

CSE 493s/599s

Lecture 10.

Tokenization for LLMs

Sewoong Oh



- First 1/2 of CSE492S/599S Advanced ML

Part I: Foundations

- A gentle start
- A formal learning model
- Learning via uniform convergence
- The bias-complexity trade-off
- The VC-dimension
- Non-uniform learnability
- The runtime of learning

Part II: From Theory to Algorithms

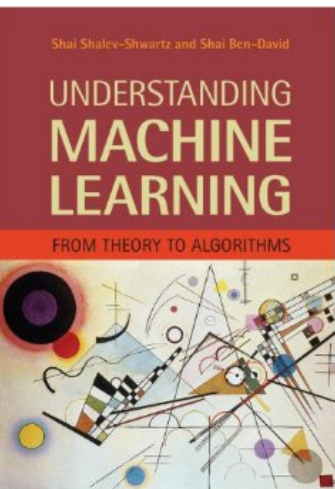
- Linear predictors
- Boosting
- Model selection and validation
- Convex learning problems
- Regularization and stability
- Stochastic gradient descent
- Support vector machines
- Kernel methods
- Multiclass, ranking, and complex prediction problems
- Decision trees
- Nearest neighbor
- Neural networks

Part III: Additional Learning Models

- Online learning
- Clustering
- Dimensionality reduction
- Generative models
- Feature selection and generation

Part IV: Advanced Theory

- Rademacher complexities
- Covering numbers
- Proof of the fundamental theorem of learning theory
- Multiclass learnability
- Compression bounds
- PAC-Bayes



My goal in designing this course was to have as little overlap as possible with other amazing courses at UW.

- First 1/2 of CSE492S/599S Advanced ML

Part I: Foundations

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- The runtime of learning

Part II: From Theory to Algorithms

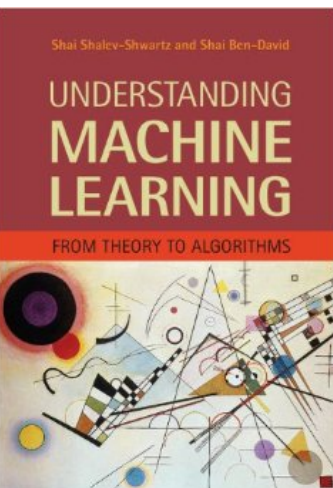
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CSE446/546

CSE541 —> CSE542

EE578

CSE 543

Theory



CSE515 Statistical
Methods

CSE541 Interactive
Learning (Kevin J)

CSE542 RL
(Kevin J)

CSE446/546
Machine Learning

CSE493S/599S
Advanced ML

CSE543 Deep
Learning
(Simon D)

CSE599J
Data-centric ML
(Pang Wei K)

CSE547 ML for
Big Data

CSE455 CV

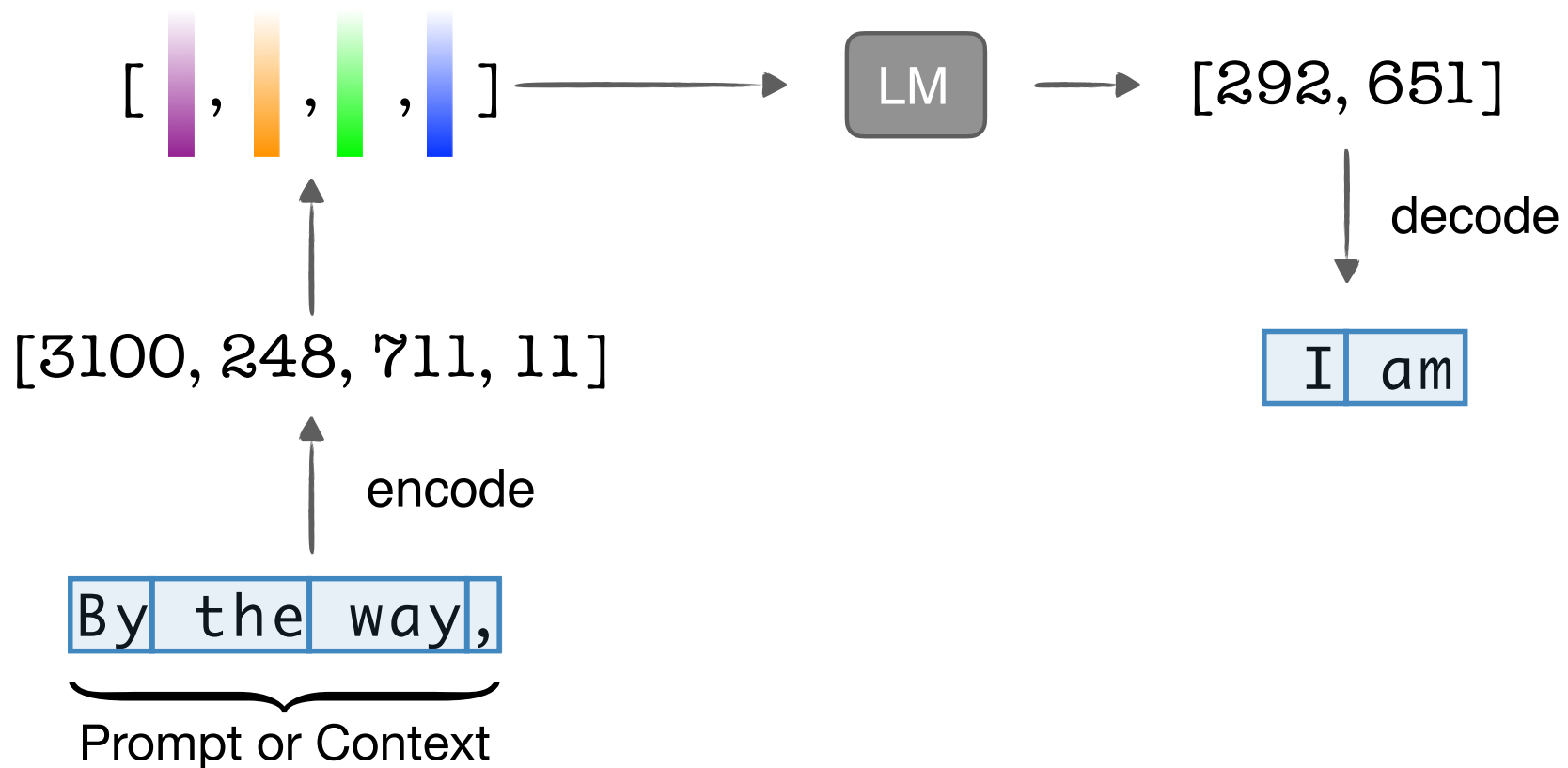
CSE576 CV

CSE447/517
NLP

Empirical/Applied

Tokenizer for LLMs

Tokens are sequences of characters used by LMs to understand text



Modern transformer-based LMs use **subword** tokenization

- Character-level:

By the way, I am a fan of the Milky way.

Character-level tokenization

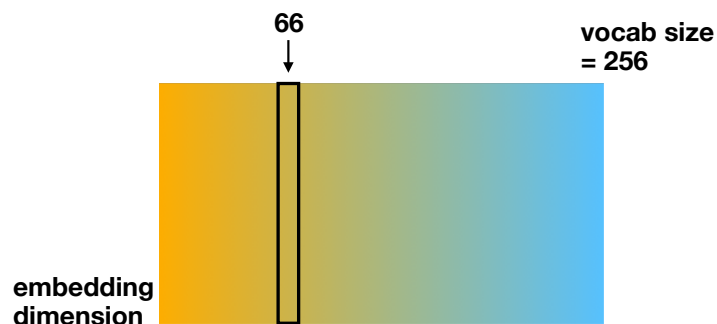
- Step 1: the text is broken into a sequence of characters

By the way, I am a fan of the Milky way.

- Step 2: Look-up table converts characters into unique integer IDs
(in this case Bytes)

[66, 121, 32, 116, 104, 101, 32, 119, 97, 121, 44, 32, 73, 32, 97, 109, 32, 97, 32, 102, 97, 110, 32, 111, 102, 32, 116, 104, 101, 32, 77, 105, 108, 107, 121, 32, 119, 97, 121, 46]

- Step 3: Learned embedding table converts IDs into embedding representations



Character-level tokenization

- Step 1: the text is broken into a sequence of characters

By the way, I am a fan of the Milky way.

- What is wrong with **character-level tokenization**?

Character-level tokenization

- Step 1: the text is broken into a sequence of characters

By the way, I am a fan of the Milky way.

- What is wrong with **character-level tokenization**?
 - **Efficiency**: the number of tokens needed to represent text is quite large, which increases the input dimension of the model (run-time is quadratic in the context length)
 - **Language diversity**: only handles English
 - A variable length code of UTF-8 is used to handle world language (together with BPE to be explained later)

Modern transformer-based LMs use **subword** tokenization

- Character-level:

By the way, I am a fan of the Milky way.

- Word-level:

By the way, I am a fan of the <UNK> Way.

- Much more efficient:
 - about 5 characters per English word on average $\implies$ 20% compression rate for context
- Typical vocabulary size $\sim$ 170,000 words (e.g., Oxford English Dictionary)
 - but can encounter new words that is not in the vocab, which is represented by a special token **<UNK>**, since there are many more uncommon words

Modern transformer-based LMs use **subword** tokenization

- Character-level:

By the way, I am a fan of the Milky way.

- Word-level:

By the way, I am a fan of the <UNK> Way.

- **Subword-level:**

By the way, I am a fan of the Milky Way.

Byte Pair Encoding (BPE)

- Universal method for learning subword tokenizers today
- Introduced by Sennrich et al. 2016 and popularized by GPT-2 (2019)
- Main idea: build vocabulary of tokens bottom-up by repeatedly merging frequent pair of tokens
- **Colab** for playing with BPE courtesy of Tayyib UI Hassan Gondal

Sennrich, Haddow, Birch, “Neural Machine Translation of Rare Words with Subword Units”, ACL 2016
Radford et al., “Language Models are Unsupervised Multitask Learners”, 2019

Byte Pair Encoding (BPE)

Training Data

Proof of the Milky Way
consisting of many stars
came in 1610 when Galileo
Galilei used a telescope to
study the Milky Way and
discovered that it is
composed of a huge number
of faint stars.

Given **training data** D

Training Data

```
{Proof, _of, _the, _Milky,  
_Way, _consisting, _of,  
_many, _stars, _came, _in,  
_1610, _when, _Galileo,  
_Galilei, _used, _a,  
_telescope, _to, _study,  
_the, _Milky, _Way, _and,  
_discovered, _that, _it,  
_is, _composed, _of, _a,  
_huge, _number, _of,  
_faint, _stars.}
```

Pretokenize D by splitting on whitespace

Training Data

_ P r o o f, _ o f, _ t h
e, _ M i l k y, _ W a y, _
c o n s i s t i n g, _ o f,
_ m a n y, _ s t a r s, _ c
a m e, _ i n, _ 1 6 1 0, _
w h e n, _ G a l i l e o, _
G a l i l e i, _ u s e d, _
a, _ t e l e s c o p e, _ t
o, _ s t u d y, _ t h e, _
M i l k y, _ W a y, _ a n
d, _ d i s c o v e r e d, _
t h a t, _ i t, _ i s, _ c
o m p o s e d, _ o f, _ a,
_ h u g e, _ n u m b e r, _
o f, _ f a i n t, _ s t a r
s .

Split D into sequence of **bytes**

Training Data

_ P r o o f, _ o f, _ t h
e, _ M i l k y, _ W a y, _
c o n s i s t i n g, _ o f,
_ m a n y, _ s t a r s, _ c
a m e, _ i n, _ 1 6 1 0, _
w h e n, _ G a l i l e o, _
G a l i l e i, _ u s e d, _
a, _ t e l e s c o p e, _ t
o, _ s t u d y, _ t h e, _
M i l k y, _ W a y, _ a n
d, _ d i s c o v e r e d, _
t h a t, _ i t, _ i s, _ c
o m p o s e d, _ o f, _ a,
_ h u g e, _ n u m b e r, _
o f, _ f a i n t, _ s t a r
s .

Pair counts

_ t	12335282
t h	10067390
_ a	9319062
h e	8771183
i n	8024060
e r	6517430
a n	6315205
r e	6031043
o n	5261131
_ i	5209828

Vocabulary

Training Data

_ P r o o f, _ o f, _ t h
e, _ M i l k y, _ W a y, _
c o n s i s t i n g, _ o f,
_ m a n y, _ s t a r s, _ c
a m e, _ i n, _ 1 6 1 0, _
w h e n, _ G a l i l e o, _
G a l i l e i, _ u s e d, _
a, _ t e l e s c o p e, _ t
o, _ s t u d y, _ t h e, _
M i l k y, _ W a y, _ a n
d, _ d i s c o v e r e d, _
t h a t, _ i t, _ i s, _ c
o m p o s e d, _ o f, _ a,
_ h u g e, _ n u m b e r, _
o f, _ f a i n t, _ s t a r
s .

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Vocabulary

_t

Training Data

_ P r o o f, _ o f, _t h e,
_ M i l k y, _ W a y, _ c o
n s i s t i n g, _ o f, _ m
a n y, _ s t a r s, _ c a m
e, _ i n, _ 1 6 1 0, _ w h
e n, _ G a l i l e o, _ G a
l i l e i, _ u s e d, _ a,
_t e l e s c o p e, _t o, _
s t u d y, _t h e, _ M i l
k y, _ W a y, _ a n d, _ d
i s c o v e r e d, _t h a
t, _ i t, _ i s, _ c o m p
o s e d, _ o f, _ a, _ h u
g e, _ n u m b e r, _ o f,
_ f a i n t, _ s t a r s .

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Vocabulary

_t

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_ M i l k y, _ W a y, _ c o
n s i s t i n g, _ o f, _ m
a n y, _ s t a r s, _ c a m
e, _ i n, _ 1 6 1 0, _ w h
e n, _ G a l i l e o, _ G a
l i l e i, _ u s e d, _ a,
_t e l e s c o p e, _t o, _
s t u d y, _t h e, _ M i l
k y, _ W a y, _ a n d, _ d
i s c o v e r e d, _t h a
t, _ i t, _ i s, _ c o m p
o s e d, _ o f, _ a, _ h u
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Vocabulary

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_ M i l k y, _ W a y, _ c o
n s i s t i n g, _ o f, _ m
a n y, _ s t a r s, _ c a m
e, _ i n, _ 1 6 1 0, _ w h
e n, _ G a l i l e o, _ G a
l i l e i, _ u s e d, _ a,
_t e l e s c o p e, _t o, _
s t u d y, _t h e, _ M i l
k y, _ W a y, _ a n d, _ d
i s c o v e r e d, _t h a
t, _ i t, _ i s, _ c o m p
o s e d, _ o f, _ a, _ h u
g e, _ n u m b e r, _ o f,
_ f a i n t, _ s t a r s .

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Vocabulary

_t

Training Data

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_ M i l k y, _ W a y, _ c o
n s i s t i n g, _ o f, _ m
a n y, _ s t a r s, _ c a m
e, _ i n, _ 1 6 1 0, _ w h
e n, _ G a l i l e o, _ G a
l i l e i, _ u s e d, _ a,
_t e l e s c o p e, _t o, _
s t u d y, _t h e, _ M i l
k y, _ W a y, _ a n d, _ d
i s c o v e r e d, _t h a
t, _ i t, _ i s, _ c o m p
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_ M i l k y, _ W a y, _ c o
n s i s t i n g, _ o f, _ m
a n y, _ s t a r s, _ c a m
e, _ i n, _ 1 6 1 0, _ w h
e n, _ G a l i l e o, _ G a
l i l e i, _ u s e d, _ a,
_t e l e s c o p e, _t o, _
s t u d y, _t h e, _ M i l
k y, _ W a y, _ a n d, _ d
i s c o v e r e d, _t h a
t, _ i t, _ i s, _ c o m p
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a n y, _ s t a r s, _ c a m
e, _ i n, _ 1 6 1 0, _ w h
e n, _ G a l i l e o, _ G a
l i l e i, _ u s e d, _ a,
_t e l e s c o p e, _t o, _
s t u d y, _t h e, _ M i l
k y, _ W a y, _ a n d, _ d
i s c o v e r e d, _t h a
t, _ i t, _ i s, _ c o m p
o s e d, _ o f, _ a, _ h u
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Vocabulary

_t
_a

Training Data

_ P r o o f, _ o f, _t h e,
_ M i l k y, _ W a y, _ c o
n s i s t i n g, _ o f, _ m
a n y, _ s t a r s, _ c a m
e, _ i n, _ 1 6 1 0, _ w h
e n, _ G a l i l e o, _ G a
l i l e i, _ u s e d, _a,
_t e l e s c o p e, _t o, _
s t u d y, _t h e, _ M i l
k y, _ W a y, _a n d, _ d i
s c o v e r e d, _t h a t,
_ i t, _ i s, _ c o m p o s
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Vocabulary

_t
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n s i s t i n g, _ o f, _ m
a n y, _ s t a r s, _ c a m
e, _ i n, _ 1 6 1 0, _ w h
e n, _ G a l i l e o, _ G a
l i l e i, _ u s e d, _a,
_t e l e s c o p e, _t o, _
s t u d y, _t h e, _ M i l
k y, _ W a y, _a n d, _ d i
s c o v e r e d, _t h a t,
_ i t, _ i s, _ c o m p o s
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_ M i l k y, _ W a y, _ c o
n s i s t i n g, _ o f, _ m
a n y, _ s t a r s, _ c a m
e, _ i n, _ 1 6 1 0, _ w h
e n, _ G a l i l e o, _ G a
l i l e i, _ u s e d, _a,
_t e l e s c o p e, _t o, _
s t u d y, _t h e, _ M i l
k y, _ W a y, _a n d, _ d i
s c o v e r e d, _t h a t,
_ i t, _ i s, _ c o m p o s
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o n	5261131
_ i	5209828
_ o	5163783
_ s	5035505
_ w	4523998

Vocabulary

_t
_a

Training Data

_ P r o o f, _ o f, _t h e,
_ M i l k y, _ W a y, _ c o
n s i s t i n g, _ o f, _ m
a n y, _ s t a r s, _ c a m
e, _ i n, _ 1 6 1 0, _ w h
e n, _ G a l i l e o, _ G a
l i l e i, _ u s e d, _a,
_t e l e s c o p e, _t o, _
s t u d y, _t h e, _ M i l
k y, _ W a y, _a n d, _ d i
s c o v e r e d, _t h a t,
_ i t, _ i s, _ c o m p o s
e d, _ o f, _a, _ h u g e,
_ n u m b e r, _ o f, _ f a
i n t, _ s t a r s .

