

Computer-Aided Reasoning for Software

CSSE507

Program Synthesis

Today

Last lecture

- Solvers as angelic runtime oracle

Today

- Program synthesis: from specs to code

Reminders

- HW3 is due on Friday.

The program synthesis problem

ϕ may be a formula, a reference implementation, input / output pairs, traces, demonstrations, etc.

Synthesis improves

- Productivity (when writing ϕ is easier than writing P).
- Correctness (when verifying ϕ is easier than verifying P).

$$\exists P. \forall x. \phi(x, P(x))$$

Find a program P that satisfies the specification ϕ on all inputs.

Two kinds of program synthesis

$$\exists P. \forall x. \phi(x, P(x))$$

SPIRAL

Deductive (classic) synthesis

Derive the program P from the constructive proof of the theorem $\forall x. \exists y. \phi(x, y)$.

FlashFill

Inductive (syntax-guided) synthesis

Discover the program P by searching a restricted space of candidate programs for one that satisfies ϕ on all inputs.

Deductive synthesis with axioms and E-graphs

Specification ϕ , given as a reference implementation.

`reg6 * 4 + 1`

1. Construct an E-graph.
2. Use a SAT solver to search the E-graph for a K-cycle program.

Denali Superoptimizer
[Joshi, Nelson,
Randall, PLDI'02]

Optimal (lowest cost) program P that is equivalent to ϕ on all inputs (values of `reg6`).

`s4addl(reg6, 1)`

$$\forall k, n. 2^n = 2^{**}n$$

$$\forall k, n. k * 2^n = k \ll n$$

$$\forall k, n. k * 4 + n = \text{s4addl}(k, n)$$

...

Two kinds of axioms:

- Instruction semantics.
- Algebraic properties of functions and relations used for specifying instruction semantics.

Denali by example

reg6 * 4 + 1

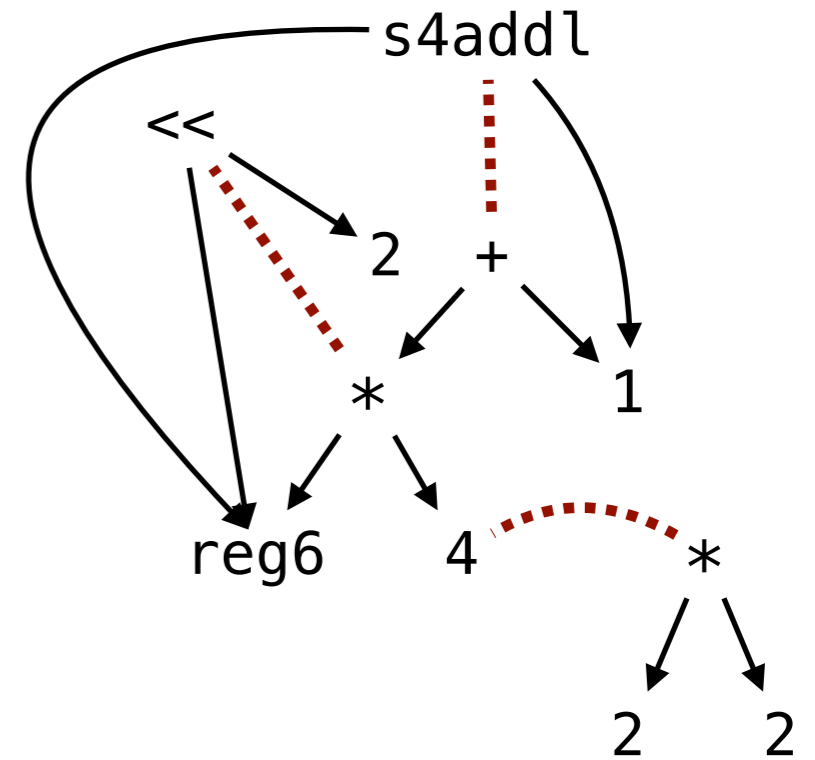
$\forall k, n. 2^n = 2^{**}n$

$\forall k, n. k * 2^n = k \ll n$

$\forall k, n. k * 4 + n = \mathbf{s4add1}(k, n)$

...

E-graph matching



s4add1(reg6, 1)

