#### **Computer-Aided Reasoning for Software**

# **Program Synthesis**

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# Today

#### Last lecture

• Solvers as angelic runtime oracle

#### Today

• Program synthesis: computers programming computers

#### Reminders

- HW3 is due tonight.
- Demo day logistics: 8 min per group, all members should present.

### The program synthesis problem

 $\exists P. \forall x. \phi(x, P(x))$ 

Find a program P that satisfies the specification  $\phi$  on all inputs.

# The program synthesis problem

φ may be a formula, a reference
implementation, input / output pairs, traces, demonstrations, etc.

∃ P. ∀ x. φ(x, P(x))

Find a program P that satisfies the specification  $\phi$  on all inputs.

# The program synthesis problem

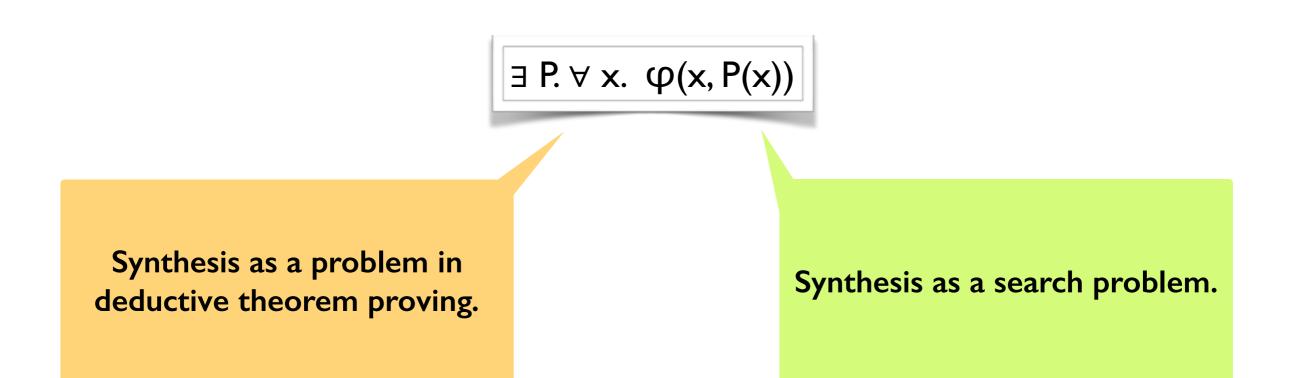
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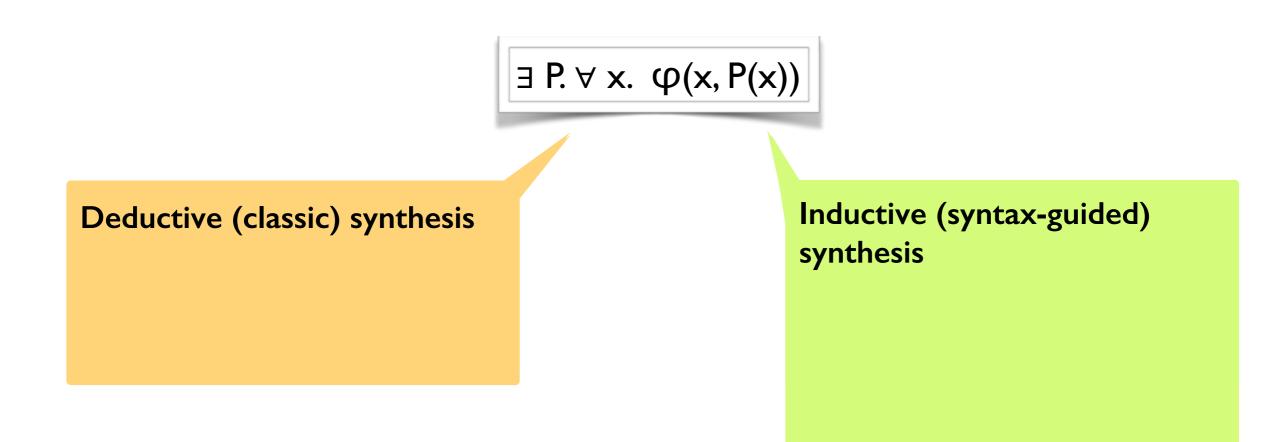
Synthesis improves

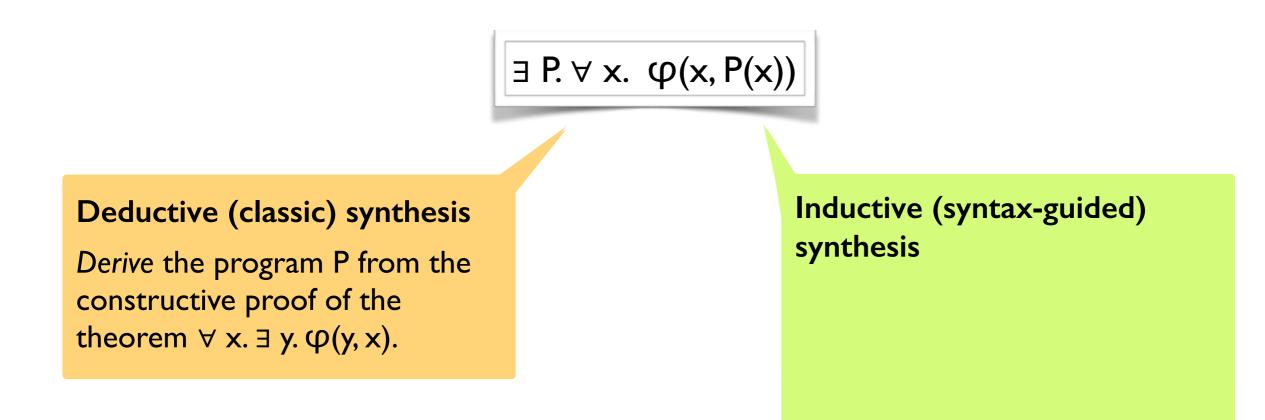
- Productivity (when writing φ is easier than writing P).
- Correctness (when verifying φ is easier than verifying P).

∃ P. ∀ x. φ(x, P(x))

Find a program P that satisfies the specification  $\phi$  on all inputs.







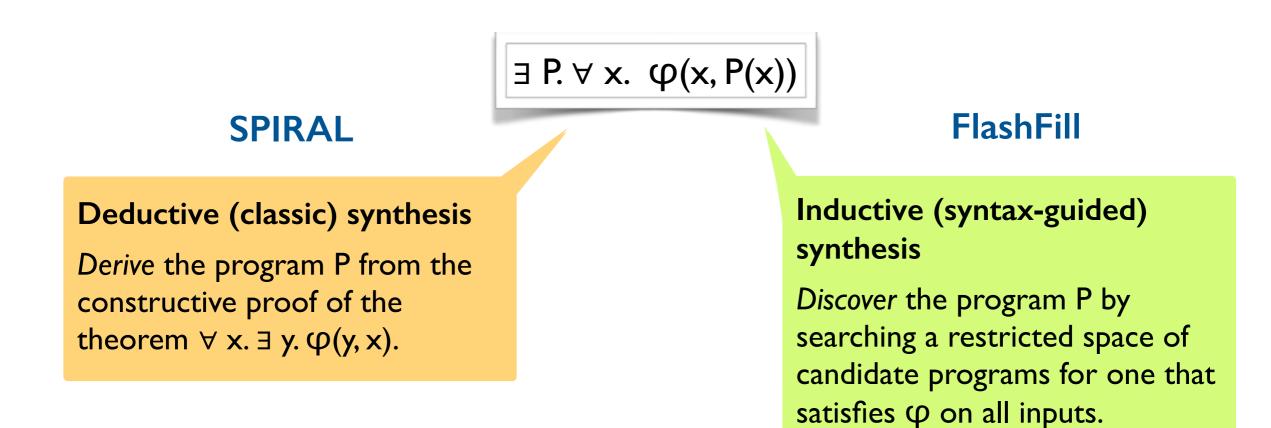
### $\exists P. \forall x. \phi(x, P(x))$

#### **Deductive (classic) synthesis**

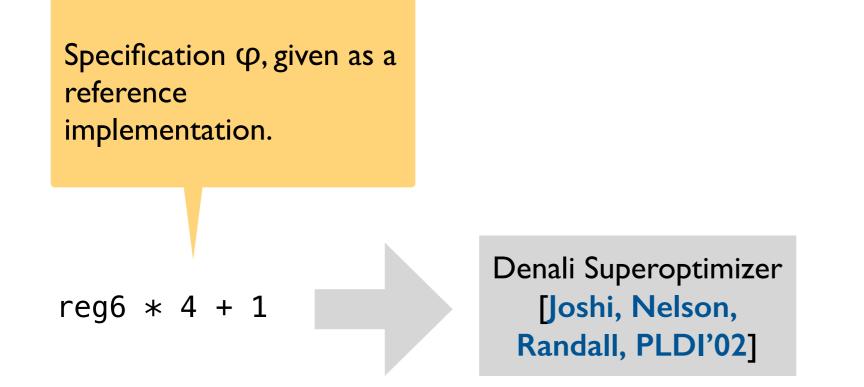
Derive the program P from the constructive proof of the theorem  $\forall x. \exists y. \varphi(y, x)$ .

