

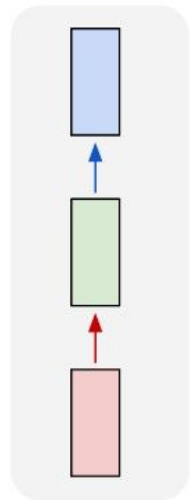
# Lecture 10: RNNs, LSTMs

# Administrative

- Assignment 2 grades will be released soon
- Quiz 2 grades has been released
- Assignment 3 is released (dropout, batchnorm, CNNs)
- Proposals due tonight

# “Vanilla” Neural Network

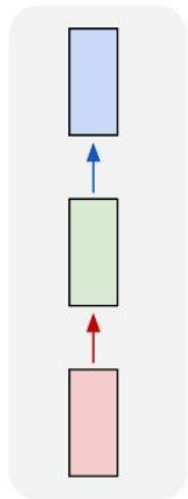
one to one



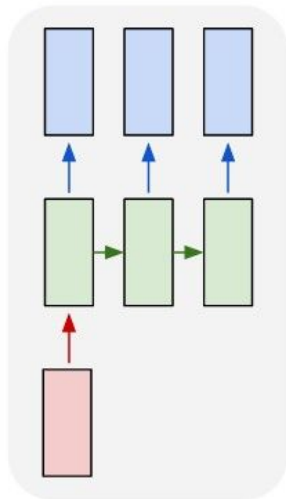
**Vanilla Neural Networks**

# Recurrent Neural Networks: Process Sequences

one to one



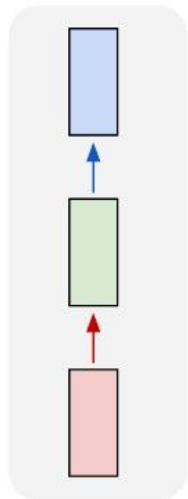
one to many



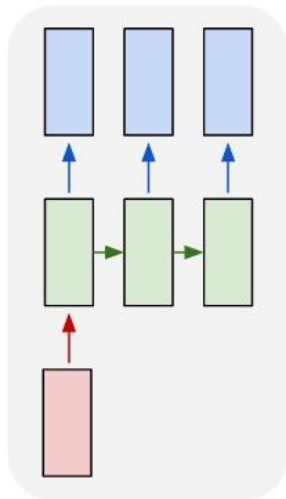
↖ e.g. **Image Captioning**  
image -> sequence of words

# Recurrent Neural Networks: Process Sequences

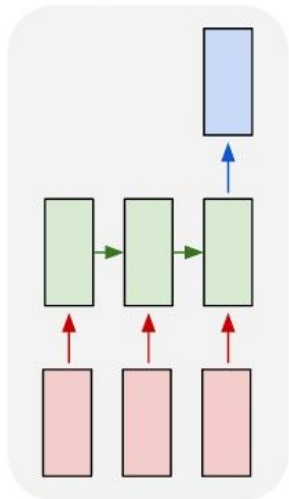
one to one



one to many



many to one

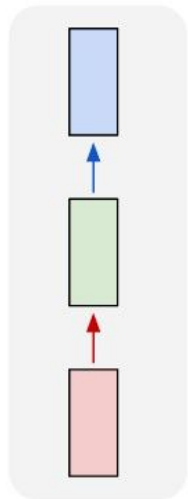


e.g. **action prediction, sentiment classification**

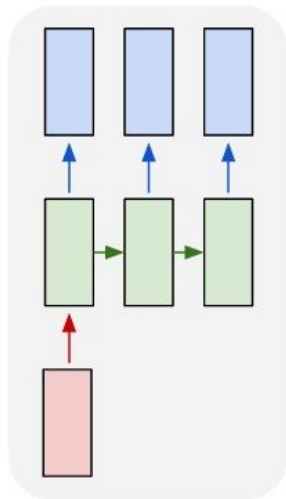
sequence of video frames -> action class

# Recurrent Neural Networks: Process Sequences

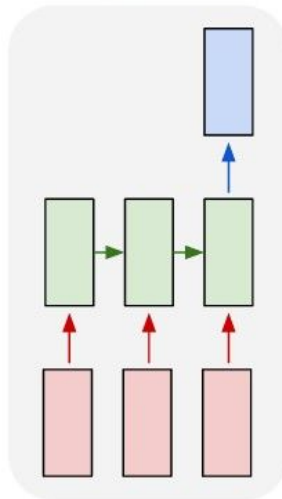
one to one



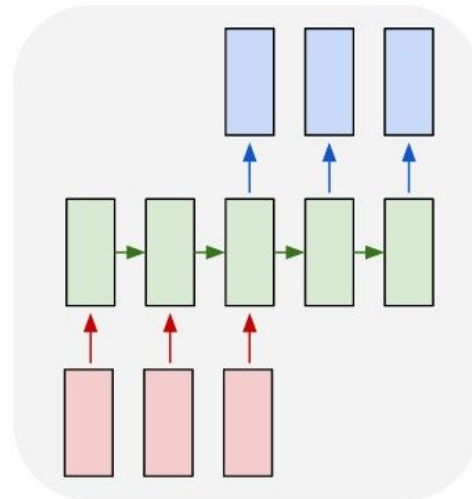
one to many



many to one



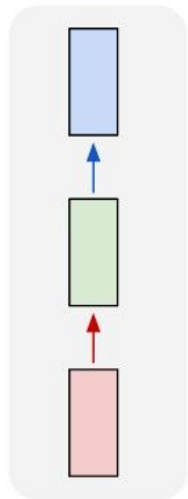
many to many



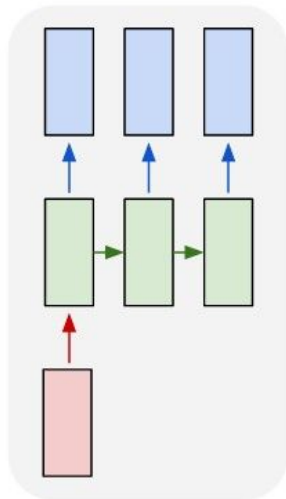
E.g. **Video Captioning**  
Sequence of video frames ->  
caption

# Recurrent Neural Networks: Process Sequences

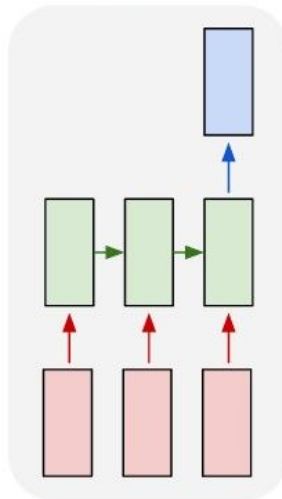
one to one



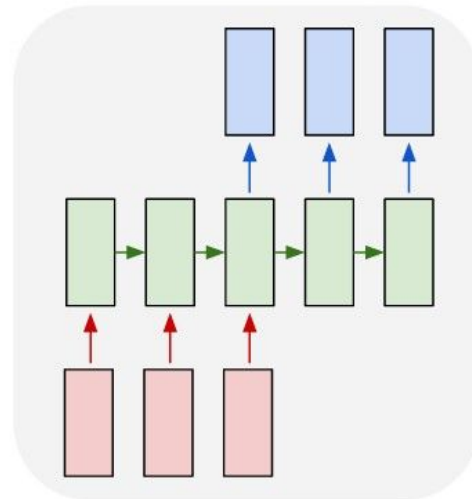
one to many



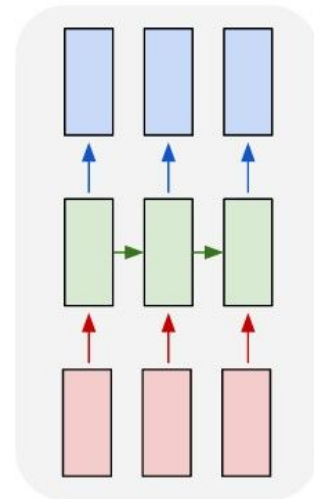
many to one



many to many



many to many



e.g. **Video classification on frame level**



# So far: Representing words as discrete symbols

In traditional NLP, we regard words as discrete symbols:

*hotel, conference, motel* – each has its own symbol.

This is a **localist representation**

Such symbols for words can be represented by **one-hot vectors**:

motel = [0 0 0 0 0 0 0 0 0 0 1 0 0 0 0]

hotel = [0 0 0 0 0 0 0 1 0 0 0 0 0 0 0]

Vector dimension = number of words in vocabulary (e.g., 500,000+)



# So far: Representing words as dense vectors

We will build a **dense vector** for each word,

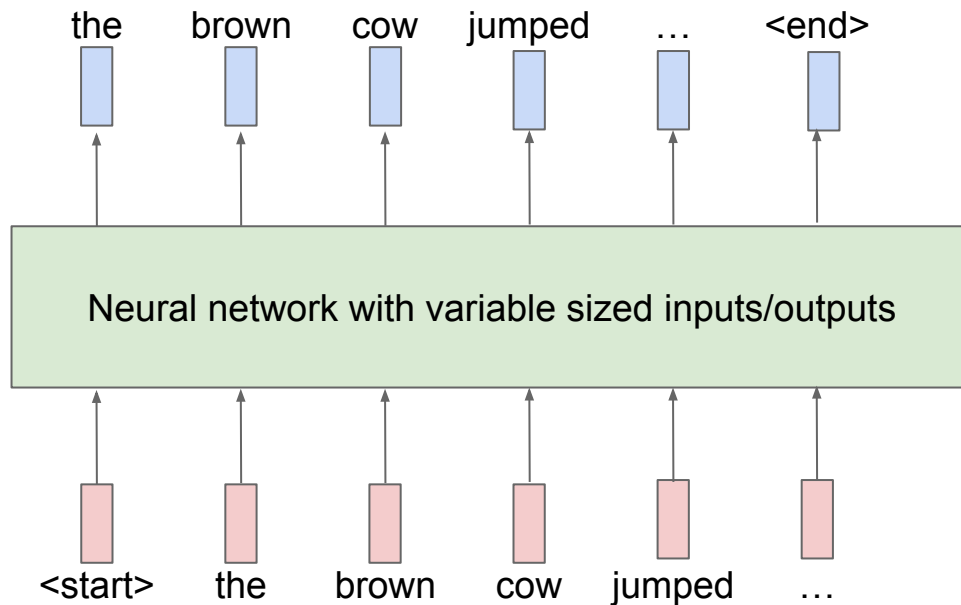
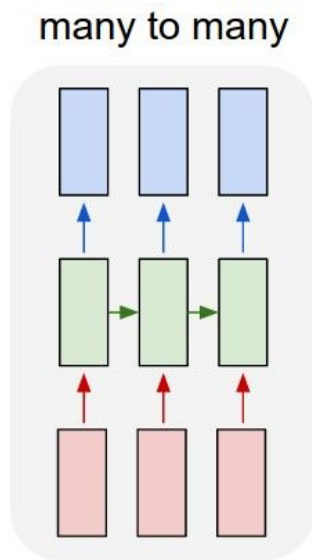
- chosen so that it is similar to vectors of words that appear in similar contexts: e.g. **jacket / coat / sweater**.
- measuring similarity as the vector dot (scalar) product.
- Word vectors are also called (word) **embeddings** or (neural) **word representations**

$$\text{Jacket} = \begin{bmatrix} 0.286 \\ 0.792 \\ -0.177 \\ -0.107 \\ 0.109 \\ -0.542 \\ 0.349 \\ 0.271 \end{bmatrix}$$

