

Computer-Aided Reasoning for Software

CSLE507

Solver-Aided Programming I

Topics

What is this course about?

Course logistics

Getting started with solver-aided programming!

about

Tools for building better software, more easily

**more reliable,
efficient, secure**

Tools for building better software, more easily

Tools for building **better software**, more easily

**automated verification and
synthesis based on
satisfiability solvers**

“solver-aided tools”

biology

systems

security

education

**By the end of this course, you'll be able to
build solver-aided tools for any domain!**

hardware

networking

databases

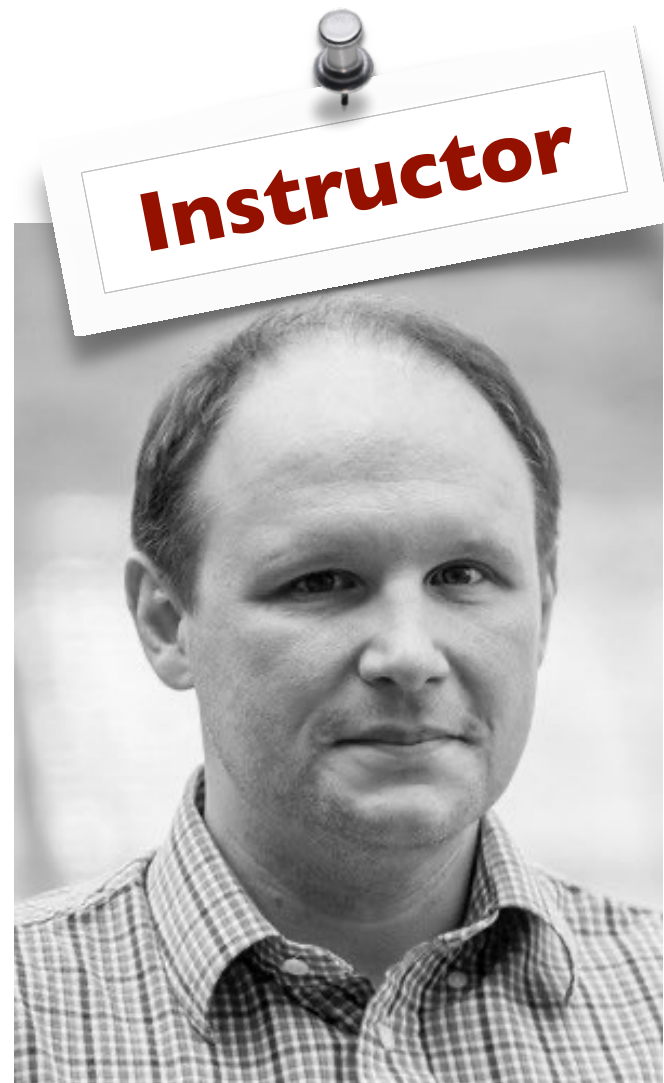
low-power computing

high-performance computing

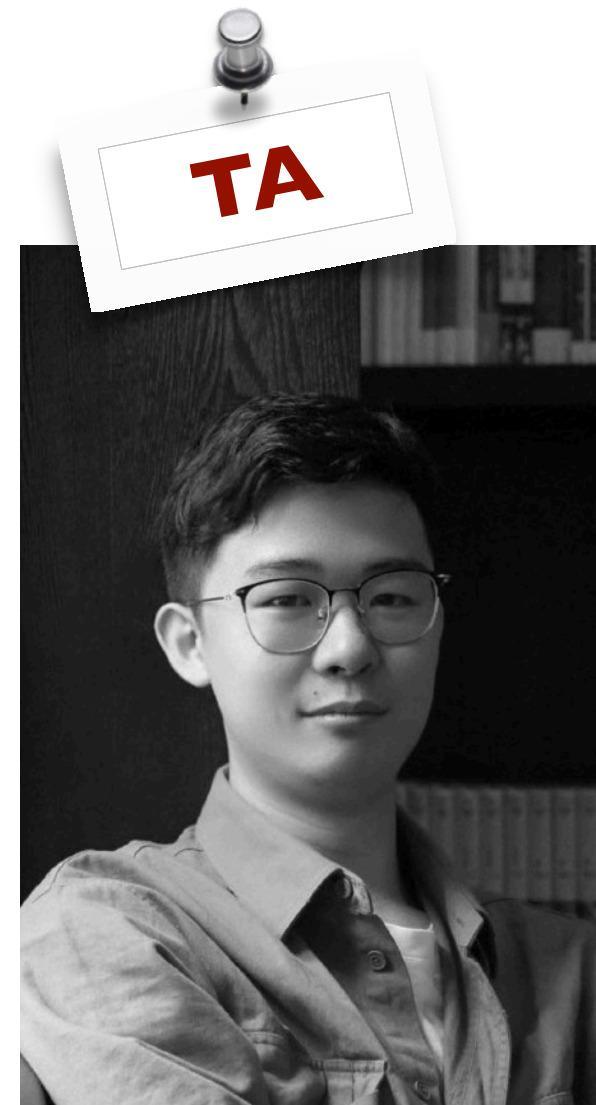
Logistics

Topics, structure, people

People



Zachary Tatlock
PLSE
CSE 201



Sirui Lu
PLSE
OHTBD

People

Instructor



Zachary Tatlock
PLSE
CSE 201

TA



Sirui Lu
PLSE
OHTBD

Students!