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_ s	5035505
_ w	4523998

Vocabulary

_t
_a

Training Data

_ P r o o f, _ o f, _t h e,
_ M i l k y, _ W a y, _ c o
n s i s t i n g, _ o f, _ m
a n y, _ s t a r s, _ c a m
e, _ i n, _ 1 6 1 0, _ w h
e n, _ G a l i l e o, _ G a
l i l e i, _ u s e d, _a,
_t e l e s c o p e, _t o, _
s t u d y, _t h e, _ M i l
k y, _ W a y, _a n d, _ d i
s c o v e r e d, _t h a t,
_ i t, _ i s, _ c o m p o s
e d, _ o f, _a, _ h u g e,
_ n u m b e r, _ o f, _ f a
i n t, _ s t a r s .

Pair counts

h e	8771183
i n	8024060
_t h	7897058
e r	6517430
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o n	5261131
_ i	5209828
_ o	5163783
_ s	5035505
_ w	4523998

Vocabulary

_t
_a
he

Training Data

_ P r o o f, _ o f, _t he,
_ M i l k y, _ W a y, _ c o
n s i s t i n g, _ o f, _ m
a n y, _ s t a r s, _ c a m
e, _ i n, _ 1 6 1 0, _ w he
n, _ G a l i l e o, _ G a l
i l e i, _ u s e d, _a, _t
e l e s c o p e, _t o, _ s
t u d y, _t he, _ M i l k
y, _ W a y, _a n d, _ d i s
c o v e r e d, _t h a t, _
i t, _ i s, _ c o m p o s e
d, _ o f, _a, _ h u g e, _
n u m b e r, _ o f, _ f a i
n t, _ s t a r s .

Pair counts

h e	8771183
i n	8024060
_t h	7897058
e r	6517430
r e	6031043
o n	5261131
_ i	5209828
_ o	5163783
_ s	5035505
_ w	4523998

Vocabulary

_t
_a
he

Training Data

_ P r o o f, _ o f, _t he,
_ M i l k y, _ W a y, _ c o
n s i s t i n g, _ o f, _ m
a n y, _ s t a r s, _ c a m
e, _ i n, _ 1 6 1 0, _ w he
n, _ G a l i l e o, _ G a l
i l e i, _ u s e d, _a, _t
e l e s c o p e, _t o, _ s
t u d y, _t he, _ M i l k
y, _ W a y, _a n d, _ d i s
c o v e r e d, _t h a t, _
i t, _ i s, _ c o m p o s e
d, _ o f, _a, _ h u g e, _
n u m b e r, _ o f, _ f a i
n t, _ s t a r s .

Pair counts

i n	8024060
e r	6517430
r e	6031043
o n	5261131
_ i	5209828
_ o	5163783
_ s	5035505
_ w	4523998

Vocabulary

_t
_a
he

Training Data

_ P r o o f, _ o f, _t he,
_ M i l k y, _ W a y, _ c o
n s i s t i n g, _ o f, _ m
a n y, _ s t a r s, _ c a m
e, _ i n, _ 1 6 1 0, _ w he
n, _ G a l i l e o, _ G a l
i l e i, _ u s e d, _a, _t
e l e s c o p e, _t o, _ s
t u d y, _t he, _ M i l k
y, _ W a y, _a n d, _ d i s
c o v e r e d, _t h a t, _
i t, _ i s, _ c o m p o s e
d, _ o f, _a, _ h u g e, _
n u m b e r, _ o f, _ f a i
n t, _ s t a r s .

Pair counts

i n	8024060
r e	6031043
_t he	5605612
e r	5279258
o n	5261131
_ i	5209828
_ o	5163783
_ s	5035505
_ w	4523998

Vocabulary

_t
_a
he

Training Data

_ P r o o f, _ o f, _t he,
_ M i l k y, _ W a y, _ c o
n s i s t i n g, _ o f, _ m
a n y, _ s t a r s, _ c a m
e, _ i n, _ 1 6 1 0, _ w he
n, _ G a l i l e o, _ G a l
i l e i, _ u s e d, _a, _t
e l e s c o p e, _t o, _ s
t u d y, _t he, _ M i l k
y, _ W a y, _a n d, _ d i s
c o v e r e d, _t h a t, _
i t, _ i s, _ c o m p o s e
d, _ o f, _a, _ h u g e, _
n u m b e r, _ o f, _ f a i
n t, _ s t a r s .

Pair counts

i n	8024060
r e	6031043
_t he	5605612
e r	5279258
o n	5261131
_ i	5209828
_ o	5163783
_ s	5035505
_ w	4523998
a t	4424733

Vocabulary

_t
_a
he

Training Data

_ P r o o f, _ o f, _t he,
_ M i l k y, _ W a y, _ c o
n s i s t i n g, _ o f, _ m
a n y, _ s t a r s, _ c a m
e, _ i n, _ 1 6 1 0, _ w he
n, _ G a l i l e o, _ G a l
i l e i, _ u s e d, _a, _t
e l e s c o p e, _t o, _ s
t u d y, _t he, _ M i l k
y, _ W a y, _a n d, _ d i s
c o v e r e d, _t h a t, _
i t, _ i s, _ c o m p o s e
d, _ o f, _a, _ h u g e, _
n u m b e r, _ o f, _ f a i
n t, _ s t a r s .

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_ M i l k y, _ W a y, _ c o
n s i s t i n g, _ o f, _ m
a n y, _ s t a r s, _ c a m
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n, _ G a l i l e o, _ G a l
i l e i, _ u s e d, _a, _t
e l e s c o p e, _t o, _ s
t u d y, _t he, _ M i l k
y, _ W a y, _a n d, _ d i s
c o v e r e d, _t h a t, _
i t, _ i s, _ c o m p o s e
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Vocabulary

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he
in

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_ M i l k y, _ W a y, _ c o
n s i s t i n g, _ o f, _ m
a n y, _ s t a r s, _ c a m
e, _ i n, _ 1 6 1 0, _ w he
n, _ G a l i l e o, _ G a l
i l e i, _ u s e d, _a, _t
e l e s c o p e, _t o, _ s
t u d y, _t he, _ M i l k
y, _ W a y, _a n d, _ d i s
c o v e r e d, _t h a t, _
i t, _ i s, _ c o m p o s e
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a n y, _ s t a r s, _ c a m
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n, _ G a l i l e o, _ G a l
i l e i, _ u s e d, _a, _t
e l e s c o p e, _t o, _ s
t u d y, _t he, _ M i l k
y, _ W a y, _a n d, _ d i s
c o v e r e d, _t h a t, _
i t, _ i s, _ c o m p o s e
d, _ o f, _a, _ h u g e, _
n u m b e r, _ o f, _ f a
i n t, _ s t a r s .

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o n	5261131
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_ s	5035505
_ w	4523998
a t	4424733
o r	4162447
e s	4010515

Vocabulary

_t
_a
he
in

Training Data

_ P r o o f, _ o f, _t he,
_ M i l k y, _ W a y, _ c o
n s i s t i n g, _ o f, _ m
a n y, _ s t a r s, _ c a m
e, _ i n, _ 1 6 1 0, _ w h e
n, _ G a l i l e o, _ G a l
i l e i, _ u s e d, _a, _t
e l e s c o p e, _t o, _ s
t u d y, _t he, _ M i l k
y, _ W a y, _a n d, _ d i s
c o v e r e d, _t h a t, _
i t, _ i s, _ c o m p o s e
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Vocabulary

_t
_a
he
in

Training Data

_ P r o o f, _ o f, _t he,
_ M i l k y, _ W a y, _ c o
n s i s t i n g, _ o f, _ m
a n y, _ s t a r s, _ c a m
e, _ i n, _ 1 6 1 0, _ w h e
n, _ G a l i l e o, _ G a l
i l e i, _ u s e d, _a, _t
e l e s c o p e, _t o, _ s
t u d y, _t he, _ M i l k
y, _ W a y, _a n d, _ d i s
c o v e r e d, _t h a t, _
i t, _ i s, _ c o m p o s e
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Vocabulary

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n s i s t i n g, _ o f, _ m
a n y, _ s t a r s, _ c a m
e, _ i n, _ 1 6 1 0, _ w he
n, _ G a l i l e o, _ G a l
i l e i, _ u s e d, _a, _t
e l e s c o p e, _t o, _ s
t u d y, _t he, _ M i l k
y, _ W a y, _a n d, _ d i s
c o v e r e d, _t h a t, _ i
t, _ i s, _ c o m p o s e
d, _ o f, _a, _ h u g e, _
n u m b e r, _ o f, _ f a
i n t, _ s t a r s .

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_ M i l k y, _ W a y, _ c o
n s i s t i n g, _ o f, _ m
a n y, _ s t a r s, _ c a m
e, _ i n, _ 1 6 1 0, _ w he
n, _ G a l i l e o, _ G a l
i l e i, _ u s e d, _a, _t
e l e s c o p e, _t o, _ s
t u d y, _t he, _ M i l k
y, _ W a y, _a n d, _ d i s
c o v e r e d, _t h a t, _ i
t, _ i s, _ c o m p o s e
d, _ o f, _a, _ h u g e, _
n u m b e r, _ o f, _ f a
i n t, _ s t a r s .

Pair counts

_t he	5605612
o n	5261131
_ o	5163783
_ s	5035505
e r	4754849
_ w	4523998
a t	4424733
o u	3838417
_ c	3831635
n d	3811435

Vocabulary

_t
_a
he
in
re

Training Data

_ P r o o f, _ o f, _t he,
_ M i l k y, _ W a y, _ c o
n s i s t i n g, _ o f, _ m
a n y, _ s t a r s, _ c a m
e, _ i n, _ 1 6 1 0, _ w he
n, _ G a l i l e o, _ G a l
i l e i, _ u s e d, _a, _t
e l e s c o p e, _t o, _ s
t u d y, _t he, _ M i l k
y, _ W a y, _a n d, _ d i s
c o v e r e d, _t h a t, _ i
t, _ i s, _ c o m p o s e
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Vocabulary

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re

Training Data

_ P r o o f, _ o f, _t he,
_ M i l k y, _ W a y, _ c o
n s i s t i n g, _ o f, _ m
a n y, _ s t a r s, _ c a m
e, _ i n, _ 1 6 1 0, _ w he
n, _ G a l i l e o, _ G a l
i l e i, _ u s e d, _a, _t
e l e s c o p e, _t o, _ s
t u d y, _t he, _ M i l k
y, _ W a y, _a n d, _ d i s
c o v e r e d, _t h a t, _ i
t, _ i s, _ c o m p o s e
d, _ o f, _a, _ h u g e, _
n u m b e r, _ o f, _ f a
i n t, _ s t a r s .

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Vocabulary

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he
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re
_the

Training Data

_ P r o o f, _ o f, _the, _
M i l k y, _ W a y, _ c o n
s i s t i n g, _ o f, _ m a
n y, _ s t a r s, _ c a m
e, _ i n, _ 1 6 1 0, _ w h e
n, _ G a l i l e o, _ G a l
i l e i, _ u s e d, _a, _t
e l e s c o p e, _t o, _ s
t u d y, _the, _ M i l k y,
_ W a y, _a n d, _ d i s c
o v e r e d, _t h a t, _ i
t, _ i s, _ c o m p o s e
d, _ o f, _a, _ h u g e, _
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i n t, _ s t a r s .

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Vocabulary

_t
_a
he
in
re
_the

Training Data

_ P r o o f, _ o f, _the, _
M i l k y, _ W a y, _ c o n
s i s t i n g, _ o f, _ m a
n y, _ s t a r s, _ c a m
e, _ i n, _ 1 6 1 0, _ w h e
n, _ G a l i l e o, _ G a l
i l e i, _ u s e d, _a, _t
e l e s c o p e, _t o, _ s
t u d y, _the, _ M i l k y,
_ W a y, _a n d, _ d i s c
o v e r e d, _t h a t, _ i
t, _ i s, _ c o m p o s e
d, _ o f, _a, _ h u g e, _
n u m b e r, _ o f, _ f a
i n t, _ s t a r s .

Pair counts

o n	5261131
_ o	5163783
_ s	5035505
e r	4754849
_ w	4523998
a t	4424733
o u	3838417
_ c	3831635
n d	3811435
o r	3661288

Vocabulary

_t
_a
he
in
re
_the

Training Data

_ P r o o f, _ o f, _the, _
M i l k y, _ W a y, _ c o n
s i s t i n g, _ o f, _ m a
n y, _ s t a r s, _ c a m
e, _ i n, _ 1 6 1 0, _ w h e
n, _ G a l i l e o, _ G a l
i l e i, _ u s e d, _a, _t
e l e s c o p e, _t o, _ s
t u d y, _the, _ M i l k y,
_ W a y, _a n d, _ d i s c
o v e r e d, _t h a t, _ i
t, _ i s, _ c o m p o s e
d, _ o f, _a, _ h u g e, _
n u m b e r, _ o f, _ f a
i n t, _ s t a r s .

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o n	5261131
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_ c	3831635
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Vocabulary

_t

_a

he

in

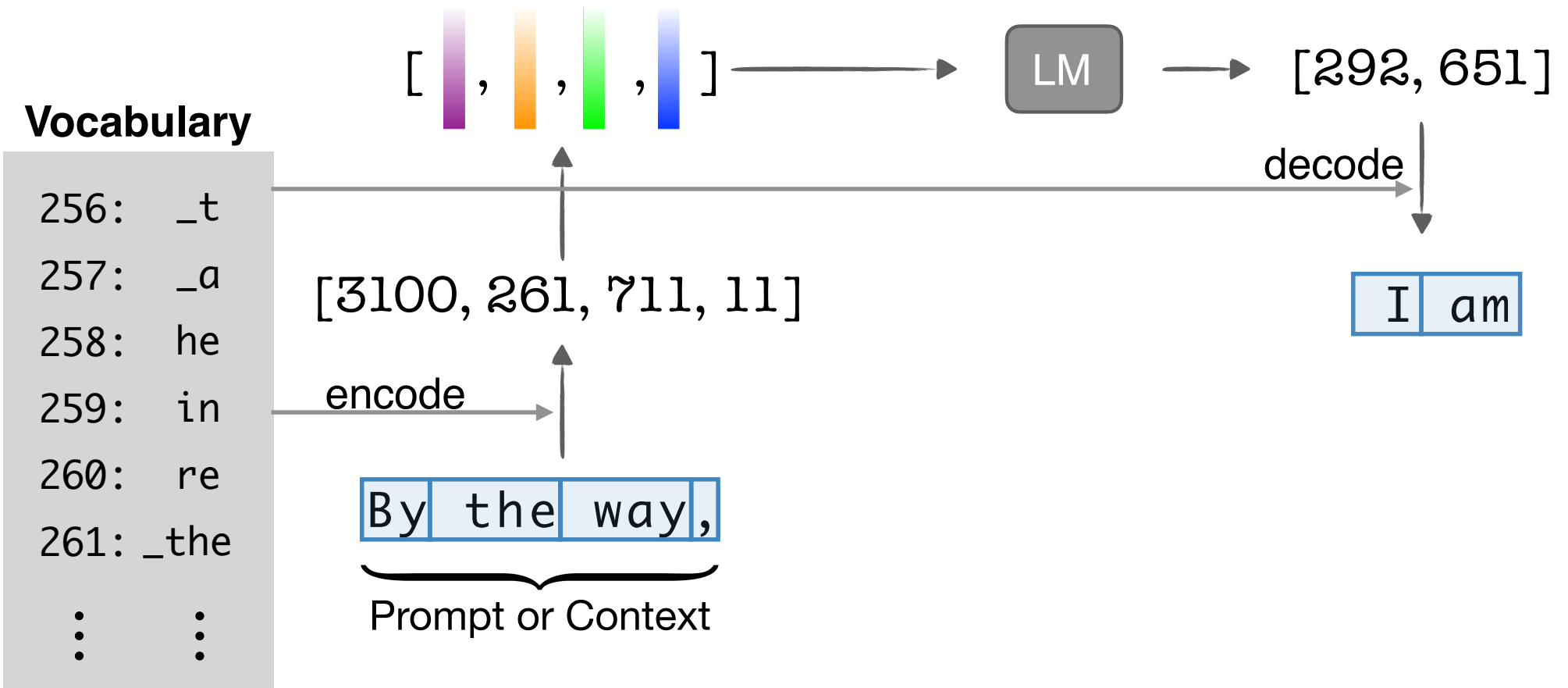
re

_the

⋮

*until we reach
desired vocab size T*

At inference time



Trade-off between vocab size and efficiency

GPT-2 Tokenizer with vocab size 50k
and not trained on coding data

gpt2

Token count
149

```
def·fizz():\n···for·i·in·range(1,·101):\n····if·i·%·5·==·0·and·i·%·3·==·0:\n······print("fizzbuzz")\n····elif·i·%·5·==·0:\n······print("buzz")\n····elif·i·%·3·==·0:\n······print("fizz")\n····else:\n······print(i)
```

