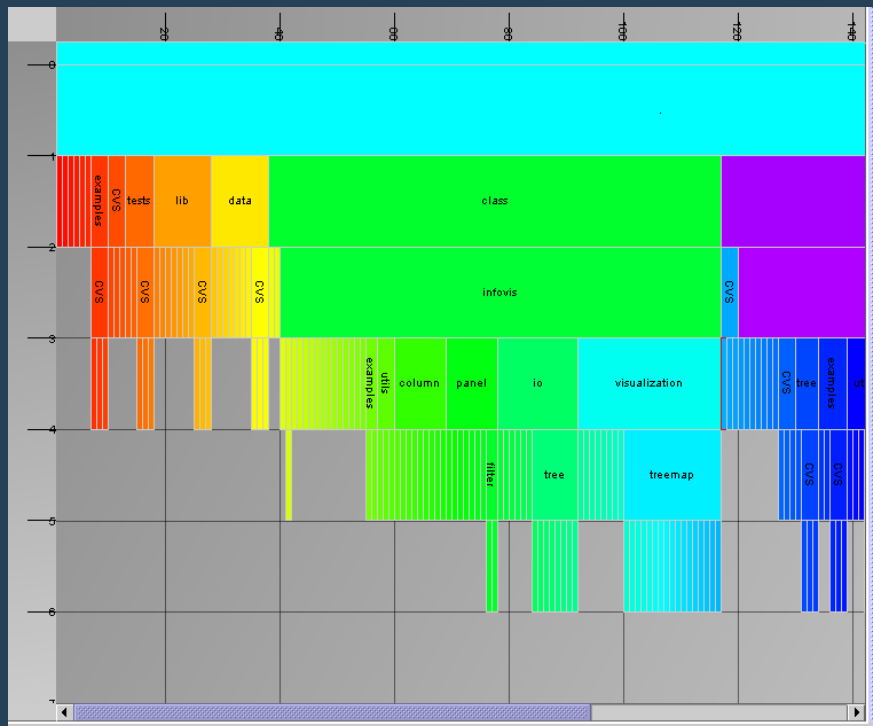
- Layering
- Adjacency
- Alignment

Involves recursive sub-division of space

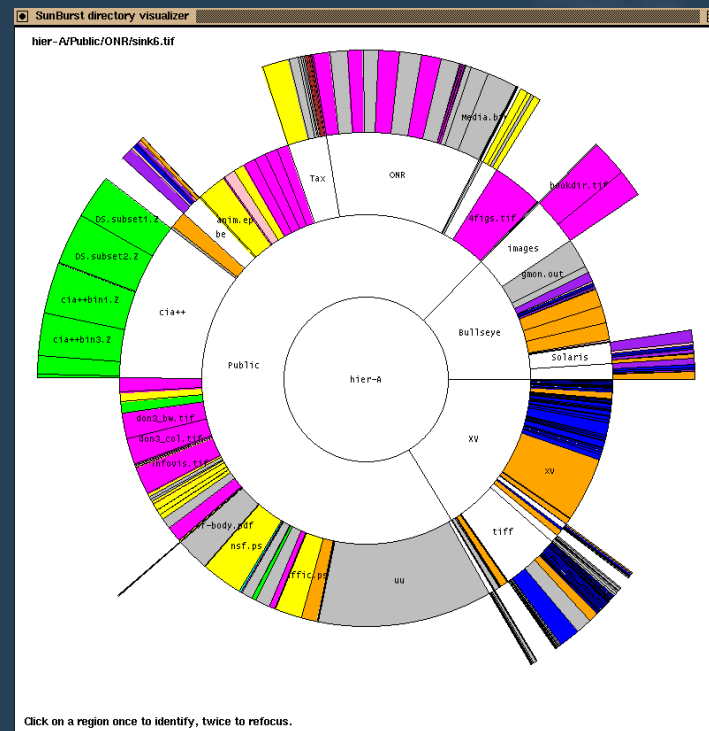
We can apply the same set of approaches as in node-link layout.



Layered diagrams



Icicle Trees

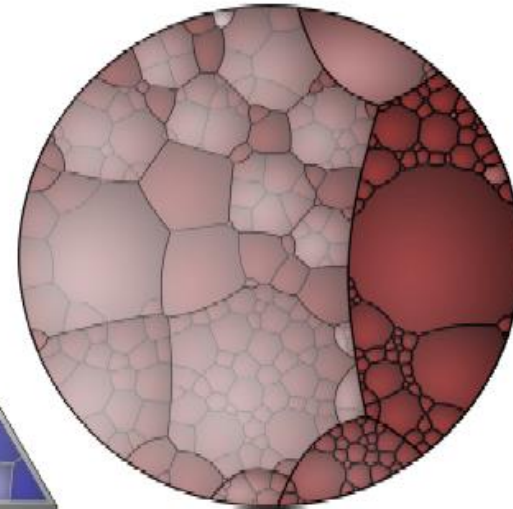
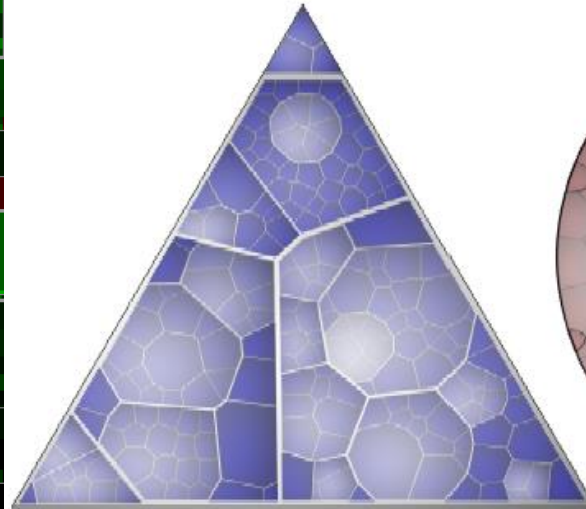
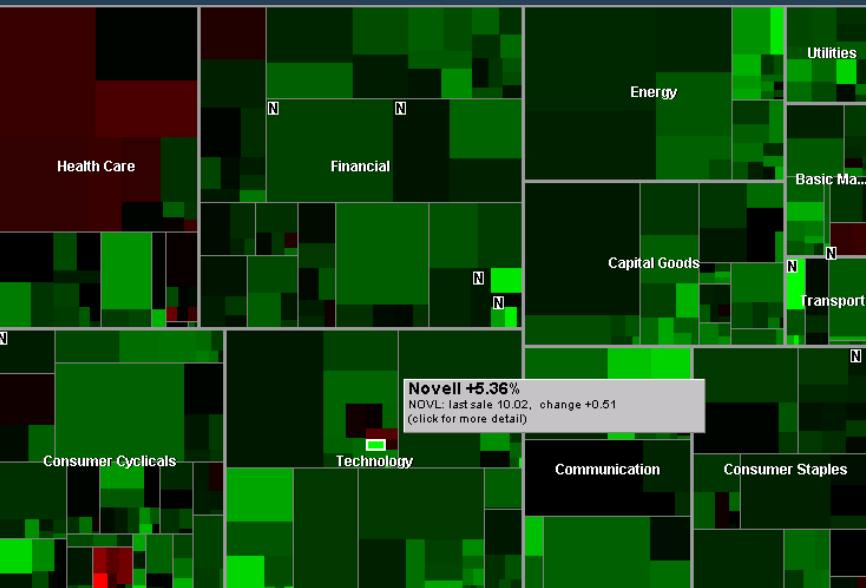


SunBurst, *Stasko et al.*,
Infovis 2000

Treemaps

Encode hierarchy using spatial enclosure

Space-filling technique



Treemaps

Benefits

Provides a single view of an entire tree

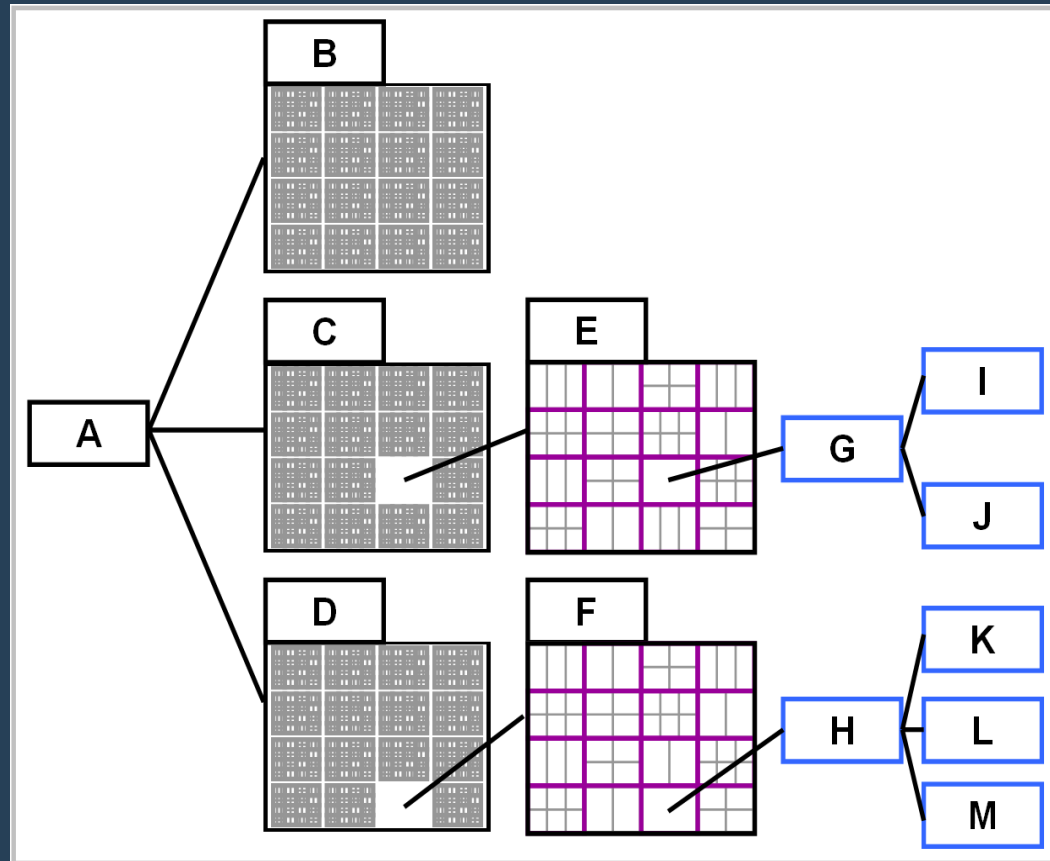
Easier to spot large/small nodes

Problems

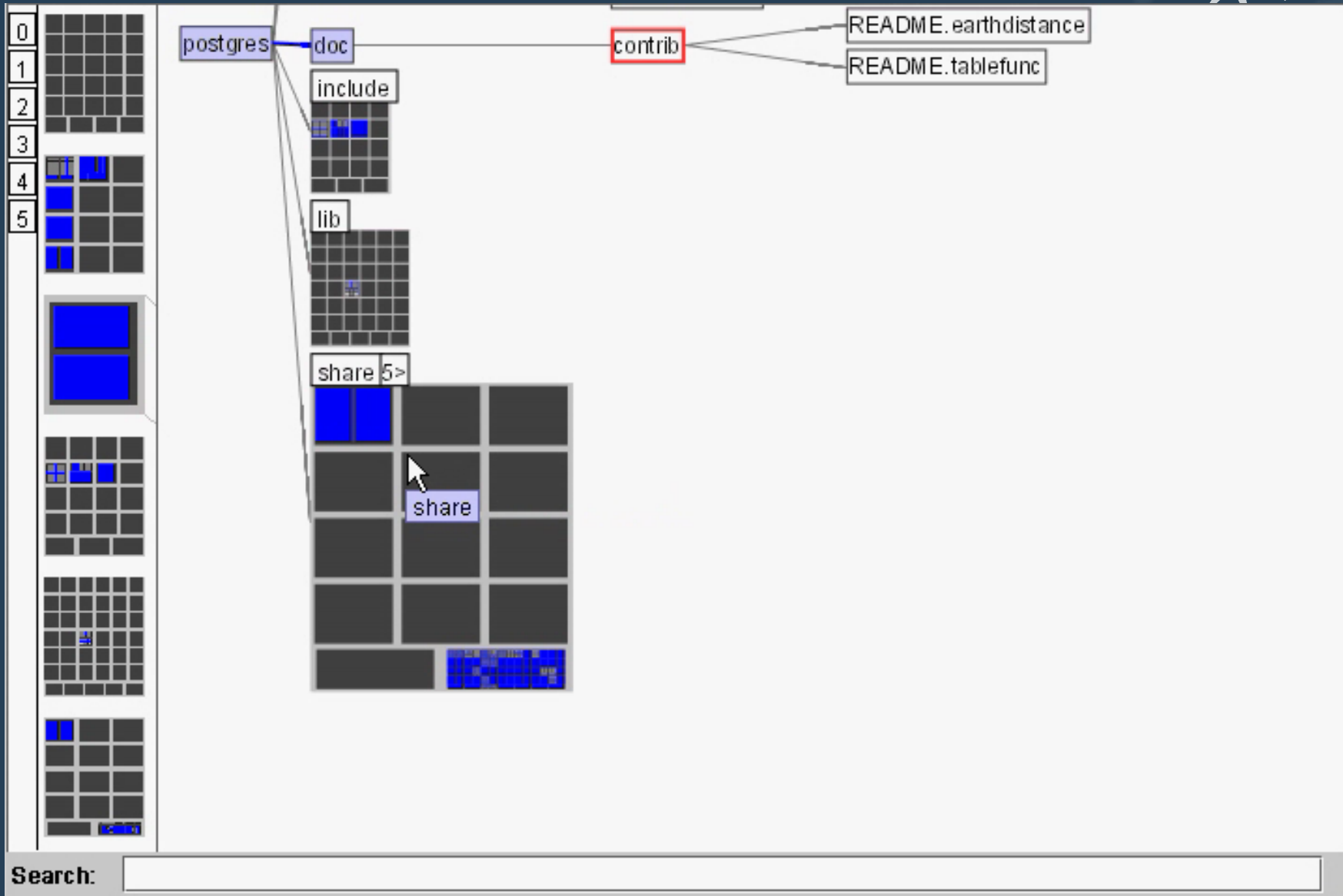
Difficult to accurately read depth



Hybrids



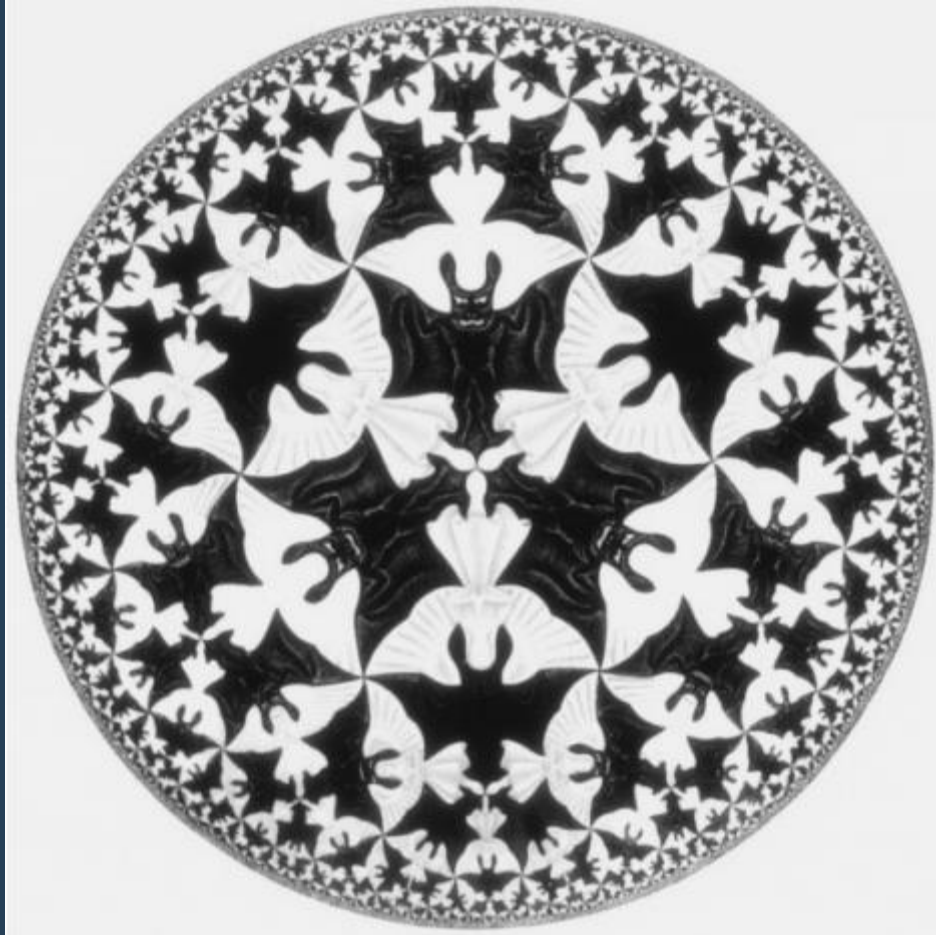
Elastic Hierarchies, *Zhao et al.*, Infovis 2005

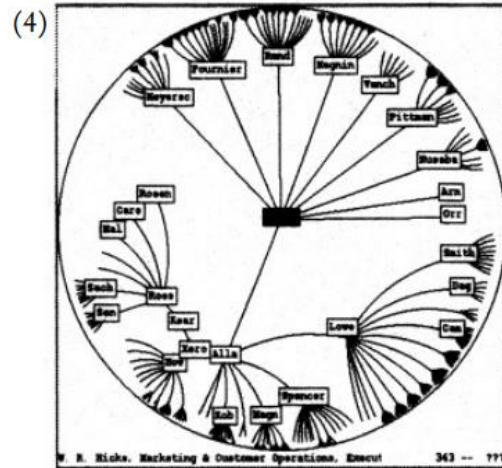
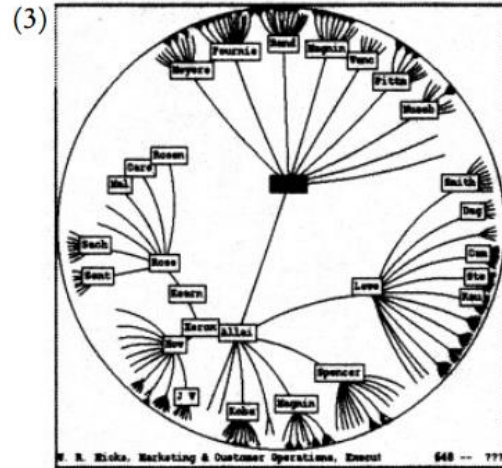