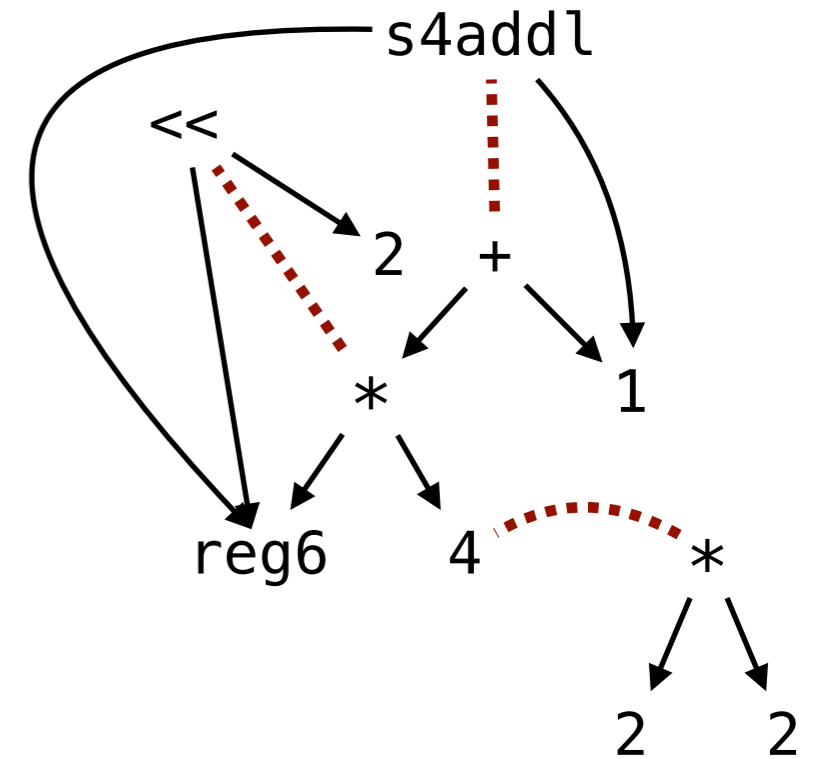
Deductive synthesis versus compilation

Deductive synthesizer

- Non-deterministic.
- Searches *all correct rewrites* for one that is optimal.

Compiler

- Deterministic.
- Lowers a source program into a target program using a *fixed sequence of rewrite steps*.



reg6 * 4 + 1
↓
reg6 << 2 + 1

Deductive synthesis versus inductive synthesis

$$\exists P. \forall x. \phi(x, P(x))$$

Deductive synthesis

- Efficient and provably correct: thanks to the semantics-preserving rules, only correct programs are explored.
- Requires *sufficient axiomatization* of the domain.
- Requires *complete* specifications to seed the derivation.

Inductive synthesis

- Works with *multi-modal and partial* specifications.
- Requires *no axioms*.
- But often at the cost of *lower efficiency* and *weaker (bounded) guarantees* on the correctness/optimalty of synthesized code.

Inductive syntax-guided synthesis

A partial or multimodal specification ϕ of the desired program (e.g., assertions, i/o pairs).

reg6 * 4 + 1

Guess a program that works on a finite set of inputs, verify it, and learn from bad guesses.

CEGIS:
Counterexample-Guided
Inductive Synthesis
[Solar-Lezama et al,
ASPLOS'06]

A program P from the given space of candidates that satisfies ϕ on all (usually bounded) inputs.

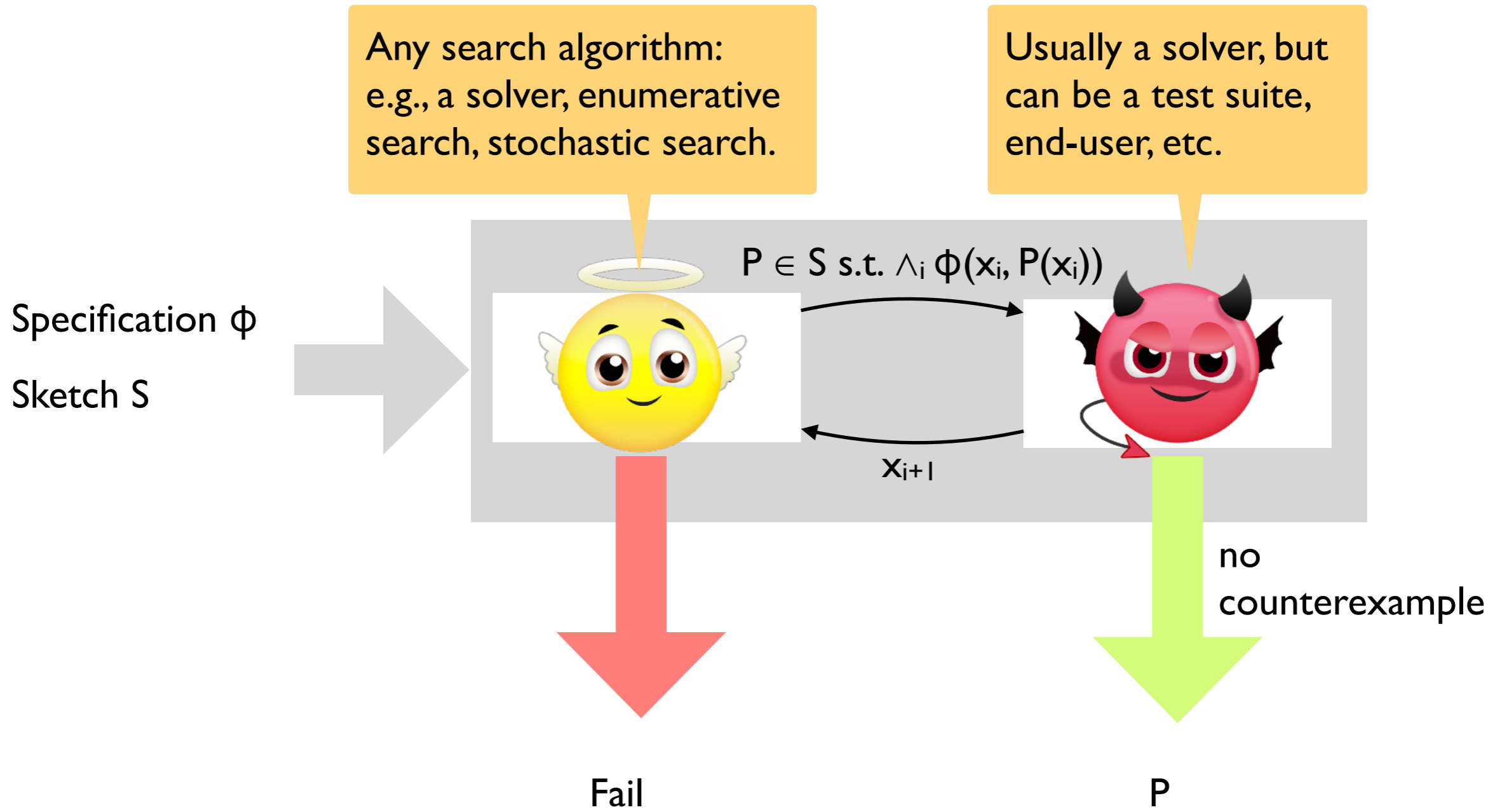
s4addl(reg6, 1)

```
expr ::=  
  const | reg6 |  
  s4addl(expr, expr) |  
  ...
```