Your name
Research area

People

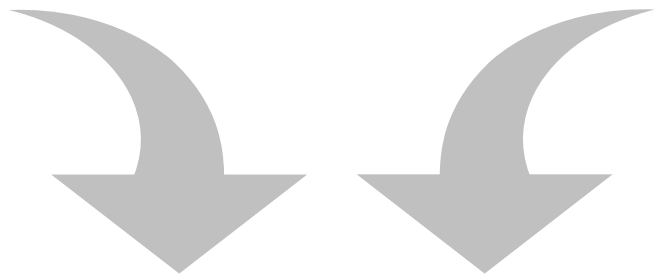


Emina Torlak

PLSE → AWS

Course overview

program question



tool

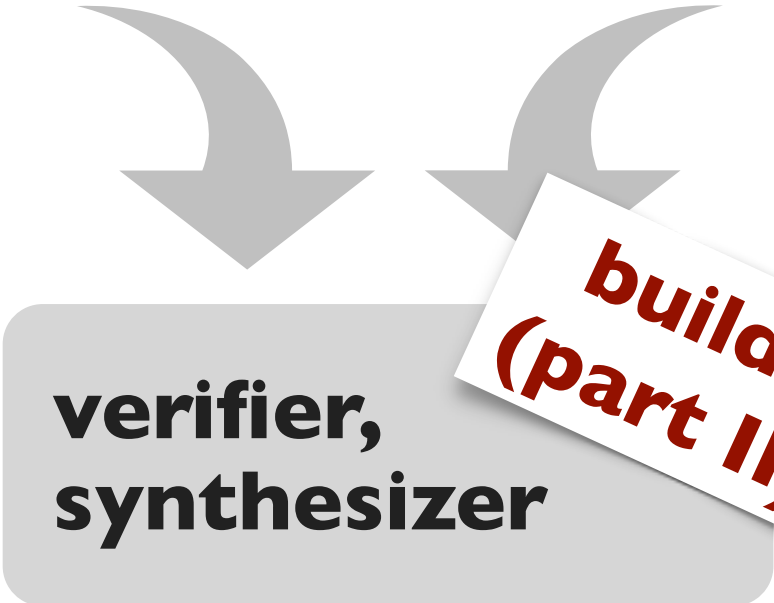
logic



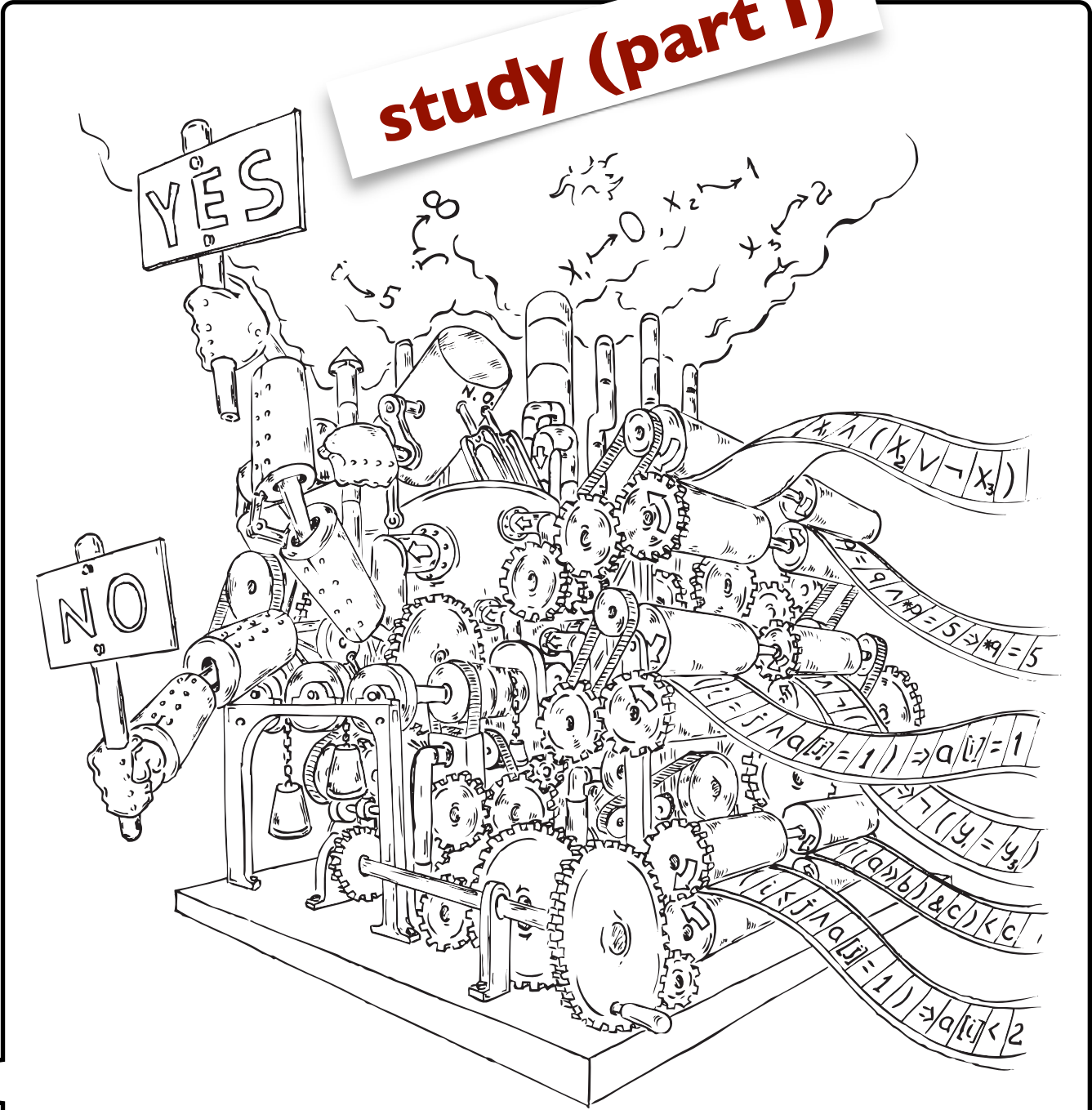
**automated
reasoning
engine**

Course overview

program question



logic



Drawing from "Decision Procedures" by Kroening & Strichman

Grading

3 homework assignments (75%)

- conceptual problems & proofs (TeX)
- implementations (Racket, Dafny, Alloy)
- completed with a partner (“whiteboard discussion” w/ others OK)

study (part I)

Course project (25%)

- build a computer-aided reasoning tool for a domain of your choice
- teams of 2-3 people
- see the course web page for timeline, deliverables and other details

**build!
(part II)**

Reading and references

Recommended readings posted on the course web page

- Complete each reading before the lecture for which it is assigned
- If multiple papers are listed, only the first is required reading

Recommended text books

- Bradley & Manna, [The Calculus of Computation](#)
- Kroening & Strichman, [Decision Procedures](#)

Advice for doing well in 507

Come to class (prepared)

- Lecture slides are enough to teach from, but not enough to learn from

Participate

- Ask and answer questions

Meet deadlines

- Turn homework in on time
- Start homework and project sooner than you think you need to
- Follow instructions for submitting code (we have to be able to run it)
- No proof should be longer than a page (most are ~1 paragraph)

A programming model that integrates solvers into the language, providing constructs for program verification, synthesis, and more.