The issue of scale

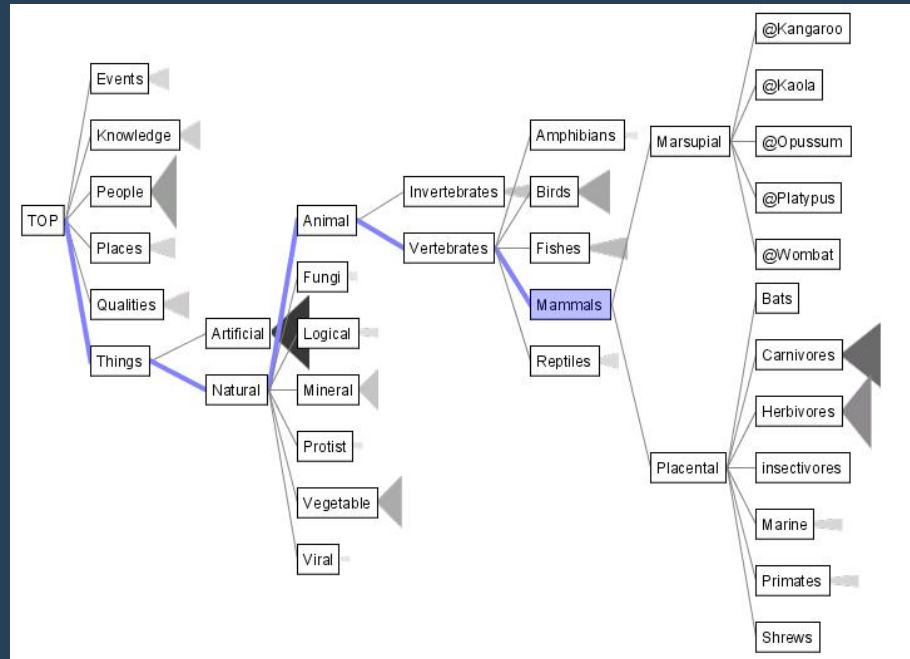


Hyperbolic Space

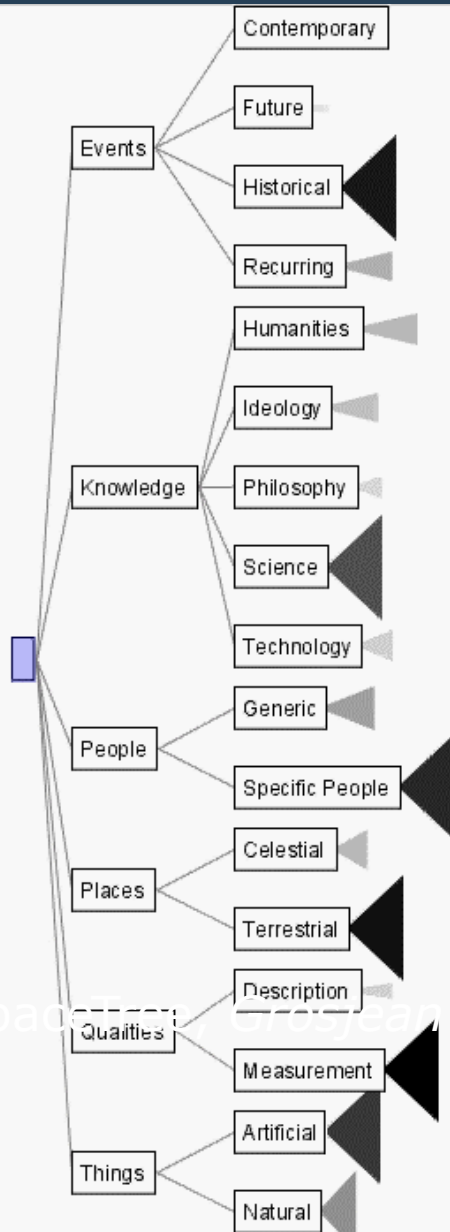




Aggregation



SpaceTree, *Grosjean et al.*, Infovis 2002

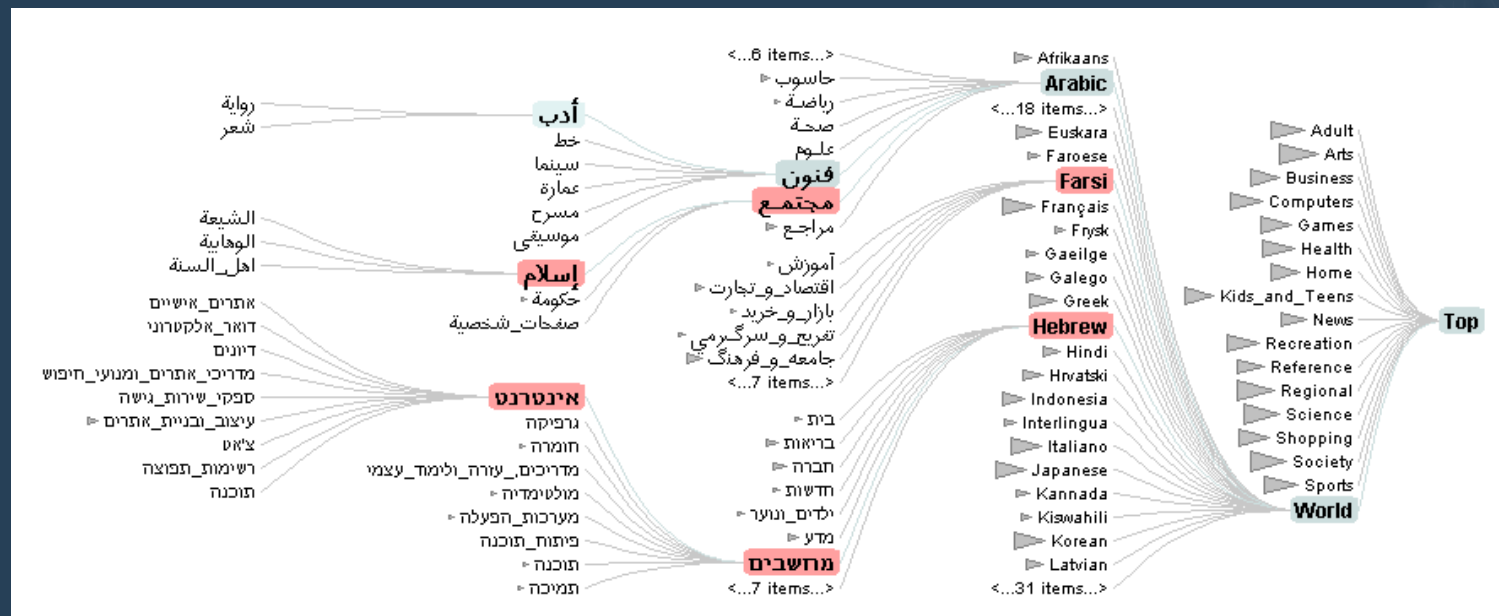


Spaak, Grosjean et al., Infovis 2002

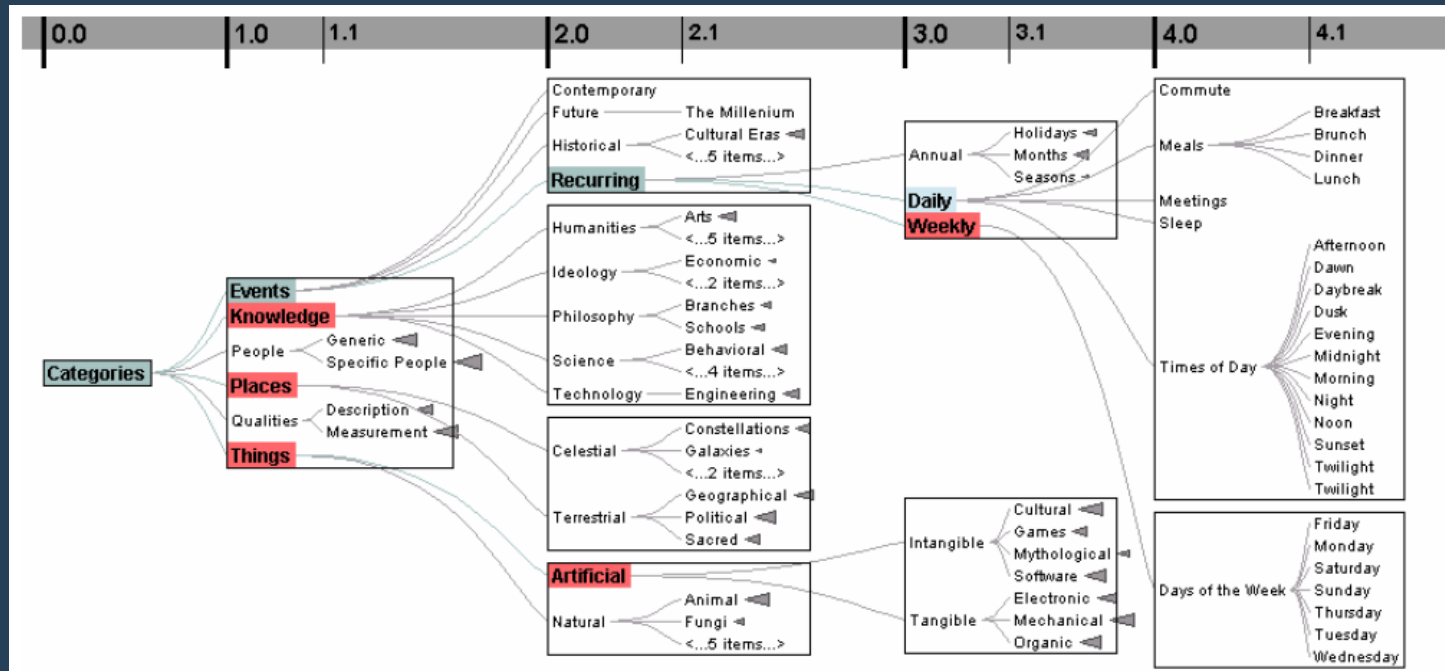
Degree-of-interest trees



Degree-of-interest trees



Degree-of-interest trees



Cull “un-interesting” nodes on a per block basis until all blocks on a level fit within bounds.

Attempt to center child blocks beneath parents.

Graphs



Graph Visualization

Two representations:

- Node-link diagrams
- Matrices

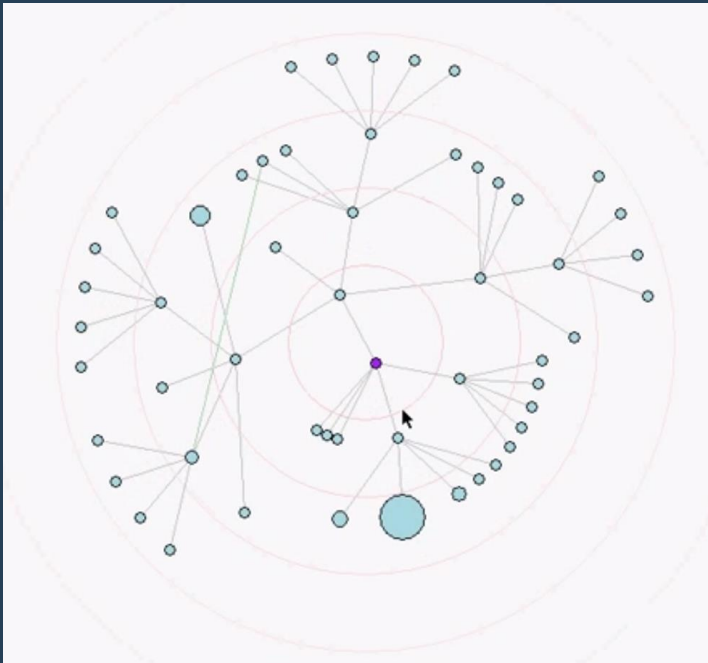
Major Node-Link Layouts

Scalability issues and solutions

Matrix-based representations



See the tree in this graph?

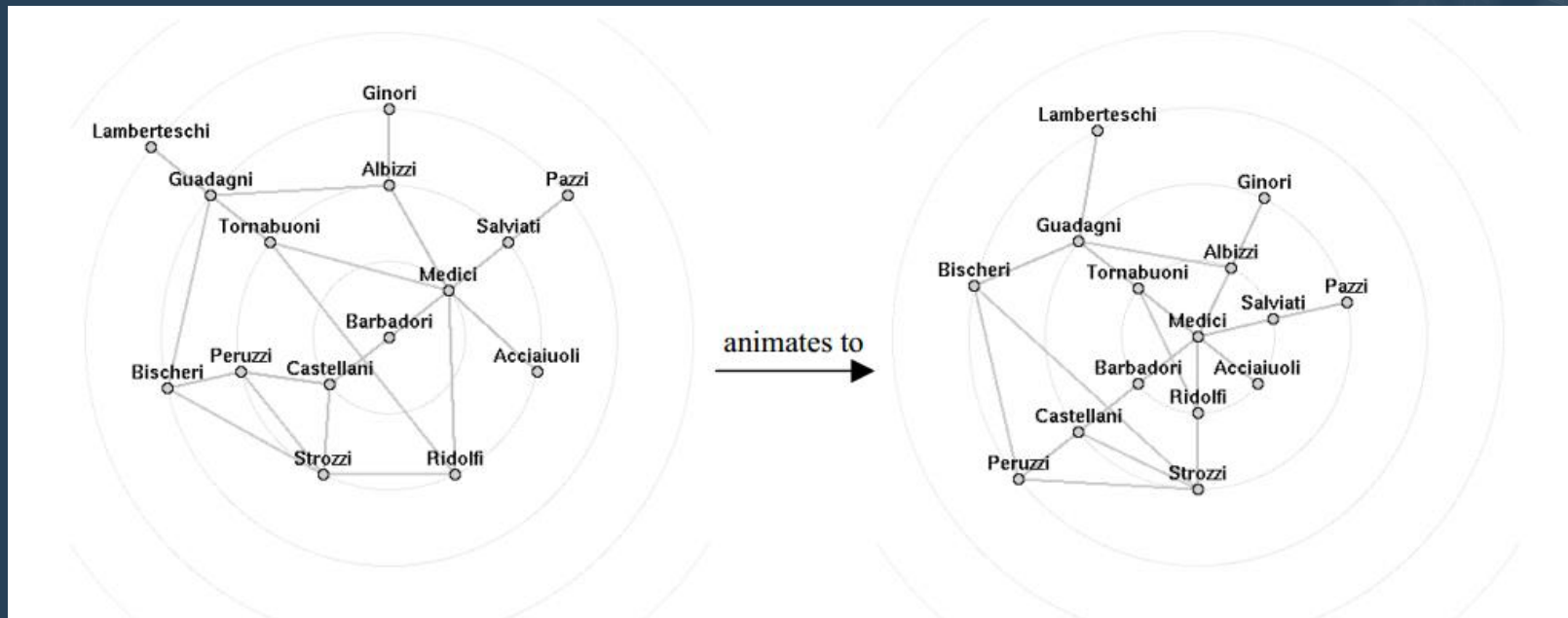


Many graphs are tree-like or have useful spanning trees

Spanning trees lead to arbitrary roots

Fast tree layouts allow graph layouts to be recalculated at interactive rates

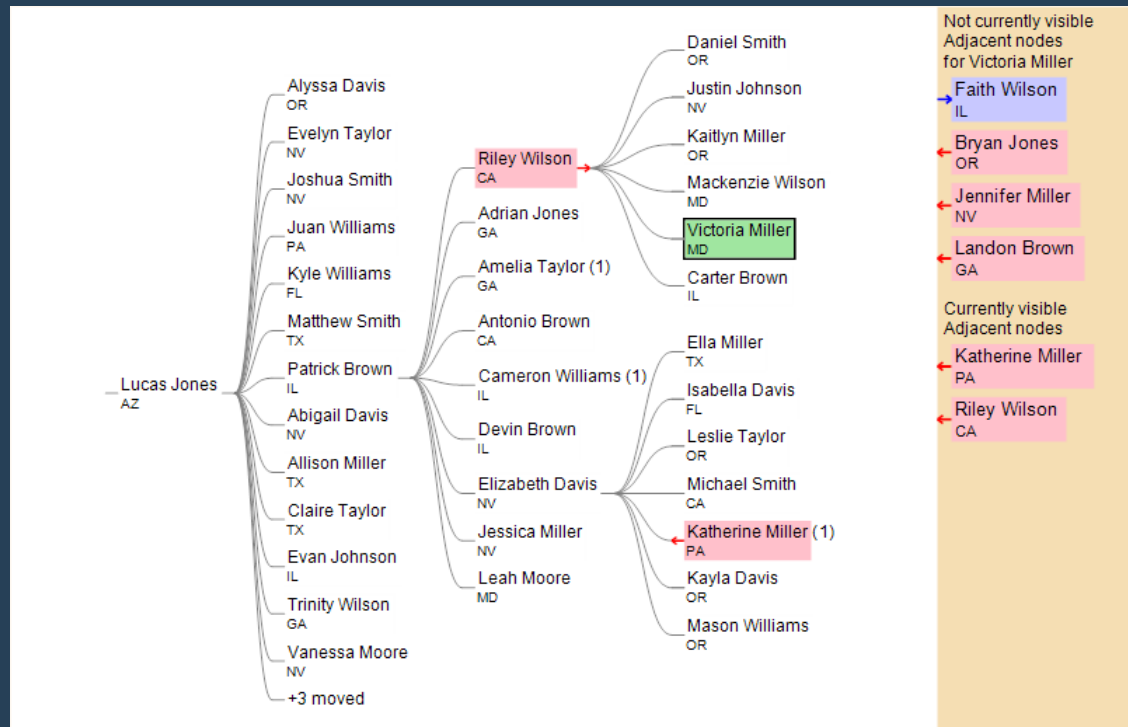
See the tree in this graph?



Animated Graphs with Radial Layout, *Yee et al.*, Infovis 2001

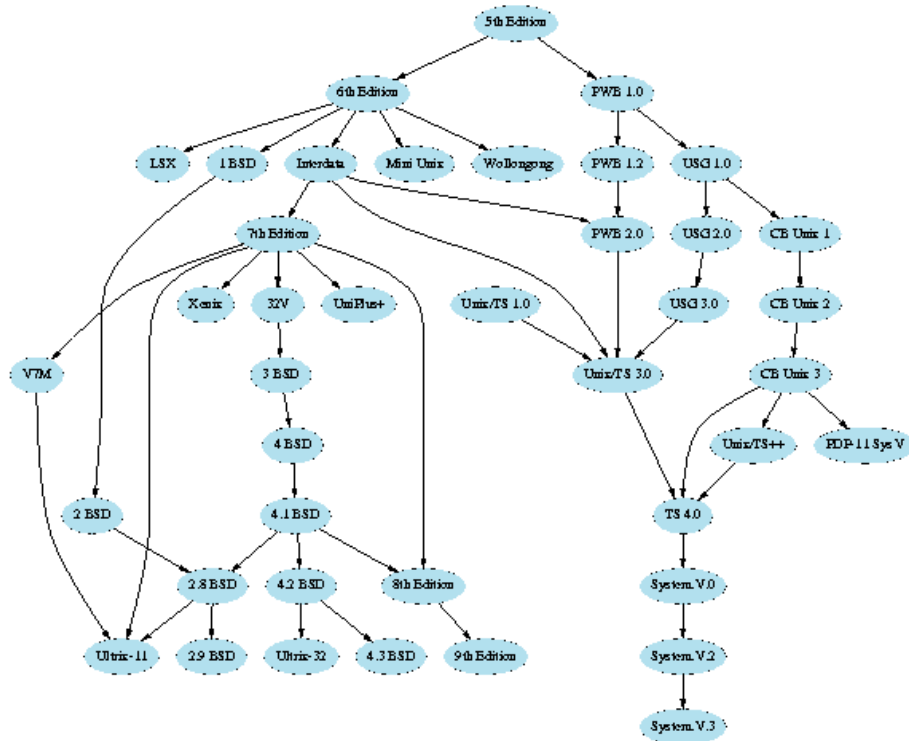
http://www.youtube.com/watch?v=OPX5iGro_IA

See the tree in this graph?



