



CSE503:
SOFTWARE ENGINEERING
SYMBOLIC TESTING, AUTOMATED TEST
GENERATION ... AND MORE!

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Spring 2011

CFG for (edge) coverage

- Test inputs $\{[x=1;y=0],[x=0;y=1]\}$
- Cover 6/7 edges, 86%
- Which edge isn't covered?
- Can it be covered?
- With what test input?

```

    graph TD
      A["x >? y"] --> B["x = x + y"]
      A --> C["end"]
      B --> D["y = x - y"]
      D --> E["x = x - y"]
      E --> F["x >? y"]
      F --> G["assert(false)"]
      F --> C
    
```

Symbolic execution $[x=\alpha; y=\beta]$

```

    graph TD
      A["x >? y"] --> B["x = x + y"]
      A --> C["end"]
      B --> D["y = x - y"]
      D --> E["x = x - y"]
      E --> F["x >? y"]
      F --> G["assert(false)"]
      F --> C
    
```

Annotations:

- Before B: $[\alpha > \beta]$
- Before D: $[x = \alpha + \beta \wedge y = \beta]$
- Before E: $[x = \alpha + \beta \wedge y = \alpha]$
- Before F: $[x = \beta \wedge y = \alpha]$
- Before G: $[\beta > \alpha] \wedge [x = \beta \wedge y = \alpha]$
- Before C: $[\alpha \leq \beta]$

Callout: $Is \beta > \alpha$ ever here?

What's really going on?

```

    if (x > y) {
      x = x + y;
      y = x - y;
      x = x - y;
      if (x > y)
        assert(false);
    }
    
```

- Create a symbolic execution tree
- Explicitly track path conditions
- Solve path conditions – “how do you get to this point in the execution tree?” – to defines test inputs
- Goal: define test inputs that reach all reachable statements

```

    graph TD
      Root["[true] x=α∧y=β"] --> B["[α>β] x=α+β"]
      Root --> C["[α≤β] end"]
      B --> D["[α>β] x=β∧y=α"]
      D --> E["[α>β] β>α"]
      E --> F["[α>β∧β>α] 'false'"]
      E --> G["[α>β∧β≤α] end"]
    
```

Callout: $\alpha > \beta \wedge \beta > \alpha$ has no solution, so the assert statement can never be executed

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Another example (Sen and Agha)

```

int double (int v){
    return 2*v;
}
void testme (int x, int y){
    z = double (y);
    if (z == x) {
        if (x > y+10) {
            ERROR;
        }
    }
}
    
```

Error: possible by solving equations

$$2*\beta = \alpha \wedge \alpha > \beta + 10$$

$$\equiv 2*\beta = \alpha \wedge 2*\beta > \beta + 10$$

$$\equiv 2*\beta = \alpha \wedge \beta > 10$$

$$\equiv 2*\beta = \alpha \wedge \beta > 10$$

- Any solution to this will cause the error state to be reached
 - $\{x=22, y=11\}, \{x=200, y=100\}, \dots$

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OK, do this in small groups for...

```

if x ≠ 0 then
    y := 5;
else
    z := z - x;
endif;
if z > 1 then
    z := z / x;
else
    z := 0;
end
    
```

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```

if x ≠ 0 then
    y := 5;
else
    z := z - x;
endif;
if z > 1 then
    z := z / x;
else
    z := 0;
end
    