Solver-aided programming in two parts:
(1) getting started and (2) going pro

How to use a solver-aided language: the workflow, constructs, and gotchas.

How to build your own solver-aided tool via direct symbolic evaluation or language embedding.

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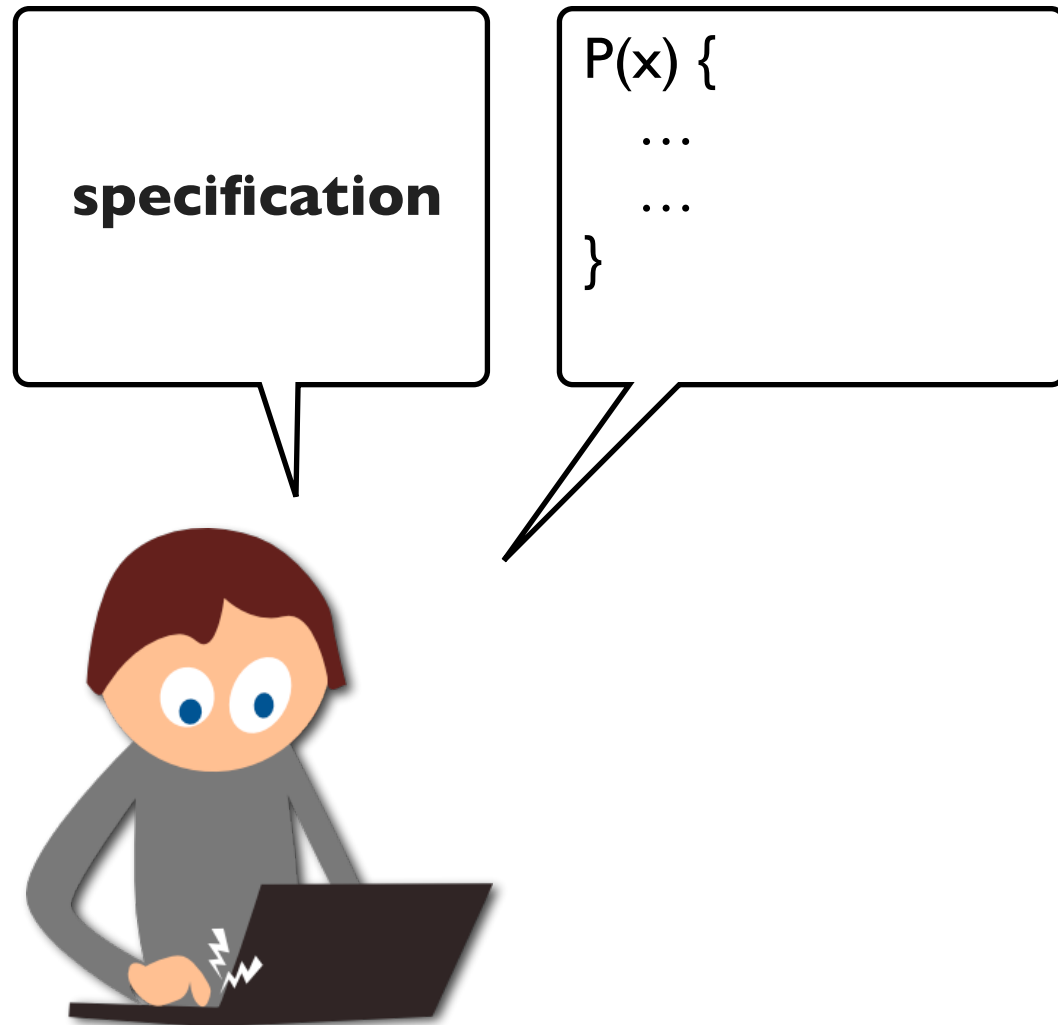
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Solver-aided programming in two parts: (1) **getting started** and (2) going pro

How to use a solver-aided language: the **workflow**, constructs and gotchas.

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Classic programming: from spec to code



Classic programming: test behaviors

test some behaviors against the specification

```
P(x) {  
  ...  
  ...  
}  
assert safe(2, P(2))
```



Solver-aided programming: *query* behaviors

query all behaviors against the specification

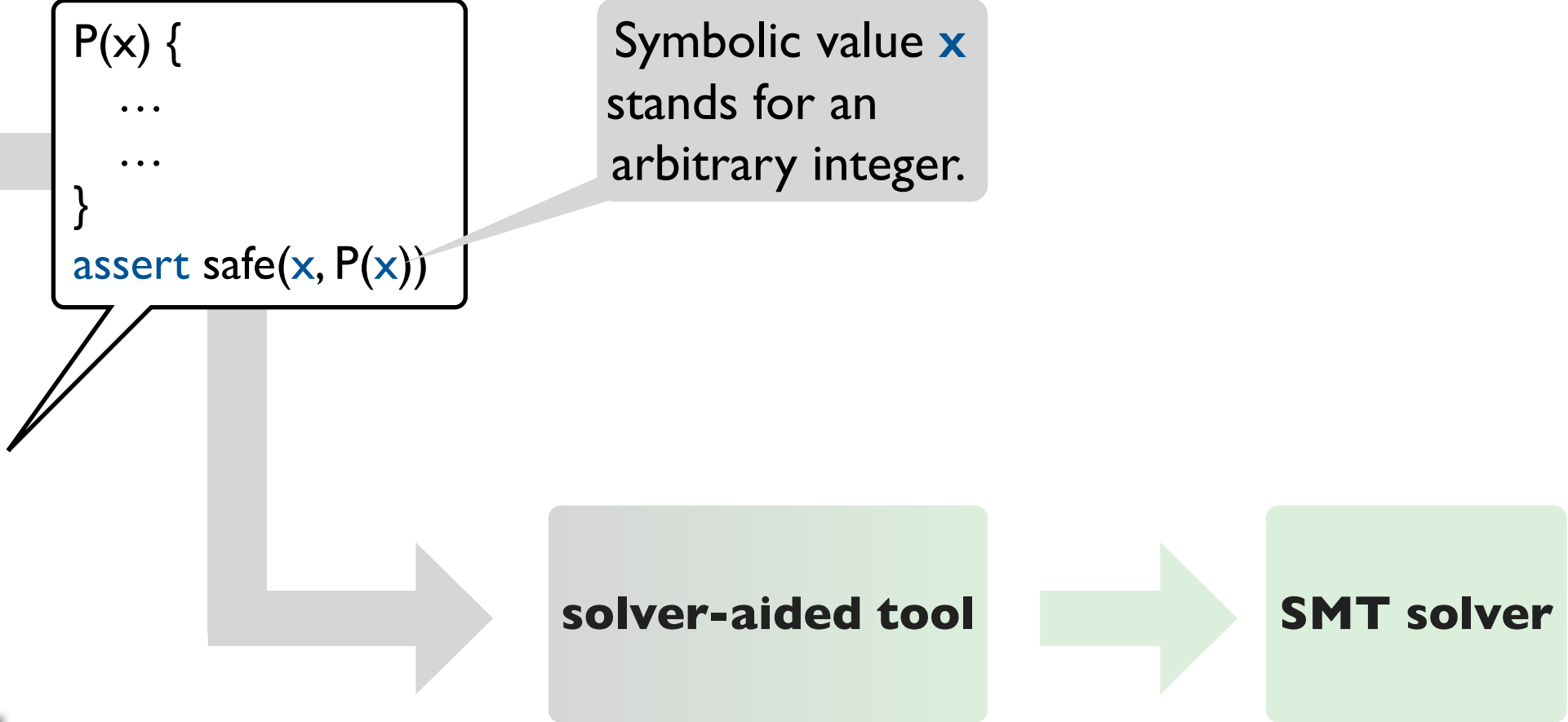
```
P(x) {  
  ...  
  ...  
}  
assert safe(x, P(x))
```