TreePlus, Lee *et al.*, VAST 2006

Hierarchical graph layout

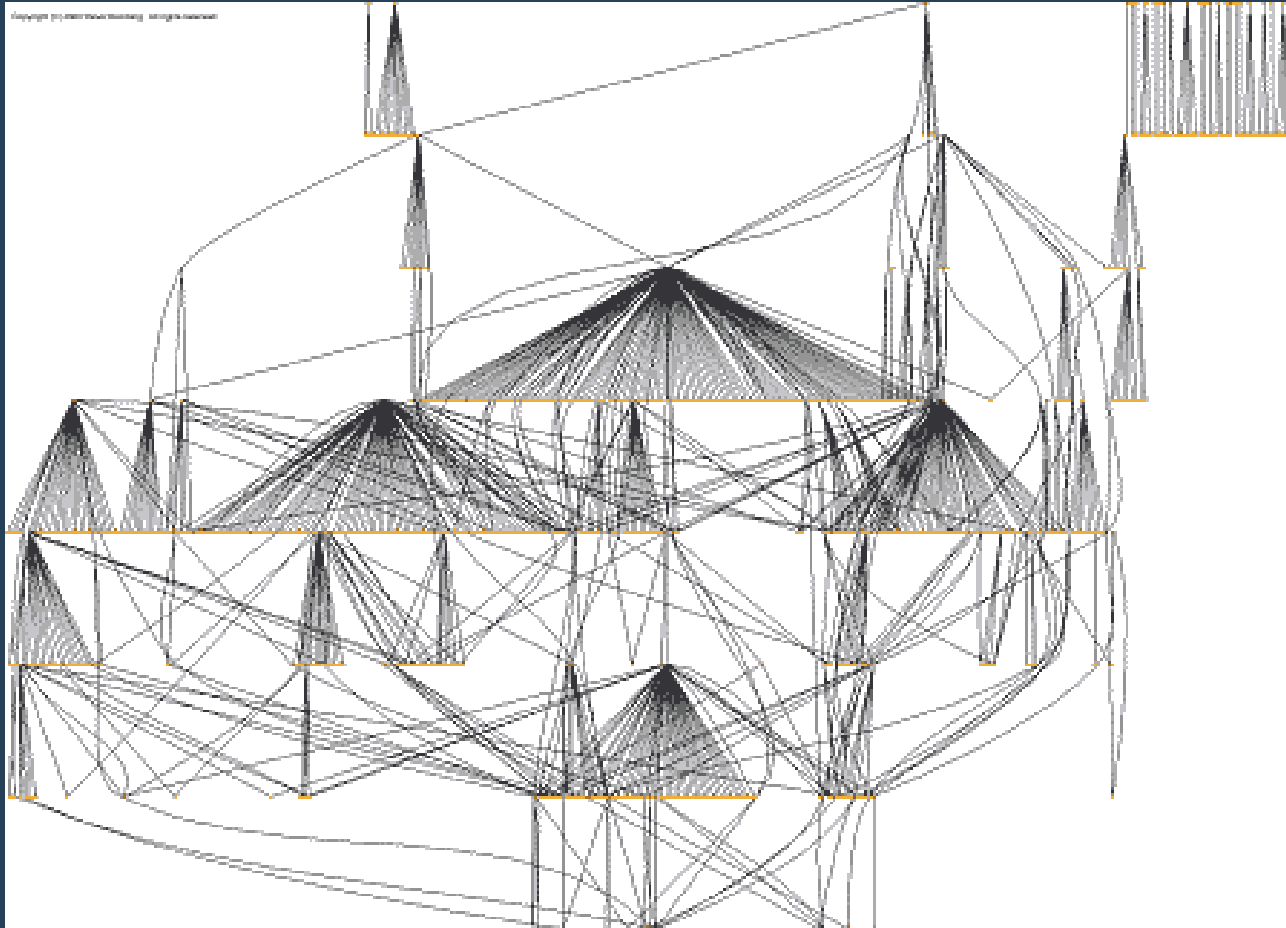


Sugiyama-style or
layered graph
drawing

Layout of a Direct
Acyclic Graph

Hierarchical layering
based on descent

Hierarchical graph layout



Optimization techniques

Treat layout as an *optimization problem*

- Define layout using an *energy model* and/or a set of *constraints*: equations the layout should try to obey
- Use optimization algorithms to solve

Regularly used for undirected graphs

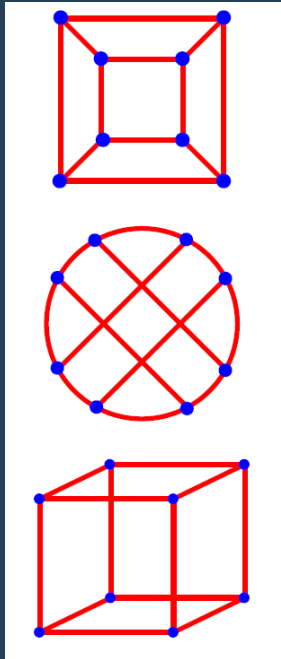
- *Force-Directed Layout* most common

We can introduce directional constraints

- *DiG-CoLa* (Di-Graph Constrained Optimization Layout) [Dwyer 05]
- Iterative constraint relaxation



"Aesthetic" constraints



Minimize edge crossings

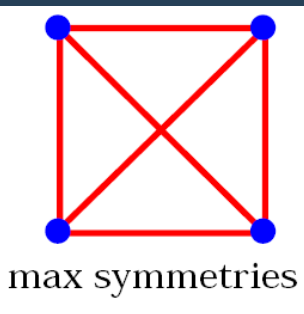
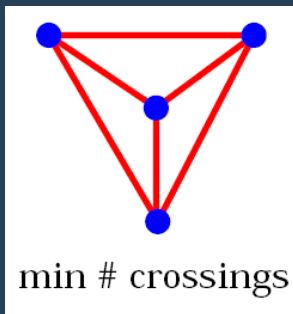
Minimize area

Minimize line bends

Minimize line slopes

Maximize smallest angle between edges

Maximize symmetry



but, can't do it all.

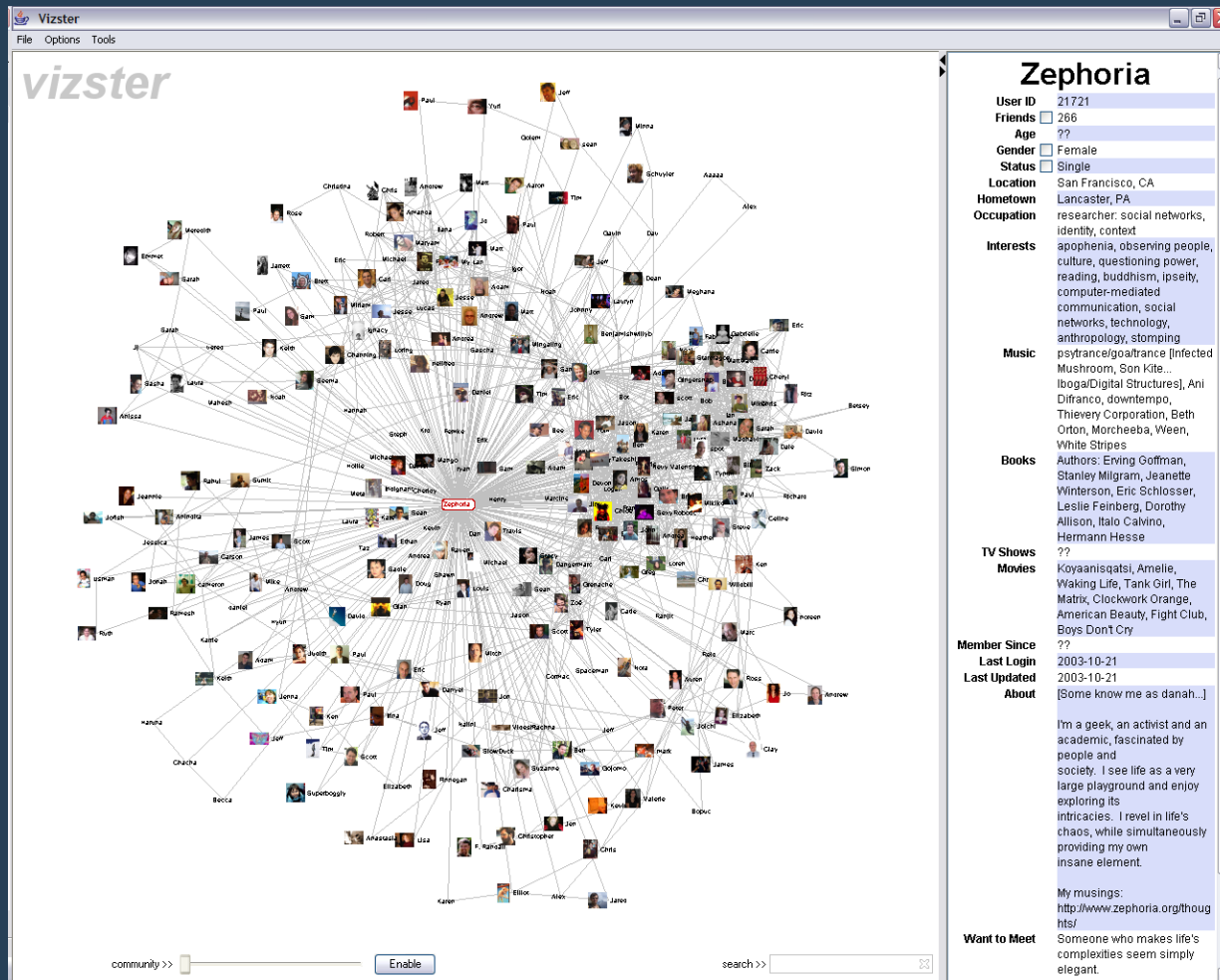
Force-directed layout

Nodes = charged particles $F = G * m_1 * m_2 / (x_i - x_j)^2$
with air resistance $F = -b * v_i$
Edges = springs $F = -k * (x_i - x_j - L)$

Repeatedly calculate forces, update node positions

- Naïve approach $O(N^2)$
- Speed up to $O(N \log N)$ using quadtree or k-d tree
- Numerical integration of forces at each time step

Ego-Centered Networks



Vizster, Heer et al., Infovis 2005

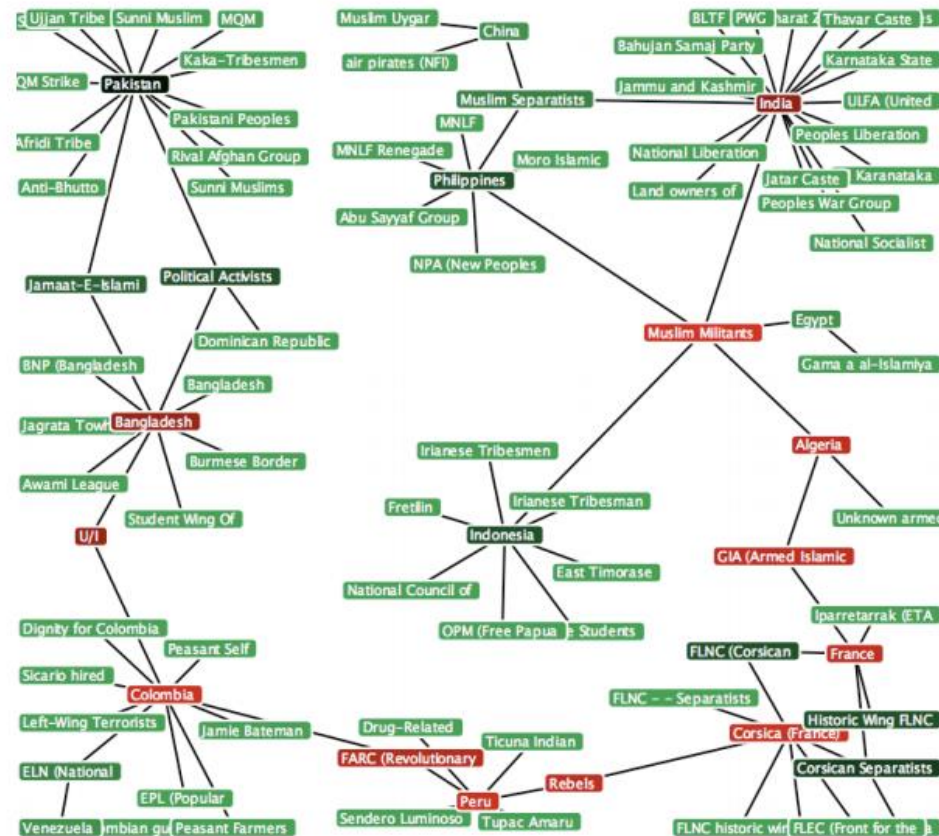
Filtered Networks

Rankings

Betweenness Centrality

The number of shortest paths between pairs of nodes that pass through a given node.

Rank	Node	Type
2,516.00	Muslim Militants	Terrorist Group
2,436.50	Corsica (France)	Country
2,413.00	Colombia	Country
2,368.00	Peru	Country
2,280.50	France	Country
2,239.00	Algeria	Country
2,226.00	Rebels	Terrorist Group
2,214.00	GIA (Armed Islamic Group)	Terrorist Group
2,124.00	FARC (Revolutionary Armed For...	Terrorist Group
1,718.00	Bangladesh	Country
1,656.00	U/I	Terrorist Group
1,598.00	India	Country
1,063.00	Pakistan	Country
798.00	Corsican Separatists	Terrorist Group
704.00	FLNC (Corsican National Libera...	Terrorist Group
704.00	Historic Wing FLNC	Terrorist Group
637.00	Indonesia	Country
614.00	Political Activists	Terrorist Group
596.00	Philippines	Country
520.00	Jamaat-E-Islami	Terrorist Group
330.00	Muslim Separatists	Terrorist Group
276.00	ELN (National Liberation Army)	Terrorist Group
187.00	Venezuela	Country
187.00	China	Country
94.00	Egypt	Country
0.00	Dignity for Colombia	Terrorist Group
0.00	Jamie Bateman Canon Front	Terrorist Group
0.00	Sendero Luminoso	Terrorist Group
0.00	Jamiat-ul-Mujahideen	Terrorist Group
0.00	Timorese Students	Terrorist Group



Social Action, Perer et al., Infovis 2006

Constraint Optimization layout

Minimize stress function

$$\text{stress}(X) = \sum_{i < j} w_{ij} (\|X_i - X_j\| - d_{ij})^2$$

- X : node positions, d : optimal edge length,
- w : normalization constants
- Use global (*majorization*) or localized (*gradient descent*) optimization

→ Says: Try to place nodes d_{ij} apart

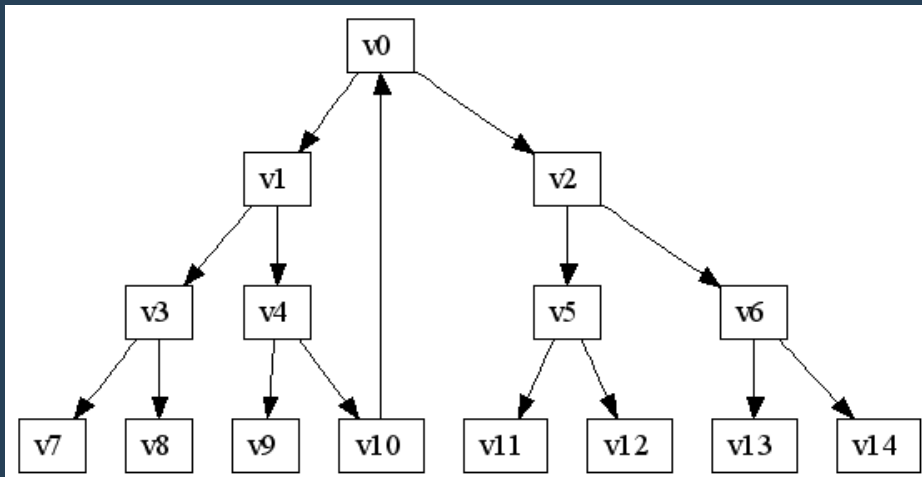
Add hierarchy ordering constraints

$$E_H(y) = \sum_{(i,j) \in E} (y_i - y_j - \delta_{ij})^2$$

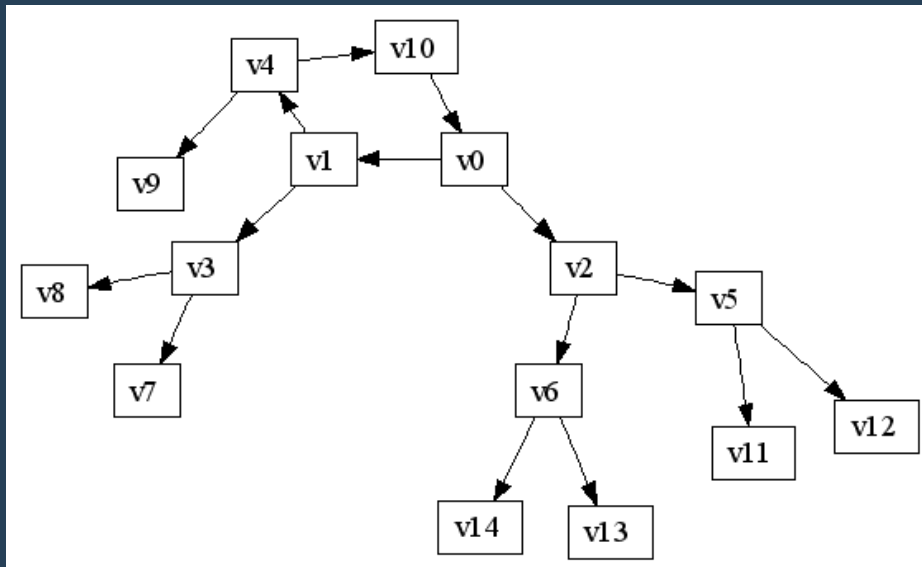
- y : node y -coordinates
- δ : edge direction (e.g., 1 for $i \rightarrow j$, 0 for undirected)

→ Says: If i points to j , it should have a lower y -value

Constraint Optimization layout



Sugiyama layout (dot)
Preserve tree structure

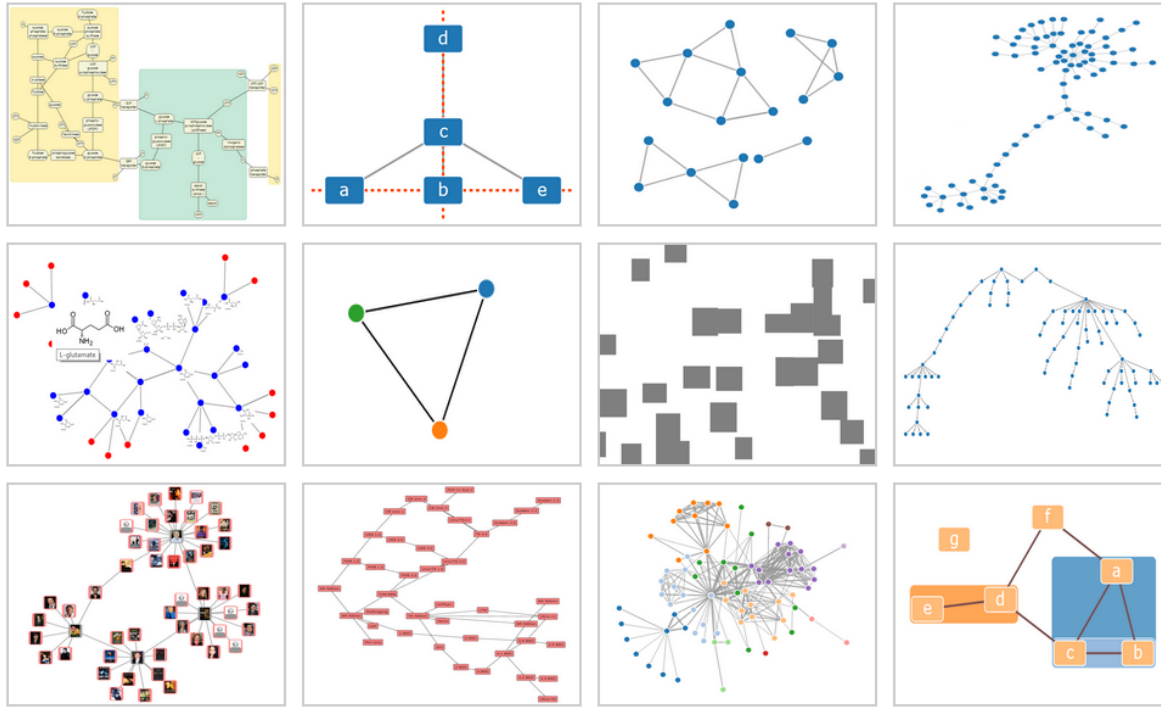


DiG-CoLa method
Preserve edge lengths

Constraint-based layout

cola.js

Constraint-Based Layout in the Browser



<http://marvl.infotech.monash.edu/webcola/>

Coping with messiness



Interaction Techniques for Selecting and Manipulating Subgraphs in Network Visualizations

