

Computer-Aided Reasoning for Software

Solver-Aided Programming II

Emina Torlak

emina@cs.washington.edu

Topics

Last lecture

- Getting started with solver-aided programming.

Today

- Going pro with solver-aided programming.



A programming model that integrates solvers into the language, providing constructs for program verification, synthesis, and more.



Solver-aided programming in two parts: **(1) getting started and (2) going pro**

How to use a solver-aided language: the workflow, constructs, and gotchas.

How to build your own solver-aided tool via direct symbolic evaluation or language embedding.

How to build your own solver-aided tool or language



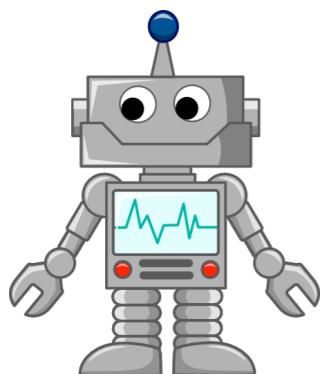
The classic (hard) way to build a tool
What is hard about building a solver-aided tool?

SDSL



SVM

SMT



An easier way: tools as languages
How to build tools by stacking layers of languages.

Behind the scenes: symbolic virtual machine
How Rosette works so you don't have to.

A last look: a few recent applications
Cool tools built with Rosette!

How to build your own solver-aided tool or language



The classic (hard) way to build a tool

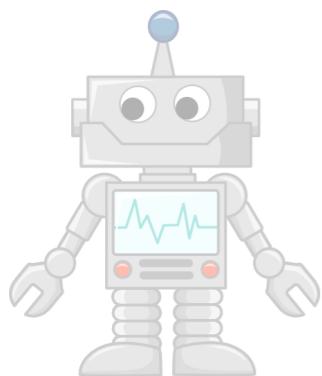
What is hard about building a solver-aided tool?

SDSL



SVM

SMT



An easier way: tools as languages

How to build tools by stacking layers of languages.

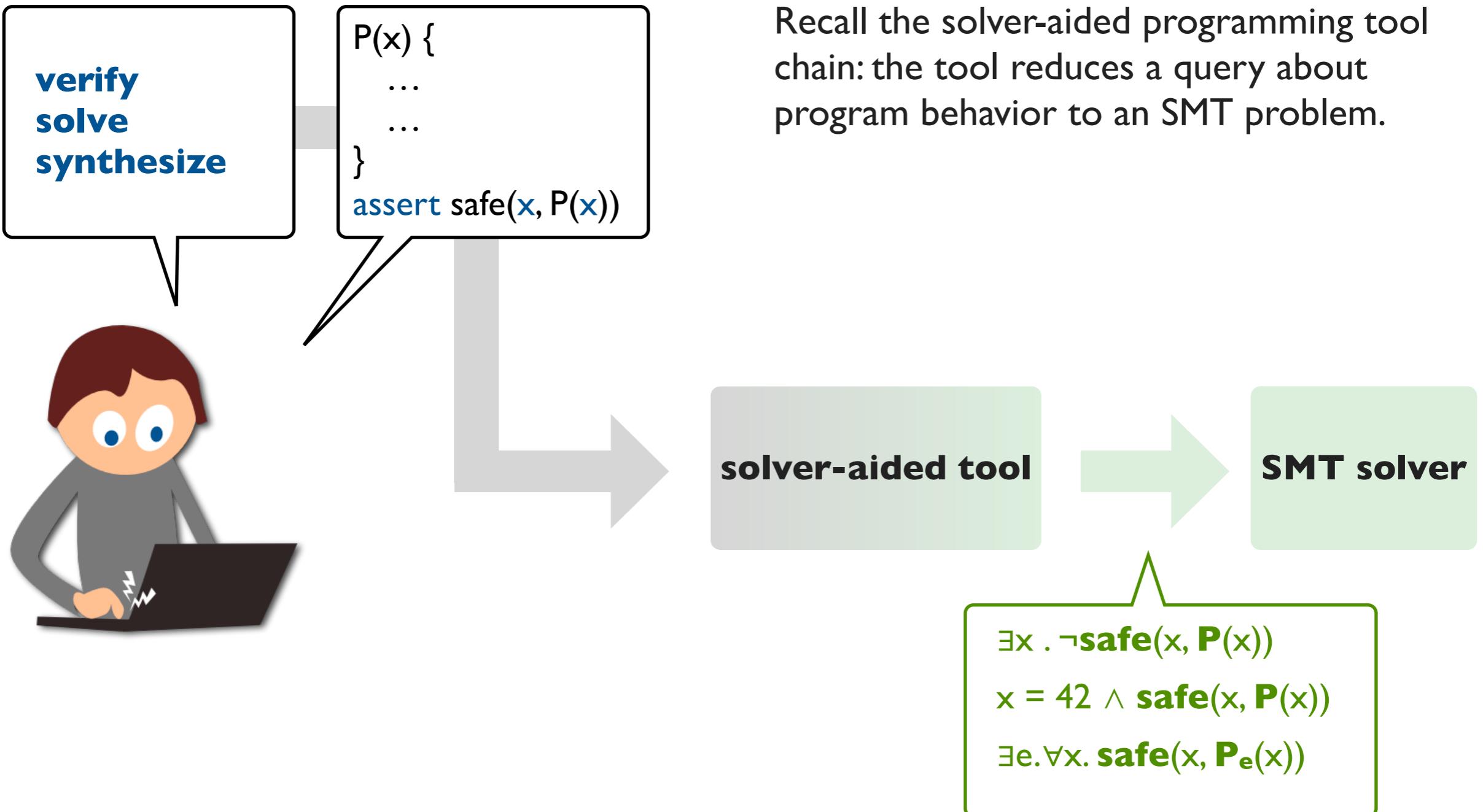
Behind the scenes: symbolic virtual machine

How Rosette works so you don't have to.

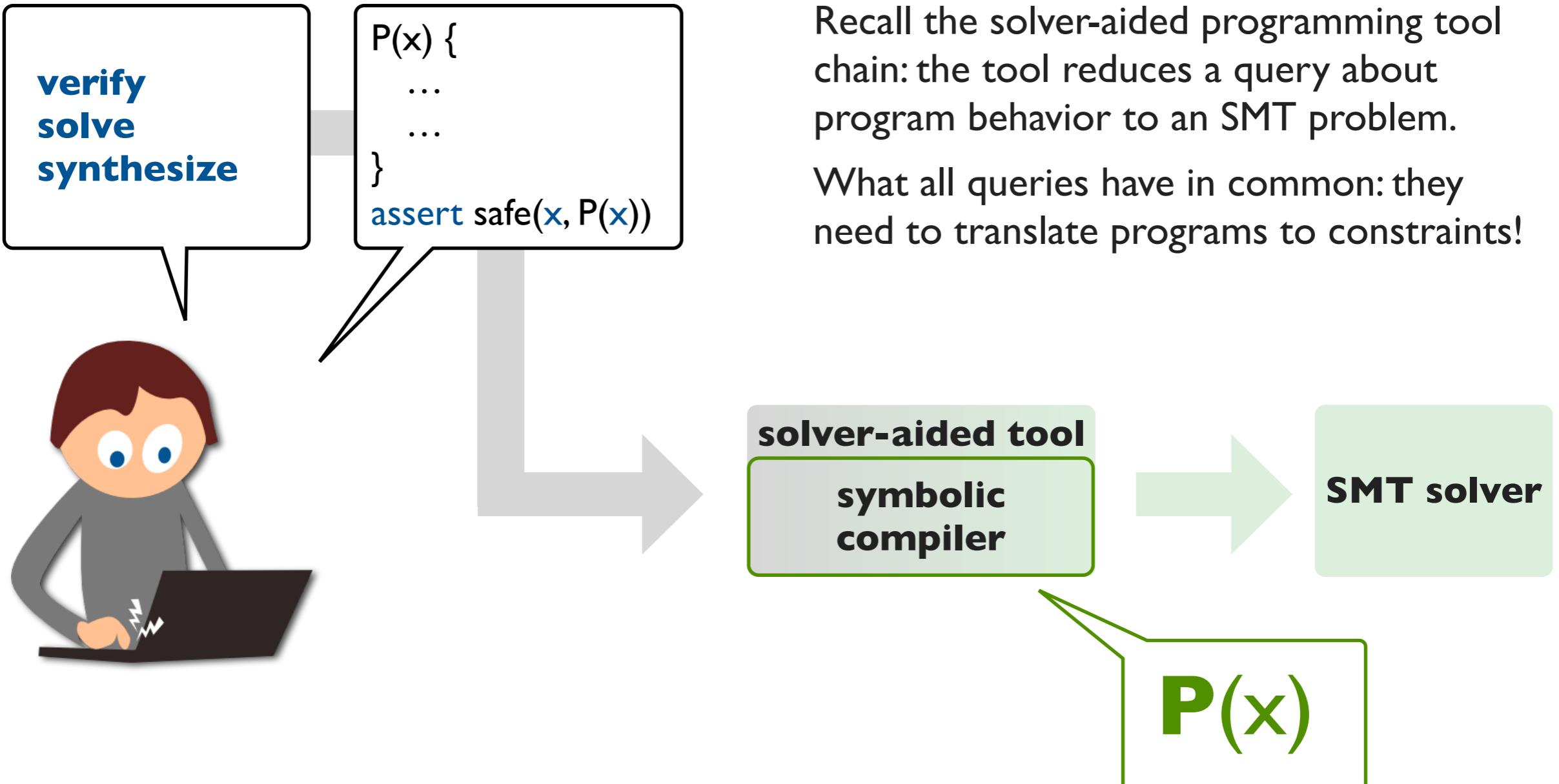
A last look: a few recent applications

Cool tools built with Rosette!

