#### **Computer-Aided Reasoning for Software**

# **Program Synthesis**

courses.cs.washington.edu/courses/cse507/18sp/

Emina Torlak

emina@cs.washington.edu

# Today

#### Last lecture

• Solvers as angelic runtime oracle

#### Today

• Program synthesis: computers programming computers

#### Reminders

• HW3 is due tonight.

# **Computers programming computers?**

"Information technology has been praised as a labor saver and cursed as a destroyer of obsolete jobs. But the entire edifice of modern computing rests on a fundamental irony: **the software that makes it all possible is, in a very real sense, handmade.** Every miraculous thing computers can accomplish begins with a human programmer entering lines of code by hand, character by character."

Interview with Moshe Vardi

Program synthesis aims to automate (tedious parts of) programming.

#### The program synthesis problem

∃ P. ∀ x. φ(x, P(x))

Find a program P that satisfies the specification φ on all inputs.

#### The program synthesis problem

φ may be a formula, a reference implementation, input/output pairs, traces, demonstrations, etc.

∃ P. ∀ x. φ(x, P(x))

Find a program P that satisfies the specification φ on all inputs.

### The program synthesis problem

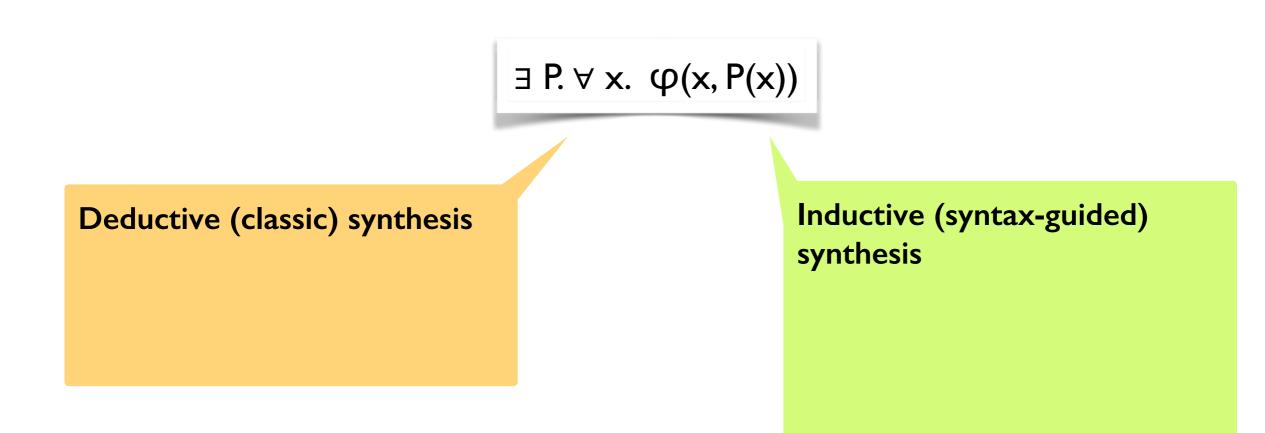
φ may be a formula, a reference implementation, input/output pairs, traces, demonstrations, etc.

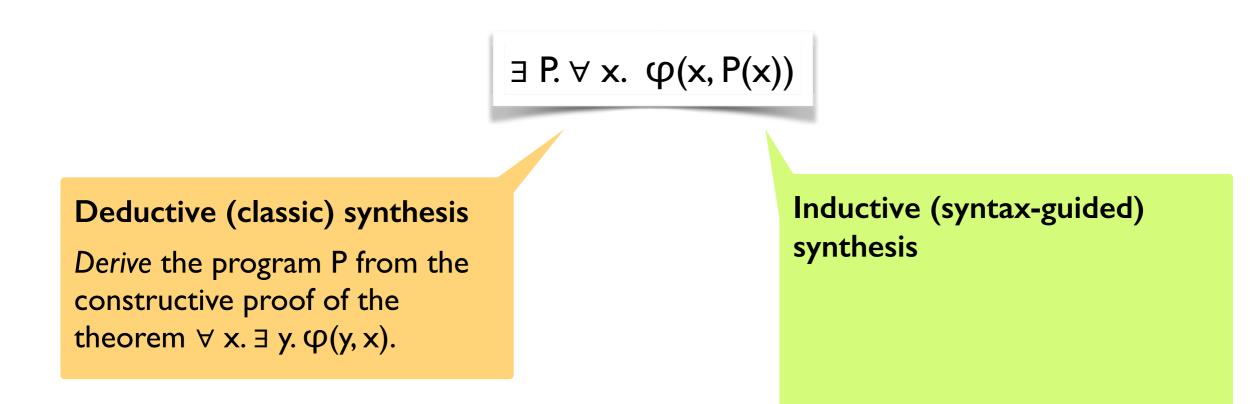
Synthesis improves

- Productivity (when writing φ is easier than writing P).
- Correctness (when verifying φ is easier than verifying P).

∃ P. ∀ x. φ(x, P(x))

Find a program P that satisfies the specification φ on all inputs.





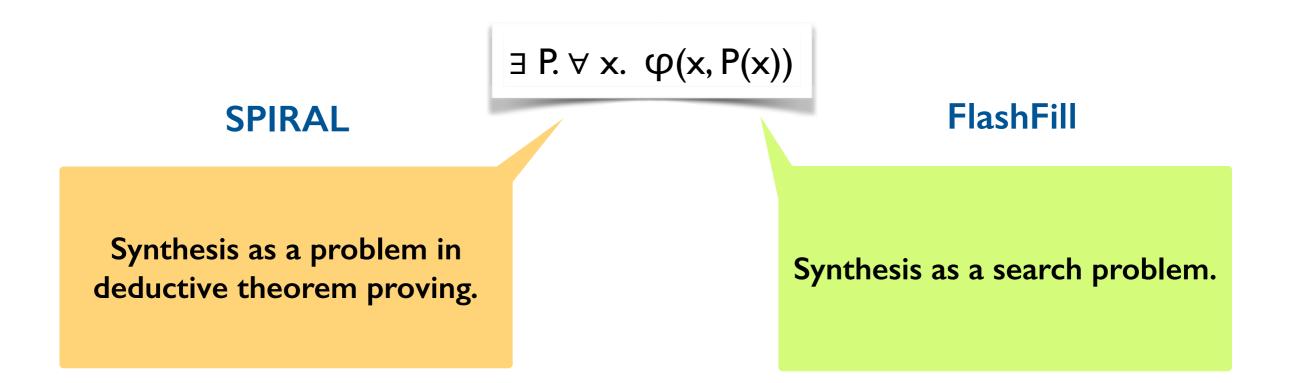
#### $\exists P. \forall x. \phi(x, P(x))$

#### **Deductive (classic) synthesis**

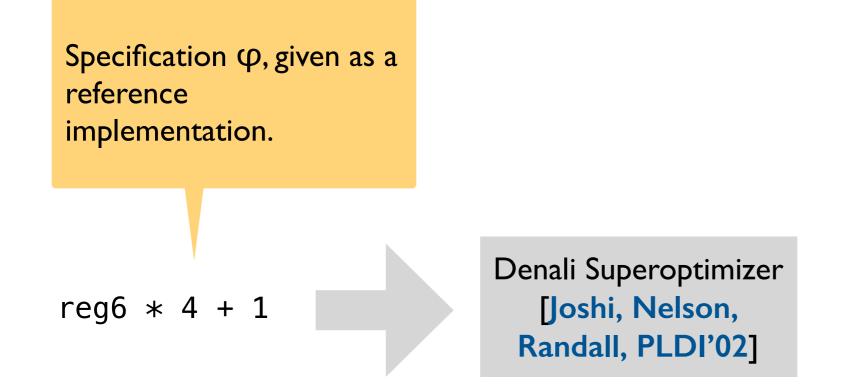
Derive the program P from the constructive proof of the theorem  $\forall x. \exists y. \varphi(y, x)$ .