# Now let's talk about how we can model language

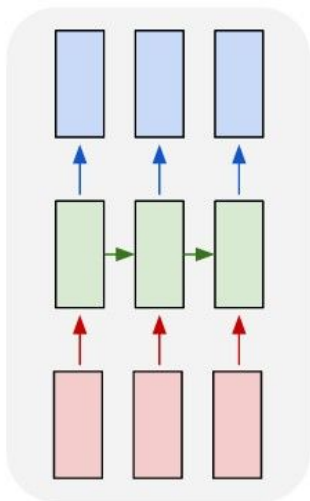
Word representations  
can be V-dimensional  
**one-hot** vectors  
Or d-dimensional  
**dense** vectors

Outputs are  
classification (softmax)  
over V-dimensions

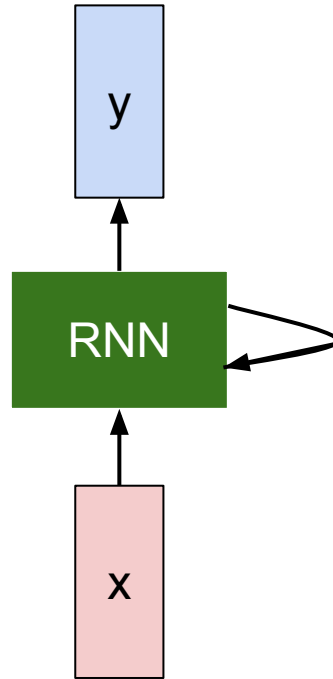


# Now let's talk about how we can model language

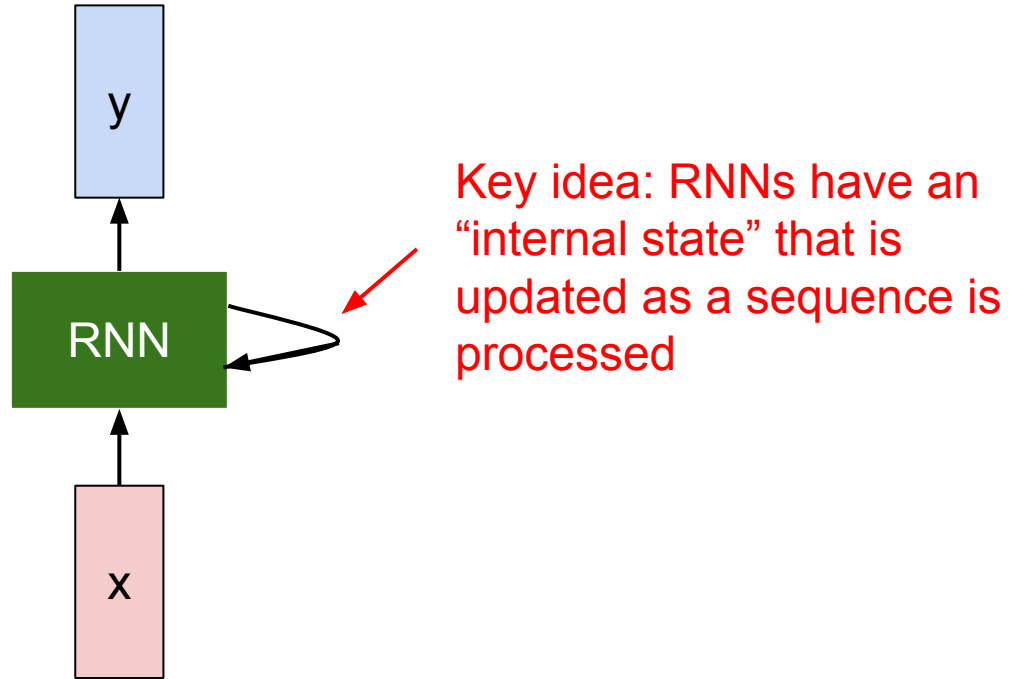
many to many



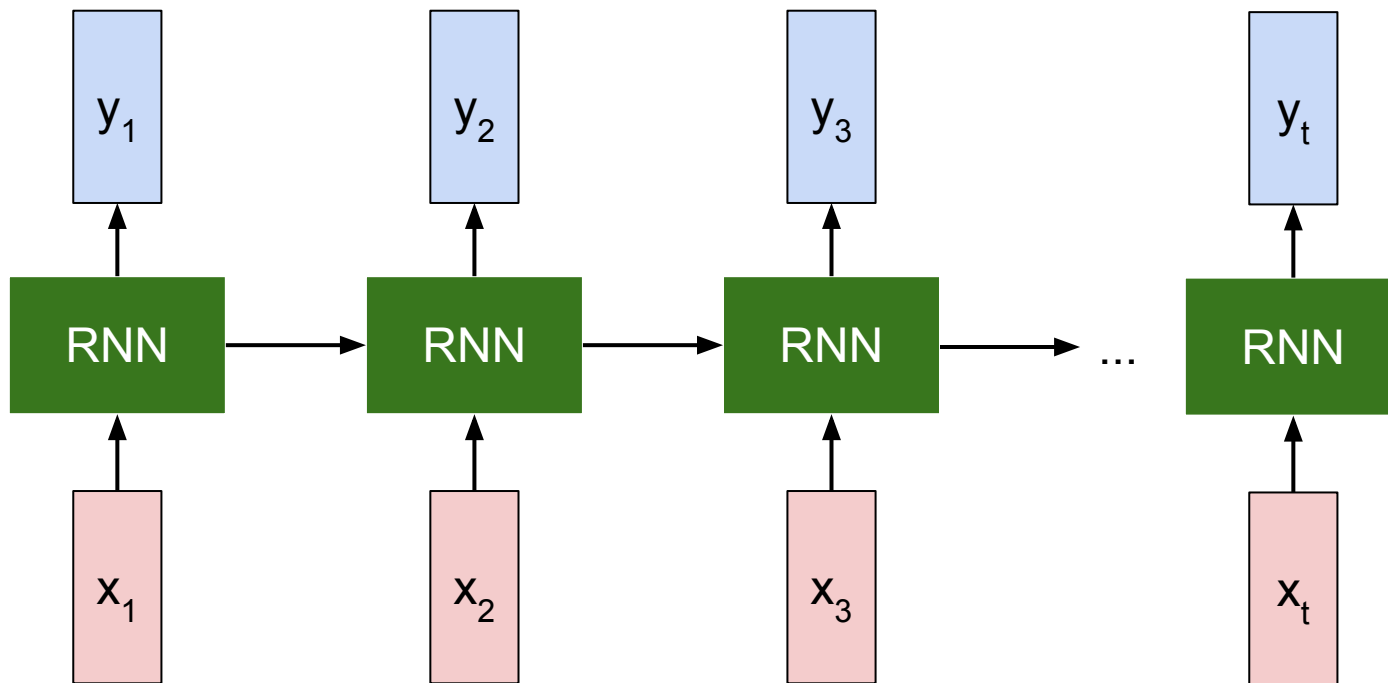
# Recurrent Neural Network



# Recurrent Neural Network



# Unrolled RNN

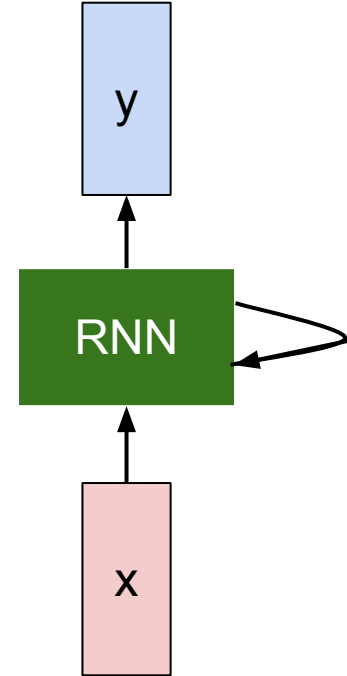


# RNN hidden state update

We can process a sequence of vectors  $\mathbf{x}$  by applying a **recurrence formula** at every time step:

$$\boxed{h_t} = \boxed{f_W}(\boxed{h_{t-1}}, \boxed{x_t})$$

new state / some function with parameters  $W$  / old state / input vector at some time step



# RNN output generation

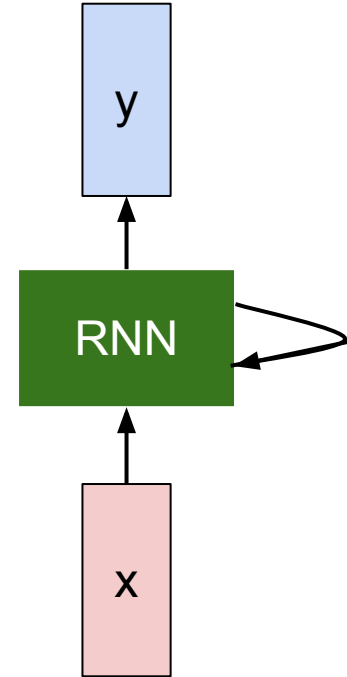
We can process a sequence of vectors  $\mathbf{x}$  by applying a **recurrence formula** at every time step:

$$\boxed{y_t} = \boxed{f_{W_{hy}}}(\boxed{h_t})$$

output

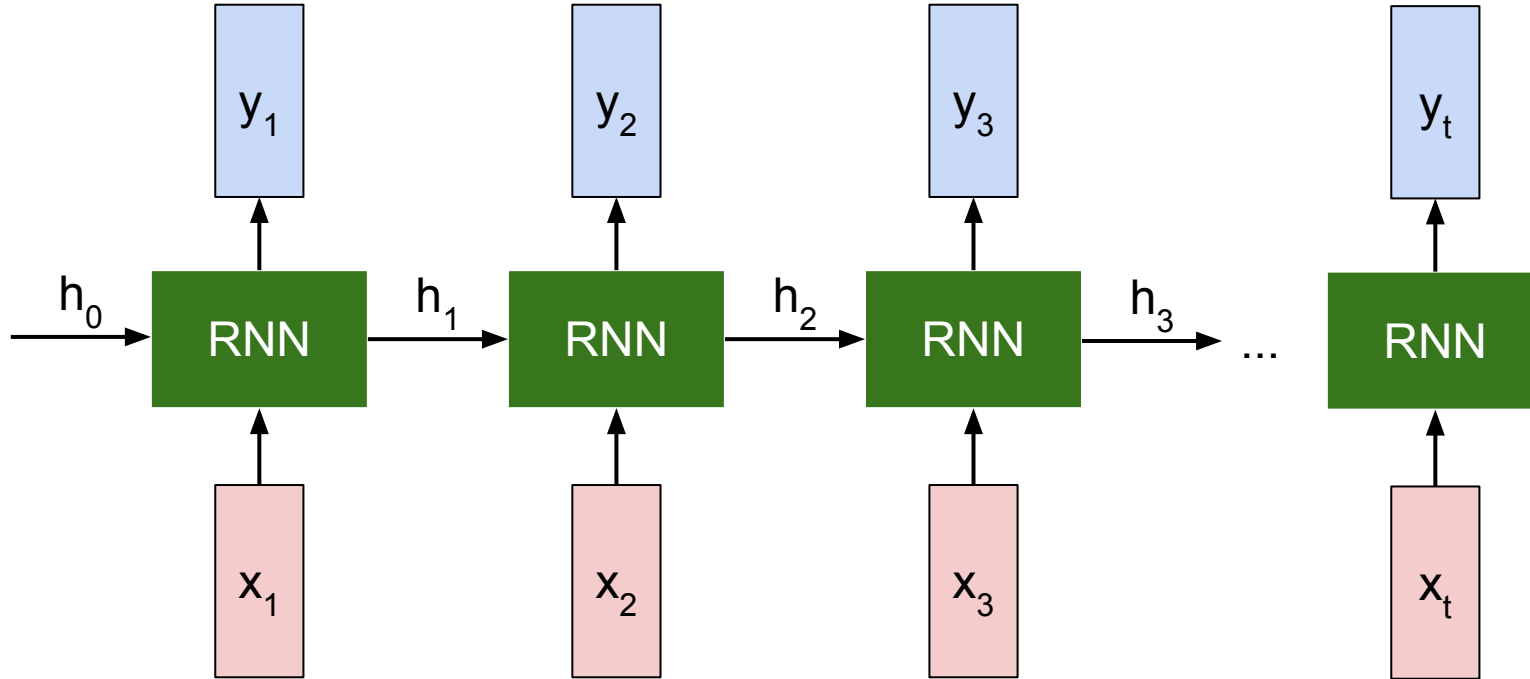
another function with parameters  $W_o$

new state





# Recurrent Neural Network

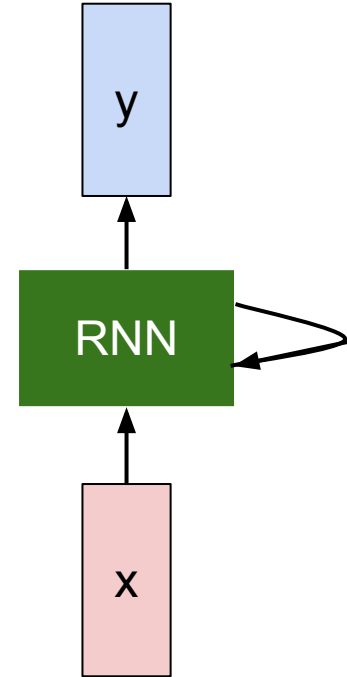


# Recurrent Neural Network

We can process a sequence of vectors  $\mathbf{x}$  by applying a **recurrence formula** at every time step:

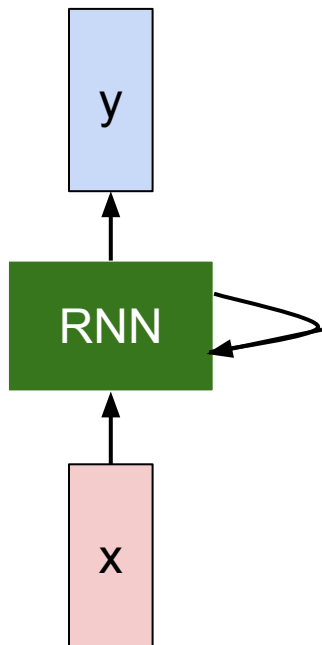
$$h_t = f_W(h_{t-1}, x_t)$$

Notice: the same function and the same set of parameters are used at every time step.



# (Simple) Recurrent Neural Network

The state consists of a single “hidden” vector  $h$ :