```

8

Way cool – we're done!

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- First example can't reach `assert(false)`, and it's easy to reach `end` via both possible paths
- Second example: can reach `error` and `end` via both possible paths
- Third example: can avoid edge coverage weakness
- Well, what if we can't solve the path conditions?
 - Some arithmetic, some recursion, some loops, some pointer expressions, etc.
 - We'll see an example
- What if we want specific test cases?

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Concolic testing: Sen et al.

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- Basically, combine concrete and symbolic execution
- More precisely...
 - Generate a random concrete input
 - Execute the program on that input both concretely and symbolically simultaneously
 - Follow the concrete execution and maintain the path conditions along with the corresponding symbolic execution
 - If and when the symbolic constraints cannot be solved by a solver, use the path conditions collected by this guided process to constrain the generation of inputs for the next iteration
 - Repeat until test inputs are produced to exercise all feasible paths

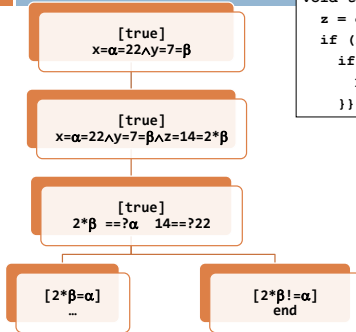
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2nd example redux
1st iteration x=22, y=7

11

```
int double (int v){
    return 2*v;
}

void testme (int x, int y){
    z = double (y);
    if (z == x) {
        if (x > y+10) {
            ERROR;
        }}
}
```



- Now solve $2*\beta = \alpha$ to force the other branch
- $x=1; y=2$ is one solution

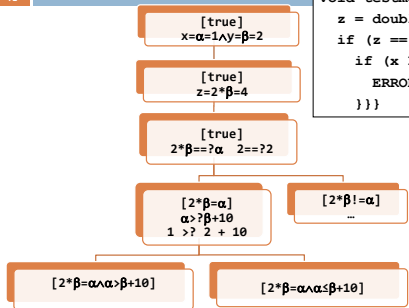
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2nd example
2nd iteration x=1, y=2

12

```
int double (int v){
    return 2*v;
}

void testme (int x, int y){
    z = double (y);
    if (z == x) {
        if (x > y+10) {
            ERROR;
        }}
}
```



- Now solve $2*\beta = \alpha \wedge \alpha \leq \beta + 10$ to force the other branch
- $x=30; y=15$ is one solution

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2nd example
3rd iteration x=30, y=15

```

int double (int v){
    return 2*v;
}

void testme (int x, int y){
    z = double (y);
    if (z == x) {
        if (x > y+10) {
            ERROR;
        }}
    }
    
```

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Three concrete test cases

```

int double (int v){ return 2*v;}
void testme (int x, int y){
    z = double (y);
    if (z == x) {
        if (x > y+10) {
            ERROR;
        }
    }
}
    
```

x	y	
22	7	Takes first else
2	1	Takes first then and second else
30	15	Takes first and second then

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Concolic testing example: P. Sağlam

- Random seed
 - x=-3; y=7
- Concrete
 - z=9
- Symbolic
 - z=x³+3x²+9
 - Take then branch with constraint x³+3x²+9≠y
 - Take else branch with constraint x³+3x²+9=y

```

void test_me(int x,int y){
    z = x*x*x + 3*x*x + 9;
    if(z != y){
        printf("Good branch");
    } else {
        printf("Bad branch");
        abort();
    }
}
    
```

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Concolic testing example: P. Sağlam

- Solving is hard for x³+3x²+9=y
- So use z's concrete value, which is currently 9, and continue concretely
- 9!=7 so then is good
- Symbolically solve 9=y for else clause
 - Execute next run with x=-3; y=9 so else is bad
 - When symbolic expression becomes unmanageable (e.g., non-linear) replace it by concrete value

```

void test_me(int x,int y){
    z = x*x*x + 3*x*x + 9;
    if(z != y){
        printf("Good branch");
    } else {
        printf("Bad branch");
        abort();
    }
}
    
```

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Example

Following N slides from Saglam

```

typedef struct cell {
  int v;
  struct cell *next;
} cell;
int f(int v) {
  return 2*v + 1;
}
int testme(cell *p, int x) {
  if (x > 0)
    if (p != NULL)
      if (f(x) == p->v)
        if (p->next == p)
          abort();
  return 0;
}
    