Symbolic value **x** stands for an arbitrary integer.

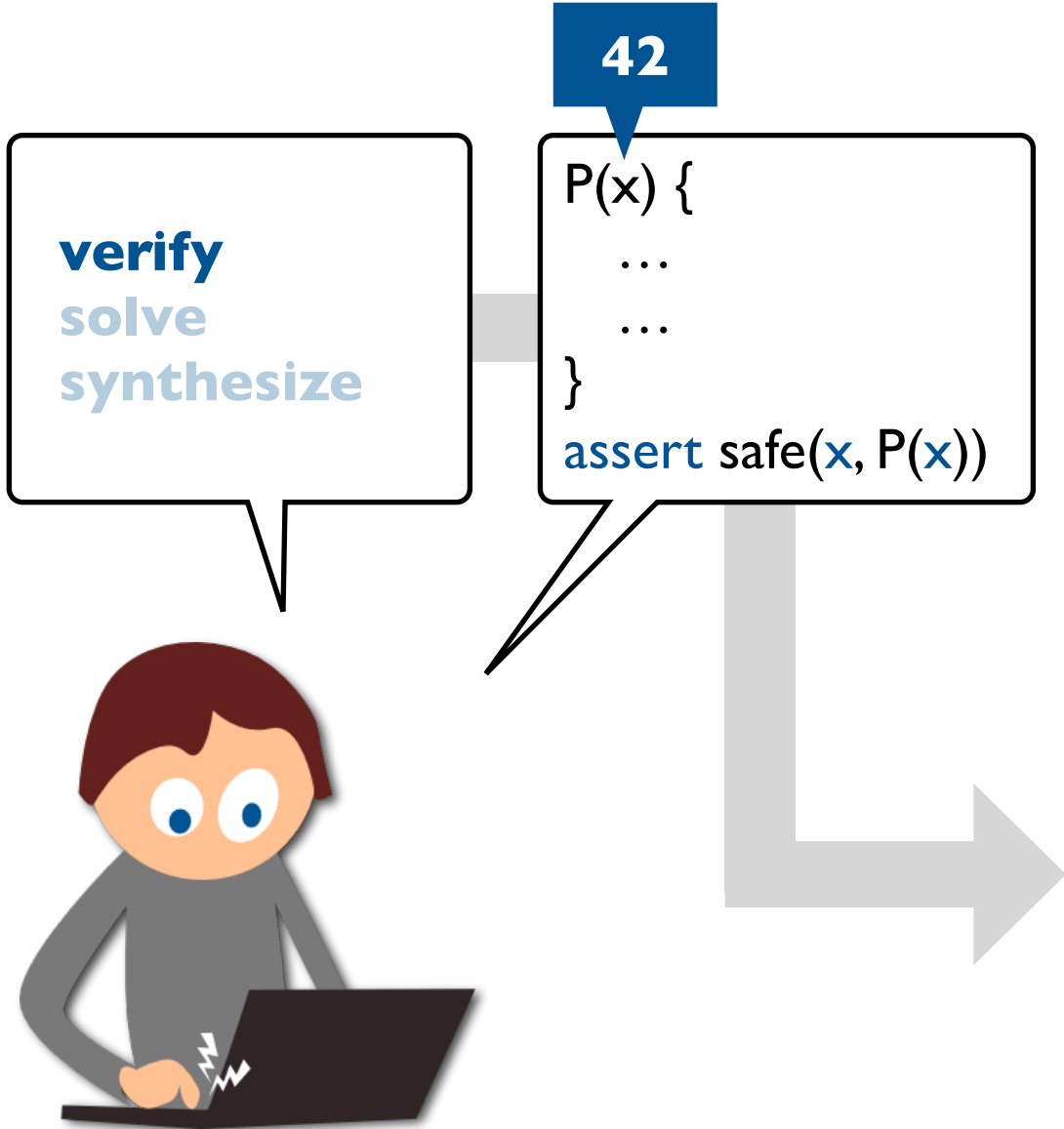


solver-aided tool

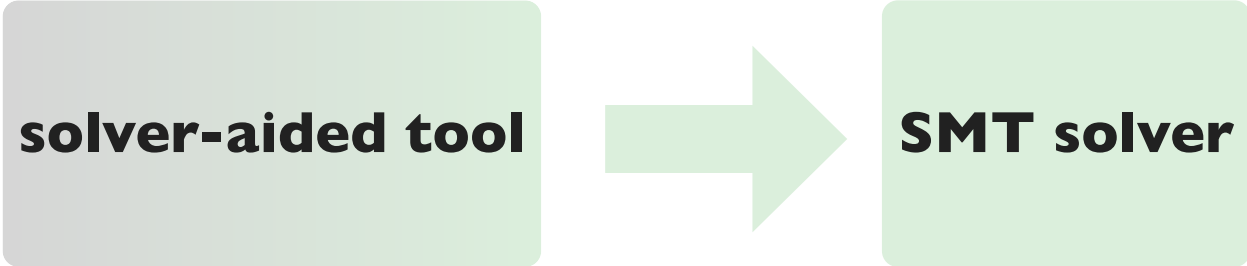
SMT solver



Solver-aided programming: verify

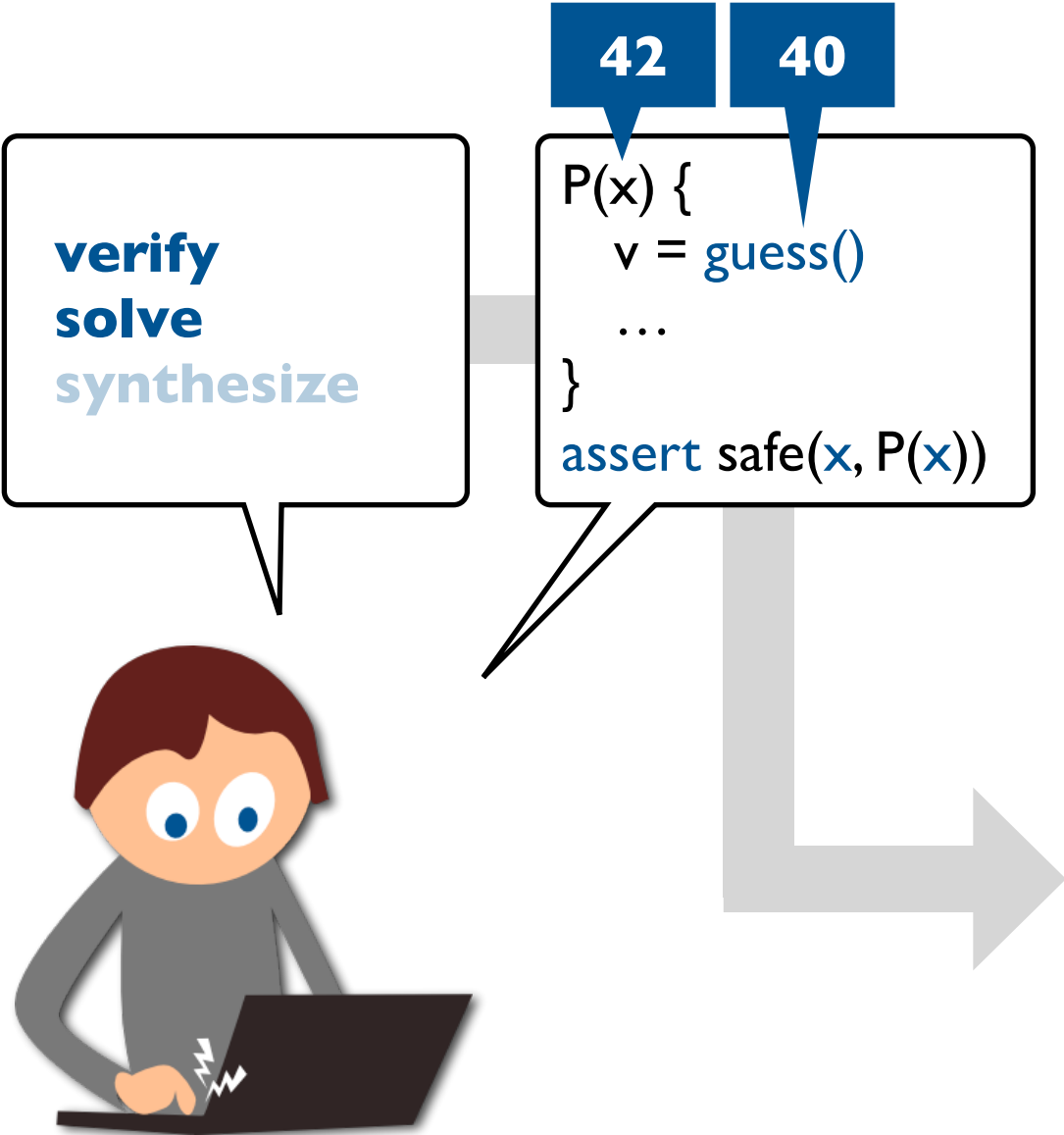


Find an input on which the program fails.