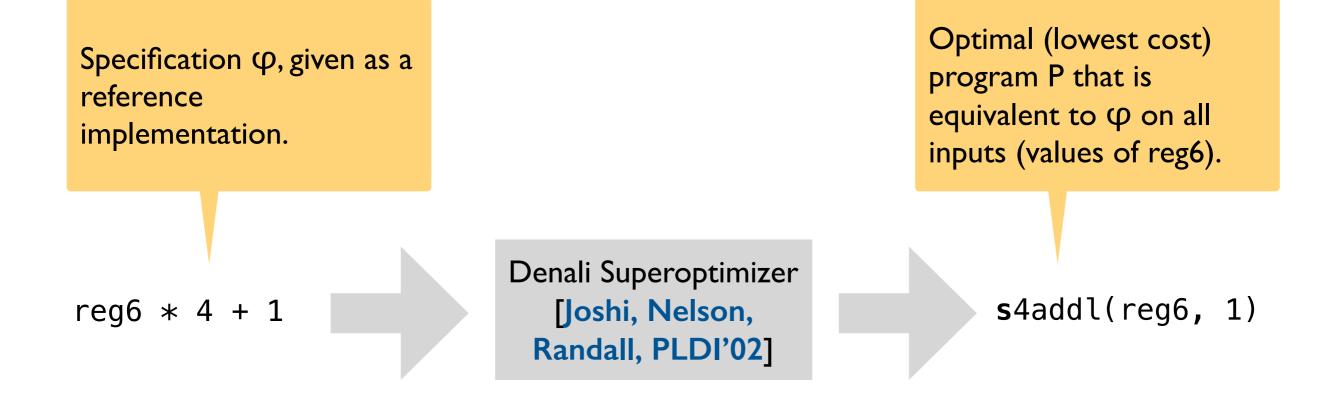
# Inductive (syntax-guided) synthesis

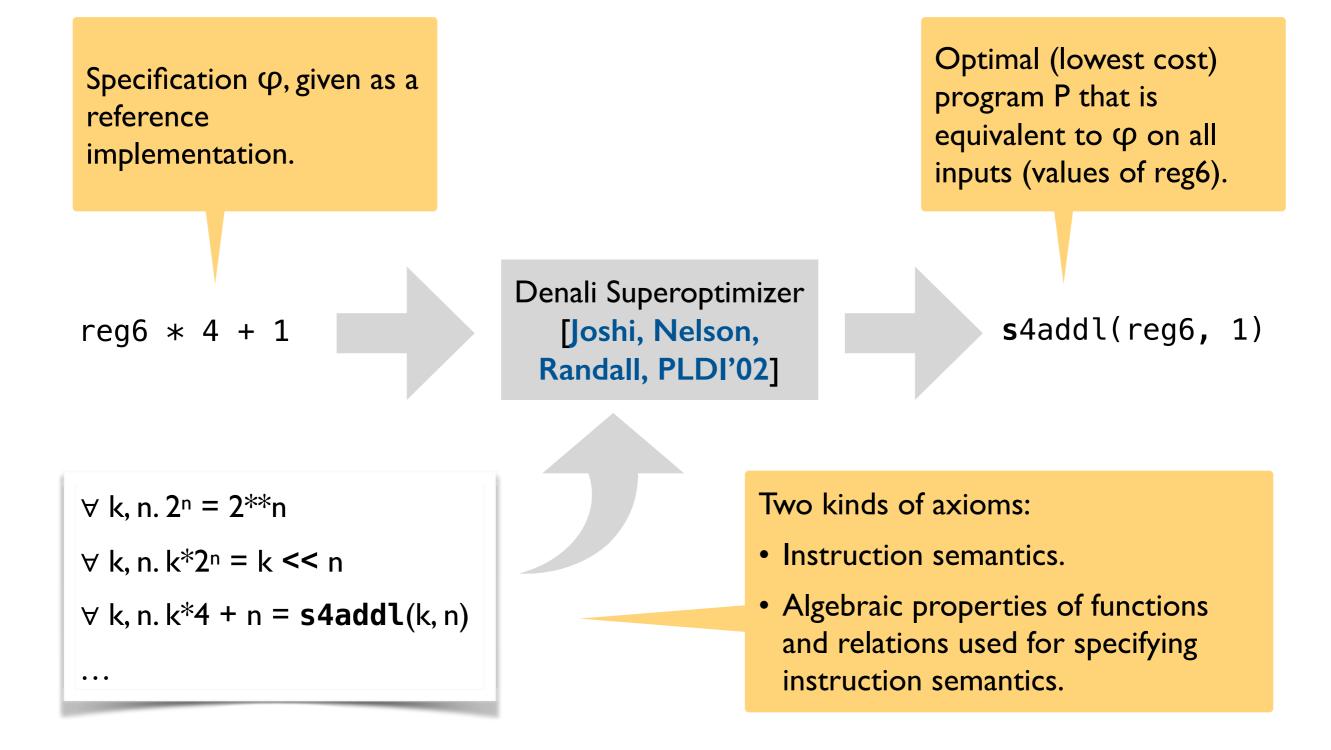
Discover the program P by searching a restricted space of candidate programs for one that satisfies  $\varphi$  on all inputs.

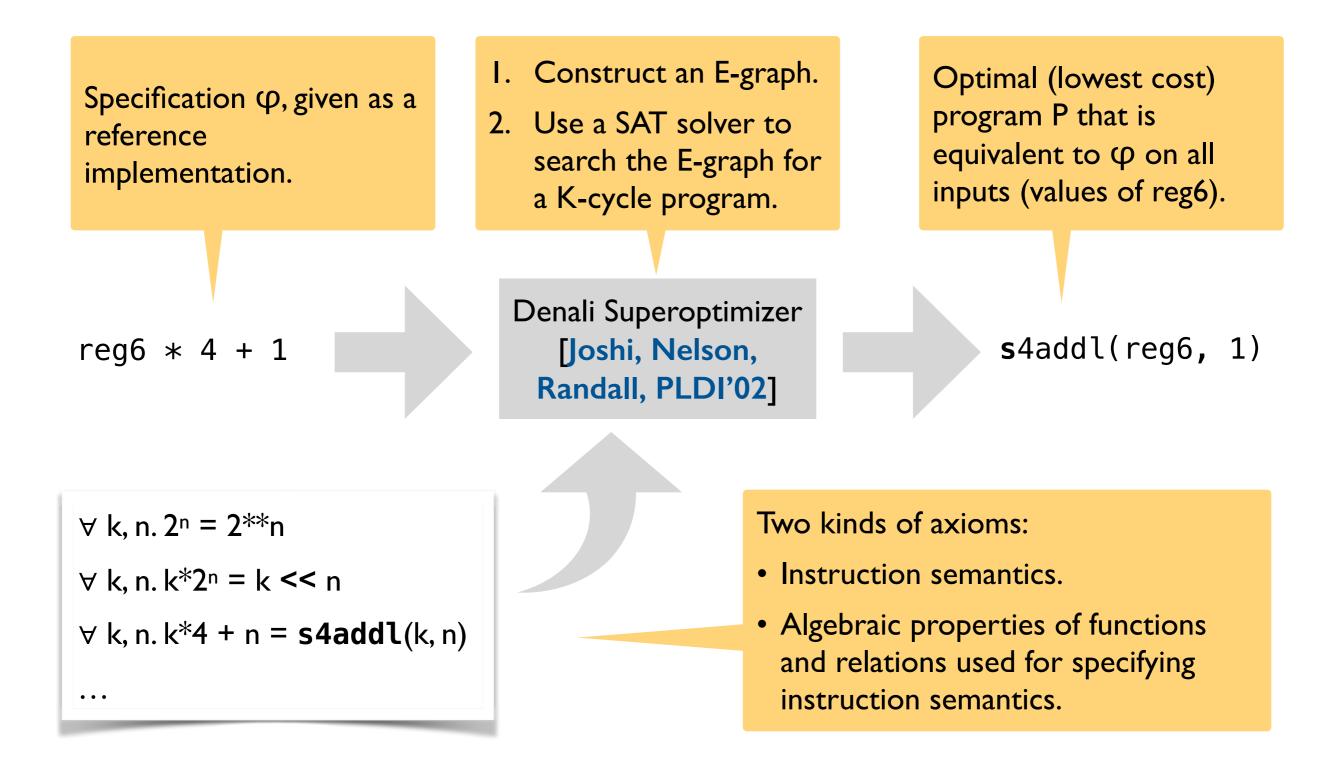


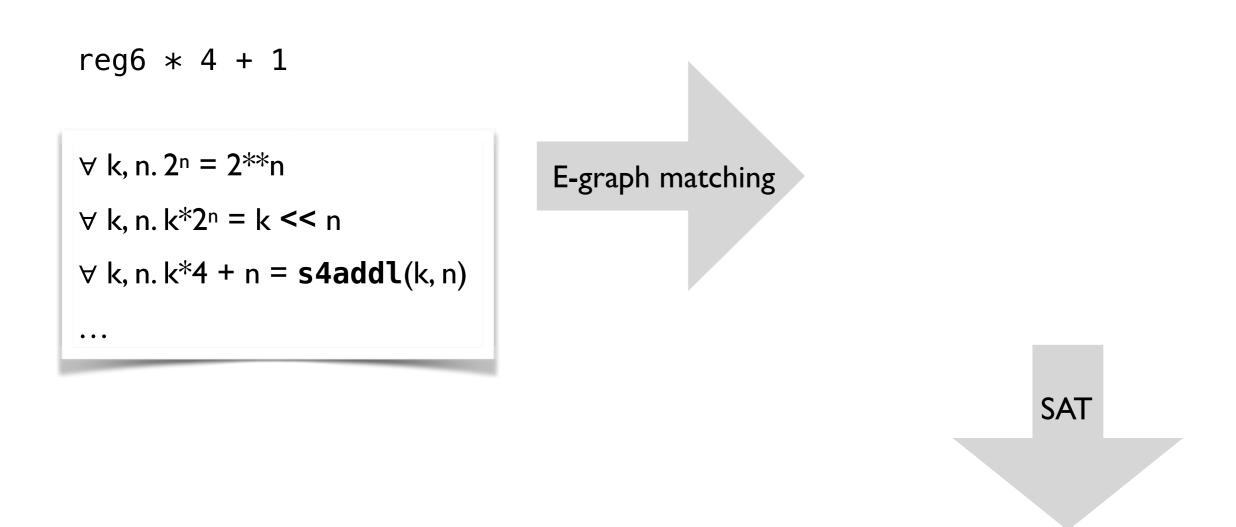
Denali Superoptimizer [Joshi, Nelson, Randall, PLDI'02]