```

- Random Test Driver:
 - random memory graph reachable from p
 - random value for x
- Probability of reaching **abort()** is extremely low

CUTE Approach

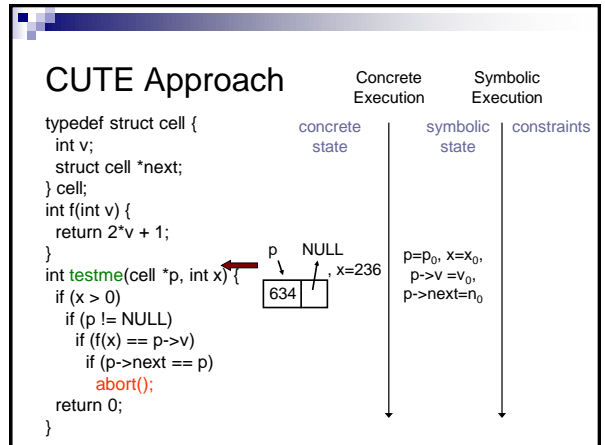
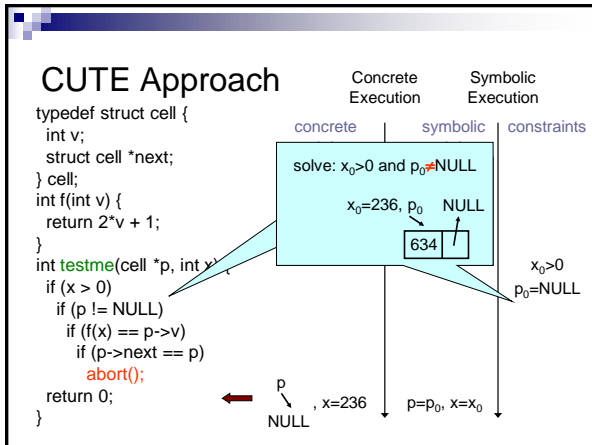
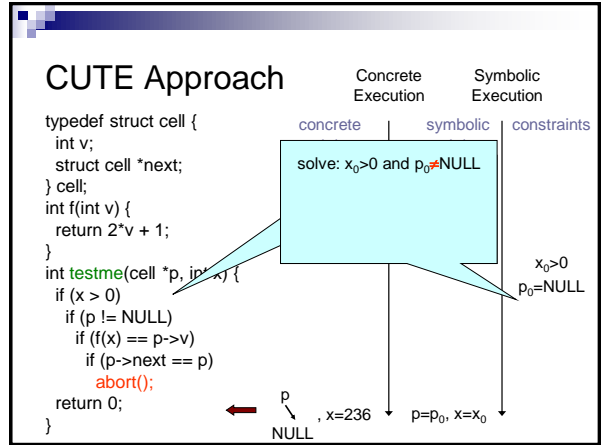
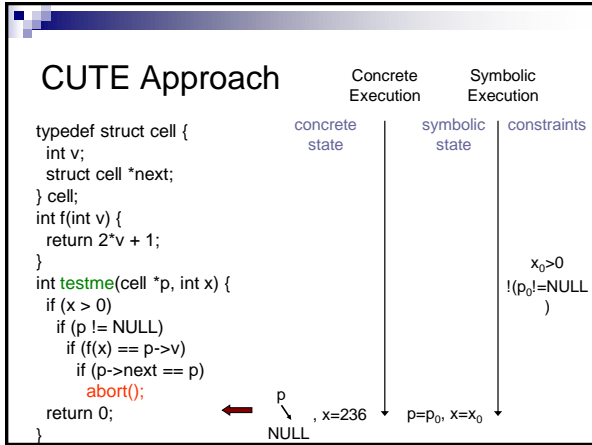
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CUTE Approach

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CUTE Approach

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CUTE Approach

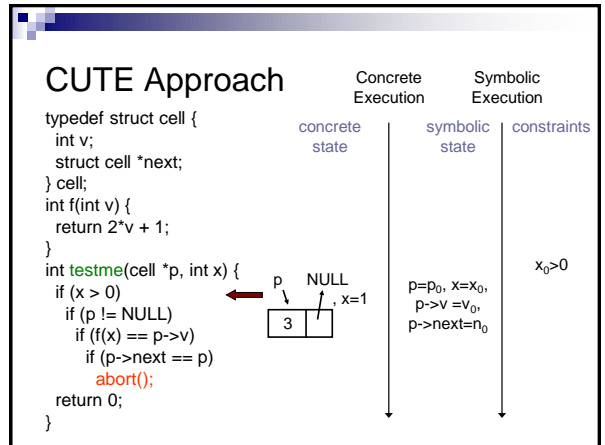
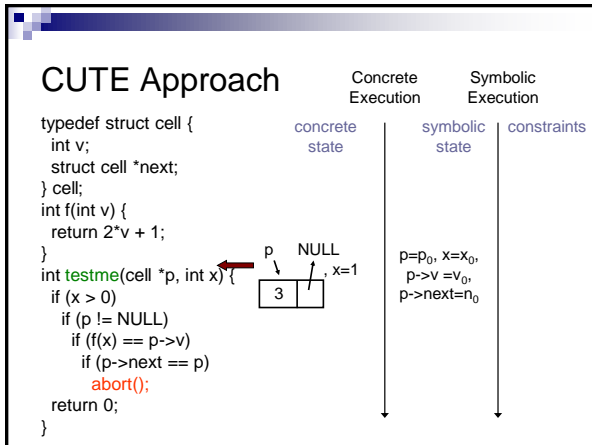
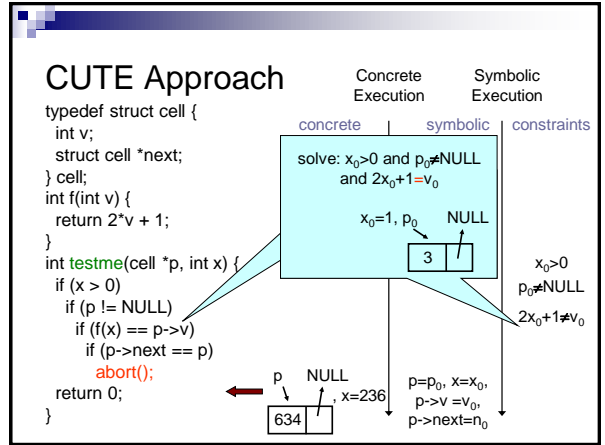
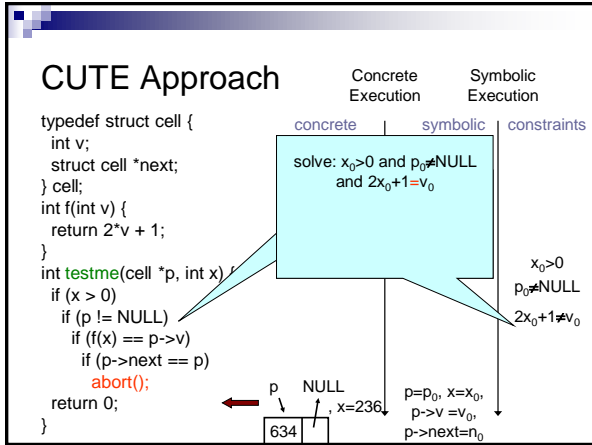
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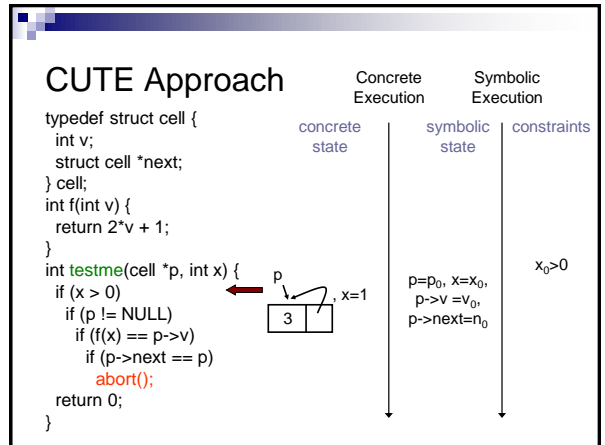