GPT-4 Tokenizer with vocab size 100k
and trained on coding data

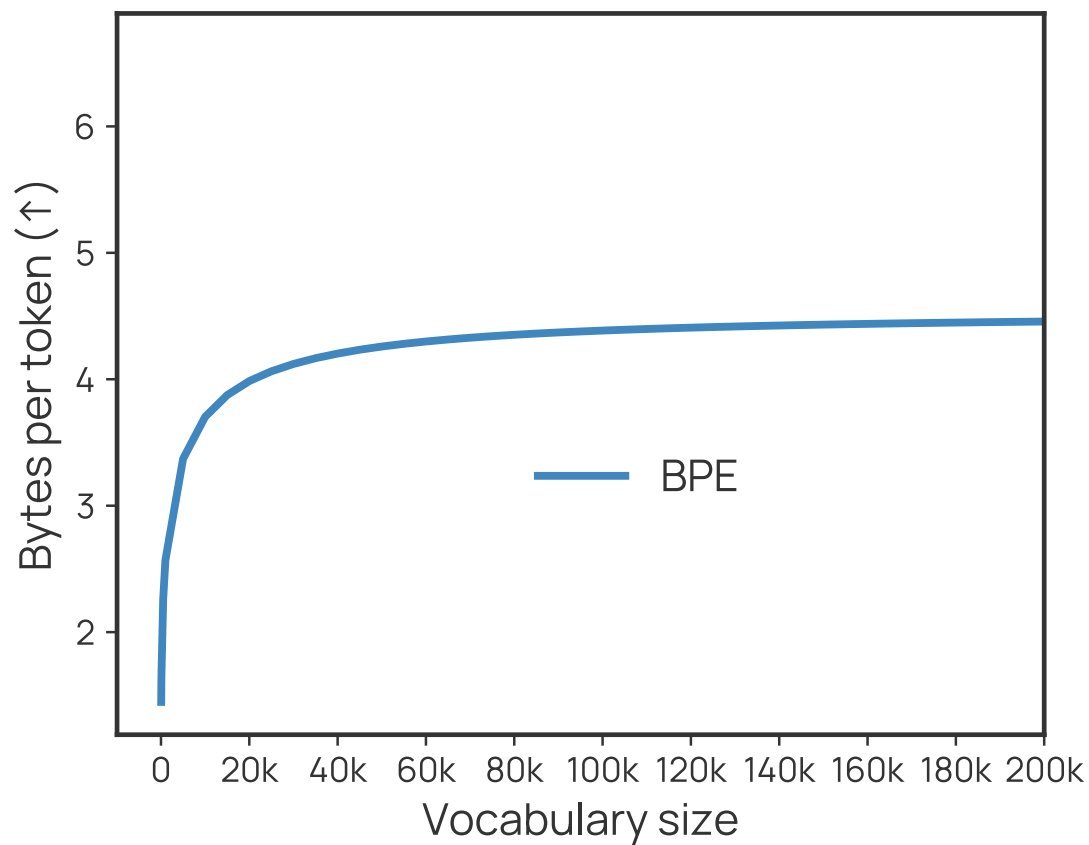
cl100k_base

Token count
77

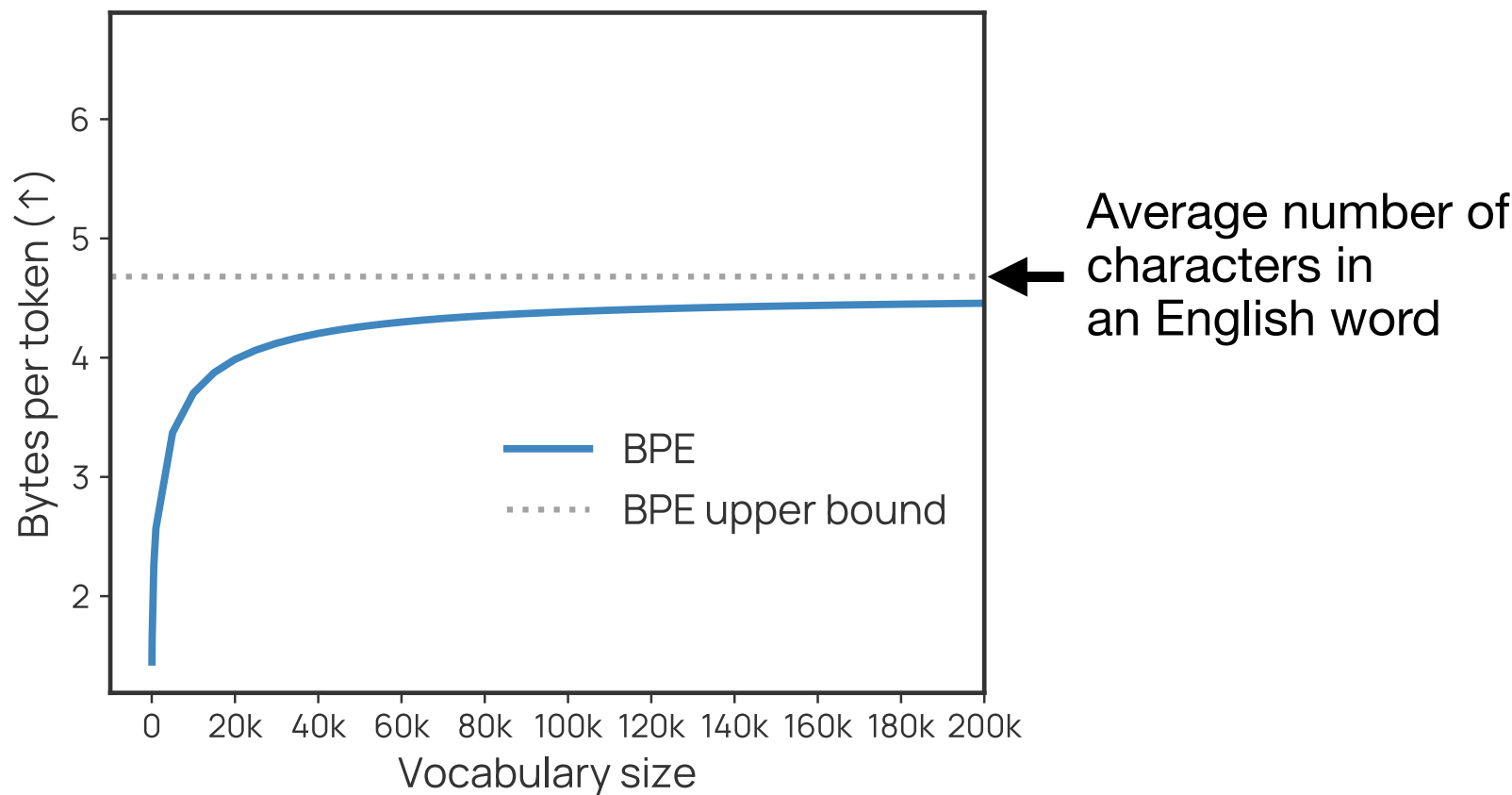
```
def·fizz():\n···for·i·in·range(1,·101):\n····if·i·%·5·==·0·and·i·%·3·==·0:\n······print("fizzbuzz")\n····elif·i·%·5·==·0:\n······print("buzz")\n····elif·i·%·3·==·0:\n······print("fizz")\n····else:\n······print(i)
```

- Why can we not arbitrarily increase the vocab size?
- Research Question 2: How do we know what training data these closed-source tokenizers are trained on?
 - courtesy of <https://github.com/openai/tiktoken>

Trade-off between vocab size and efficiency



Trade-off between vocab size and efficiency



- Research Question 1: Can we beat this fundamental limit of sub-word tokenization?

Challenges with BPE tokenization (in GPT-2)

- Loss of performance for non-English languages
 - Reason: Training data contains majority of English text, which causes majority of tokens being assigned to compress English
- Loss of performance for Python
 - Lots of whitespaces for indentation requires a lot of tokens
- YAML works better than JSON

YAML is more efficiently tokenized than JSON

gpt-3.5-turbo

Token count
29

Price per prompt
\$0.000029

```
loggingLevel: DEBUG
database:
  host: localhost
  port: 5432
  user: admin
  password: secret>
```

[26330, 4549, 25, 12946, 198, 12494, 512, 220, 3552, 25, 48522, 198, 220, 2700, 25, 220, 19642, 17, 198, 220, 1217, 25, 4074, 198, 220, 3636, 25, 6367, 69209]

gpt-3.5-turbo

Token count
46

Price per prompt
\$0.000046

```
{
  "loggingLevel": "DEBUG",
  "database": {
    "host": "localhost",
    "port": 5432,
    "user": "admin",
    "password": "secret"
  }
}
```

[517, 220, 330, 26330, 4549, 794, 330, 5261, 761, 220, 330, 12494, 794, 341, 262, 330, 3875, 794, 330, 8465, 761, 262, 330, 403, 794, 220, 19642, 17, 345, 262, 330, 882, 794, 330, 2953, 761, 262, 330, 3918, 794, 330, 21107, 702, 220, 457, 92]

***Research Question 1:
Why do we need to limit tokens
to parts of words?***

SuperBPE: Space Travel for Language Models

*Alisa Liu^{♡♠} *Jonathan Hayase[♡]

Valentin Hofmann^{◇♡} Sewoong Oh[♡] Noah A. Smith^{♡◇} Yejin Choi[♠]

[♡]University of Washington [♠]NVIDIA [◇]Allen Institute for AI

Abstract

The assumption across nearly all language model (LM) tokenization schemes is that tokens should be *subwords*, i.e., contained within word boundaries. While providing a seemingly reasonable inductive bias, is this common practice limiting the potential of modern LMs? Whitespace is not a reliable delimiter of meaning, as evidenced by multi-word expressions (e.g., *by the way*), crosslingual variation in the number of words needed to express a concept (e.g., *spacesuit helmet* in German is *Raumanzughelm*), and languages that do not use whitespace at all (e.g., Chinese). To explore the potential of tokenization beyond subwords, we introduce a “superword” tokenizer, **SuperBPE**, which incorporates a simple pretokenization curriculum into the byte-pair encoding (BPE) algorithm to first learn subwords, then superwords that bridge whitespace. This brings dramatic improvements in encoding efficiency: when fixing the vocabulary size to 200k, SuperBPE encodes a fixed piece of text with up to 33% fewer tokens than

Research Question 1: Why do we need to limit tokens to parts of words?

- Multi-word expressions

“by the way,” “by accident,” “for a living,” “in the long run”

- Some languages (e.g., Chinese) do not use **whitespace** at all!

“This is a really long sentence that goes on and on” → “这是一个很长的句子，没完没了”

SuperBPE

- Phase 1: Run BPE with whitespace barrier from pretokenization until $t < T$
- Phase 2: Run BPE without whitespace barrier until T
- Intuition: learn the basic units of meaning (words) in the first phase, and then merge common word sequences (superwords)

SuperBPE

- Phase 1: Run BPE with whitespace barrier from pretokenization until $t < T$
- Phase 2: Run BPE without whitespace barrier until T
- Intuition: learn the basic units of meaning (words) in the first phase, and then merge common word sequences (superwords)

POS tag	#	Random examples
NN, IN	906	_case_of, _depend_on, _availability_of, _emphasis_on, _distinction_between
VB, DT	566	_reached_a, _discovered_the, _identify_the, _becomes_a, _issued_a
DT, NN	498	_this_month, _no_idea, _the_earth, _the_maximum, _this_stuff
IN, NN	406	_on_top, _by_accident, _in_effect, _for_lunch, _in_front
IN, DT, NN	333	_for_a_living, _by_the_way, _into_the_future, _in_the_midst
IN, DT, NN, IN	33	_at_the_time_of, _in_the_presence_of, _in_the_middle_of, _in_a_way_that

Training Data

Proof of the Milky Way consisting of many stars came in 1610 when Galileo Galilei used a telescope to study the Milky Way and discovered that it is composed of a huge number of faint stars.

Training Data

```
{Proof_of_the_Milky_Way_consisting_of_many_stars_came_in_1610,_when_Galileo_Galilei_used_a_telescope_to_study_the_Milky_Way_and_discovered_that_it_is_composed_of_a_huge_number_of_faint_stars.}
```

- 2nd phase:
 - Skip whitespace pretokenization
 - but can still use other pretokenization rules, e.g., numbers

Training Data

```
{P r o o f _ o f _ t h e _  
M i l k y _ W a y _ c o n s  
i s t i n g _ o f _ m a n y  
_ s t a r s _ c a m e _ i  
n , _ 1 6 1 0 , _ w h e n _ G  
a l i l e o _ G a l i l e i  
_ u s e d _ a _ t e l e s c  
o p e _ t o _ s t u d y _ t  
h e _ M i l k y _ W a y _ a  
n d _ d i s c o v e r e d _  
t h a t _ i t _ i s _ c o m  
p o s e d _ o f _ a _ h u g  
e _ n u m b e r _ o f _ f a  
i n t _ s t a r s . }
```

Split D into sequence of bytes

Training Data

{Proof _of _the _Milky _Way
_consisting _of _many
_stars _came _in_, 1 610,
_when _Gal _ileo _Galilei
_used _a _telescope _to
_study _the _Milky _Way
_and _discovered _that _it
_is _composed _of _a _huge
_number _of _faint _stars.}

Apply tokenizer learned so far

Training Data

{Proof _of _the _Milky _Way
_consisting _of _many
_stars _came _in_, 1 610,
_when _Gal ileo _Galilei
_used _a _telescope _to
_study _the _Milky _Way
_and _discovered _that _it
_is _composed _of _a _huge
_number _of _faint _stars.}

Pair counts

_of _the	517482
' s	456028
, _and	413189
_in _the	362529
' t	247975
. _The	232178
, _the	226412
_to _the	222524
, _but	200360
_on _the	164233

Vocabulary

stage 1 {
_t
_a
he
in
re
_the
⋮
_Aleg

Training Data

{Proof _of _the _Milky _Way
_consisting _of _many
_stars _came _in_, 1 610,
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_used _a _telescope _to
_study _the _Milky _Way
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_when _Gal_ileo _Galilei
_used _a _telescope _to
_study _the _Milky _Way
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Pair counts

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' t	247975
. _The	232178
, _the	226412
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, _but	200360
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Vocabulary

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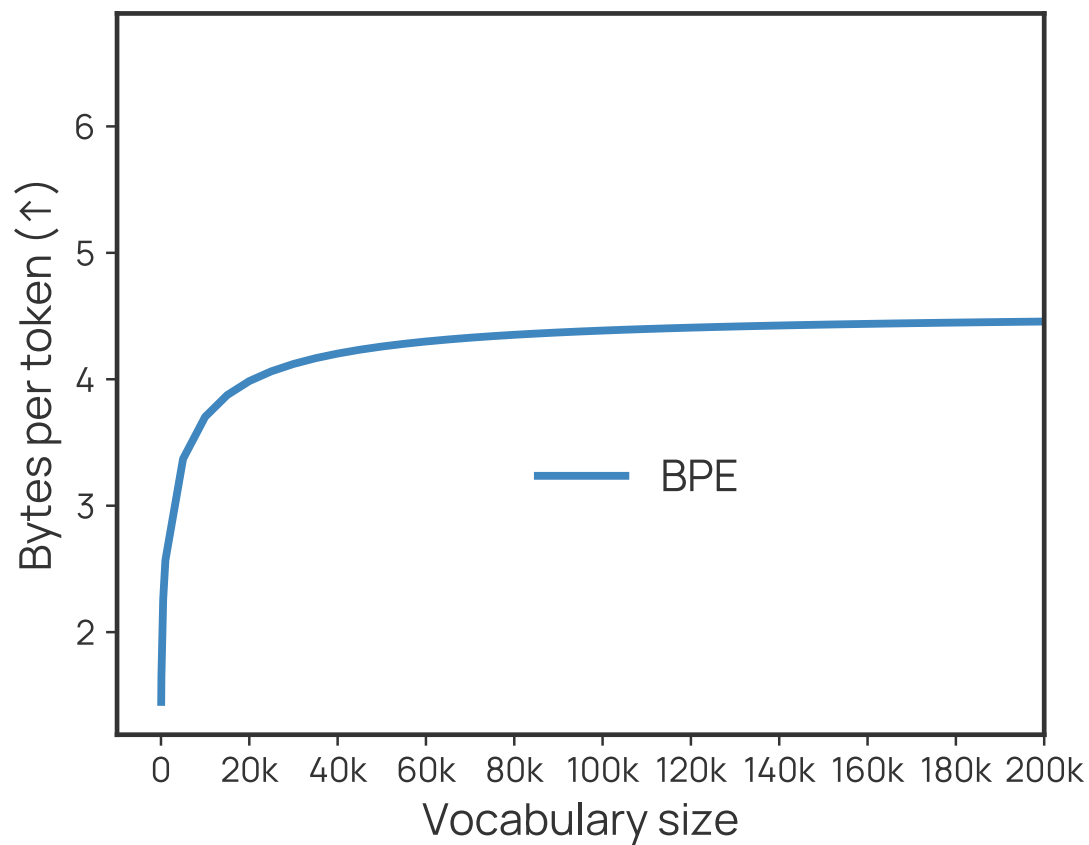
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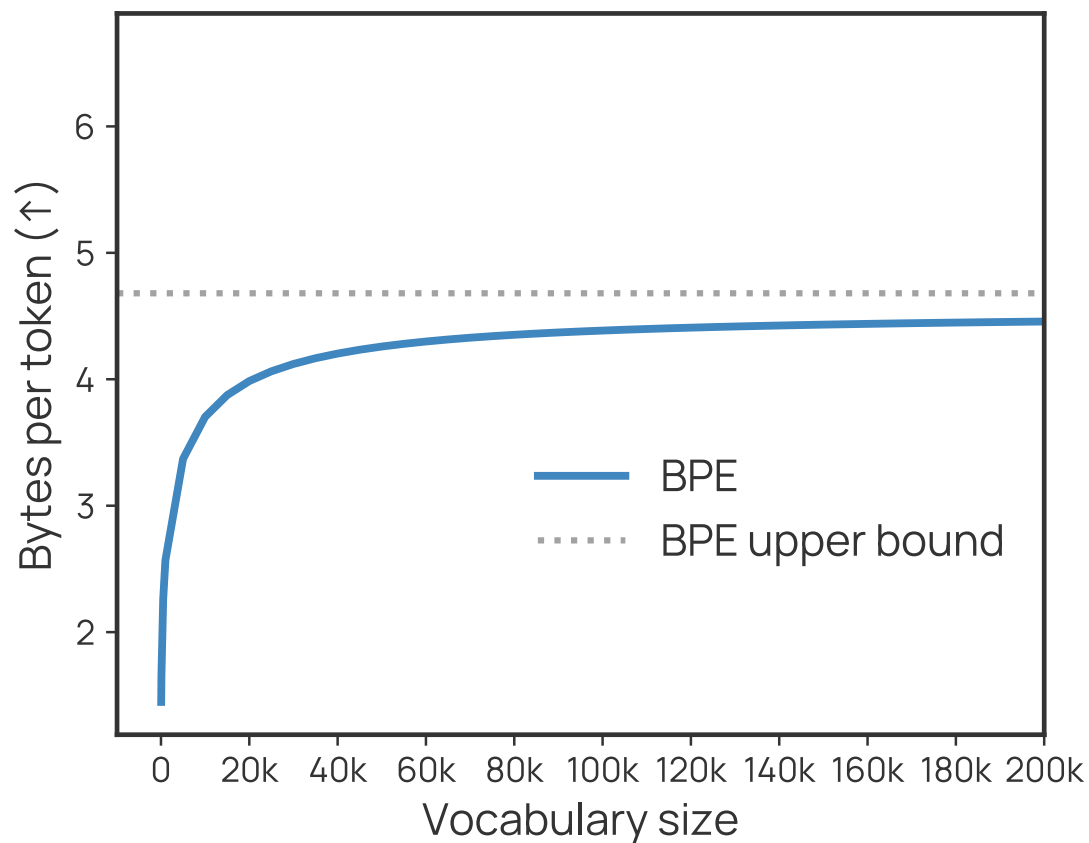
Vocabulary

