

Computer-Aided Reasoning for Software

Angelic Execution

CSE507

courses.cs.washington.edu/courses/cse507/14au/

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Today

Today

Last lecture

- Verifying compiler optimizations with SMT solvers

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- Beyond verification: solvers as interpreters

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Last lecture

- Verifying compiler optimizations with SMT solvers

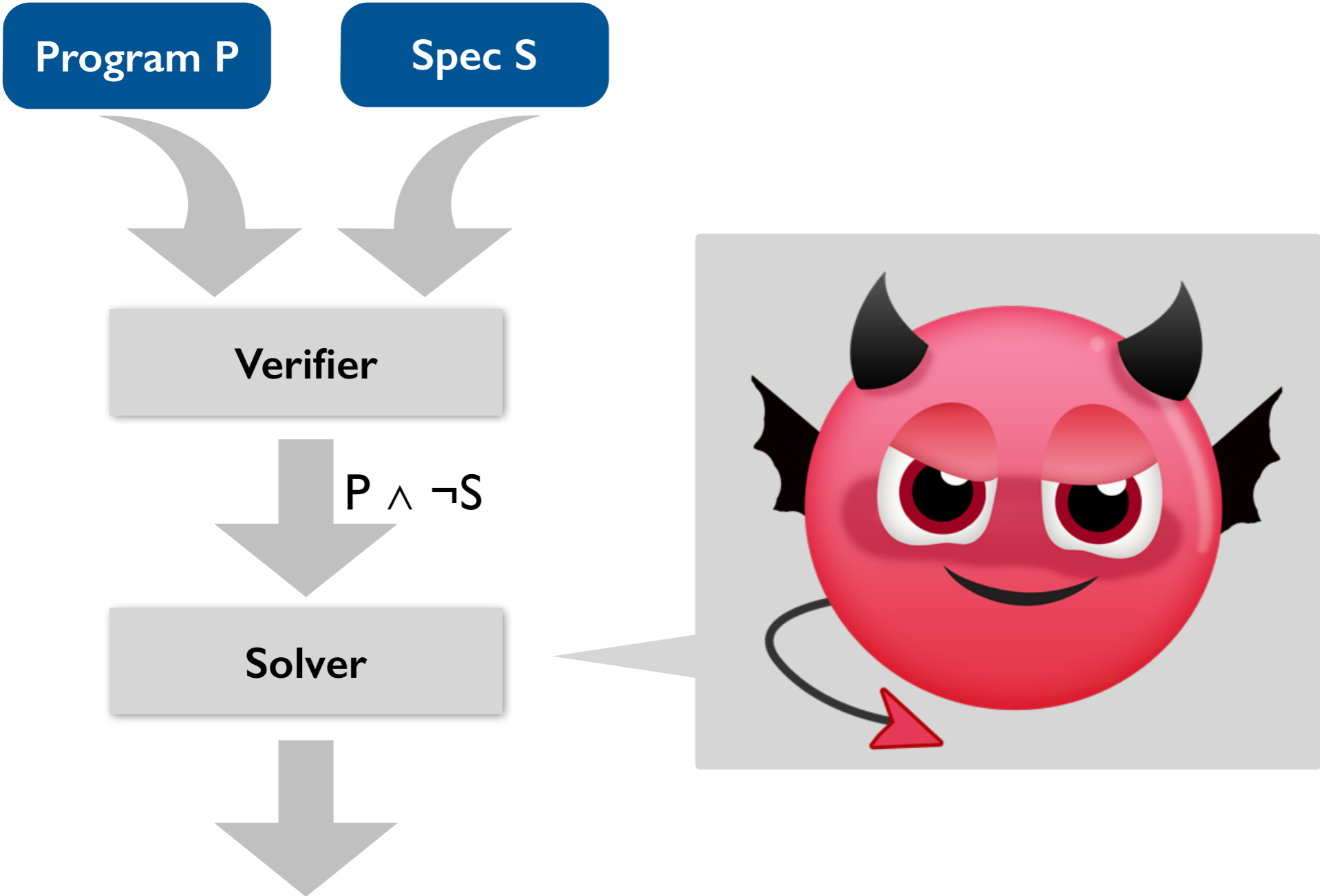
Today

- Beyond verification: solvers as interpreters

Announcements

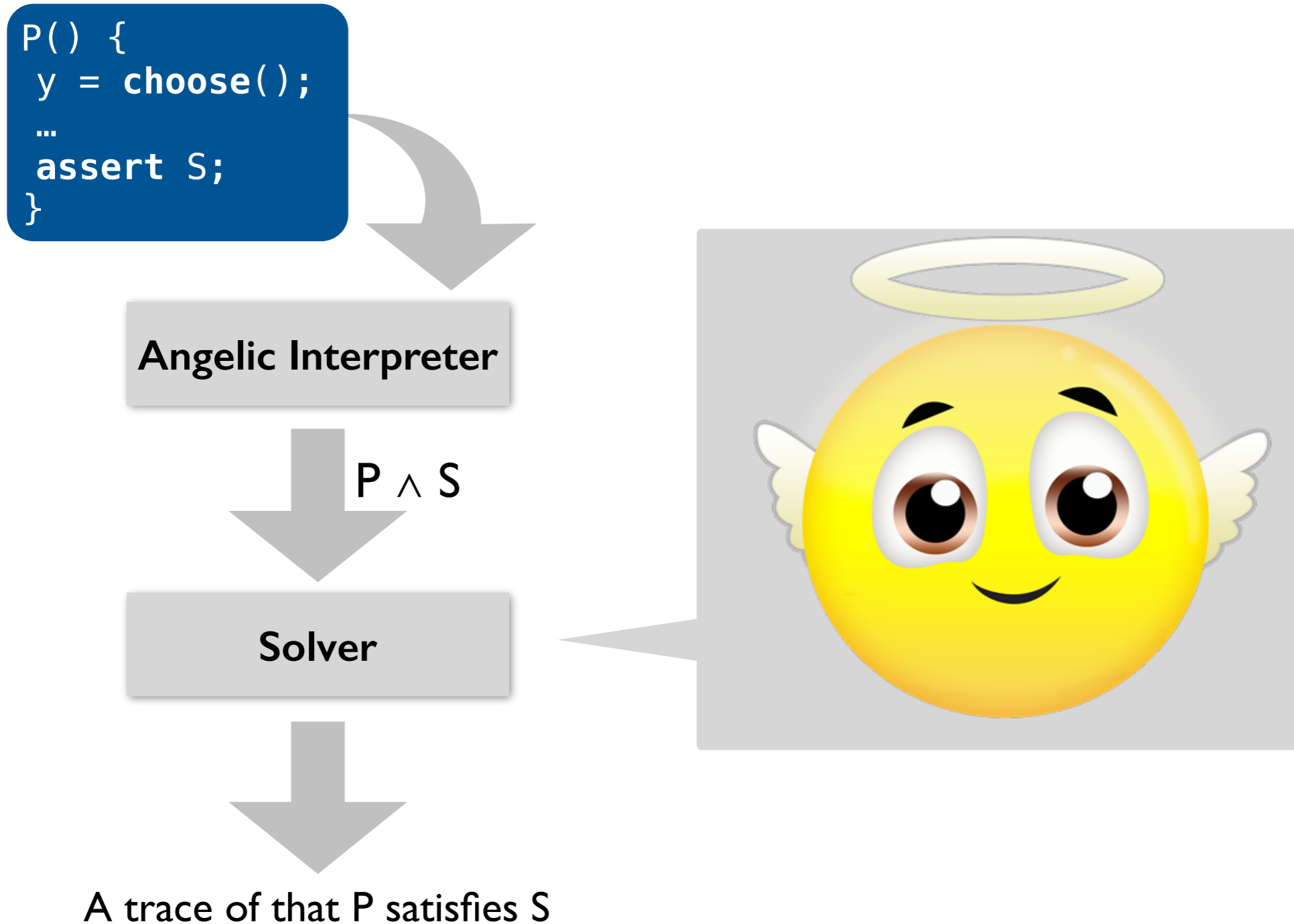
- Project presentation logistics:
 - 8 min talk (problem statement, demo, results)
 - An electronic poster (single slide)

So far, we have used solvers as demonic oracles



An input i on which P violates S

But solvers can also act as angelic oracles



But solvers can also act as angelic oracles

```
P() {  
  y = choose();  
  ...  
  assert S;  
}
```

Angelic Interpreter

$P \wedge S$

Solver

A trace of that P satisfies S

1. Definitions
2. Implementations
3. Applications



Angelic non-determinism, two ways

Angelic choice:

`choose(T)`



Robert Floyd, 1966

Specification statement:

$X_1, \dots, X_n \leftarrow [\text{pre}, \text{post}]$



Carroll Morgan, 1988

Angelic non-determinism, two ways

Angelic choice:

`choose(T)`

Specification statement:

$x_1, \dots, x_n \leftarrow [\text{pre}, \text{post}]$



Robert Floyd, 1966

Non-deterministically chooses a value of (finite) type T so that the rest of the program terminates successfully.

Designed to abstract away the details of backtracking search.



Carroll Morgan, 1988

A programming abstraction

Angelic non-determinism, two ways

Angelic choice:

`choose(T)`



Robert Floyd, 1966

A programming abstraction

Specification statement:

$x_1, \dots, x_n \leftarrow [pre, post]$

Non-deterministically modifies the values of frame variables x_1, \dots, x_n so that *post* holds in the next state if *pre* holds in the current state.

Designed to enable derivation of programs from specifications via step-wise refinement.