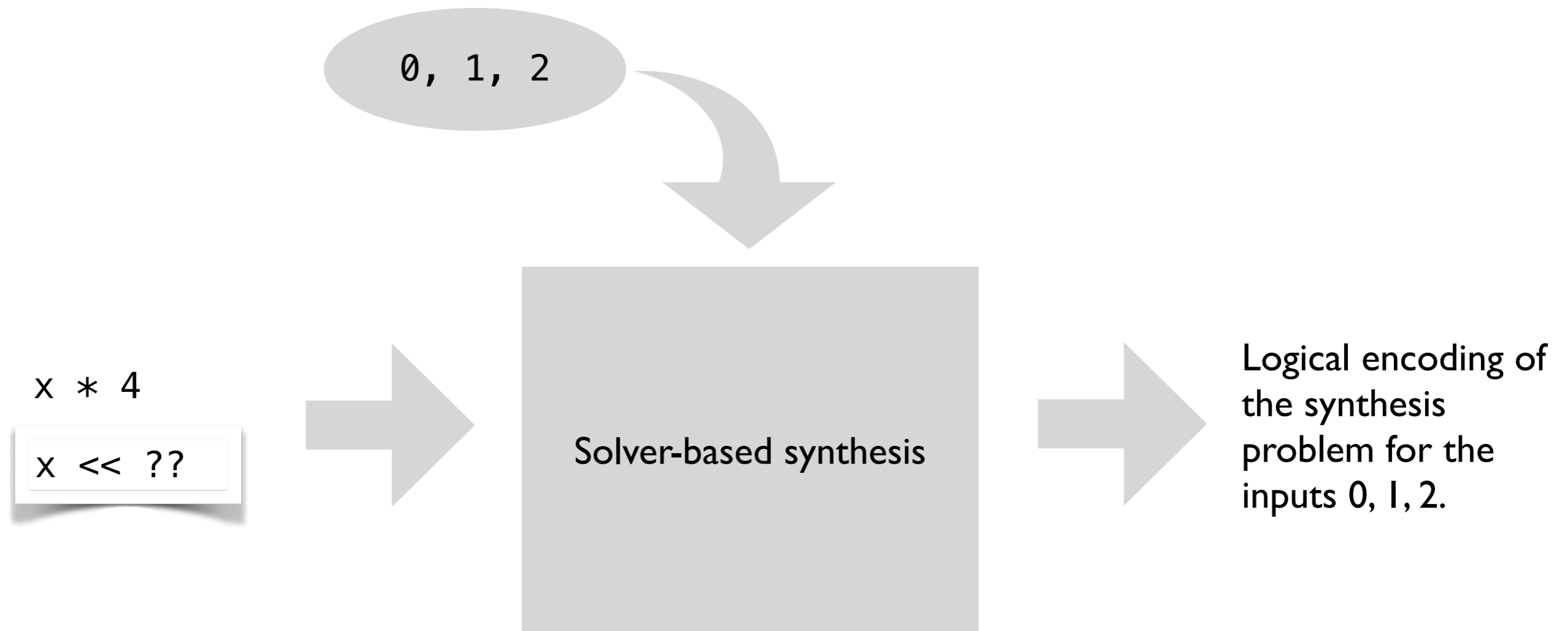
A syntactic *sketch* (e.g., a grammar) describing the shape of the desired program P.