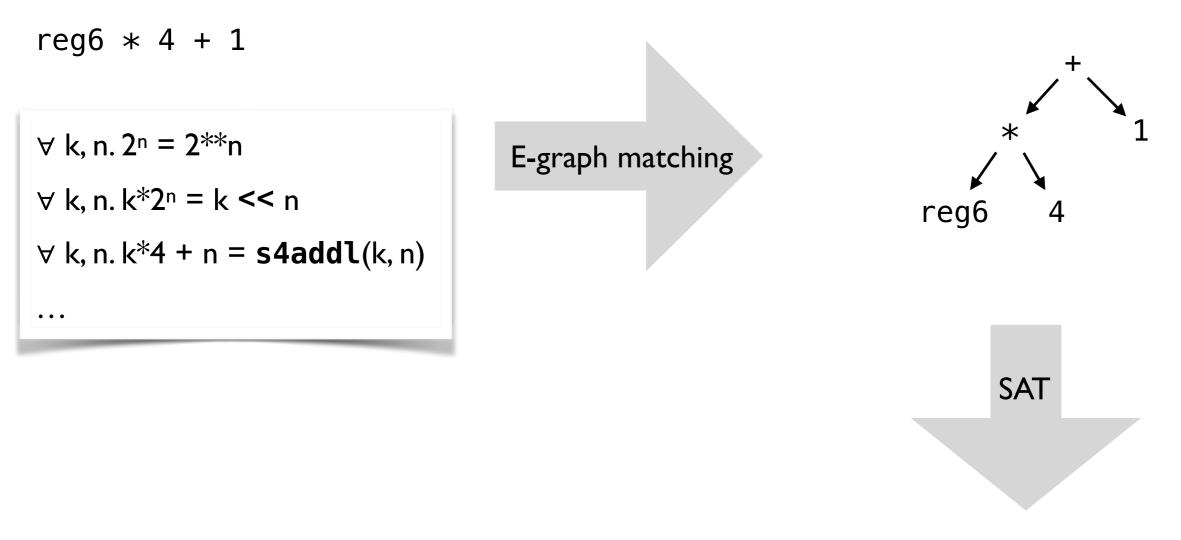




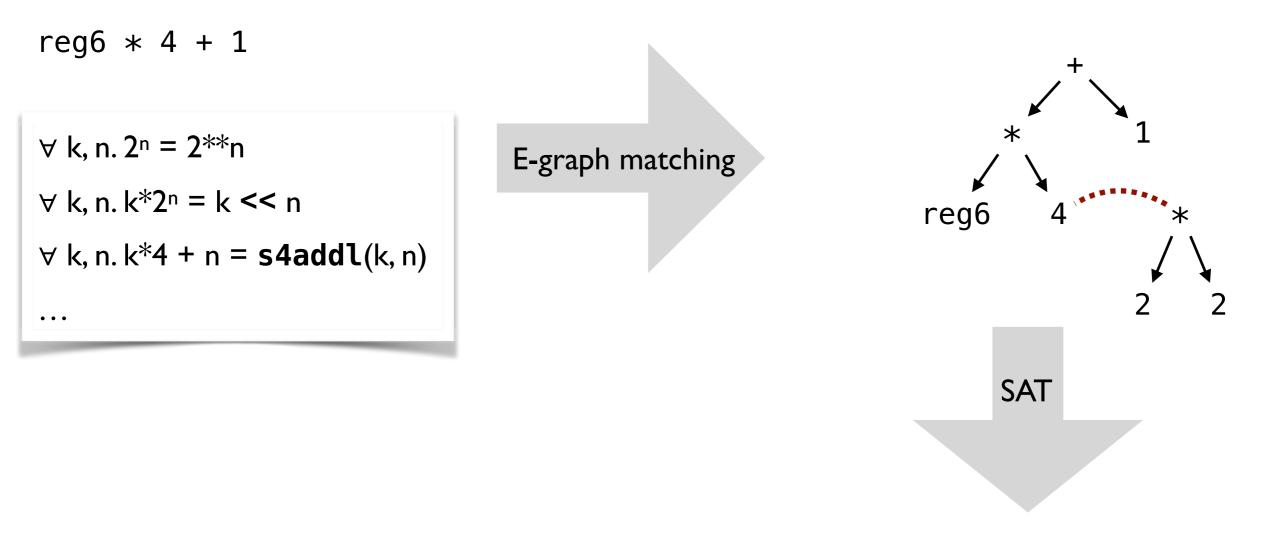


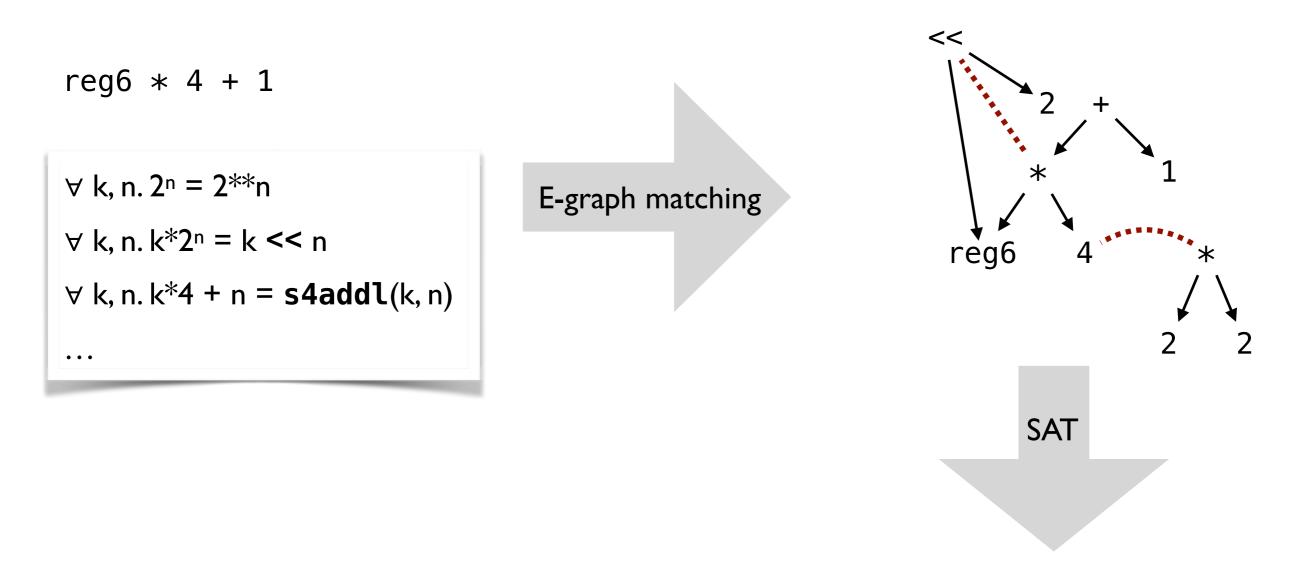


#### s4addl(reg6, 1)

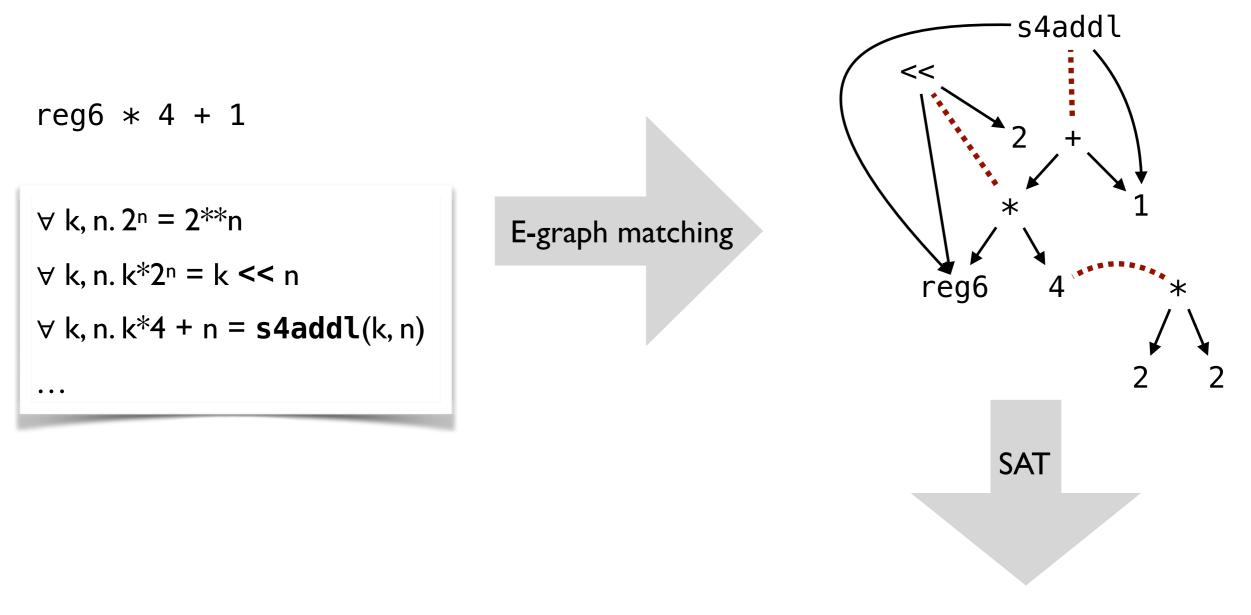


#### s4addl(reg6, 1)





#### s4addl(reg6, 1)



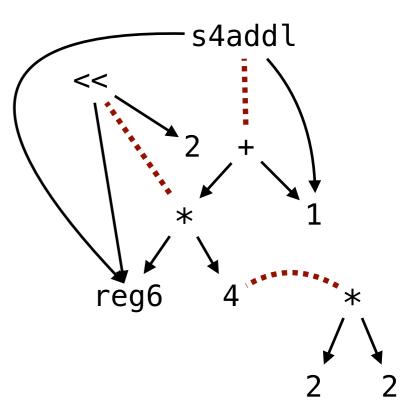
# **Deductive synthesis versus compilation**

#### **Deductive synthesizer**

- Non-deterministic.
- Searches all correct rewrites for one that is optimal.