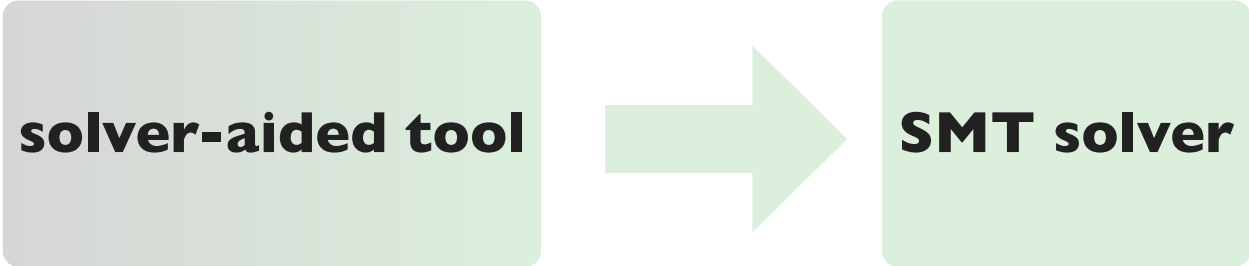


$\exists x . \neg \text{safe}(x, P(x))$

Solver-aided programming: solve

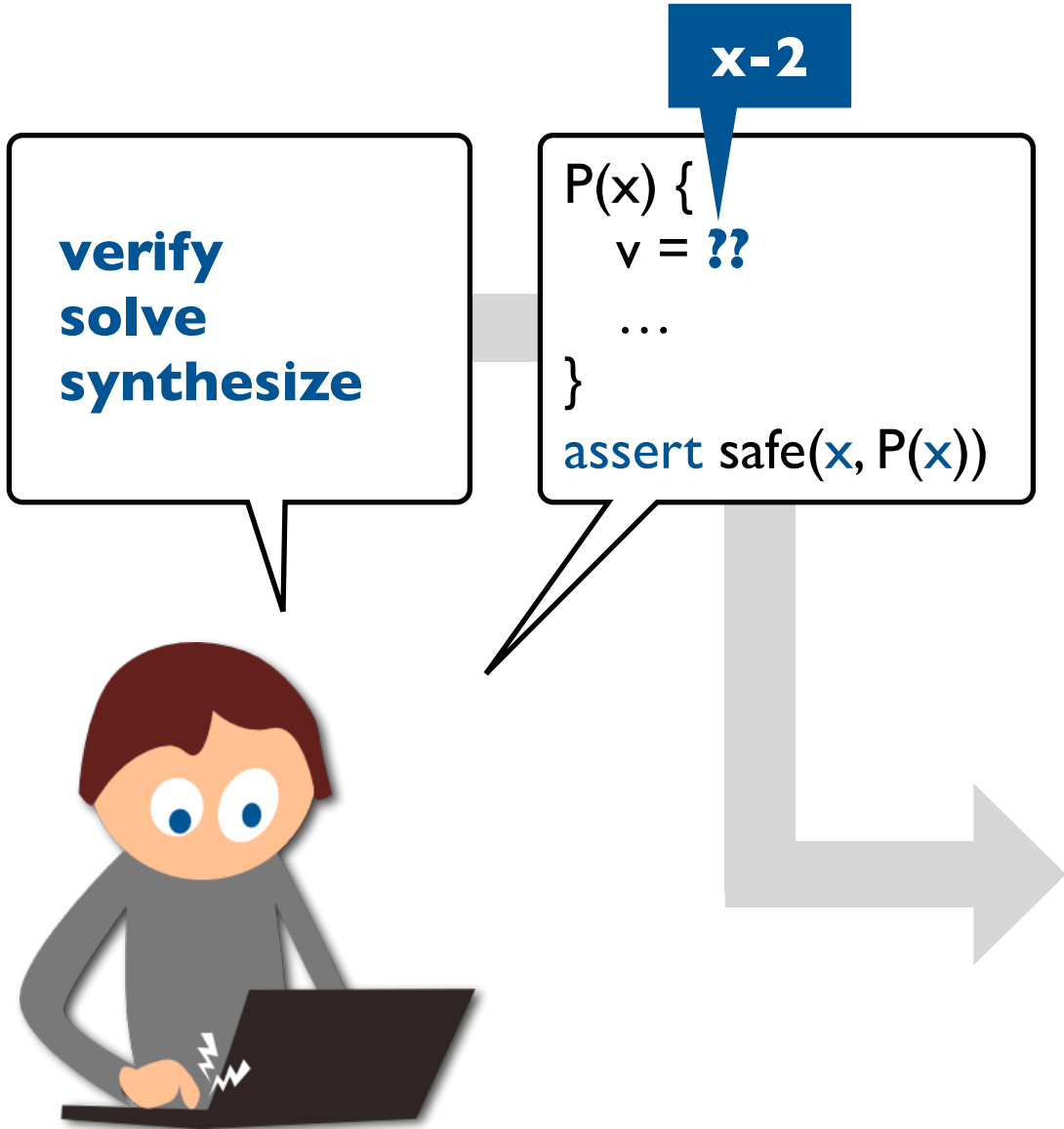


Find an input on which the program fails.
Find values that repair the failing run.

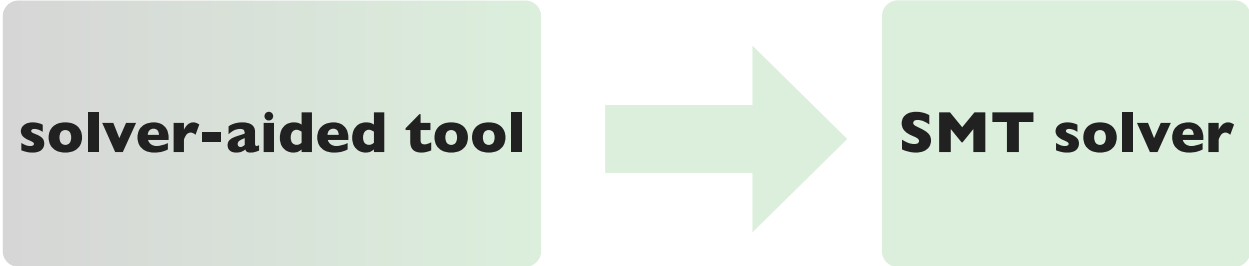