$$h_t = f_W(h_{t-1}, x_t)$$

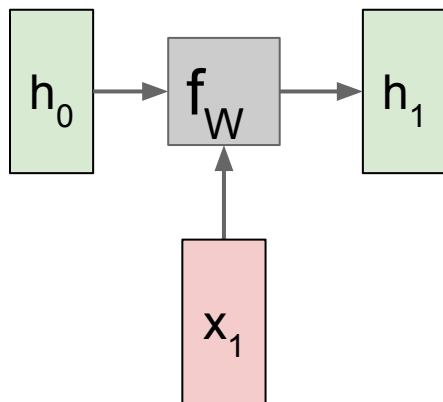


$$h_t = \tanh(W_{hh}h_{t-1} + W_{xh}x_t)$$

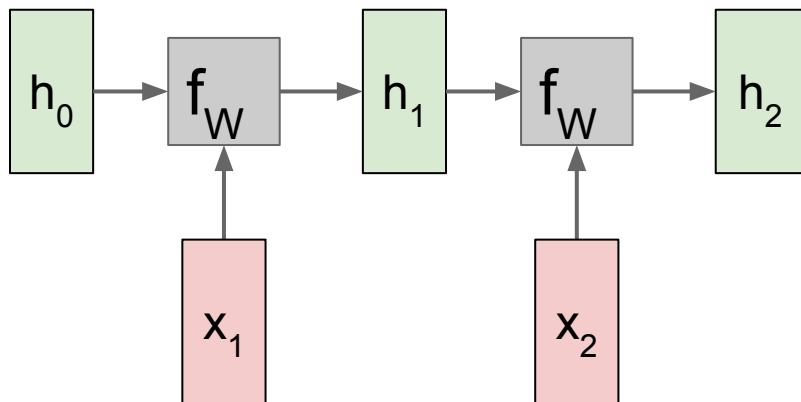
$$y_t = W_{hy}h_t$$

Sometimes called a “Vanilla RNN” or an “Elman RNN” after Prof. Jeffrey Elman

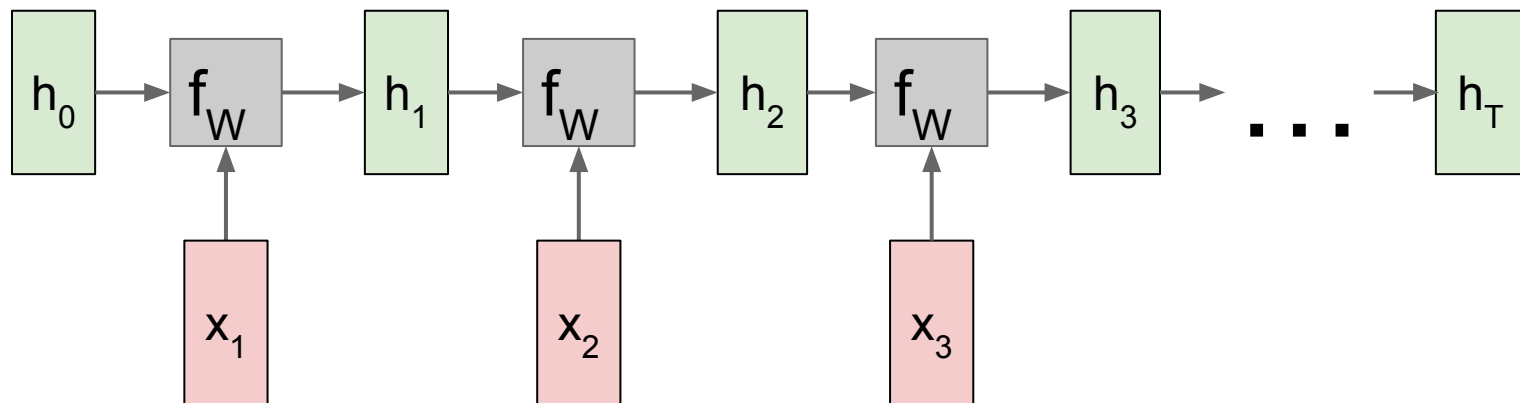
# RNN: Computational Graph



# RNN: Computational Graph

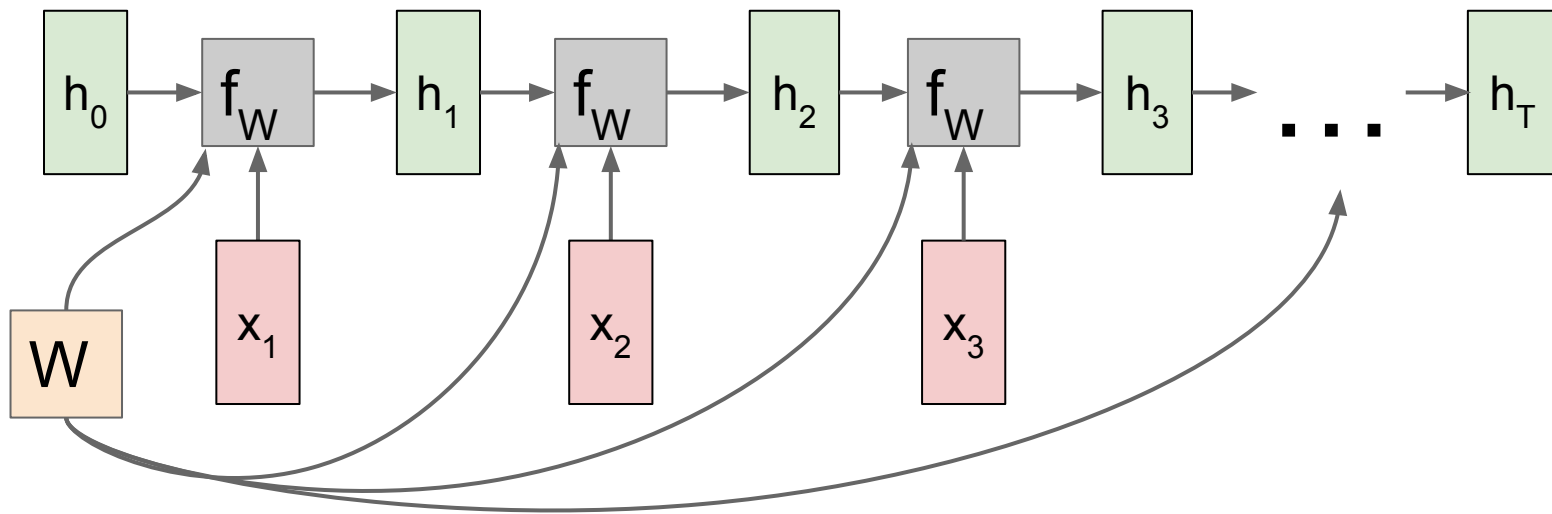