#### Compiler

- Deterministic.
- Lowers a source program into a target program using a *fixed sequence of rewrite steps*.



reg6 \* 4 + 1 reg6 << 2 + 1

#### **Deductive synthesis versus inductive synthesis**

#### $\exists P. \forall x. \phi(x, P(x))$

#### **Deductive synthesis**

- Efficient and provably correct: thanks to the semantics-preserving rules, only correct programs are explored.
- Requires *sufficient axiomatization* of the domain.
- Requires *complete* specifications to seed the derivation.

#### **Deductive synthesis versus inductive synthesis**

#### $\exists P. \forall x. \phi(x, P(x))$

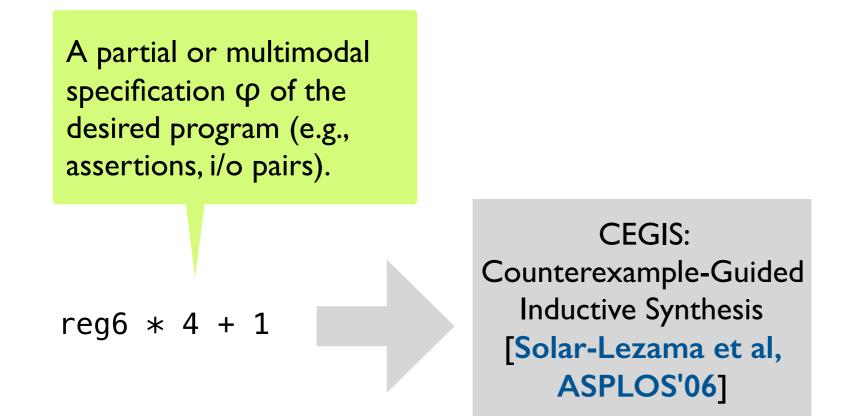
#### **Deductive synthesis**

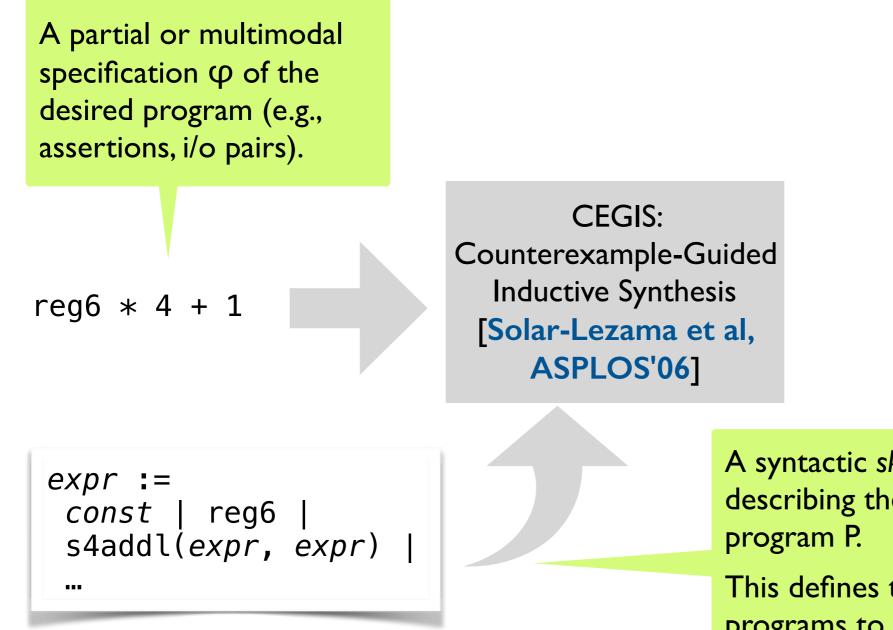
- Efficient and provably correct: thanks to the semantics-preserving rules, only correct programs are explored.
- Requires sufficient axiomatization of the domain.
- Requires *complete* specifications to seed the derivation.

#### Inductive synthesis

- Works with *multi-modal and partial* specifications.
- Requires no axioms.
- But often at the cost of lower efficiency and weaker (bounded) guarantees on the correctness/ optimality of synthesized code.

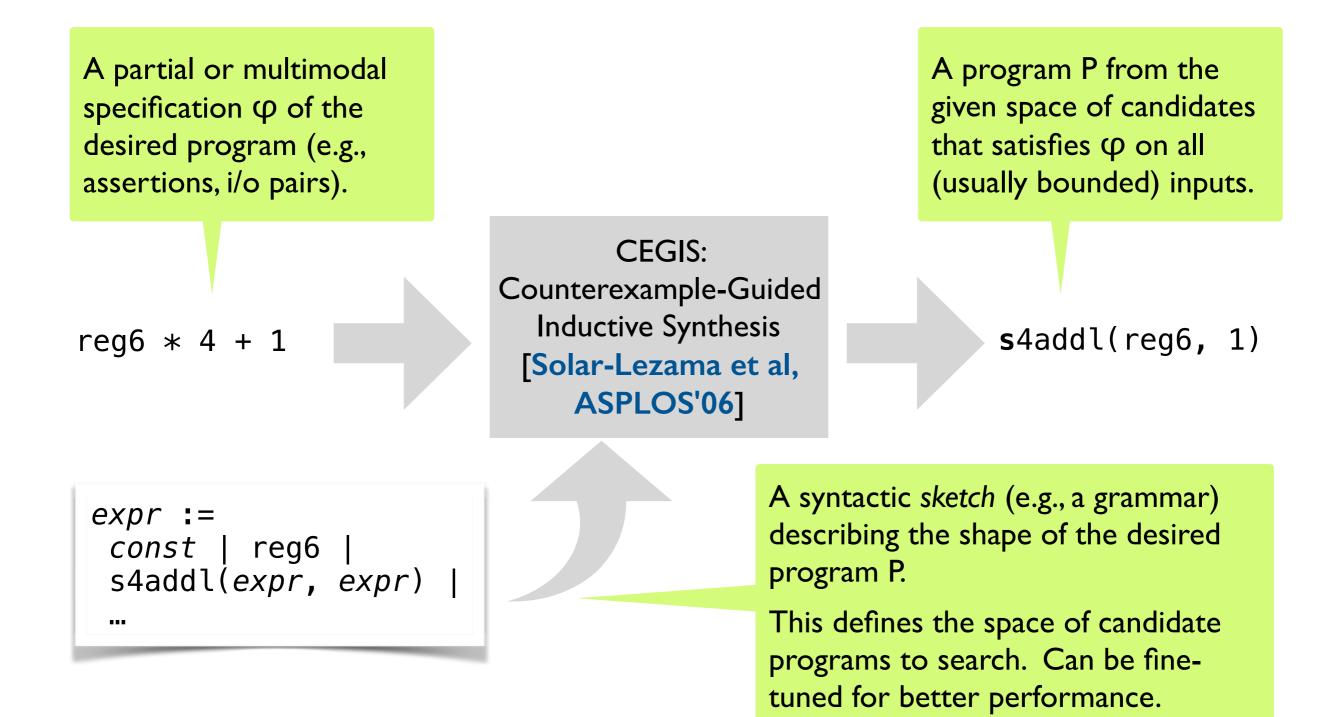
CEGIS: Counterexample-Guided Inductive Synthesis [Solar-Lezama et al, ASPLOS'06]