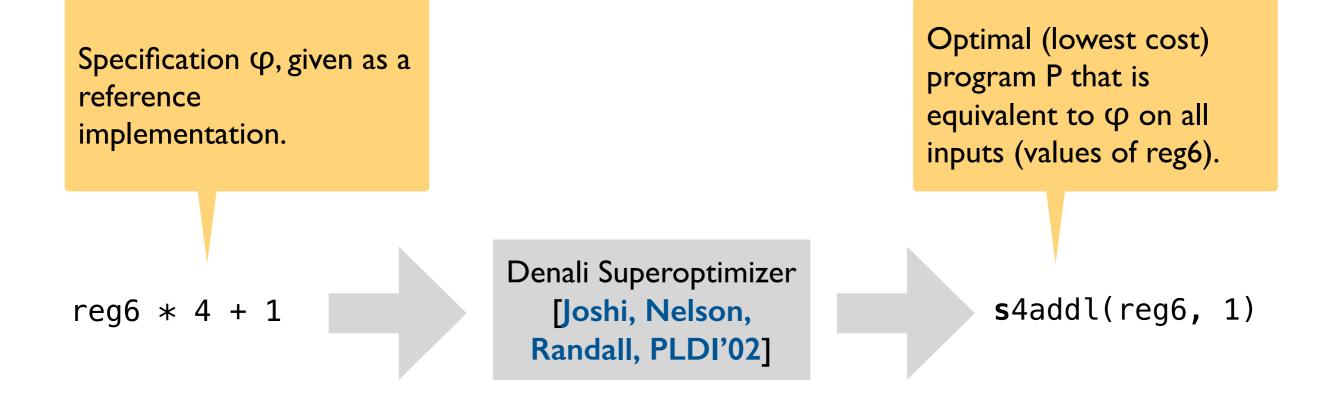
# Inductive (syntax-guided) synthesis

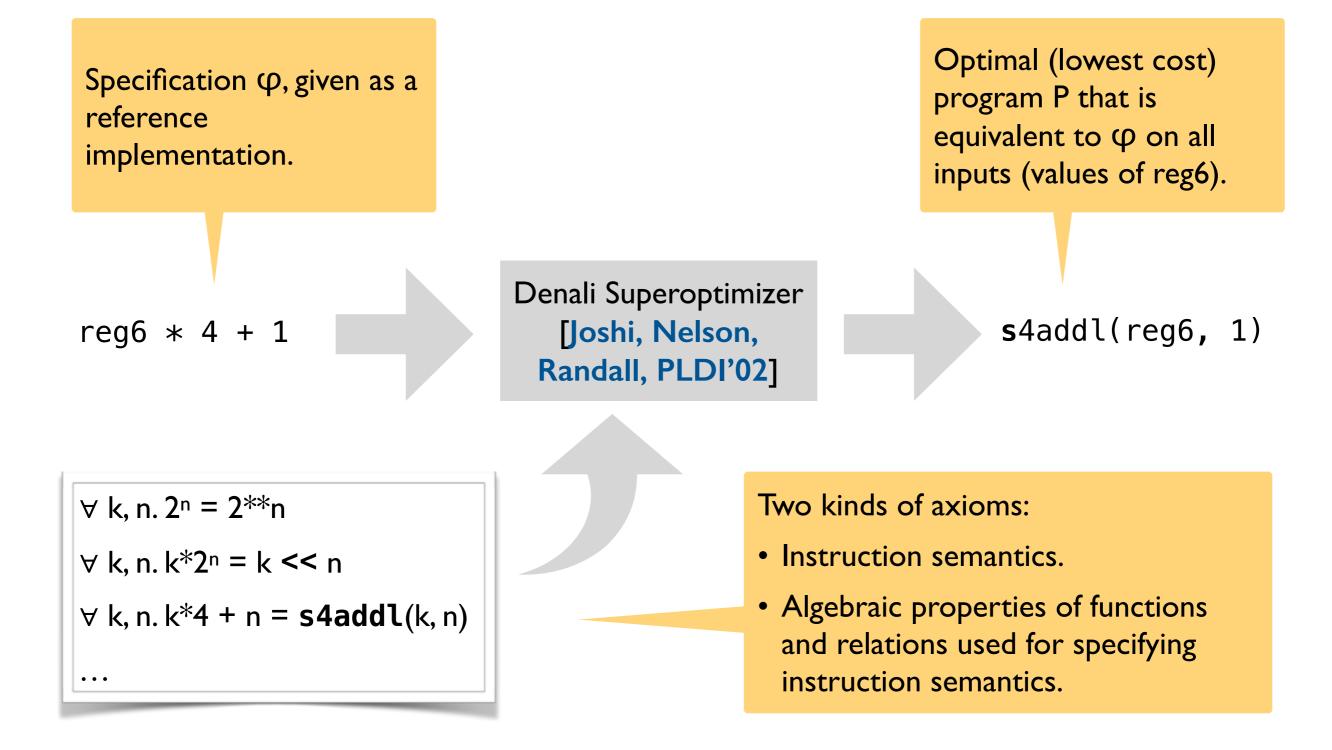
Discover the program P by searching a restricted space of candidate programs for one that satisfies  $\varphi$  on all inputs.

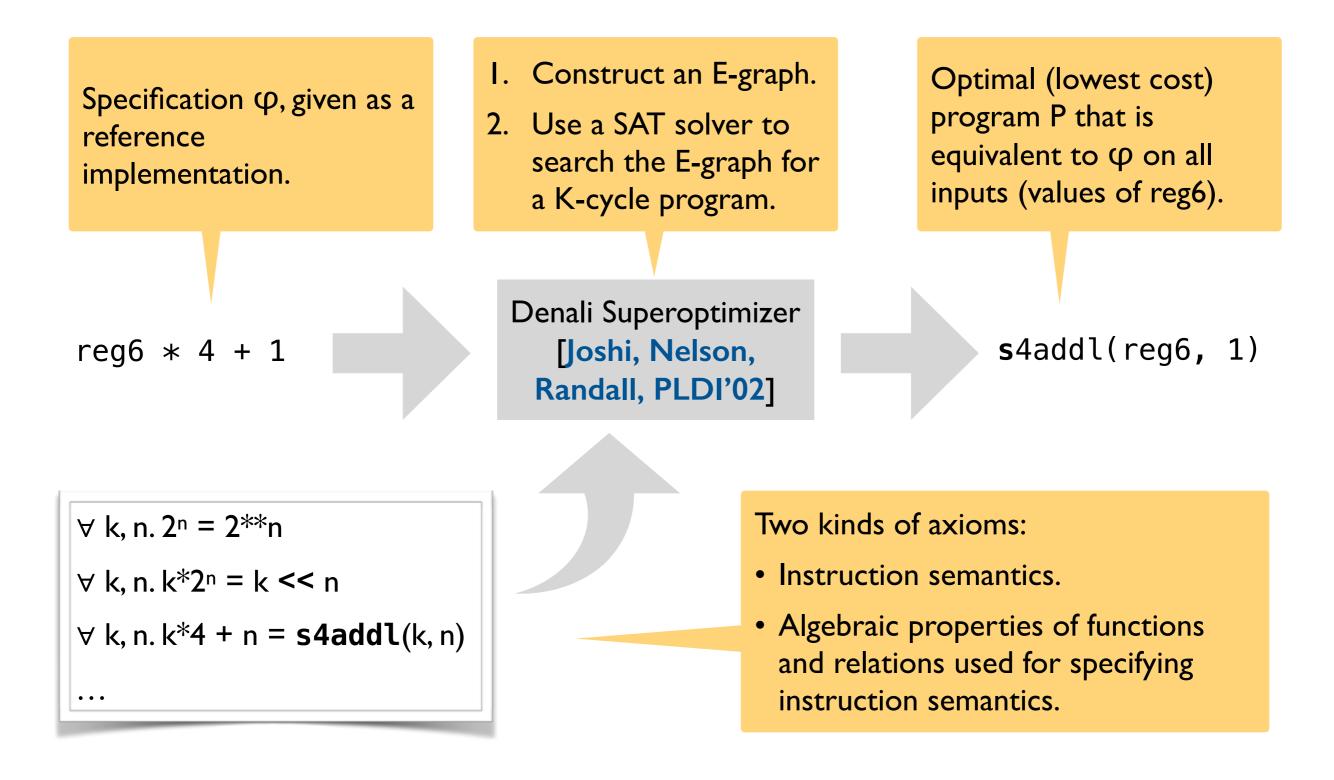


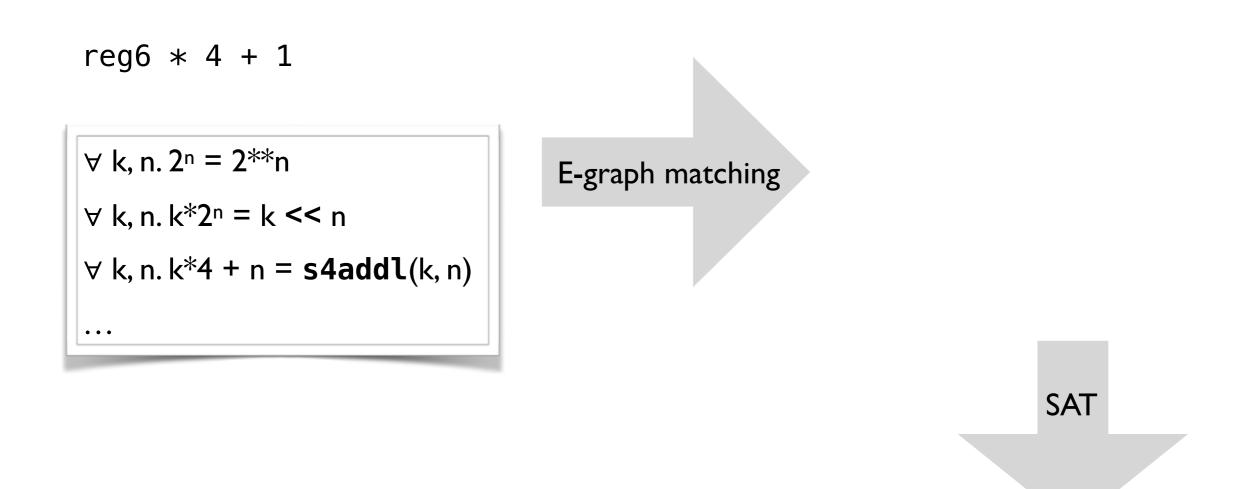
Denali Superoptimizer [Joshi, Nelson, Randall, PLDI'02]