This defines the space of candidate programs to search. Can be fine-tuned for better performance.

Overview of CEGIS

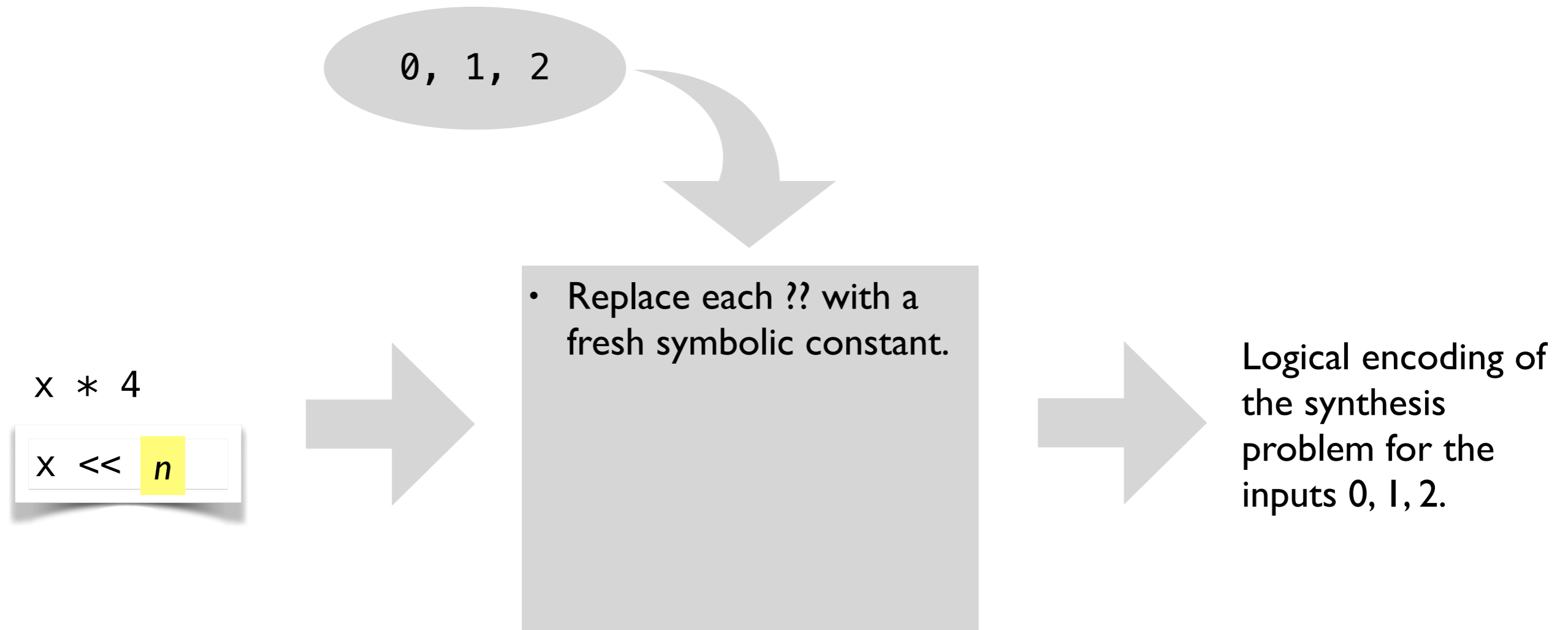


Synthesizing programs with a solver



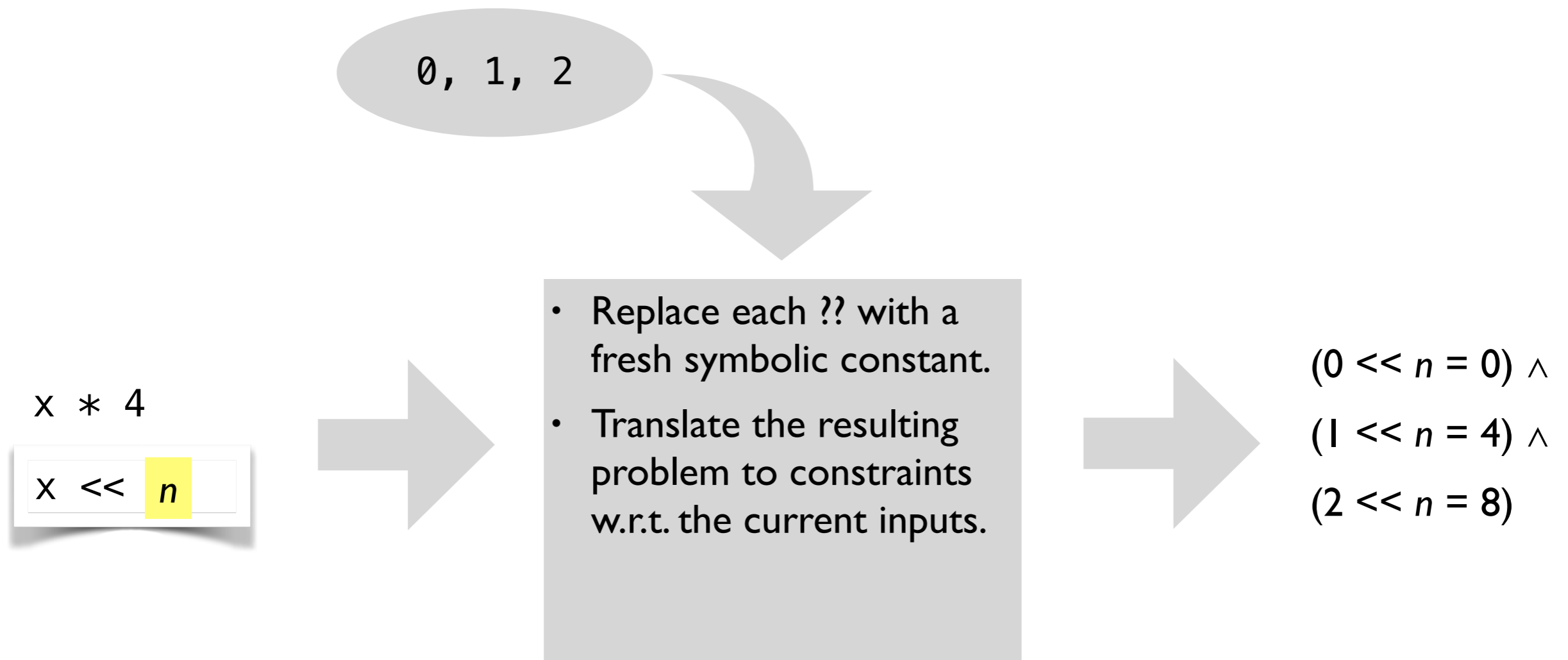
[Solar-Lezama et al, ASPLOS'06]

Synthesizing programs with a solver



[Solar-Lezama et al, ASPLOS'06]

Synthesizing programs with a solver



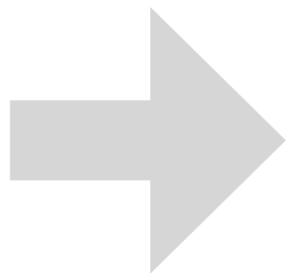
[Solar-Lezama et al, ASPLOS'06]

Synthesizing programs with a solver

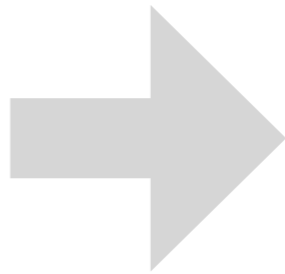
0, 1, 2



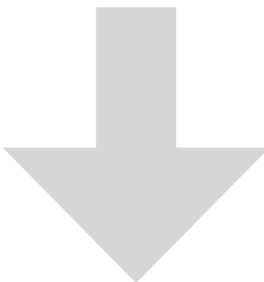
```
x * 4  
x << n
```



- Replace each ?? with a fresh symbolic constant.
- Translate the resulting problem to constraints w.r.t. the current inputs.
- If SAT, convert the model to a program P.



