Computer-Aided Reasoning for Software

Symbolic Execution

Today

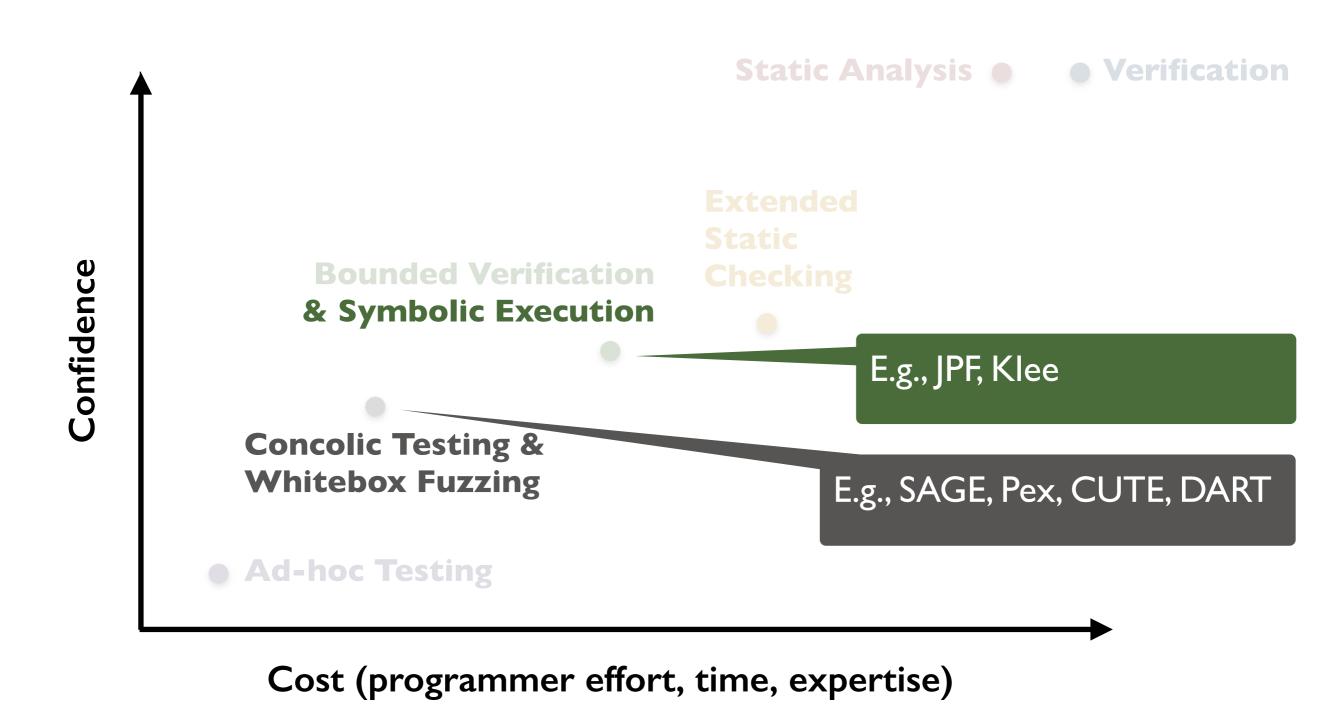
Last lecture

Verification with Dafny

Today

- Symbolic execution: strongest postconditions for finite programs
- Concolic testing

The spectrum of program validation tools



A brief history of symbolic execution

1976: A system to generate test data and symbolically execute programs (Lori Clarke)

1976: Symbolic execution and program testing (James King)

2005-present: practical symbolic execution

- Using SMT solvers
- Heuristics to control exponential explosion
- Heap modeling and reasoning about pointers
- Environment modeling
- Dealing with solver limitations

Symbolic execution: basic idea

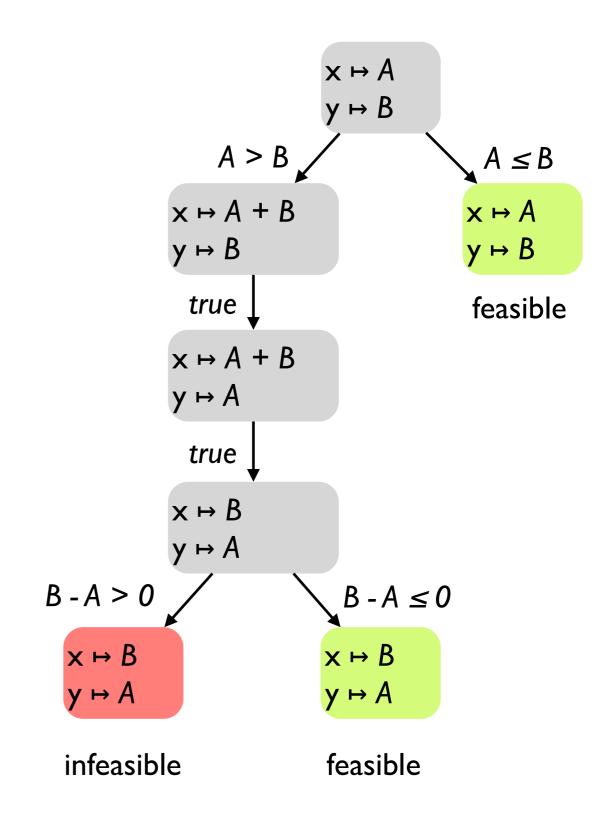
```
def f (x, y):
    if (x > y):
        x = x + y
        y = x - y
        x = x - y
        if (x - y > 0):
        assert false
    return (x, y)
```

Execute the program on symbolic values.