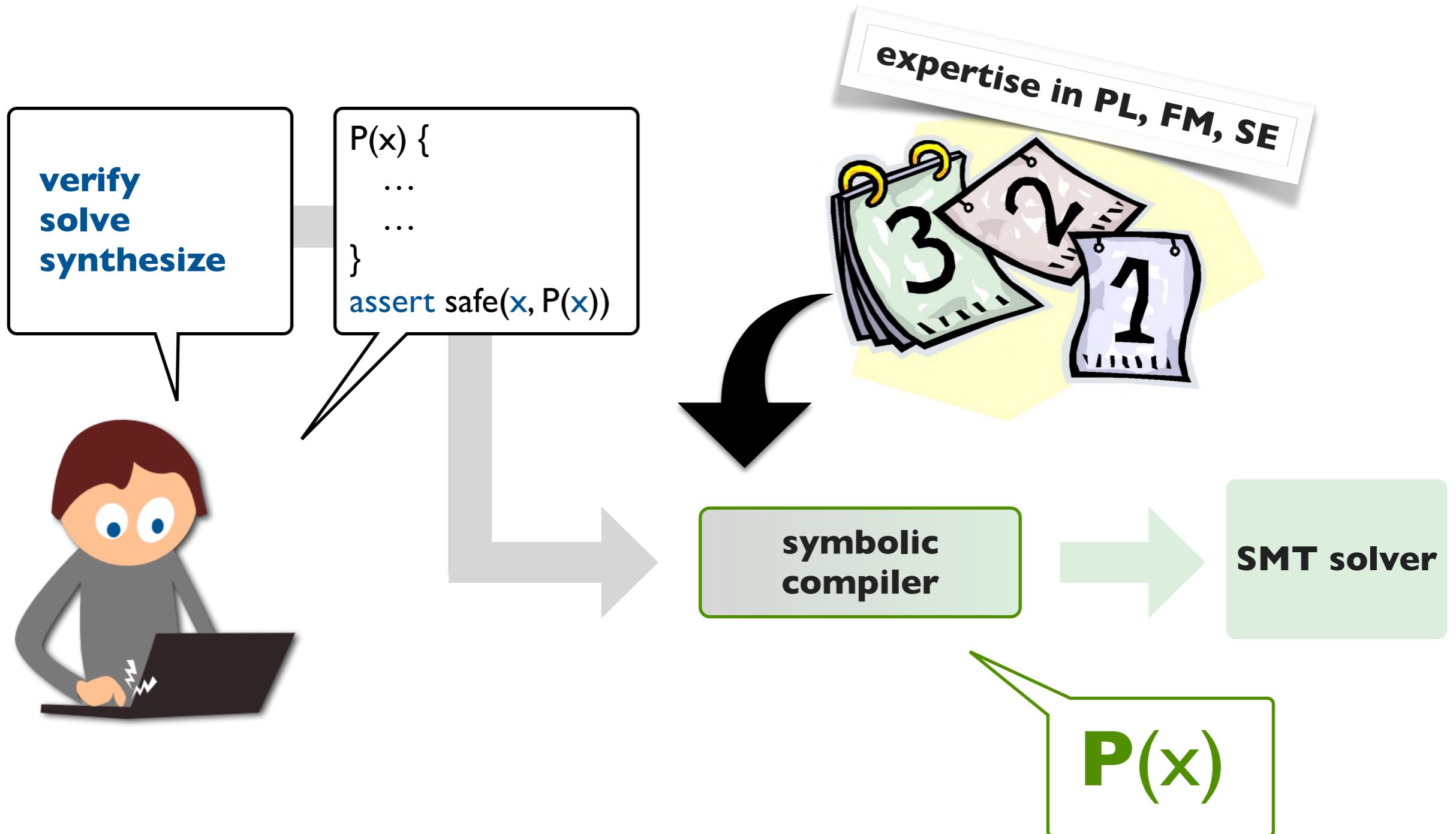
The classic (hard) way to build a tool



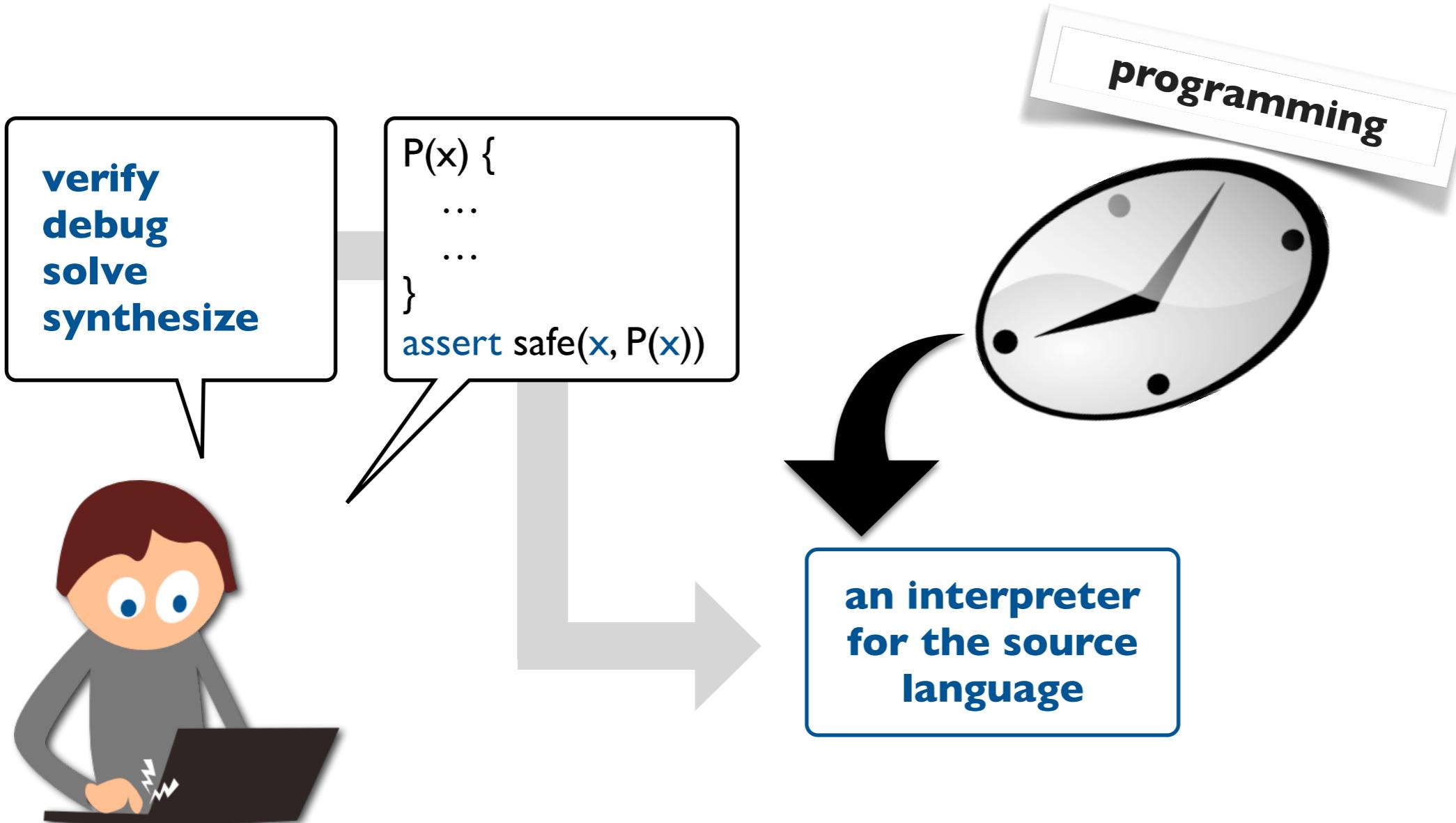
The classic (hard) way to build a tool



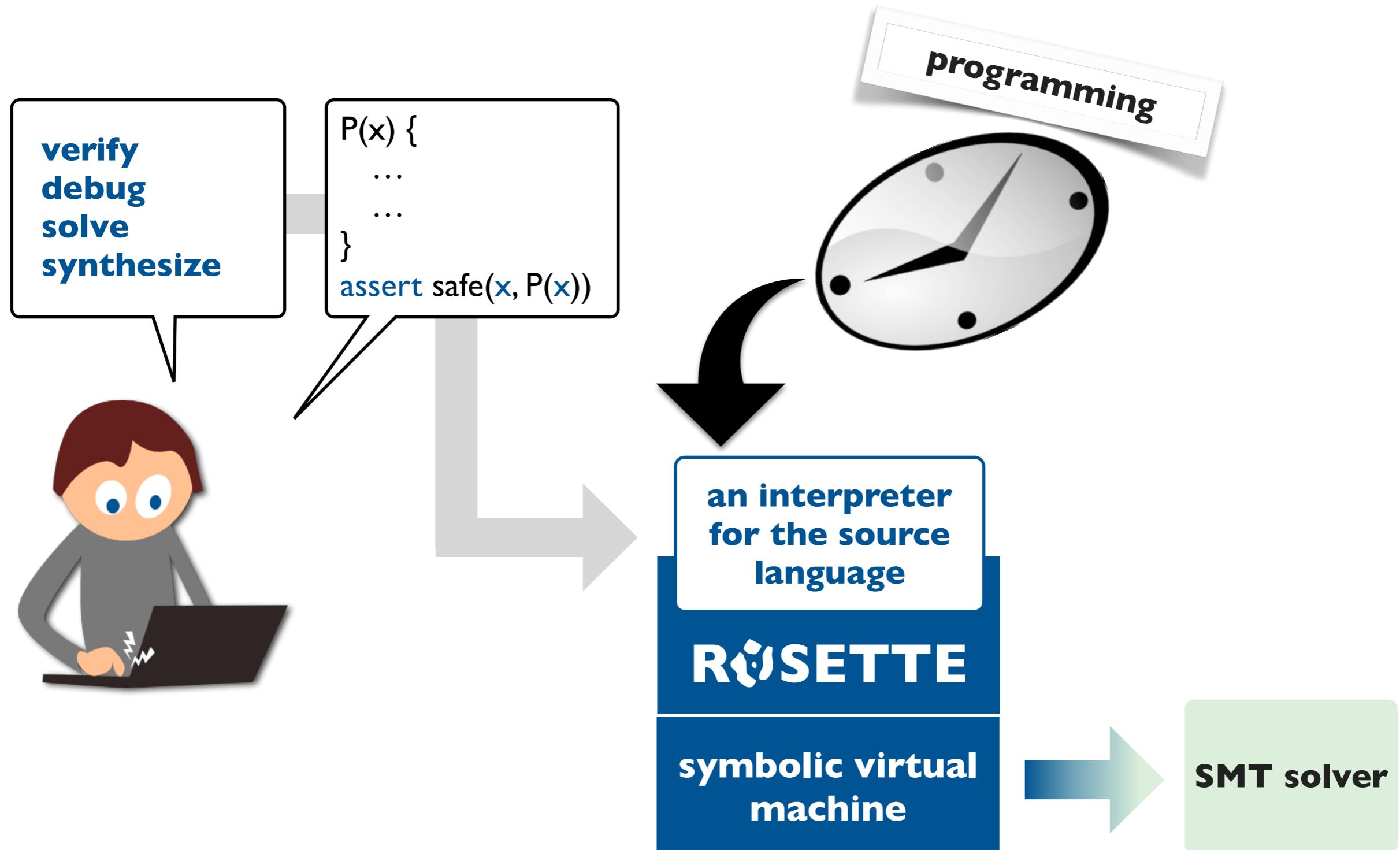
The classic (hard) way to build a tool



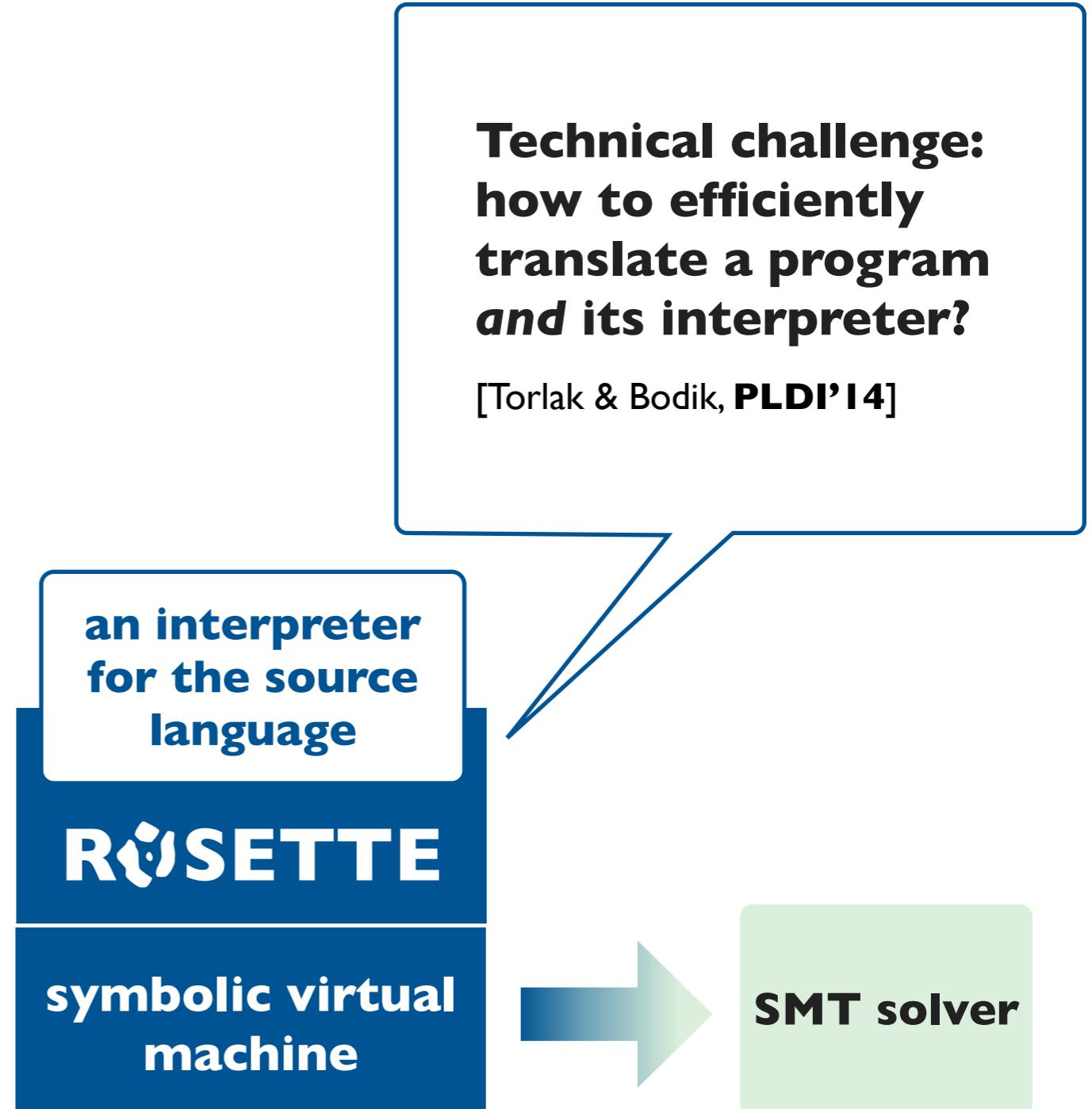
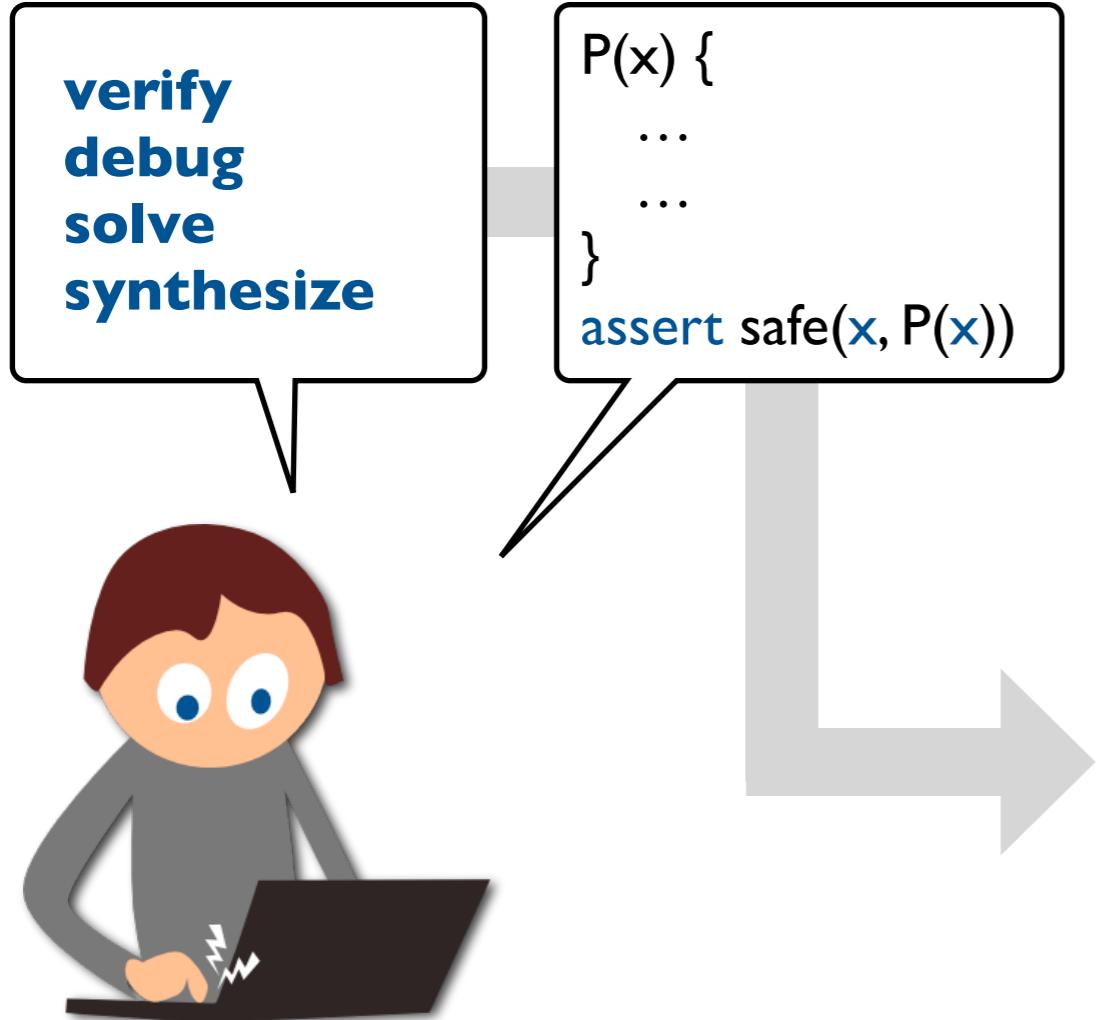
Wanted: an easier way to build tools



Wanted: an easier way to build tools



Wanted: an easier way to build tools



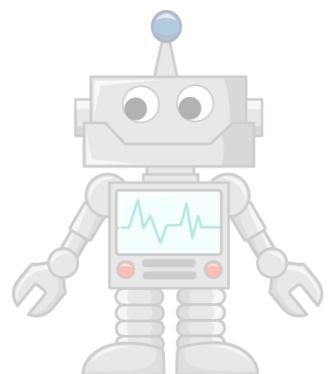
How to build your own solver-aided tool or language



The classic (hard) way to build a tool
What is hard about building a solver-aided tool?



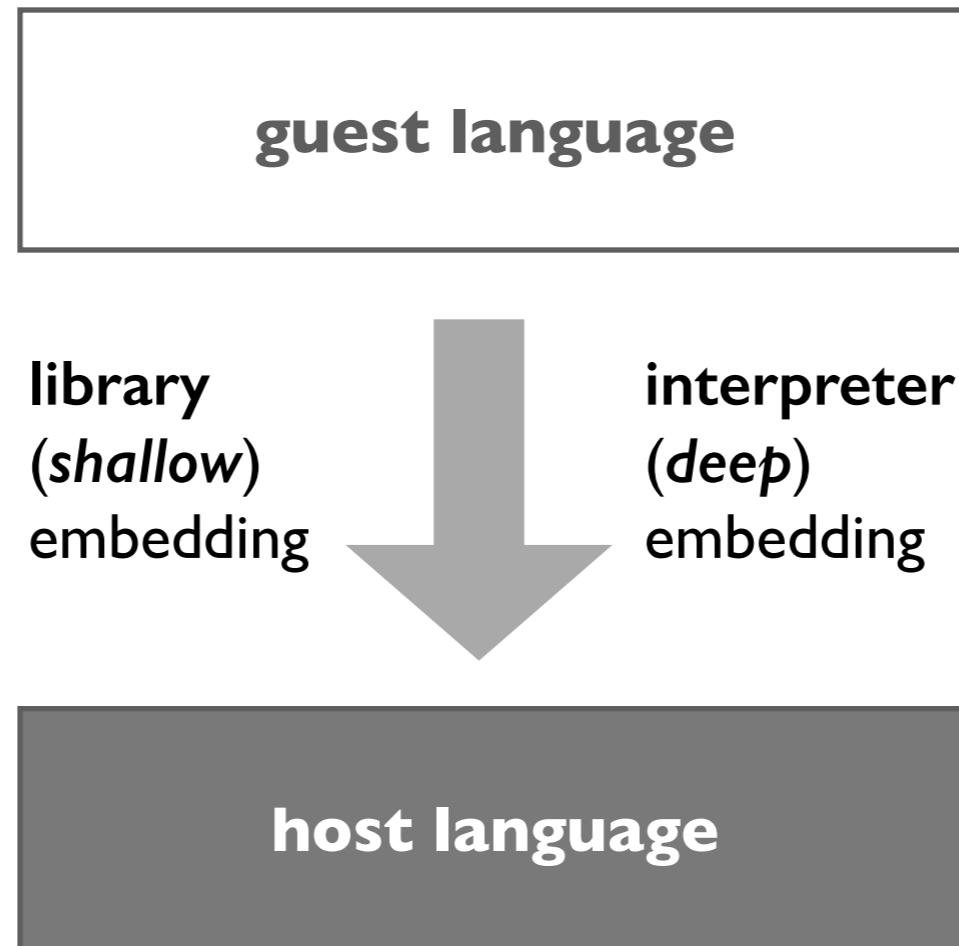
An easier way: tools as languages
How to build tools by stacking layers of languages.



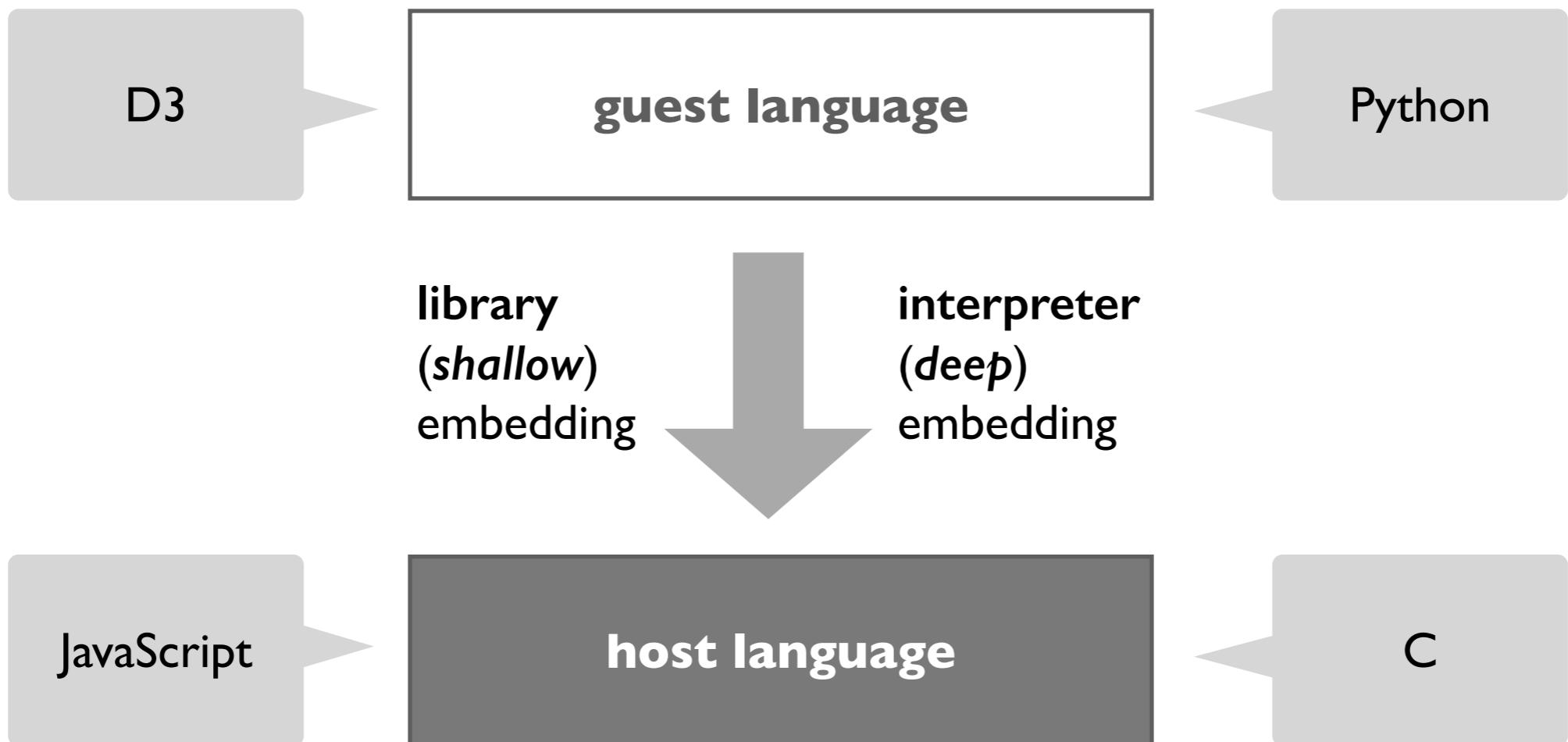
Behind the scenes: symbolic virtual machine
How Rosette works so you don't have to.

A last look: a few recent applications
Cool tools built with Rosette!

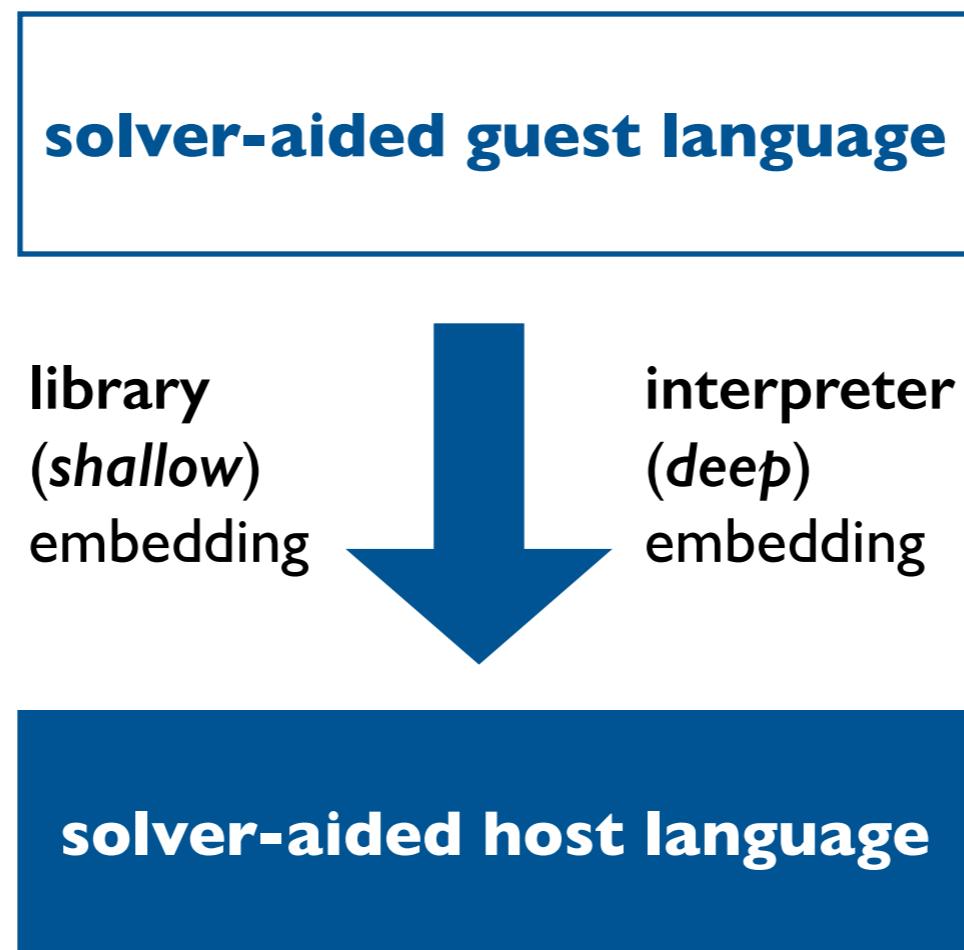
Layers of classic languages: guests and hosts



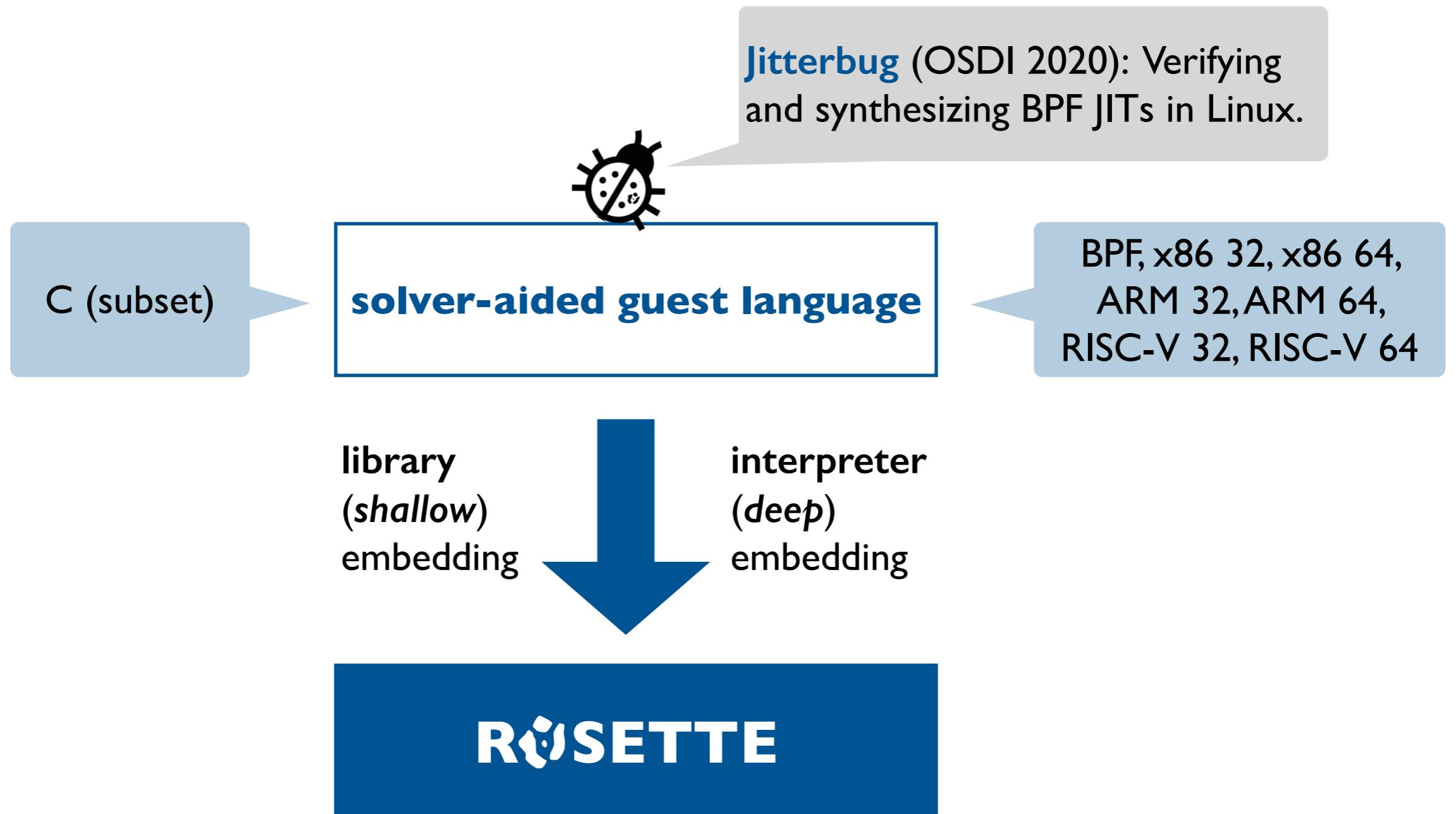
Layers of classic languages: guests and hosts



Layers of solver-aided languages



Layers of solver-aided languages



A tiny example solver-aided guest language

```
def bvmax(r0, r1) :  
    r2 = bvsge(r0, r1)  
    r3 = bvneg(r2)  
    r4 = bvxor(r0, r2)  
    r5 = bvand(r3, r4)  
    r6 = bvxor(r1, r5)  
    return r6
```

BV: A tiny assembly-like language for writing fast, low-level library functions.

A tiny example solver-aided guest language

```
def bvmax(r0, r1) :  
    r2 = bvsge(r0, r1)  
    r3 = bvneg(r2)  
    r4 = bvxor(r0, r2)  
    r5 = bvand(r3, r4)  
    r6 = bvxor(r1, r5)  
    return r6
```

BV: A tiny assembly-like language for writing fast, low-level library functions.

We want to **test**, **verify**, and **synthesize** programs in the BV SDSL.

A tiny example solver-aided guest language

```
def bvmax(r0, r1) :  
    r2 = bvsge(r0, r1)  
    r3 = bvneg(r2)  
    r4 = bvxor(r0, r2)  
    r5 = bvand(r3, r4)  
    r6 = bvxor(r1, r5)  
    return r6
```

BV: A tiny assembly-like language for writing fast, low-level library functions.

1. interpreter [50 LOC]
2. verifier [free]
3. synthesizer [free]



We want to **test**, **verify**, and **synthesize** programs in the BV SDSL.

A tiny example language

```
def bvmax(r0, r1) :  
    r2 = bvsge(r0, r1)  
    r3 = bvneg(r2)  
    r4 = bvxor(r0, r2)  
    r5 = bvand(r3, r4)  
    r6 = bvxor(r1, r5)  
    return r6
```

```
> bvmax(-2, -1)
```

ROSETTE

A tiny example language

```
def bvmax(r0, r1) :  
    r2 = bvsge(r0, r1)  
    r3 = bvneg(r2)  
    r4 = bvxor(r0, r2)  
    r5 = bvand(r3, r4)  
    r6 = bvxor(r1, r5)  
    return r6
```

```
> bvmax(-2, -1)
```

parse

R^oSSETTE

```
(define bvmax  
  `((2 bvsge 0 1)  
   (3 bvneg 2)  
   (4 bvxor 0 2)  
   (5 bvand 3 4)  
   (6 bvxor 1 5)))
```

A tiny example language

```
def bvmax(r0, r1) :  
    r2 = bvsge(r0, r1)  
    r3 = bvneg(r2)  
    r4 = bvxor(r0, r2)  
    r5 = bvand(r3, r4)  
    r6 = bvxor(r1, r5)  
    return r6
```

```
> bvmax(-2, -1)
```

parse

```
(define bvmax  
  `((2 bvsge 0 1)  
   (3 bvneg 2)  
   (4 bvxor 0 2)  
   (5 bvand 3 4)  
   (6 bvxor 1 5))))
```

(out opcode in ...)

