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<pre> Require Import List. Require Import String. Require Import ZArith. Open Scope list_scope. Open Scope string_scope. Open Scope Z_scope. Require Import ImpSyntax. Require Import ImpCommon. Inductive eval_unop : op1 -> val -> val -> Prop := eval_neg : forall i, eval_unop Oneg (Vint i) (Vint (Z.opp i)) eval_not : forall b, eval_unop Onot (Vbool b) (Vbool (negb b)). Inductive eval_binop : op2 -> val -> val -> val -> Prop := eval_add_i : forall i1 i2, eval_binop Oadd (Vint i1) (Vint i2) (Vint (Z.add i1 i2)) eval_add_s : forall s1 s2, eval_binop Oadd (Vstr s1) (Vstr s2) (Vstr (String.append s1 s2)) eval_sub : forall i1 i2, eval_binop Osub (Vint i1) (Vint i2) (Vint (Z.sub i1 i2)) eval_mul : forall i1 i2, eval_binop Omul (Vint i1) (Vint i2) (Vint (Z.mul i1 i2)) eval_div : forall i1 i2, i2 <> 0 -> eval_binop Odiv (Vint i1) (Vint i2) (Vint (Z.div i1 i2)) eval_mod : forall i1 i2, i2 <> 0 -> eval_binop Omod (Vint i1) (Vint i2) (Vint (Z.modulo i1 i2)) eval_eq : forall v1 v2, eval_binop Oeq v1 v2 (Vbool (imp_eq v1 v2)) eval_lt : forall i1 i2, eval_binop Olt (Vint i1) (Vint i2) (Vbool (imp_lt i1 i2)) eval_le : forall i1 i2, eval_binop Ole (Vint i1) (Vint i2) (Vbool (imp_le i1 i2)) eval_conj : forall b1 b2, eval_binop Oconj (Vbool b1) (Vbool b2) (Vbool (andb b1 b2)) eval_disj : forall b1 b2, eval_binop Odisj (Vbool b1) (Vbool b2) (Vbool (orb b1 b2)). </pre>		

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<pre> Inductive eval_e (s : store) (h : heap) : expr -> val -> Prop := eval_val : forall v, eval_e s h (Eval v) v eval_var : forall x v, lkup s x = Some v -> eval_e s h (Evar x) v eval_op1 : forall op e v v', eval_e s h e v -> eval_unop op v v' -> eval_e s h (Eop1 op e) v' eval_op2 : forall op e1 e2 v1 v2 v', eval_e s h e1 v1 -> eval_e s h e2 v2 -> eval_binop op v1 v2 v' -> eval_e s h (Eop2 op e1 e2) v' eval_len_a : forall e a l, eval_e s h e (Vaddr a) -> read h a = Some (Vint l) -> eval_e s h (Elen e) (Vint l) eval_len_s : forall e cs l, eval_e s h e (Vstr cs) -> Z.of_nat (String.length cs) = l -> eval_e s h (Elen e) (Vint l) eval_idx_a : forall e1 e2 a l i v, eval_e s h e1 (Vaddr a) -> eval_e s h e2 (Vint i) -> read h a = Some (Vint l) -> 0 <= i < l -> read h (Zsucc (a + i)) = Some v -> eval_e s h (Eidx e1 e2) v eval_idx_s : forall e1 e2 cs i c, eval_e s h e1 (Vstr cs) -> eval_e s h e2 (Vint i) -> 0 <= i -> String.get (Z.to_nat i) cs = Some c -> eval_e s h (Eidx e1 e2) (Vstr (String c EmptyString)). Inductive evals_e (s : store) (h : heap) : list expr -> list val -> Prop := evals_nil : evals_e s h nil nil evals_cons : forall e es v vs, eval_e s h e v -> evals_e s h es vs -> evals_e s h (e :: es) (v :: vs). Inductive eval_s (env : env) : store -> heap -> stmt -> store -> heap -> Prop := eval_nop : forall s h, eval_s env s h Snop s h eval_set : forall s h x e v, eval_e s h e v -> eval_s env s h (Sset x e) (update s x v) h </pre>		

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| eval_alloc :
  forall s h x e1 e2 i v,
    eval_e s h e1 (Vint i) ->
    eval_e s h e2 v ->
    0 <= i ->
    eval_s env
      s h (Salloc x e1 e2)
      (update s x (Vaddr (zlen h))) (alloc h i v)
| eval_write :
  forall s h x e1 e2 a l i v h',
    lkup s x = Some (Vaddr a) ->
    read h a = Some (Vint l) ->
    eval_e s h e1 (Vint i) ->
    eval_e s h e2 v ->
    0 <= i < l ->
    write h (Zsucc (a + i)) v = Some h' ->
    eval_s env
      s h (Swrite x e1 e2)
      s h'
| eval_call_internal :
  forall s h f params body ret vs sf sf' h' x es v,
    locate env f = Some (Func f params body ret) ->
    evals_e s h es vs ->
    updates store_0 params vs = Some sf ->
    eval_s env
      sf h body
      sf' h' ->
    eval_e sf' h' ret v ->
    eval_s env
      s h (Scall x f es)
      (update s x v) h'
| eval_call_external :
  forall x f es s h vs v' h',
    locate env f = None ->
    evals_e s h es vs ->
    extcall_spec f vs h v' h' ->
    eval_s env
      s h (Scall x f es)
      (update s x v') h'
| eval_ifelse_t :
  forall s h e p1 p2 s' h',
    eval_e s h e (Vbool true) ->
    eval_s env
      s h p1
      s' h' ->
    eval_s env
      s h (Sifelse e p1 p2)
      s' h'
| eval_ifelse_f :
  forall s h e p1 p2 s' h',
    eval_e s h e (Vbool false) ->
    eval_s env
      s h p2
      s' h' ->
    eval_s env
      s h (Sifelse e p1 p2)
      s' h'
| eval_while_t :
  forall s1 h1 e p s2 h2 s3 h3,
    eval_e s1 h1 e (Vbool true) ->
    eval_s env
      s1 h1 p
      s2 h2 ->
    eval_s env
      s2 h2 (Swhile e p)
      s3 h3 ->
    eval_s env
      s1 h1 (Swhile e p)
      s3 h3

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| eval_while_f :
  forall s h e p,
    eval_e s h e (Vbool false) ->
    eval_s env
      s h (Swhile e p)
      s h
| eval_seq :
  forall s1 h1 p1 s2 h2 p2 s3 h3,
    eval_s env
      s1 h1 p1
      s2 h2 ->
    eval_s env
      s2 h2 p2
      s3 h3 ->
    eval_s env
      s1 h1 (Sseq p1 p2)
      s3 h3
| eval_incall :
  forall s1 h1 body s2 h2 v r1 ret rs,
    eval_s env
      s1 h1 body
      s2 h2 ->
    eval_e s2 h2 ret v ->
    eval_s env
      s1 h1 (Sincall body ret r1 rs)
      (update rs r1 v) h2.
Inductive eval_p : prog -> val -> Prop :=
| eval_prog :
  forall funcs main ret s' h' v,
    eval_s funcs
      store_0 heap_0 main
      s' h' ->
    eval_e s' h' ret v ->
    eval_p (Prog funcs main ret) v.

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