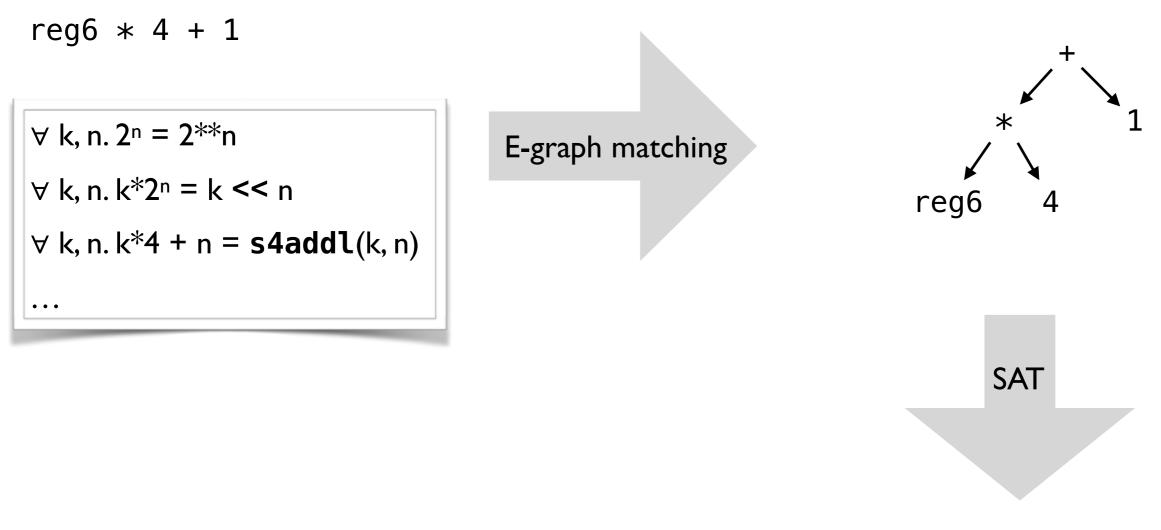




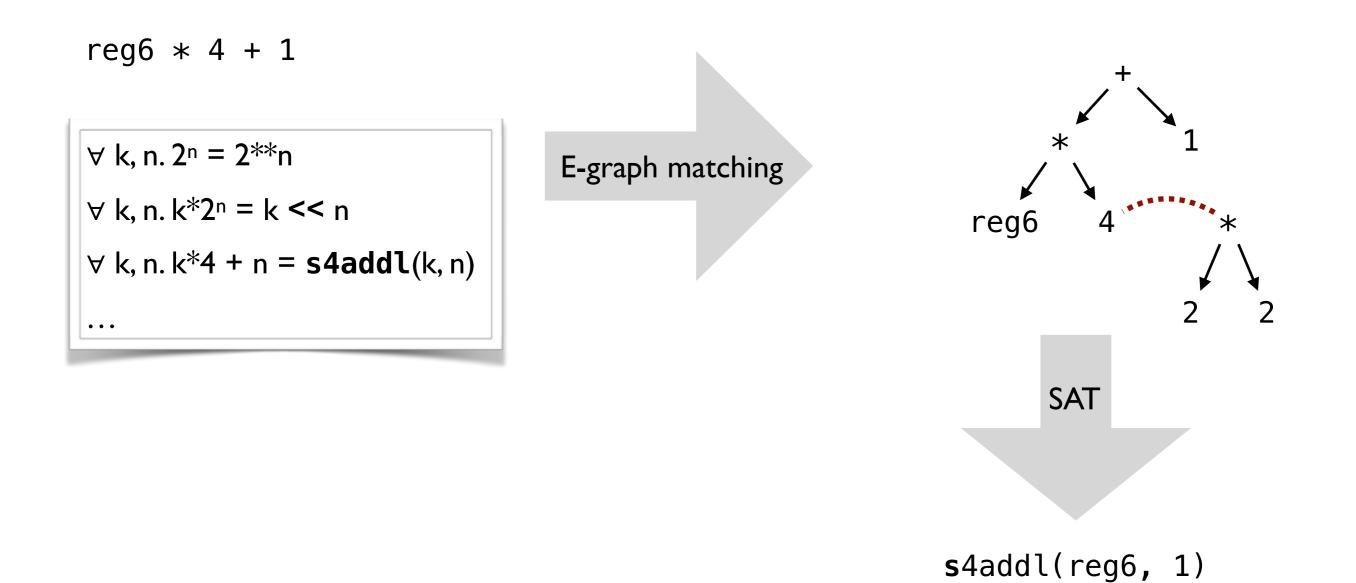


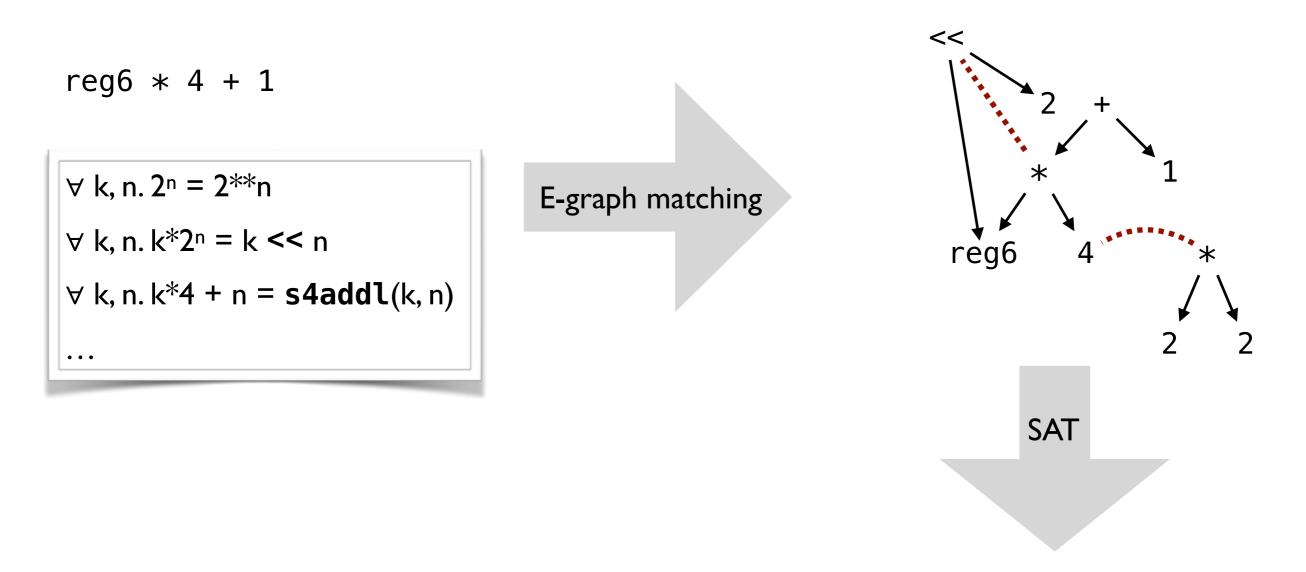


#### s4addl(reg6, 1)

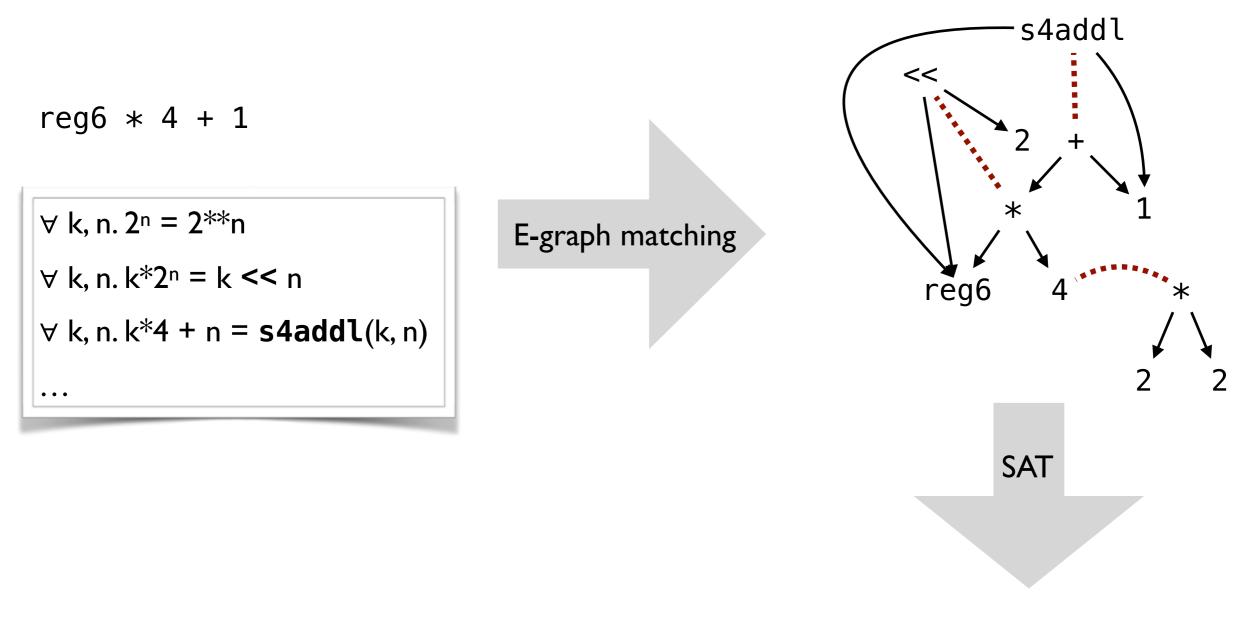


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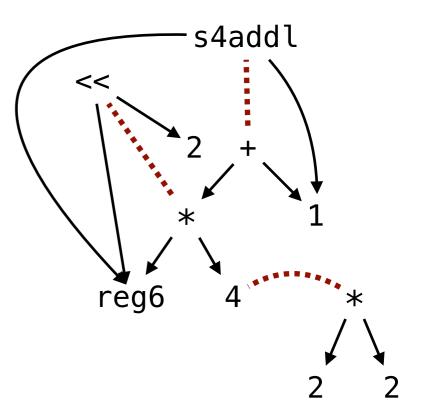
# **Deductive synthesis versus compilation**

#### **Deductive synthesizer**

- Non-deterministic.
- Searches all correct rewrites for one that is optimal.

### Compiler

- Deterministic.
- Lowers a source program into a target program using a *fixed sequence of rewrite steps*.



reg6 \* 4 + 1 reg6 << 2 + 1

## **Deductive synthesis versus inductive synthesis**

#### $\exists P. \forall x. \phi(x, P(x))$

#### **Deductive synthesis**

- Efficient and provably correct: thanks to the semantics-preserving rules, only correct programs are explored.
- Requires *sufficient axiomatization* of the domain.
- Requires *complete* specifications to seed the derivation.