R^oSSETTE

A tiny example language

```
def bvmax(r0, r1) :  
    r2 = bvsge(r0, r1)  
    r3 = bvneg(r2)  
    r4 = bvxor(r0, r2)  
    r5 = bvand(r3, r4)  
    r6 = bvxor(r1, r5)  
return r6
```

```
> bvmax(-2, -1)
```

interpret

RJSETTE

```
(define bvmax  
  `((2 bvsge 0 1)  
   (3 bvneg 2)  
   (4 bvxor 0 2)  
   (5 bvand 3 4)  
   (6 bvxor 1 5)))
```

`(-2 -1)

```
(define (interpret prog inputs)  
  (make-registers prog inputs)  
  (for ([stmt prog])  
    (match stmt  
      [(list out opcode in ...)  
       (define op (lookup opcode))  
       (define args (map load in))  
       (store out (apply op args))])  
      (load (last))))
```

A tiny example language

```
def bvmax(r0, r1) :  
    r2 = bvsge(r0, r1)  
    r3 = bvneg(r2)  
    r4 = bvxor(r0, r2)  
    r5 = bvand(r3, r4)  
    r6 = bvxor(r1, r5)  
return r6
```

```
> bvmax(-2, -1)
```

interpret

```
(define bvmax  
  `((2 bvsge 0 1)  
   (3 bvneg 2)  
   (4 bvxor 0 2)  
   (5 bvand 3 4)  
   (6 bvxor 1 5))))
```

0	-2
1	-1
2	
3	
4	
5	
6	

```
(define (interpret prog inputs)  
  (make-registers prog inputs)  
  (for ([stmt prog])  
   (match stmt  
    [(list out opcode in ...)  
     (define op (lookup opcode))  
     (define args (map load in))  
     (store out (apply op args))])])  
  (load (last)))
```

Rosette

A tiny example language

```
def bvmax(r0, r1) :  
    r2 = bvsge(r0, r1)  
    r3 = bvneg(r2)  
    r4 = bvxor(r0, r2)  
    r5 = bvand(r3, r4)  
    r6 = bvxor(r1, r5)  
return r6
```

```
> bvmax(-2, -1)
```

interpret

```
(define bvmax  
  `((2 bvsge 0 1)  
   (3 bvneg 2)  
   (4 bvxor 0 2)  
   (5 bvand 3 4)  
   (6 bvxor 1 5)))
```

0	-2
1	-1
2	
3	
4	
5	
6	

```
(define (interpret prog inputs)  
  (make-registers prog inputs)  
  (for ([stmt prog])  
   (match stmt  
    [(list out opcode in ...)  
     (define op (lookup opcode))  
     (define args (map load in))  
     (store out (apply op args))])])  
  (load (last)))
```

Rosette

A tiny example language

```
def bvmax(r0, r1) :  
    r2 = bvsge(r0, r1)  
    r3 = bvneg(r2)  
    r4 = bvxor(r0, r2)  
    r5 = bvand(r3, r4)  
    r6 = bvxor(r1, r5)  
  
    return r6
```

```
> bvmax(-2, -1)
```

interpret

```
(define bvmax  
  `((2 bvsge 0 1)  
   (3 bvneg 2)  
   (4 bvxor 0 2)  
   (5 bvand 3 4)  
   (6 bvxor 1 5)))
```

0	-2
1	-1
2	
3	
4	
5	
6	

```
(define (interpret prog inputs)  
  (make-registers prog inputs)  
  (for ([stmt prog])  
    (match stmt  
      [(list out opcode in ...)  
       (define op (lookup opcode))  
       (define args (map load in))  
       (store out (apply op args))])  
      (load (last))))
```

Rosette

A tiny example language

```
def bvmax(r0, r1) :  
    r2 = bvsge(r0, r1)  
    r3 = bvneg(r2)  
    r4 = bvxor(r0, r2)  
    r5 = bvand(r3, r4)  
    r6 = bvxor(r1, r5)  
return r6
```

```
> bvmax(-2, -1)
```

interpret

```
(define bvmax  
  `((2 bvsge 0 1)  
   (3 bvneg 2)  
   (4 bvxor 0 2)  
   (5 bvand 3 4)  
   (6 bvxor 1 5)))
```

0	-2
1	-1
2	
3	
4	
5	
6	

```
(define (interpret prog inputs)  
  (make-registers prog inputs)  
  (for ([stmt prog])  
   (match stmt  
    [(list out opcode in ...)  
     (define op (lookup opcode))  
     (define args (map load in))  
     (store out (apply op args))])])  
  (load (last)))
```

Rosette

A tiny example language

```
def bvmax(r0, r1) :  
    r2 = bvsge(r0, r1)  
    r3 = bvneg(r2)  
    r4 = bvxor(r0, r2)  
    r5 = bvand(r3, r4)  
    r6 = bvxor(r1, r5)  
  
    return r6
```

```
> bvmax(-2, -1)
```

interpret

```
(define bvmax  
  `((2 bvsge 0 1)  
   (3 bvneg 2)  
   (4 bvxor 0 2)  
   (5 bvand 3 4)  
   (6 bvxor 1 5)))
```

0	-2
1	-1
2	0
3	
4	
5	
6	

```
(define (interpret prog inputs)  
  (make-registers prog inputs)  
  (for ([stmt prog])  
    (match stmt  
      [(list out opcode in ...)  
       (define op (lookup opcode))  
       (define args (map load in))  
       (store out (apply op args))])  
      (load (last))))
```

RJSETTE

A tiny example language

```
def bvmax(r0, r1) :  
    r2 = bvsge(r0, r1)  
    r3 = bvneg(r2)  
    r4 = bvxor(r0, r2)  
    r5 = bvand(r3, r4)  
    r6 = bvxor(r1, r5)  
  
    return r6
```

```
> bvmax(-2, -1)
```

interpret

```
(define bvmax  
  `((2 bvsge 0 1)  
   (3 bvneg 2)  
   (4 bvxor 0 2)  
   (5 bvand 3 4)  
   (6 bvxor 1 5))))
```

0	-2
1	-1
2	0
3	0
4	-2
5	0
6	-1

```
(define (interpret prog inputs)  
  (make-registers prog inputs)  
  (for ([stmt prog])  
    (match stmt  
      [(list out opcode in ...)  
       (define op (lookup opcode))  
       (define args (map load in))  
       (store out (apply op args))])  
      (load (last))))
```

Rosette

A tiny example language

```
def bvmax(r0, r1) :  
    r2 = bvsge(r0, r1)  
    r3 = bvneg(r2)  
    r4 = bvxor(r0, r2)  
    r5 = bvand(r3, r4)  
    r6 = bvxor(r1, r5)  
  
    return r6
```

```
> bvmax(-2, -1)  
-1
```

interpret

```
(define bvmax  
  `((2 bvsge 0 1)  
   (3 bvneg 2)  
   (4 bvxor 0 2)  
   (5 bvand 3 4)  
   (6 bvxor 1 5))))
```

0	-2
1	-1
2	0
3	0
4	-2
5	0
6	-1

```
(define (interpret prog inputs)  
  (make-registers prog inputs)  
  (for ([stmt prog])  
    (match stmt  
      [(list out opcode in ...)  
       (define op (lookup opcode))  
       (define args (map load in))  
       (store out (apply op args))])  
      (load (last))))
```

RJSETTE

A tiny example language

```
def bvmax(r0, r1) :  
    r2 = bvsge(r0, r1)  
    r3 = bvneg(r2)  
    r4 = bvxor(r0, r2)  
    r5 = bvand(r3, r4)  
    r6 = bvxor(r1, r5)  
return r6
```

```
> bvmax(-2, -1)  
-1
```

```
(define bvmax  
  `((2 bvsge 0 1)  
   (3 bvneg 2)  
   (4 bvxor 0 2)  
   (5 bvand 3 4)  
   (6 bvxor 1 5)))
```

```
(define (interpret prog inputs)  
  (make-registers prog inputs)  
  (for ([stmt prog])  
   (match stmt  
     [(list out opcode in ...)  
      (define op (lookup opcode))  
      (define args (map load in))  
      (store out (apply op args))])  
    (load (last))))
```

- ▶ pattern matching
- ▶ first-class & higher-order procedures
- ▶ side effects

A tiny example language

```
def bvmax(r0, r1) :  
    r2 = bvsge(r0, r1)  
    r3 = bvneg(r2)  
    r4 = bvxor(r0, r2)  
    r5 = bvand(r3, r4)  
    r6 = bvxor(r1, r5)  
return r6  
  
> verify(bvmax, max)
```

query

R^oSSETTE

```
(define-symbolic x y int32?)  
(define in (list x y))  
(verify  
  (assert (equal? (interpret bvmax in)  
                  (apply max in))))
```

A tiny example language

```
def bvmax(r0, r1) :  
    r2 = bvsge(r0, r1)  
    r3 = bvneg(r2)  
    r4 = bvxor(r0, r2)  
    r5 = bvand(r3, r4)  
    r6 = bvxor(r1, r5)  
    return r6
```

```
> verify(bvmax, max)
```

```
(define (max x y)  
  (if (bvsge x y) x y))
```

query

R^oSSETTE

```
(define-symbolic x y int32?)  
(define in (list x y))  
(verify  
  (assert (equal? (interpret bvmax in)  
                  (apply max in))))
```

A tiny example language

```
def bvmax(r0, r1) :  
    r2 = bvsge(r0, r1)  
    r3 = bvneg(r2)  
    r4 = bvxor(r0, r2)  
    r5 = bvand(r3, r4)  
    r6 = bvxor(r1, r5)  
return r6  
  
> verify(bvmax, max)
```

query

R^{OSSETTE}

Creates two fresh symbolic values of type 32-bit integer and binds them to the variables x and y.

```
(define-symbolic x y int32?)  
(define in (list x y))  
(verify  
  (assert (equal? (interpret bvmax in)  
                  (apply max in))))
```

A tiny example language

```
def bvmax(r0, r1) :  
    r2 = bvsge(r0, r1)  
    r3 = bvneg(r2)  
    r4 = bvxor(r0, r2)  
    r5 = bvand(r3, r4)  
    r6 = bvxor(r1, r5)  
return r6  
  
> verify(bvmax, max)
```

query

R_SSETTE

Creates two fresh symbolic values of type 32-bit integer and binds them to the variables x and y.

```
(define-symbolic x y int32?)  
(define in (list x y))  
(verify  
  (assert (equal? (interpret bvmax in)  
                    (apply max in))))
```

Symbolic values can be used just like concrete values of the same type.

A tiny example language

R_{OSSETTE}

```
def bvmax(r0, r1) :  
    r2 = bvsge(r0, r1)  
    r3 = bvneg(r2)  
    r4 = bvxor(r0, r2)  
    r5 = bvand(r3, r4)  
    r6 = bvxor(r1, r5)  
return r6  
  
> verify(bvmax, max)
```

query

Creates two fresh symbolic values of type 32-bit integer and binds them to the variables x and y.

```
(define-symbolic x y int32?)  
(define in (list x y))  
(verify  
  (assert (equal? (interpret bvmax in)  
                    (apply max in))))
```

(**verify** *expr*) searches for a concrete interpretation of symbolic values that causes *expr* to fail.

Symbolic values can be used just like concrete values of the same type.

A tiny example language

```
def bvmax(r0, r1) :  
    r2 = bvsge(r0, r1)  
    r3 = bvneg(r2)  
    r4 = bvxor(r0, r2)  
    r5 = bvand(r3, r4)  
    r6 = bvxor(r1, r5)  
    return r6
```

```
> verify(bvmax, max)  
[0, -2]
```



query

ROSETTE

```
(define-symbolic x y int32?)  
(define in (list x y))  
(verify  
  (assert (equal? (interpret bvmax in)  
                  (apply max in))))
```

A tiny example language

```
def bvmax(r0, r1) :  
    r2 = bvsge(r0, r1)  
    r3 = bvneg(r2)  
    r4 = bvxor(r0, r2)  
    r5 = bvand(r3, r4)  
    r6 = bvxor(r1, r5)  
    return r6
```

```
> verify(bvmax, max)
```

```
[0, -2]
```

```
> bvmax(0, -2)
```

```
-1
```

R^oSSETTE

query

```
(define-symbolic x y int32?)  
(define in (list x y))  
(verify  
  (assert (equal? (interpret bvmax in)  
                  (apply max in))))
```

A tiny example language

```
def bvmax(r0, r1) :  
    r2...r6 = inst??(bvsge, bvneg,  
                      bvxor, bvand)  
  
    return r6
```

```
> synthesize(bvmax, max)
```

query

Rosette

```
(define-symbolic x y int32?)  
(define in (list x y))  
(synthesize  
  #:forall in  
  #:guarantee  
  (assert (equal? (interpret bvmax in)  
                 (apply max in)))))
```

A tiny example language

```
def bvmax(r0, r1) :  
    r2 = bvsge(r0, r1)  
    r3 = bvneg(r2)  
    r4 = bvxor(r0, r1)  
    r5 = bvand(r3, r4)  
    r6 = bvxor(r1, r5)  
    return r6  
  
> synthesize(bvmax, max)
```



ROSSETTE

```
(define-symbolic x y int32?)  
(define in (list x y))  
(synthesize  
  #:forall in  
  #:guarantee  
  (assert (equal? (interpret bvmax in)  
                 (apply max in)))))
```

How to build your own solver-aided tool or language



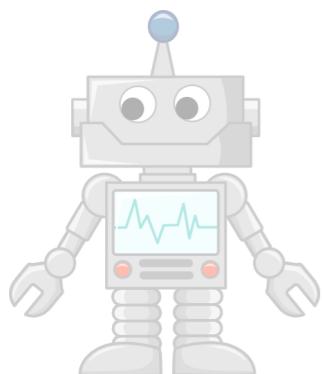
The classic (hard) way to build a tool
What is hard about building a solver-aided tool?

SDSL



SVM

SMT

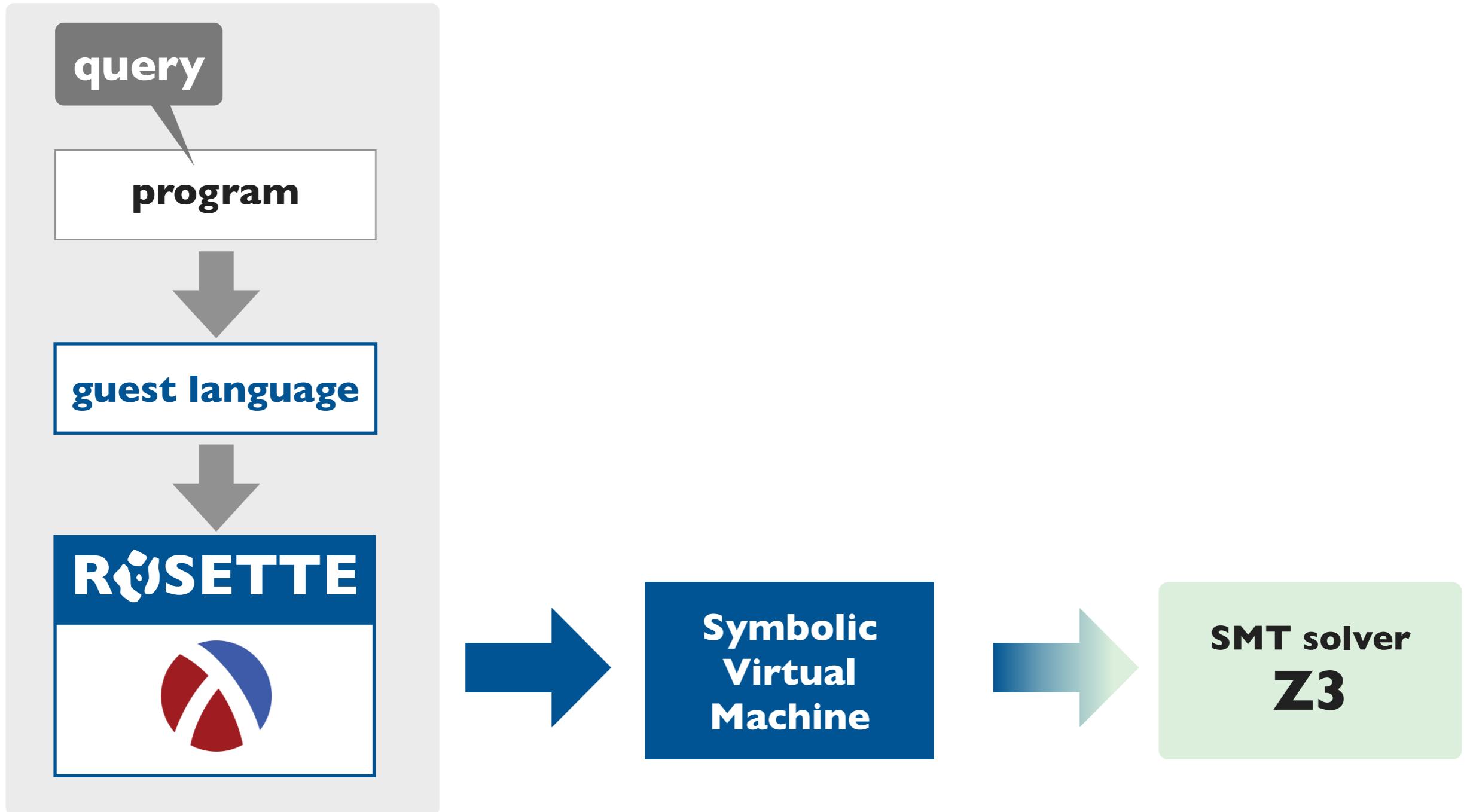


An easier way: tools as languages
How to build tools by stacking layers of languages.

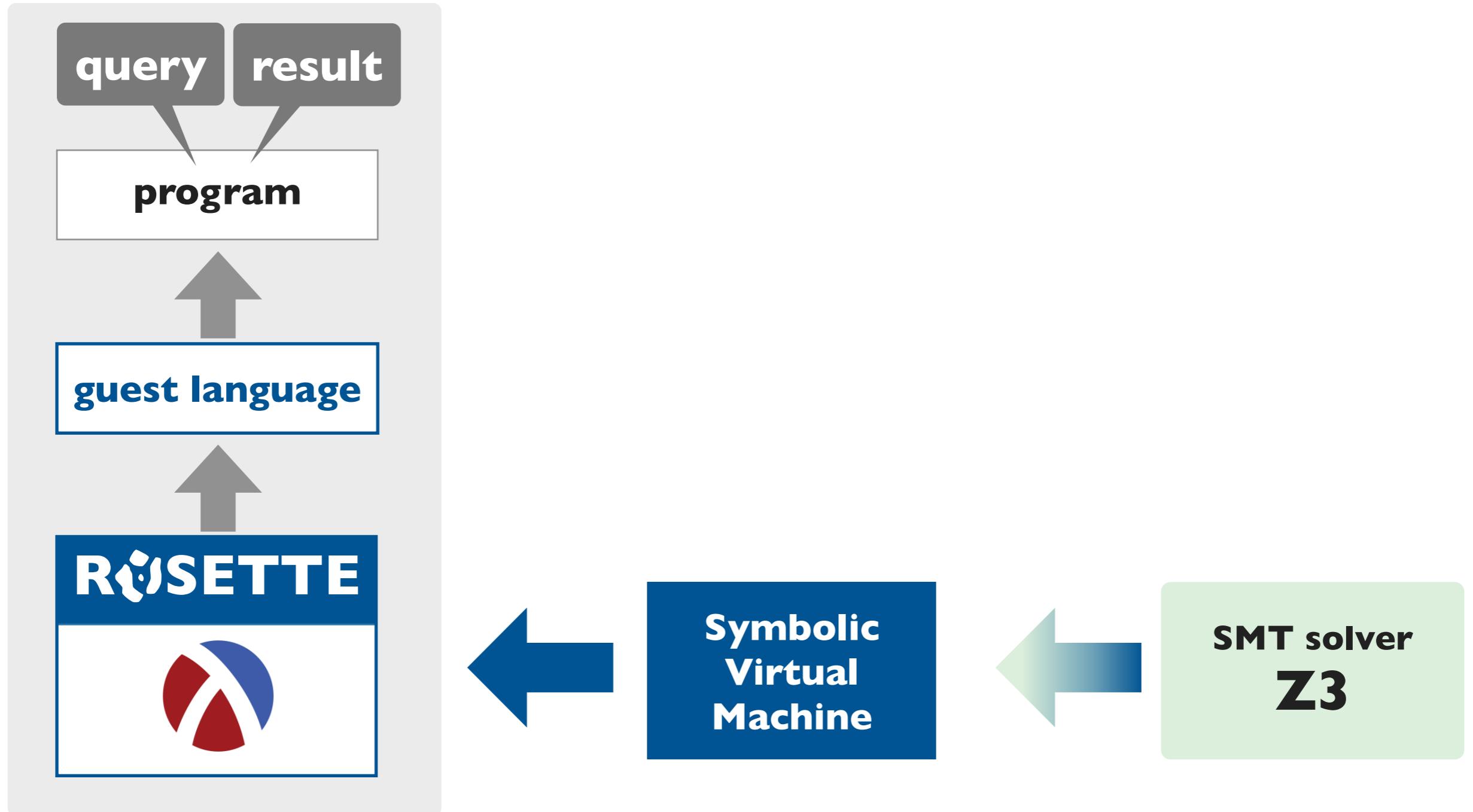
Behind the scenes: symbolic virtual machine
How Rosette works so you don't have to.

A last look: a few recent applications
Cool tools built with Rosette!