$\exists x . \neg \text{safe}(x, P(x))$
 $x = 42 \wedge \text{safe}(x, P(x))$

Solver-aided programming: synthesize



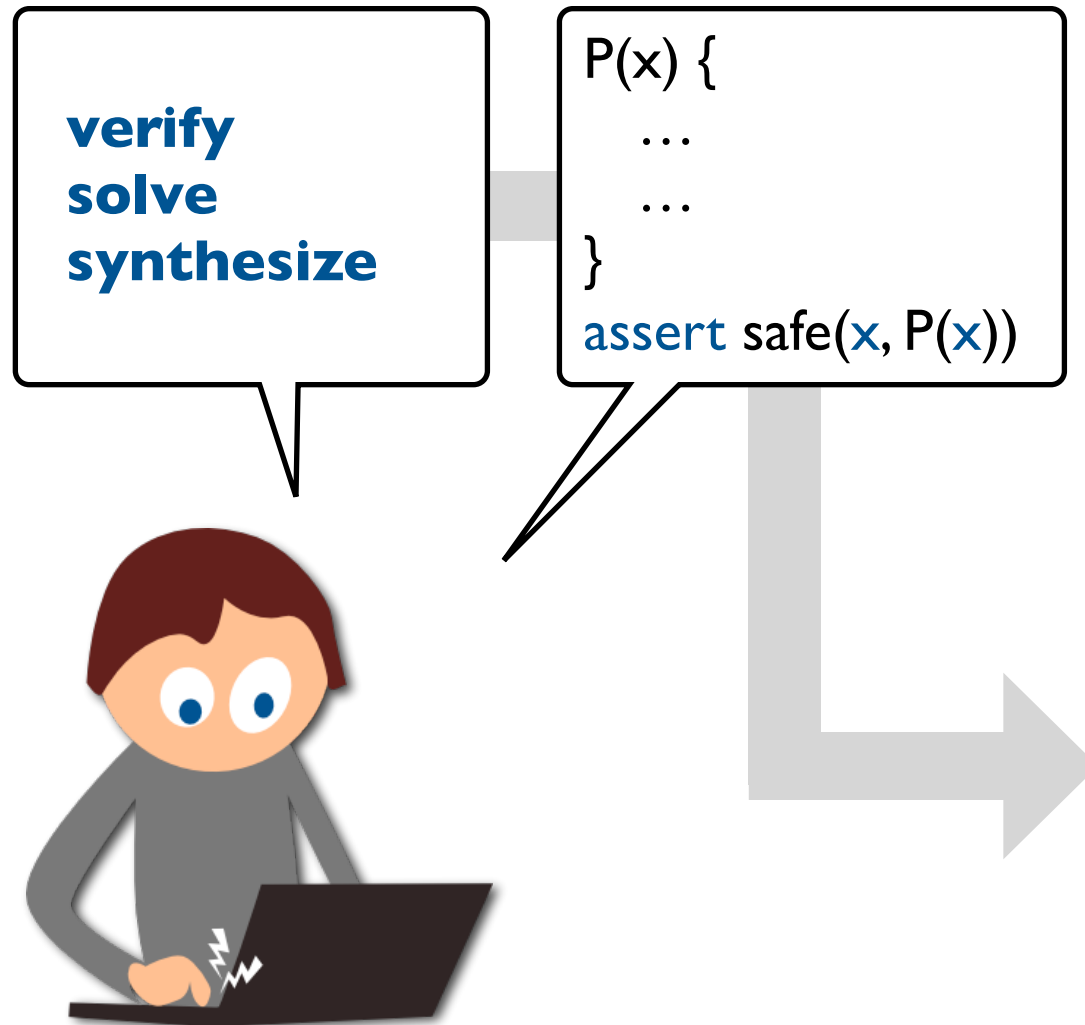
Find an input on which the program fails.
Find values that repair the failing run.
Find code that repairs the program.