Presented at IEEE InfoVis 2009

Michael J. McGuffin

École de technologie supérieure

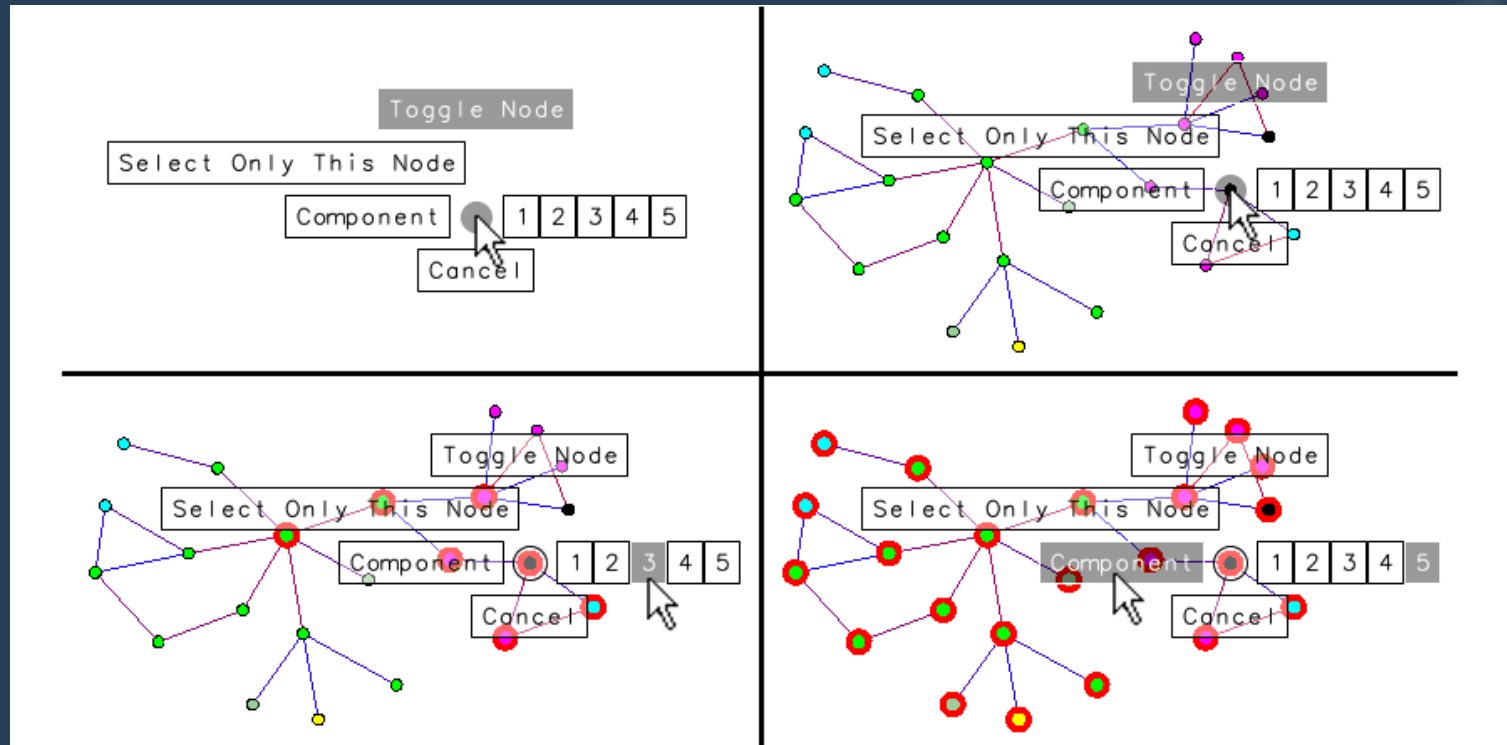
Montréal, Canada, <http://profs.logti.etsmtl.ca/mmcguffin/>

Igor Jurisica

Ontario Cancer Institute, PMH/UHN

Toronto, Canada, <http://www.cs.toronto.edu/~juris/>

Layout Interaction Techniques



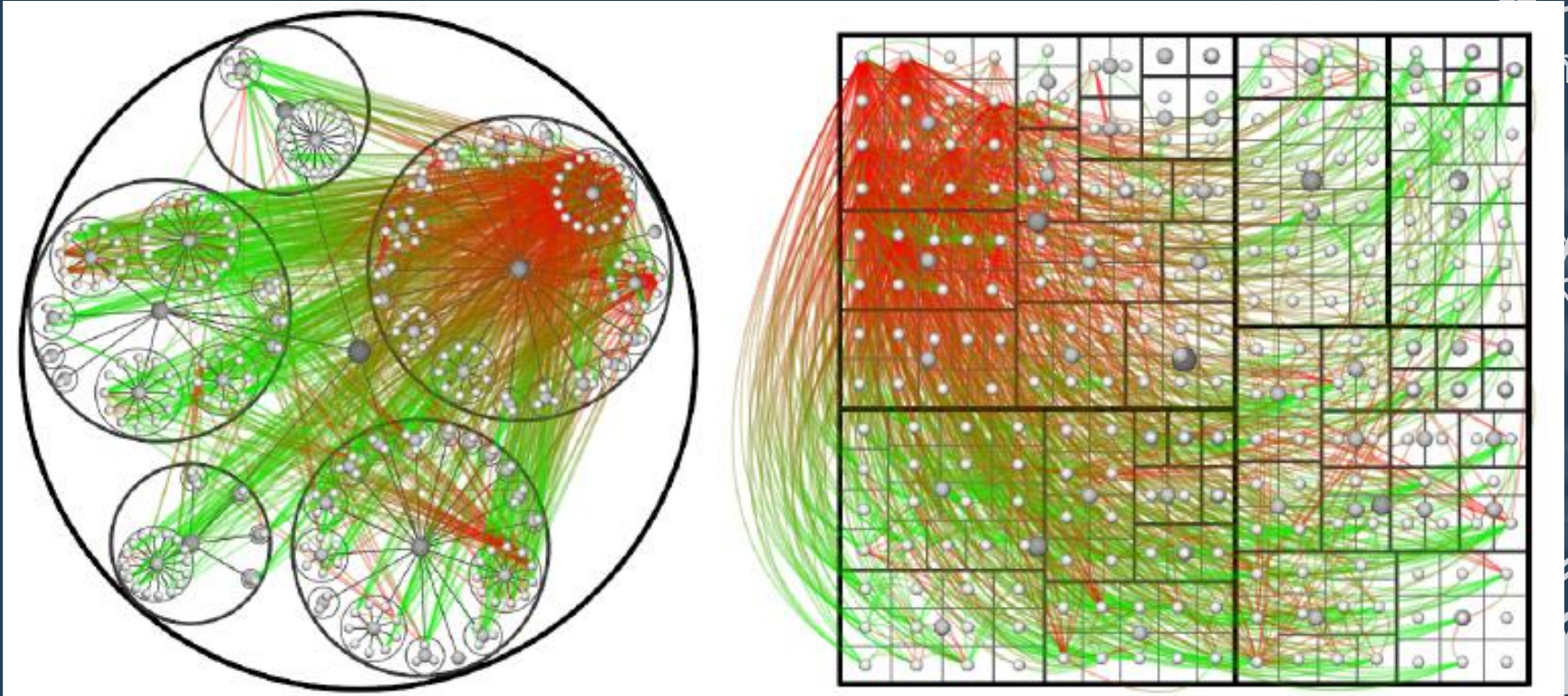
HotBox, McGuffin et al., Infovis 2009

Edge Interaction Techniques

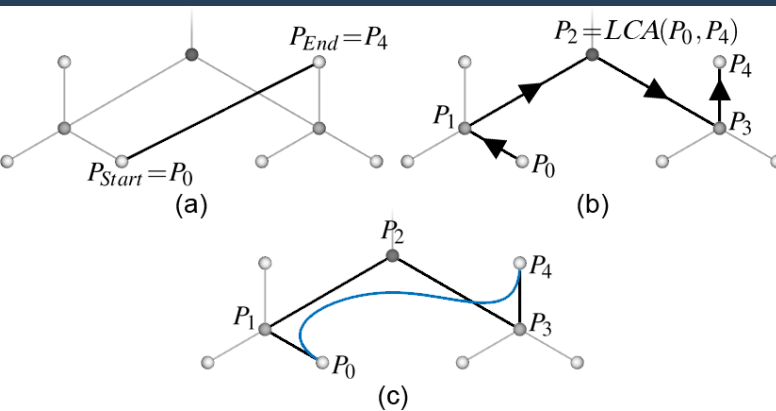


Multitouch Edge Interaction, *Schmidt et al.*, ITS 2010

Edge Bundling

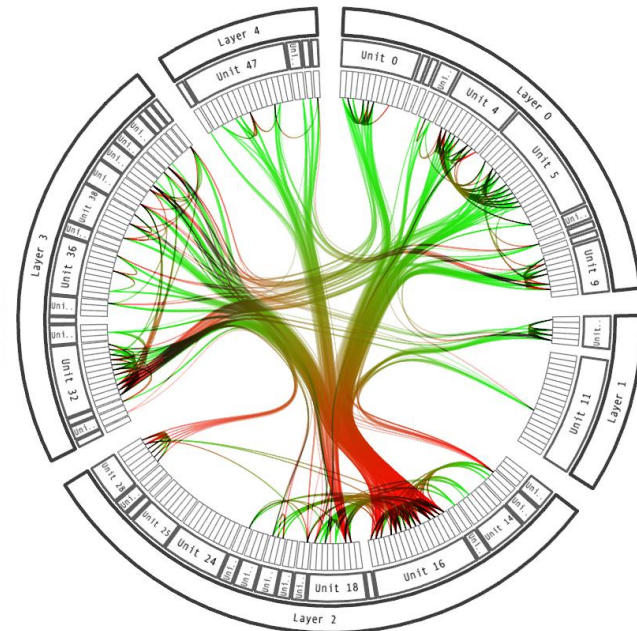
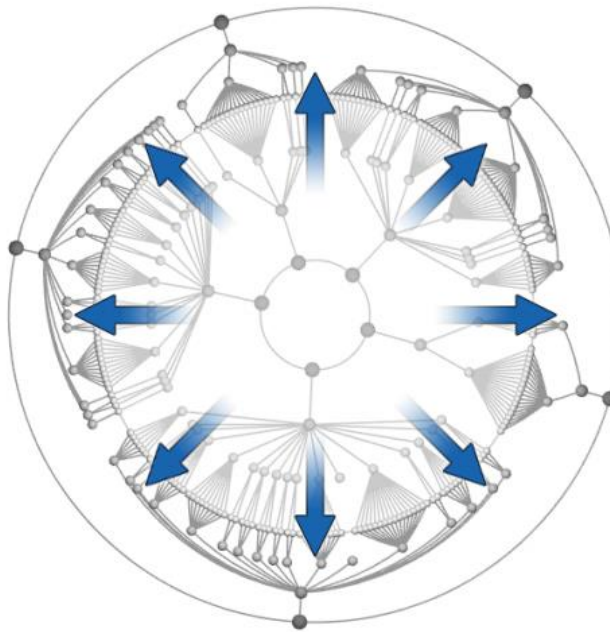
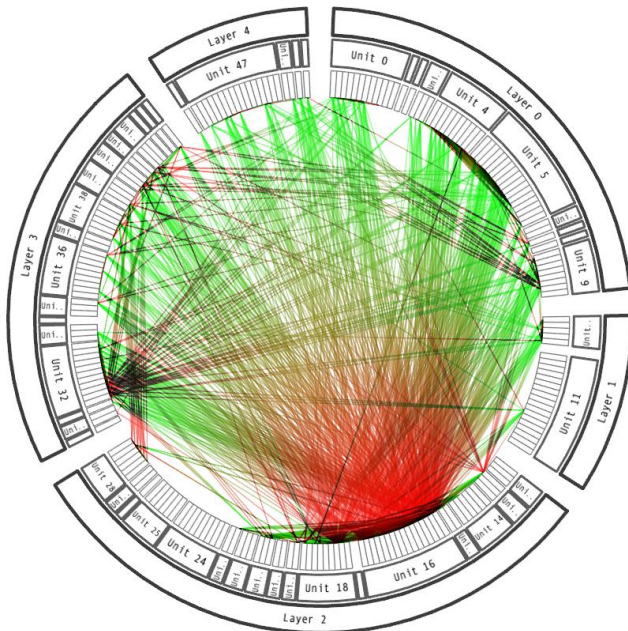


Hierarchical Edge Bundling



Use the hierarchy to bundle edges

Holten, Infovis 2006

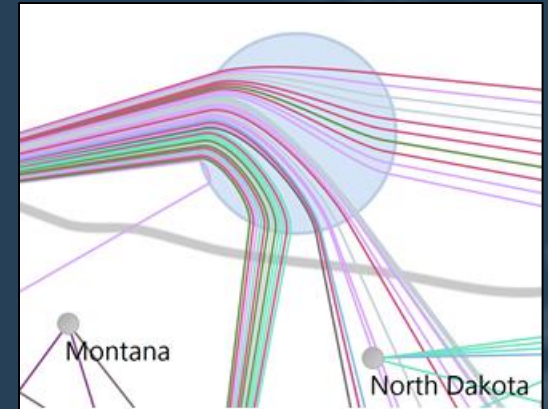


Bundle-based exploration

Recorded trajectories
Bundling and unbundling
exploration

Interactive Bundling

Interactive Bundling



The issue of scale



Solutions

Extracting network motifs

Taking advantage of node attributes

to layout/filter

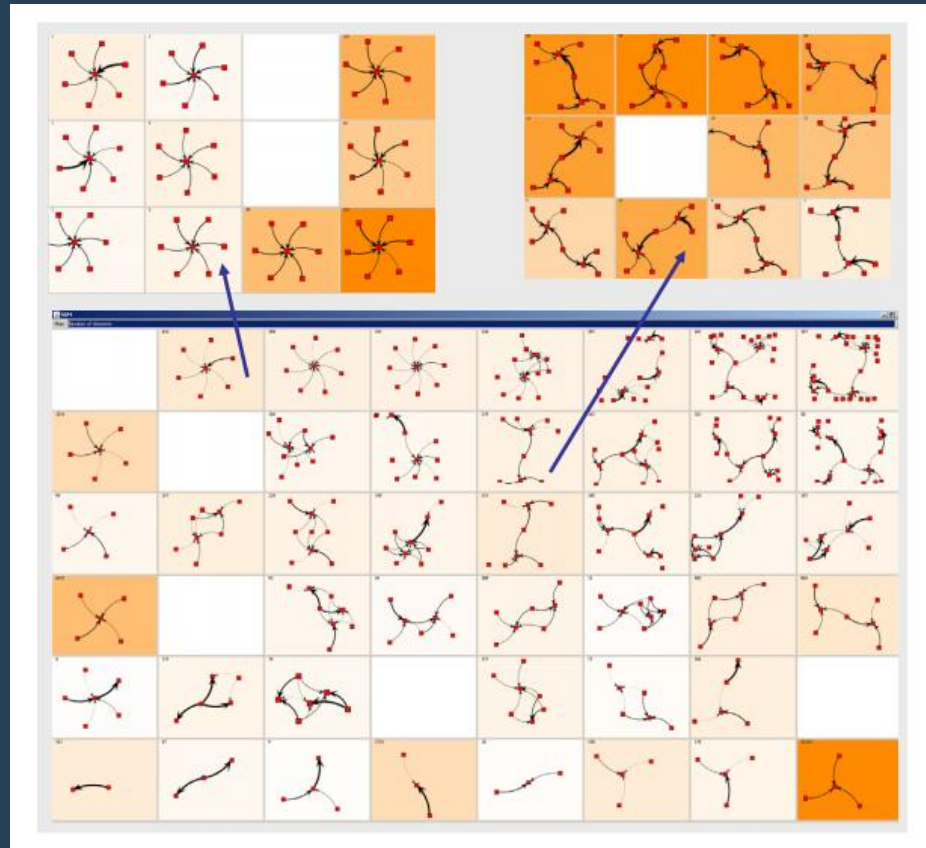
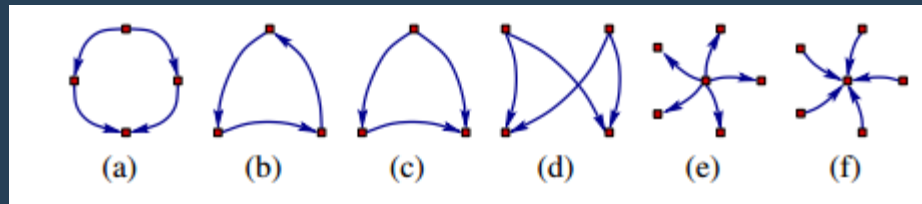
to aggregate

Degree-of-Interest graphs

Use the alternative representation

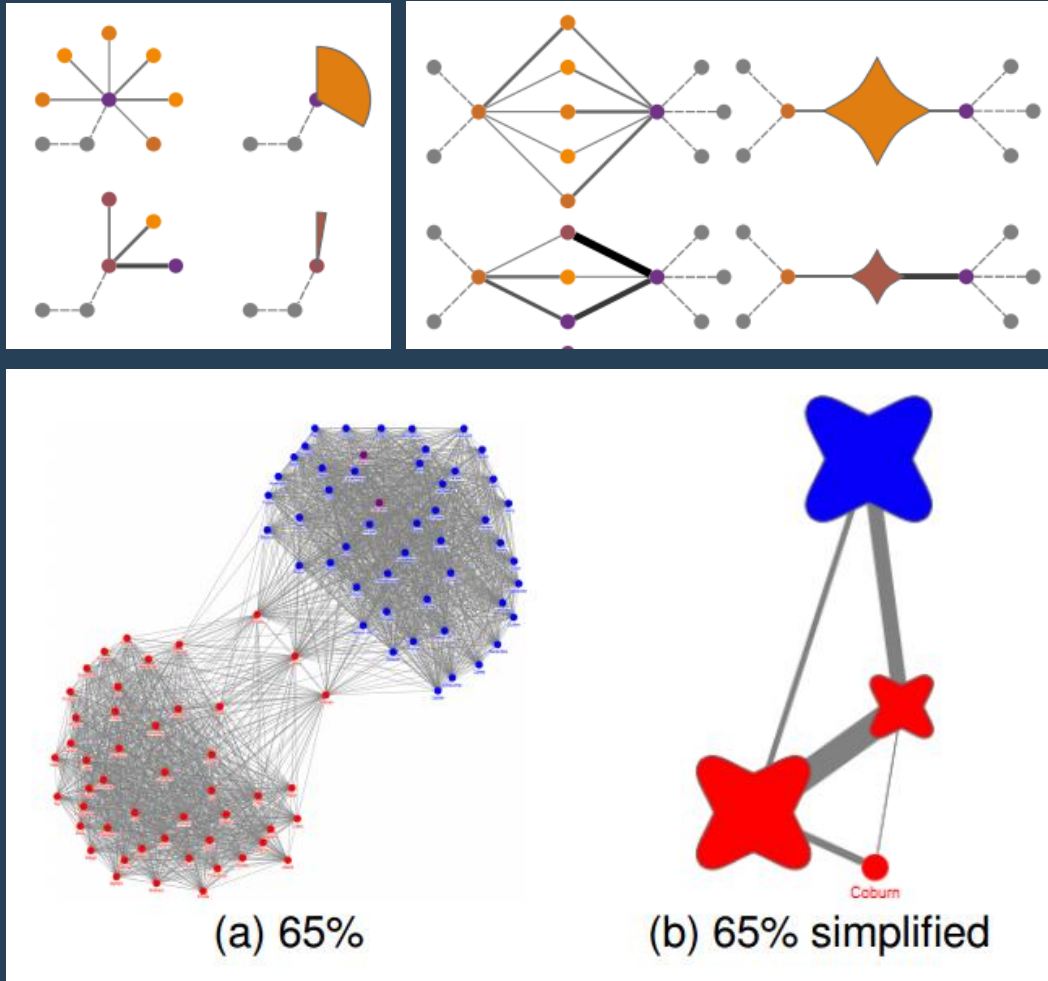


Motifs



Motifs, von Landsberger et al., VAST 2009

Motifs of higher order



Attribute-driven layout

Large node-link diagrams get messy!

Is there additional structure we can exploit?