# **Deductive synthesis versus inductive synthesis**

#### $\exists P. \forall x. \phi(x, P(x))$

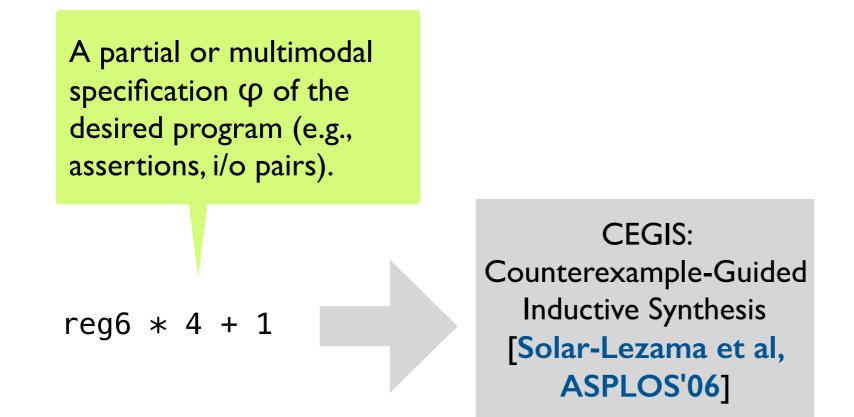
#### **Deductive synthesis**

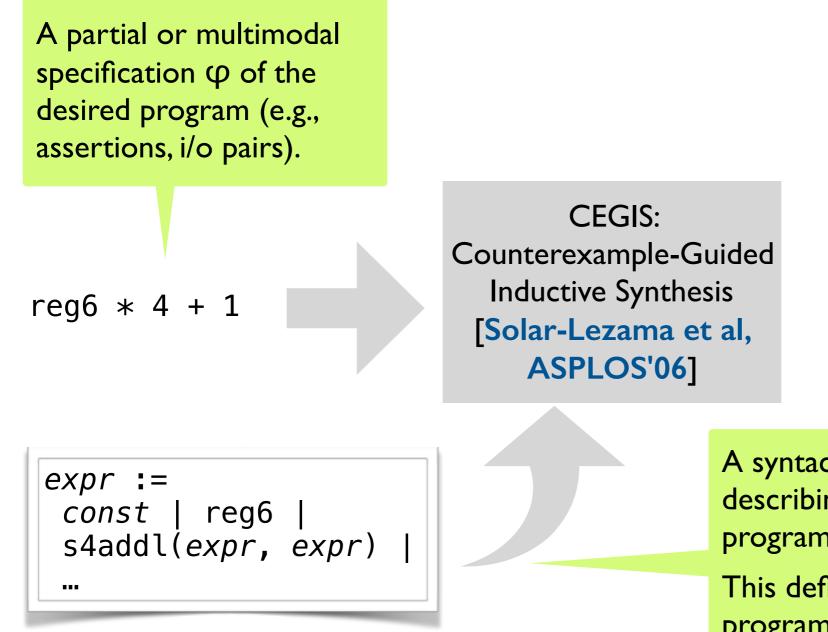
- Efficient and provably correct: thanks to the semantics-preserving rules, only correct programs are explored.
- Requires *sufficient axiomatization* of the domain.
- Requires *complete* specifications to seed the derivation.

#### Inductive synthesis

- Works with *multi-modal and partial* specifications.
- Requires no axioms.
- But often at the cost of lower efficiency and weaker (bounded) guarantees on the correctness/ optimality of synthesized code.

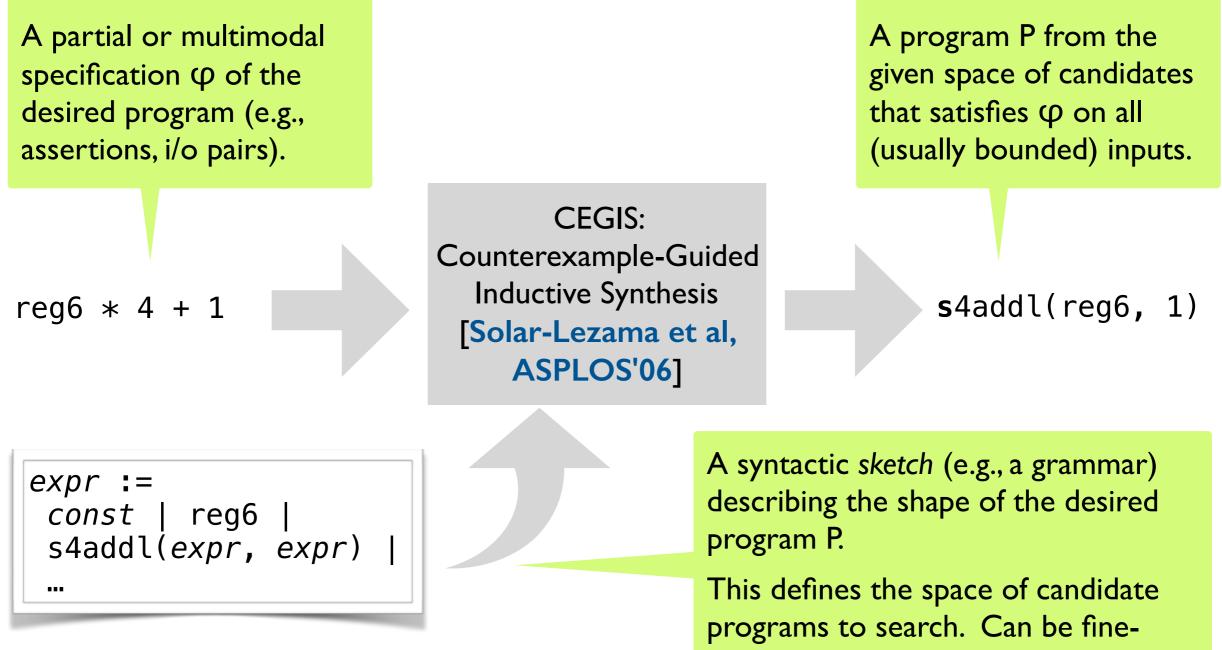
CEGIS: Counterexample-Guided Inductive Synthesis [Solar-Lezama et al, ASPLOS'06]



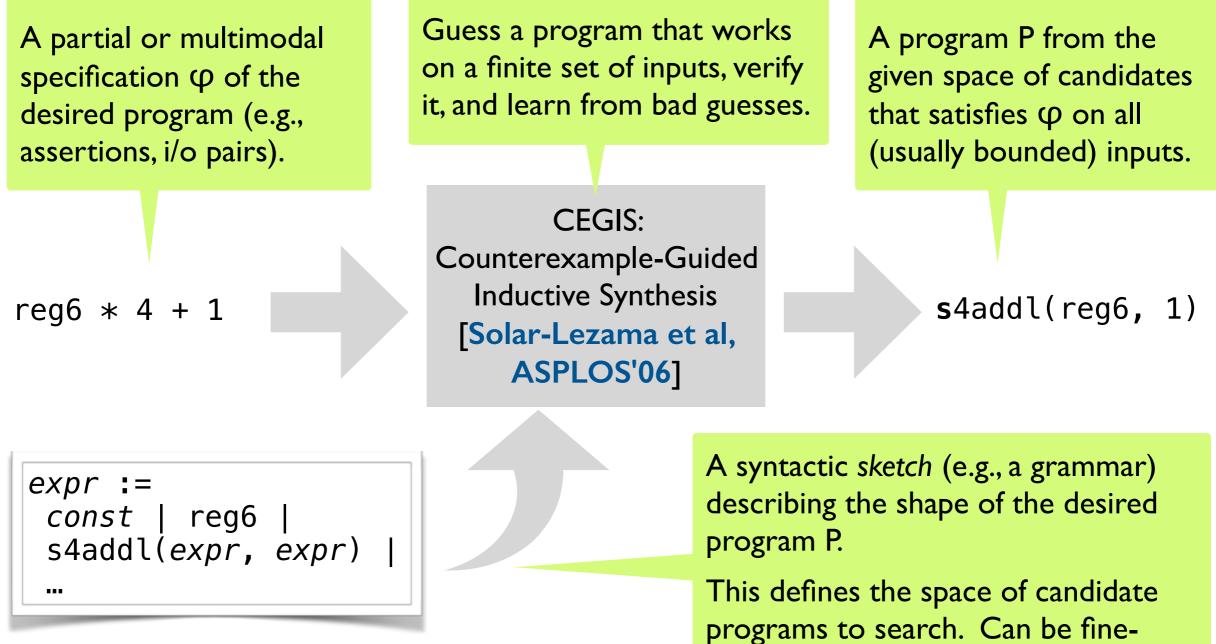


A syntactic sketch (e.g., a grammar) describing the shape of the desired program P.