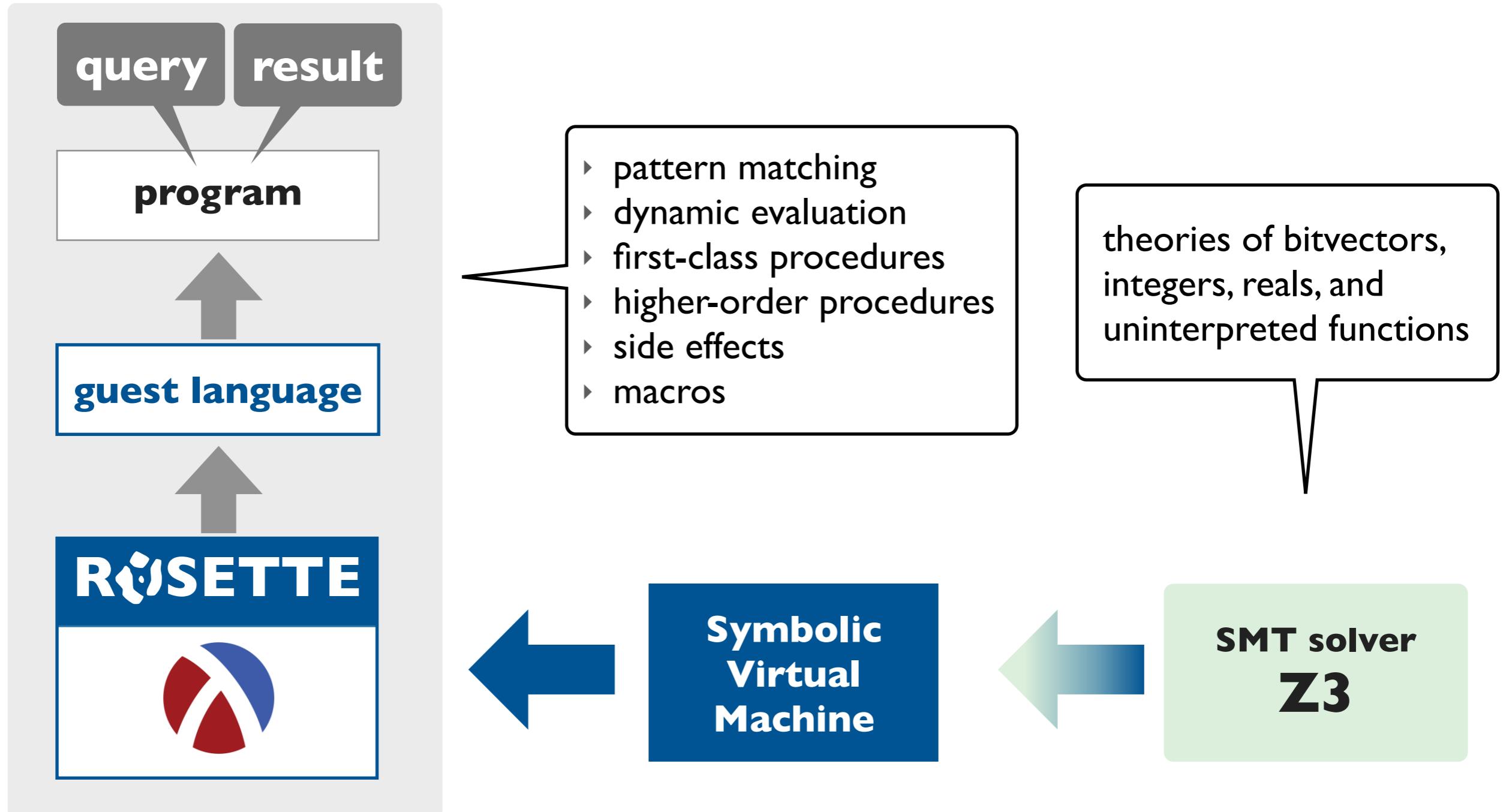
How it all works: a big picture view



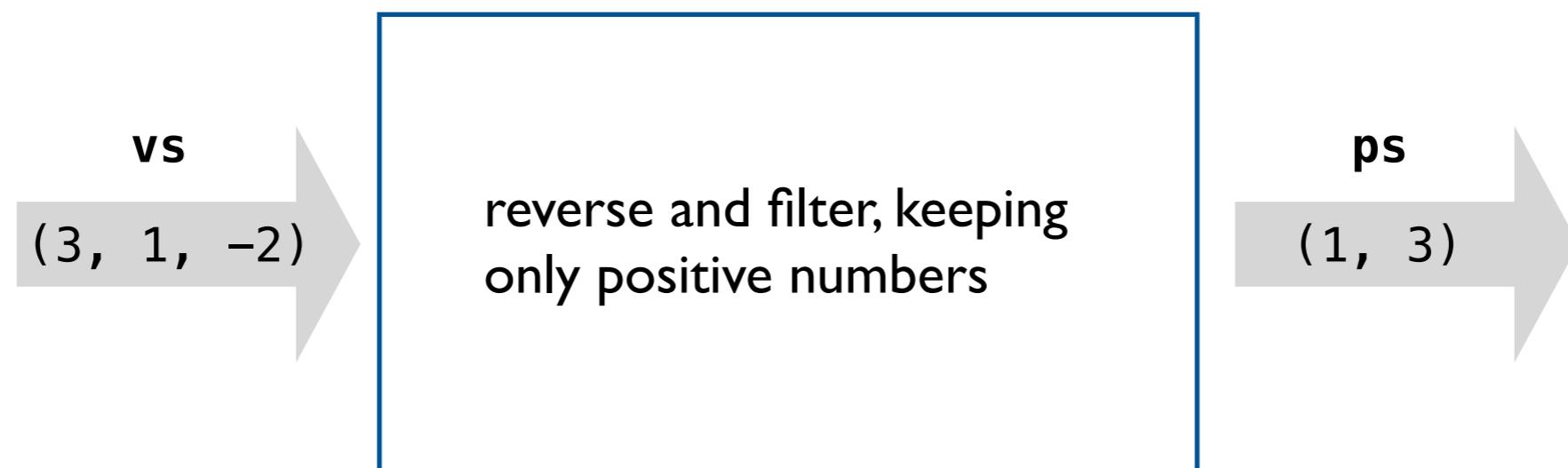
How it all works: a big picture view



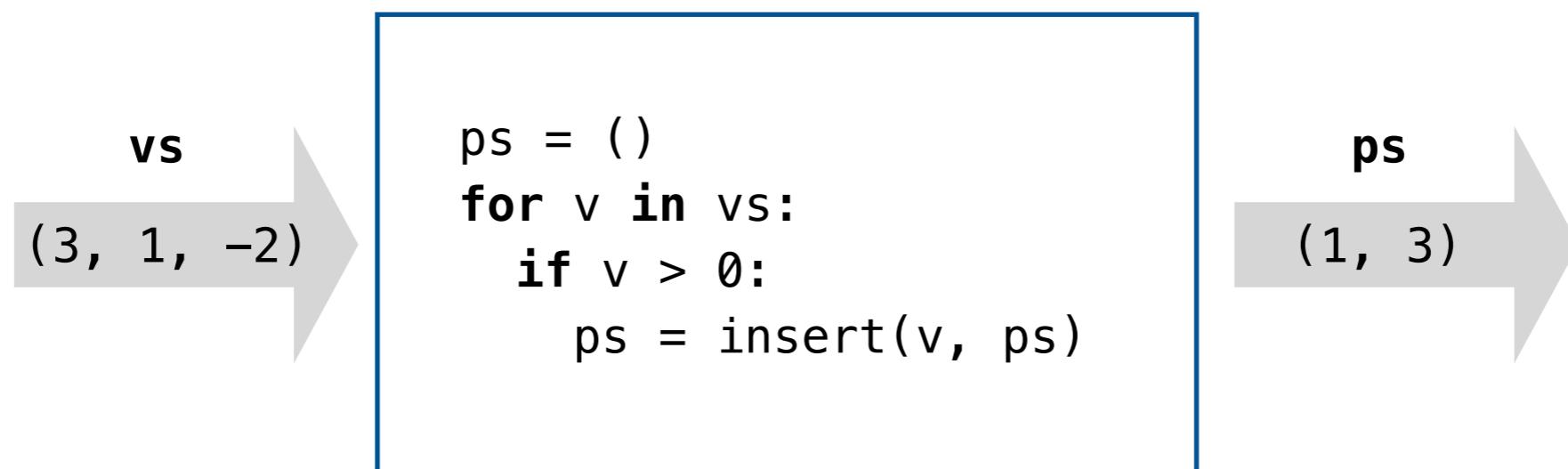
How it all works: a big picture view



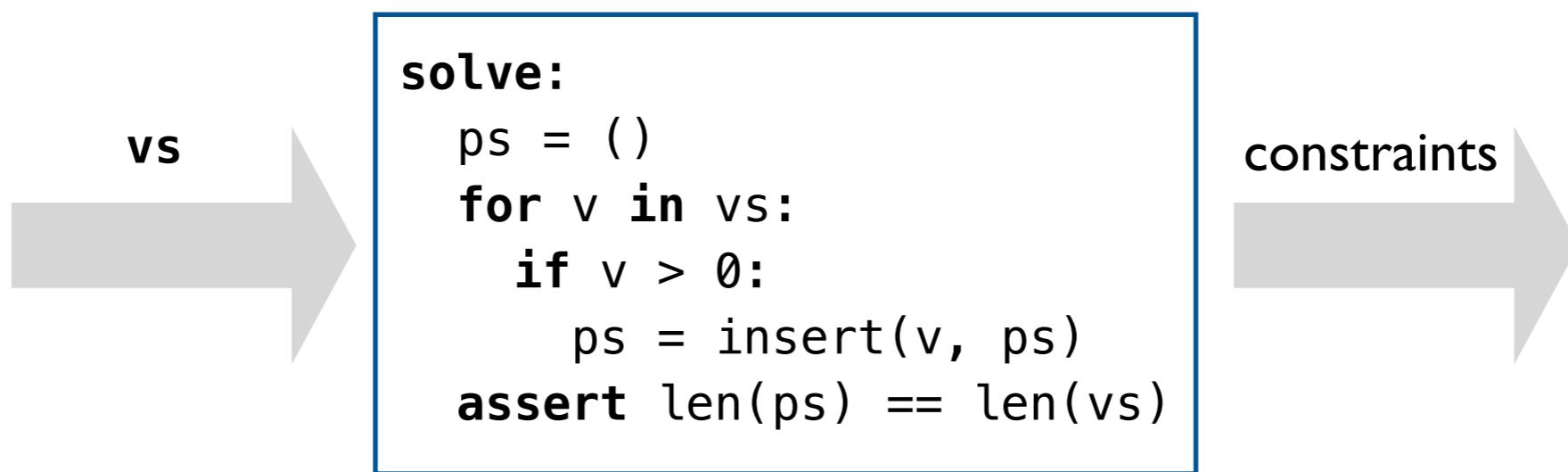
Translation to constraints by example



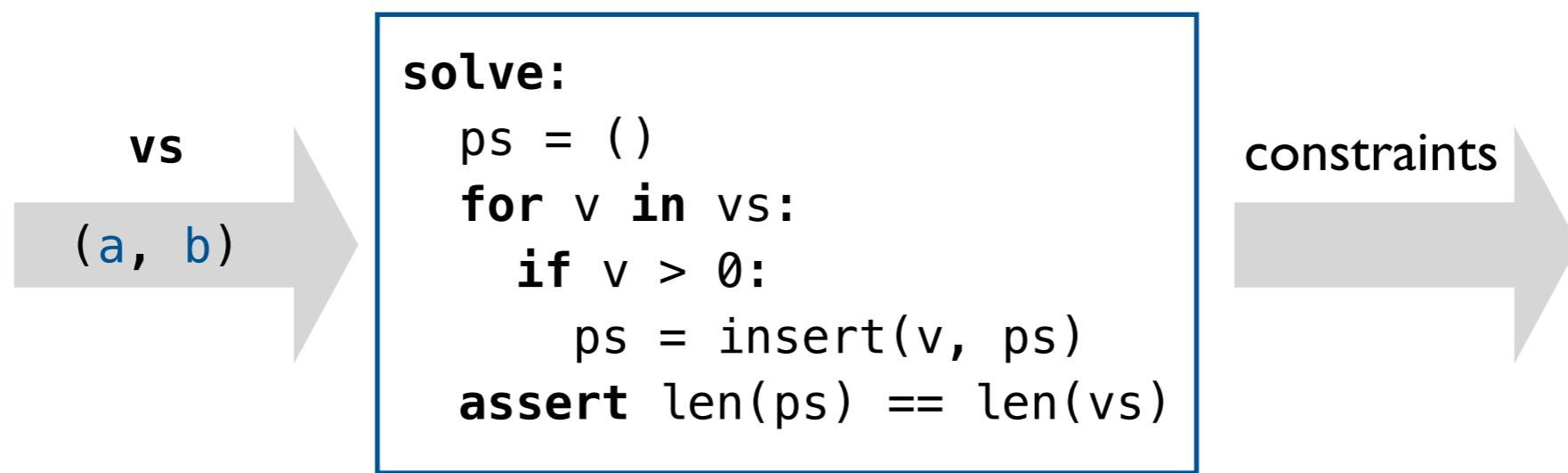
Translation to constraints by example



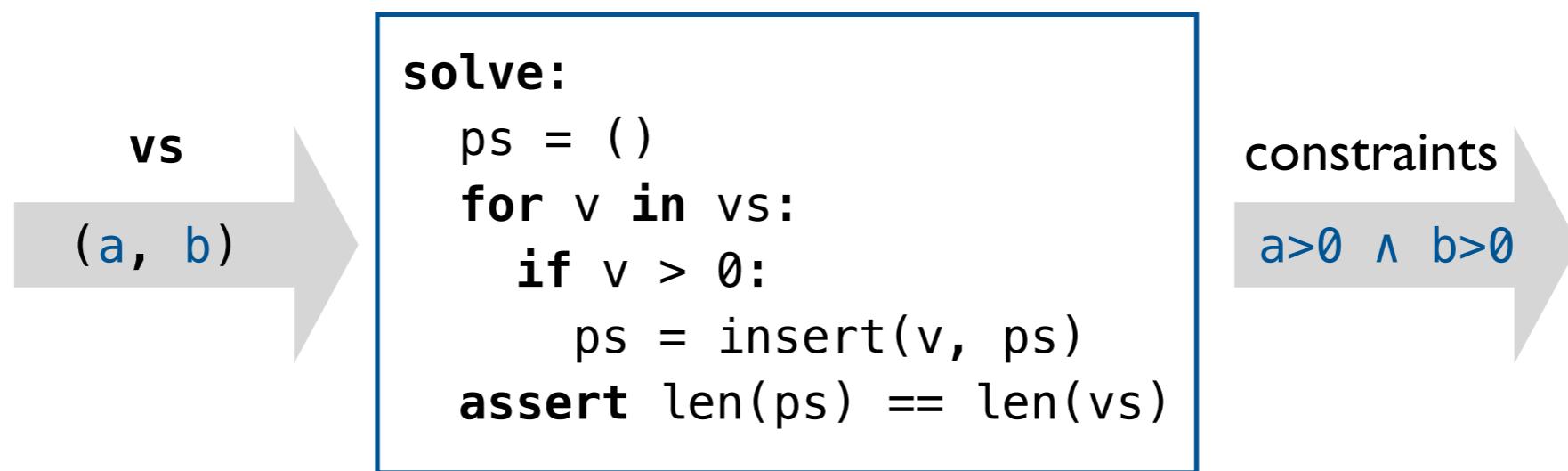
Translation to constraints by example



Translation to constraints by example



Translation to constraints by example

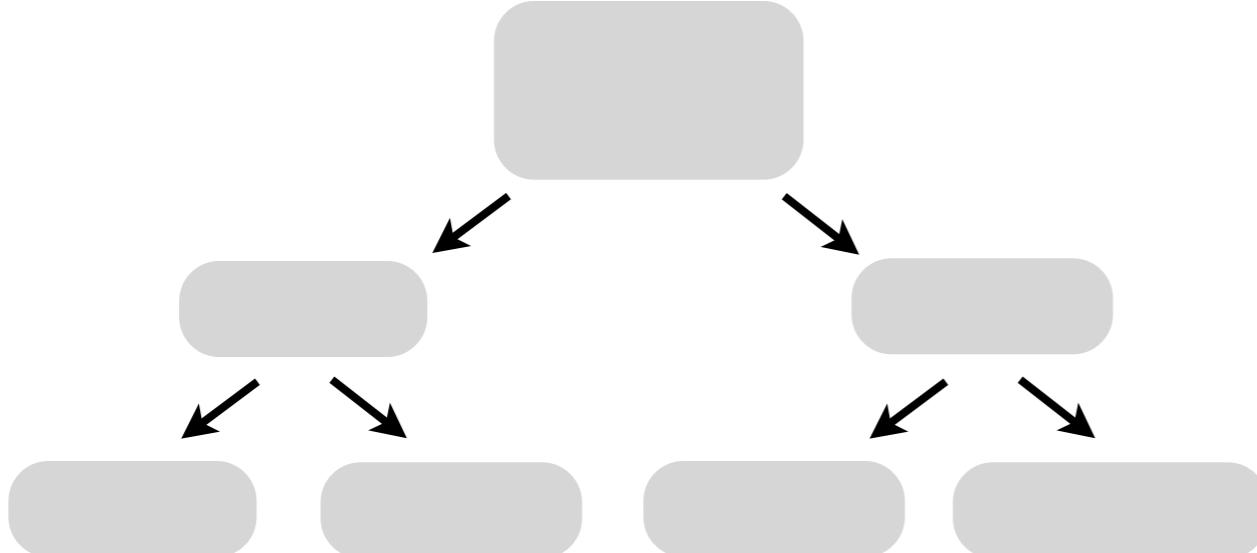


Design space of precise symbolic encodings

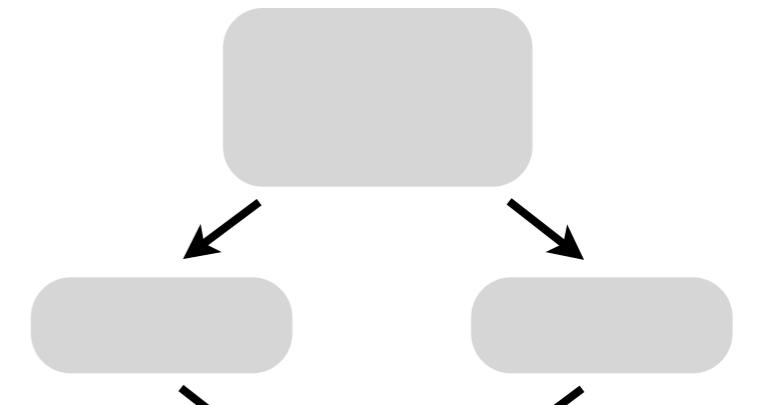
solve:

```
ps = ()  
for v in vs:  
    if v > 0:  
        ps = insert(v, ps)  
assert len(ps) == len(vs)
```

symbolic execution



bounded model checking



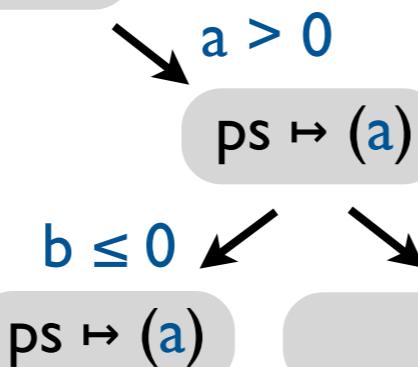
Design space of precise symbolic encodings

solve:

```
ps = ()  
for v in vs:  
    if v > 0:  
        ps = insert(v, ps)  
assert len(ps) == len(vs)
```

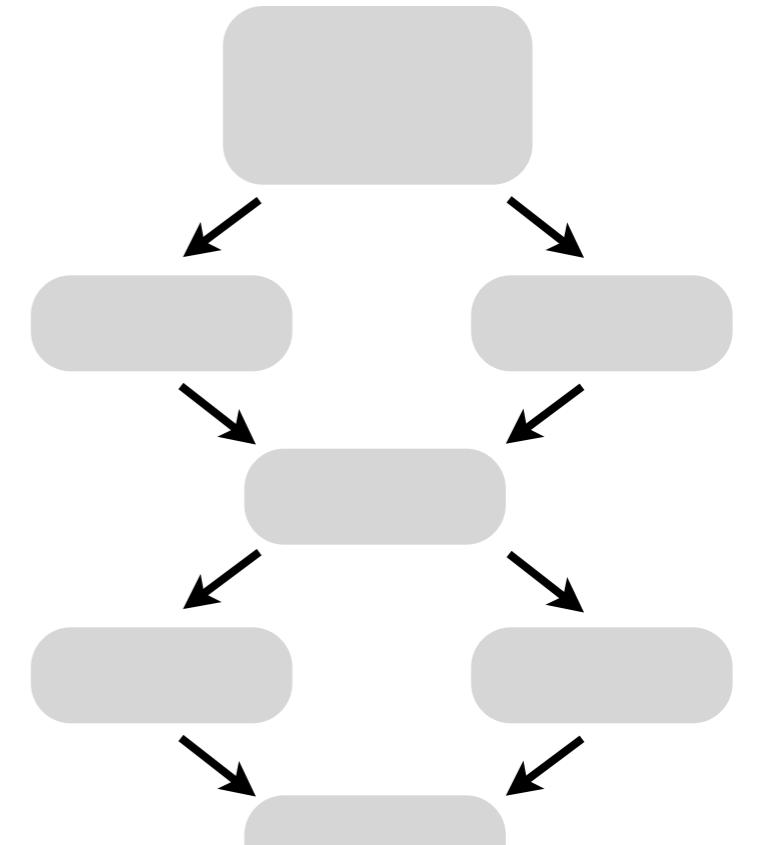
symbolic execution

$vs \mapsto (a, b)$
 $ps \mapsto ()$



$$\left\{ \begin{array}{l} a > 0 \\ b \leq 0 \\ \text{false} \end{array} \right\}$$

bounded model checking



Design space of precise symbolic encodings

solve:

```
ps = ()  
for v in vs:  
    if v > 0:  
        ps = insert(v, ps)  
assert len(ps) == len(vs)
```