Carroll Morgan, 1988

A refinement abstraction

Angelic non-determinism, two ways: an example

Angelic choice:

`choose(T)`

```
s = 16
r = choose(int)
if (r ≥ 0)
  assert r*r ≤ s < (r+1)*(r+1)
else
  assert r*r ≤ s < (r-1)*(r-1)
```

Specification statement:

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s = 16
r ← [(r ≥ 0 ∧
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      (r < 0 ∧
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```

Interleaves imperative and angelic execution. As a result, implementation requires global constraint solving.

Specification statement:

$x_1, \dots, x_n \leftarrow [\text{pre}, \text{post}]$

```
s = 16
r ← [(r ≥ 0 ∧
      r*r ≤ s < (r+1)*(r+1)) ∨
      (r < 0 ∧
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```

Alternates between angelic and imperative execution. As a result, implementation requires only local constraint solving.

Angelic non-determinism, two ways: an example

Angelic choice:

`choose(T)`

```
s = 16
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```

“Angelic Interpretation”

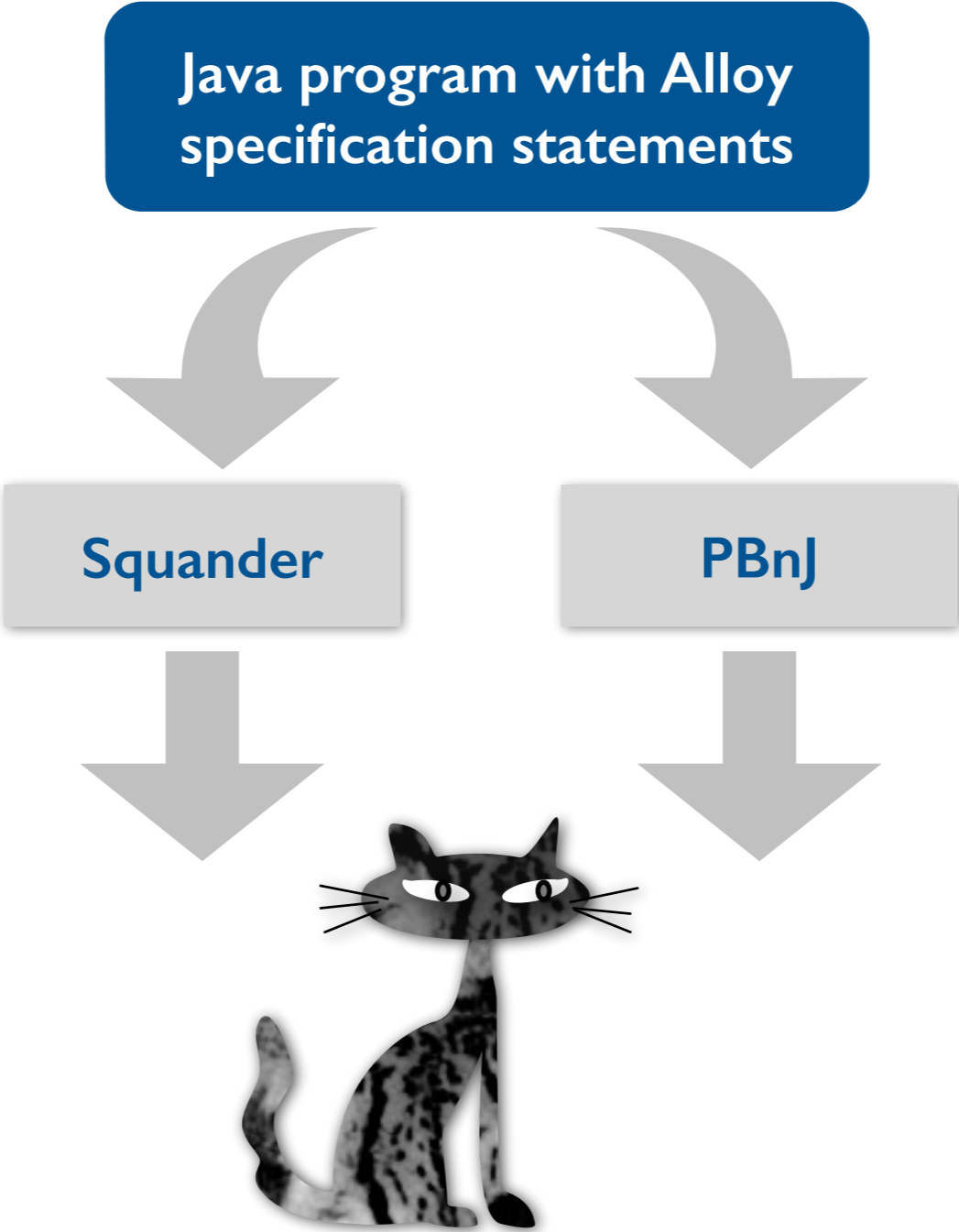
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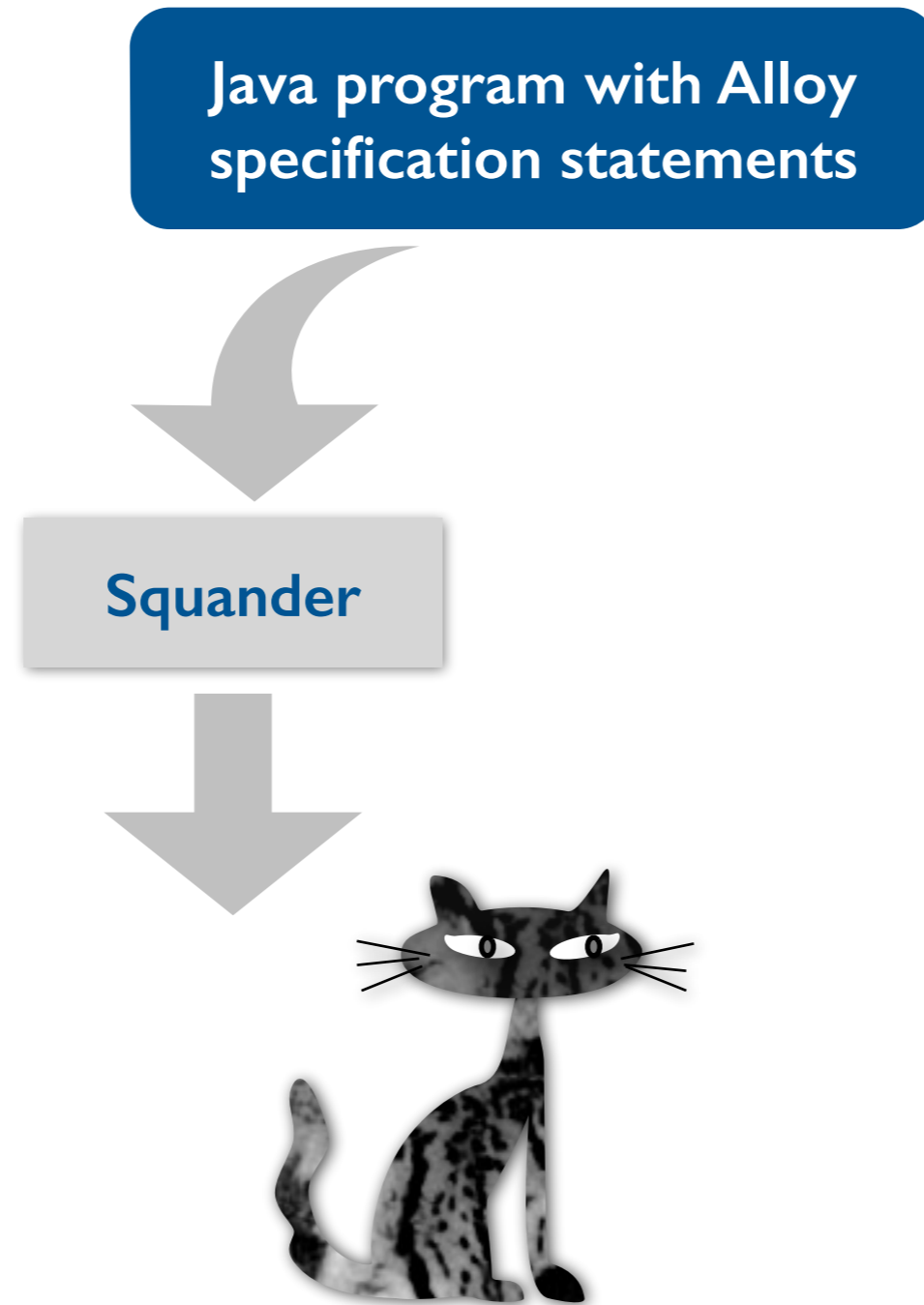
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```