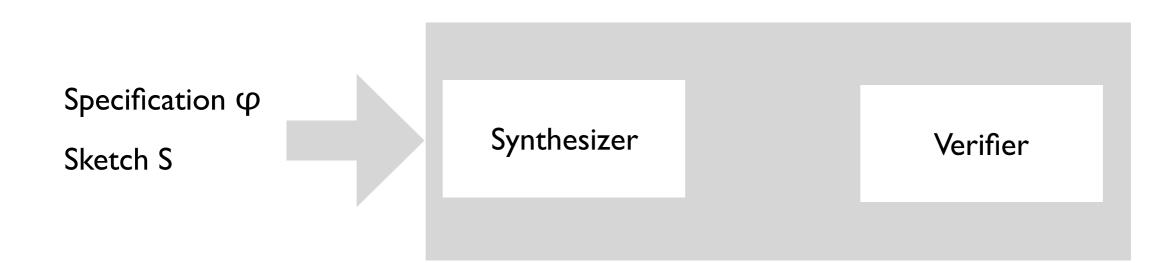
This defines the space of candidate programs to search. Can be fine-tuned for better performance.

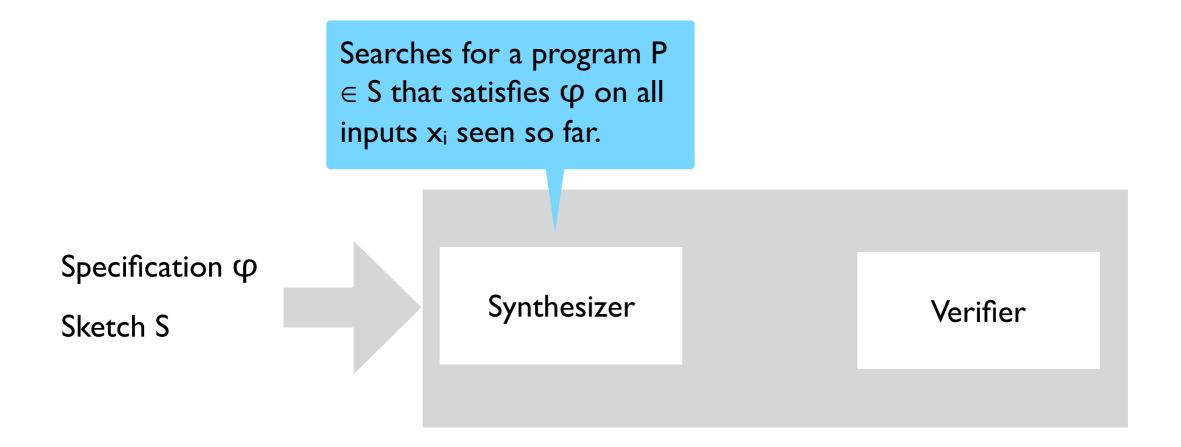


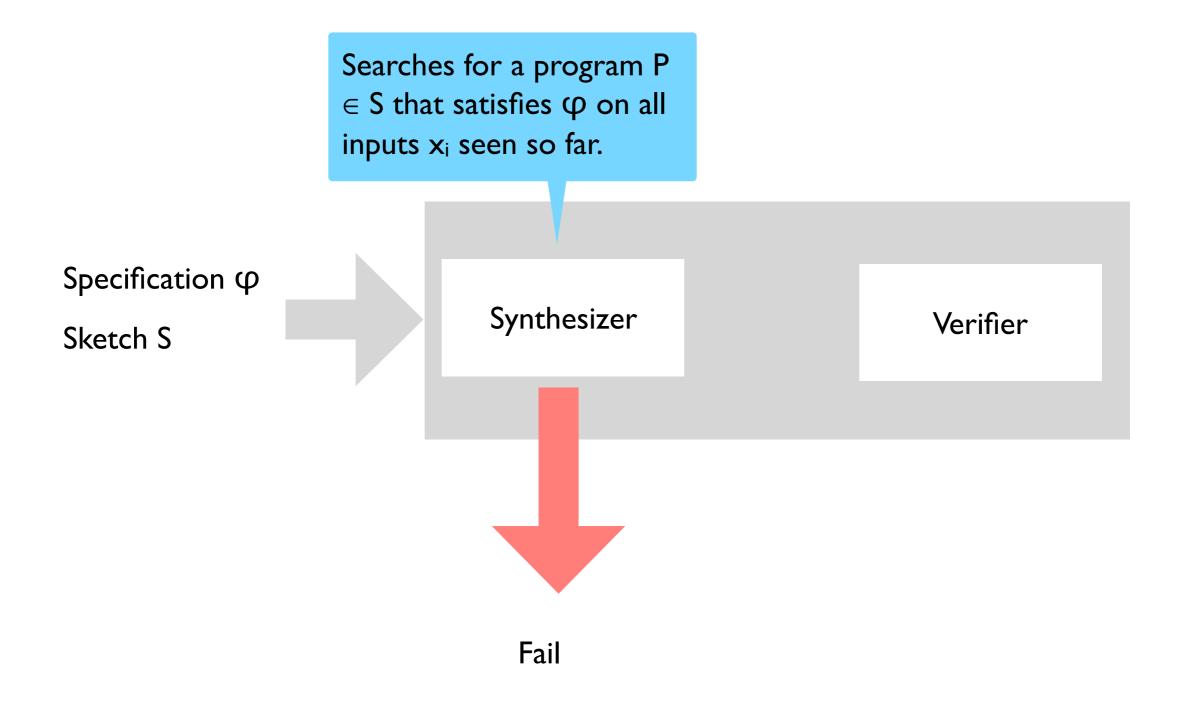
tuned for better performance.