symbolic execution

$vs \mapsto (a, b)$
 $ps \mapsto ()$

$a \leq 0$
 $ps \mapsto ()$

$a > 0$
 $ps \mapsto (a)$

$b \leq 0$
 $ps \mapsto ()$

$b > 0$
 $ps \mapsto (b)$

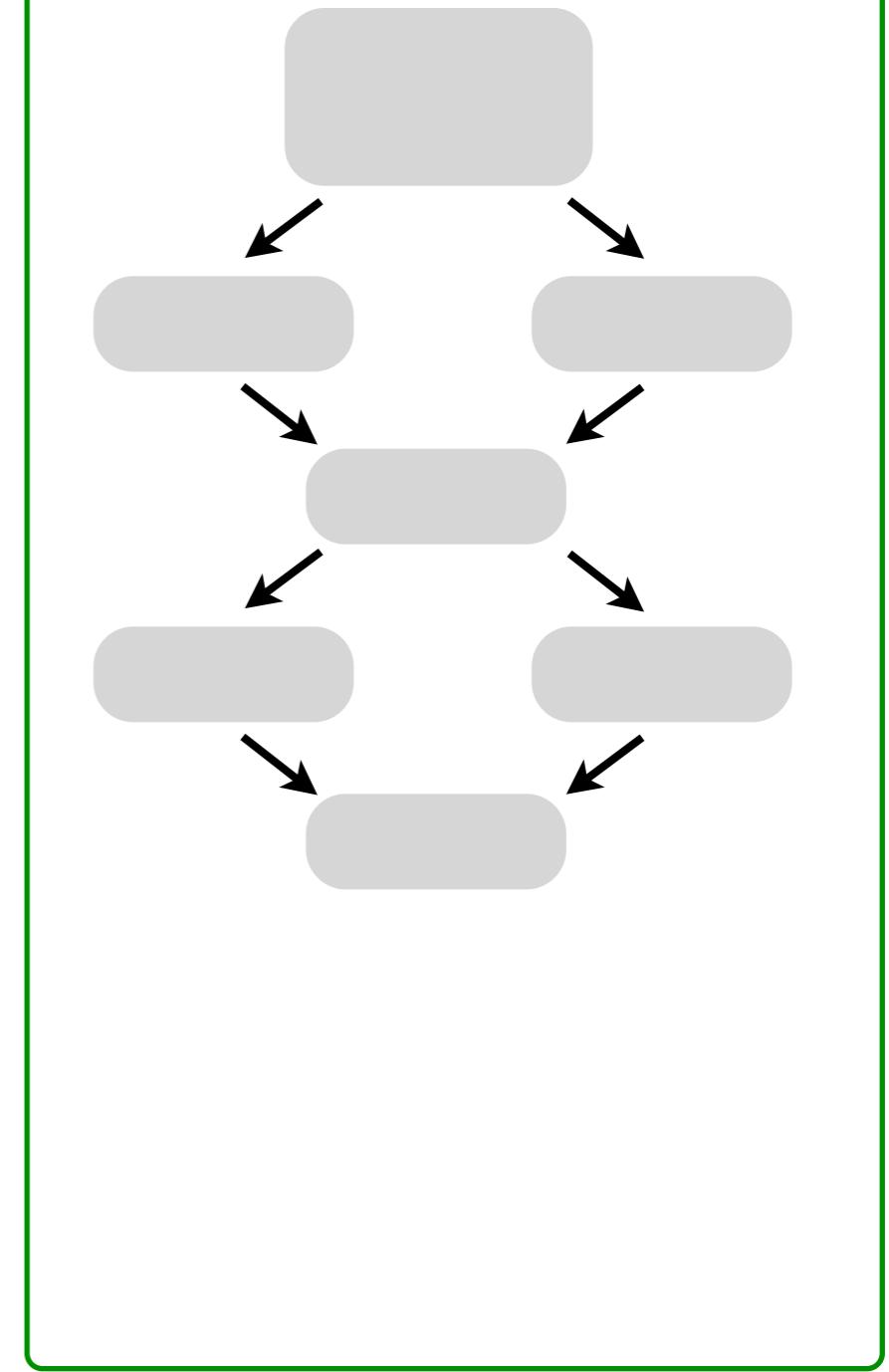
$b \leq 0$
 $ps \mapsto (a)$

$b > 0$
 $ps \mapsto (b, a)$

$$\left\{ \begin{array}{l} a \leq 0 \\ b \leq 0 \end{array} \right\} \vee \left\{ \begin{array}{l} a \leq 0 \\ b > 0 \end{array} \right\} \vee \left\{ \begin{array}{l} a > 0 \\ b \leq 0 \end{array} \right\} \vee \left\{ \begin{array}{l} a > 0 \\ b > 0 \end{array} \right\}$$

false true

bounded model checking



Design space of precise symbolic encodings

solve:

```
ps = ()  
for v in vs:  
    if v > 0:  
        ps = insert(v, ps)  
assert len(ps) == len(vs)
```

symbolic execution

vs $\mapsto (a, b)$
ps $\mapsto ()$

a ≤ 0
ps $\mapsto ()$

a > 0
ps $\mapsto (a)$

b ≤ 0
ps $\mapsto ()$

b > 0
ps $\mapsto (b)$

b ≤ 0
ps $\mapsto (a)$

b > 0
ps $\mapsto (b, a)$

$$\left\{ \begin{array}{l} a \leq 0 \\ b \leq 0 \end{array} \right\} \vee \left\{ \begin{array}{l} a \leq 0 \\ b > 0 \end{array} \right\} \vee \left\{ \begin{array}{l} a > 0 \\ b \leq 0 \end{array} \right\} \vee \left\{ \begin{array}{l} a > 0 \\ b > 0 \end{array} \right\}$$

bounded model checking

vs $\mapsto (a, b)$
ps $\mapsto ()$

a ≤ 0 a > 0
ps $\mapsto ()$ ps $\mapsto (a)$

ps $\mapsto ps_0$

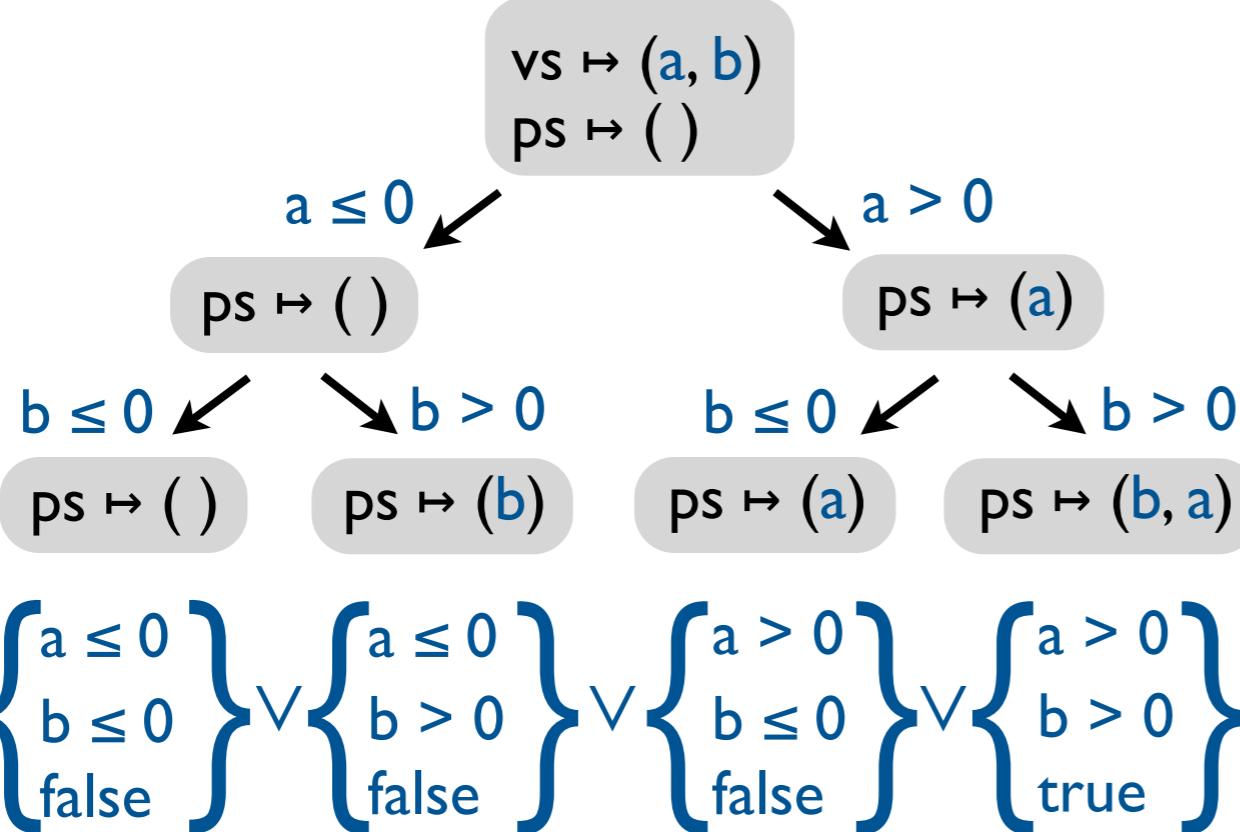
ps₀ = ite(a > 0, (a), ())

Design space of precise symbolic encodings

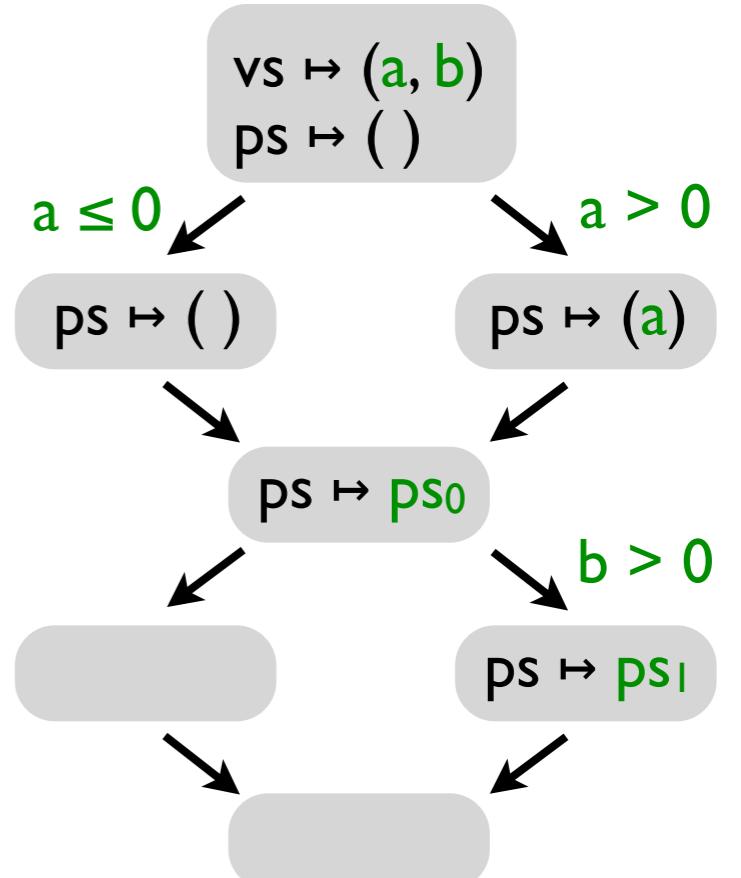
solve:

```
ps = ()  
for v in vs:  
    if v > 0:  
        ps = insert(v, ps)  
assert len(ps) == len(vs)
```

symbolic execution



bounded model checking



$$\begin{aligned} ps_0 &= \text{ite}(a > 0, (a), ()) \\ ps_1 &= \text{insert}(b, ps_0) \end{aligned}$$

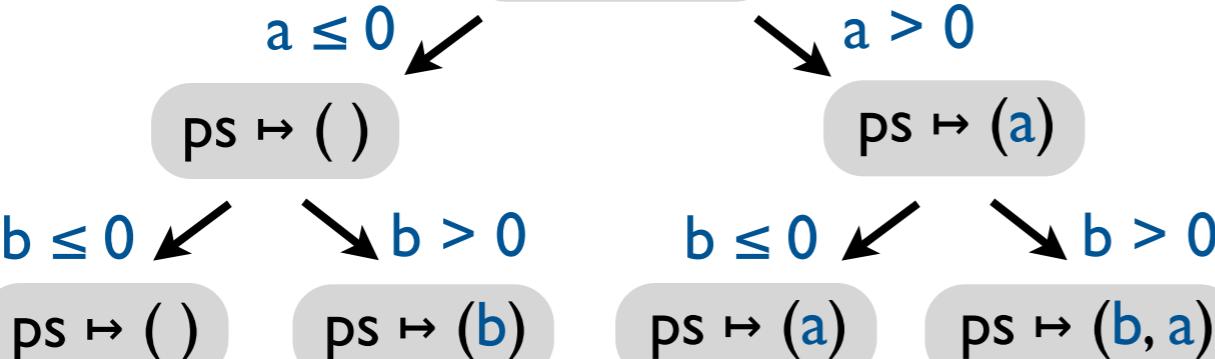
Design space of precise symbolic encodings

solve:

```
ps = ()  
for v in vs:  
    if v > 0:  
        ps = insert(v, ps)  
assert len(ps) == len(vs)
```

symbolic execution

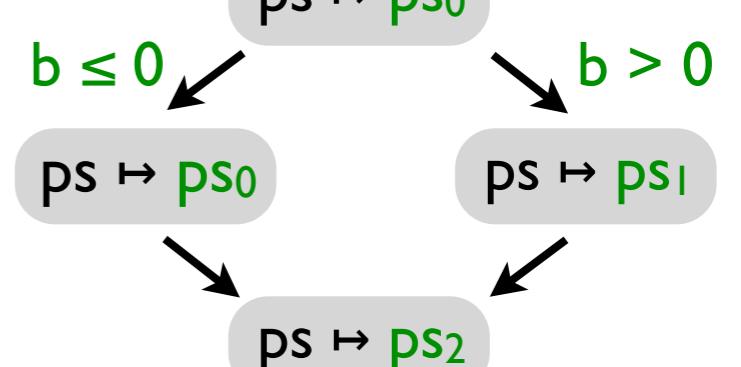
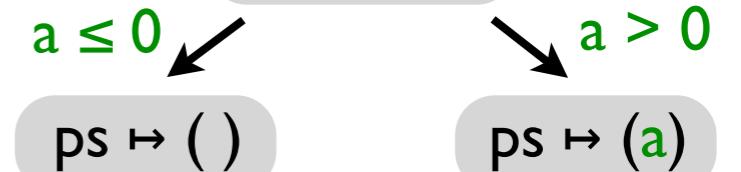
vs $\mapsto (a, b)$
ps $\mapsto ()$



$$\left\{ \begin{array}{l} a \leq 0 \\ b \leq 0 \end{array} \right\} \vee \left\{ \begin{array}{l} a \leq 0 \\ b > 0 \end{array} \right\} \vee \left\{ \begin{array}{l} a > 0 \\ b \leq 0 \end{array} \right\} \vee \left\{ \begin{array}{l} a > 0 \\ b > 0 \end{array} \right\}$$

bounded model checking

vs $\mapsto (a, b)$
ps $\mapsto ()$



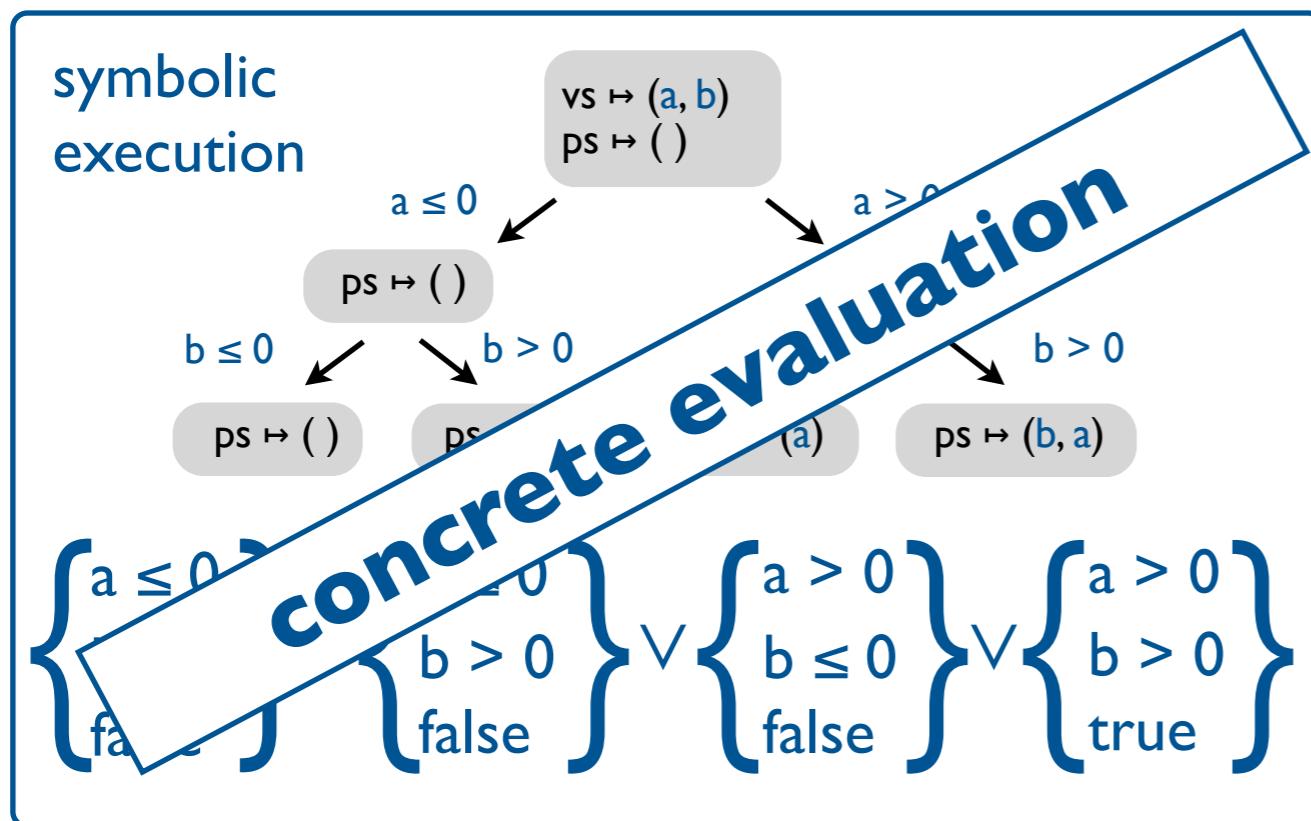
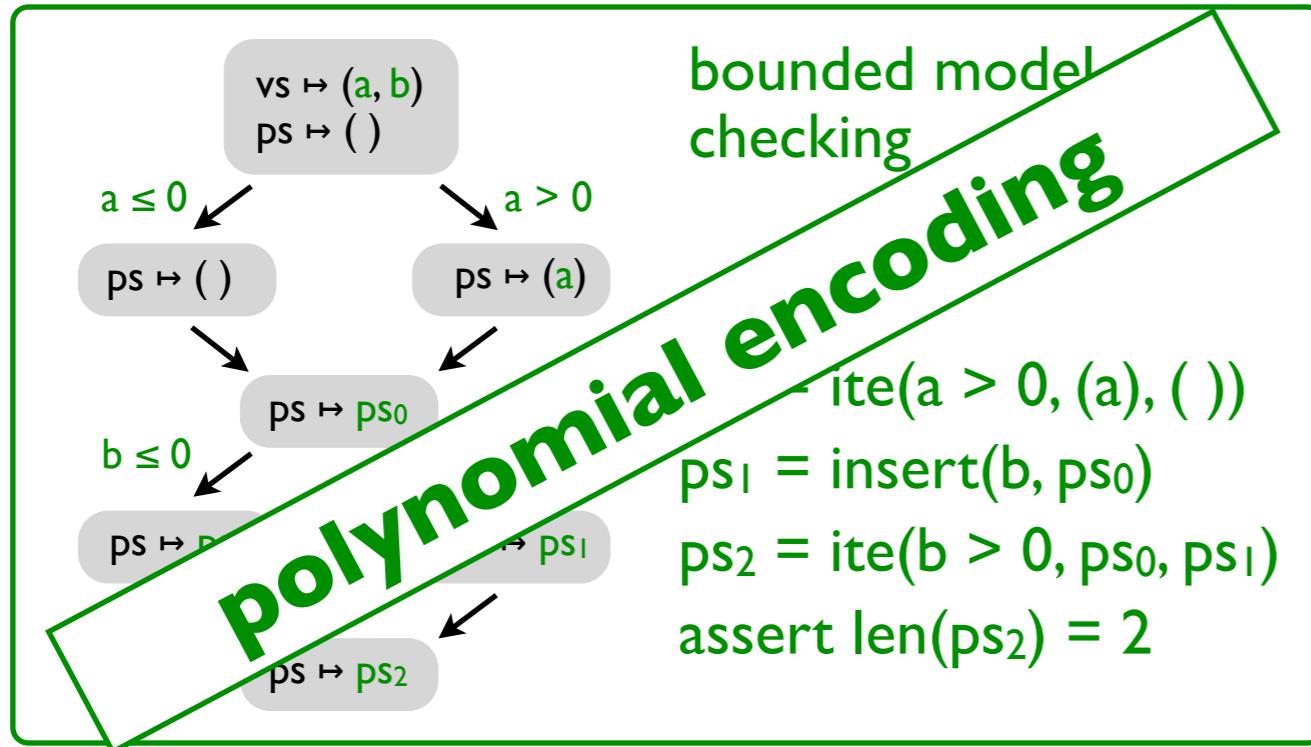
ps₀ = ite(a > 0, (a), ())

ps₁ = insert(b, ps₀)

ps₂ = ite(b > 0, ps₀, ps₁)

assert len(ps₂) = 2

Challenge: simple vs compact encoding (SE and BMC)

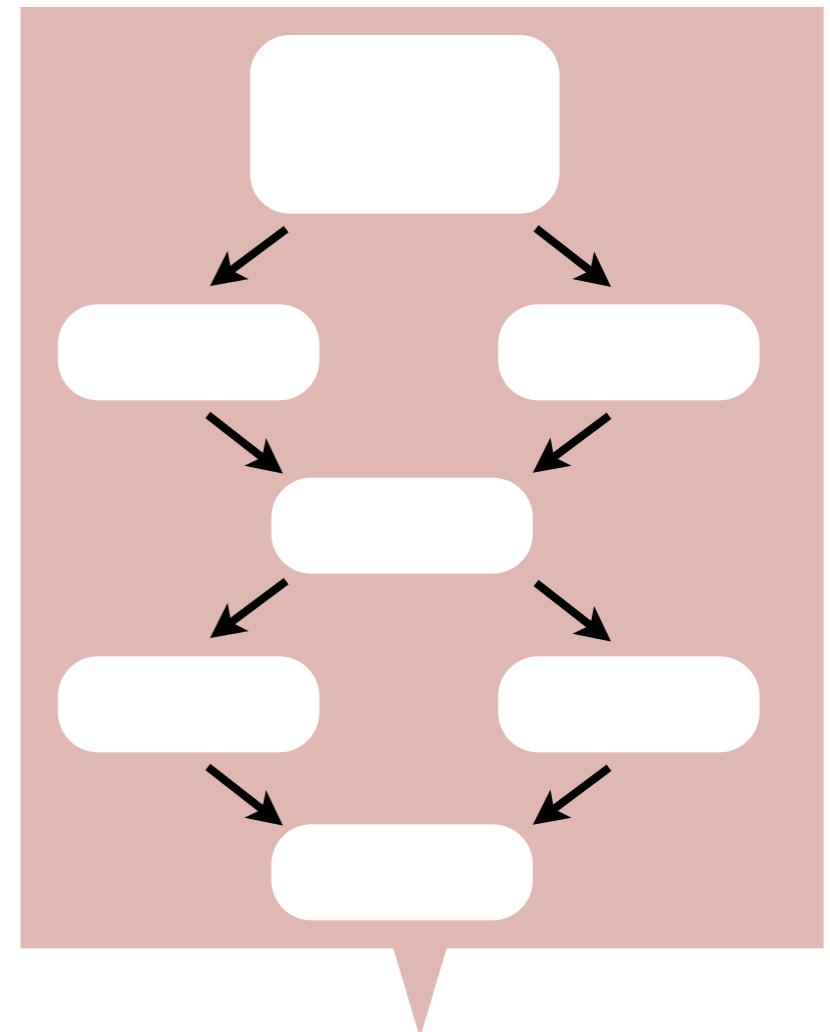


Can we have both a polynomially sized encoding (like BMC) and concrete evaluation of complex operations (like SE)?