Symbolic state maps variables to symbolic values.

Path condition is a quantifier-free formula over the symbolic inputs that encodes all branch decisions taken so far.

All paths in the program form its execution tree, in which some paths are feasible and some are infeasible.



Symbolic execution: practical issues

Loops and recursion: infinite execution trees

Path explosion: exponentially many paths

Heap modeling: symbolic data structures and pointers

Solver limitations: dealing with complex PCs

Environment modeling: dealing with native / system / library calls

Loops and recursion

Dealing with infinite execution trees:

Finitize paths by unrolling loops and recursion (bounded verification)

init;

- Finitize paths by limiting the size of PCs (bounded verification)
- Use loop invariants (verification)

```
assert I;
init;
while (C) {
    B;
}
assert P;

I

assume I;
if (C) {
    B;
    assert I;
    assume false;
}
assert P;
```

Path explosion

Achieving good coverage in the presence of exponentially many paths:

- Select next branch at random
- Select next branch based on coverage
- Interleave symbolic execution with random testing



Heap modeling

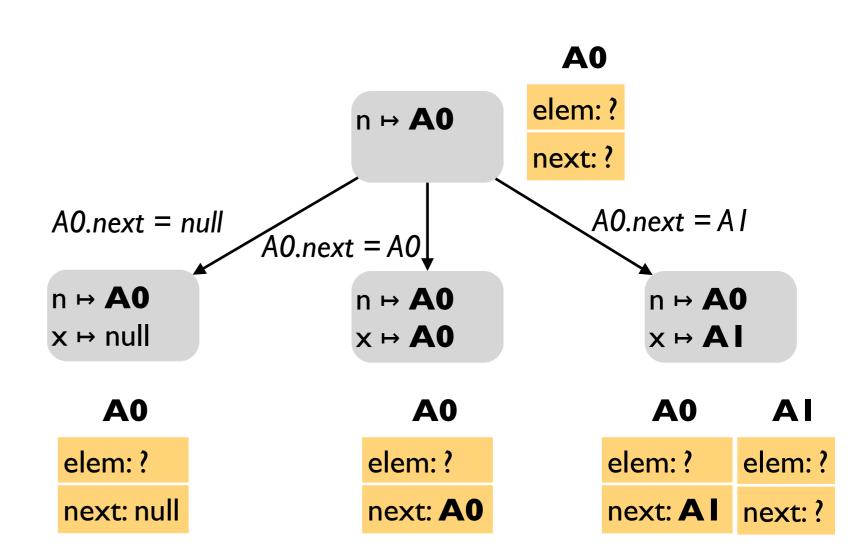
Modeling symbolic heap values and pointers

- Bit-precise memory modeling with the theory of arrays (EXE, Klee, SAGE)
- Lazy concretization (JPF)
- Concolic lazy concretization (CUTE)

Heap modeling: lazy concretization

```
class Node {
   int elem;
   Node next;
}

n = symbolic(Node);
x = n.next;
```



Heap modeling: concolic testing

```
typedef struct cell {
  int ∨;
  struct cell *next;
} cell;
int f(int v) {
  return 2*v + 1;
int testme(cell *p, int x) {
  if (x > 0)
    if (p != NULL)
      if (f(x) == p->v)
        if (p->next == p)
          assert false;
  return 0;
```

```
Concrete
                                              PC
                  p → null
                                       x > 0 \land p=null
                 x → 236
   A0
next: null
                 p → A0
                                       x > 0 \land p \neq null \land
                 x → 236
v: 634
                                       p.v \neq 2x + 1
   A<sub>0</sub>
                                       x > 0 \land p \neq null \land
next: null
                 p → A0
                                       p.v = 2x + 1 \wedge
                 X \mapsto
v: 3
                                       p.next ≠ p
   A0
                                       x > 0 \land p \neq null \land
next: A0
                 p → A0
                                       p.v = 2x + 1 \wedge
                  X \mapsto I
v: 3
                                       p.next = p
```

Execute concretely and symbolically. Negate last decision and solve for new inputs.

Solver limitations

Reducing the demands on the solver:

- On-the-fly expression simplification
- Incremental solving
- Solution caching
- Substituting concrete values for symbolic in complex PCs (CUTE)

Environment modeling

Dealing with system / native / library calls:

- Partial state concretization
- Manual models of the environment (Klee)

Summary

Today

Practical symbolic execution and concolic testing

Next lecture

Angelic execution