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*until we reach
desired vocab size T*

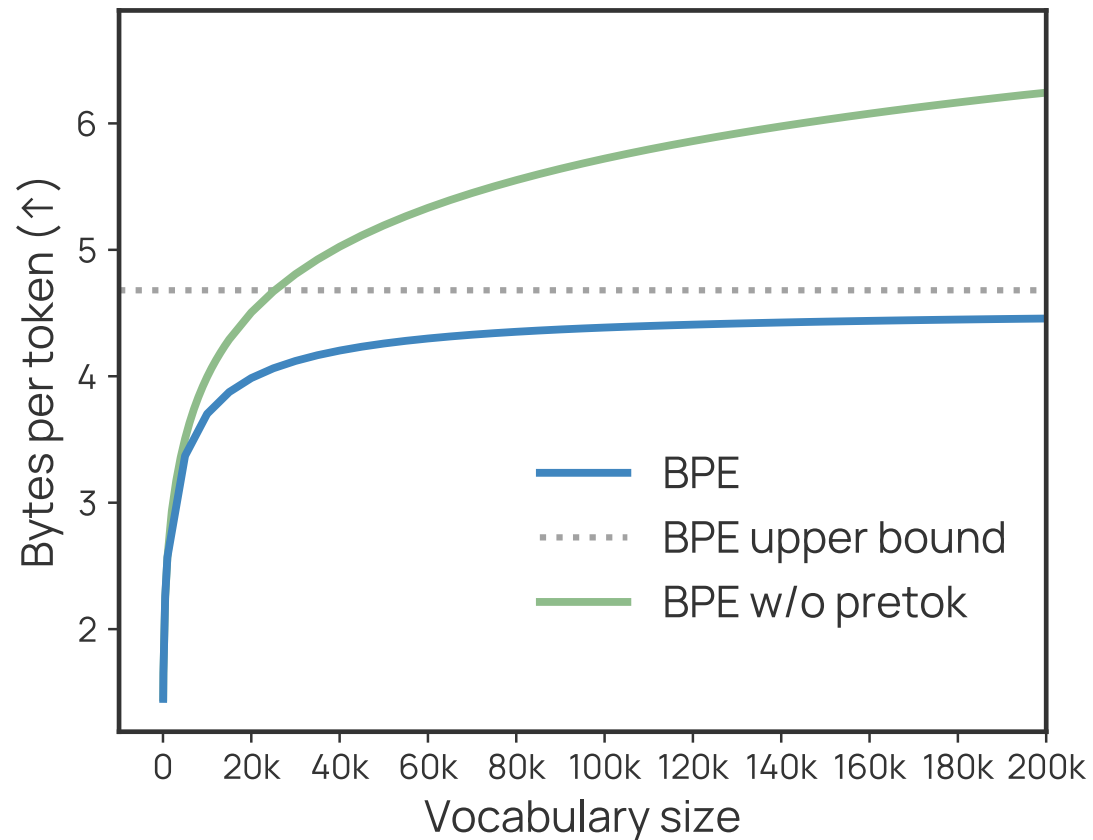
SuperBPE encodes text more efficiently



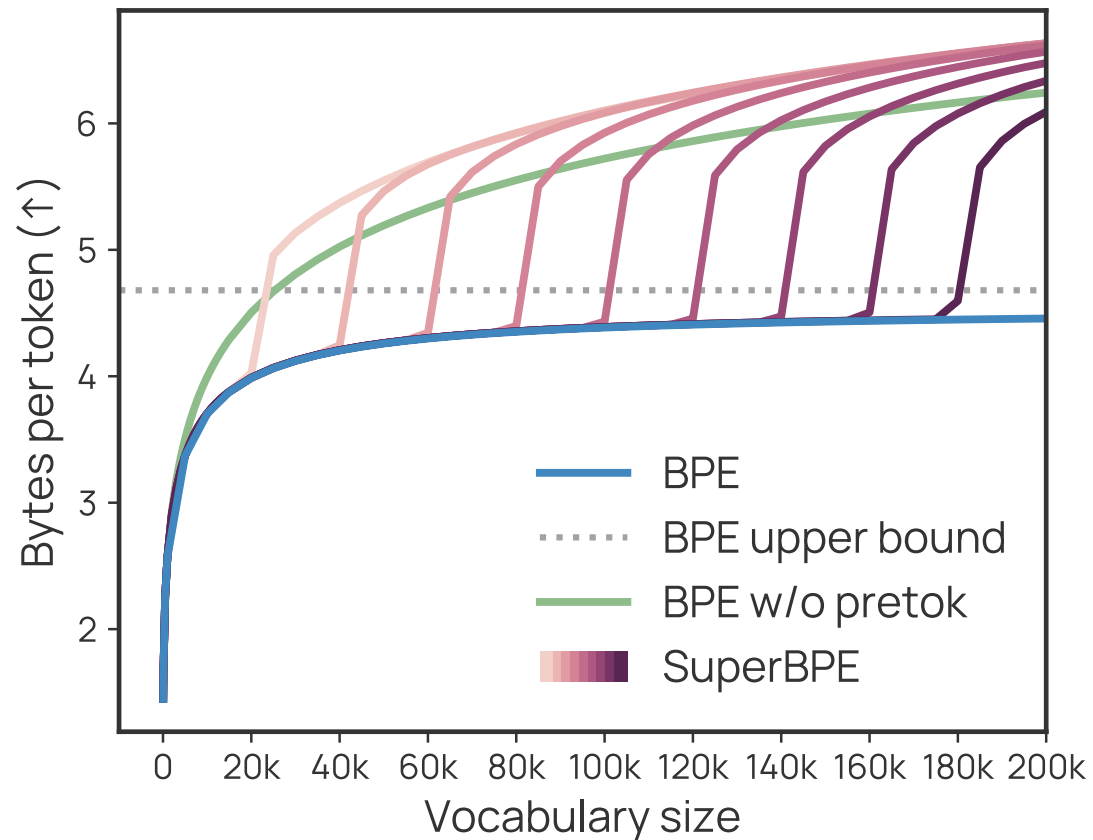
SuperBPE encodes text more efficiently



SuperBPE encodes text 35% more efficiently



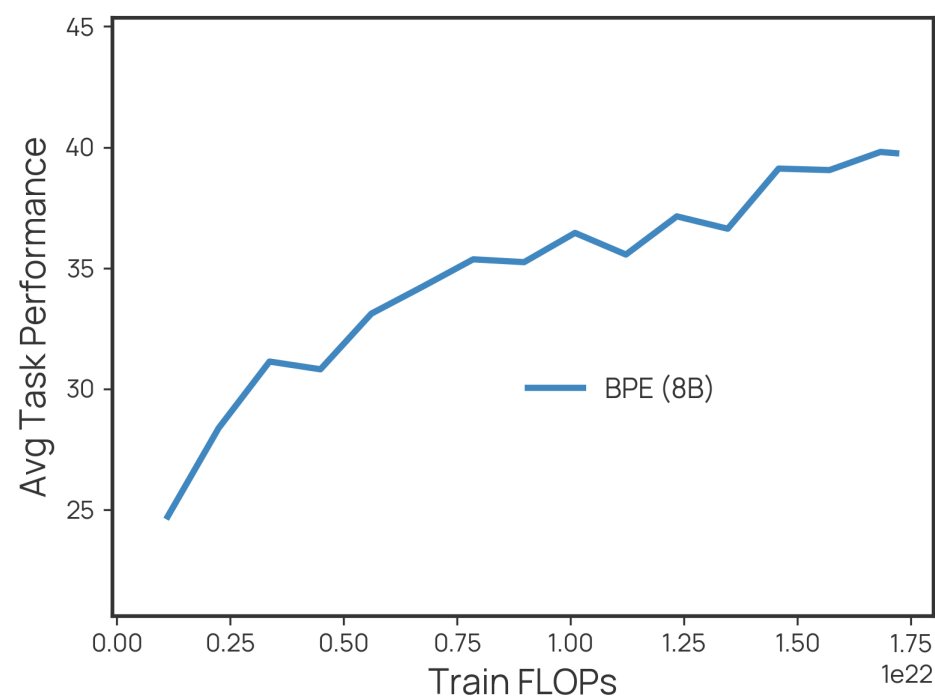
SuperBPE encodes text 35% more efficiently



Changing tokenizer requires pretraining LLM

Baseline: **BPE 8B** (Olmo2 @ 330B tokens)

- Tokenizer: **BPE** with 200k tokens
- Model size: **8B** parameters
- Number of tokens in training: **330B** tokens
- Evaluation
 - Average performance on 30 tasks

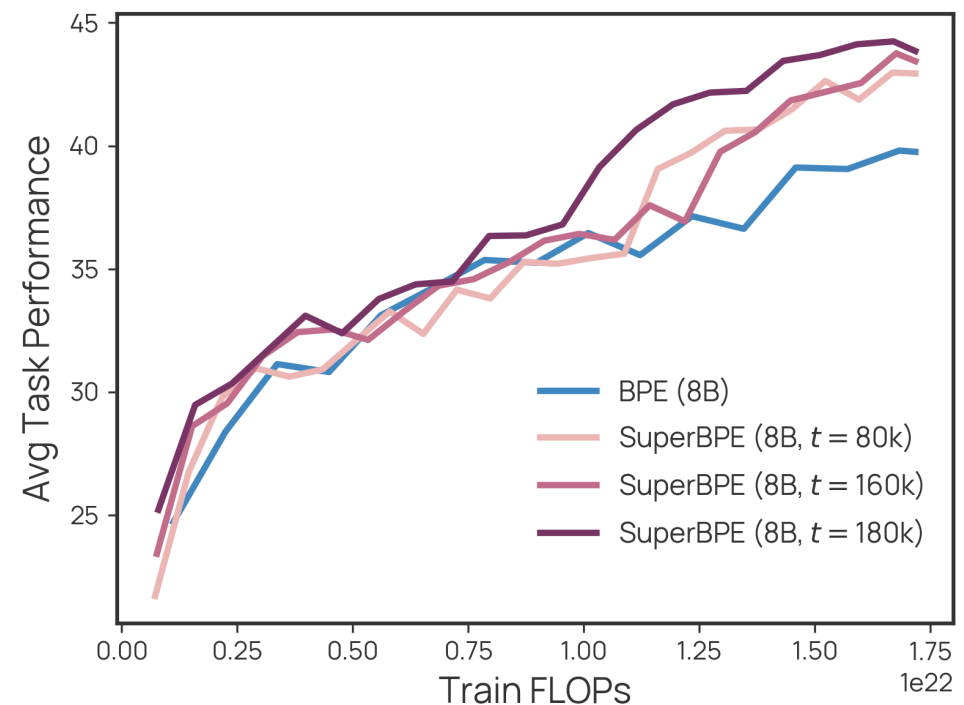


In a fair comparison, SuperBPE outperforms in 30 downstream tasks

Baseline: **BPE 8B** (Olmo2 @ 330B tokens)

SuperBPE 8B

- ✓ model size
- ✓ training compute
- ✗ inference compute (35% less)
- ✗ amount of text seen (41% more)

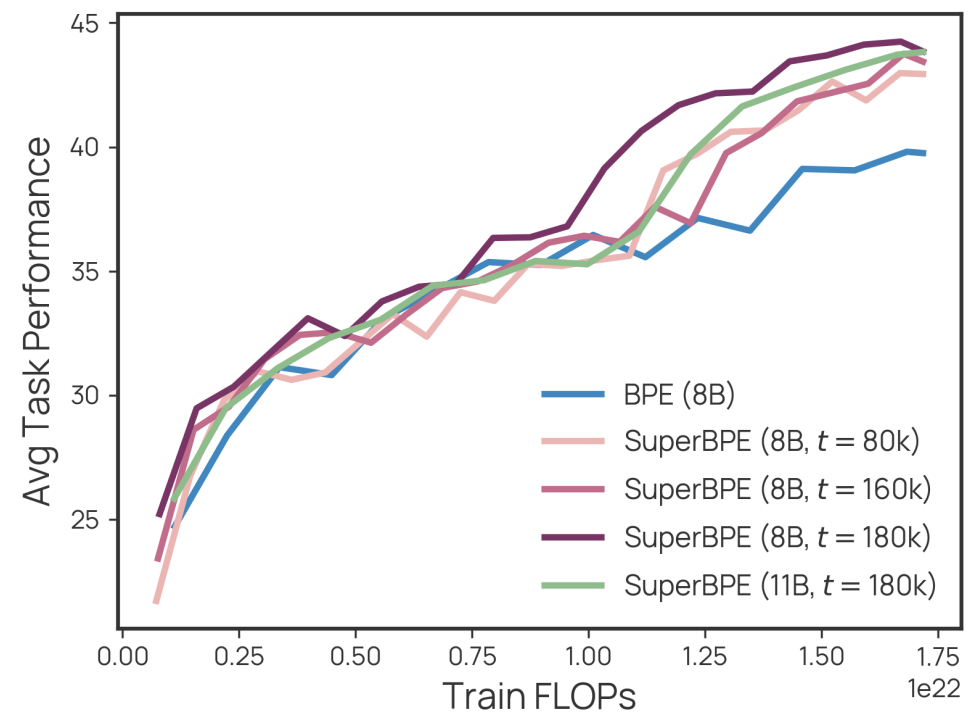


In a fair comparison, SuperBPE outperforms in 30 downstream tasks

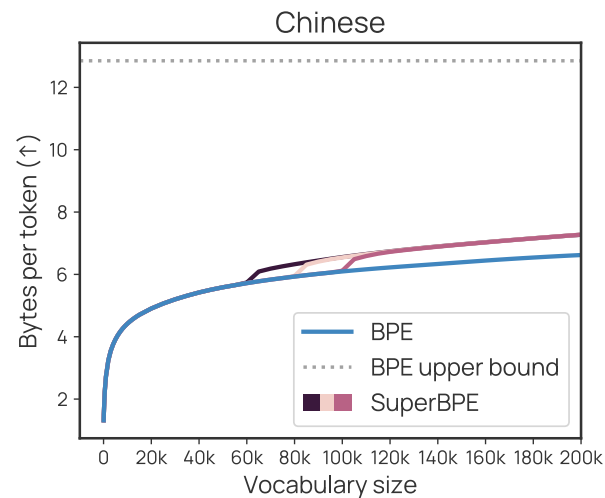
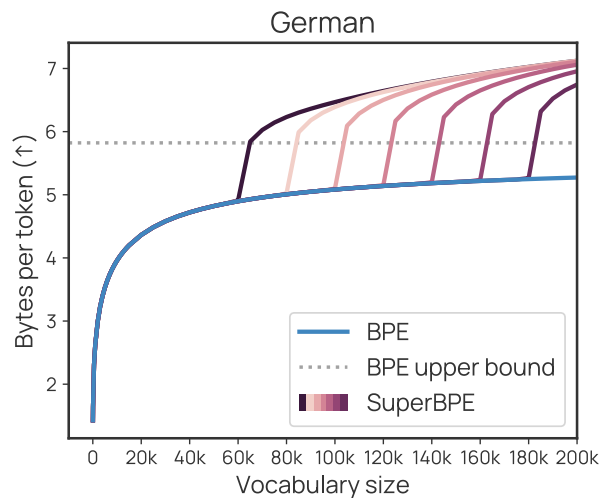
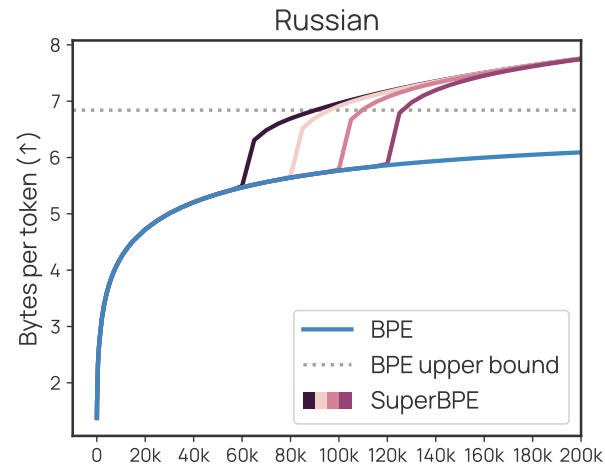
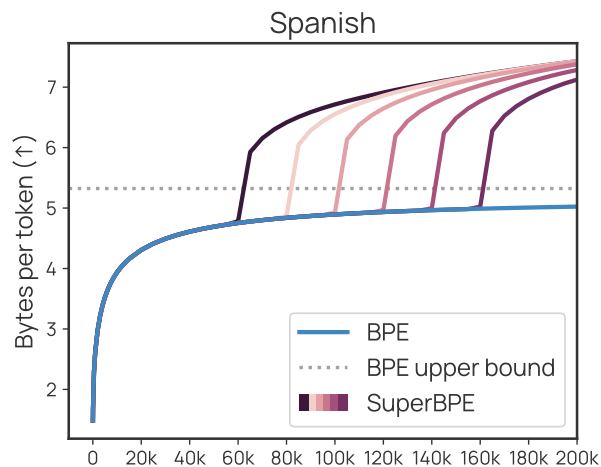
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SuperBPE 11B