Solution: type-driven state merging

solve:

```
ps = ()  
for v in vs:  
    if v > 0:  
        ps = insert(v, ps)  
assert len(ps) == len(vs)
```



$$\left\{ \begin{array}{l} a > 0 \\ b > 0 \\ \text{true} \end{array} \right\}$$



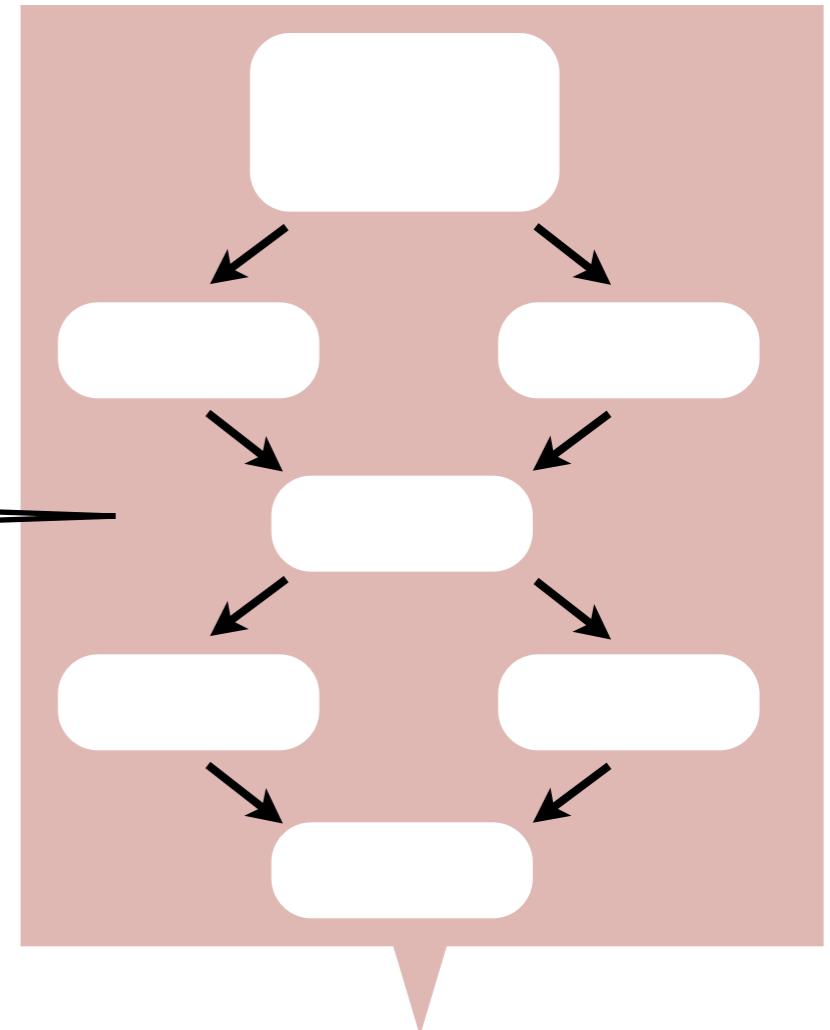
Solution: type-driven state merging

solve:

```
ps = ()  
for v in vs:  
    if v > 0:  
        ps = insert(v, ps)  
assert len(ps) == len(vs)
```

Merge instances of

- primitive types: symbolically
- value types: structurally
- all other types: via unions



$$\left\{ \begin{array}{l} a > 0 \\ b > 0 \\ \text{true} \end{array} \right\}$$



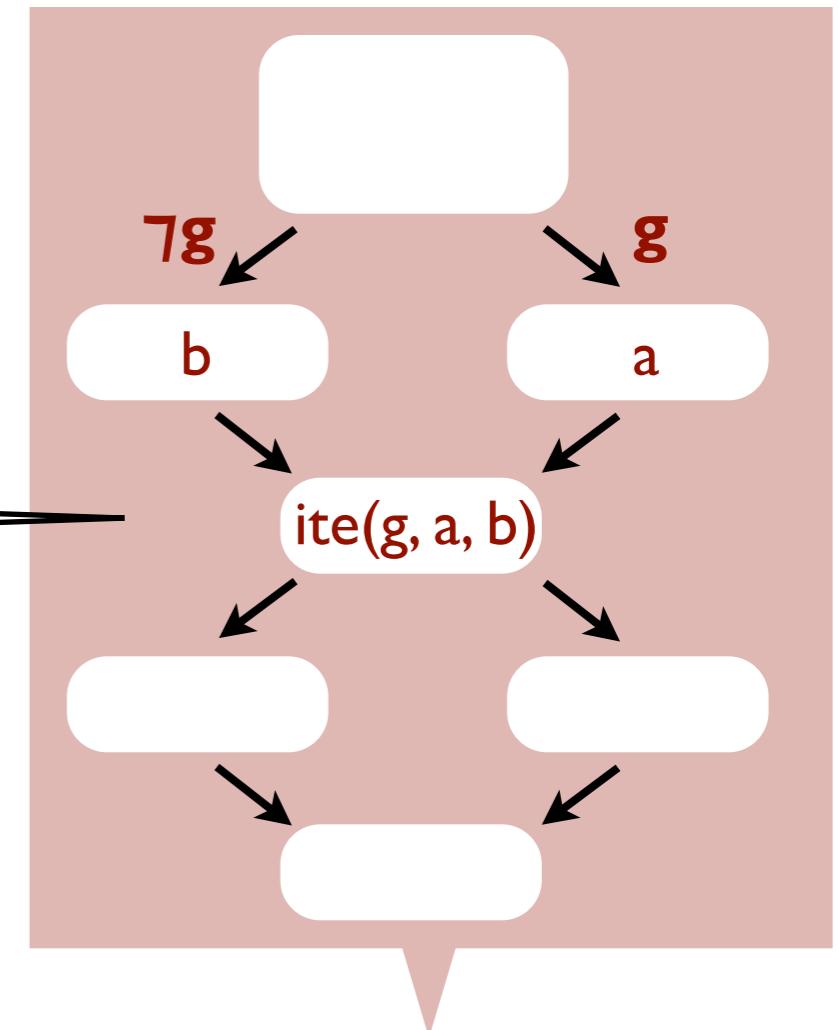
Solution: type-driven state merging

solve:

```
ps = ()  
for v in vs:  
    if v > 0:  
        ps = insert(v, ps)  
assert len(ps) == len(vs)
```

Merge instances of

- ▶ primitive types: symbolically
- ▶ value types: structurally
- ▶ all other types: via unions



$$\left\{ \begin{array}{l} a > 0 \\ b > 0 \\ \text{true} \end{array} \right\}$$



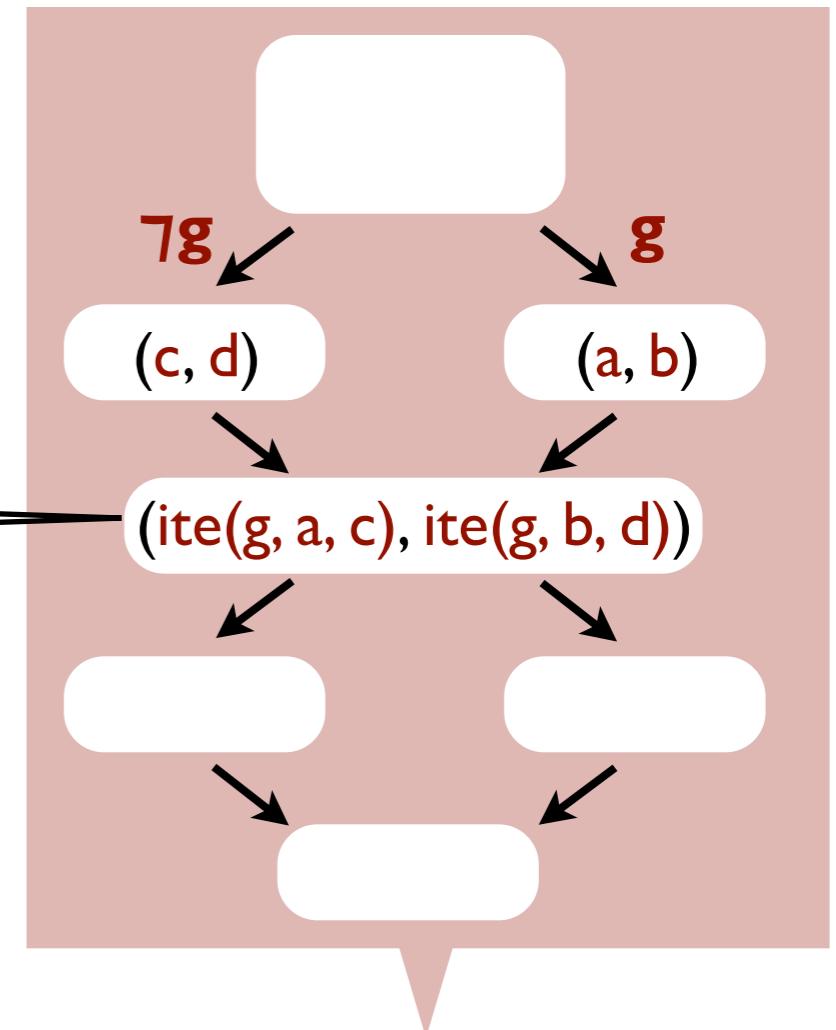
Solution: type-driven state merging

solve:

```
ps = ()  
for v in vs:  
    if v > 0:  
        ps = insert(v, ps)  
assert len(ps) == len(vs)
```

Merge instances of

- ▶ primitive types: symbolically
- ▶ value types: structurally
- ▶ all other types: via unions



$$\left\{ \begin{array}{l} a > 0 \\ b > 0 \\ \text{true} \end{array} \right\}$$



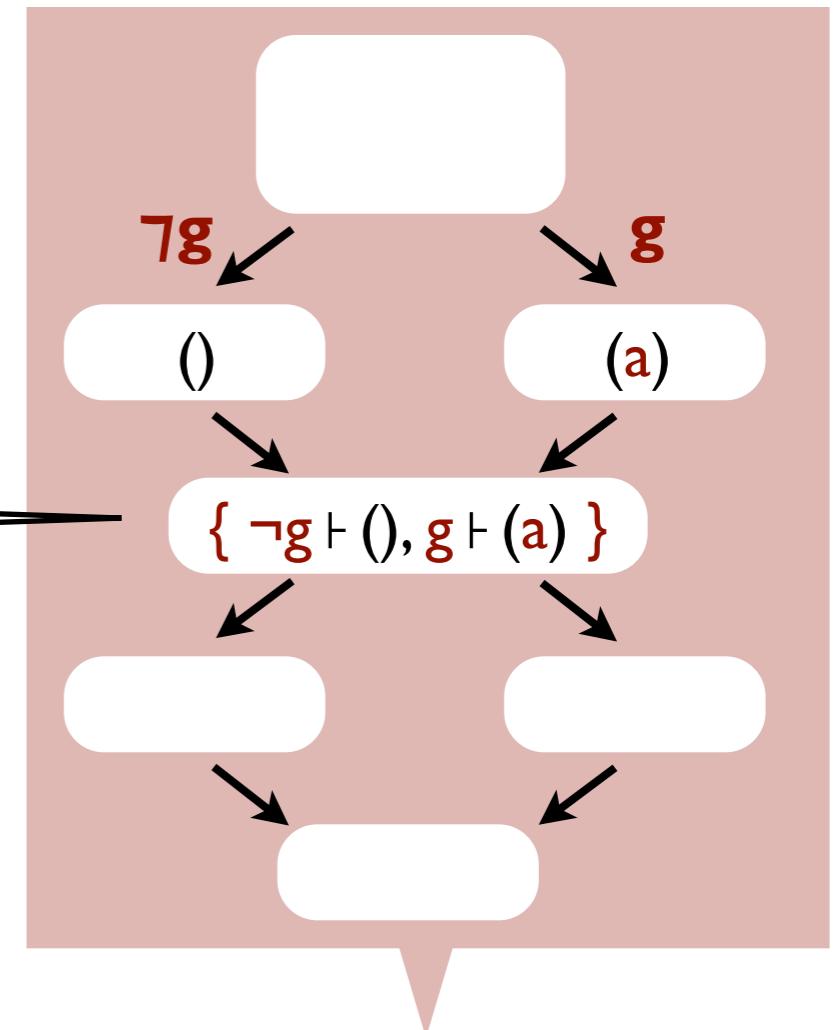
Solution: type-driven state merging

solve:

```
ps = ()  
for v in vs:  
    if v > 0:  
        ps = insert(v, ps)  
assert len(ps) == len(vs)
```

Merge instances of

- ▶ primitive types: symbolically
- ▶ value types: structurally
- ▶ all other types: via unions



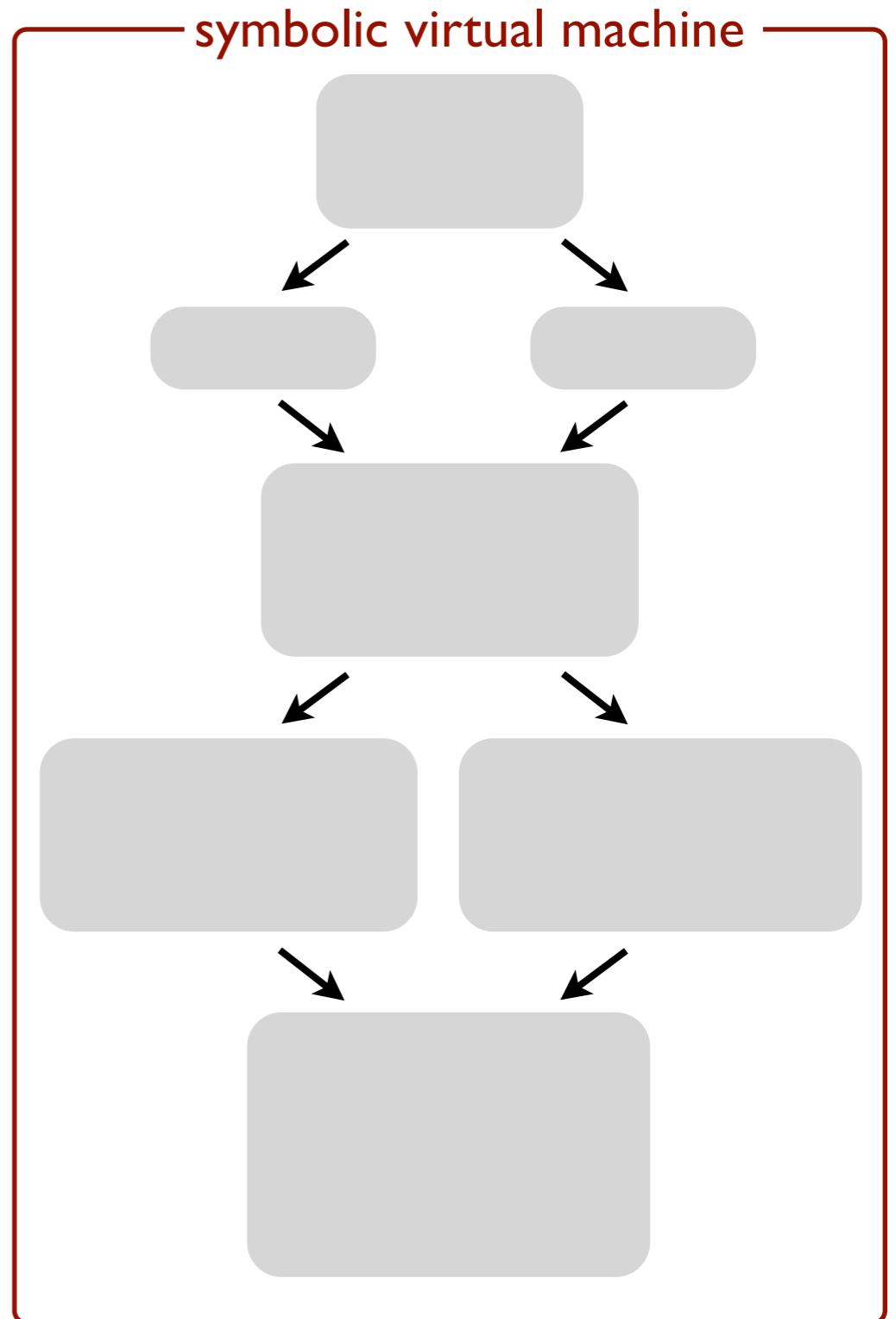
$$\left\{ \begin{array}{l} a > 0 \\ b > 0 \\ \text{true} \end{array} \right\}$$



Solution: type-driven state merging

solve:

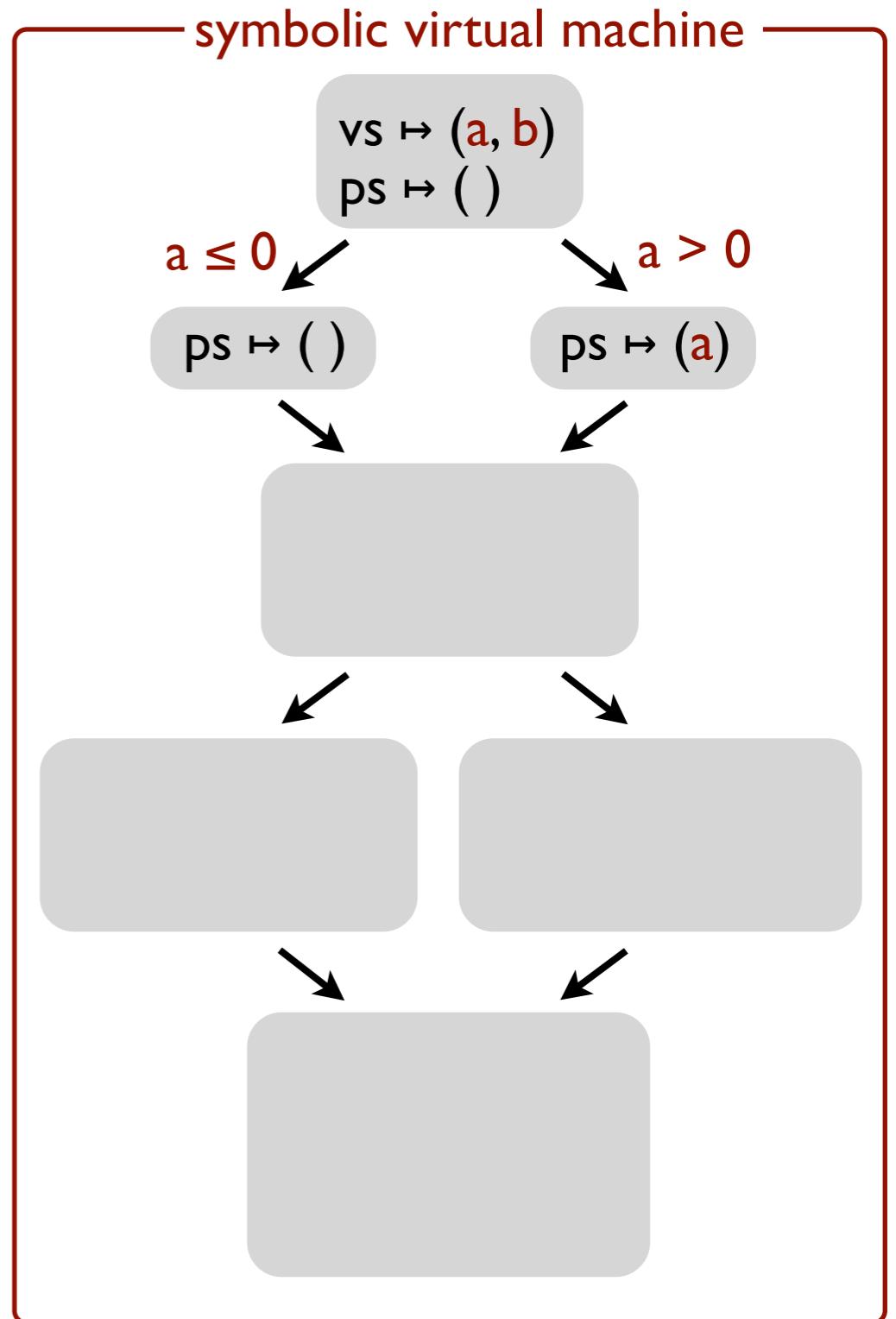
```
ps = ()  
for v in vs:  
    if v > 0:  
        ps = insert(v, ps)  
assert len(ps) == len(vs)
```



Solution: type-driven state merging

solve:

```
ps = ()  
for v in vs:  
    if v > 0:  
        ps = insert(v, ps)  
assert len(ps) == len(vs)
```



Solution: type-driven state merging

solve:

```
ps = ()  
for v in vs:  
    if v > 0:  
        ps = insert(v, ps)  
assert len(ps) == len(vs)
```

Symbolic union: a set of
guarded values, with
disjoint guards.