A green-bordered callout box containing the following logical formulas:

- $\exists x . \neg \mathbf{safe}(x, \mathbf{P}(x))$
- $x = 42 \wedge \mathbf{safe}(x, \mathbf{P}(x))$
- $\exists e . \forall x . \mathbf{safe}(x, \mathbf{P}_e(x))$

Solver-aided programming: workflow



Use **assertions**, **assumptions**, and **symbolic values** to express the specification.

Ask **queries** about program behavior (on symbolic inputs) with respect to the specification.



$\exists x . \neg \mathbf{safe}(x, \mathbf{P}(x))$

$x = 42 \wedge \mathbf{safe}(x, \mathbf{P}(x))$

$\exists e . \forall x . \mathbf{safe}(x, \mathbf{P}_e(x))$

A programming model that integrates solvers into the language, providing constructs for program verification, synthesis, and more.

ROSETTE

symbolic values
assertions
assumptions
queries

Solver-aided programming in two parts:
(1) getting started and **(2) going pro**

How to use a solver-aided language: the workflow, **constructs, and gotchas.**

How to build your own solver-aided tool via direct symbolic evaluation or language embedding.

Rosette extends Racket with solver-aided constructs



=



+

```
(define-symbolic id type)  
(define-symbolic* id type)
```

**symbolic
values**

```
(assert expr)
```

assertions

```
(assume expr)
```

assumptions

```
(verify expr)
```

queries

```
(solve expr)
```

```
(synthesize
```

```
  #:forall expr
```

```
  #:guarantee expr)
```

Rosette extends **Racket** with solver-aided constructs

“A programming language
for creating new
programming languages”



=



+

A modern descendent of
Scheme and Lisp with
powerful macro-based meta
programming.

```
(define-symbolic id type)  
(define-symbolic* id type)
```

**symbolic
values**

```
(assert expr)
```

assertions

```
(assume expr)
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assumptions

```
(verify expr)
```

queries

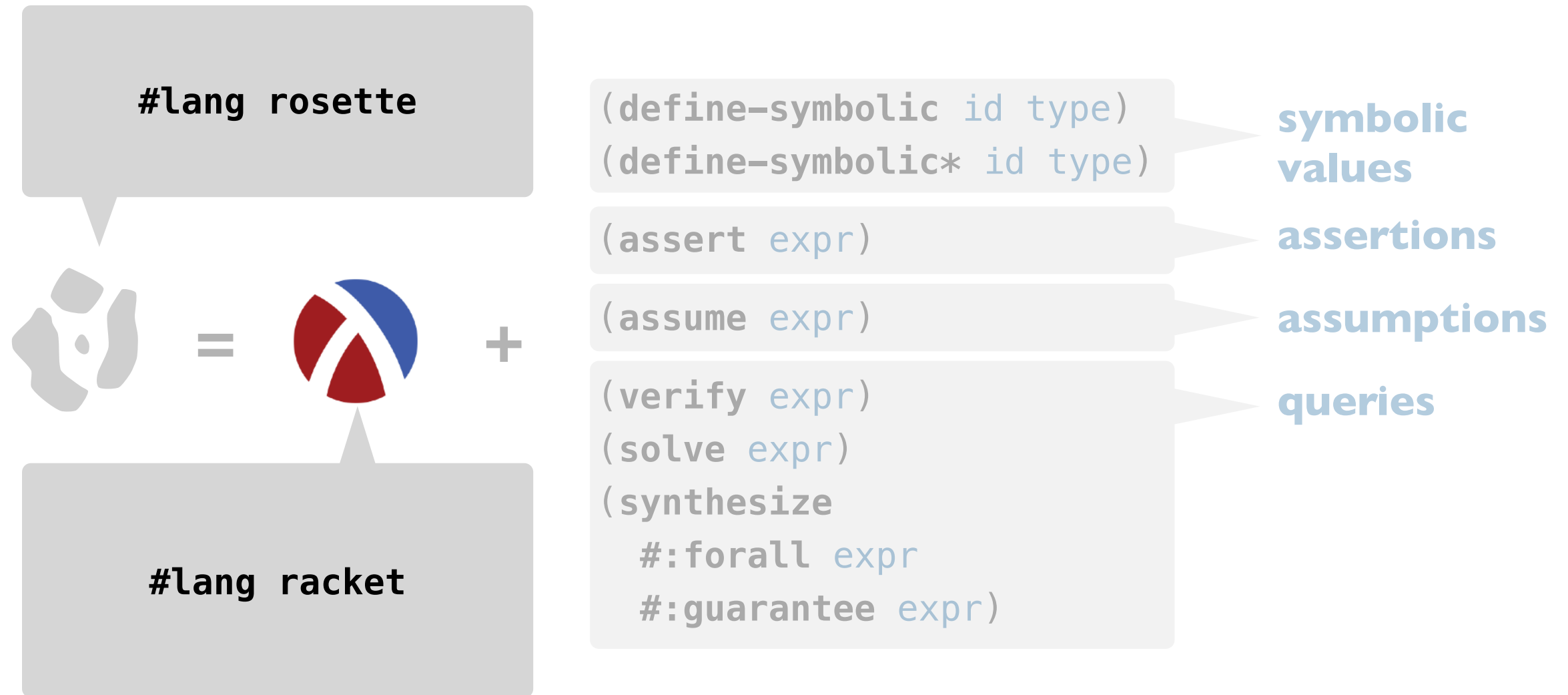
```
(solve expr)
```