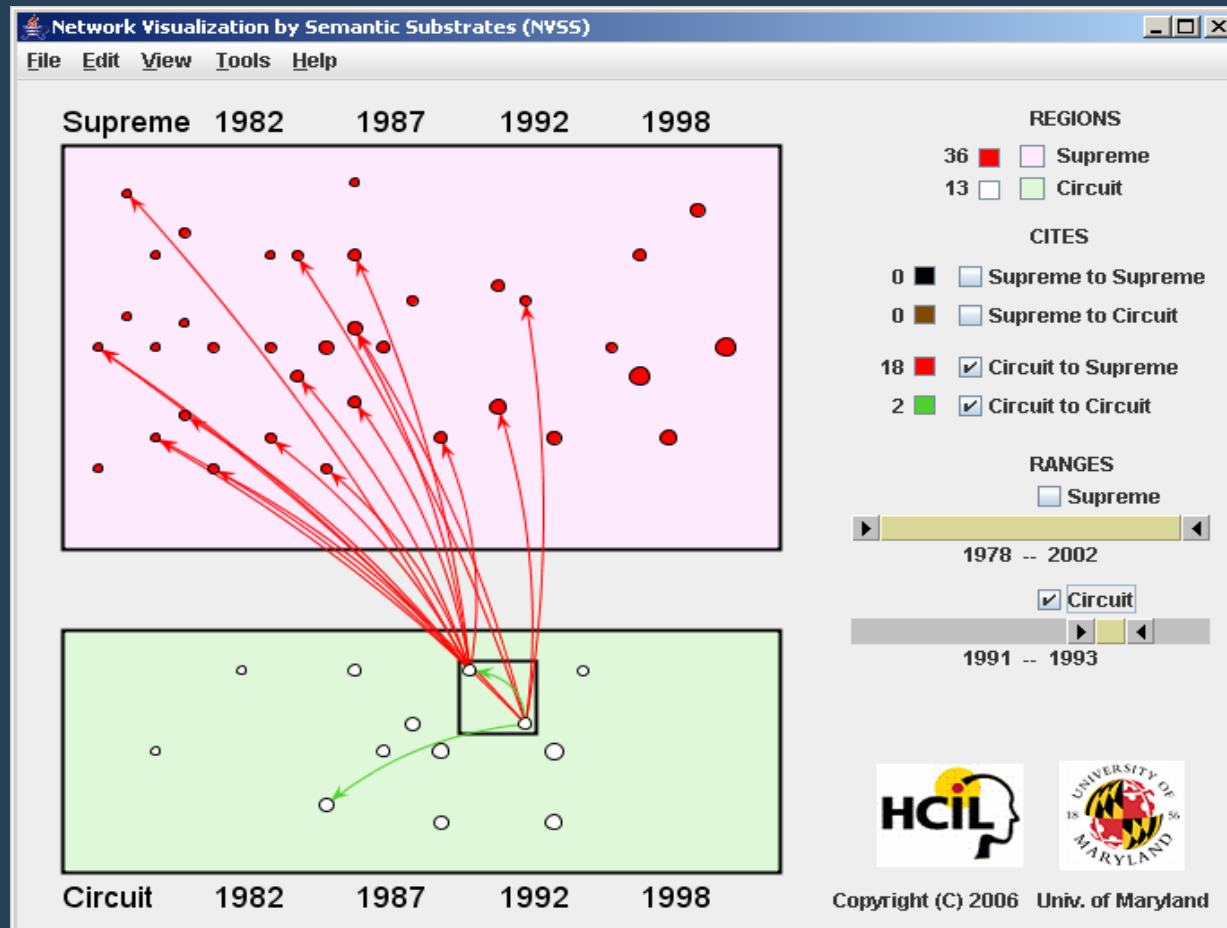
Idea: Use data attributes to perform layout

e.g., scatter plot based on node values

Dynamic queries and/or brushing can be used to explore connectivity

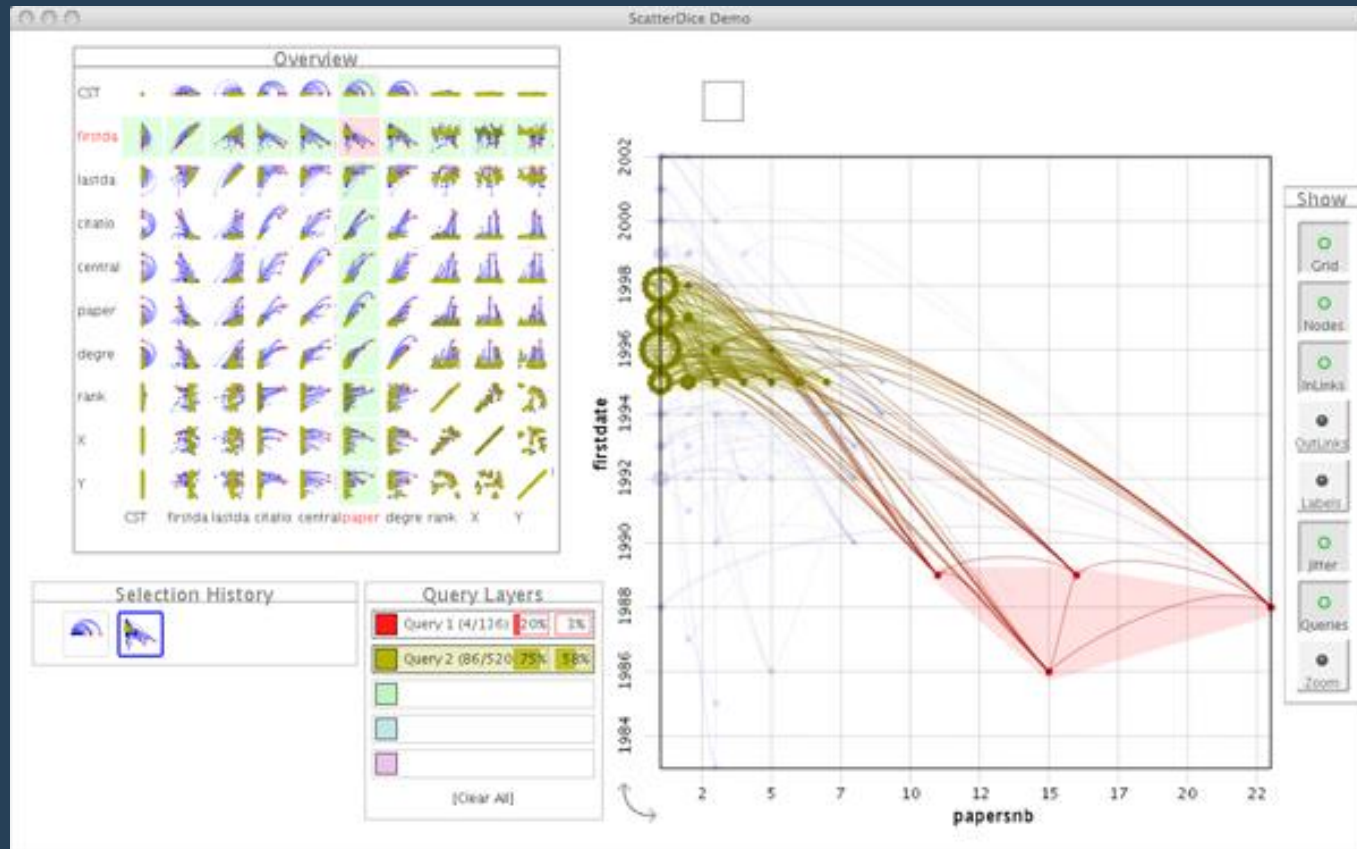


Attribute-driven layout



Semantic Substrates, *Shneiderman et al.*, Infovis 2006

Attribute-driven layout



GraphDice, *Bezerianos et al.*, Eurovis 2010

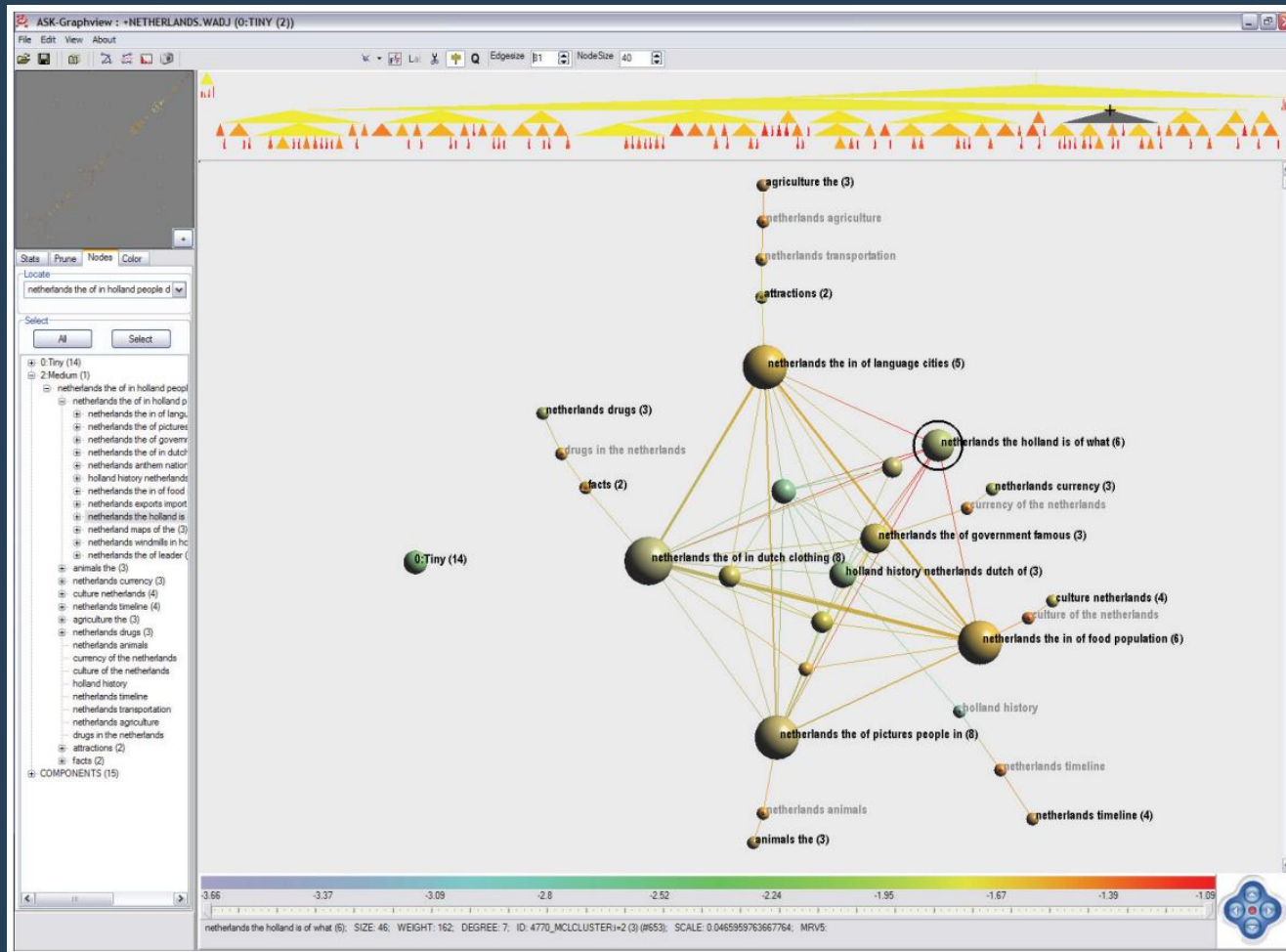
GraphDice: A System for Exploring Multivariate Social Networks

A. Bezerianos
F. Chevalier
P. Dragicevic
N. Elmqvist
J-D. Fekete

INRIA
École Centrale Paris
Purdue University

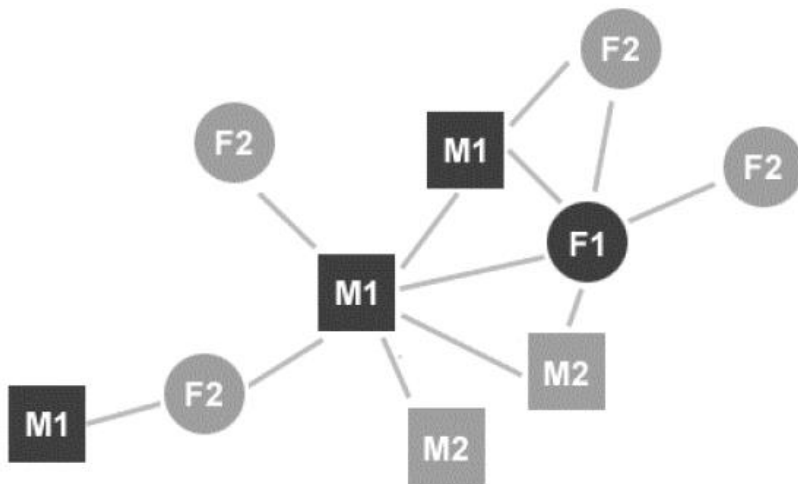
GraphDice, *Bezerianos et al.*, Eurovis 2010

Hierarchical Aggregation

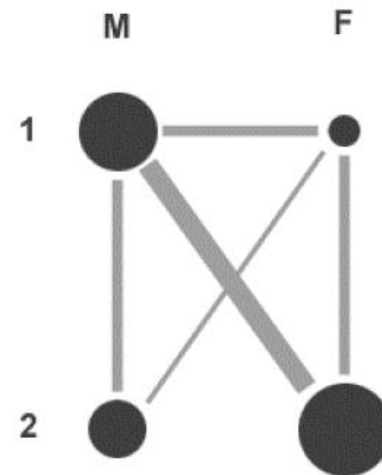


ASK-GraphView, *Abello et al.*, Infovis 2006

Attribute-driven aggregation

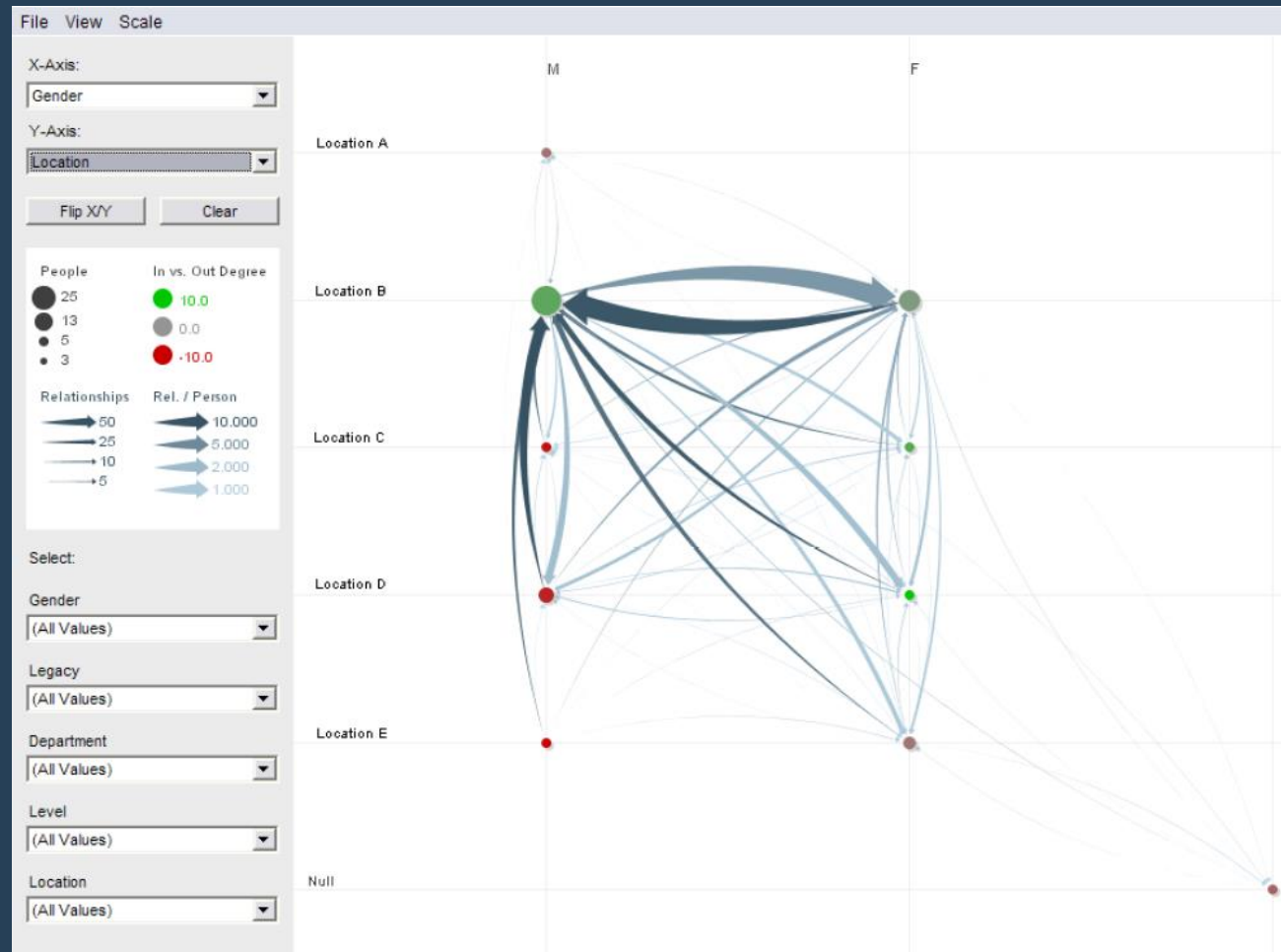


Node and Link Diagram



PivotGraph Roll-up

PivotGraph



Gender

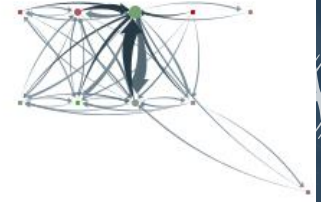
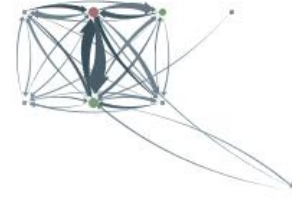
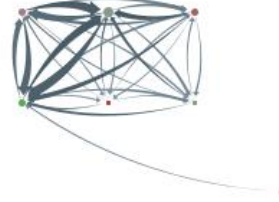
Legacy

Department

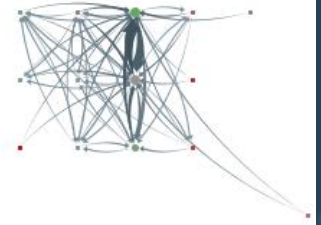
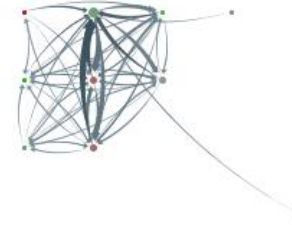
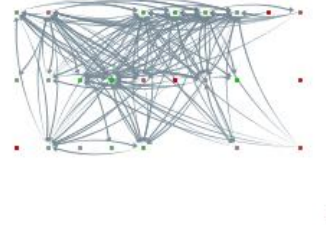
Level

Location

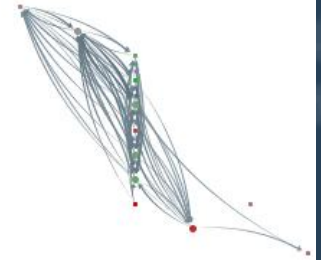
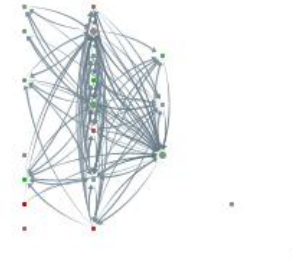
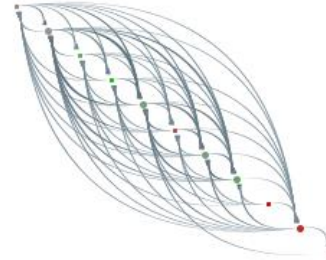
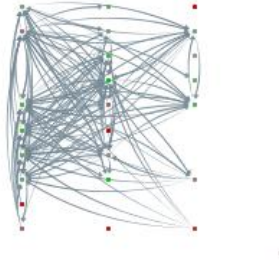
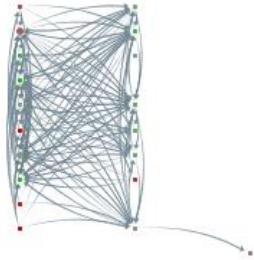
Gender



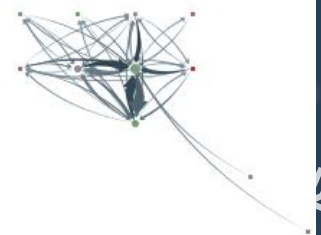
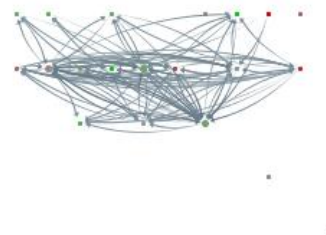
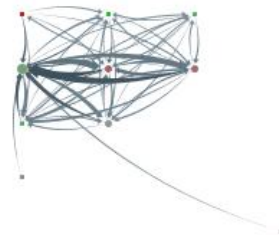
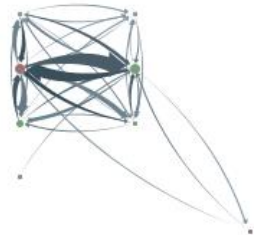
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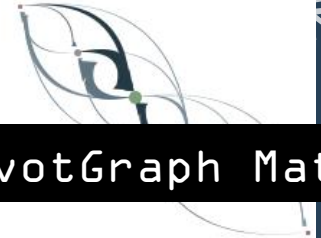
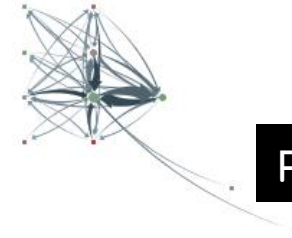
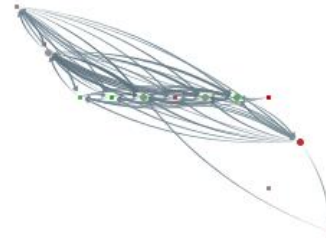
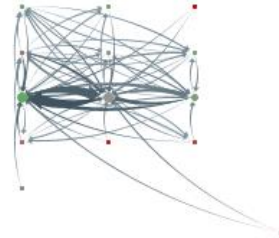
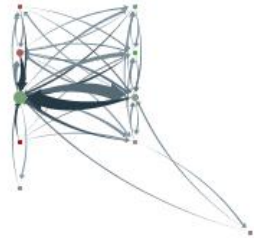
Department