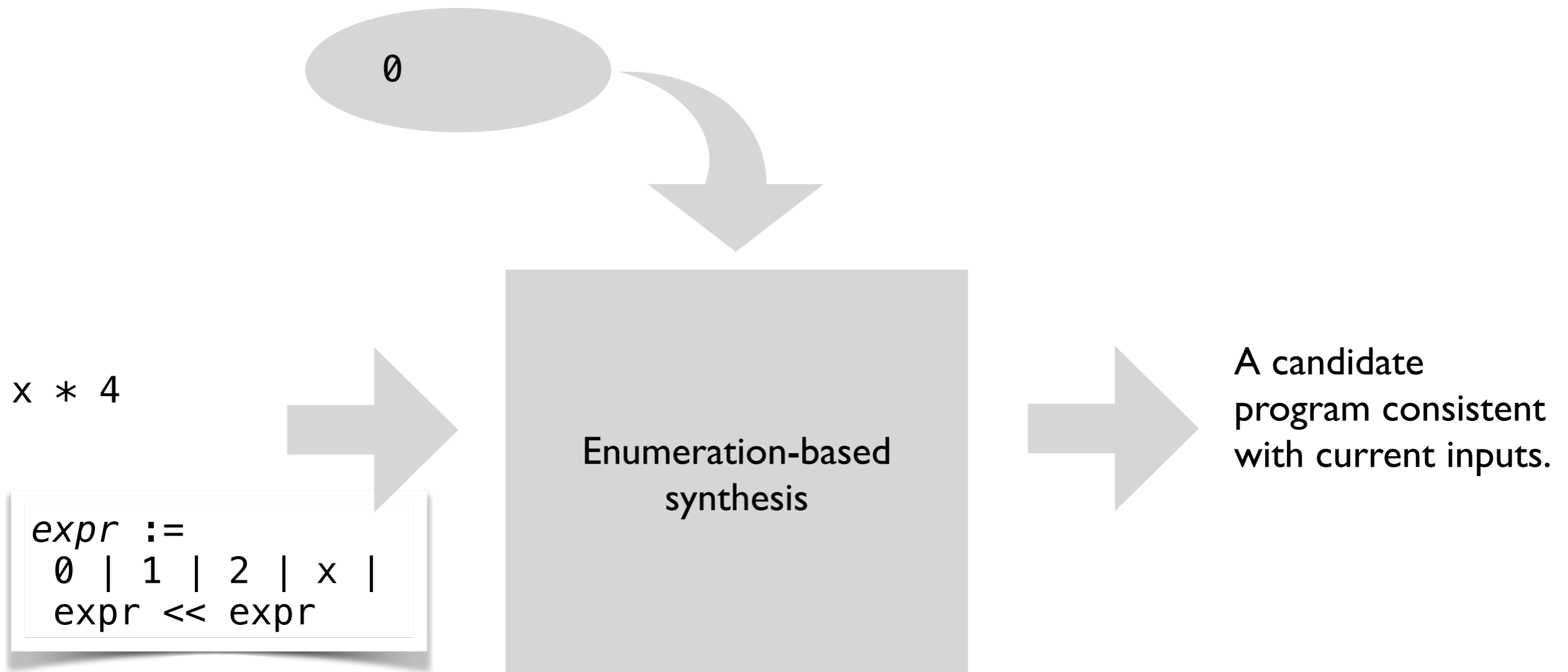
$(0 \ll n = 0) \wedge$
 $(1 \ll n = 4) \wedge$
 $(2 \ll n = 8)$



```
x << 2
```

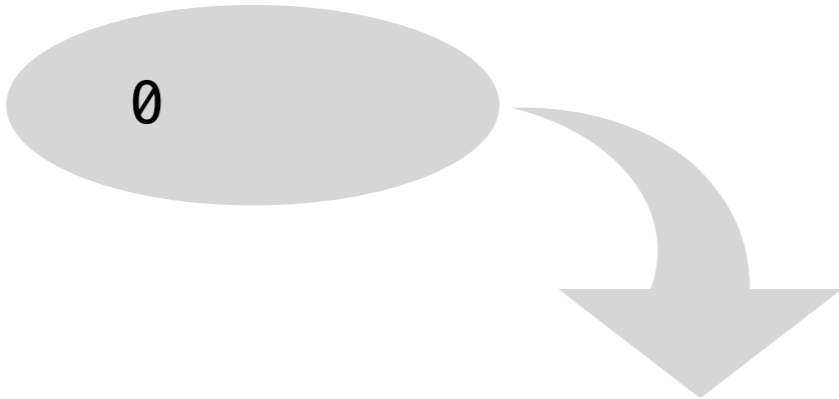
[Solar-Lezama et al, ASPLOS'06]

Synthesizing programs with enumerative search



[Udupa et al, PLDI'13]

Synthesizing programs with enumerative search

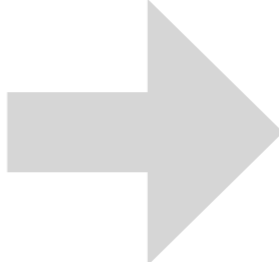


$x * 4$



```
expr ::=  
0 | 1 | 2 | x |  
expr << expr
```

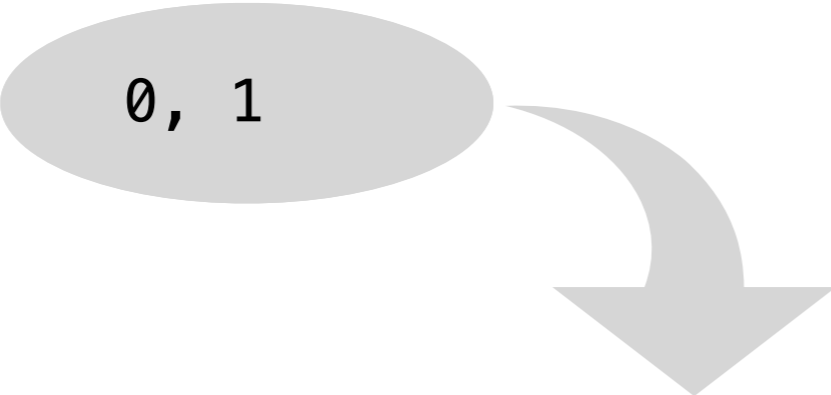
- Iteratively construct all programs of size K until one is consistent with the current inputs.
- If two programs produce the same output on all current inputs, keep just one of the two.