# RNN: Computational Graph

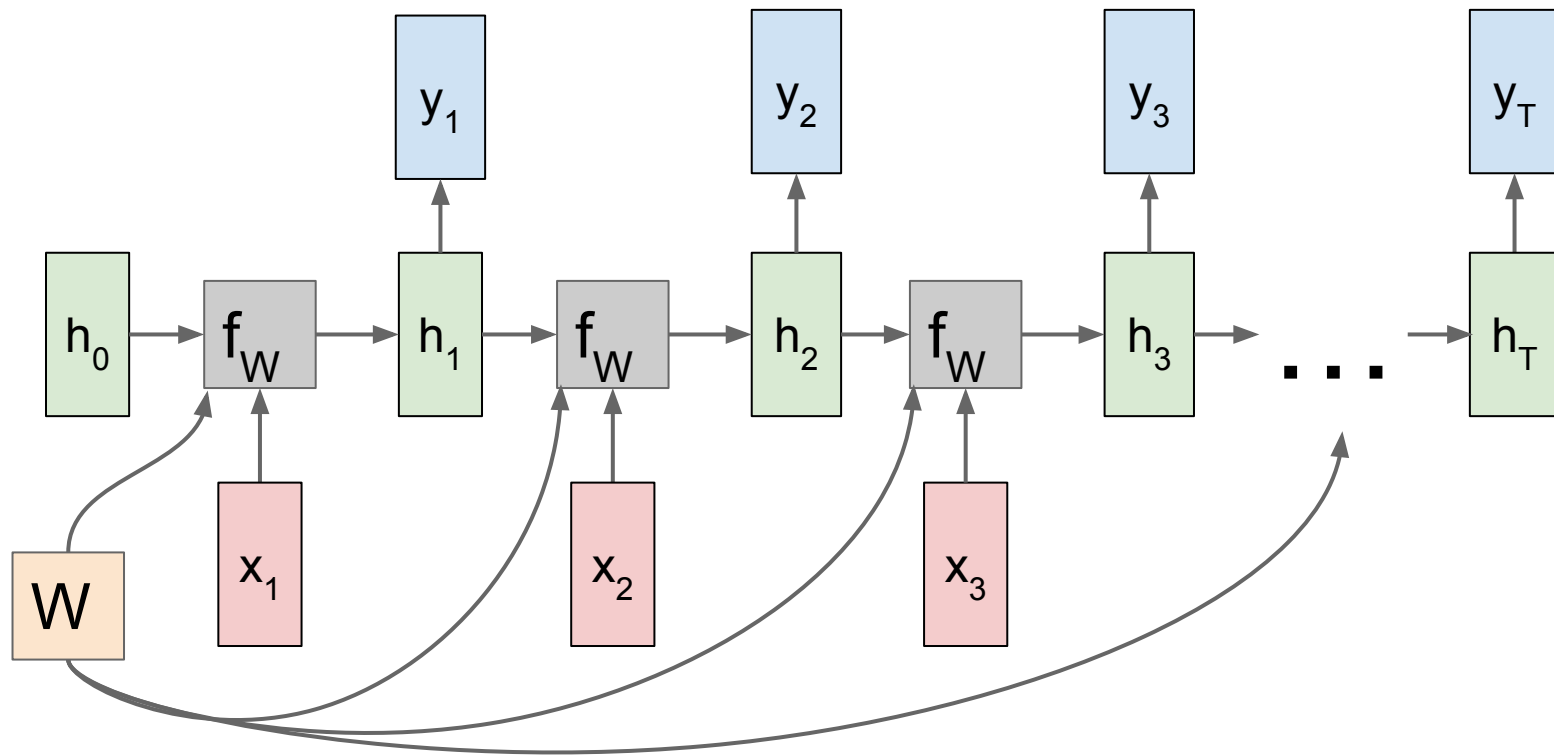


# RNN: Computational Graph

Re-use the same weight matrix at every time-step

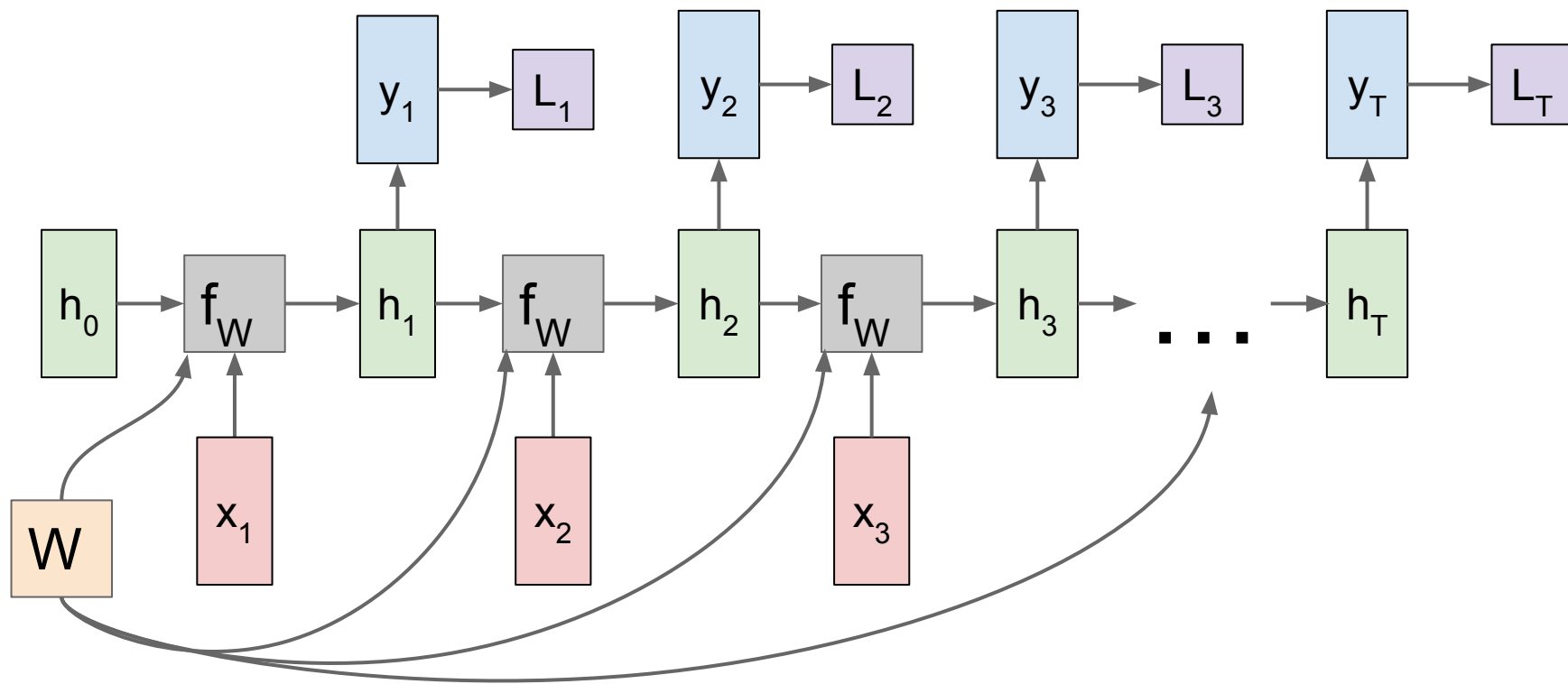


# RNN: Computational Graph: Many to Many

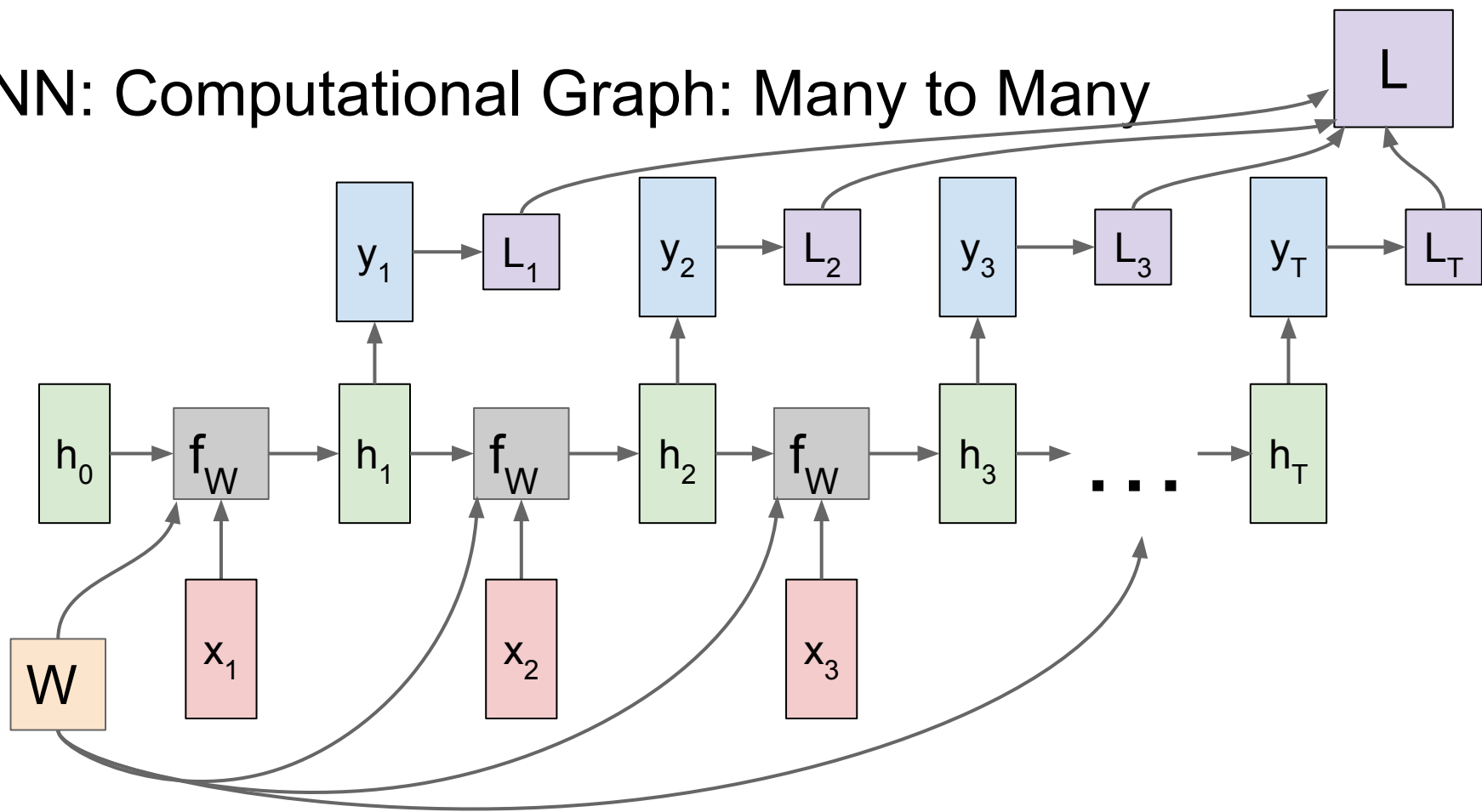




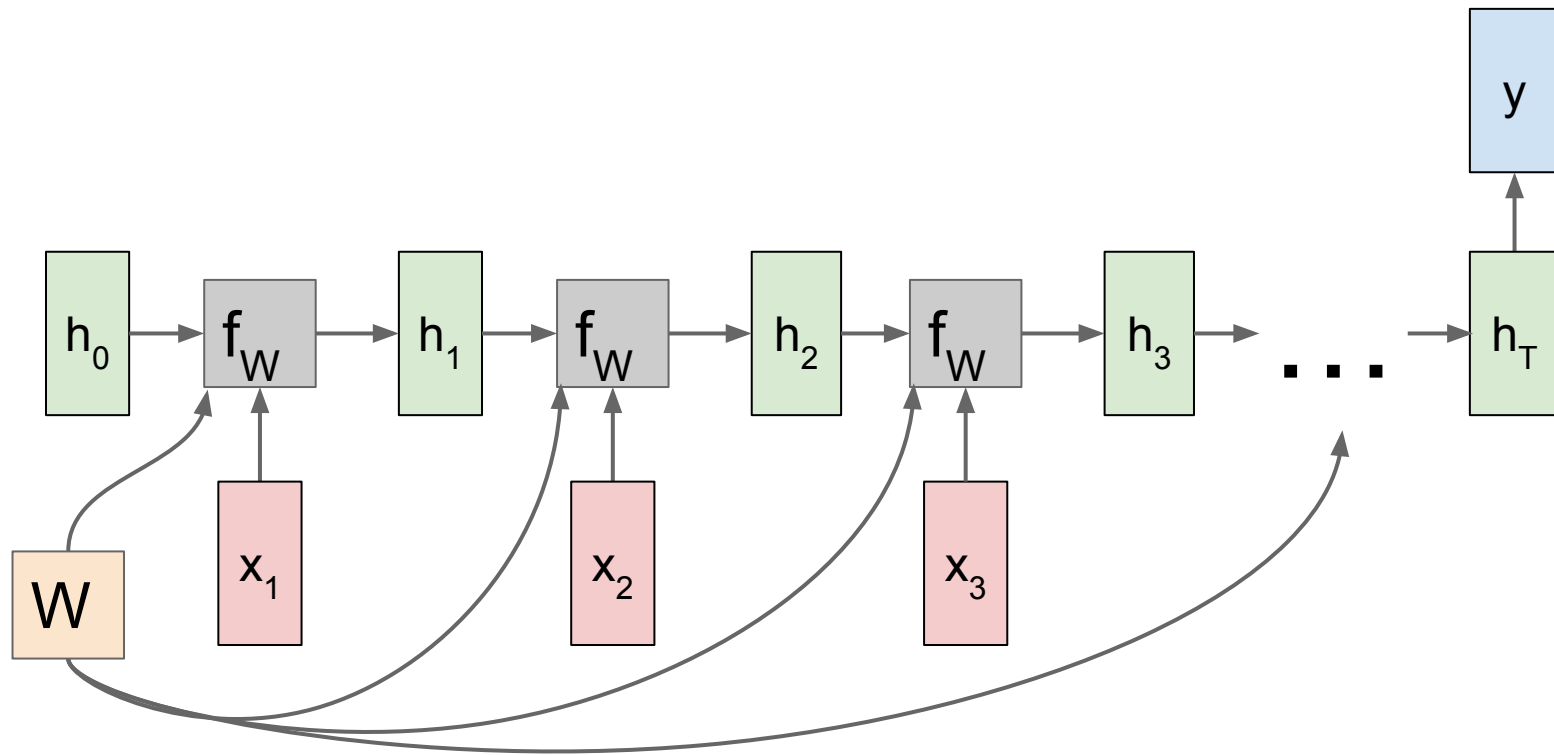
# RNN: Computational Graph: Many to Many



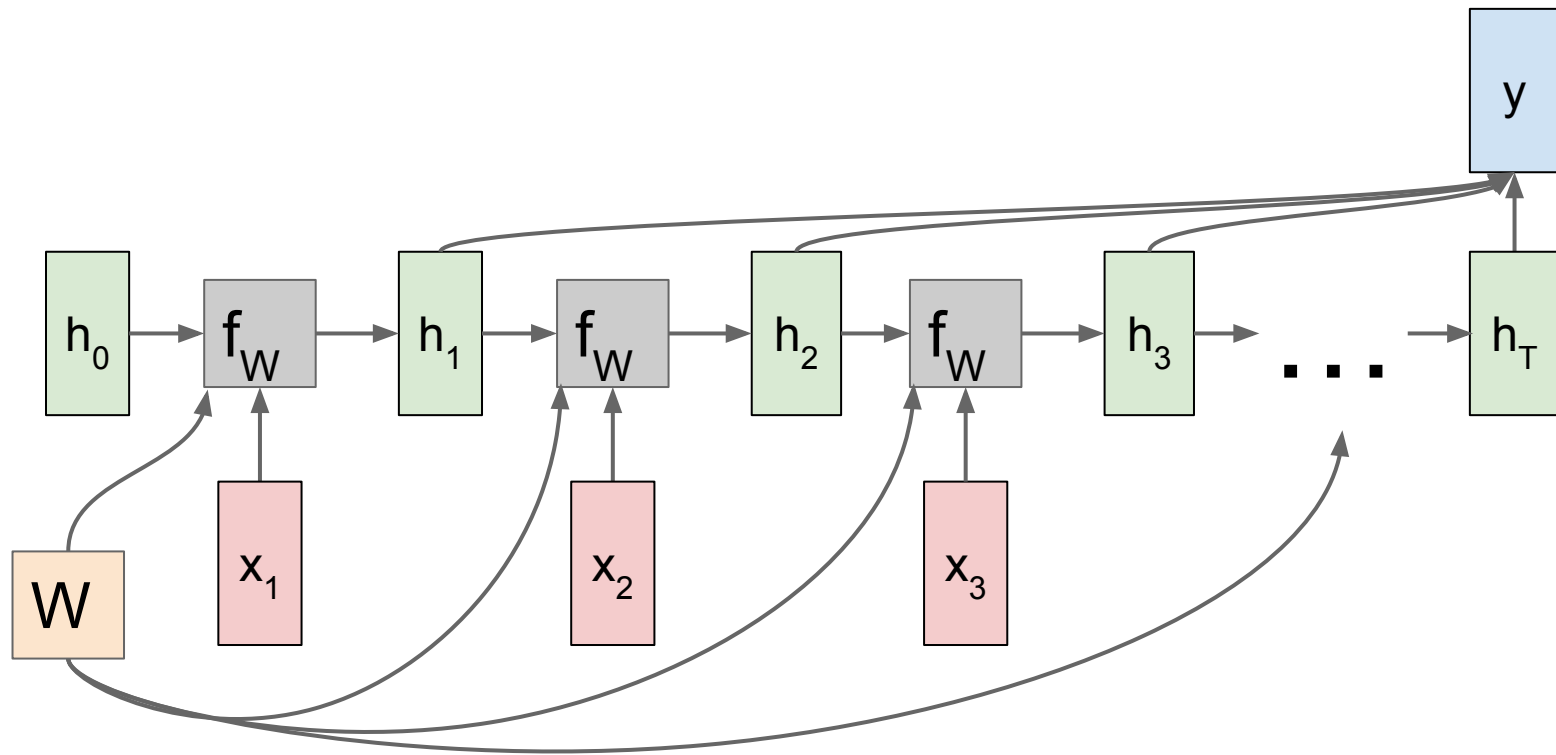
# RNN: Computational Graph: Many to Many