Level



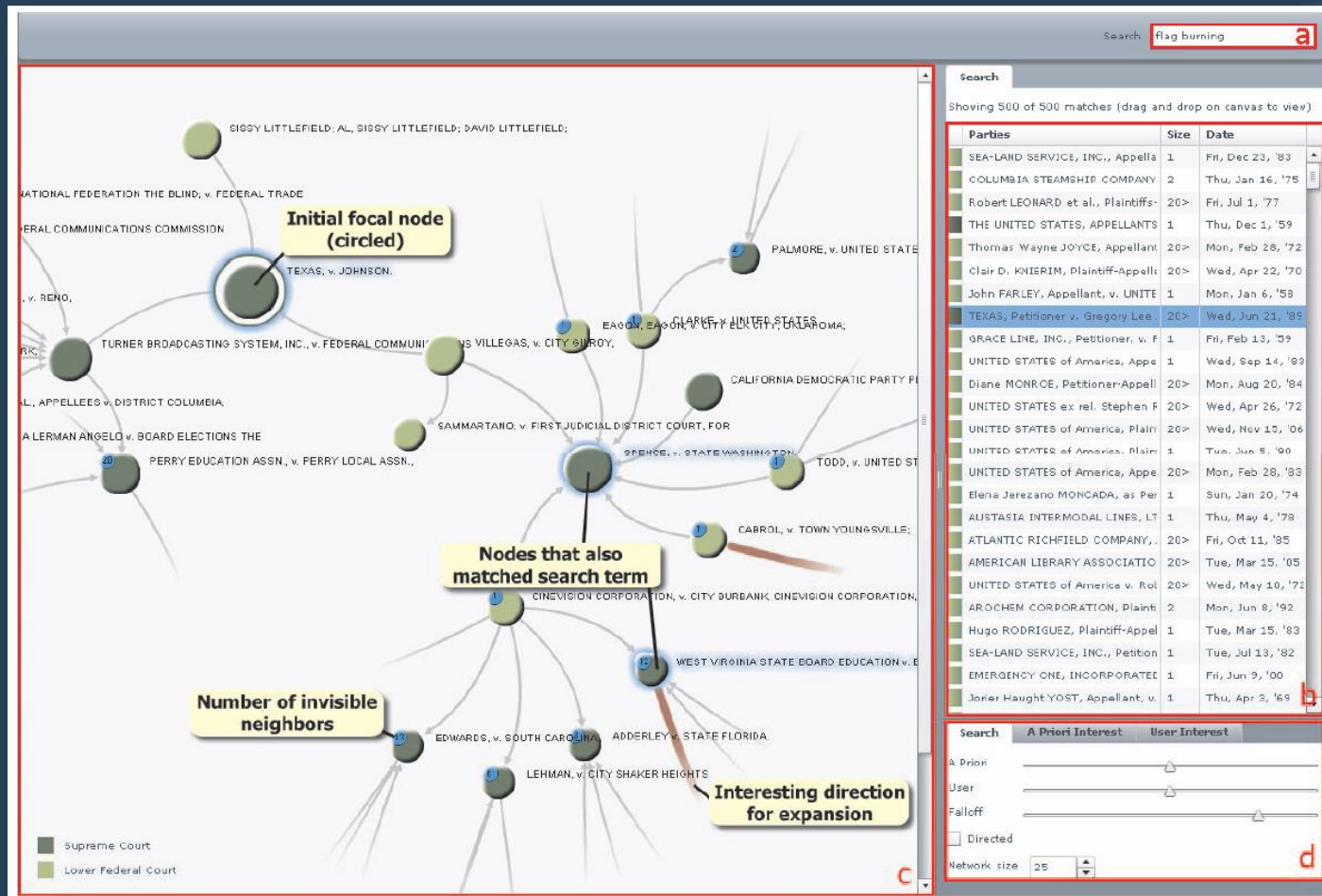
Location



PivotGraph Mat

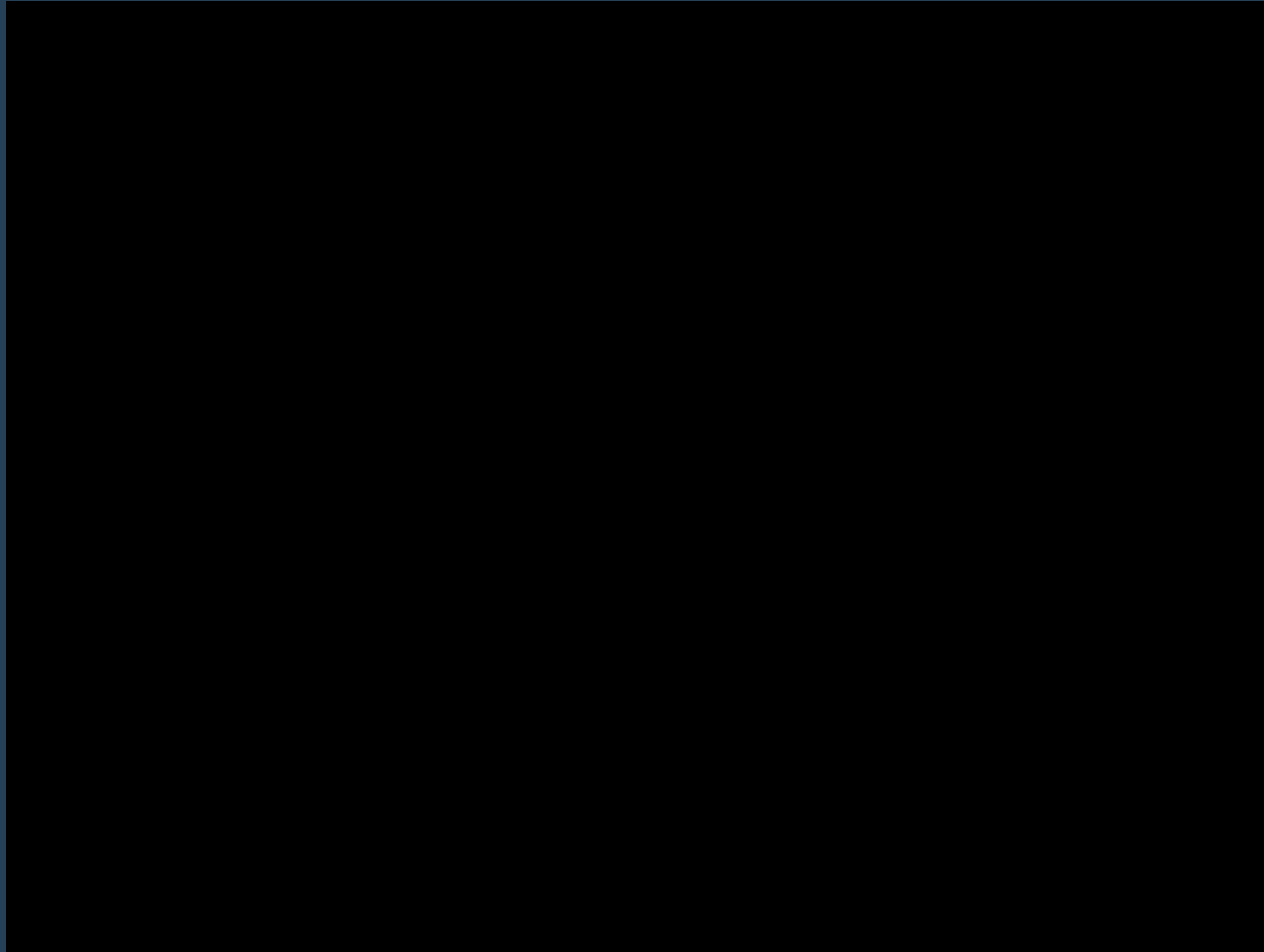


Degree-of-Interest Graphs



Search, Show Context, Expand, *Perer et al.*, Infovis 2009

Search & Browse

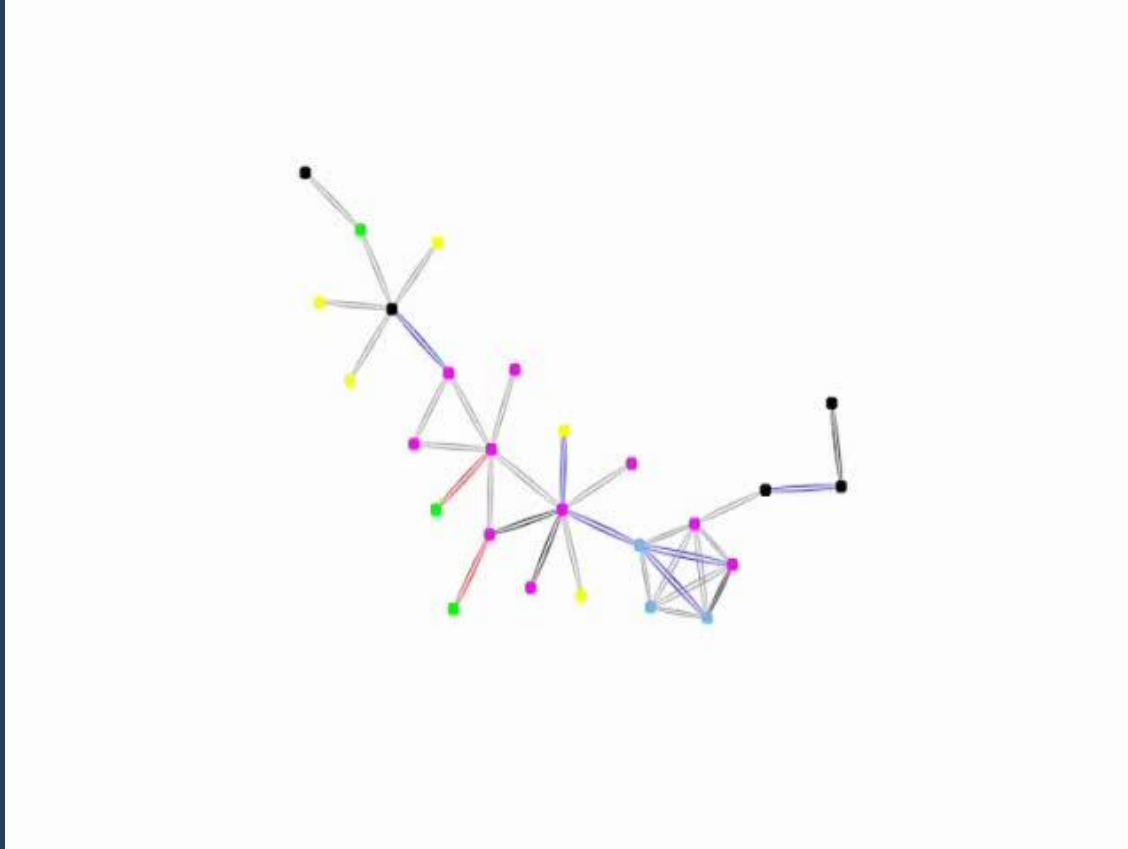


PivotPaths, *Doerk et al.*, Infovis 2012

Use the Alternative

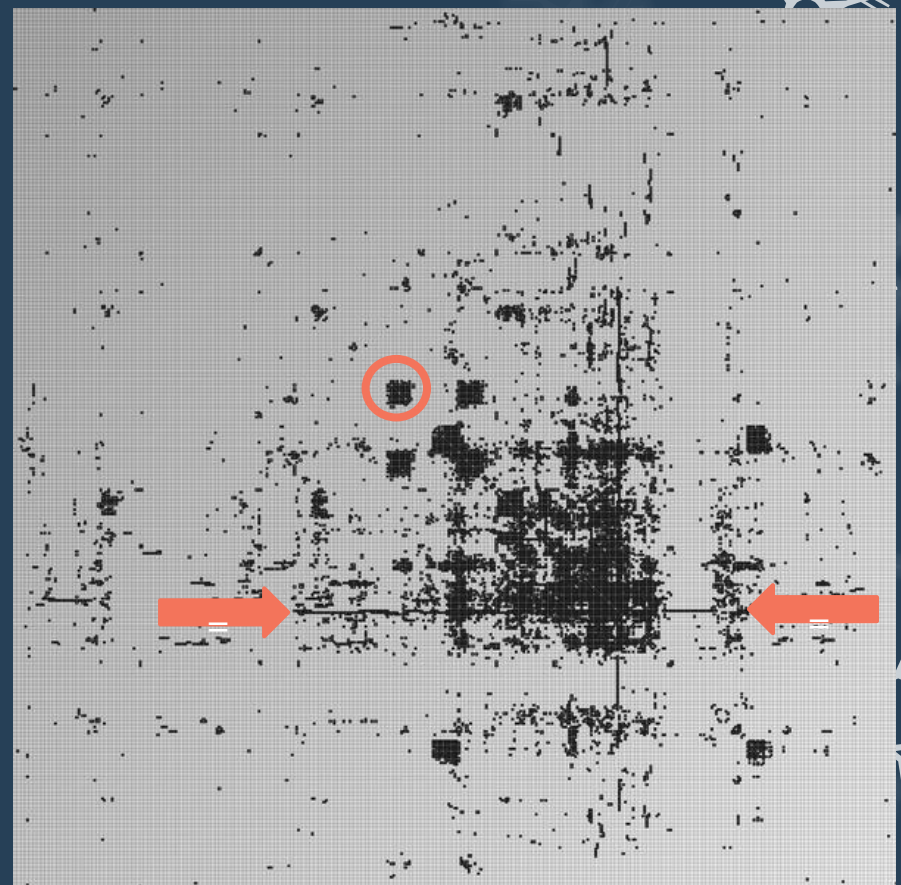
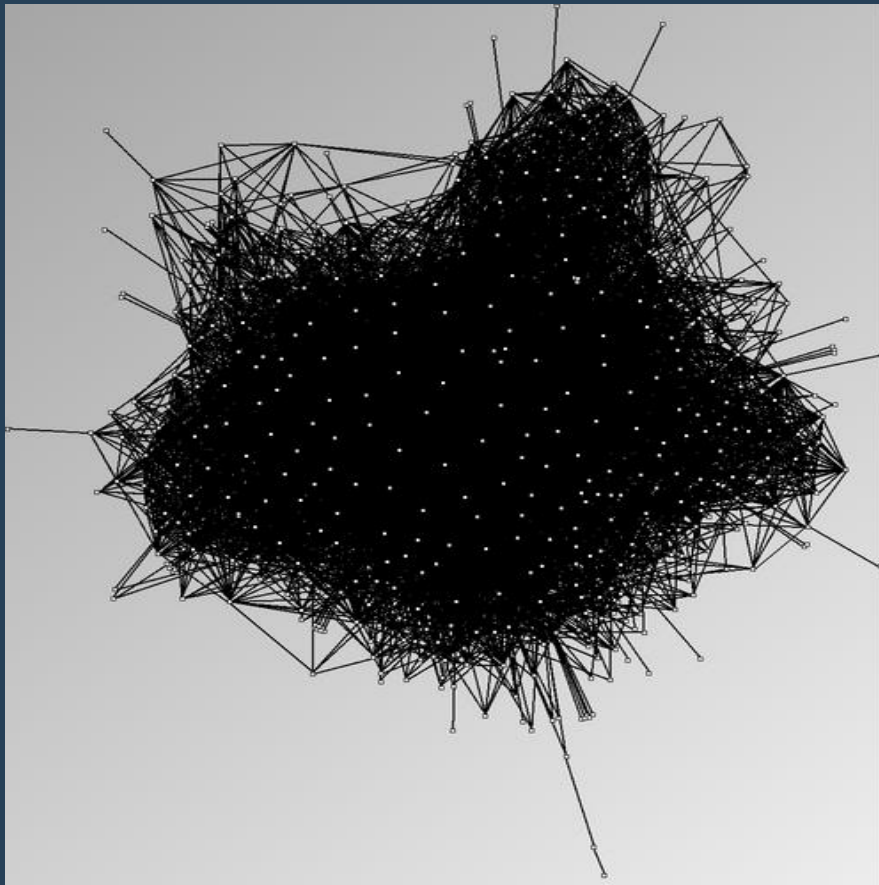


Matrices

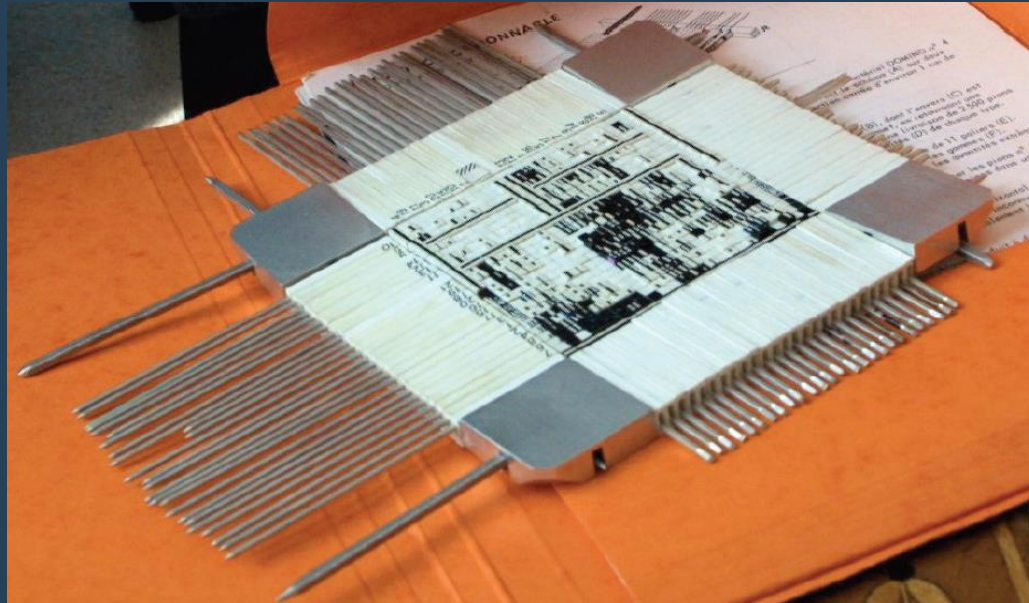


Matrices

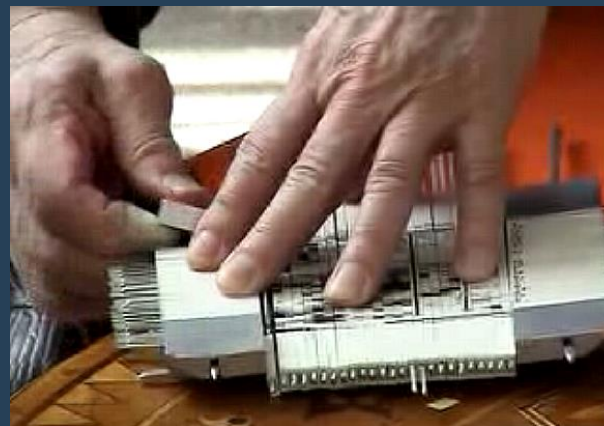
one year of email between ~ 500 researchers