“Mixed Interpretation”

Mixed interpretation with a model finder (1/4)



Mixed interpretation with a model finder (1/4)



Mixed interpretation with a model finder (2/4)

```
@Requires("z.key !in this.nodes.key")
@Ensures("this.nodes = @old(this.nodes) + z")
@Modifies("this.root,
          this.nodes.left | _<1> = null,
          this.nodes.right | _<1> = null")

public void insert(Node z) {
    Squander.exe(this, z); }
}
```

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```

Specification statements describing insertion of a new node z into a binary search tree.

Mixed interpretation with a model finder (2/4)

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```

```
public void insert(Node z) {
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```

Specification statements describing insertion of a new node z into a binary search tree.

Call to the Squander mixed interpreter ensures that the state of this tree and the node z is mutated so that the insertion specification is satisfied when the insert method returns.

Mixed interpretation with a model finder (2/4)

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Specification statements describing insertion of a new node z into a binary search tree.

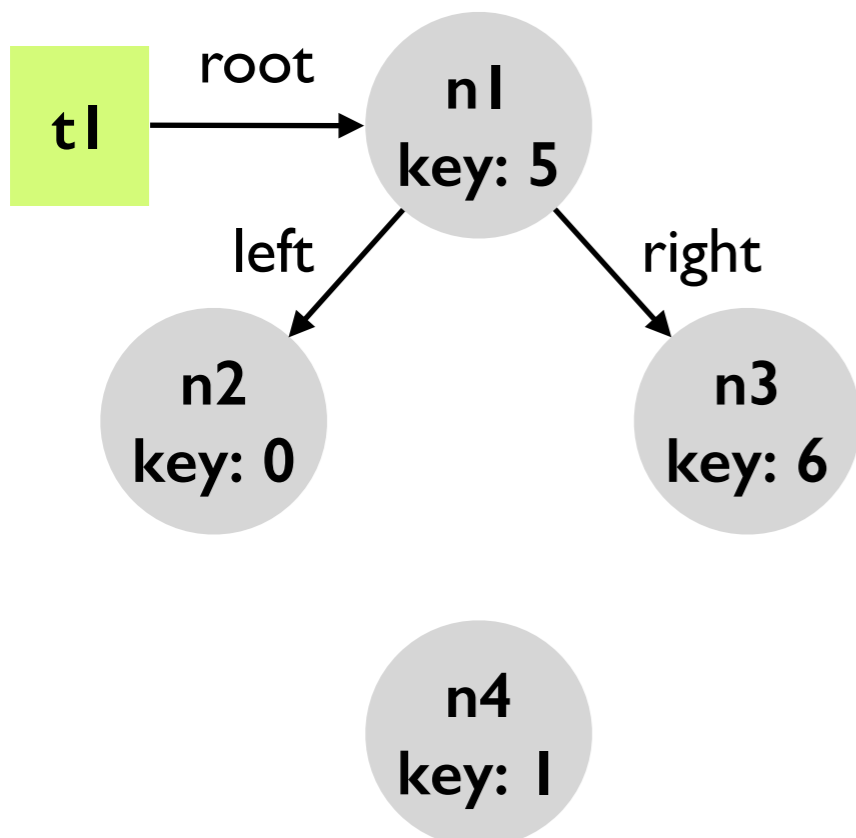
Execution steps:

- Serialize the relevant part of the heap to a universe and bounds
- Use Kodkod to solve the specs against the resulting universe / bounds
- Deserialize the solution (if any) and update the heap accordingly

Mixed interpretation with a model finder (3/4)

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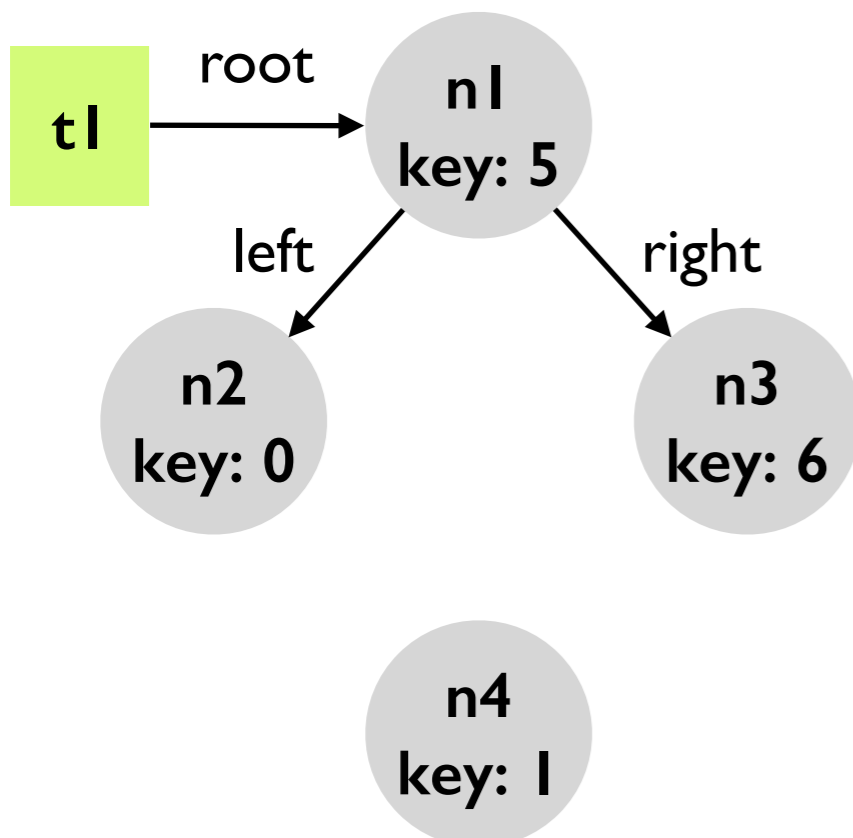
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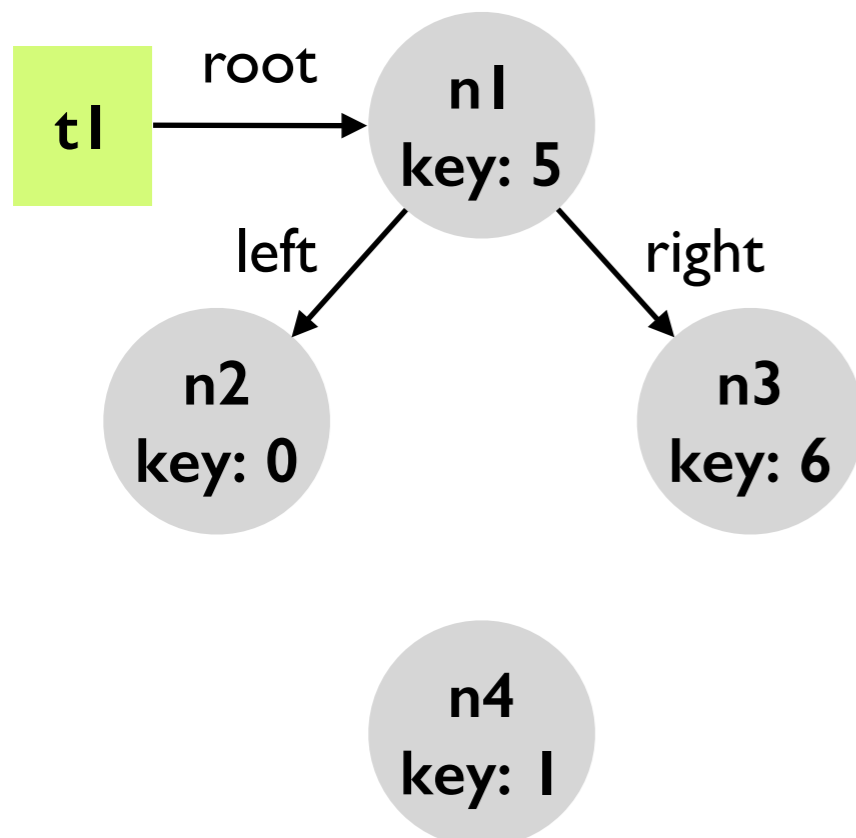
reachable objects