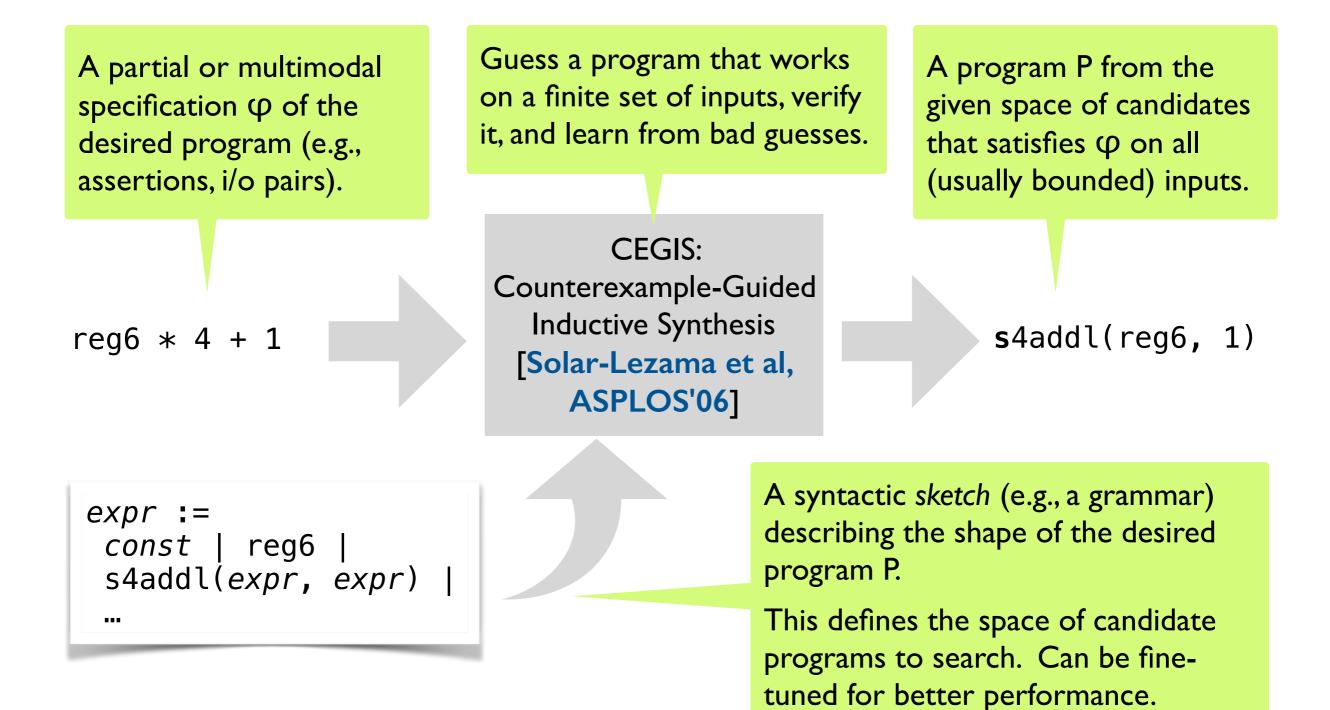


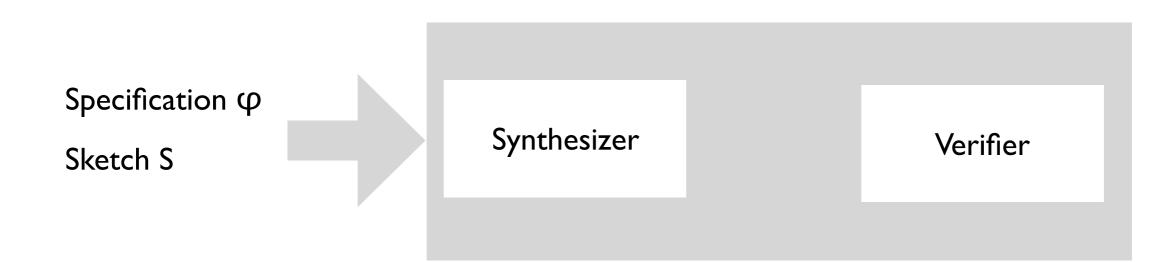


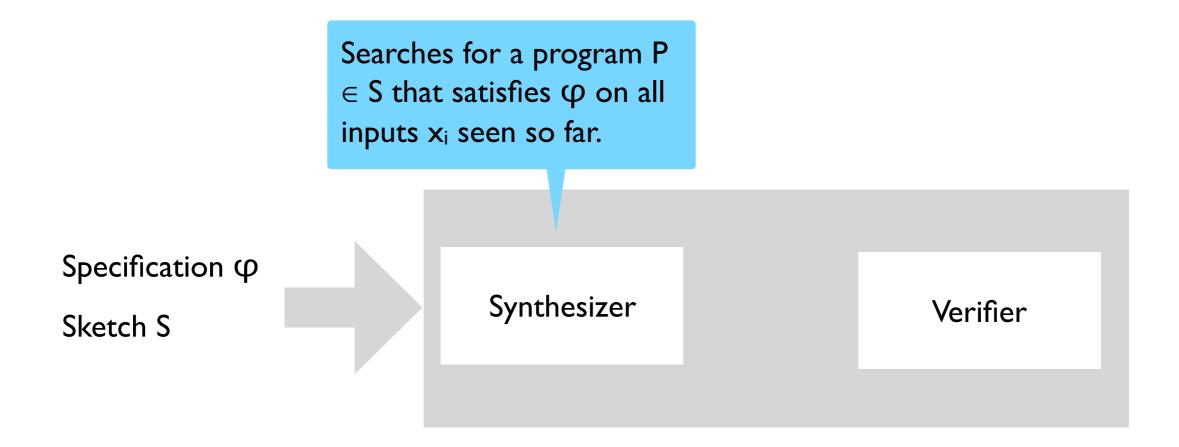
A syntactic sketch (e.g., a grammar) describing the shape of the desired program P.

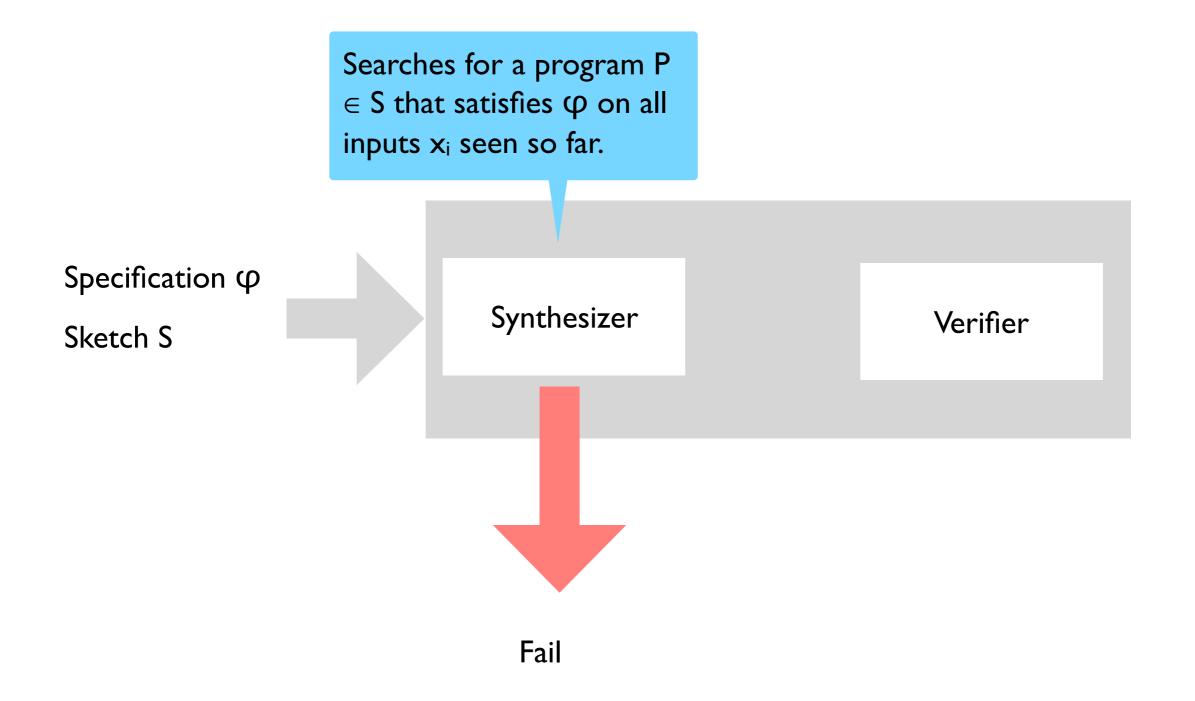
This defines the space of candidate programs to search. Can be fine-tuned for better performance.