$g_0 = a > 0$

symbolic virtual machine

$vs \mapsto (a, b)$
 $ps \mapsto ()$

$\neg g_0$

$ps \mapsto ()$

g_0

$ps \mapsto (a)$

$ps \mapsto \{ g_0 \vdash (a),$
 $\neg g_0 \vdash () \}$

$ps \mapsto \{ \}$

$ps \mapsto \{ \}$

$ps \mapsto \{ \}$

$ps \mapsto \{ \}$

Solution: type-driven state merging

```
solve:  
ps = ()  
for v in vs:  
    if v > 0:  
        ps = insert(v, ps)  
assert len(ps) == len(vs)
```

Execute insert concretely on all lists in the union.

$$\begin{aligned}g_0 &= a > 0 \\g_1 &= b > 0\end{aligned}$$

symbolic virtual machine

$$\begin{aligned}vs &\mapsto (a, b) \\ps &\mapsto ()\end{aligned}$$

$$\begin{aligned}\neg g_0 \swarrow && \searrow g_0 \\ps &\mapsto () & ps \mapsto (a)\end{aligned}$$

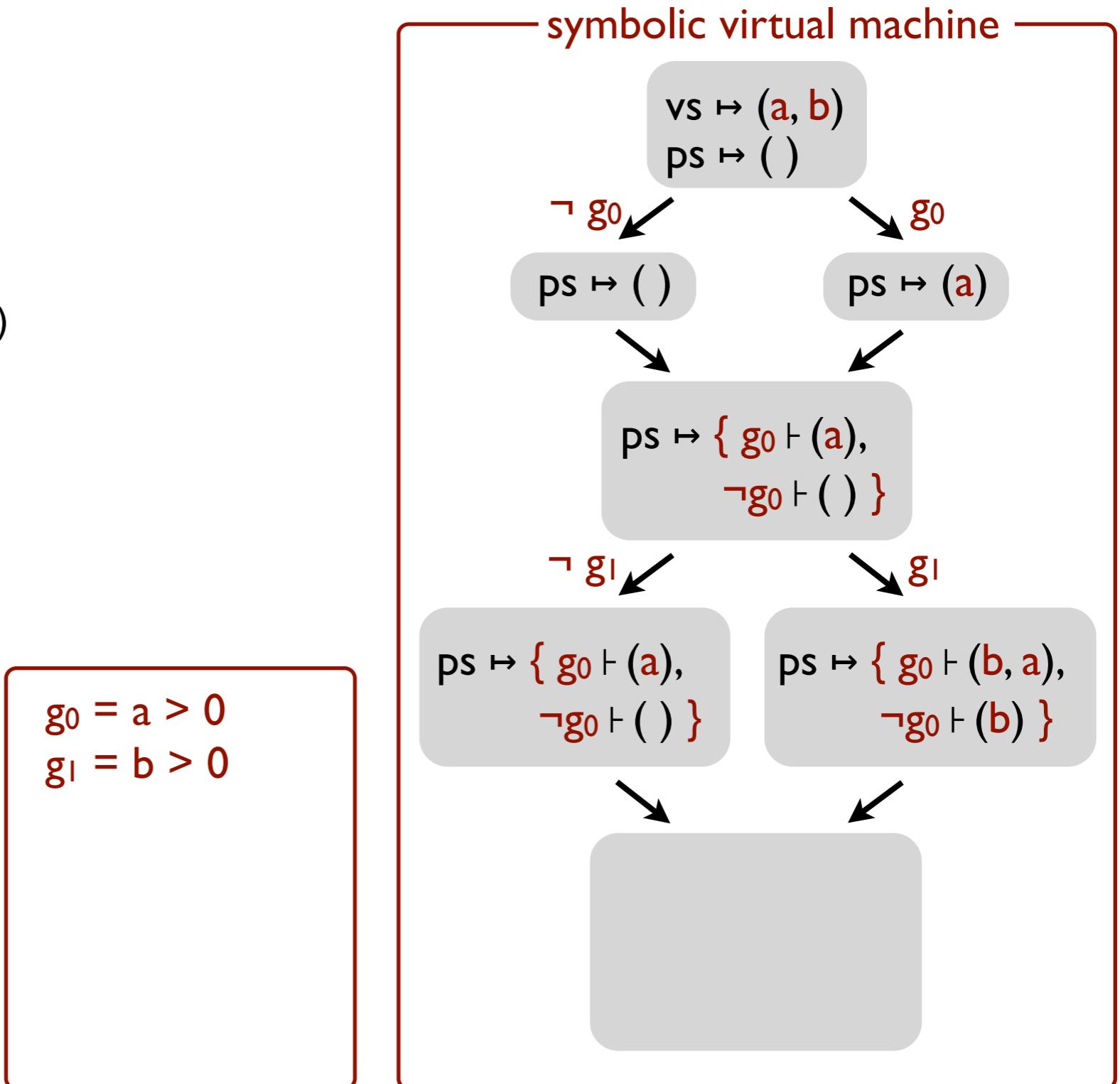
$$ps \mapsto \{ g_0 \vdash (a), \neg g_0 \vdash () \}$$

$$\begin{aligned}\swarrow && \searrow g_1 \\&& ps \mapsto \{ g_0 \vdash (b, a), \neg g_0 \vdash (b) \}\end{aligned}$$

Solution: type-driven state merging

solve:

```
ps = ()  
for v in vs:  
    if v > 0:  
        ps = insert(v, ps)  
assert len(ps) == len(vs)
```



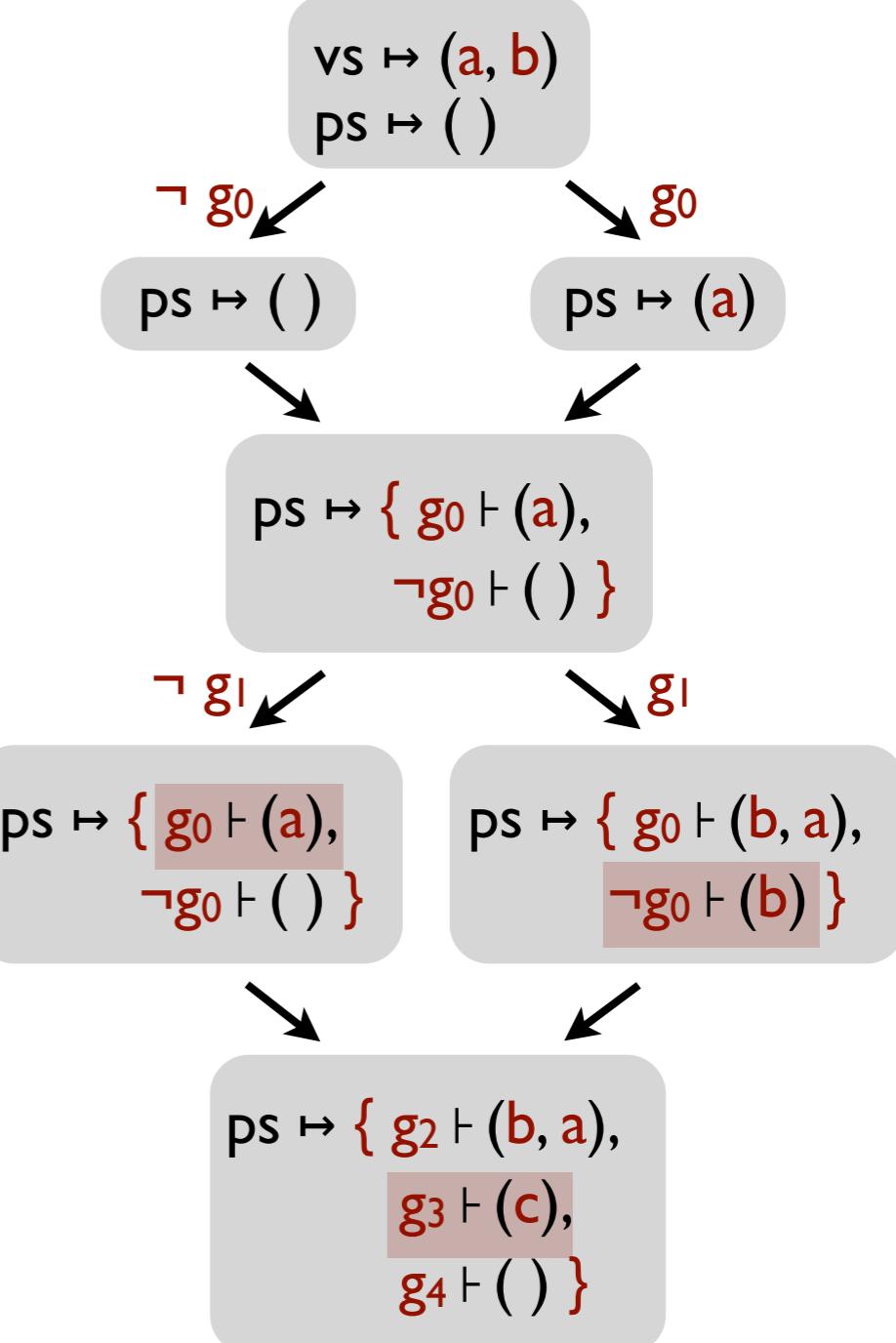
Solution: type-driven state merging

solve:

```
ps = ()  
for v in vs:  
    if v > 0:  
        ps = insert(v, ps)  
assert len(ps) == len(vs)
```

$g_0 = a > 0$
 $g_1 = b > 0$
 $g_2 = g_0 \wedge g_1$
 $g_3 = \neg(g_0 \Leftrightarrow g_1)$
 $g_4 = \neg g_0 \wedge \neg g_1$
 $c = \text{ite}(g_1, b, a)$

symbolic virtual machine



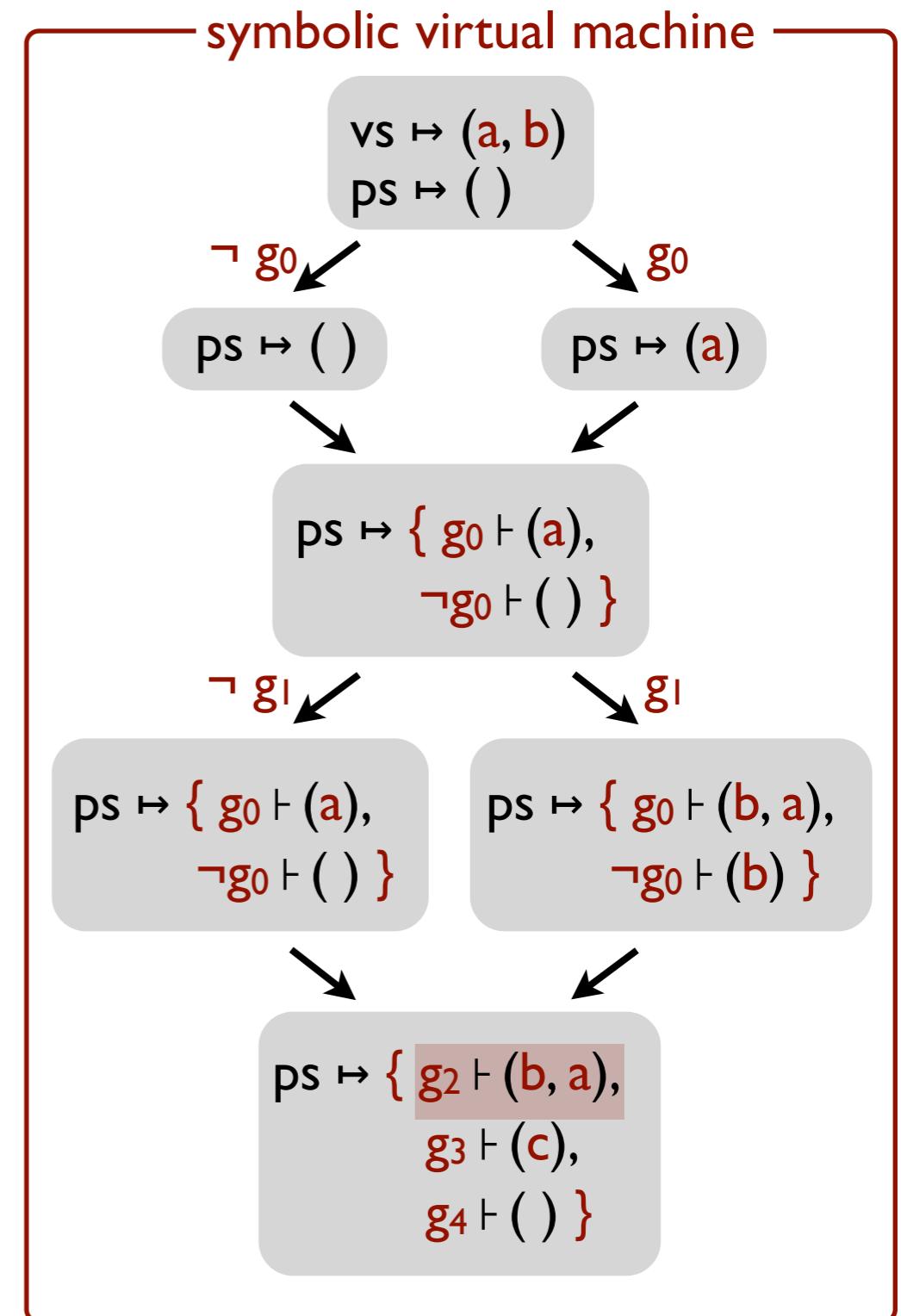
Solution: type-driven state merging

solve:

```
ps = ()  
for v in vs:  
    if v > 0:  
        ps = insert(v, ps)  
assert len(ps) == len(vs)
```

Evaluate `len` concretely
on all lists in the union;
assertion true only on
the list guarded by g_2 .

```
g0 = a > 0  
g1 = b > 0  
g2 = g0 ∧ g1  
g3 = ¬(g0 ⇔ g1)  
g4 = ¬g0 ∧ ¬g1  
c = ite(g1, b, a)  
assert g2
```



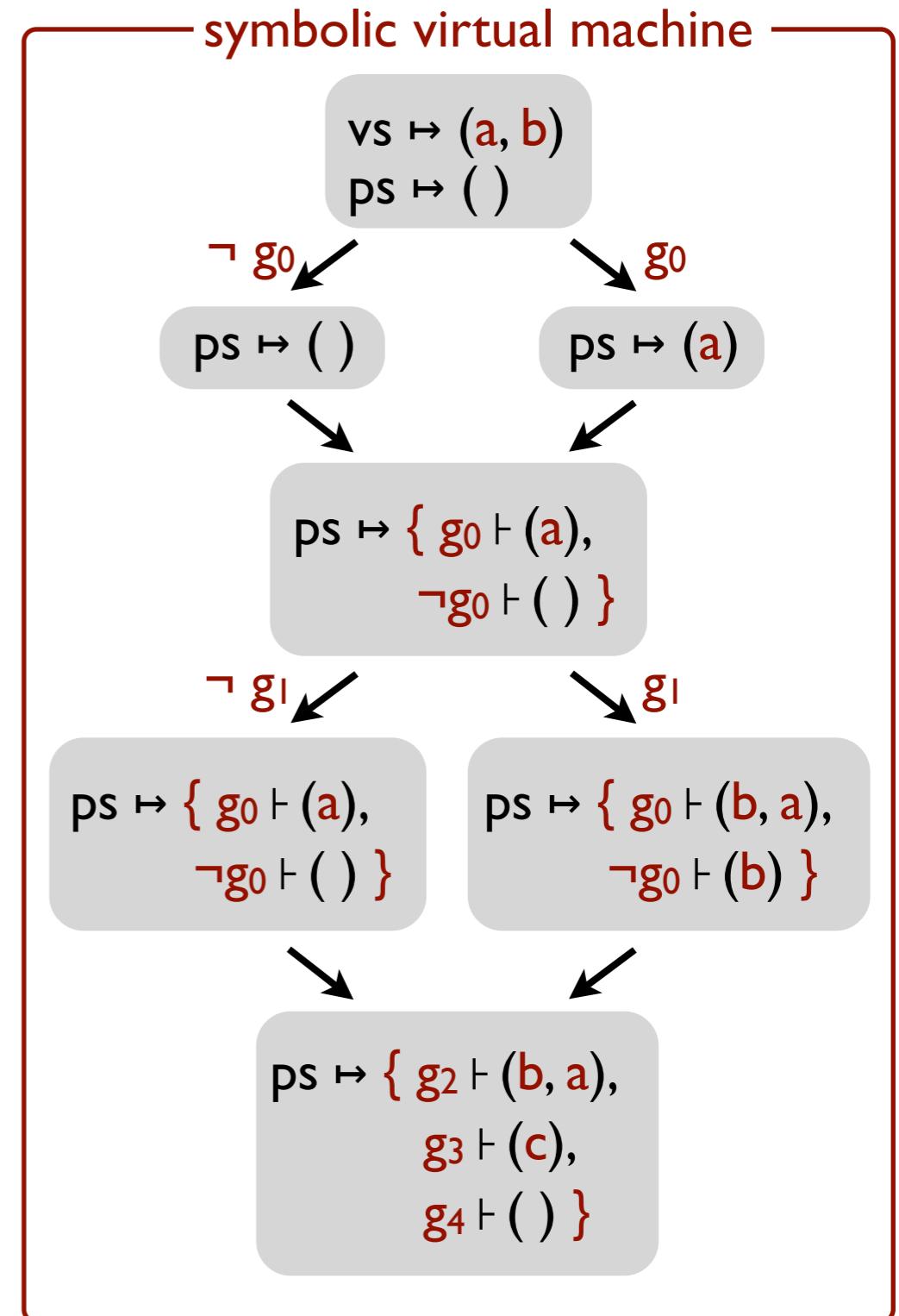
Solution: type-driven state merging

solve:

```
ps = ()  
for v in vs:  
    if v > 0:  
        ps = insert(v, ps)  
assert len(ps) == len(vs)
```

polynomial encoding
concrete evaluation

```
g0 = a > 0  
g1 = b > 0  
g2 = g0 ∧ g1  
g3 = ¬(g0 ⇔ g1)  
g4 = ¬g0 ∧ ¬g1  
c = ite(g1, b, a)  
assert g2
```



Solution: type-driven state merging

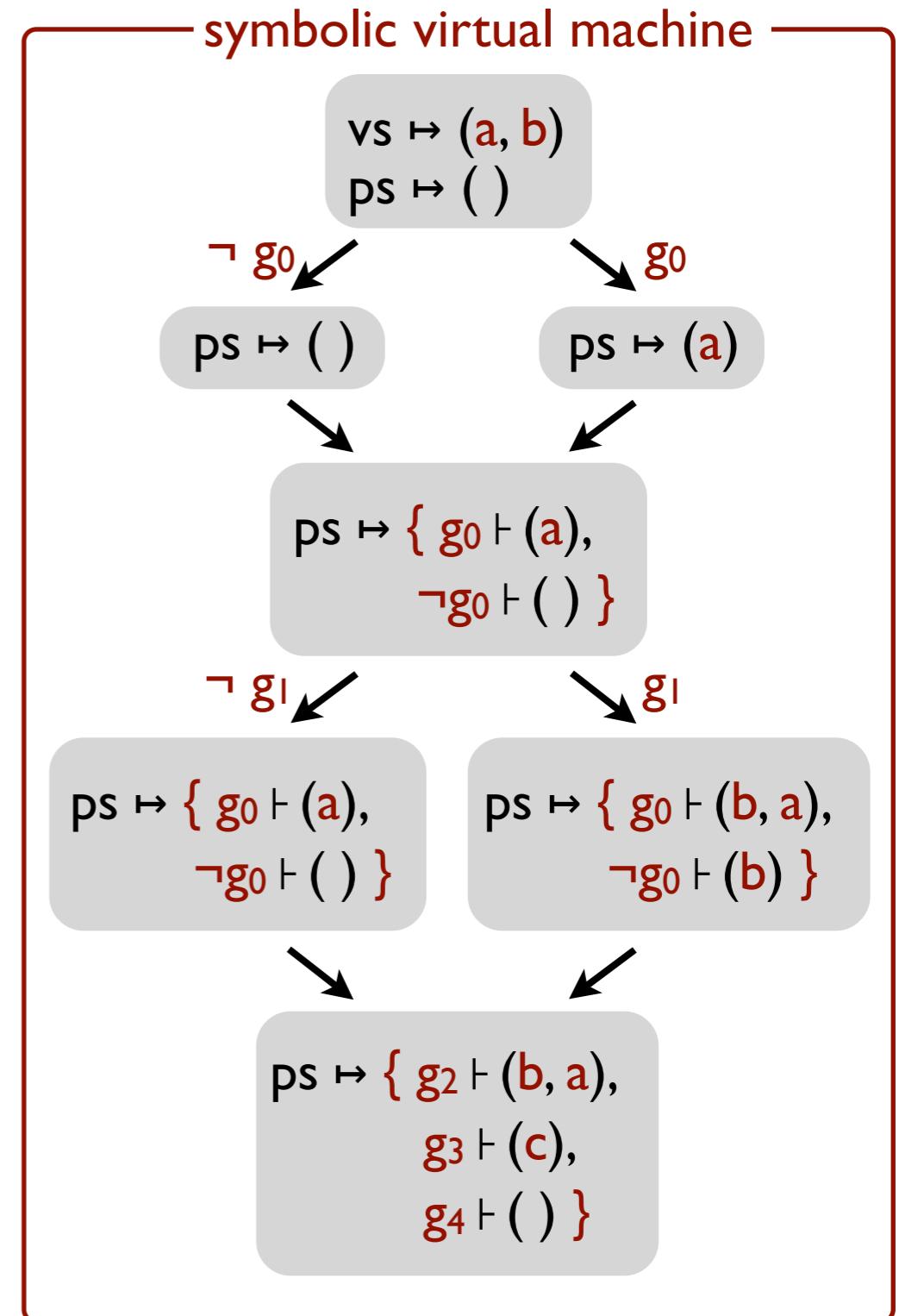
solve:

```
ps = ()  
for v in vs:  
    if v > 0:  
        ps = insert(v, ps)  
assert len(ps) == len(vs)
```

SymPro (OOPSLA'18): use **symbolic profiling** to find performance bottlenecks in solver-aided code.

polynomial encoding
concrete evaluation

```
g0 = a > 0  
g1 = b > 0  
g2 = g0 ∧ g1  
g3 = ¬(g0 ⇔ g1)  
g4 = ¬g0 ∧ ¬g1  
c = ite(g1, b, a)  
assert g2
```



How to build your own solver-aided tool or language



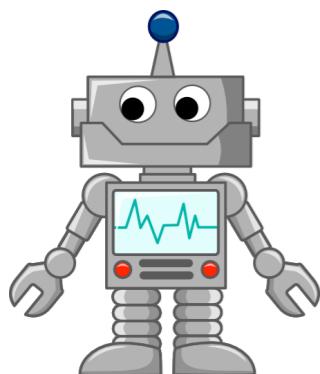
The classic (hard) way to build a tool
What is hard about building a solver-aided tool?

SDSL



SVM

SMT



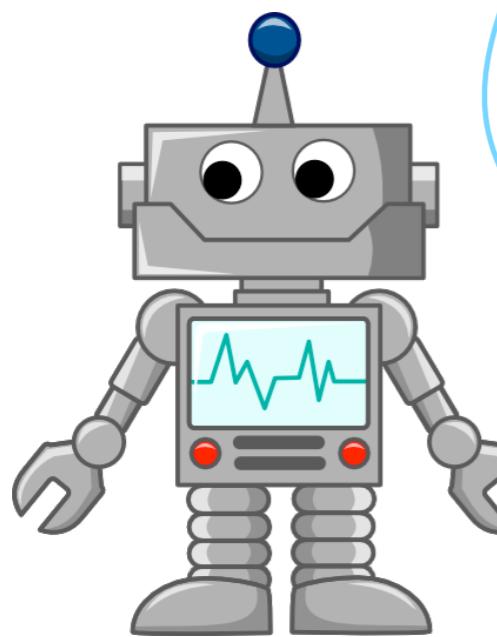
An easier way: tools as languages
How to build tools by stacking layers of languages.

Behind the scenes: symbolic virtual machine
How Rosette works so you don't have to.

A last look: a few recent applications
Cool tools built with Rosette!