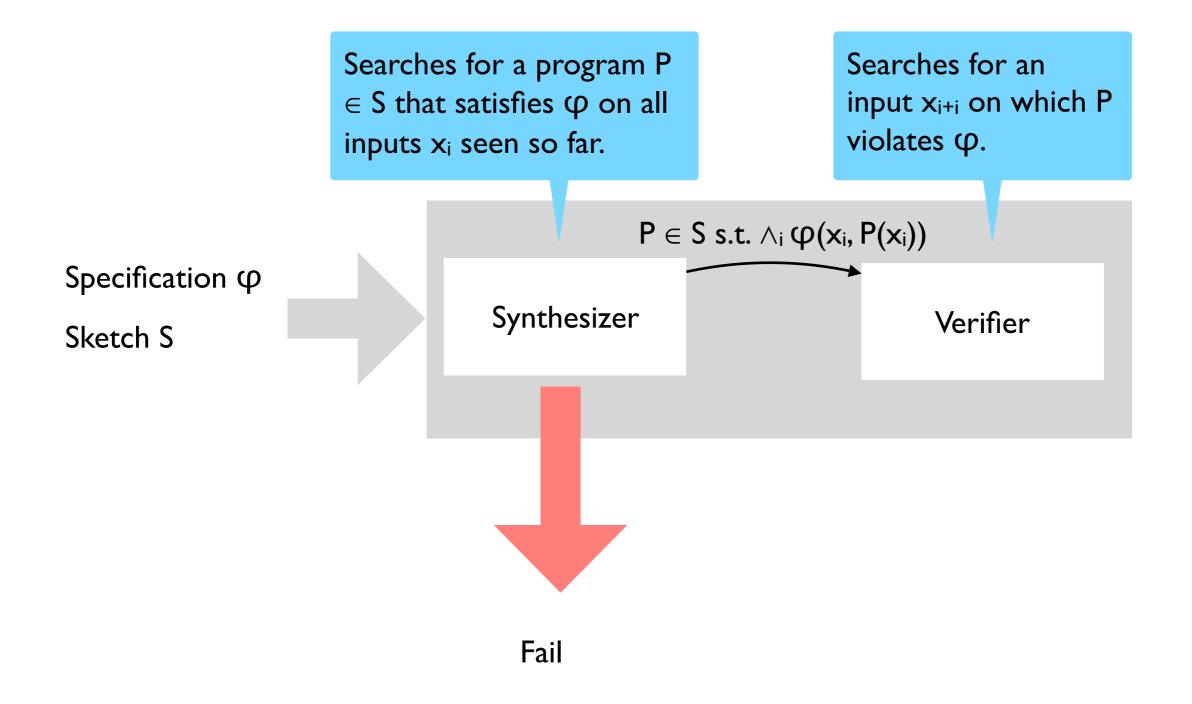


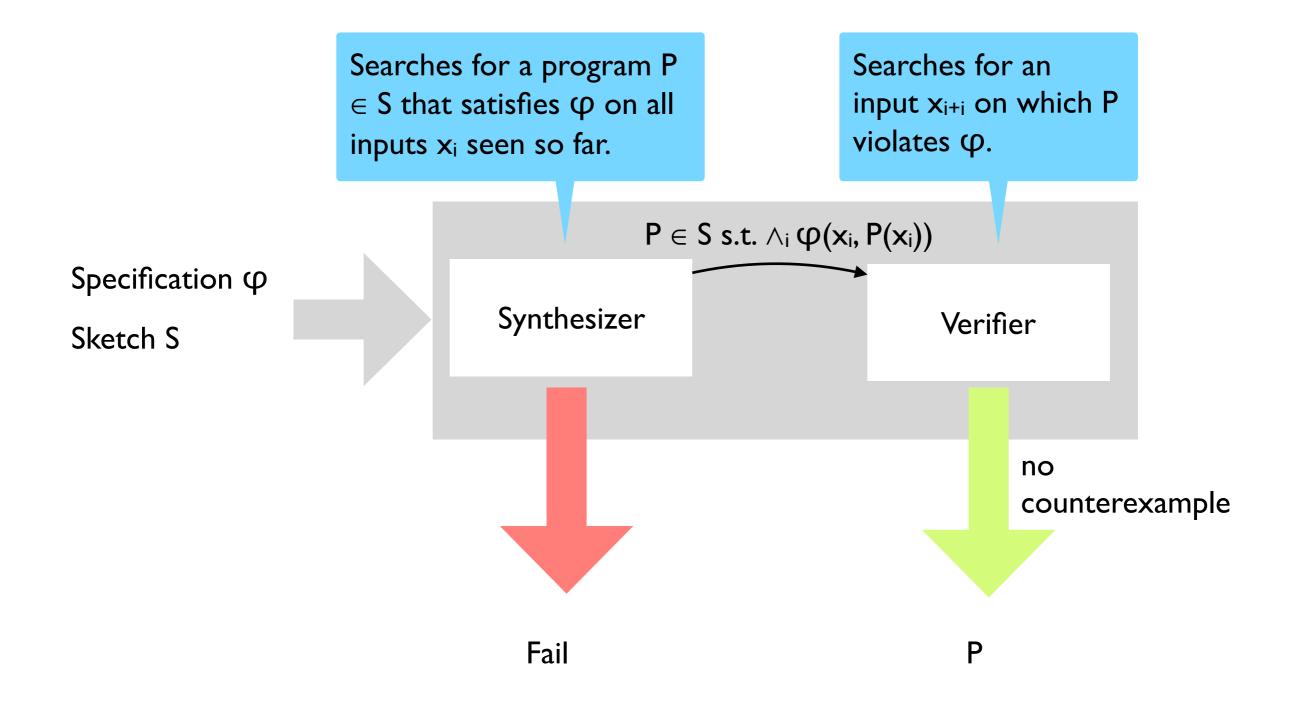
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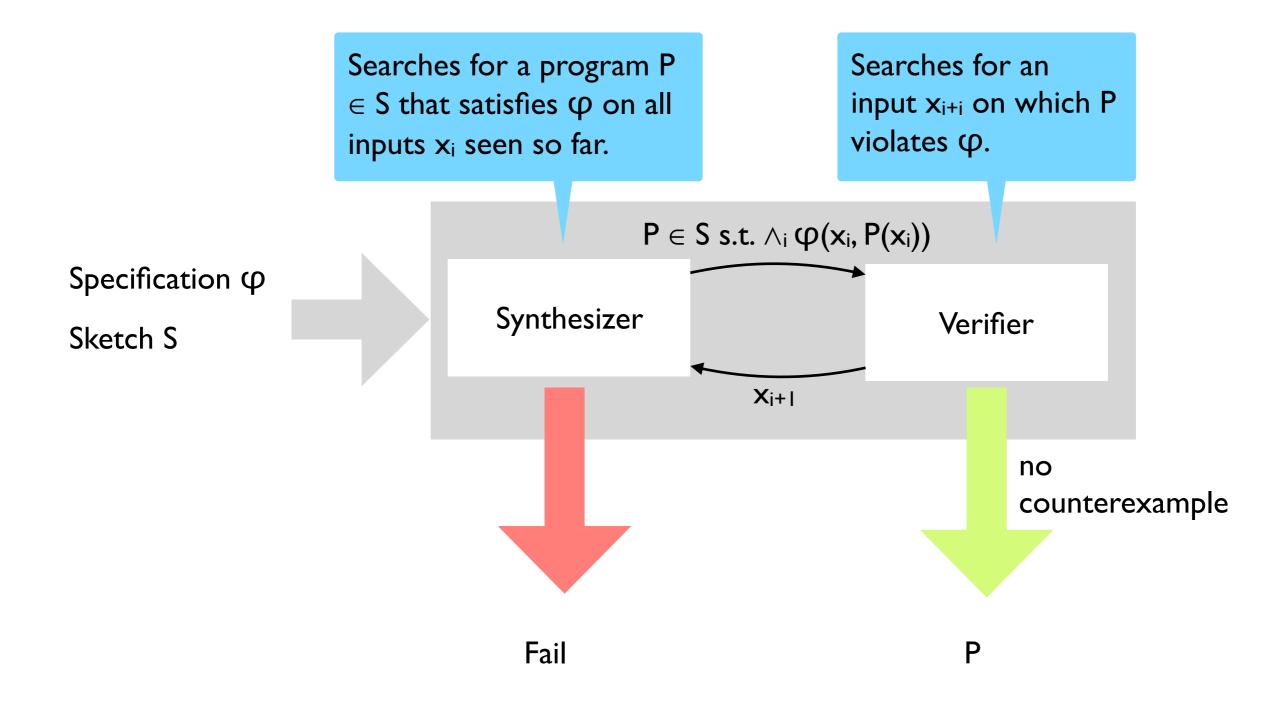