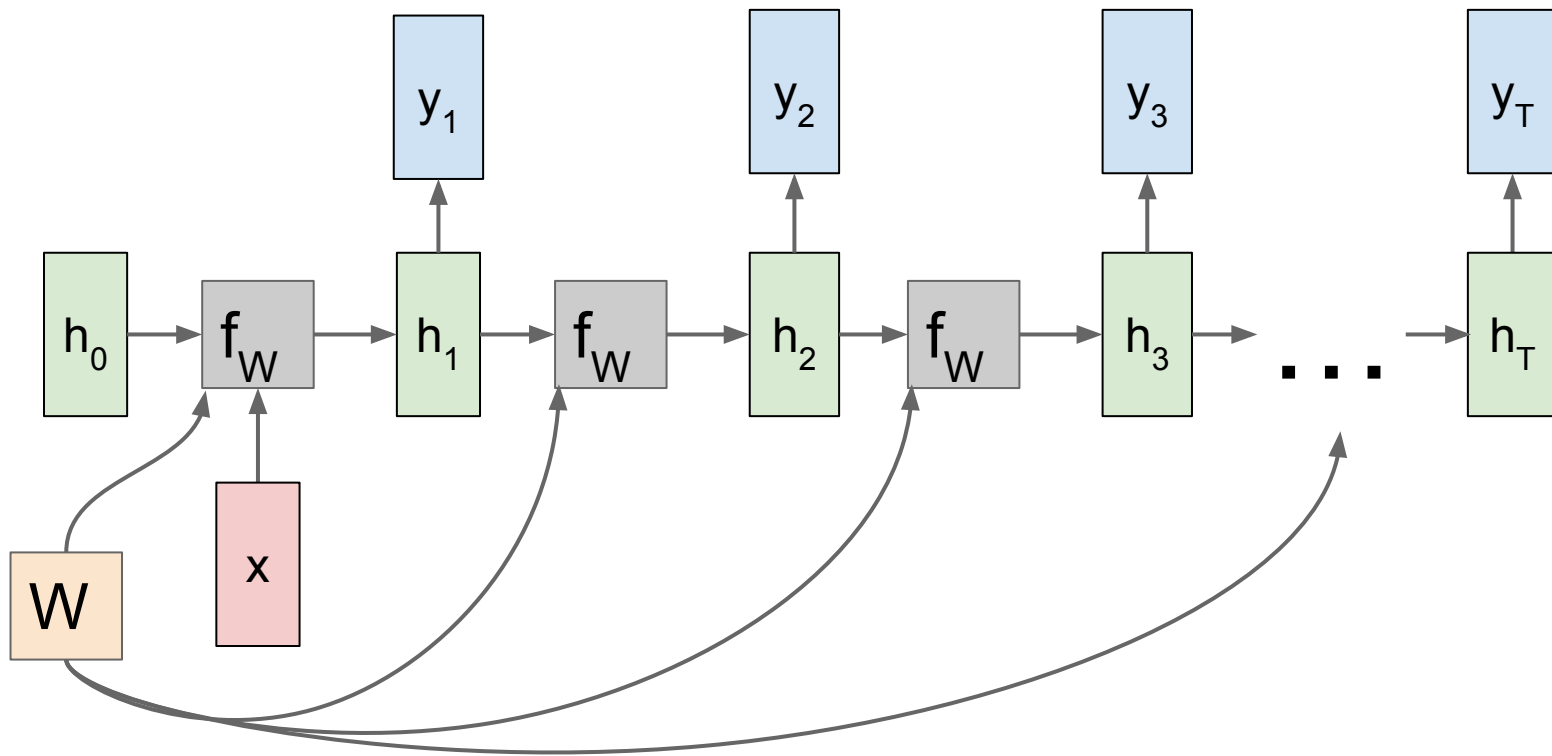
# RNN: Computational Graph: Many to One



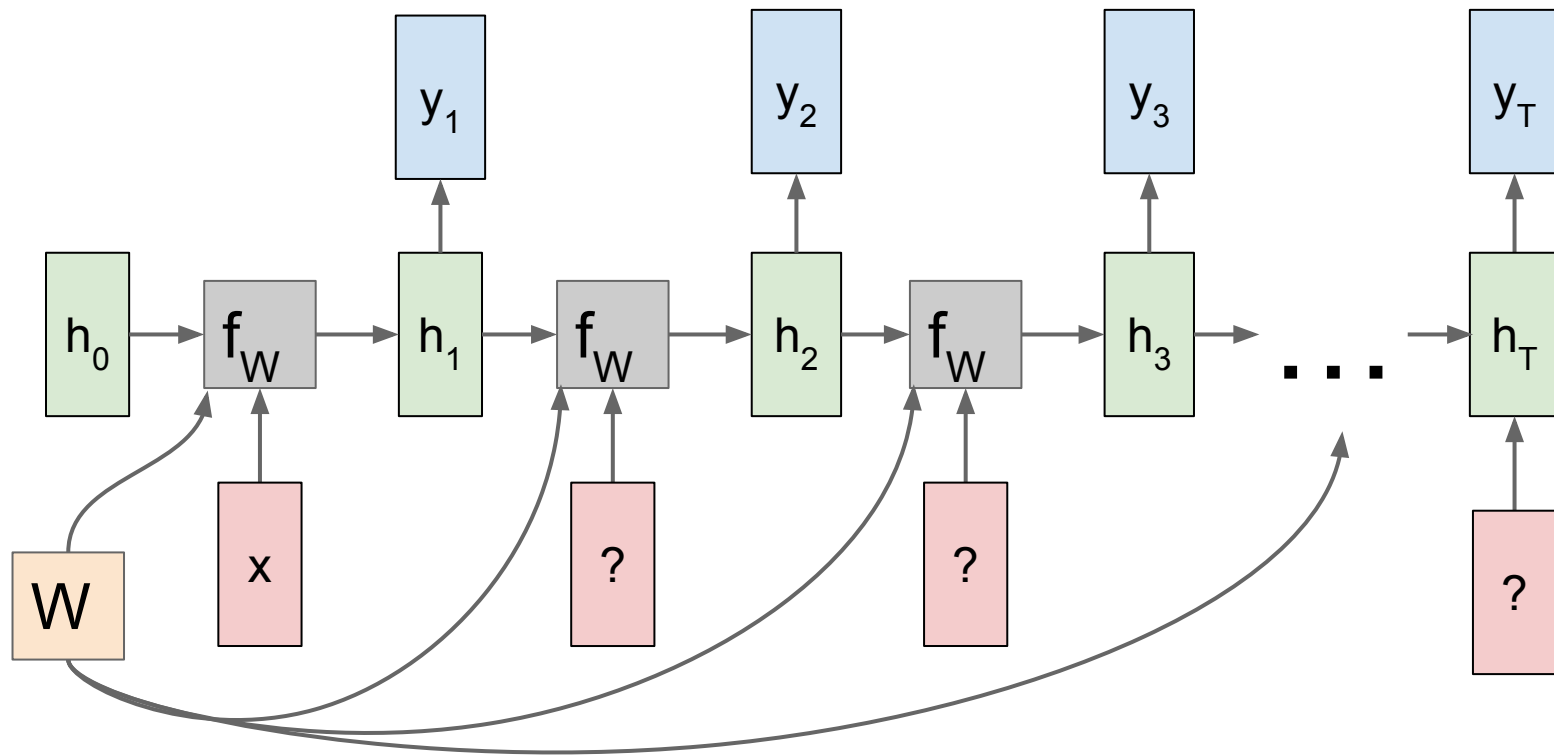
# RNN: Computational Graph: Many to One



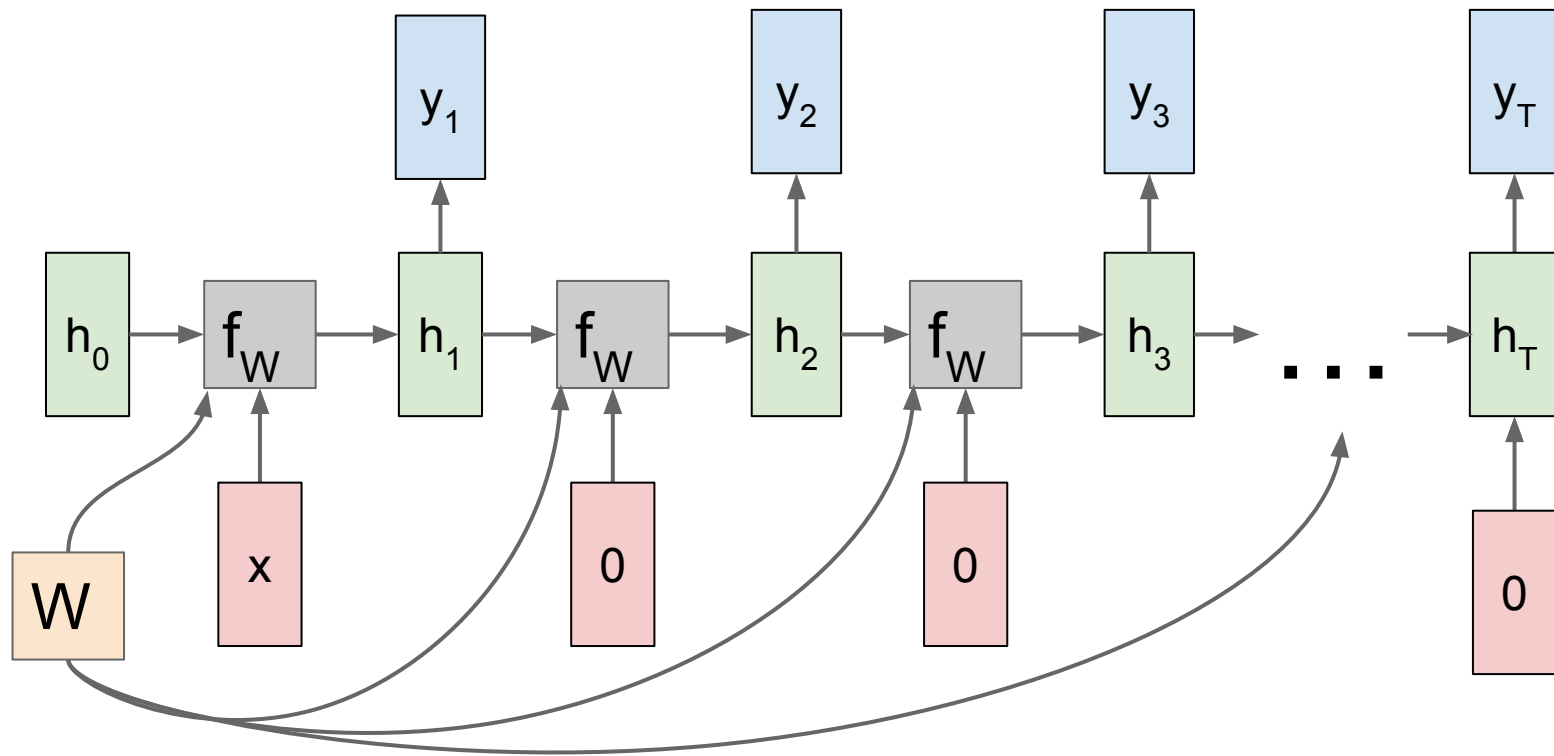
# RNN: Computational Graph: One to Many



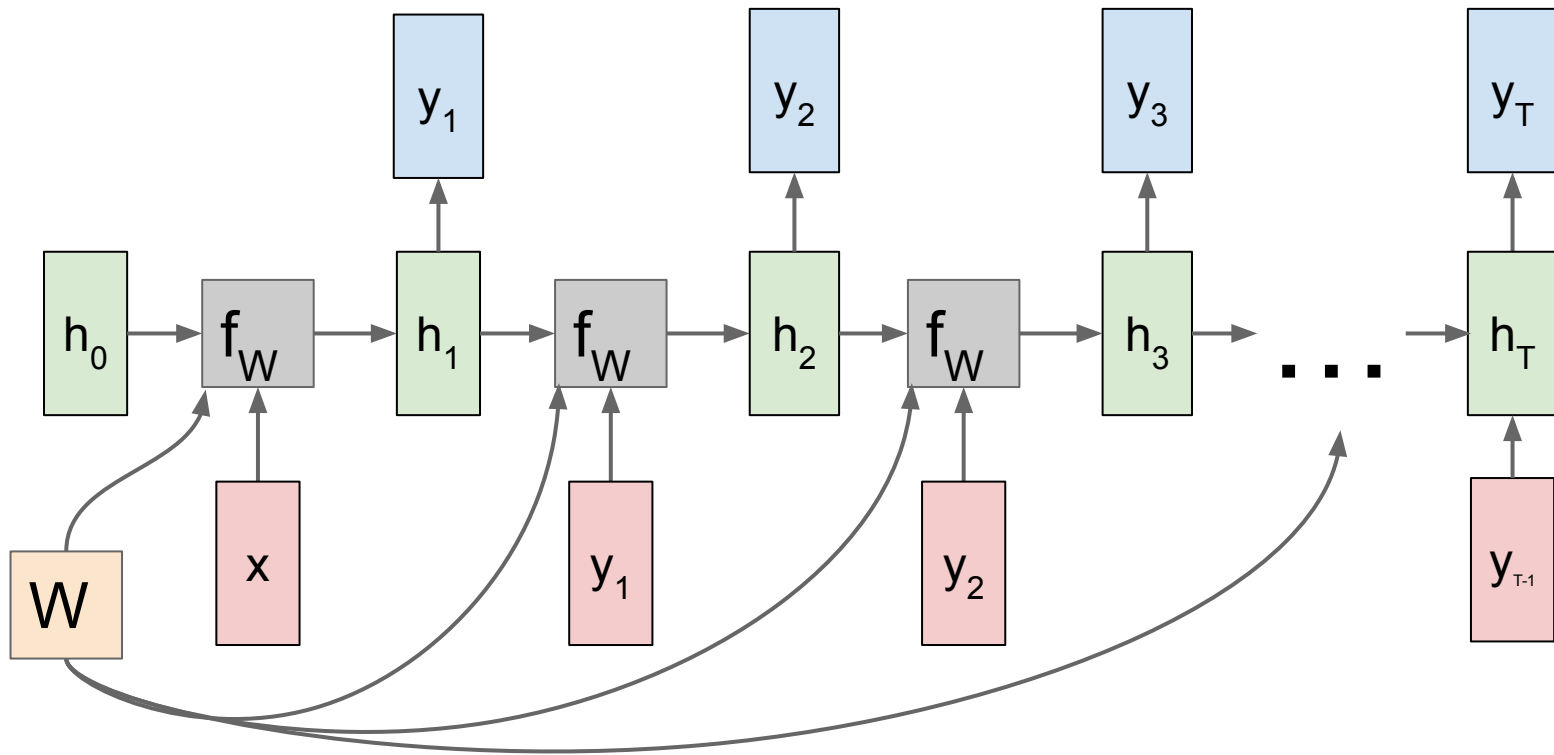
# RNN: Computational Graph: One to Many



# RNN: Computational Graph: One to Many



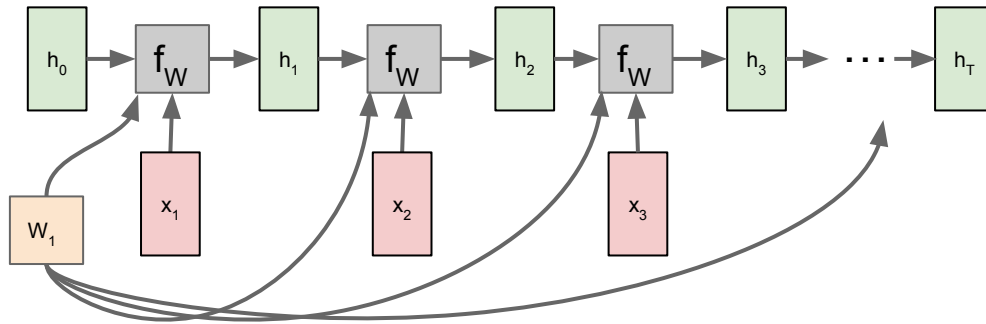
# RNN: Computational Graph: One to Many





# Sequence to Sequence: Many-to-one + one-to-many

**Many to one:** Encode input sequence in a single vector

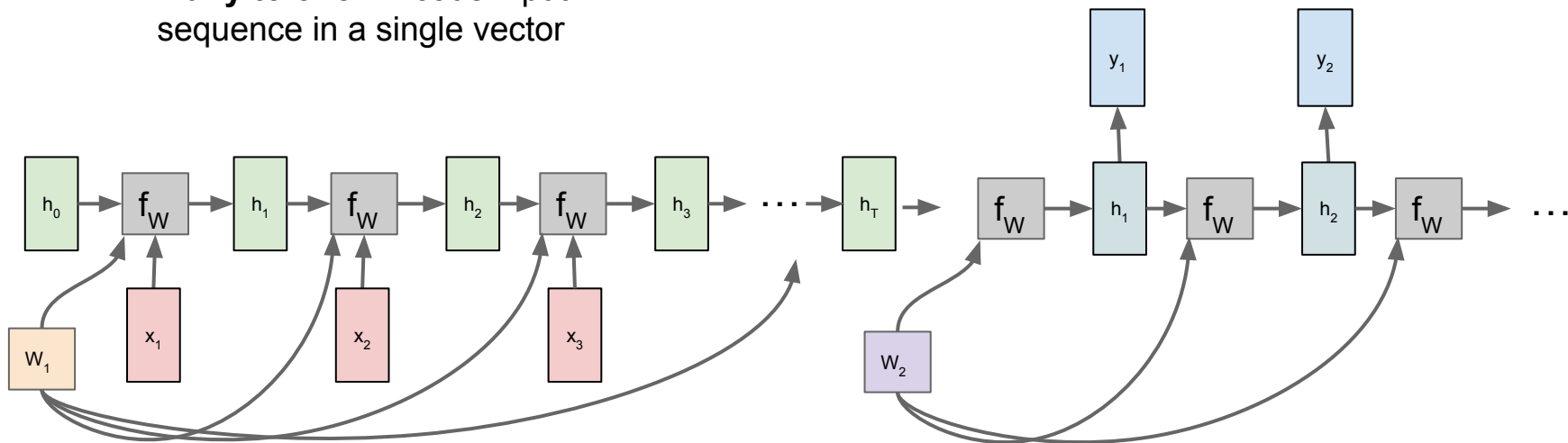


Sutskever et al, "Sequence to Sequence Learning with Neural Networks", NIPS 2014

# Sequence to Sequence: Many-to-one + one-to-many

**Many to one:** Encode input sequence in a single vector

**One to many:** Produce output sequence from single input vector

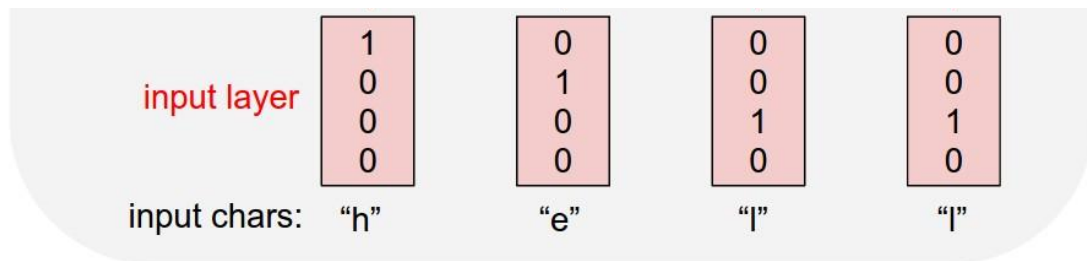


Sutskever et al, "Sequence to Sequence Learning with Neural Networks", NIPS 2014

# Example: Character-level Language Model

Vocabulary:  
[h,e,l,o]

Example training  
sequence:  
“hello”

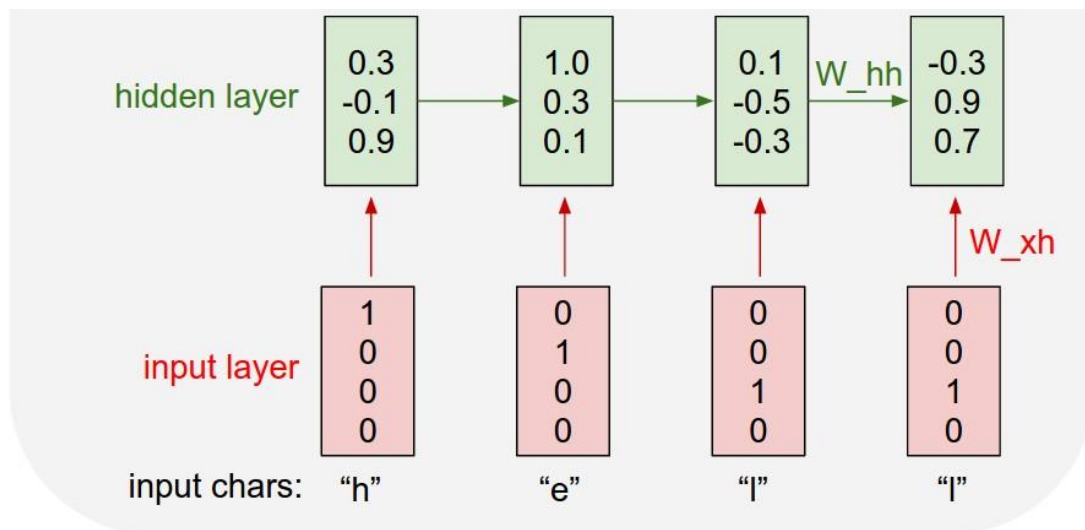