```
(synthesize
```

```
  #:forall expr
```

```
  #:guarantee expr)
```

Rosette extends **Racket** with solver-aided constructs



Rosette constructs by example

```
(define-symbolic id type)  
(define-symbolic* id type)
```

```
(assert expr)
```

```
(assume expr)
```

```
(verify expr)
```

```
(solve expr)
```

```
(synthesize
```

```
  #:forall expr
```

```
  #:guarantee expr)
```

demo

<https://courses.cs.washington.edu/courses/cse507/21au/doc/bvudiv2.rkt>

Common pitfalls and gotchas

Reasoning precision
Unbounded loops
Unsafe features



“A gotcha is a valid construct in a system, program or programming language that works as documented but is counter-intuitive and almost invites mistakes because it is both easy to invoke and unexpected or unreasonable in its outcome.”

—*Wikipedia*

<https://courses.cs.washington.edu/courses/cse507/23au/doc/gotchas.rkt>

Common pitfalls and gotchas: reasoning precision

Reasoning precision

Unbounded loops

Unsafe features

- Determines if integers and reals are approximated using k -bit words or treated as infinite-precision values.
- Controlled by setting `current-bitwidth` to an integer $k > 0$ or `#f` for approximate or precise reasoning, respectively.

Common pitfalls and gotchas: reasoning precision

Reasoning precision

Unbounded loops

Unsafe features

- Determines if integers and reals are approximated using k-bit words or treated as infinite-precision values.
- Controlled by setting `current-bitwidth` to an integer $k > 0$ or `#f` for approximate or precise reasoning, respectively.

```
; default current-bitwidth is #f
```

```
> (define-symbolic x integer?)
```

```
> (solve (assert (= x 64)))
```

```
(model [x 64])
```

```
> (verify (assert (not (= x 64))))
```

```
(model [x 64])
```

```
> (current-bitwidth 5)
```

```
> (solve (assert (= x 64)))
```

```
(model [x 0])
```

```
> (verify (assert (not (= x 64))))
```

```
(model [x 0])
```

Common pitfalls and gotchas: unbounded loops

Reasoning precision

Unbounded loops

Unsafe features

- Loops and recursion must be *bounded* (aka *self-finitizing*) by
 - concrete termination conditions, or
 - upper bounds on size of iterated (symbolic) data structures.
- Unbounded loops and recursion run forever.

Common pitfalls and gotchas: unbounded loops

Reasoning precision

Unbounded loops

Unsafe features

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```
(define (search x xs)
  (cond
    [(null? xs) #f]
    [(equal? x (car xs)) #t]
    [else (search x (cdr xs))]))

> (define-symbolic xs integer? #:length 5)
> (define-symbolic xl i integer?)
> (define ys (take xs xl))
> (verify
  (begin
    (assume (<= 0 i (- xl 1))
      (assert (search (list-ref ys i) ys))))
  (unsat))
```

Terminates because search iterates over a bounded structure.

Common pitfalls and gotchas: unbounded loops

Reasoning precision

Unbounded loops

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```
(define (factorial n)
  (cond
    [(= n 0) 1]
    [else (* n (factorial (- n 1)))]))
```

```
> (define-symbolic k integer?)
> (solve
  (assert (> (factorial k) 10)))
```

Unbounded because factorial termination depends on k.

Common pitfalls and gotchas: unbounded loops

Reasoning precision

Unbounded loops

Unsafe features

- Loops and recursion must be *bounded* (aka *self-finitizing*) by
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- Unbounded loops and recursion run forever.

Bound the recursion with a concrete guard.

```
(define (factorial n g)
  (assert (>= g 0))
  (cond
    [(= n 0) 1]
    [else (* n (factorial (- n 1) (- g 1)))]))
```

```
> (define-symbolic k integer?)
> (solve
  (assert (> (factorial k 3) 10)))
```

(unsat)

UNSAT because the bound is too small to find a solution.

Common pitfalls and gotchas: unbounded loops

Reasoning precision

Unbounded loops

Unsafe features

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Bound the recursion with a concrete guard.

```
(define (factorial n g)
  (assert (>= g 0))
  (cond
    [(= n 0) 1]
    [else (* n (factorial (- n 1) (- g 1)))]))
```

```
> (define-symbolic k integer?)
> (solve
  (assert (> (factorial k 4) 10)))
```

```
(model
 [k 4])
```

Make sure the bound is large enough ...

Common pitfalls and gotchas: unsafe features

Reasoning precision

Unbounded loops

Unsafe features

- Rosette *lifts* only a core subset of Racket to operate on symbolic values. This includes all constructs in `#lang rosette/safe`
- Unlifted constructs can be used in `#lang rosette` but require care: the programmer must determine when it is okay for symbolic values to flow to unlifted code.

Common pitfalls and gotchas: unsafe features

Reasoning precision

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```
; vectors are lifted
```

```
> (define v (vector 1 2))
```

```
> (define-symbolic k integer?)
```

```
> (vector-ref v k)
```

```
(ite* (⊢ (= 0 k) 1) (⊢ (= 1 k) 2)))
```

```
; hashes are unlifted
```

```
> (define h (make-hash '((0 . 1)(1 . 2))))
```

```
> (hash-ref h k)
```

```
hash-ref: no value found for key  
key: k
```

```
> (hash-set! h k 3)
```

```
> (hash-ref h k)
```

```
3
```


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ROSETTE

emina.github.io/rosette/

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Summary

Today

- Course overview & logistics
- Getting started with solver-aided programming

Next lecture

- Going pro with solver-aided programming