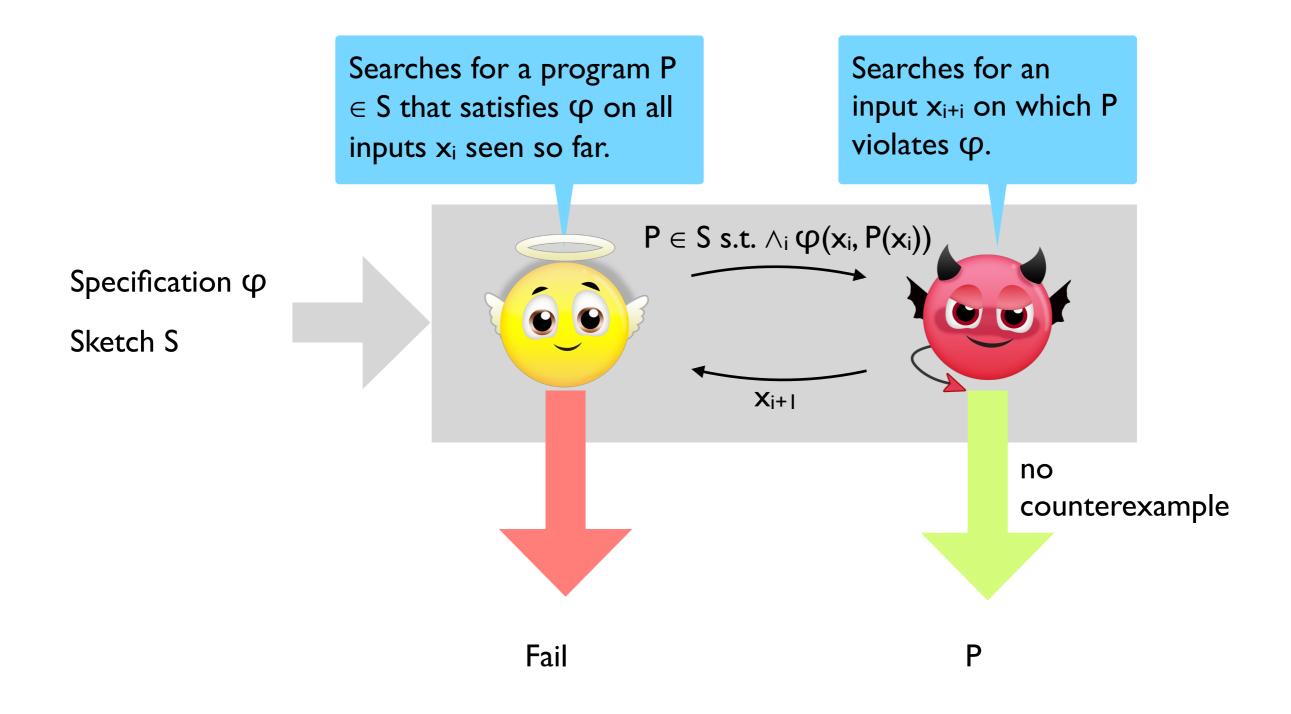


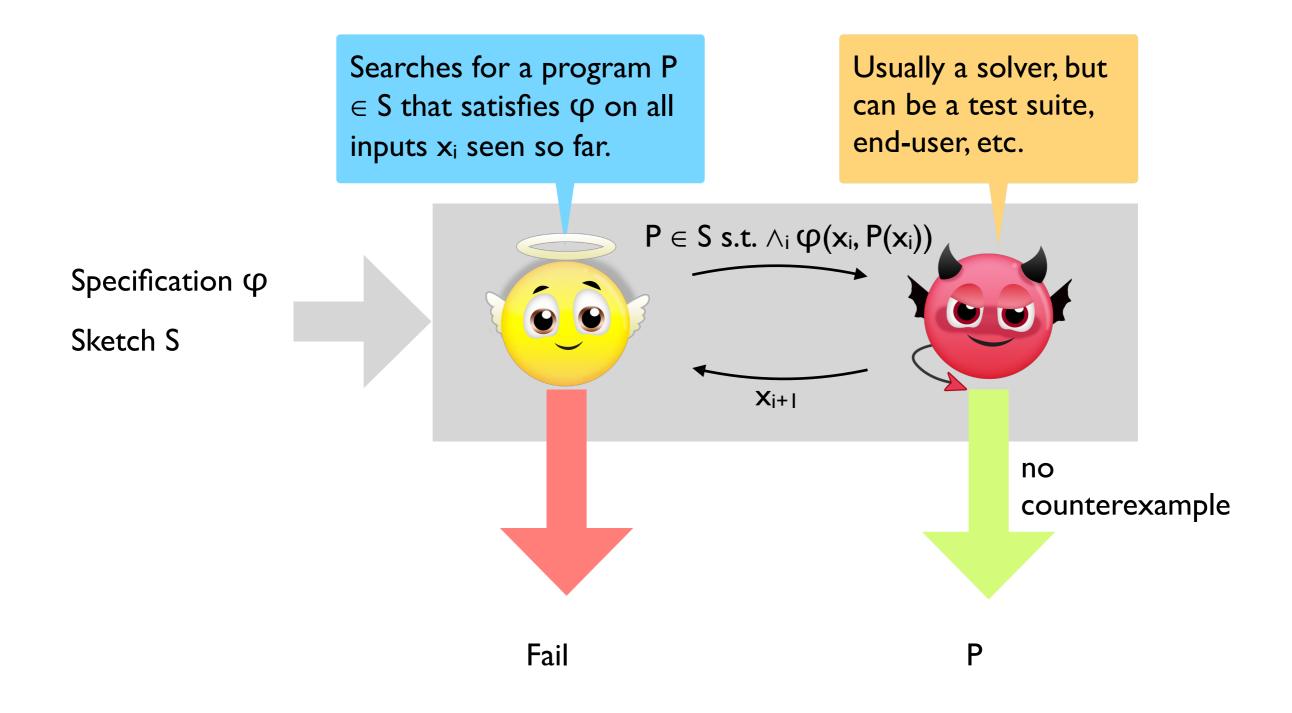




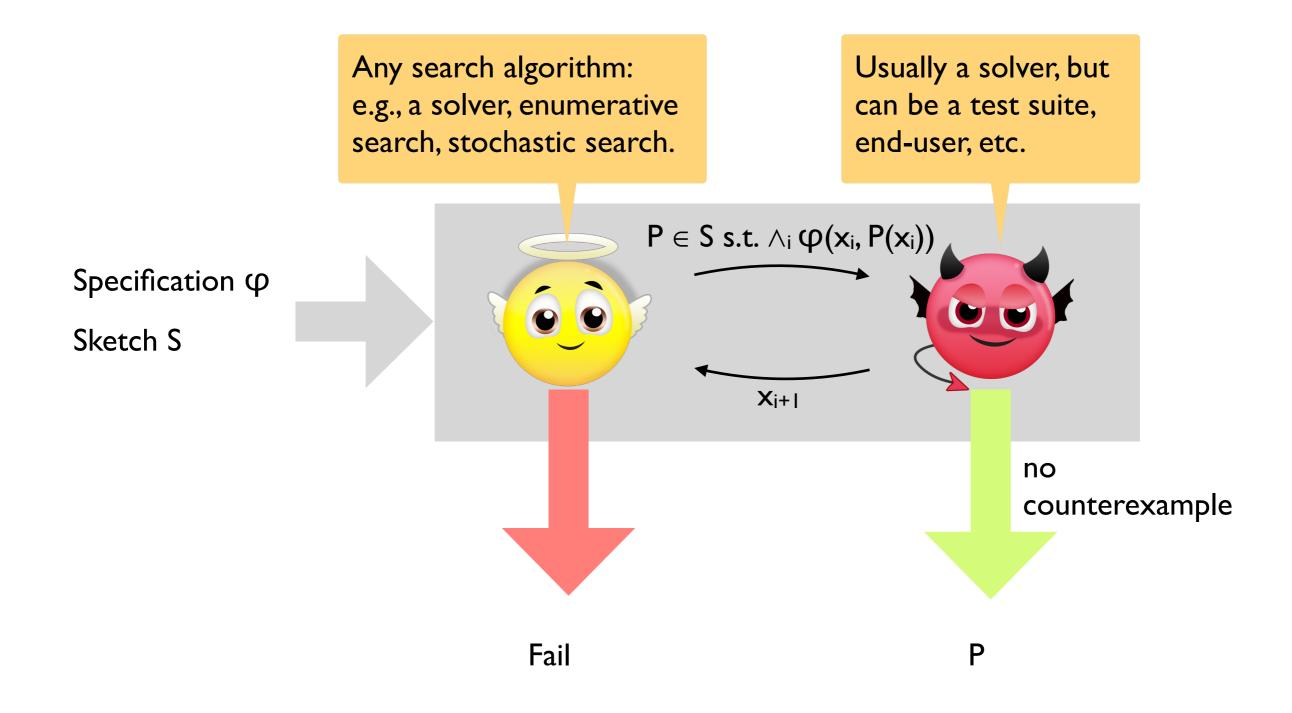


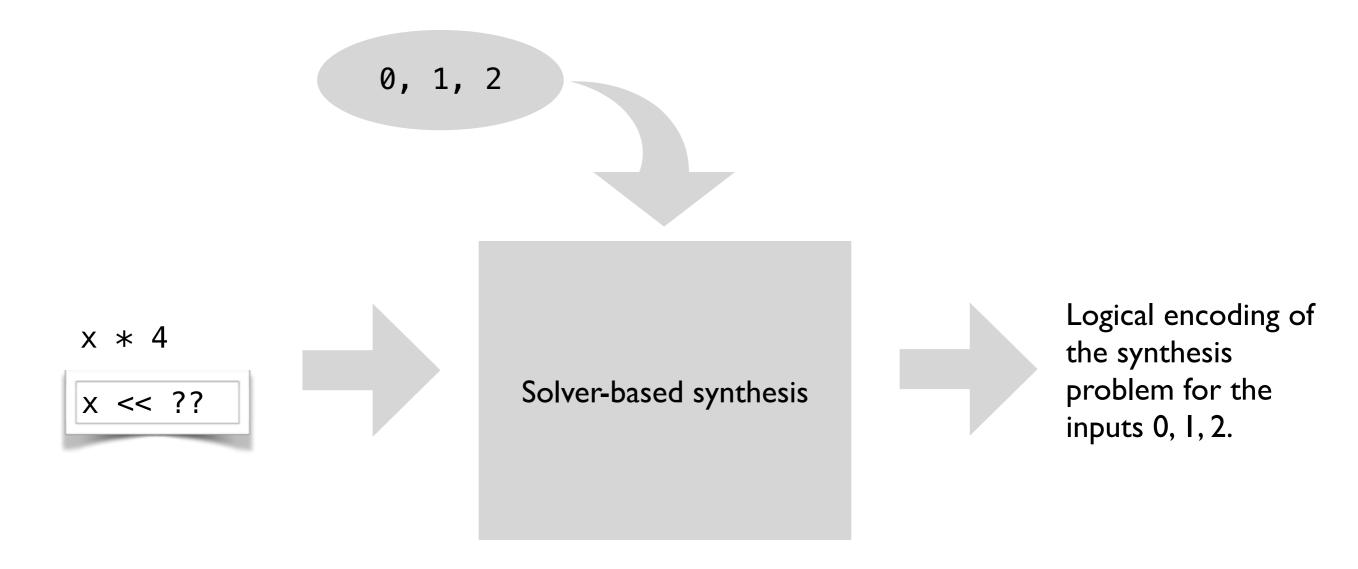




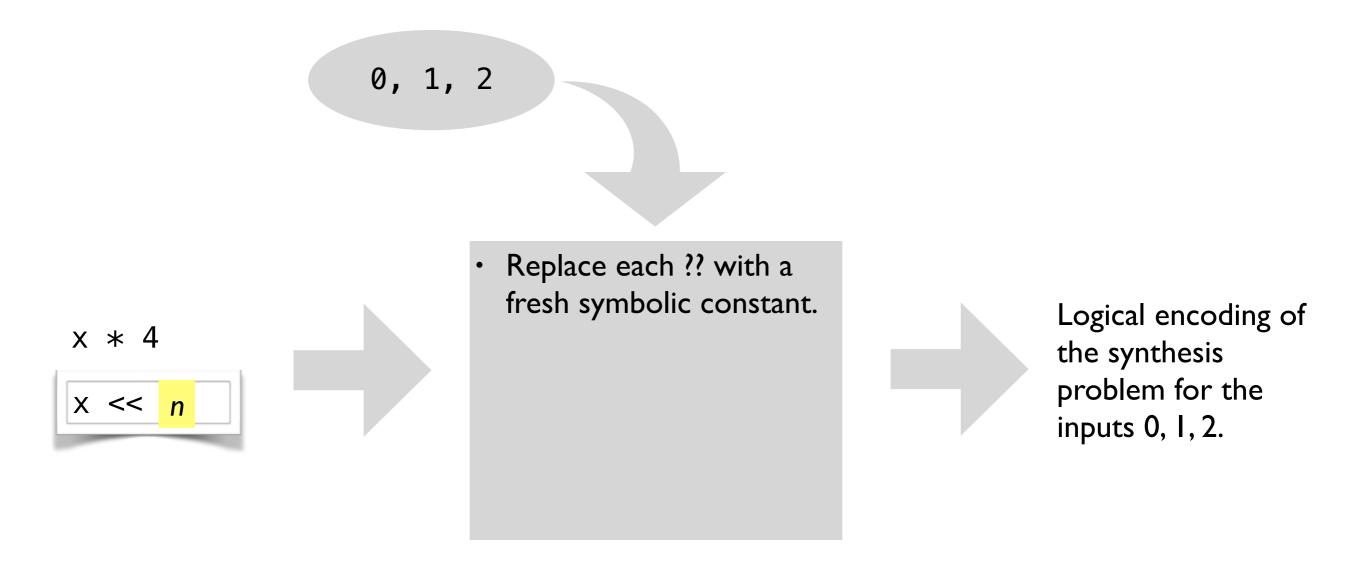


# **Overview of CEGIS**





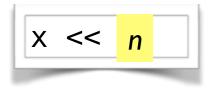
#### [Solar-Lezama et al, ASPLOS'06]



#### [Solar-Lezama et al, ASPLOS'06]

0, 1, 2

x \* 4



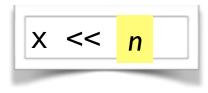
- Replace each ?? with a fresh symbolic constant.
- Translate the resulting problem to constraints w.r.t. the current inputs.

 $(0 << n = 0) \land$  $(1 << n = 4) \land$ (2 << n = 8)

#### [Solar-Lezama et al, ASPLOS'06]

0, 1, 2

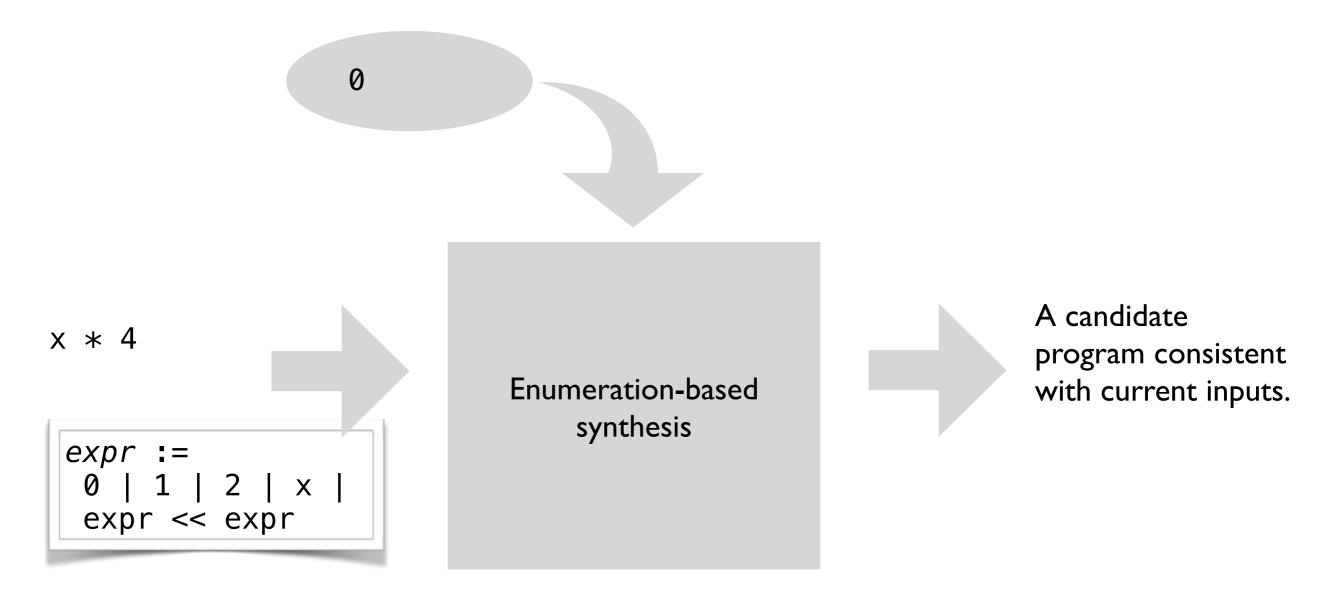
x \* 4



- Replace each ?? with a fresh symbolic constant.
- Translate the resulting problem to constraints w.r.t. the current inputs.
- If SAT, convert the model to a program P.

#### [Solar-Lezama et al, ASPLOS'06]

 $(0 << n = 0) \land$  $(1 << n = 4) \land$ (2 << n = 8)



x \* 4
expr :=
0 | 1 | 2 | x |
expr << expr</pre>

0

- Iteratively construct all programs of size K until one is consistent with the current inputs.
- If two programs produce the same output on all current inputs, keep just one of the two.

A candidate program consistent with current inputs.

x \* 4

expr :=
0 | 1 | 2 | x |
expr << expr</pre>

0

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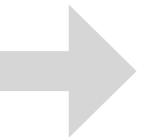
K=1: 0

0, 1

x \* 4