30+ tools

programming languages,
software engineering,
systems, architecture,
networks, security,
formal methods,
databases,
education,
games,
...



programming languages, formal methods, and software engineering

type systems and programming models
compilation and parallelization
safety-critical systems
test input generation
software diversification



education and games

hints and feedback
problem generation
problem-solving strategies



systems, architecture, networks, security, and databases

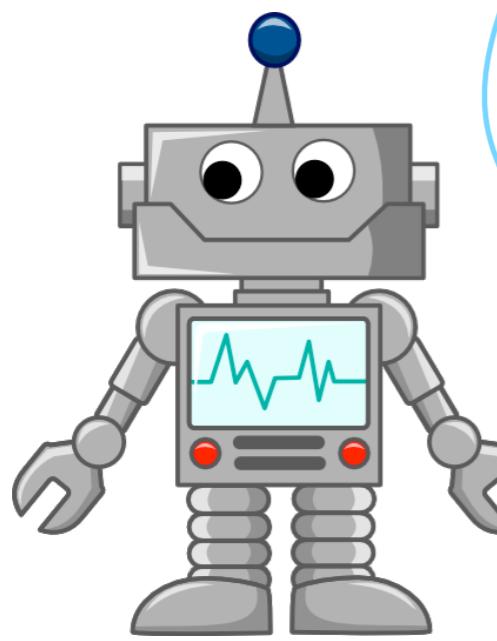
memory models
OS components
data movement for GPUs
router configuration
cryptographic protocols





30+ tools

programming languages,
software engineering,
systems, architecture,
networks, security,
formal methods,
databases,
education,
games,
...



programming languages, formal methods, and software engineering

type systems and programming models
compilation and parallelization
safety-critical systems [CAV'16]
test input generation
software diversification



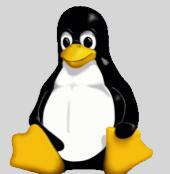
education and games

hints and feedback
problem generation
problem-solving strategies



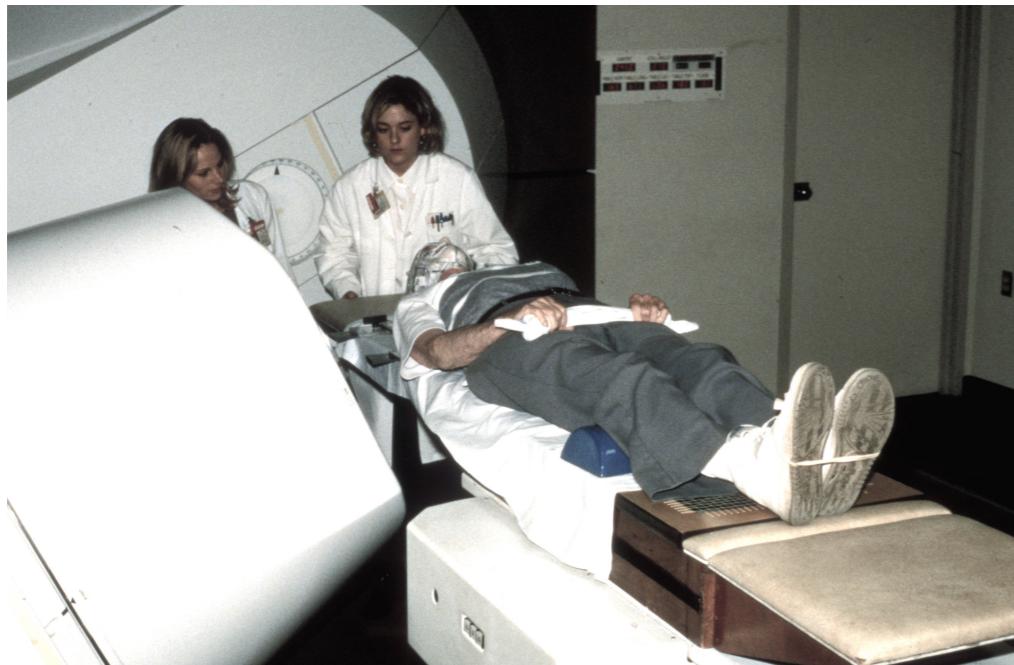
systems, architecture, networks, security, and databases

memory models
OS components
data movement for GPUs
router configuration
cryptographic protocols



Verifying a radiation therapy system

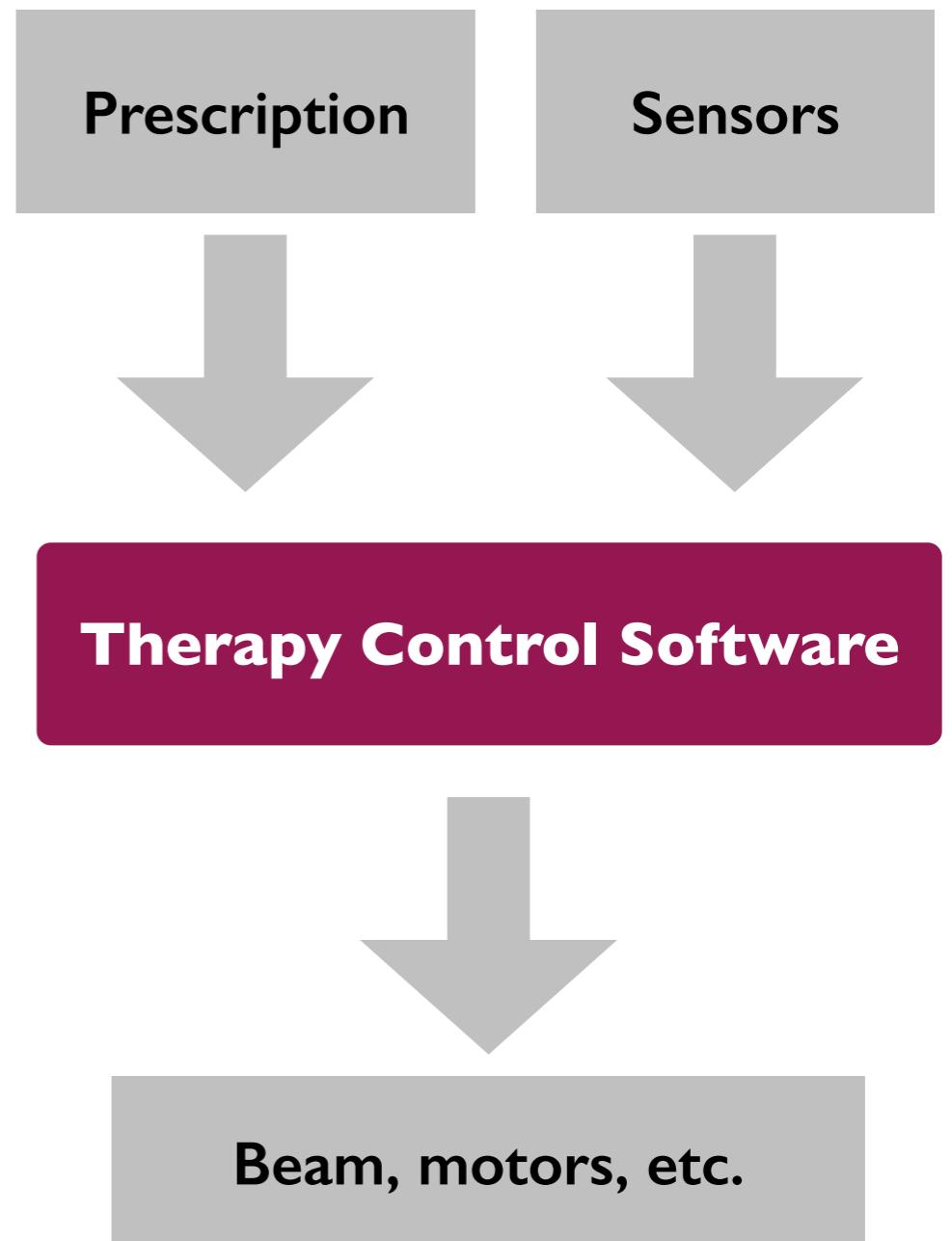
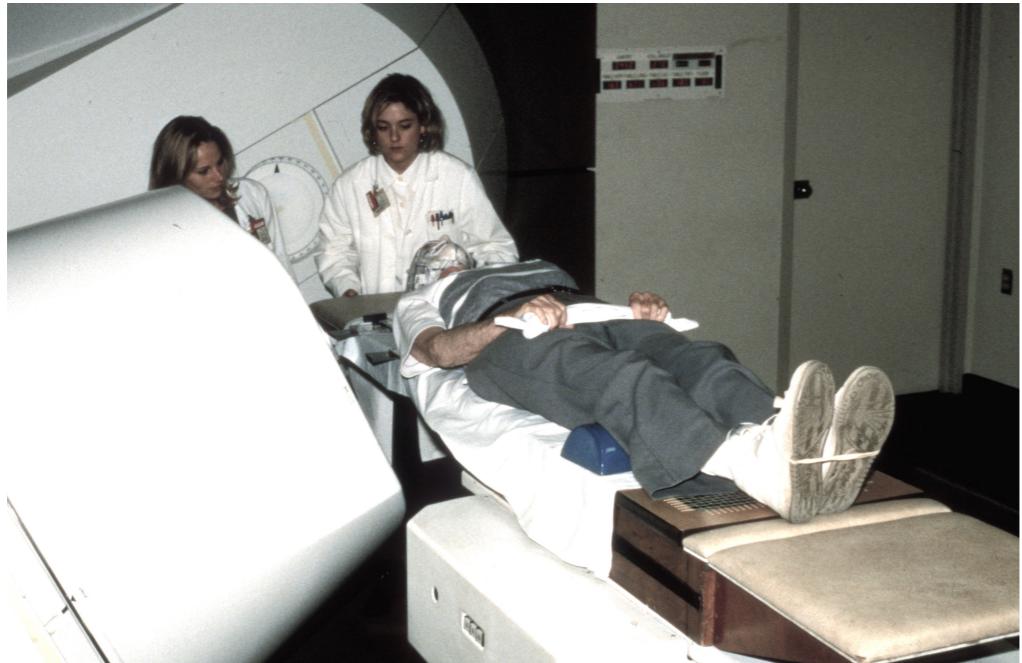
Clinical Neutron Therapy System (CNTS) at UW



- 30 years of incident-free service.
- Controlled by custom software, built by CNTS engineering staff.
- Third generation of Therapy Control software built recently.

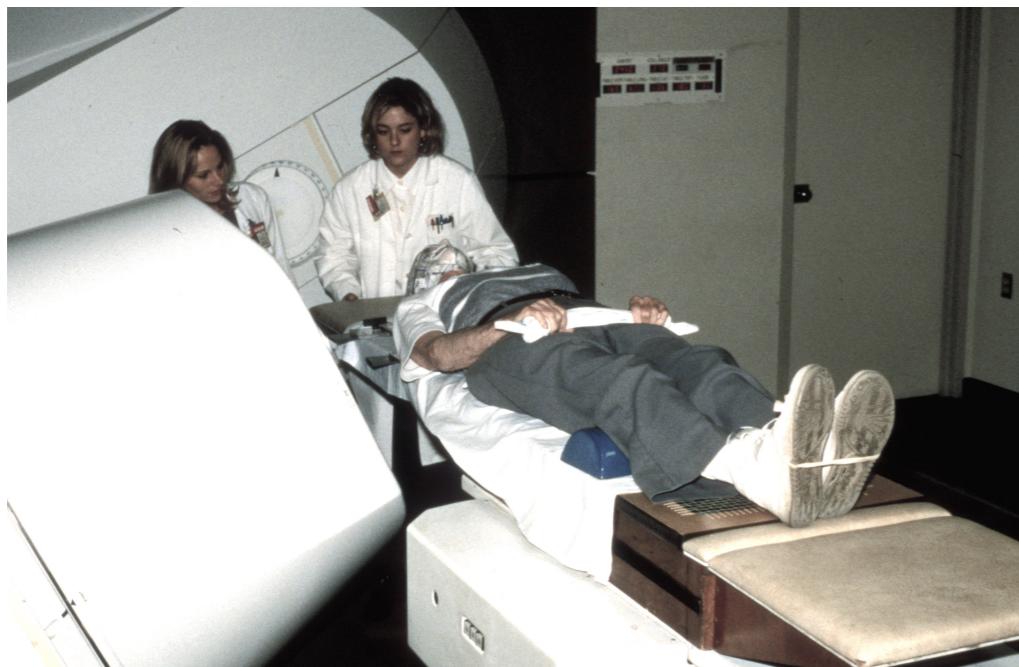
Verifying a radiation therapy system

**Clinical Neutron Therapy
System (CNTS) at UW**



Verifying a radiation therapy system

Clinical Neutron Therapy System (CNTS) at UW

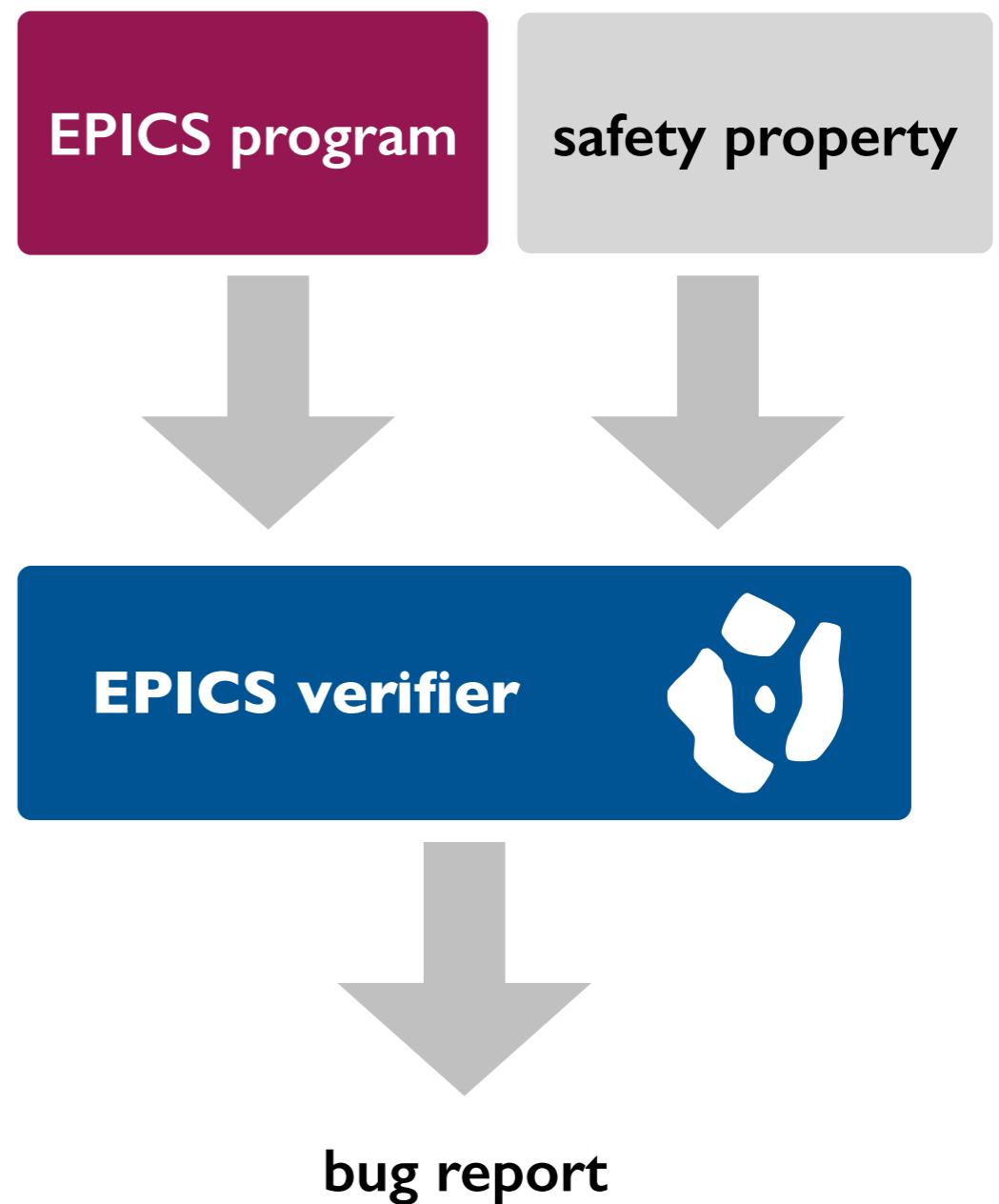
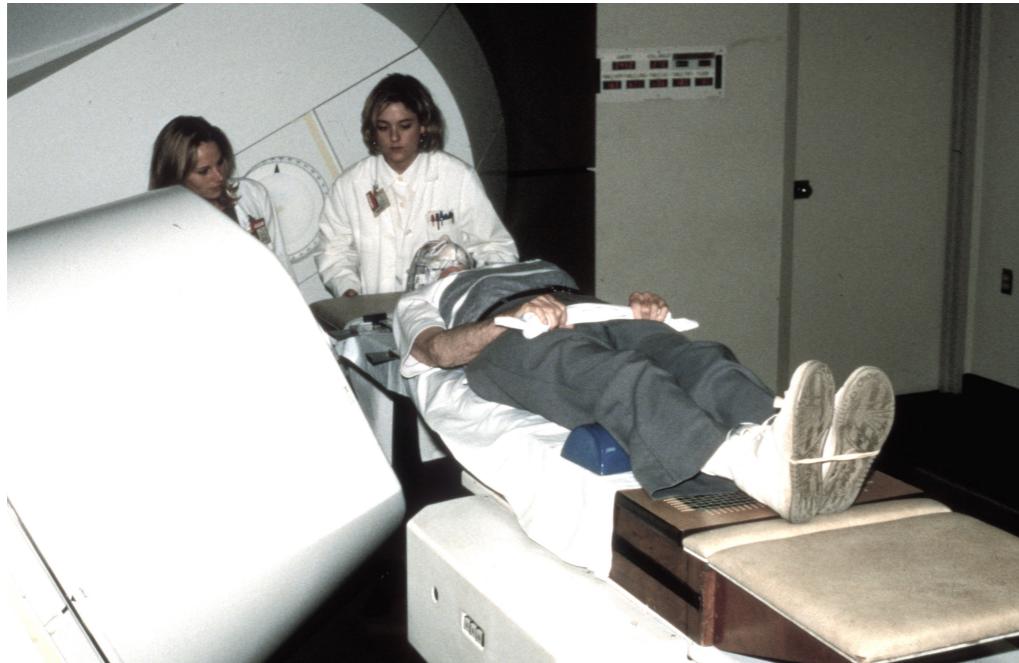


Experimental Physics and Industrial Control System (EPICS) Dataflow Language

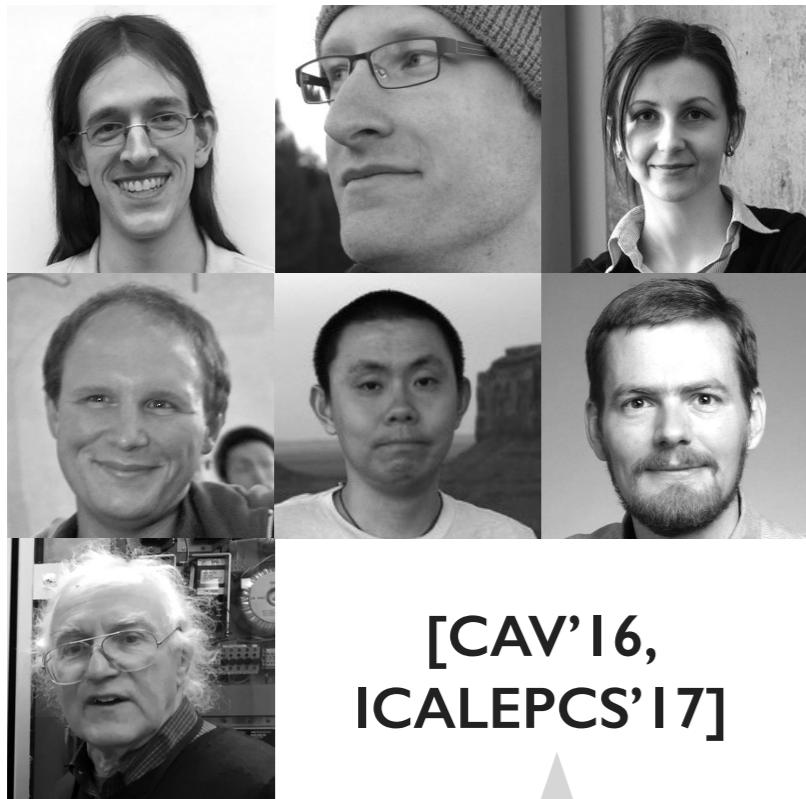
Therapy Control Software

Verifying a radiation therapy system

Clinical Neutron Therapy
System (CNTS) at UW



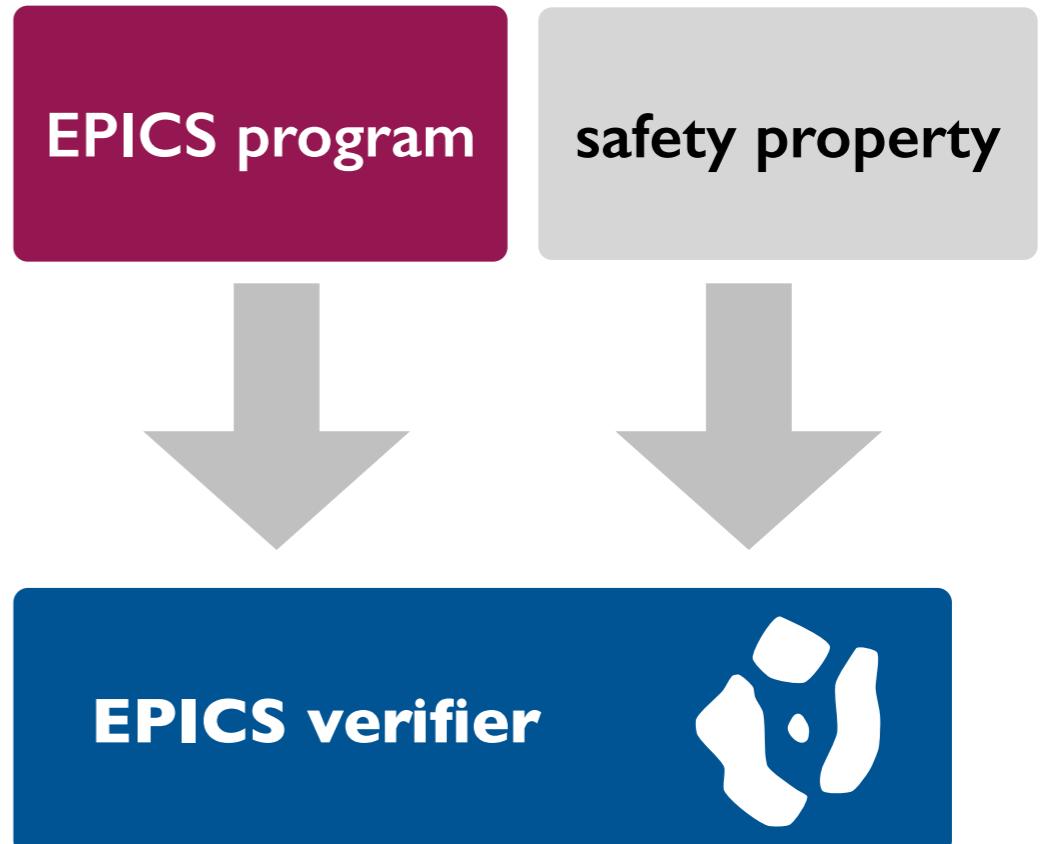
Verifying a radiation therapy system



[CAV'16,
ICALEPCS'17]

Found safety-critical defects
in a pre-release version of
the therapy control software.

Used by CNTS staff to verify
changes to the controller.



bug report

Summary

Today

- Going pro with solver-aided programming.

Next lecture

- Getting started with SAT solving!