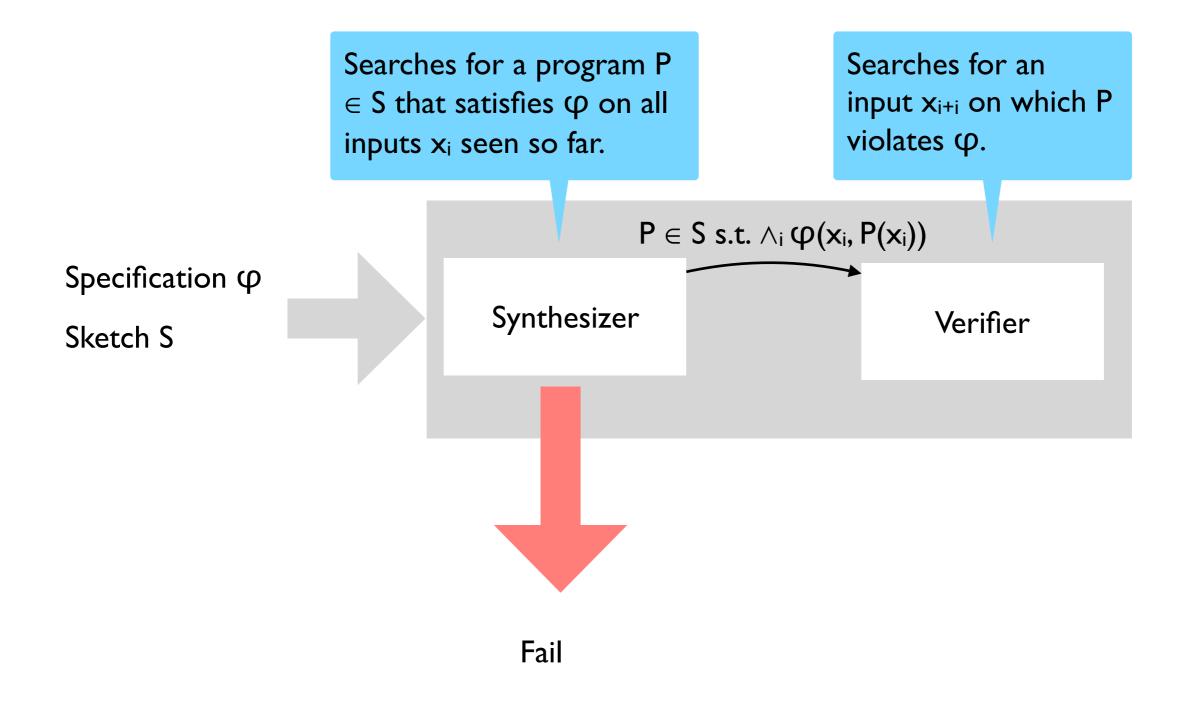


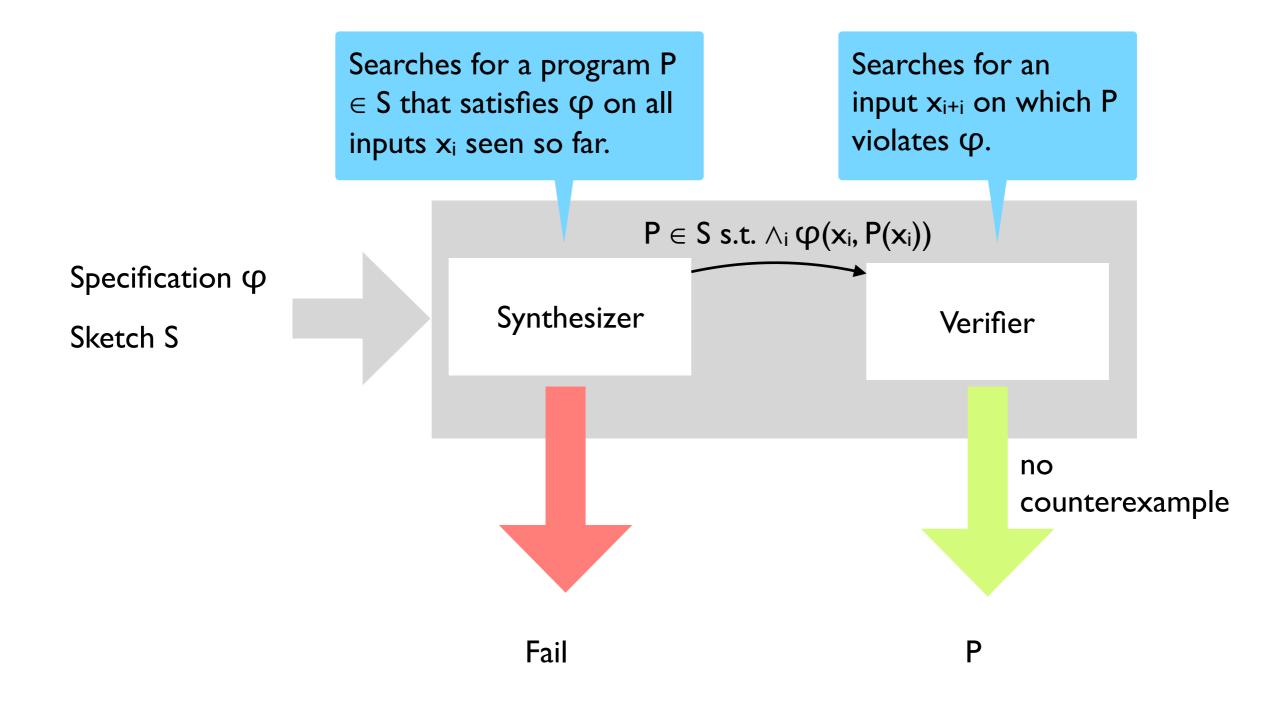


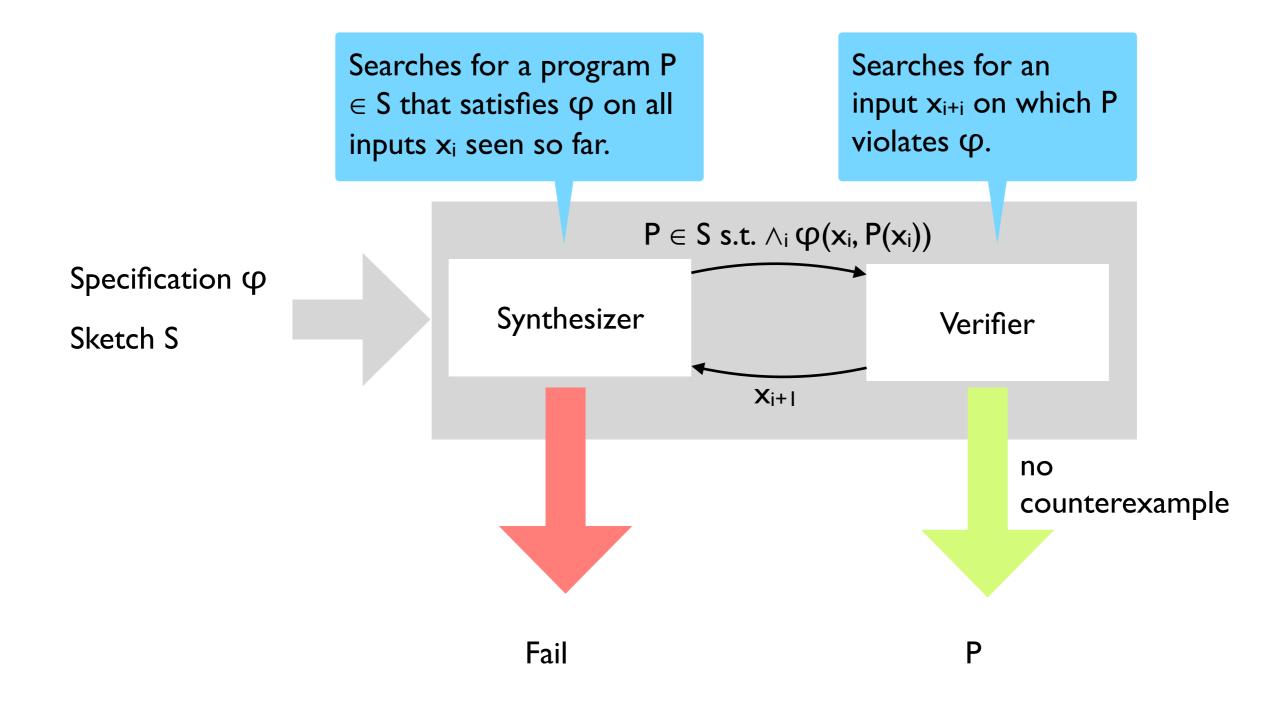


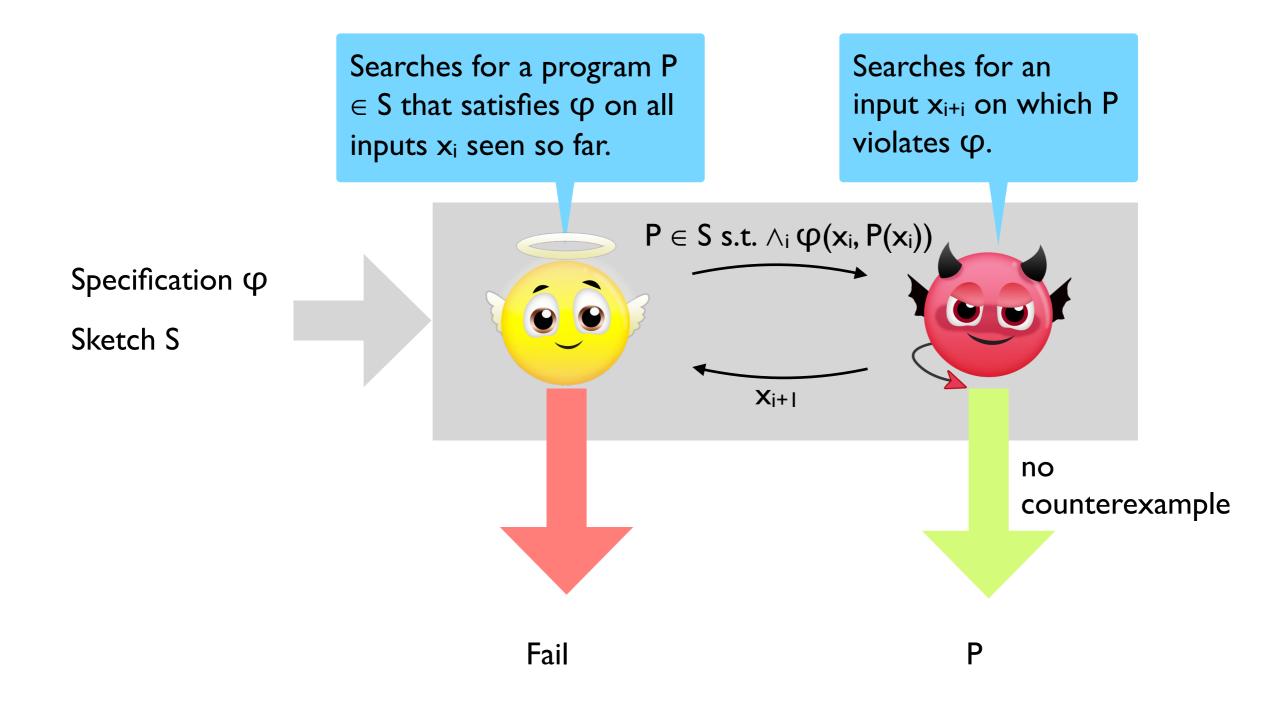


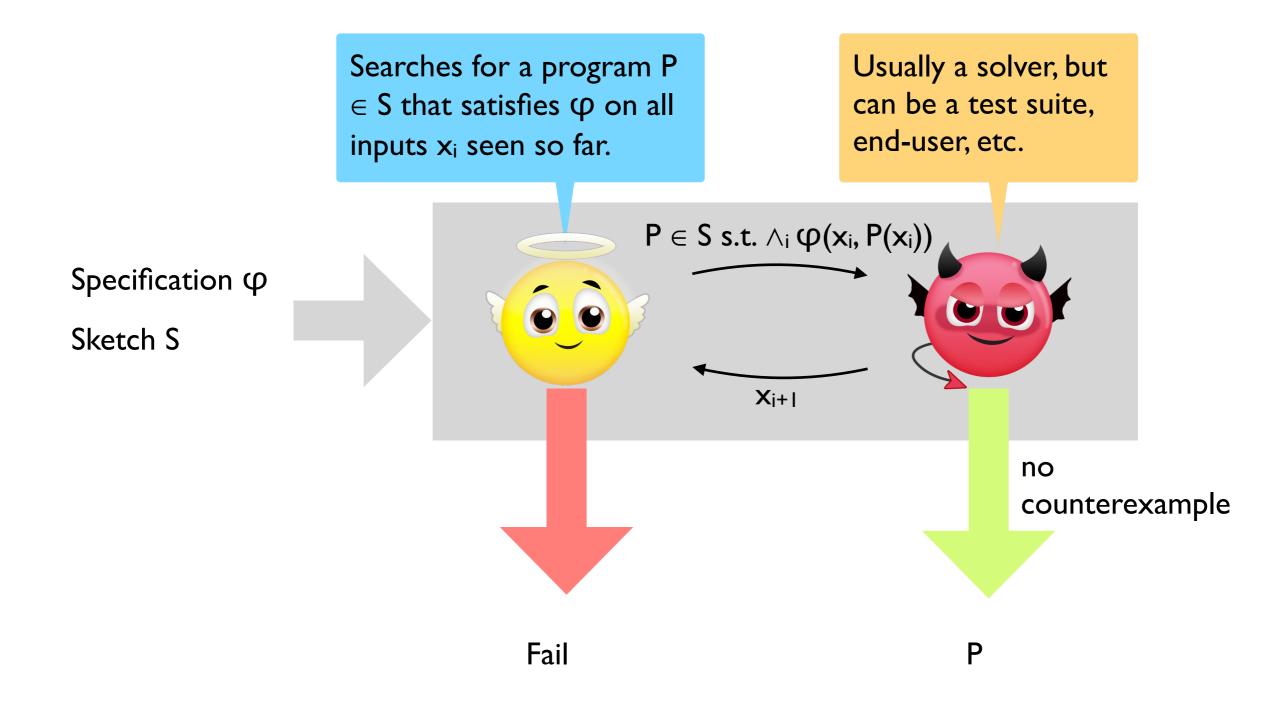




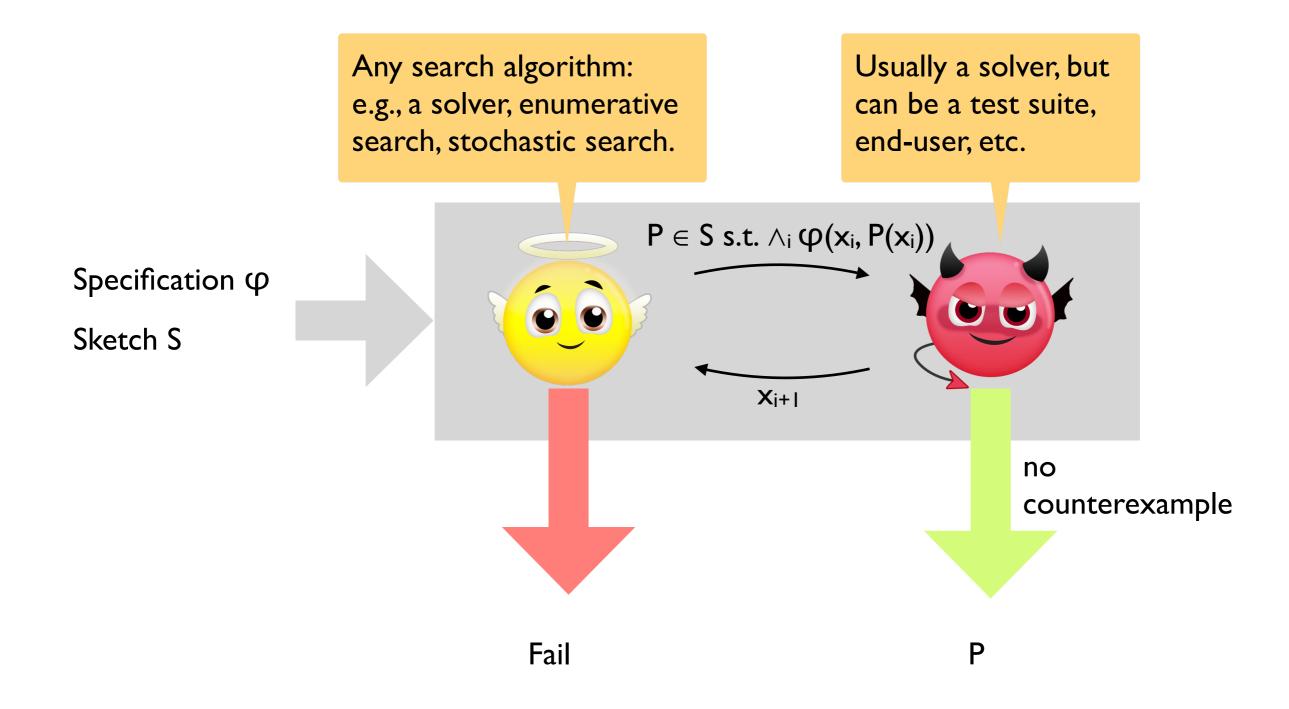


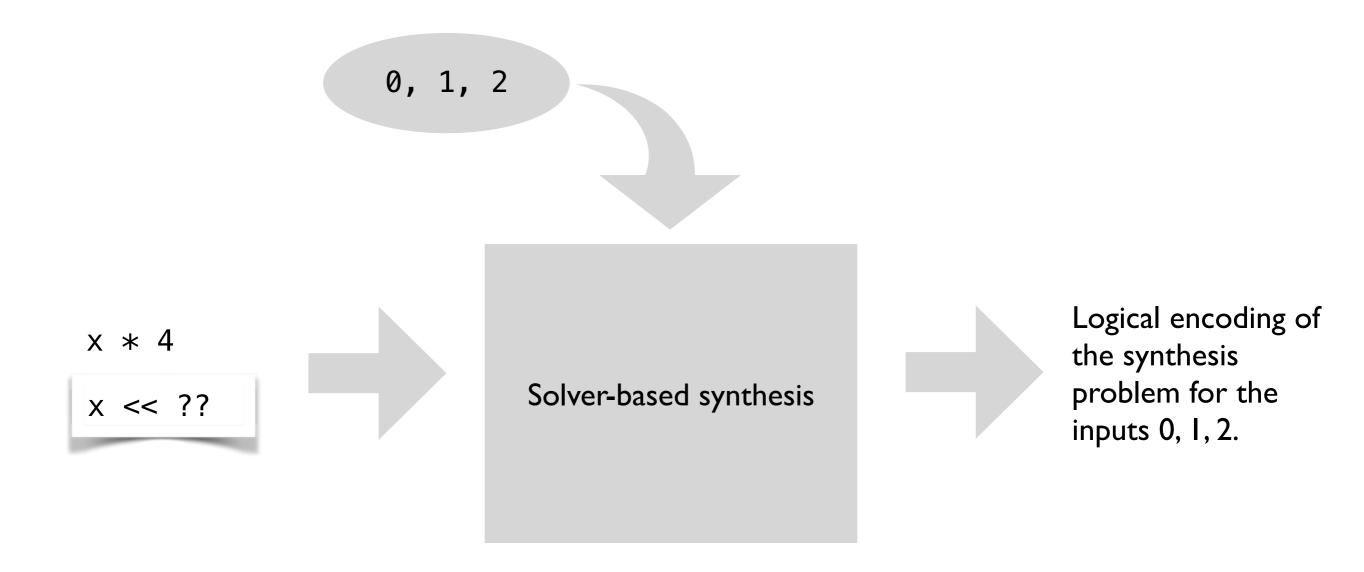




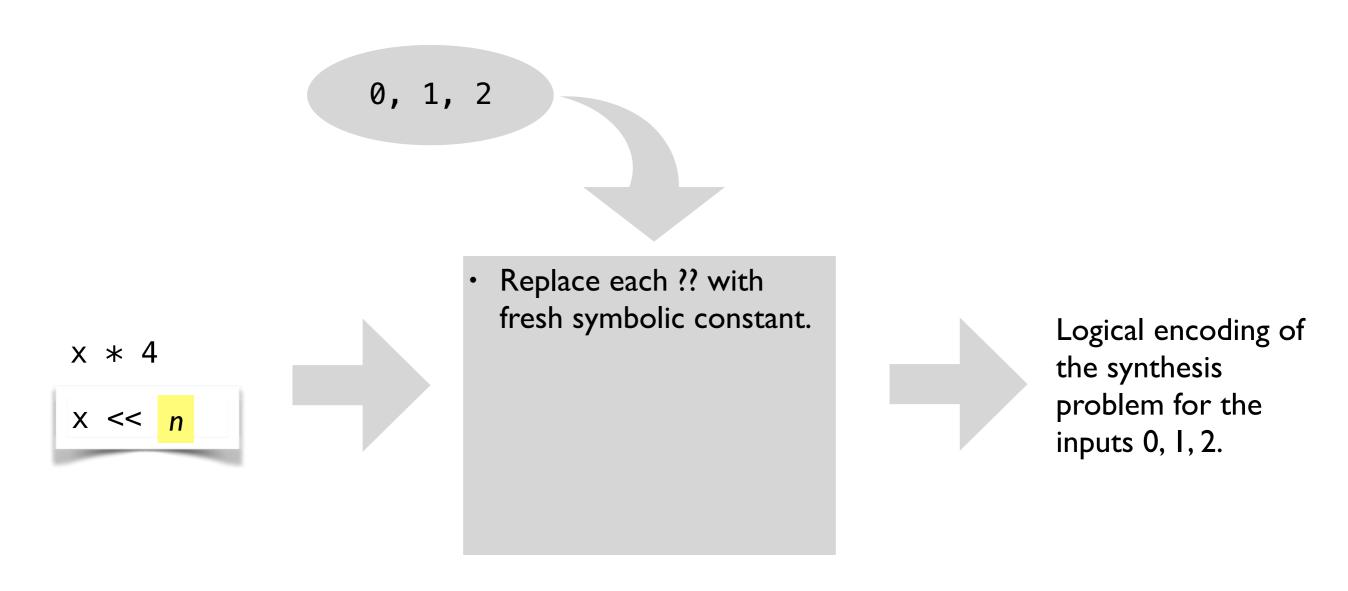


# **Overview of CEGIS**



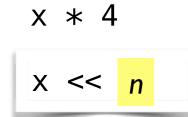


#### [Solar-Lezama et al, ASPLOS'06]



#### [Solar-Lezama et al, ASPLOS'06]

0, 1, 2



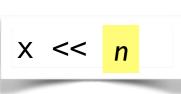
- Replace each ?? with fresh symbolic constant.
- Translate the resulting problem to constraints w.r.t. the current inputs.

 $(0 << n = 0) \land$  $(1 << n = 4) \land$ (2 << n = 8)

### [Solar-Lezama et al, ASPLOS'06]

0, 1, 2

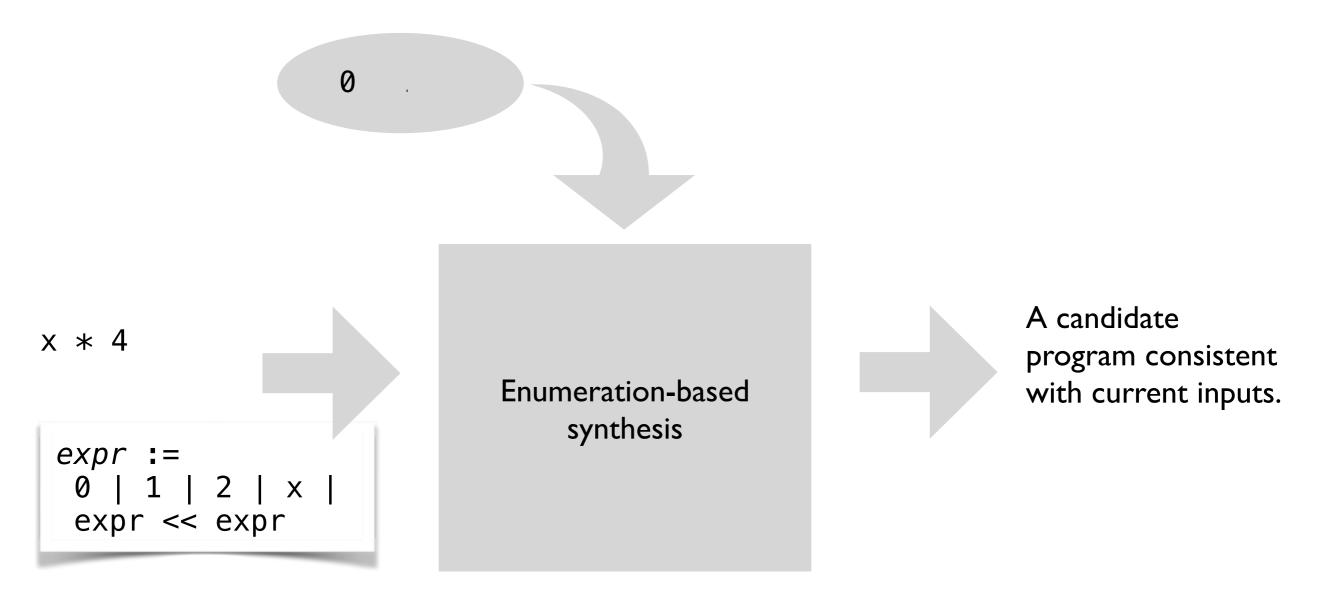




- Replace each ?? with fresh symbolic constant.
- Translate the resulting problem to constraints w.r.t. the current inputs.