expr :=	, , , , , , , , , , , , , , , , , , ,
0 1 1	2   x
expr <<	expr

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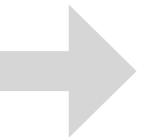


0, 1

x \* 4

expr :=	, , , , , , , , , , , , , , , , , , ,
0 1 1	2   x
expr <<	expr

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0, 1

x \* 4

expr	:=			
0 1	1	2	X	
	-   r //		I	
exh	r <<		γμ	

- Iteratively construct all programs of size K until one is consistent with the current inputs.
- If two programs produce the same output on all current inputs, keep just one of the two.

#### [Udupa et al, PLDI'13]

#### *K*=*I*:0, I, 2, ×

0, 1

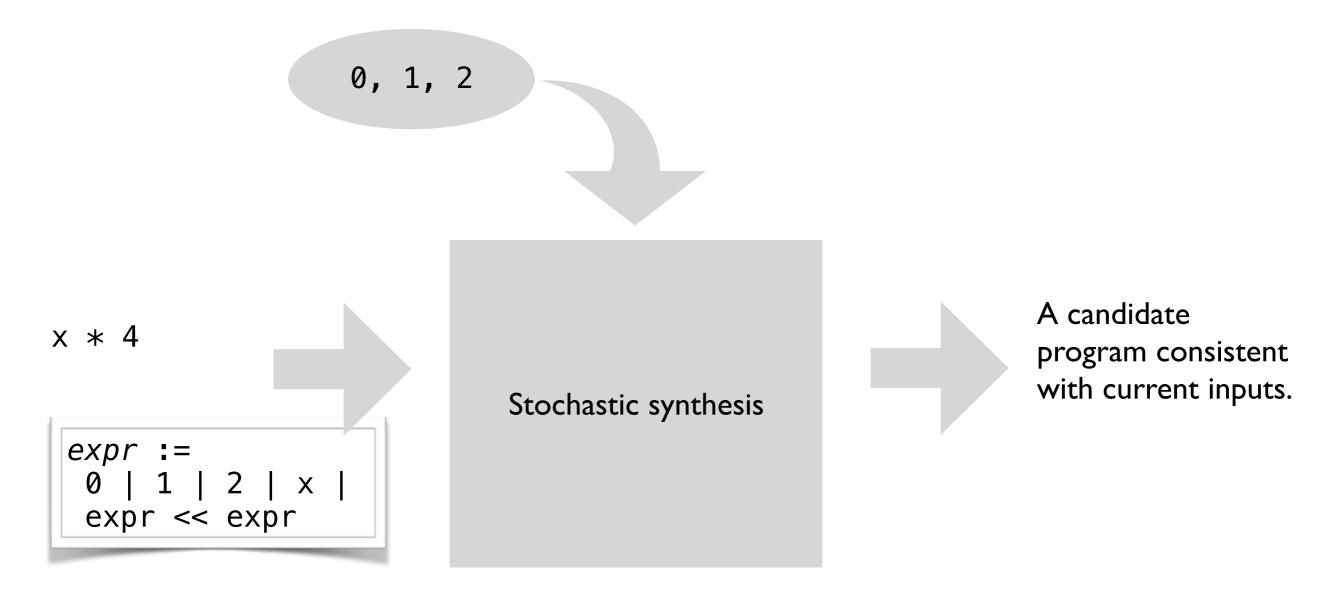
x \* 4

[		1
expr :=		
	2   x	
expr <<		
		J

- Iteratively construct all programs of size K until one is consistent with the current inputs.
- If two programs produce the same output on all current inputs, keep just one of the two.

K=1:0, I, 2, x K=2: I << 2, 2 << 2, x << I, x << 2

## Synthesizing programs with stochastic search



### [Schkufza et al, ASPLOS'13]

## Synthesizing programs with stochastic search

0, 1, 2

x \* 4

expr :=	r III	
0   1	2   X	
expr << expr		
с., р.		

- Use Metropolis-Hastings to sample expressions.
- Mutate the current
   candidate program and
   keep the mutation with
   probability proportional
   to its correctness w.r.t.
   the current inputs.

A candidate program consistent with current inputs.

### [Schkufza et al, ASPLOS'13]

# Thanks for a great quarter!