# Example: Character-level Language Model

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[h,e,l,o]

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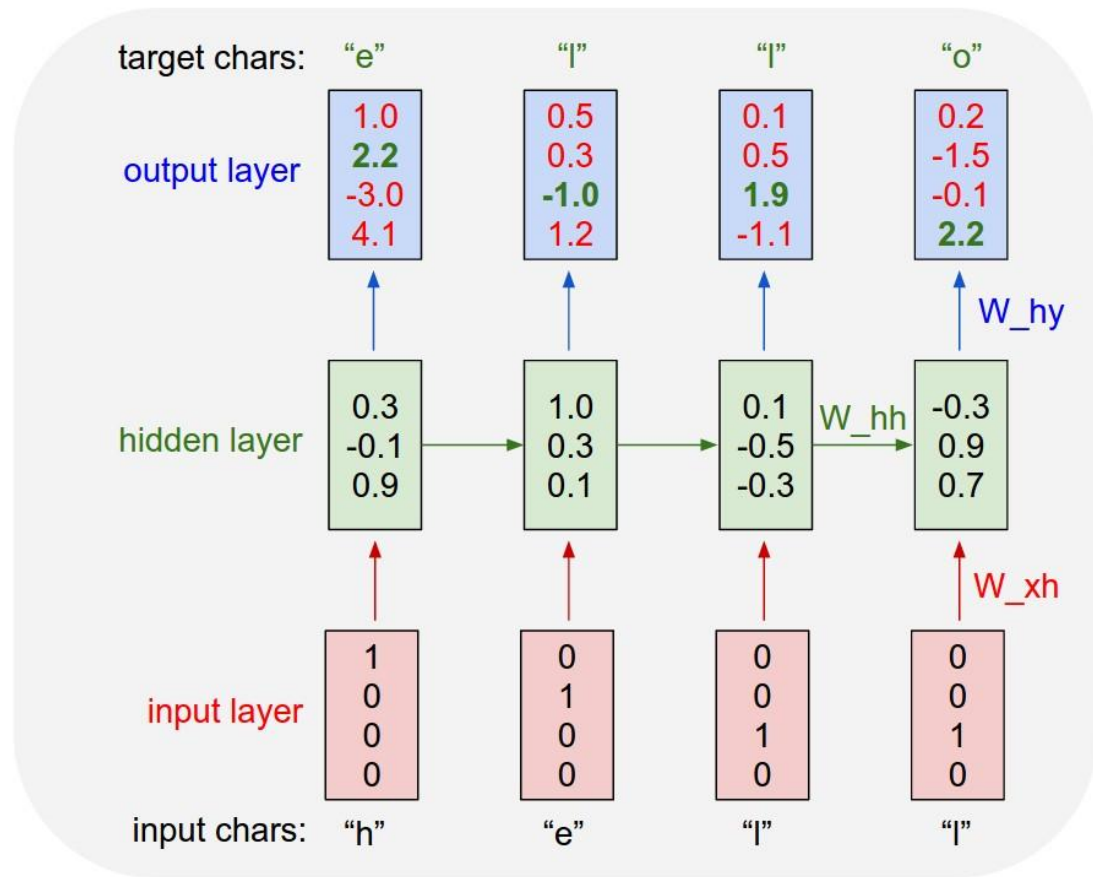
$$h_t = \tanh(W_{hh}h_{t-1} + W_{xh}x_t)$$



# Example: Character-level Language Model

Vocabulary:  
[h,e,l,o]

Example training  
sequence:  
“hello”



# Example: Character-level Language Model

Vocabulary:  
[h,e,l,o]

Example training  
sequence:  
“hello”

High SVM loss

target chars:

“e”

“l”

“l”

“o”

output layer

1.0  
2.2  
-3.0  
4.1

0.5  
0.3  
-1.0  
1.2

0.1  
0.5  
1.9  
-1.1

0.2  
-1.5  
-0.1  
2.2

$W_{hy}$

hidden layer

0.3  
-0.1  
0.9

1.0  
0.3  
0.1

0.1  
-0.5  
-0.3

$W_{hh}$

-0.3  
0.9  
0.7

input layer

1  
0  
0  
0

0  
1  
0  
0

0  
0  
1  
0

0  
0  
1  
0

$W_{xh}$

input chars: “h”

“e”

“l”

“l”

# Example: Character-level Language Model

So far: encode inputs as one-hot-vector

$$\begin{bmatrix} W_{11} & W_{12} & W_{13} & W_{14} \\ W_{21} & W_{22} & W_{23} & W_{24} \\ W_{31} & W_{32} & W_{33} & W_{34} \end{bmatrix} \begin{bmatrix} 1 \\ 0 \\ 0 \\ 0 \end{bmatrix} = \begin{bmatrix} W_{11} \\ W_{21} \\ W_{31} \end{bmatrix}$$