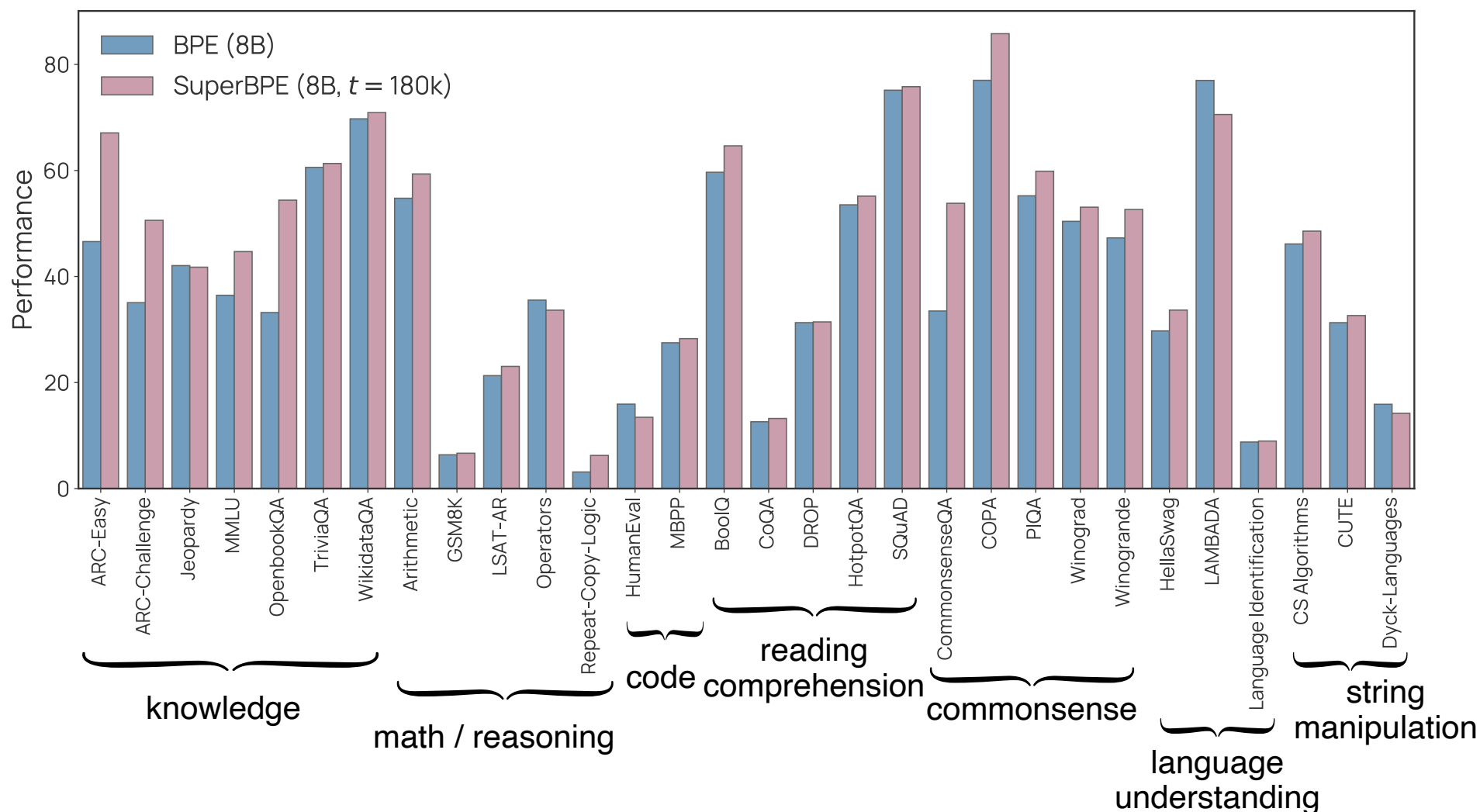
- ✗ model size (39% bigger)
- ✓ training compute
- ✓ inference compute
- ✓ amount of text seen



Efficiency scaling for non-English languages



SuperBPE downstream performance



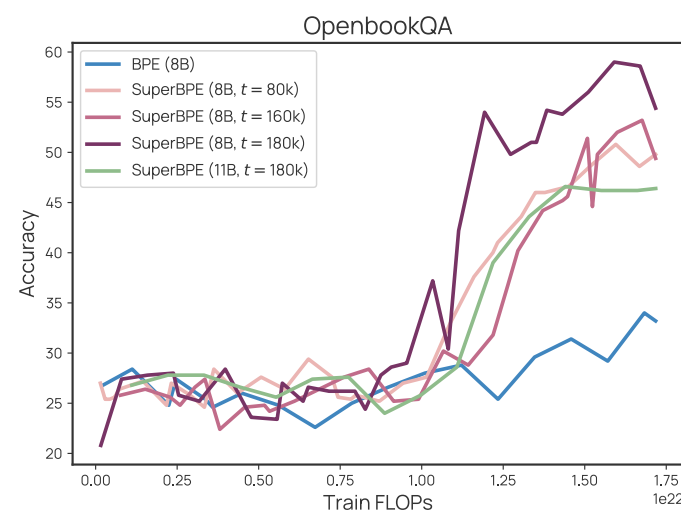
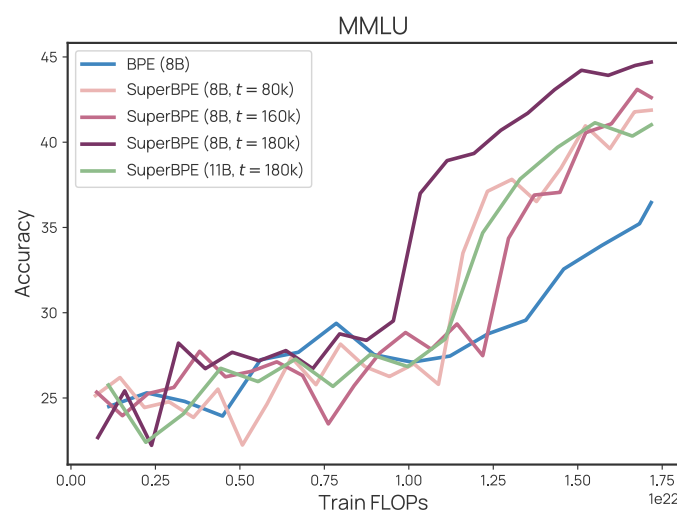
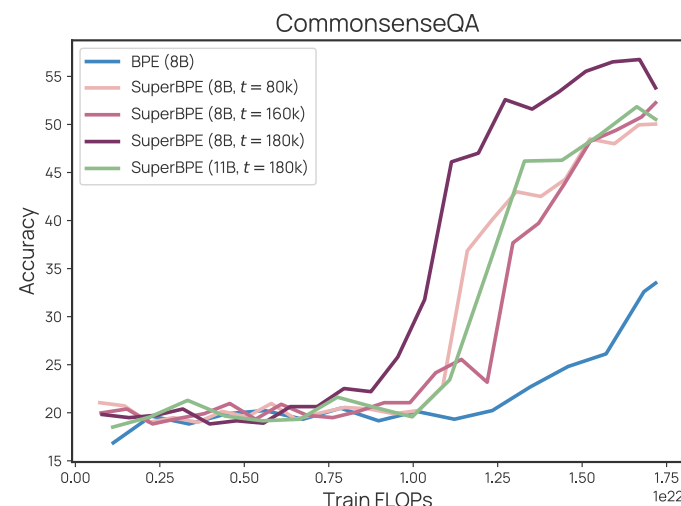
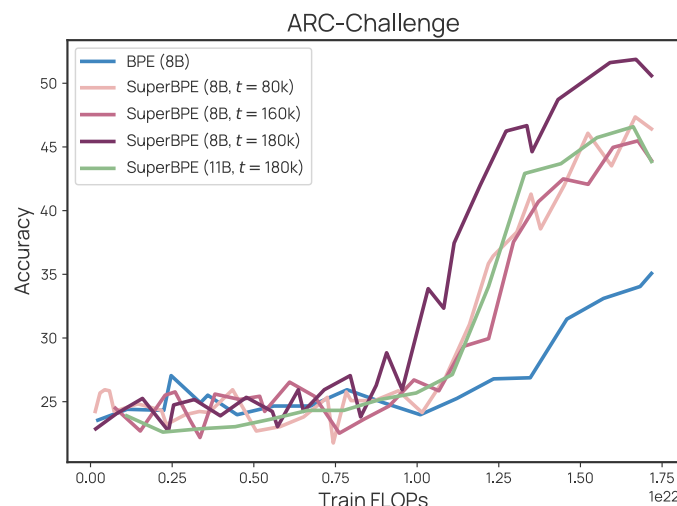
Examples of multiple choice tasks

- ARC-Challenge measures common sense
 - Q. George wants to warm his hands quickly by rubbing them. Which skin surface will produce the most heat?
 - (A) **dry palms**, (B) wet palms, (C) palms covered with oil, (D) palms covered with lotion
- CommonsenseQA
 - Q. What do all humans want to experience in their own home?
 - (A) **feel comfortable**, (B) work hard, (C) fall in love, (D) lay eggs, (E) live forever
- MMLU (Massive Multitask Language Understanding)
 - Find all c in $\mathbb{Z}_3$ such that $\frac{\mathbb{Z}_3[x]}{(x^2 + c)}$ is a field.
 - (A) 0 , (B) **1** , (C) 2 , (D) 3
- OpenbookQA
 - Q. As a car approaches you in the night
 - (A) **the headlights become more intense**, (B) the headlights recede into the dark, (C) the headlights remain at a constant, and (D) the headlights turn off

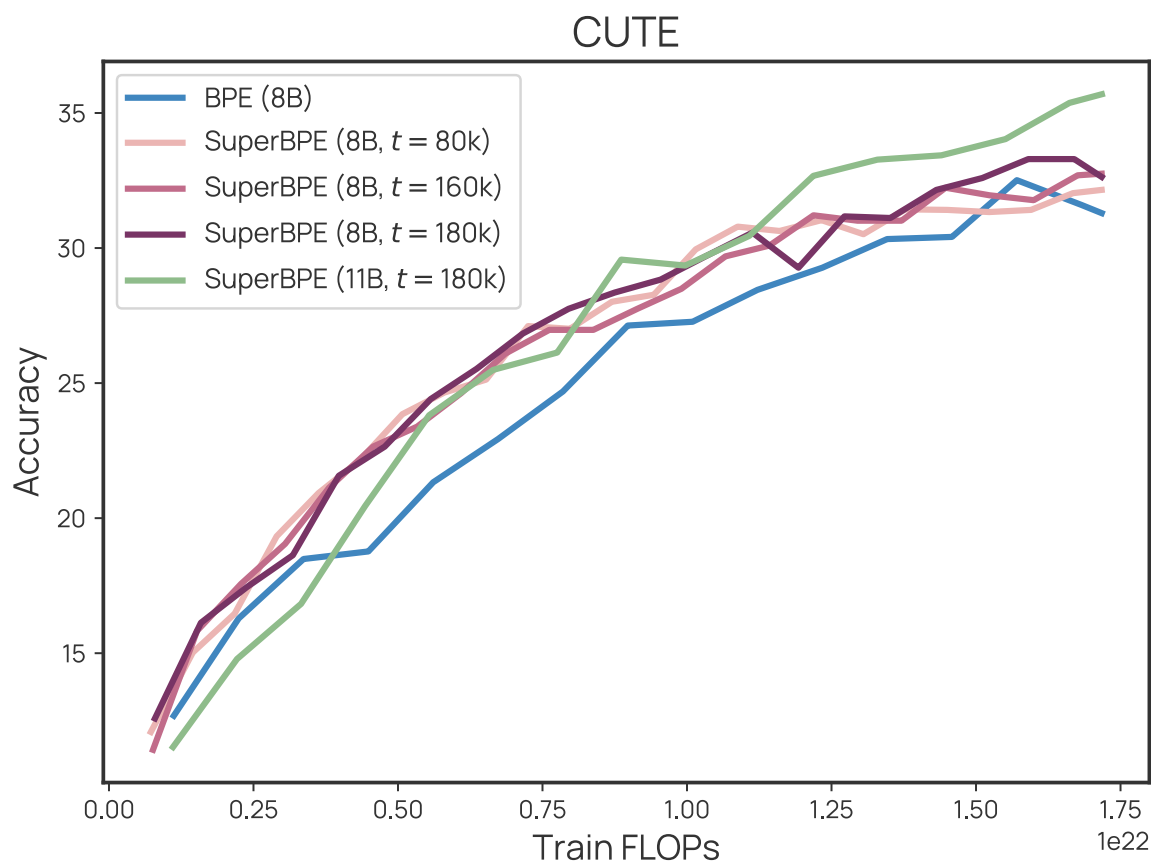
Multiple Choice

SuperBPE achieves large improvements in MC

All models begin to achieve better-than-random performance at a particular moment



String manipulation tasks



Is there a " c " in " also "?

*Delete every instance of "
t " in " data ".*

*Swap " k " and " e " in "
make ".*

***Research Question 2:
How do we know what data is
used to train the tokenizer?***

Data Mixture Inference: What do BPE Tokenizers Reveal about their Training Data?

*Jonathan Hayase[♡] *Alisa Liu[♡] Yejin Choi^{♡♣} Sewoong Oh[♡] Noah A. Smith^{♡♣}
[♡]University of Washington [♣]Allen Institute for AI
{jhayase, alisaliu}@cs.washington.edu

Abstract

The pretraining data of today’s strongest language models is opaque; in particular, little is known about the proportions of various domains or languages represented. In this work, we tackle a task which we call *data mixture inference*, which aims to uncover the distributional make-up of training data. We introduce a novel attack based on a previously overlooked source of information: byte-pair encoding (BPE) tokenizers, used by the vast majority of modern language models. Our key insight is that the ordered list of merge rules learned by a BPE tokenizer naturally reveals information about the token frequencies in its training data. Given a tokenizer’s merge list along with example data for each category of interest, we formulate a linear program that solves for the proportion of each category in the tokenizer’s training set. In controlled experiments, we show that our attack recovers mixture ratios with high precision for tokenizers trained on known mixtures of natural languages, programming languages, and data sources. We then apply our approach to off-the-shelf tokenizers released with recent LMs. We confirm much publicly disclosed information about these models, and also make several new inferences: GPT-4O and MISTRAL NEMO’s tokenizers are much more multilingual than their predecessors, training on 39% and 47% non-English language data, respectively; LLAMA 3 extends GPT-3.5’s tokenizer primarily for multilingual (48%) use; GPT-3.5’s and CLAUDE’s tokenizers are trained on predominantly code ($\sim 60\%$). We hope our work sheds light on current design practices for pretraining data, and inspires continued research into data mixture inference for LMs.¹

Data Mixture Inference

English $\mathcal{D}_{\text{En}}$

Normalize **th**e dig**it**s, **th**en
ensure **th**at **th**ey sum to 1.

Python $\mathcal{D}_{\text{Py}}$

```
x = logits.softmax() # get probs  
assert x.sum().item() == 1 # compare
```

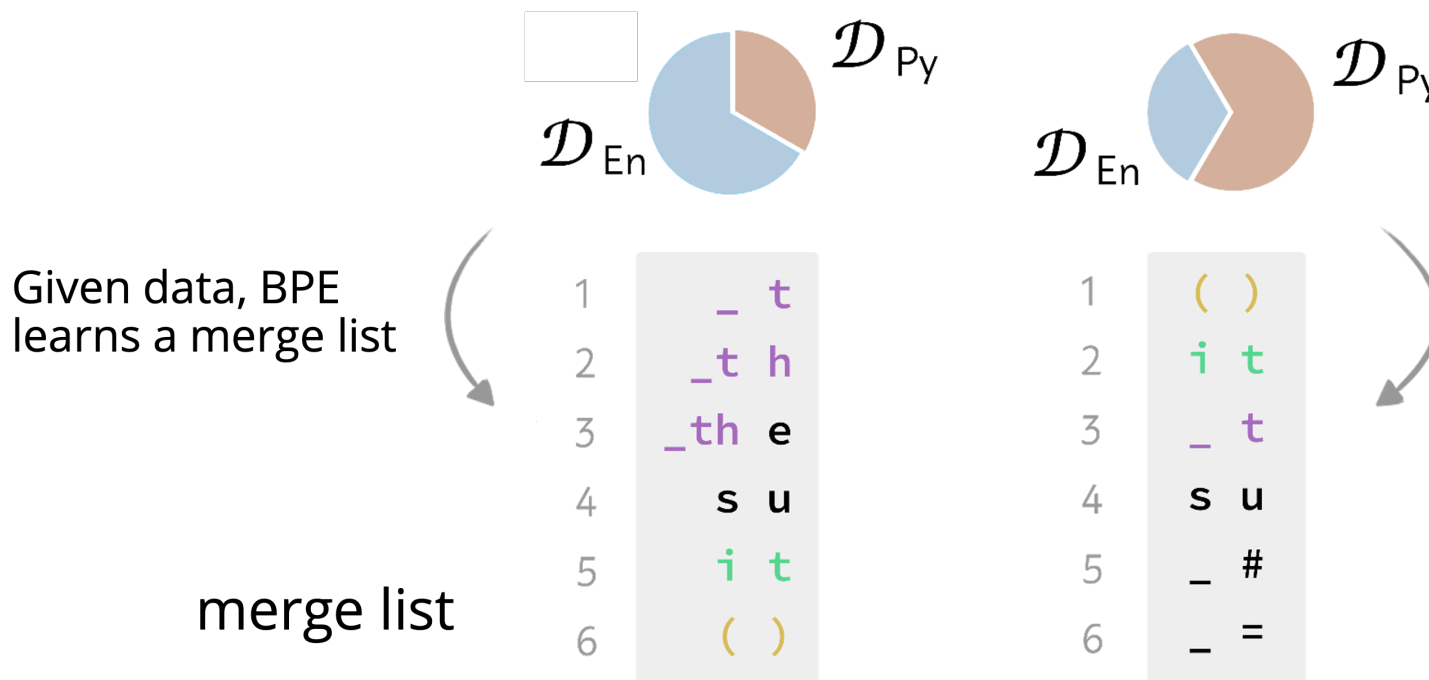
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The learned merge list is (very) sensitive to the mixture ratio of data distributions

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merge list



1	-	t
2	-	t h
3	-	th e
4		s u
5		i t
6		()



1	()
2	i t
3	- t
4	s u
5	- #
6	- =

Given a merge list,
can we solve for the
mixture ratio?