A candidate program consistent with current inputs.

[Udupa et al, PLDI'13]

Synthesizing programs with enumerative search

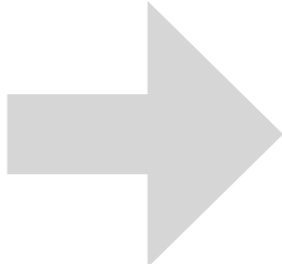


$x * 4$



```
expr ::=  
0 | 1 | 2 | x |  
expr << expr
```

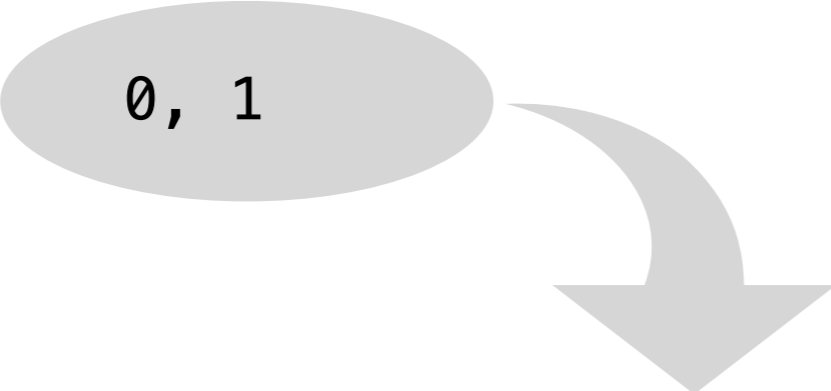
- Iteratively construct all programs of size K until one is consistent with the current inputs.
- If two programs produce the same output on all current inputs, keep just one of the two.



$K=1: 0$

[Udupa et al, PLDI'13]

Synthesizing programs with enumerative search

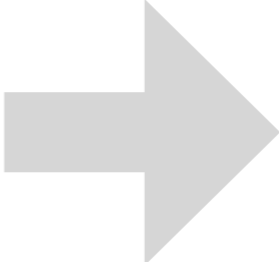


$x * 4$



```
expr ::=  
0 | 1 | 2 | x |  
expr << expr
```

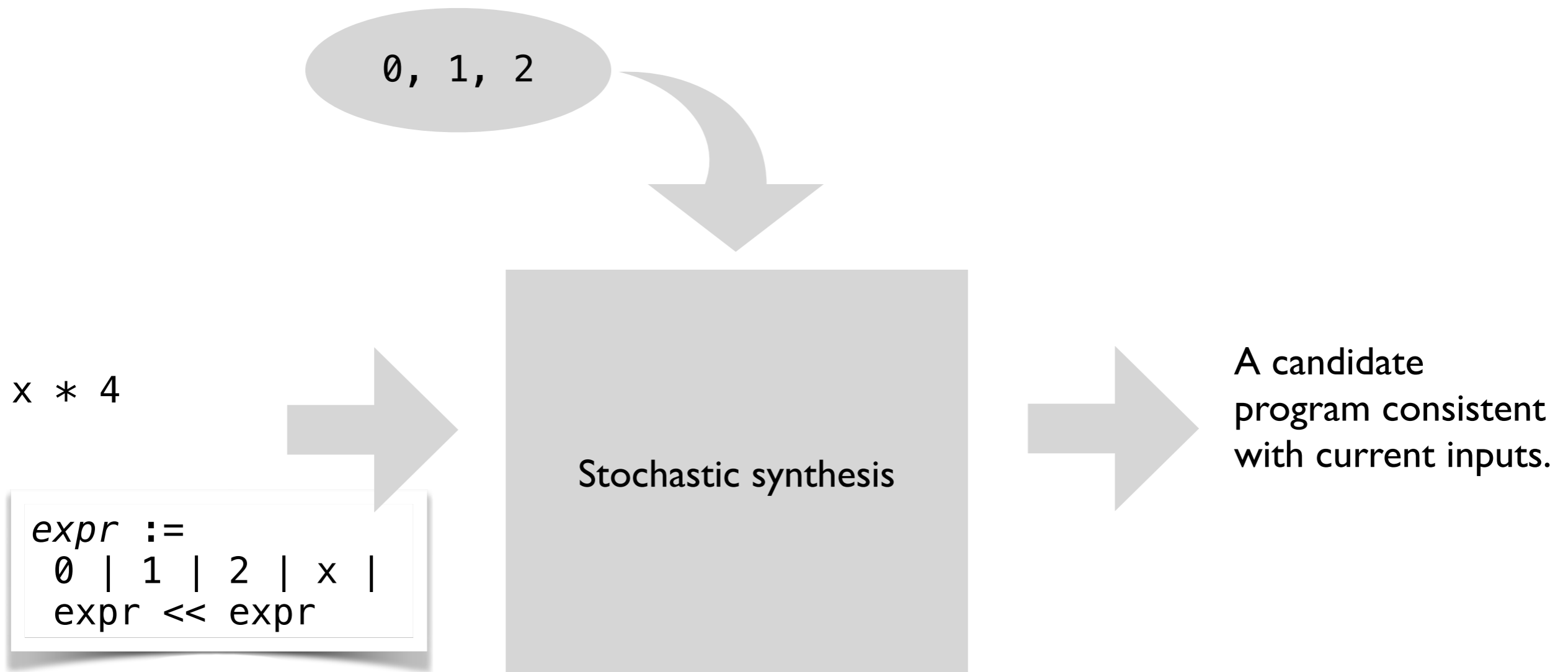
- Iteratively construct all programs of size K until one is consistent with the current inputs.
- If two programs produce the same output on all current inputs, keep just one of the two.