- If SAT, convert the model to a program P.

### [Solar-Lezama et al, ASPLOS'06]

 $(0 << n = 0) \land$  $(1 << n = 4) \land$ (2 << n = 8)



x \* 4

expr	:=				<i>P</i>
	1	2		Х	
expr	^ <<	ex	рі		

0

- Iteratively construct all programs of size K until one is consistent with the current inputs.
- If two programs produce the same output on all current inputs, keep just one of the two.

A candidate program consistent with current inputs.

x \* 4

expr := 0 | 1 | 2 | x | expr << expr

0

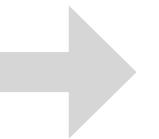
- Iteratively construct all programs of size K until one is consistent with the current inputs.
- If two programs produce the same output on all current inputs, keep just one of the two.

0, 1

x \* 4

expr	`:=			r
0	1	2	X	
exp	r <-	< ex	pr	

- Iteratively construct all programs of size K until one is consistent with the current inputs.
- If two programs produce the same output on all current inputs, keep just one of the two.



0, 1

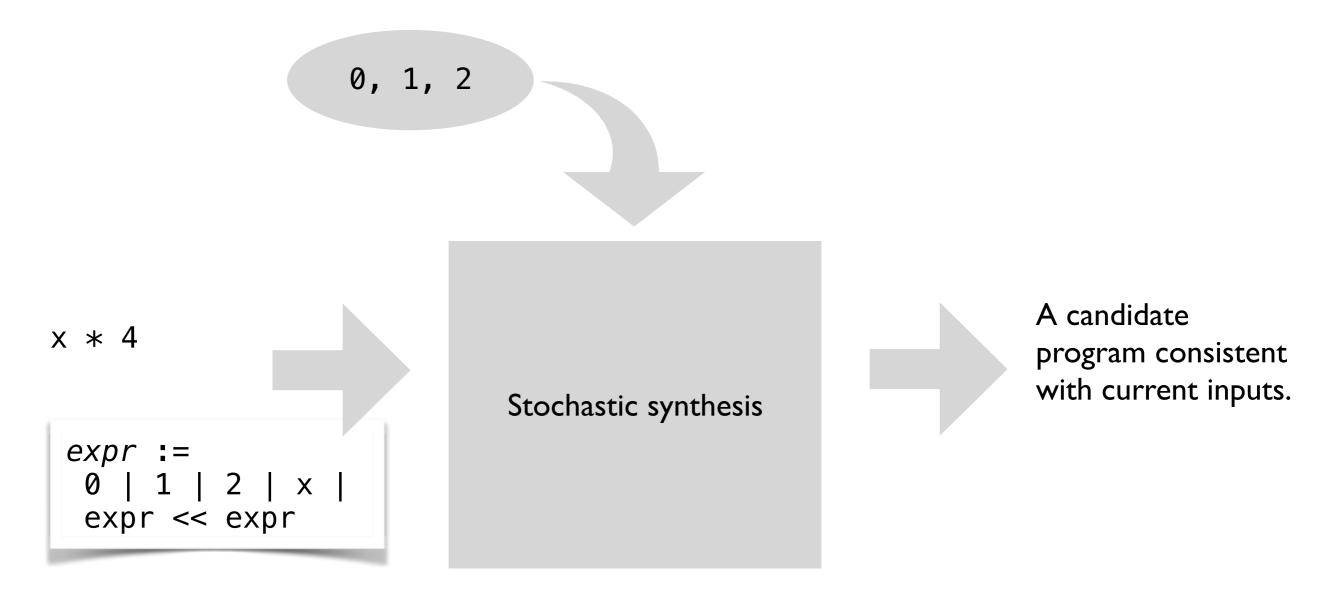
x \* 4

expr	:=			V
0	1	2	Х	
exp	r <<	expr		

- Iteratively construct all programs of size K until one is consistent with the current inputs.
- If two programs produce the same output on all current inputs, keep just one of the two.

K=1:0, I, 2, x K=2: I << 2, 2 << 2, x << I, x << 2

# Synthesizing programs with stochastic search



### [Schkufza et al, ASPLOS'13]

# Synthesizing programs with stochastic search

0, 1, 2

x \* 4

expr := 0 | 1 | 2 | x | expr << expr

- Use Metropolis-Hastings to sample expressions.
- Mutate the current
  candidate program and
  keep the mutation with
  probability proportional
  to its correctness w.r.t.
  the current inputs.

A candidate program consistent with current inputs.

### [Schkufza et al, ASPLOS'13]

# Summary

### Today

- Deductive synthesis with axioms and E-graphs
- Inductive synthesis with solvers, enumeration, and stochastic search

### **Next lecture**

• Solver-aided languages