```
T = {⟨t1⟩}
N = {⟨n1⟩, ..., ⟨n4⟩}
null = {⟨null⟩}
this = {⟨t1⟩}
z = {⟨n4⟩}
ints = {⟨0⟩, ⟨1⟩, ⟨5⟩, ⟨6⟩ }
```

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```
public void insert(Node z) {
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```



pre-state

```
keyold = {⟨n1, 5⟩, ..., ⟨n4, 1⟩}
rootold = {⟨t1, n1⟩}
leftold = {⟨n1, n2⟩, ..., ⟨n4, null⟩}
rightold = {⟨n1, n3⟩, ..., ⟨n4, null⟩}
```

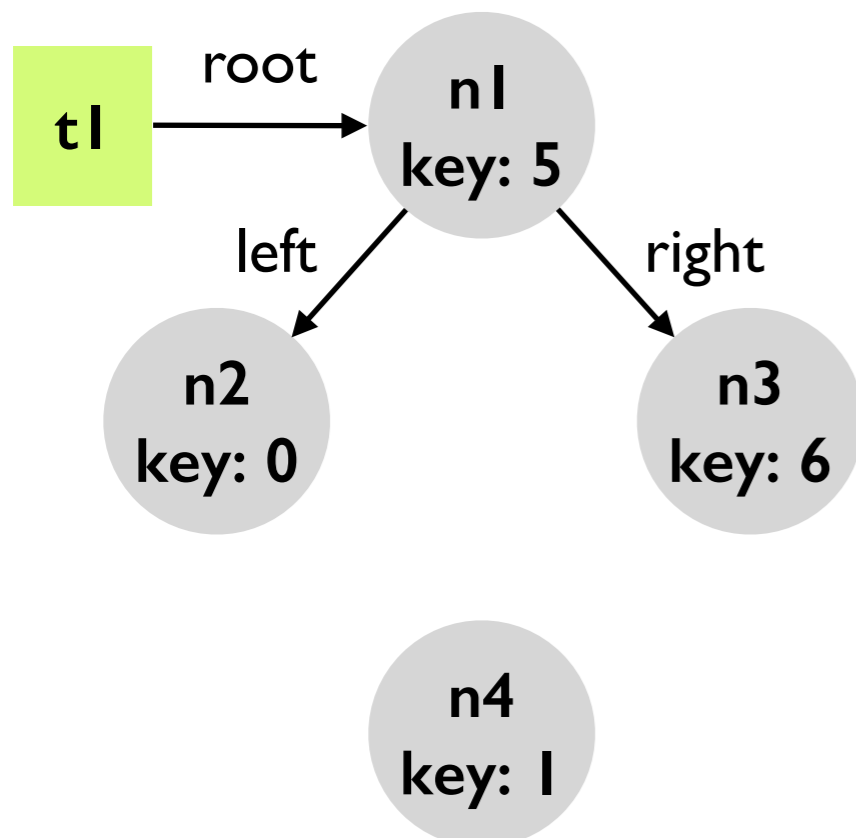
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public void insert(Node z) {
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reachable objects

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```

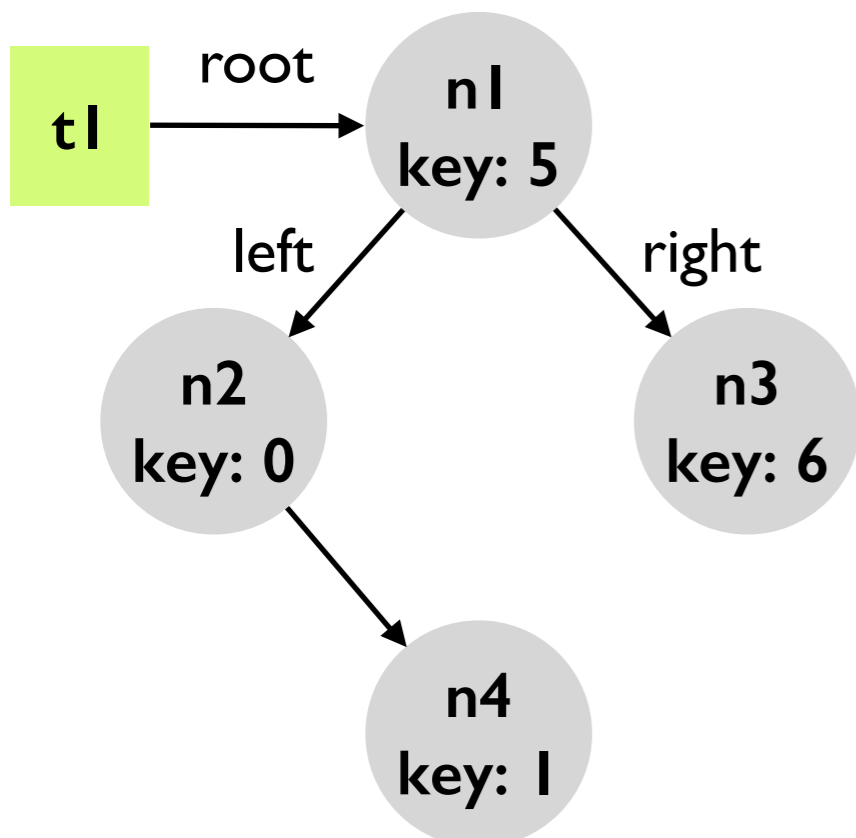
post-state

```
{ } ⊆ root ⊆
{t1} × {n1, ..., n4, null}
{⟨n1, n2⟩} ⊆ left ⊆
{n2, n3, n4} × {n1, ..., n4, null}
{⟨n1, n3⟩} ⊆ right ⊆
{n2, n3, n4} × {n1, ..., n4, null}
```


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Mixed interpretation with a model finder (4/4)

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@Requires("z.key !in this.nodes.key")
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public void insert(Node z) {
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```

Many more features (e.g., support for obtaining all solutions, support for data abstraction, etc.).

See [Unifying Execution of Declarative and Imperative Code](#) for details.

Mixed interpretation with a model finder (4/4)