The learned merge list is (very) sensitive to the mixture ratio of data distributions

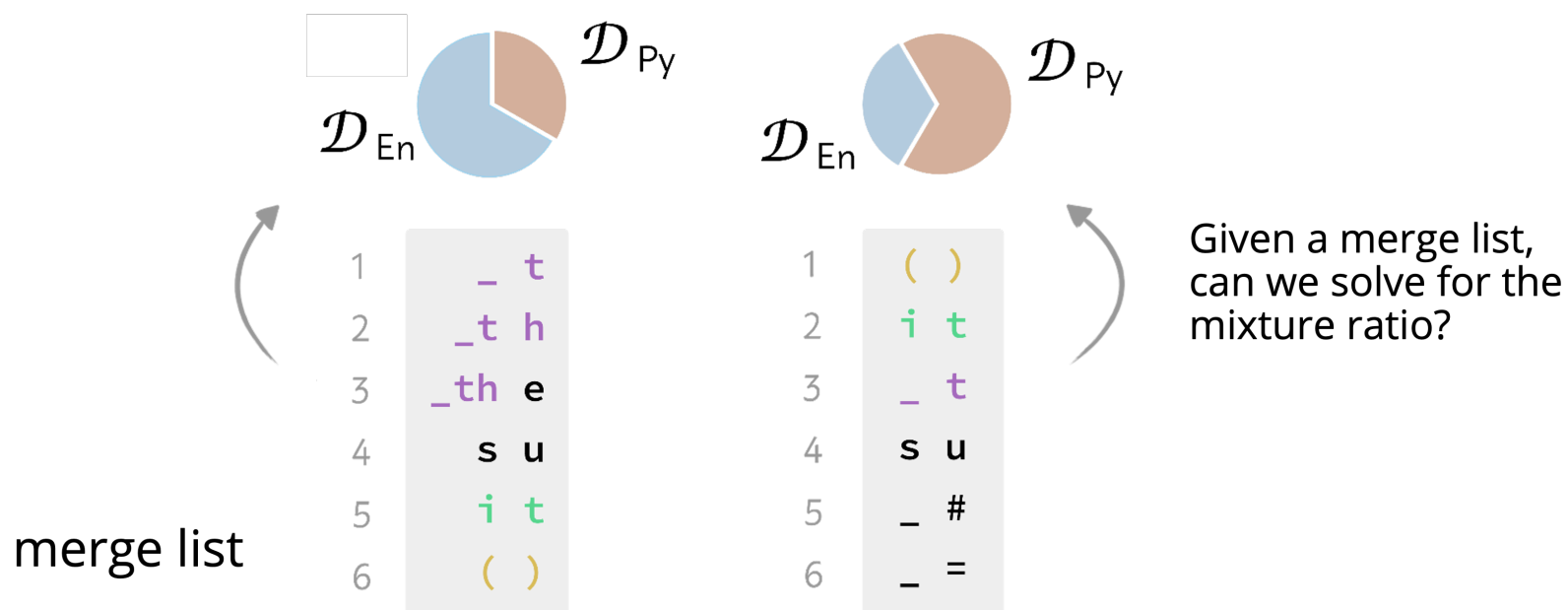
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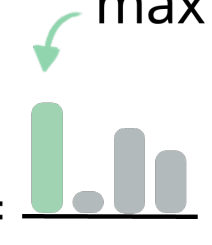
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```



Merge List

counts in En corpus

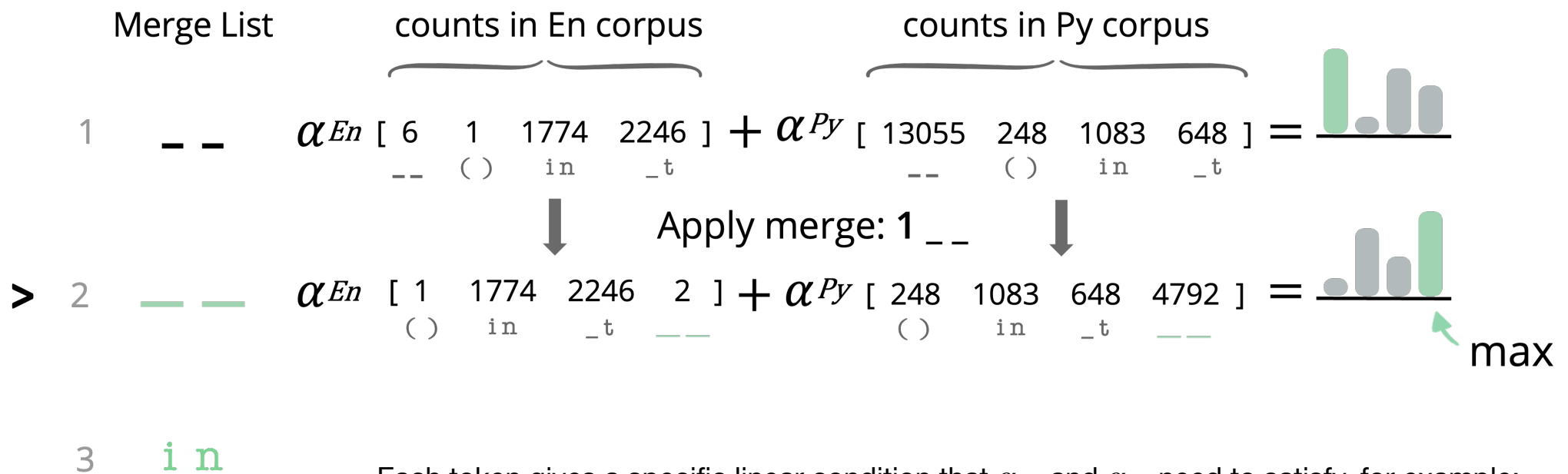
counts in Py corpus

> 1 $\alpha^{En} [\underset{\text{--}}{6} \quad \underset{()}{1} \quad 1774 \quad 2246] + \alpha^{Py} [\underset{\text{--}}{13055} \quad \underset{()}{248} \quad 1083 \quad 648] =$ 

2

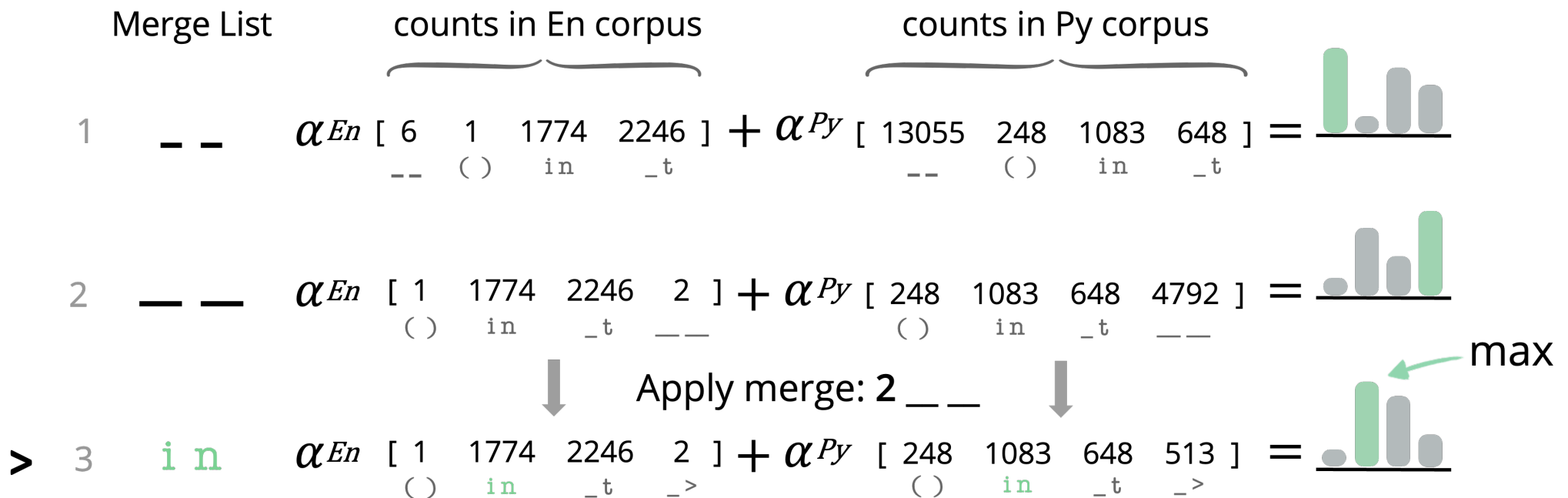
Each token gives a specific linear condition that α_{En} and α_{Py} need to satisfy, for example:

3 i n $6 \alpha_{En} + 13055 \alpha_{Py} \geq \max_{token \neq _} \{ \alpha_{En} C_{En,token}^{(1)} + \alpha_{Py} C_{Py,token}^{(1)} \}$



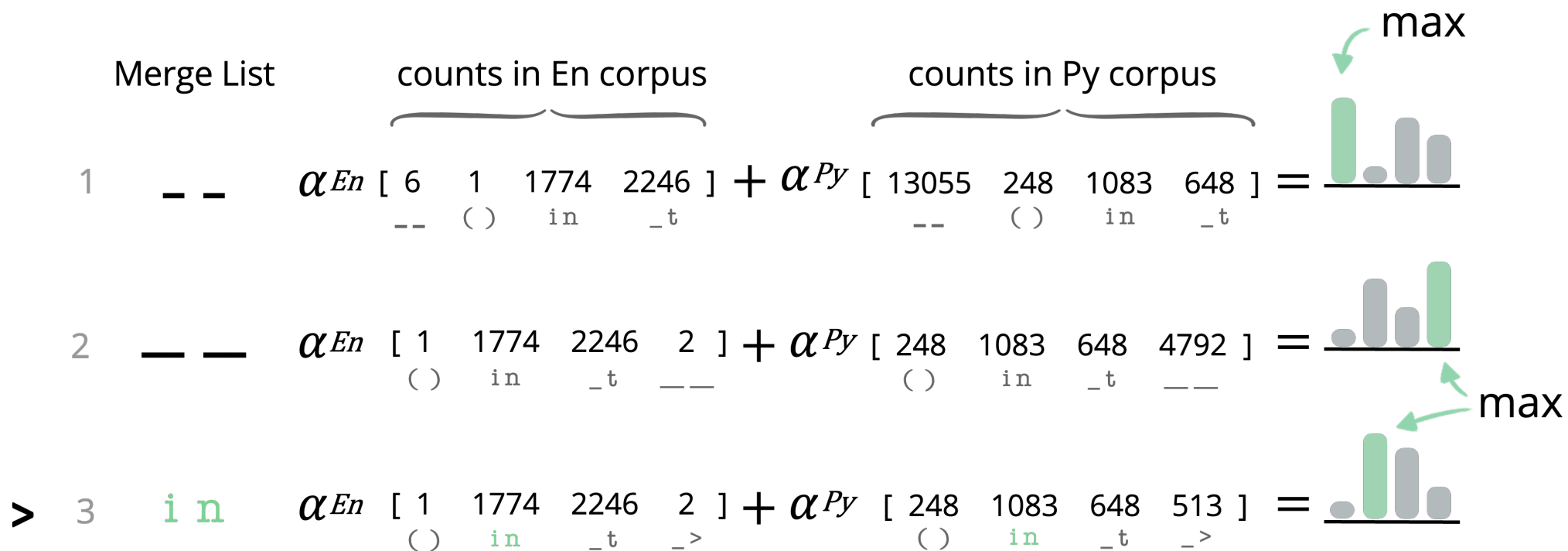
Each token gives a specific linear condition that α_{En} and α_{Py} need to satisfy, for example:

$$2 \alpha_{En} + 4792 \alpha_{Py} \geq \max_{token \neq \text{---}} \{ \alpha_{En} C_{En,token}^{(2)} + \alpha_{Py} C_{Py,token}^{(2)} \}$$



Each token gives a specific linear condition that α_{En} and α_{Py} need to satisfy, for example:

$$1774 \alpha_{En} + 1083 \alpha_{Py} \geq \max_{token \neq in} \left\{ \alpha_{En} C_{En,token}^{(3)} + \alpha_{Py} C_{Py,token}^{(3)} \right\}$$



At every step, the mixture ratios should give a vector with the true merge's index as the max value.

$$\sum_{i=1}^n \alpha_i c_{i,m^{(t)}}^{(t)} \geq \sum_{i=1}^n \alpha_i c_{i,p}^{(t)} \text{ for all } p \neq m^{(t)}$$

We can formulate this as a linear program

Objective: minimize $\sum_{t=1}^M v^{(t)} + \sum_p v_p$

Subject to constraints:

At every time step t ,

constraint violation

$$v^{(t)} + v_p + \sum_{i=1}^n \alpha_i c_{i,m^{(t)}}^{(t)} \geq \sum_{i=1}^n \alpha_i c_{i,p}^{(t)} \text{ for all } p \neq m^{(t)}$$

for each time step t for each pair p

Naively this has 10s of billions of constraints, see paper for how we solve it efficiently :)

Controlled Experiments

Evaluate attack on tokenizers trained with known mixtures!

Natural languages (112) from Oscar (web data)

Programming languages (37) from raw Github data

Domains (5) from RedPajama (all English) — web, books, Wiki, code, ArXiv

For $n \in \{5, 10, 30, 112\}$, sample n categories and weights uniformly.

Sample 10G of data with the desired mixture ratio for tokenizer training. For the attack, sample 1G of data per category.

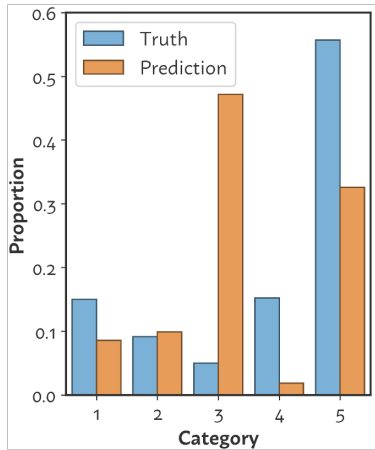
$$\text{Report MSE} = \frac{1}{n} \sum_{i=1}^n (\hat{\alpha}_i - \alpha_i)^2.$$

Results

Log₁₀ MSE (↓)

number of categories	n	Random	Languages	Code	Domains
	5				
	10				
	30				
	112				

Results

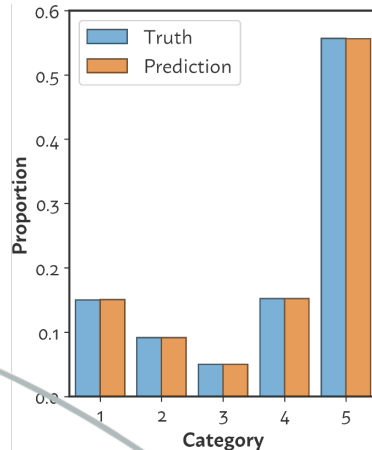
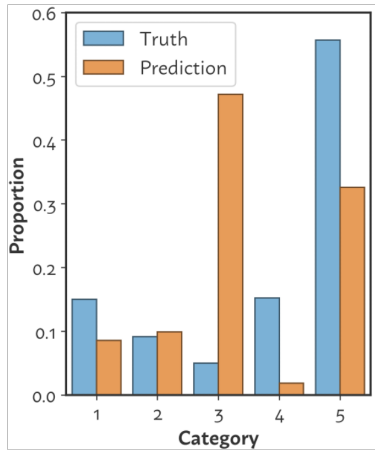


$\text{Log}_{10} \text{MSE} (\downarrow)$

number of
categories

n	random guess baseline	Languages	Code	Domains
5	-1.39			
10				
30				
112				

Results

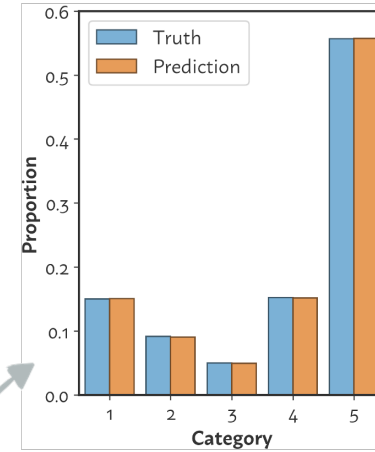
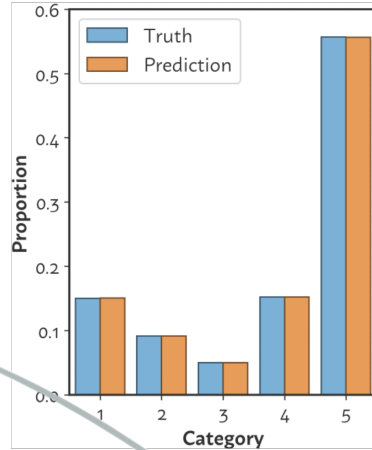
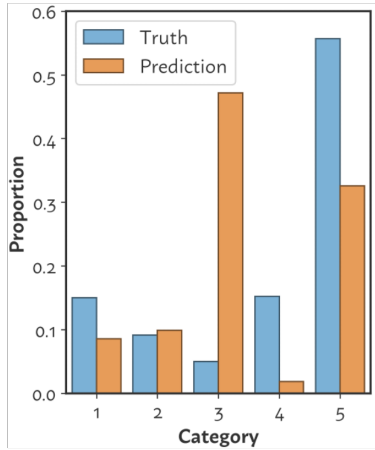