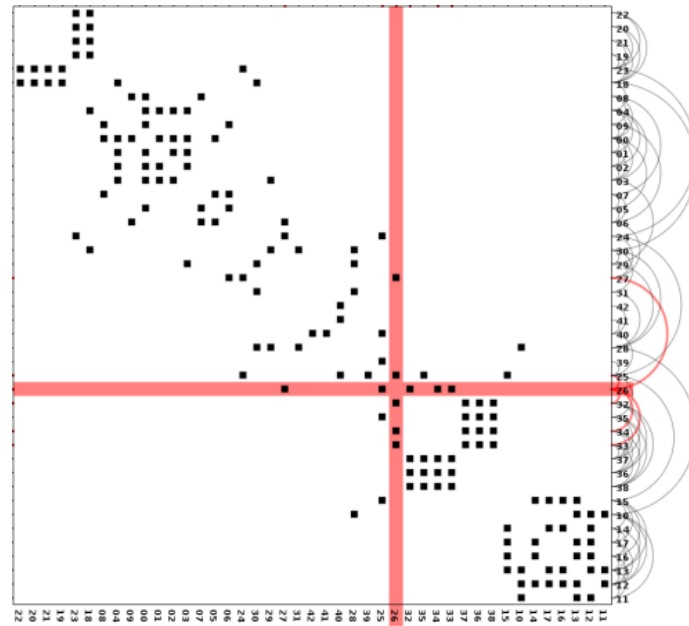
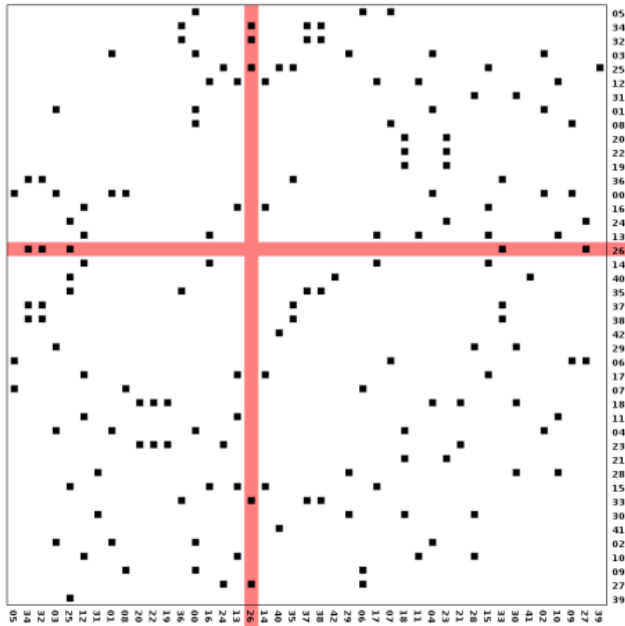
The Reorderable Matrix



Jacques
Bertin
1967



Revealing patterns



Matrix vs Node-Link

- ✗ Require learning

- ✓ No overlap

- ✓ No crossings

- ✗ Use a lot of space

- ✓ Dense graphs

- ✗ Sparse graphs

- ✓ Familiar

- ✗ Node overlap

- ✗ Link crossing

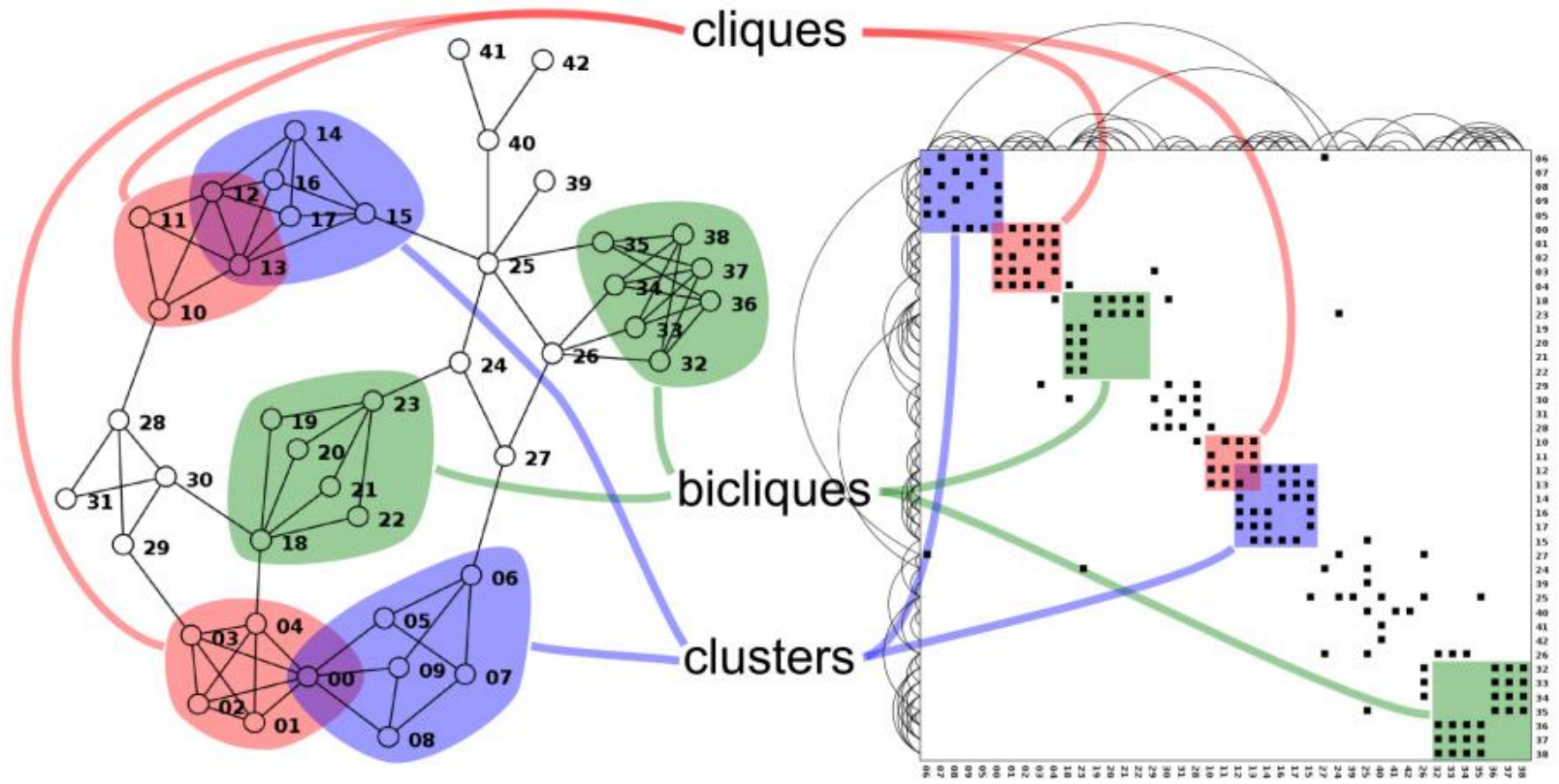
- ✓ More compact

- ✗ Dense graphs

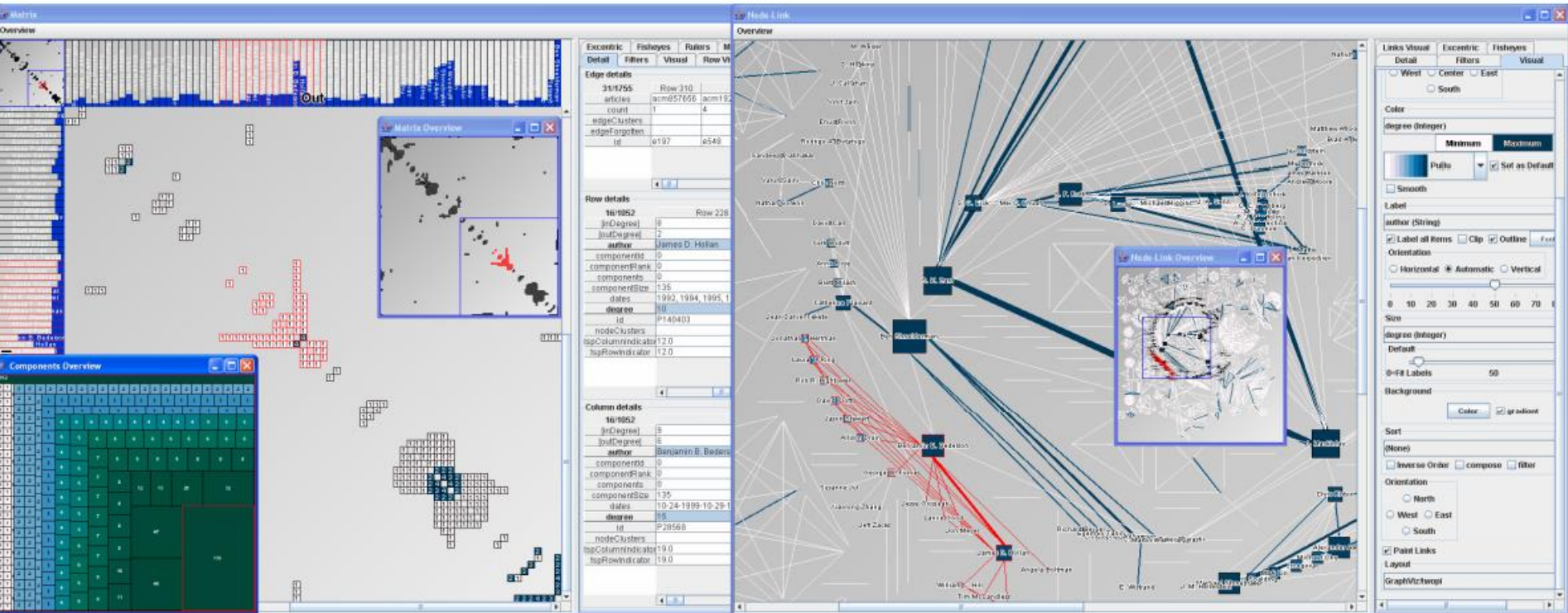
- ✓ Sparse graphs



Learning phase

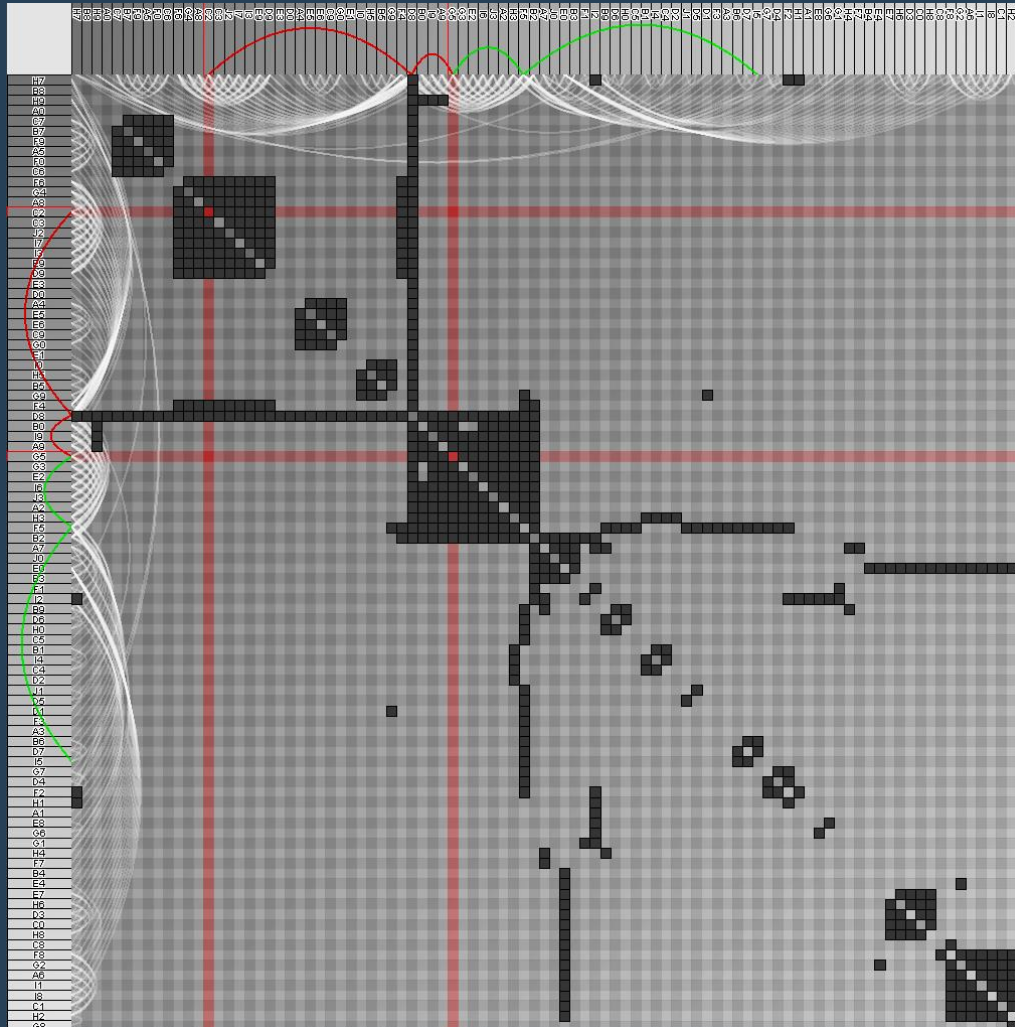


Matrix + Node-Link



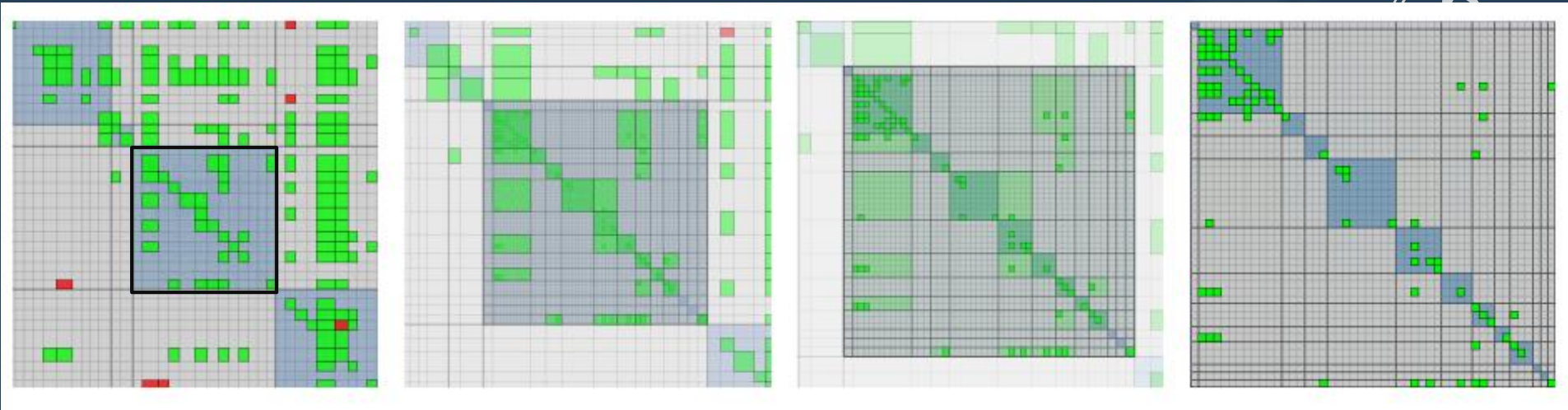
MatrixExplorer, Henry et al., Infovis 2006