```
@Requires("z.key !in this.nodes.key")
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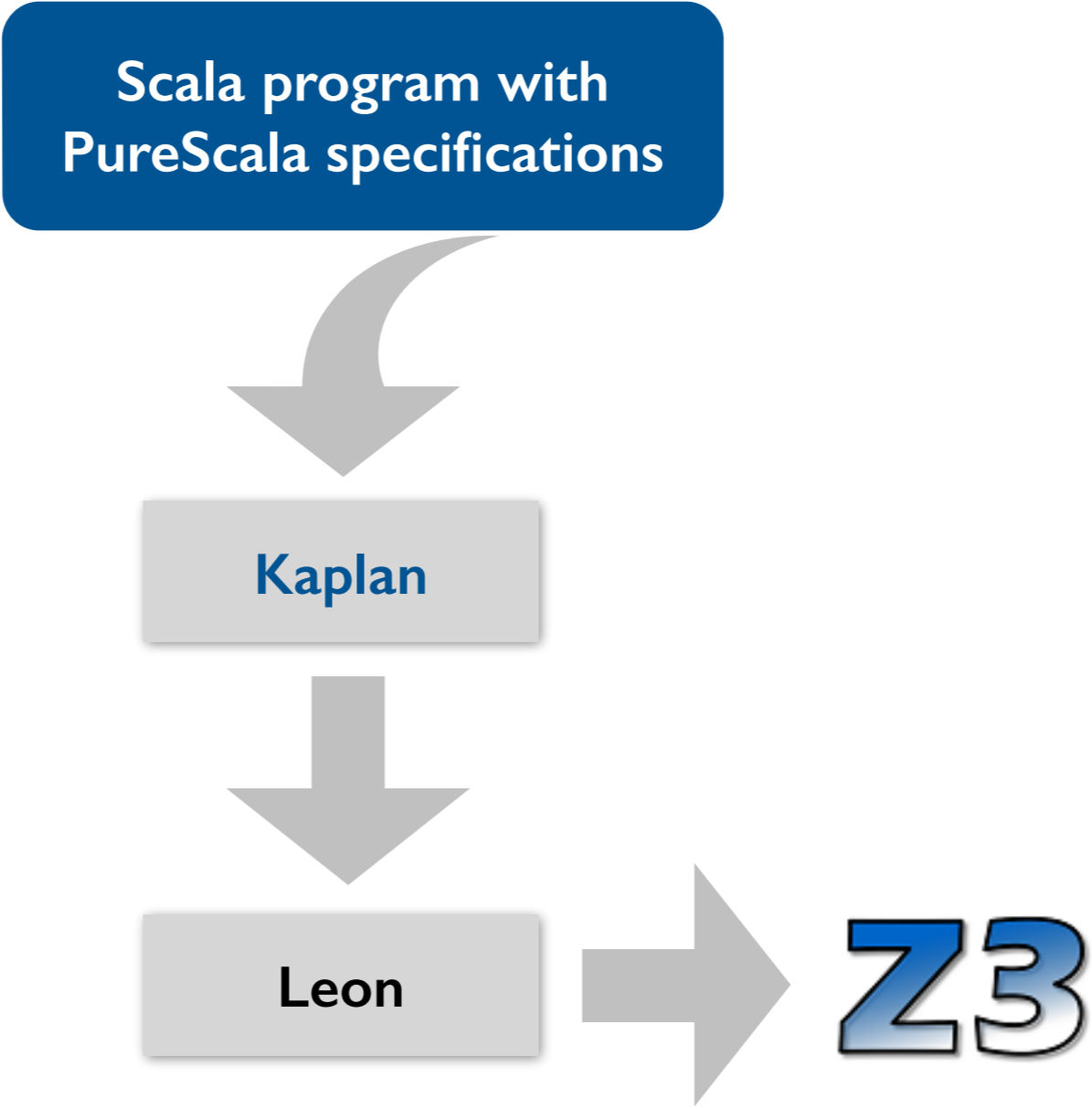
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Incompleteness due to finitization: Squander bounds the number of new instances of a given type that Kodkod can create to satisfy the specification.

Mixed interpretation with an SMT solver (1/3)



Mixed interpretation with an SMT solver (1/3)

Scala program with
PureScala specifications

PureScala is a pure, Turing complete subset of Scala that supports unbounded datatypes and arbitrary recursive functions.

Kaplan

Leon

Z3

Mixed interpretation with an SMT solver (2/3)

```
@spec def noneDivides(from: Int, j: Int) : Boolean {  
  from == j ||  
  (j % from != 0 && noneDivides(from+1, j))  
}
```

```
@spec def isPrime(i: Int) : Boolean {  
  i >= 2 && noneDivides(2, i)  
}
```

```
val primes =  
  ((isPrime(_Int)) minimizing  
   ((x:Int) => x)).findAll
```

```
> primes.take(10).toList  
List(2, 3, 4, 5, 11, 17, 19, 23, 29)
```

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Recursive specification functions. Mutual recursion also allowed.

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```

Call the Kaplan mixed interpreter to obtain the first 10 primes.

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Two execution modes:

- Eager: uses Leon to find a satisfying assignment for a given specification.
- Lazy: accumulates specifications, checking their feasibility, until the programmer asks for the *value* of a logical variable. The variable is then frozen (permanently bound) to the returned value.

Mixed interpretation with an SMT solver (3/3)

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Many more features (e.g., support for optimization).
See [Constraints as Control](#) for details.

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}
```

Incompleteness due to undecidability of PureScala.

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```

Execution steps:

- Translate the entire program to constraints using either BMC or SE.
- Query the solver for one or all solutions that satisfy the constraints.
- Convert each solution to a valid program trace (represented, e.g., as a sequence of choices made by the oracle in a given execution).

Applications of angelic execution

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Declarative mocking [Samimi et al., ISSTA'13]

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Angelic debugging [Chandra et al., ICSE'11]

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Dynamic program repair [Samimi et al., ECOOP'10]

Test case generation [Khurshid et al., ASE'01]

...

Summary

Today

- Angelic nondeterminism with specifications statements and angelic choice
- Angelic execution with model finders and SMT solvers
- Applications of angelic execution

Next lecture

- Program synthesis