$\text{Log}_{10} \text{MSE} (\downarrow)$

number of
categories

n	Random	Languages	Code	Domains
5	-1.39	-7.30		
10				
30				
112				

Results

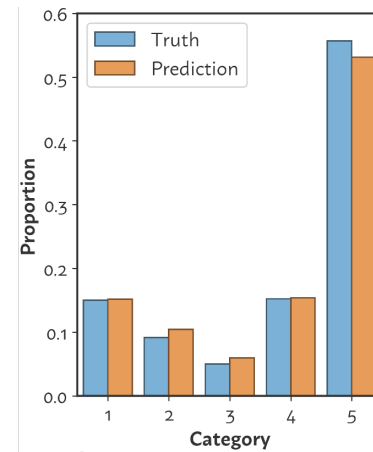
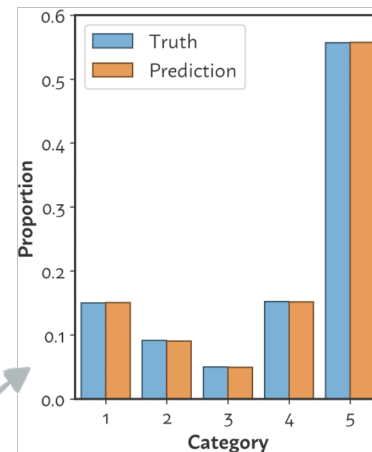
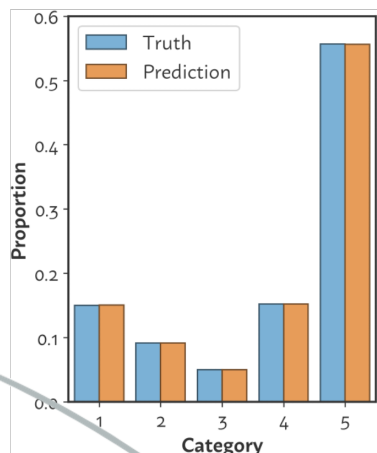
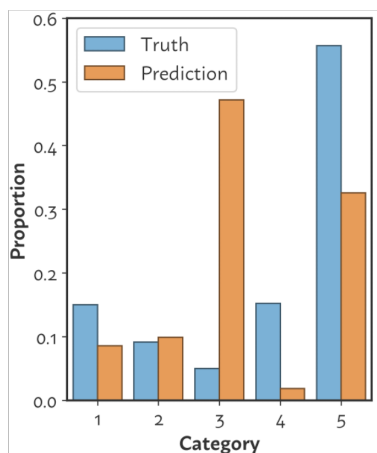


Log₁₀ MSE (↓)

number of
categories

n	Random	Languages	Code	Domains
5	-1.39	-7.30	-6.46	
10				
30				
112				

Results



$\text{Log}_{10} \text{MSE} (\downarrow)$

number of
categories

n	Random	Languages	Code	Domains
5	-1.39	-7.30	-6.46	-3.74
10				
30				
112				

Log₁₀ MSE (↓)

number of categories	n	Random	Languages	Code	Domains
	5	-1.39	-7.30	-6.46	-3.74
	10	-1.84	-7.66	-6.30	-
	30	-2.70	-7.73	-5.98	-
	112	-3.82	-7.69	-	-

Our attack achieves performance 10^2 to $10^6\times$ better than random!

Commercial Tokenizers

Let's apply our attack to off-the-shelf tokenizers released with LLMs!

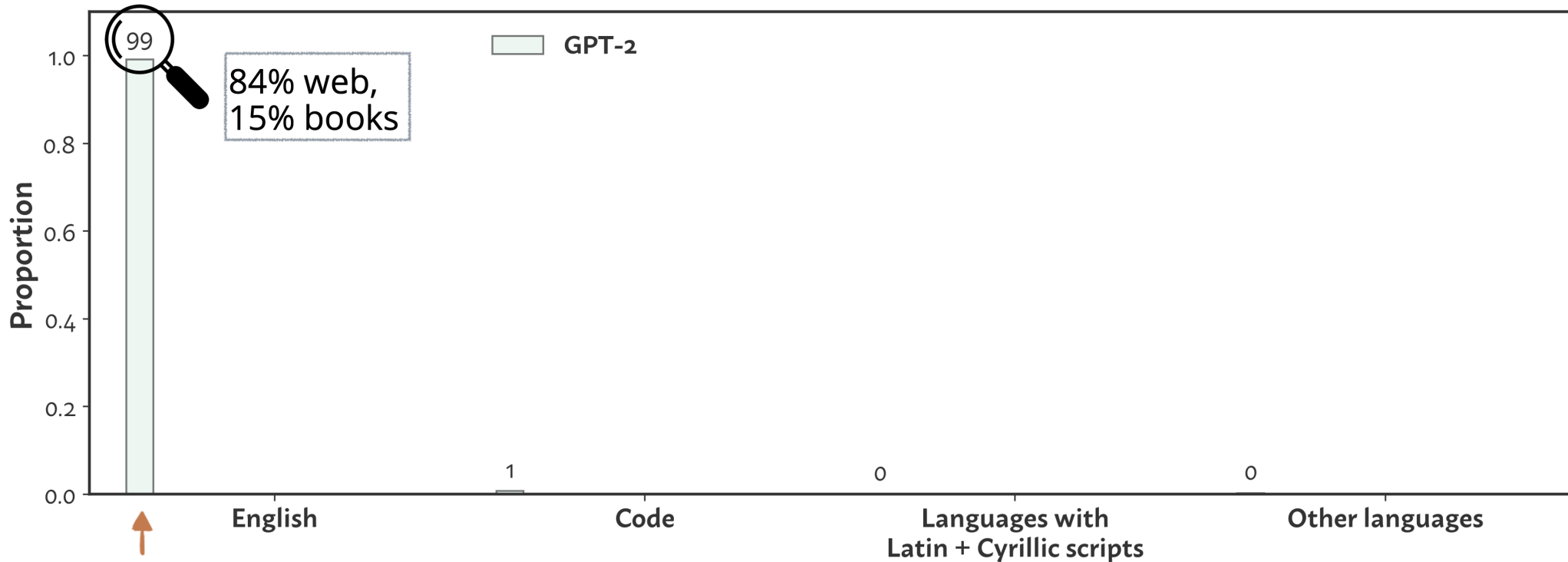
Total set of 116 categories: 111 languages, code, and 4 En domains.

Split "English" into 4 En domains: web, Wikipedia, ArXiv, books.

Combine programming languages into 1 code domain.

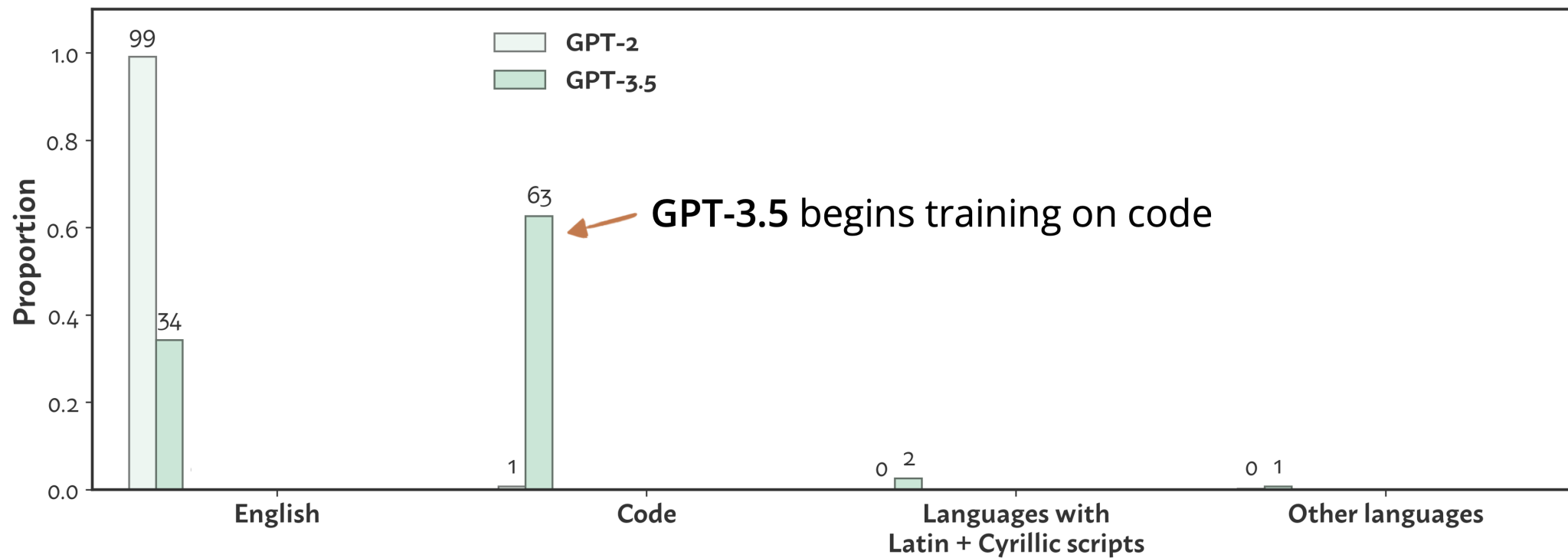
We study: GPT-2, GPT-3.5, GPT-4o, Llama, Llama 3, Mistral, Mistral-Nemo, GPT-NeoX, Gemma, Claude, Command R, ...

Our Inference for LLM Tokenizers

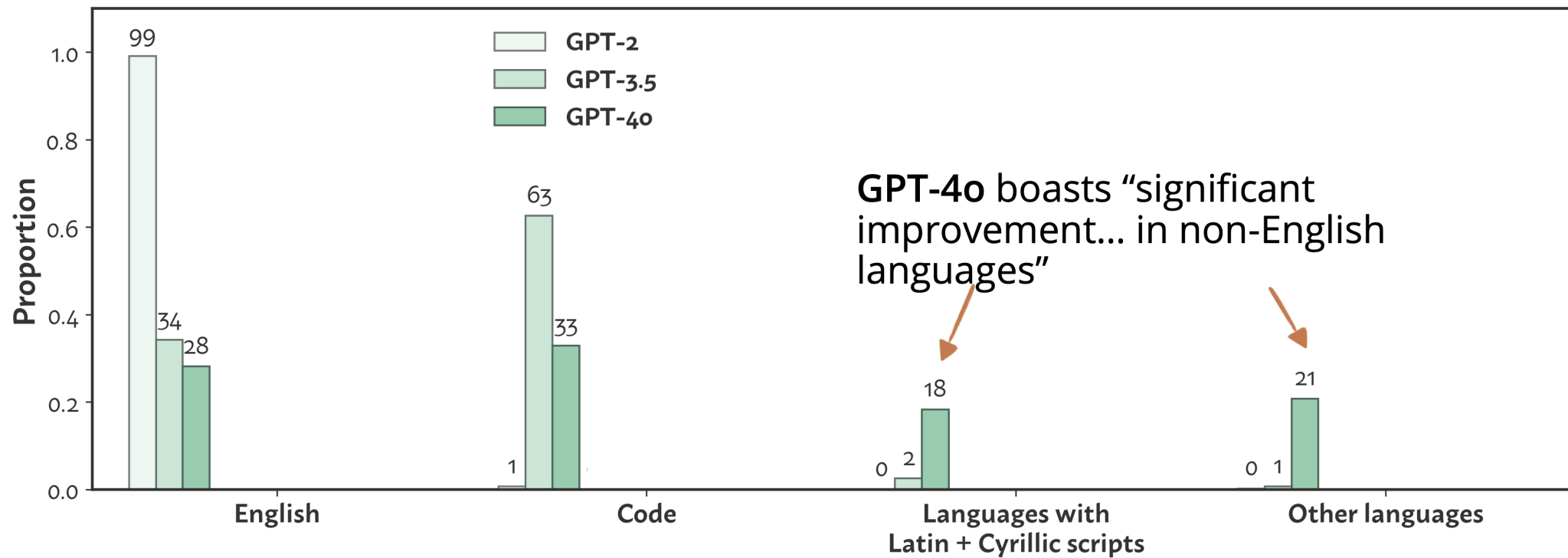


For **GPT-2**, "a filter was used to produce an English only dataset"