$K=1: 0, 1, 2, x$
 $K=2: 1 \ll 2, 2 \ll 2,$
 $x \ll 1, x \ll 2$

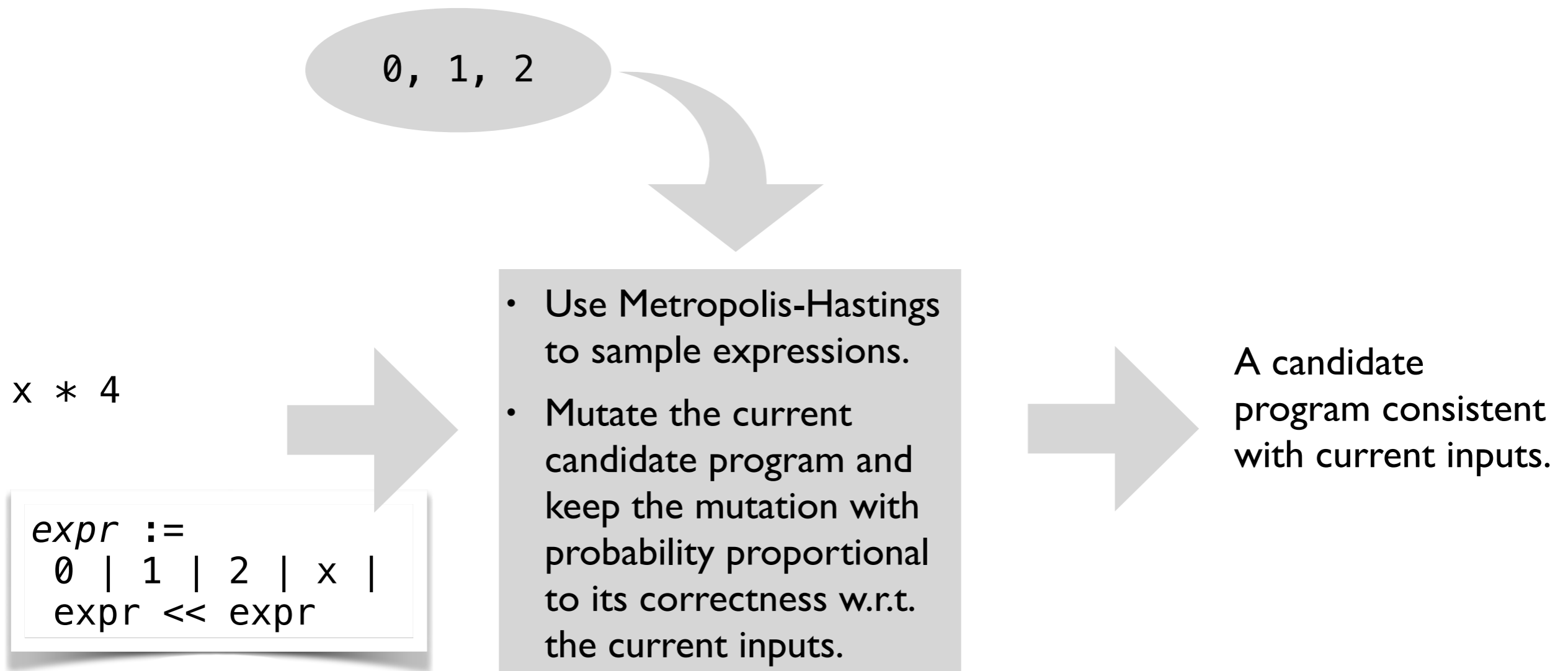
[Udupa et al, PLDI'13]

Synthesizing programs with stochastic search



[Schkufza et al, ASPLOS'13]

Synthesizing programs with stochastic search



[Schkufza et al, ASPLOS'13]

Summary

Today

- Deductive and inductive synthesis
- Syntax-guided synthesis with symbolic, enumerative, and stochastic search

Next

- Two exciting guest lectures!
- Program verification in the real world.