Following paths in Matrices



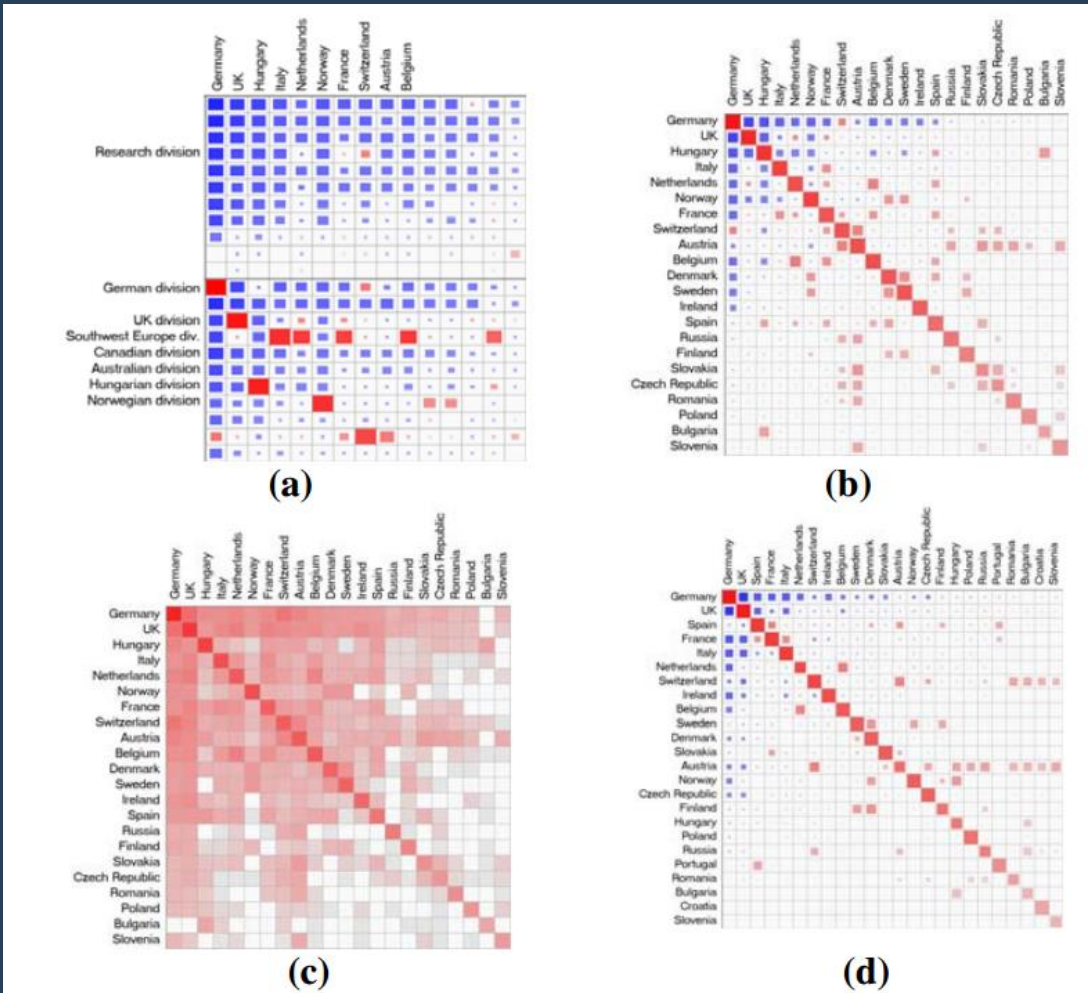


Hierarchical Aggregation



MatrixZoom, *van Ham*, Infovis 2003

Attribute-driven Aggregation



Honeycomb, *van Ham et al.*, Interact 2009

Hybrid Graph Representation

Merging Node-Link Diagrams and Matrices

Hybrid Graph Representation

**Supporting Community Analysis
while Exploring Large Matrices**

Active research topics

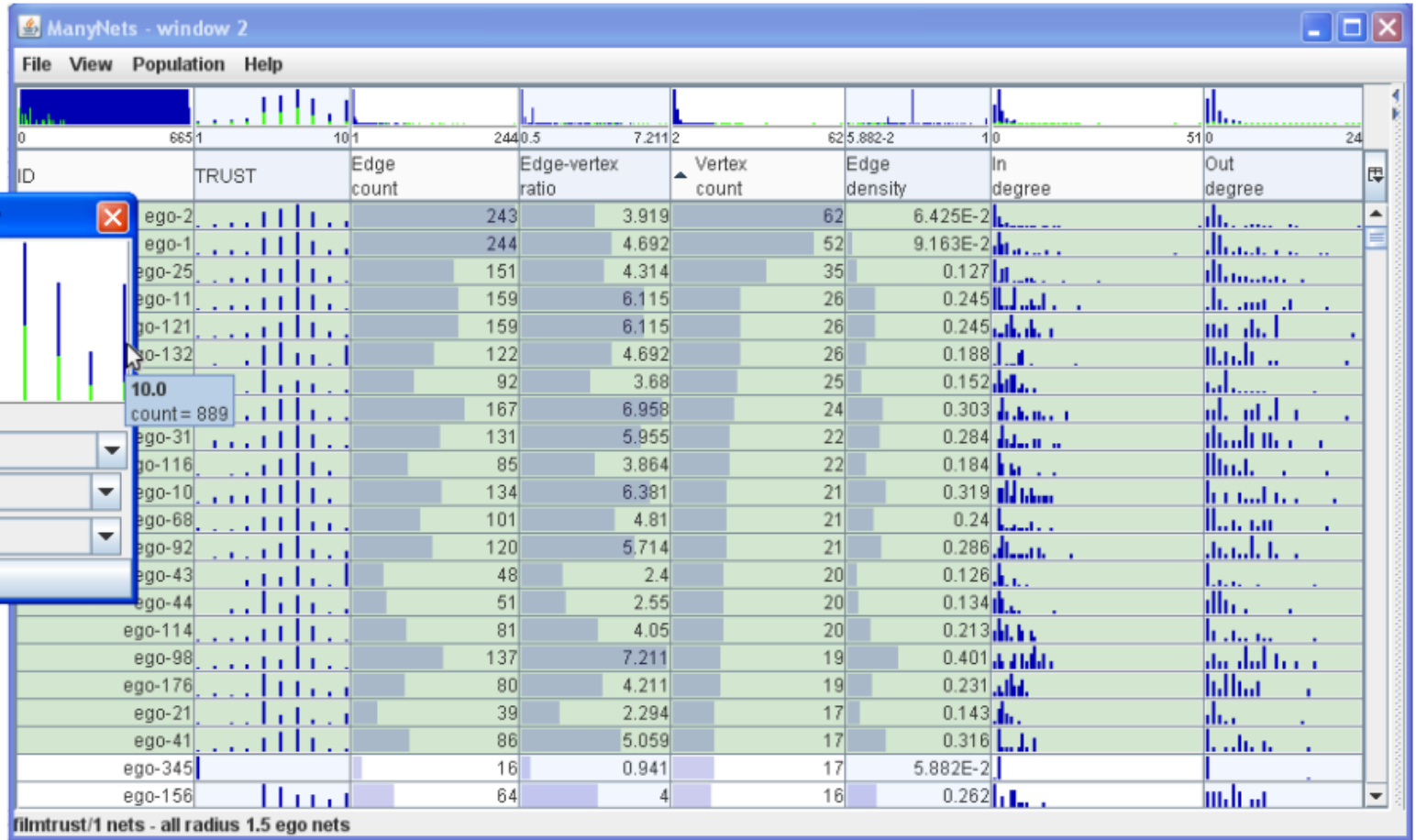
Network Comparison

Heterogeneous Networks

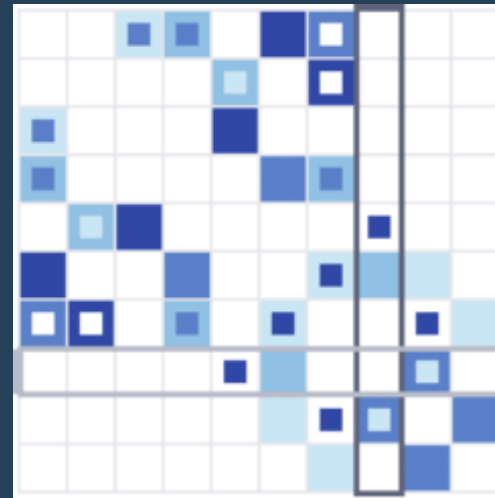
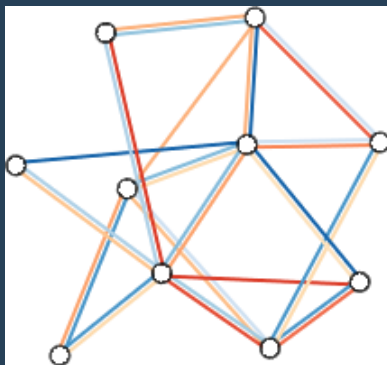
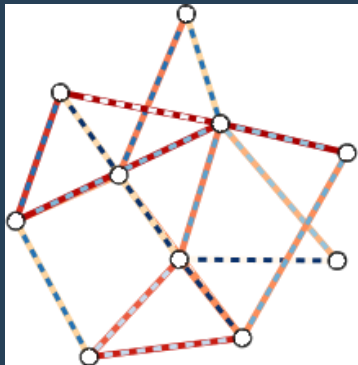
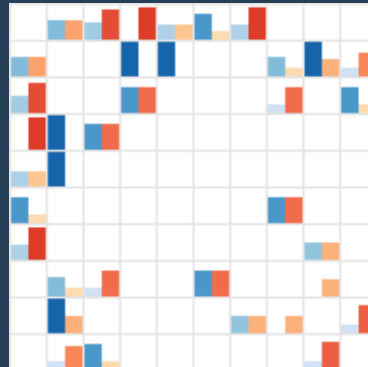
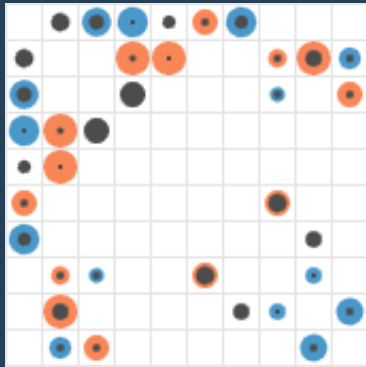
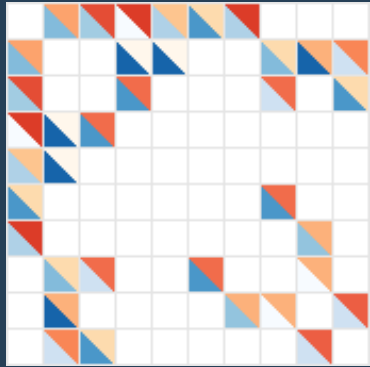
Dynamic Networks



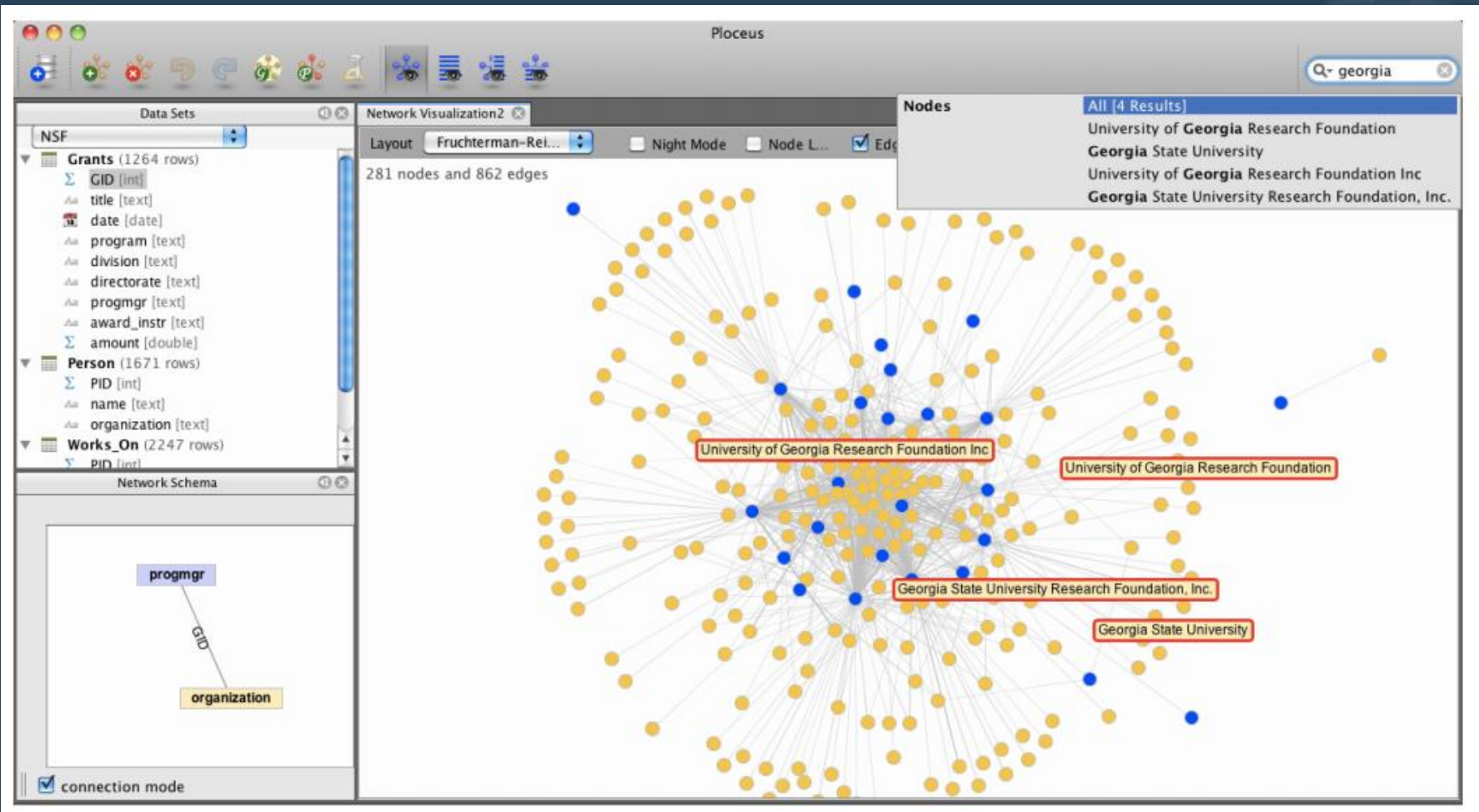
Comparing Networks



Comparing Weighted Networks

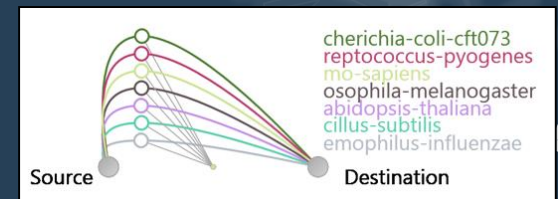
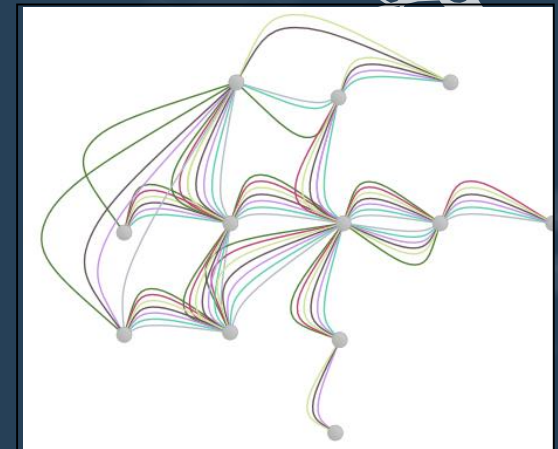


Heterogeneous Networks

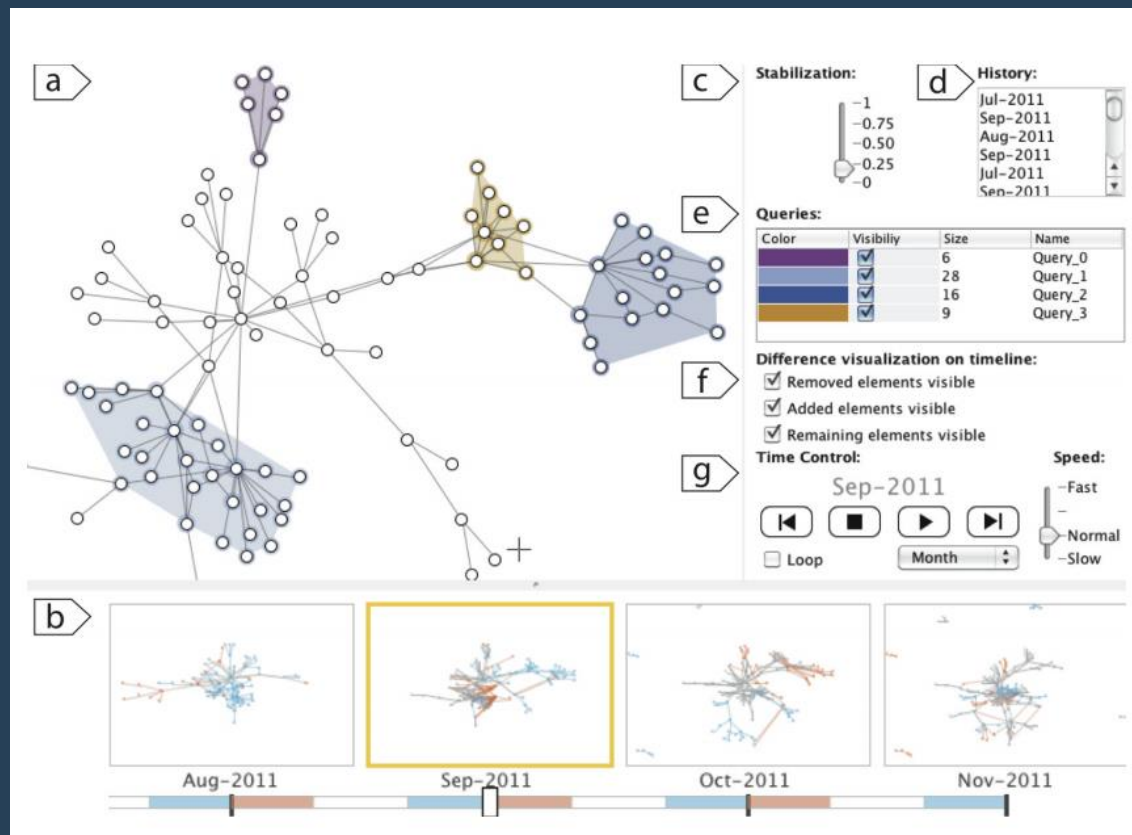


Heterogeneous Networks

Interactive Link Legends

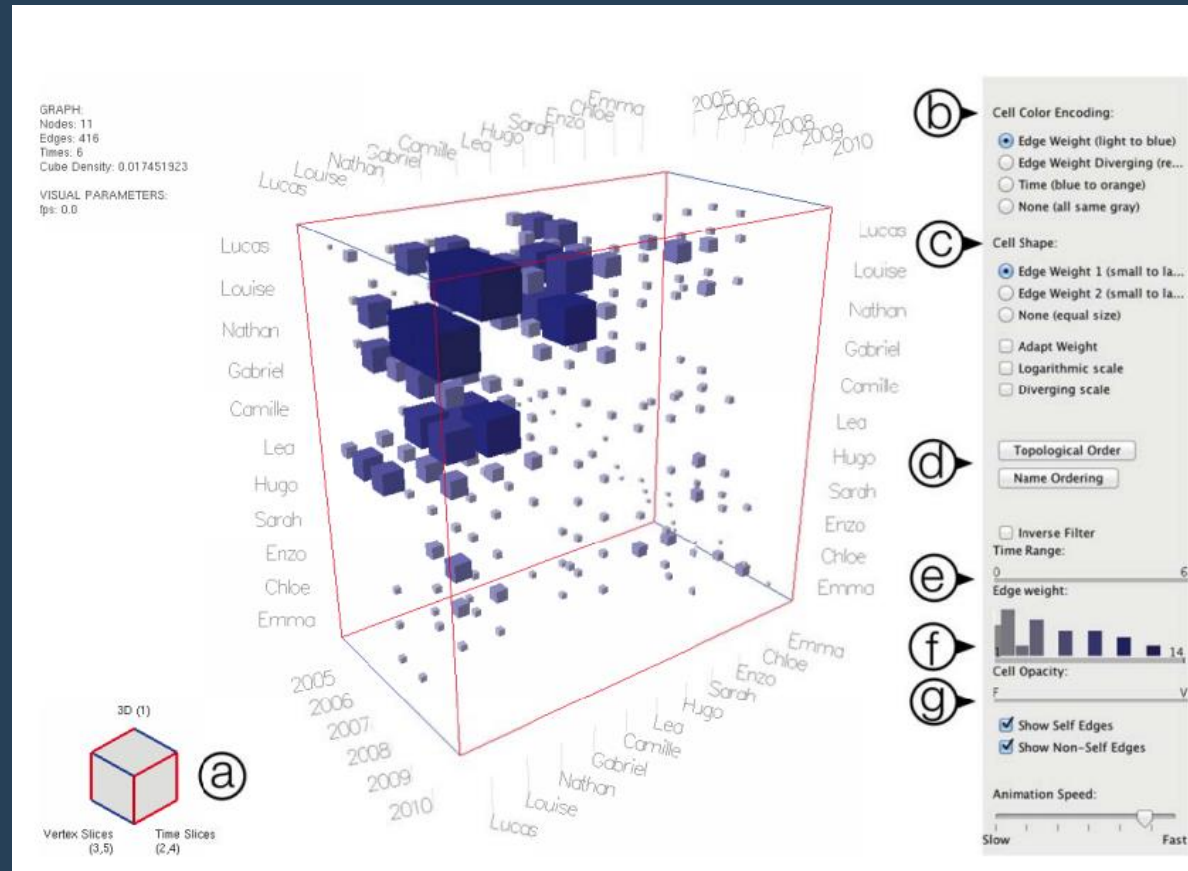


Dynamic graphs



Graph Diaries, *Bach et al.*, TVCG 2013

Dynamic graphs

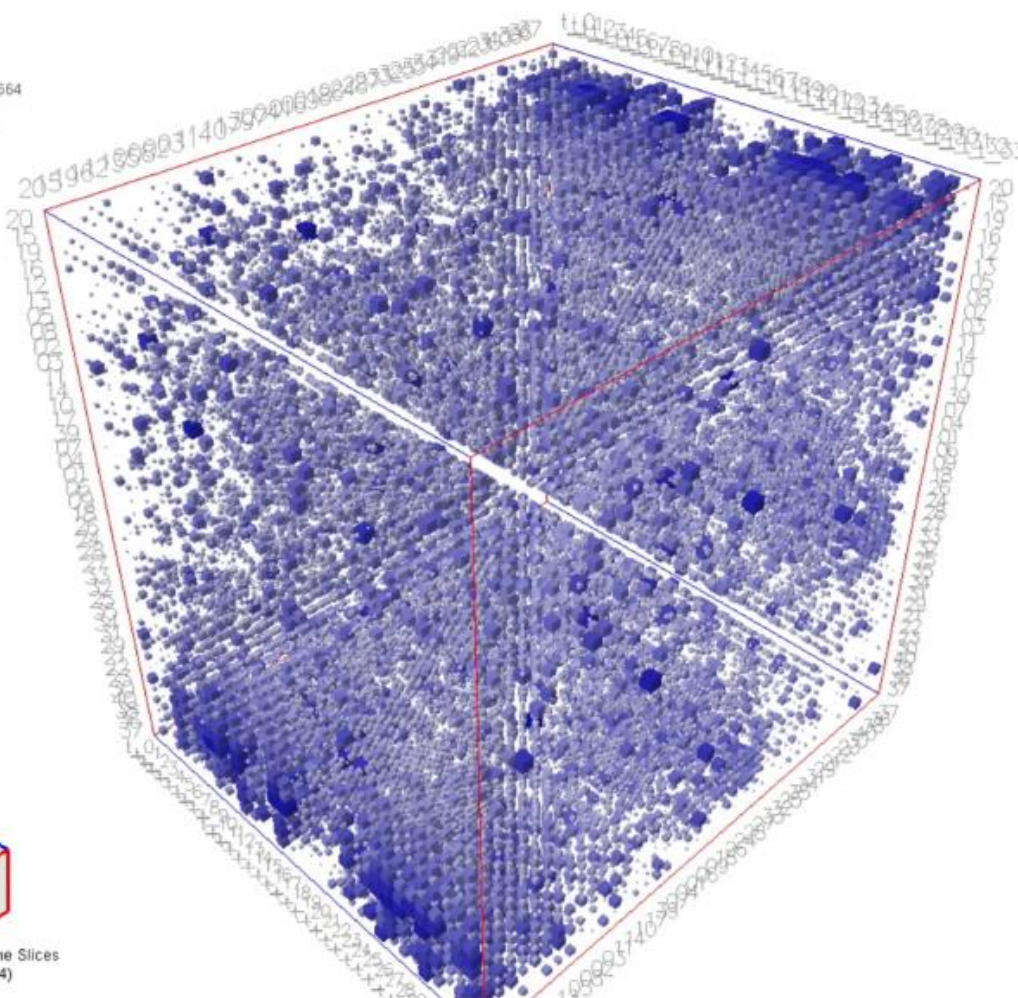


Cubix, *Bach et al.*, CHI 2014



GRAPH:
Nodes: 40
Edges: 57556
Times: 34
Cube Density: 0.009451664

VISUAL PARAMETERS:
fps: 0.0



Cell Color Encoding:

- ☒ Edge Weight (light to blue)
- ☐ Edge Weight Diverging (re...
- ☐ Time (blue to orange)
- ☐ None (all same gray)

Cell Shape:

- ☒ Edge Weight 1 (small to la...
- ☐ Edge Weight 2 (small to la...
- ☐ None (equal size)
- ☒ Adapt Weight
- ☐ Logarithmic scale
- ☐ Diverging scale

Topological Order

Name Ordering

☐ Inverse Filter

Time Range:

0 34

Edge weight:



Cell Opacity:

F V

☒ Show Self Edges

☒ Show Non-Self Edges

Animation Speed:

Slow Fast

3D (1)



Vertex Slices
(3,5)

Time Slices
(2,4)

Summary

Fast algorithms exists for tree visualizations

While most familiar representations, node-link diagrams have many issues

- Several can be fixed by interaction techniques
- Others require using different visualization paradigms, such as matrices

Graph visualization is still an active research topic!!