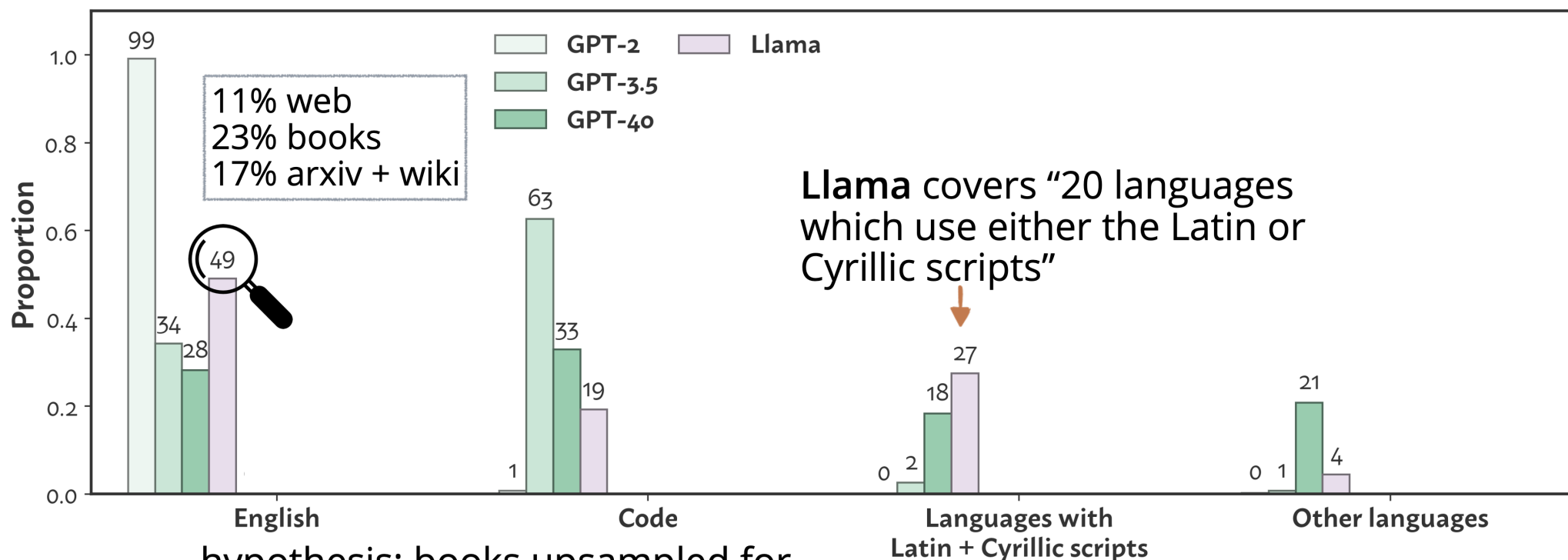
Our Inference for LLM Tokenizers



Our Inference for LLM Tokenizers

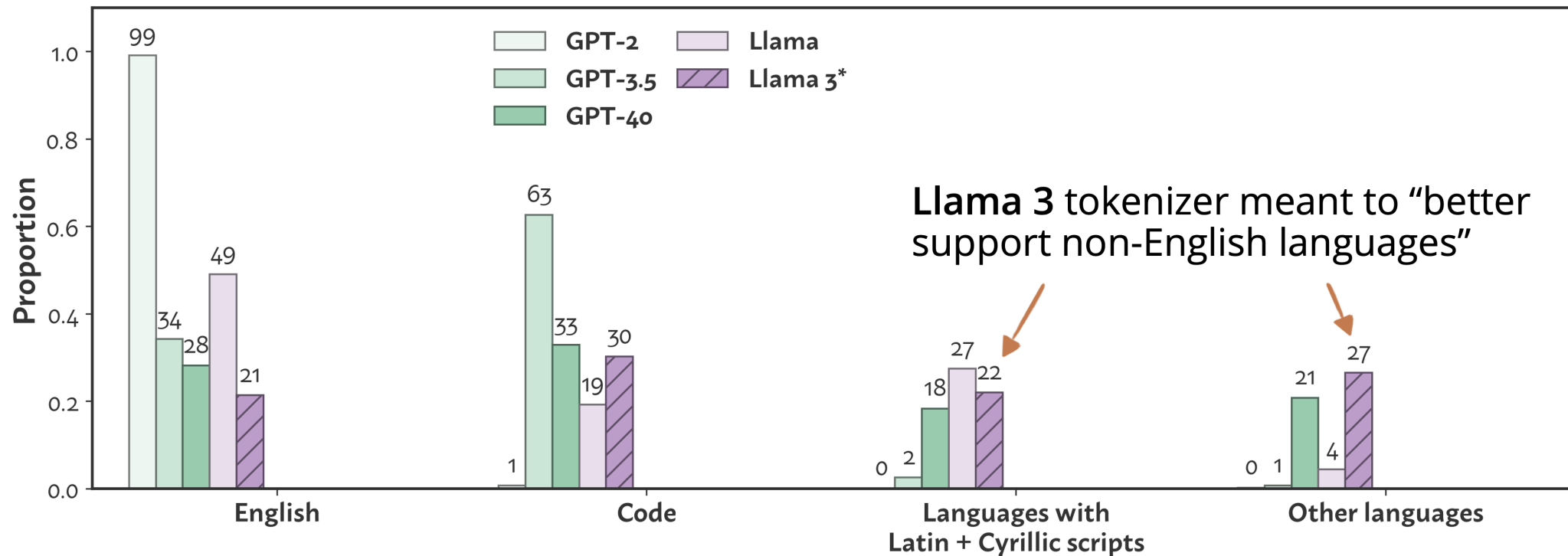


Our Inference for LLM Tokenizers



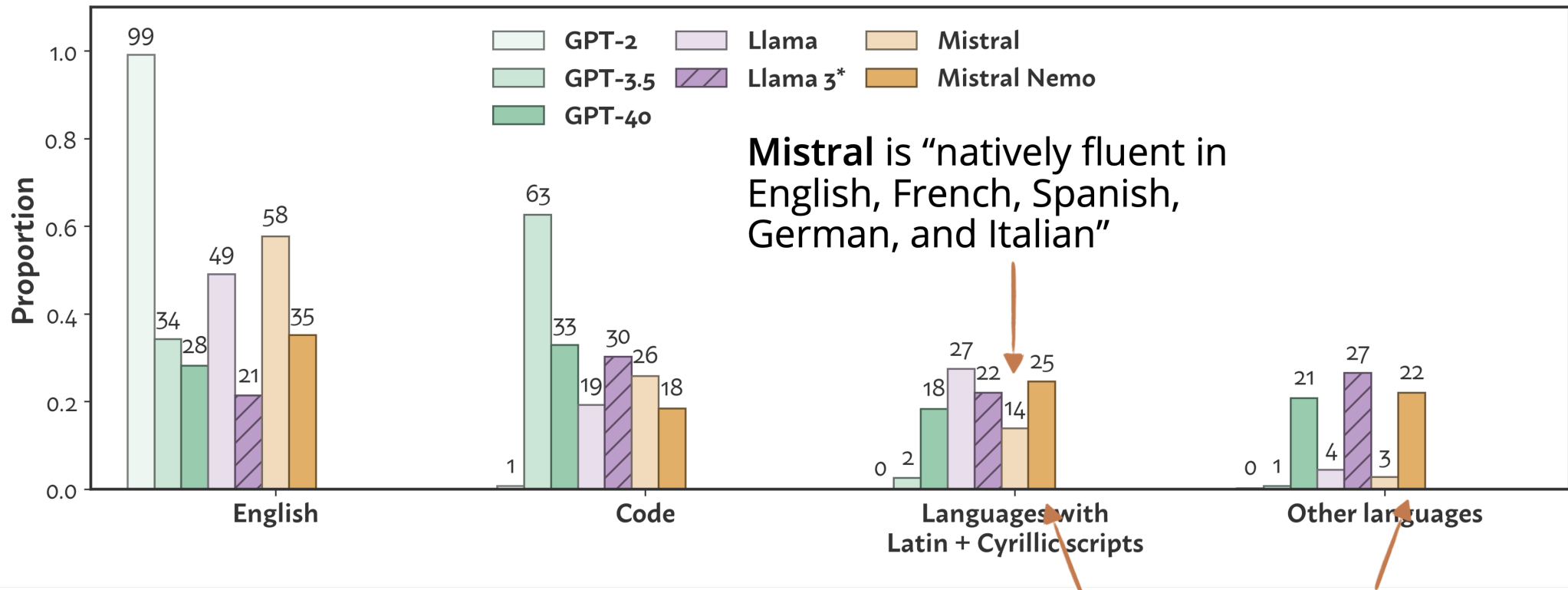
hypothesis: books upsampled for tokenizer training because it uses a more standard vocabulary than web?

Our Inference for LLM Tokenizers



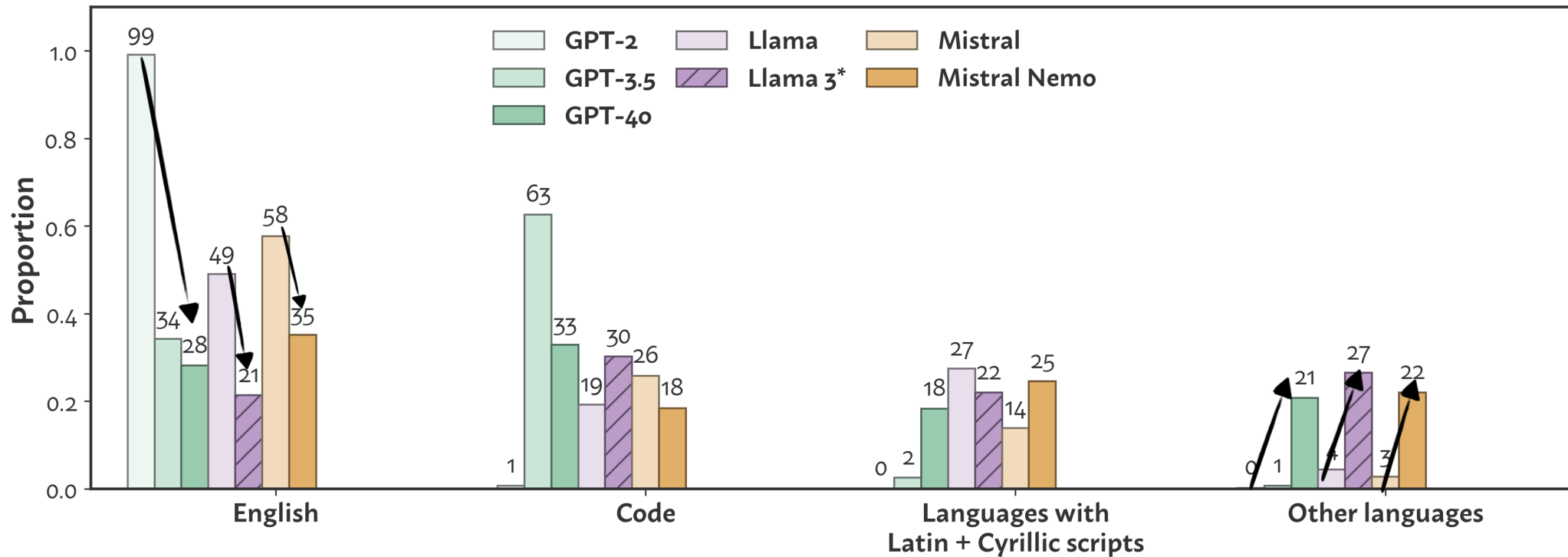
*Llama 3 extends GPT-3.5's tokenizer by 28K additional merges, so we apply the attack to those new merges

Our Inference for LLM Tokenizers



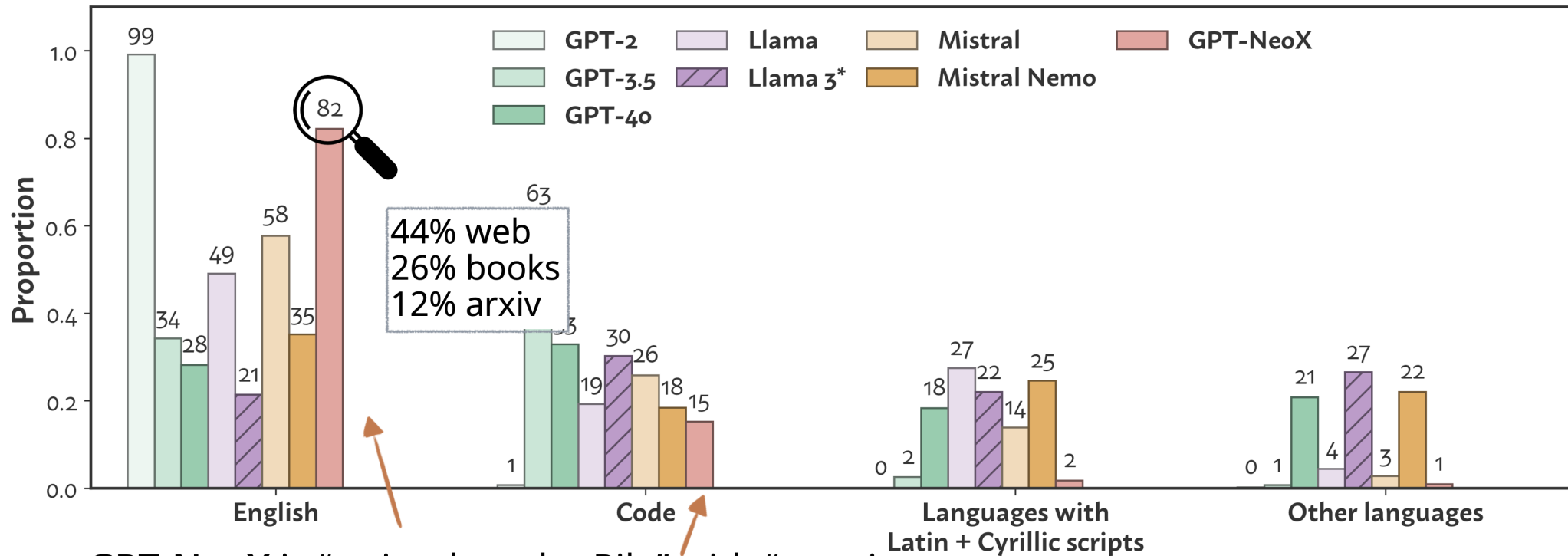
Mistral Nemo is “designed for global, multilingual applications,” “bringing frontier AI models to... all languages”

Our Inference for LLM Tokenizers



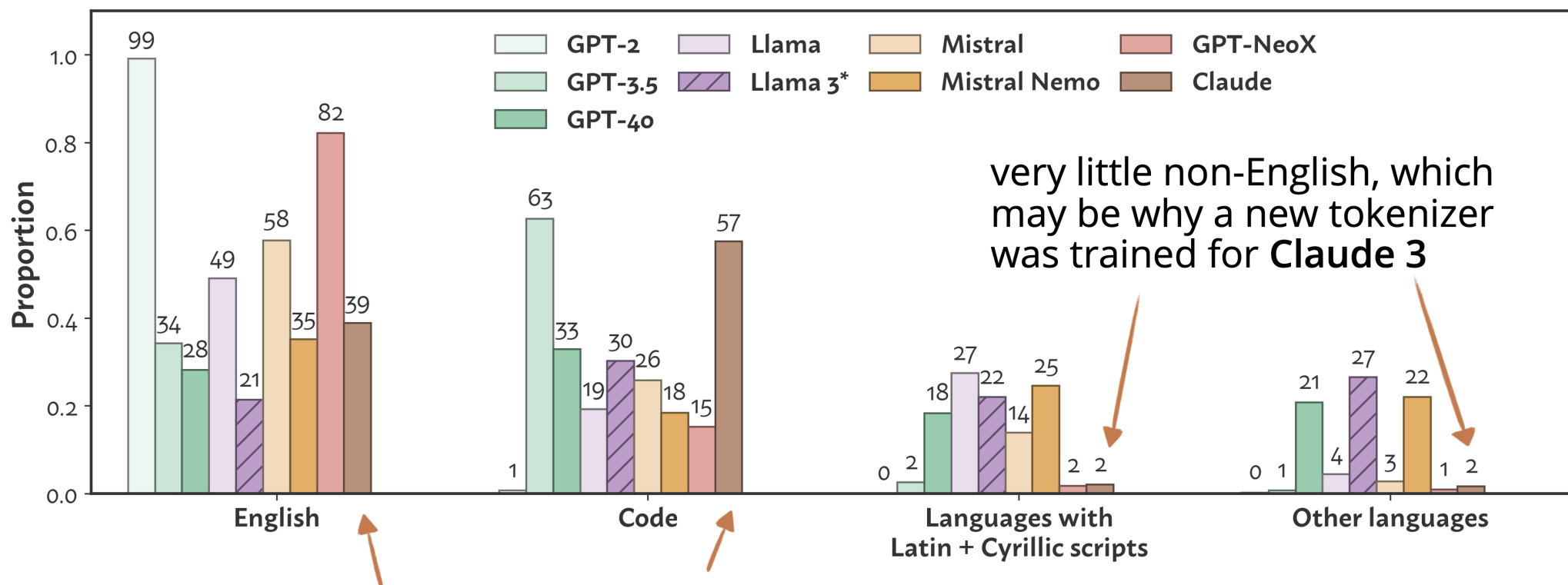
Trend: newer generations of models are more multilingual

Our Inference for LLM Tokenizers

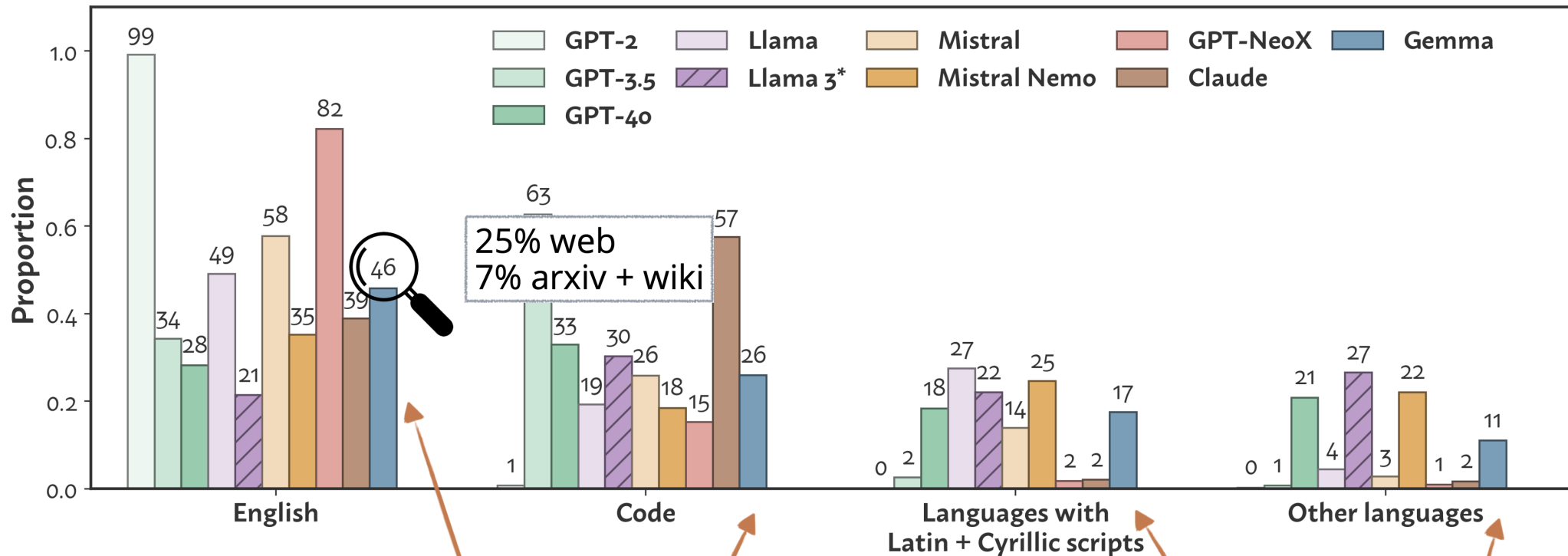


GPT-NeoX is “trained on the Pile” with “certain components... upsampled” — our findings are quite consistent but suggest books were upsampled

Our Inference for LLM Tokenizers



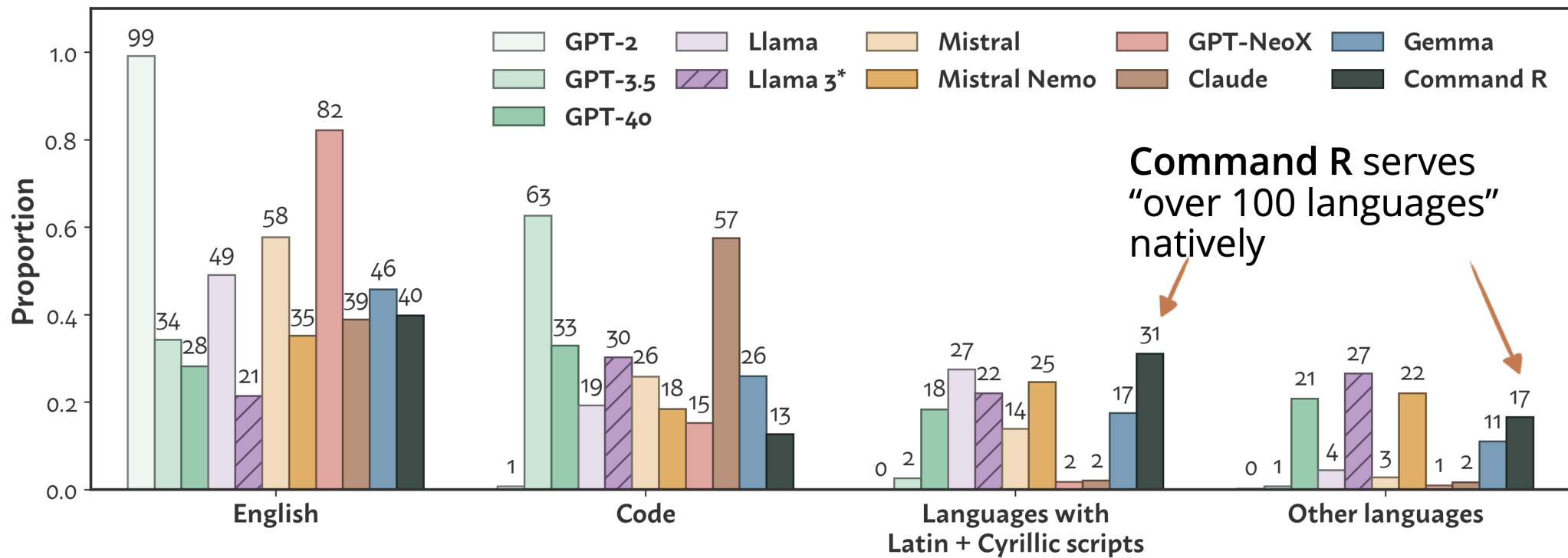
Our Inference for LLM Tokenizers



Gemma trained on “primarily-English data from web documents, mathematics, and code”

Gemma tokenizer is huge (256K tokens), likely to support non-English languages!

Our Inference for LLM Tokenizers



References

- **“SuperBPE: Space Travel for Language Models”**, Alisa Liu, Jonathan Hayase, Valentin Hofmann, Sewoong Oh, Noah A. Smith, Yejin Choi, <https://arxiv.org/pdf/2503.13423>,
- **“Data Mixture Inference Attack: BPE Tokenizers Reveal Training Data Compositions”**, Jonathan Hayase, Alisa Liu, Yejin Choi, Sewoong Oh, Noah A. Smith, *NeurIPS 2024*

Sources

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 - <https://github.com/openai/tiktoken>
- Failure modes of tokenizers
 - <https://seantrott.substack.com/p/tokenization-in-large-language-models>