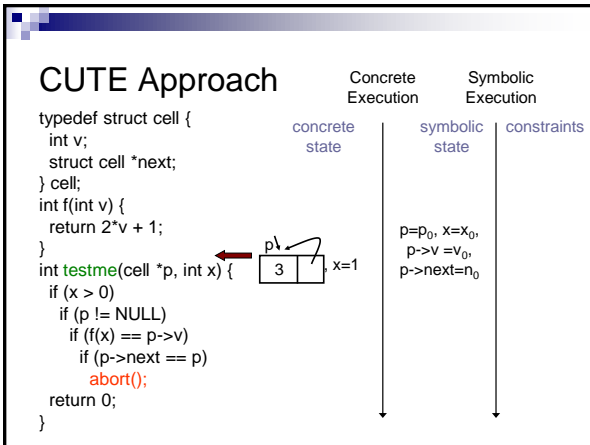
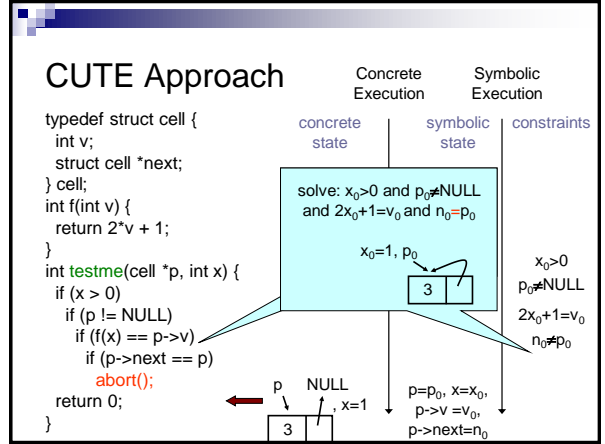
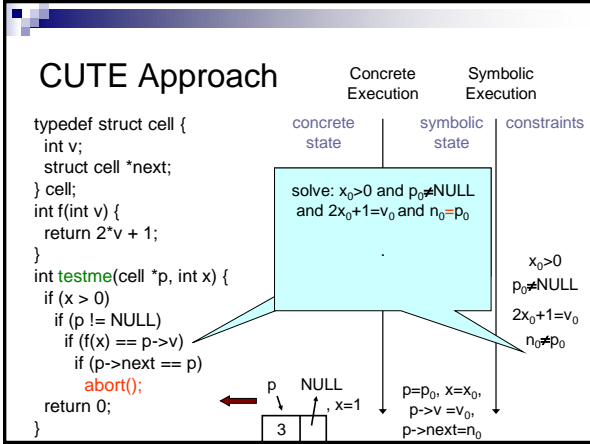
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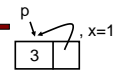
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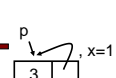
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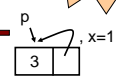
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Program Error



Concolic testing example: P. Sağlam

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- Random
 - Random memory graph reachable from **p**
 - Random value for **x**
 - Probability of reaching **abort()** is extremely low
- (Why is this a somewhat misleading motivation?)

```

typedef struct cell {
  int v;
  struct cell *next;
} cell;
int f(int v) {
  return 2*v + 1;
}
int testme(cell *p, int x) {
  if (x > 0)
    if (p != NULL)
      if (f(x) == p->v)
        if (p->next == p)
          abort();
  return 0;
}

```

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Concolic: status

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- The jury is still out on concolic testing – but it surely has potential
- There are many papers on the general topic
- Here's one that is somewhat high-level Microsoft-oriented
 - Godefroid et al. [Automating Software Testing Using Program Analysis](#) *IEEE Software* (Sep/Oct 2008)
 - They tend to call the approach DART – Dynamic Automated Random Testing

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