Matrix multiply with a one-hot vector just extracts a column from the weight matrix. Often extract this into a separate **embedding layer**

High SVM loss

target chars:

output layer

hidden layer

input layer

input chars:

"e"

"l"

"l"

"o"

1.0  
2.2  
-3.0  
4.1

0.5  
0.3  
-1.0  
1.2

0.1  
0.5  
1.9  
-1.1

0.2  
-1.5  
-0.1  
2.2

0.3  
-0.1  
0.9

1.0  
0.3  
0.1

0.1  
-0.5  
-0.3

-0.3  
0.9  
0.7

1  
0  
0  
0

0  
1  
0  
0

0  
0  
1  
0

0  
0  
1  
0

$W_{hh}$

$W_{hy}$

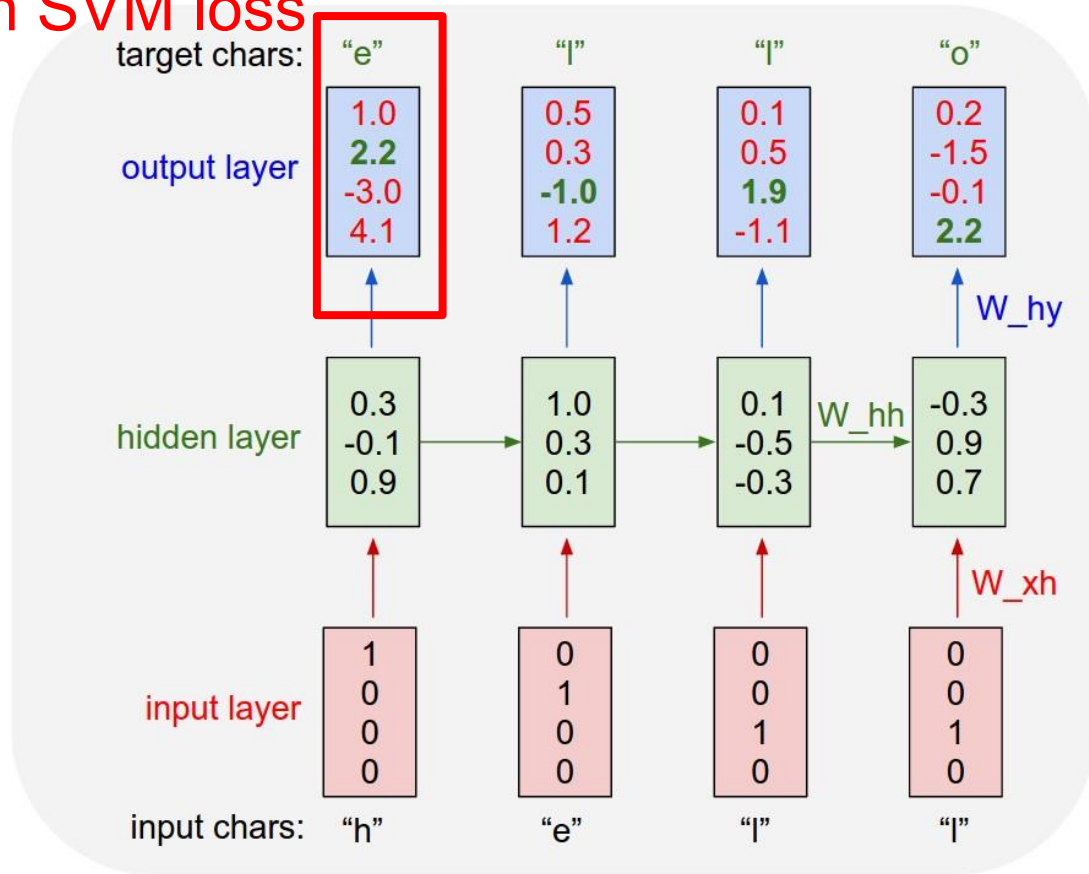
$W_{xh}$

"h"

"e"

"l"

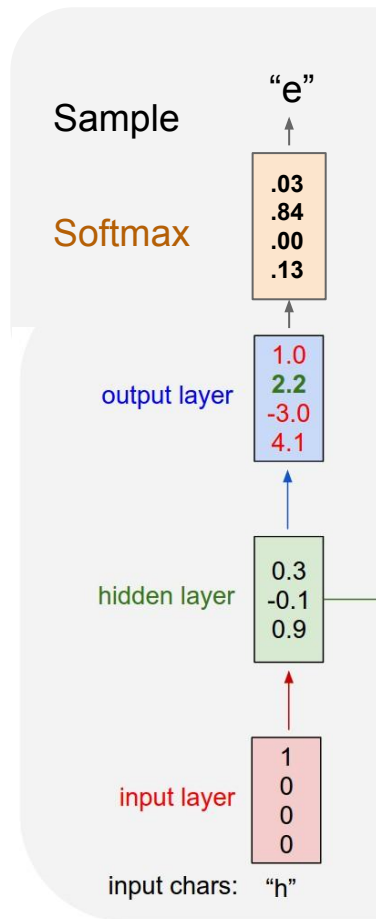
"l"



# Example: Character-level Language Model Sampling

Vocabulary:  
[h,e,l,o]

At test-time sample  
characters one at a time,  
feed back to model

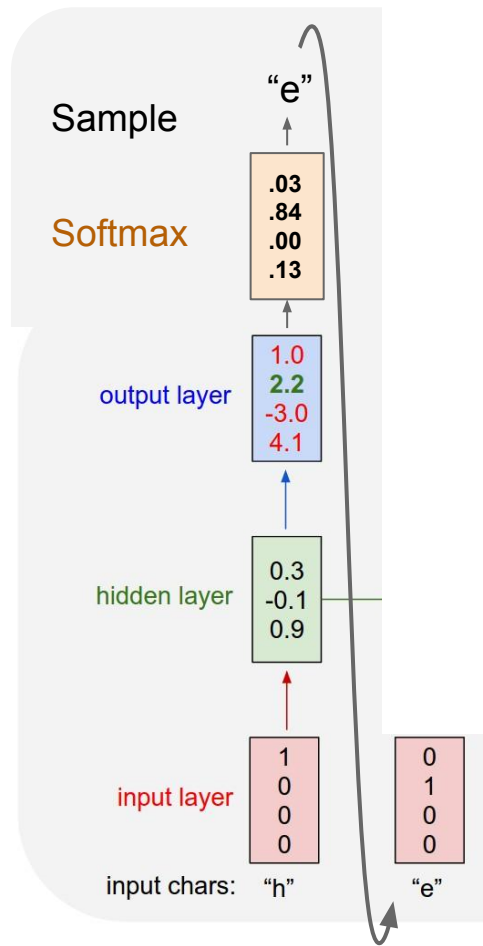




# Example: Character-level Language Model Sampling

Vocabulary:  
[h,e,l,o]

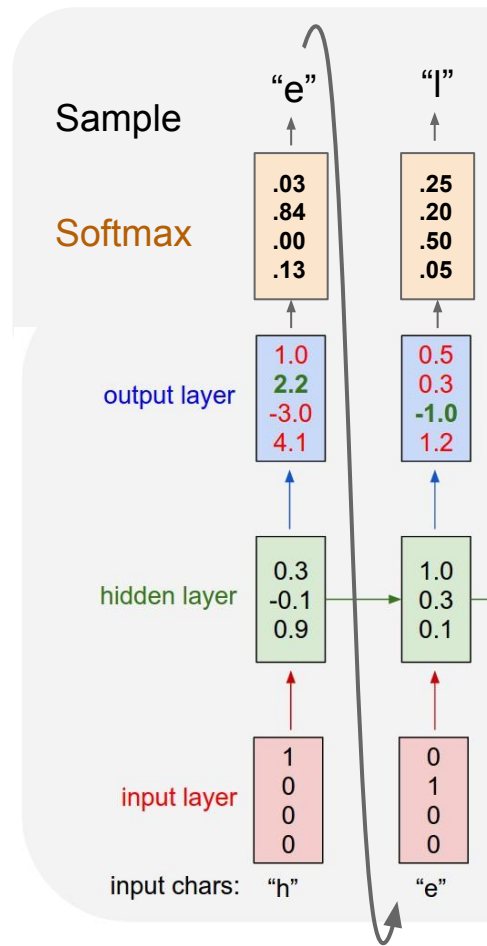
At test-time sample  
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feed back to model



# Example: Character-level Language Model Sampling

Vocabulary:  
[h,e,l,o]

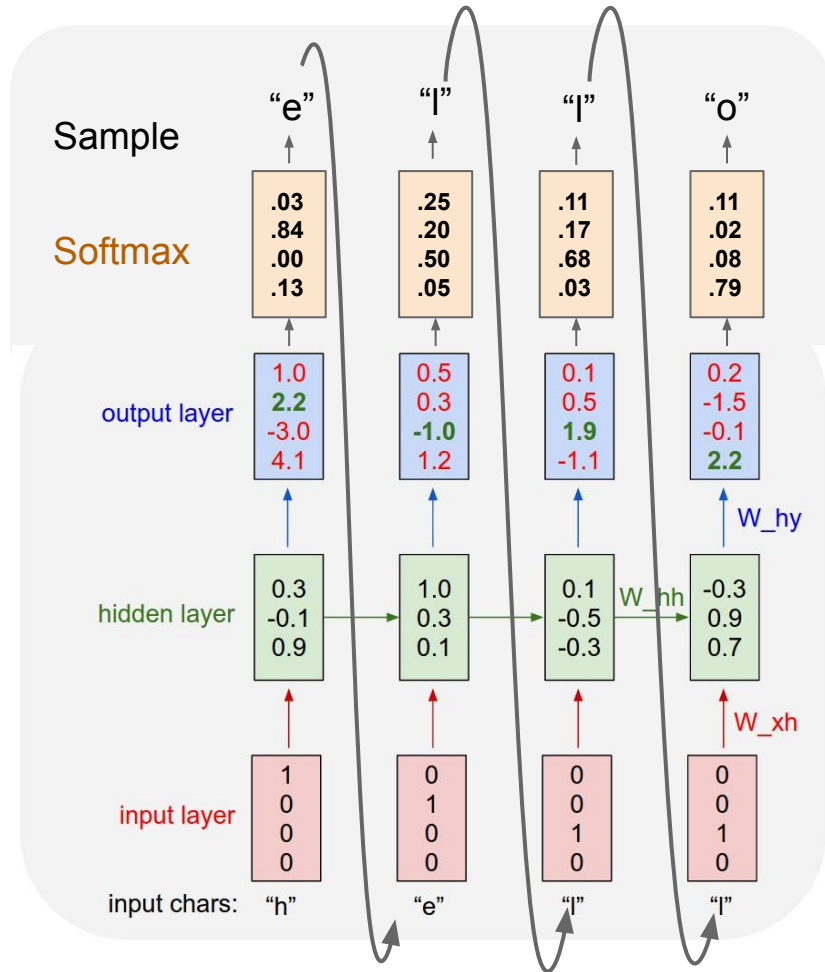
At test-time sample  
characters one at a time,  
feed back to model



# Example: Character-level Language Model Sampling

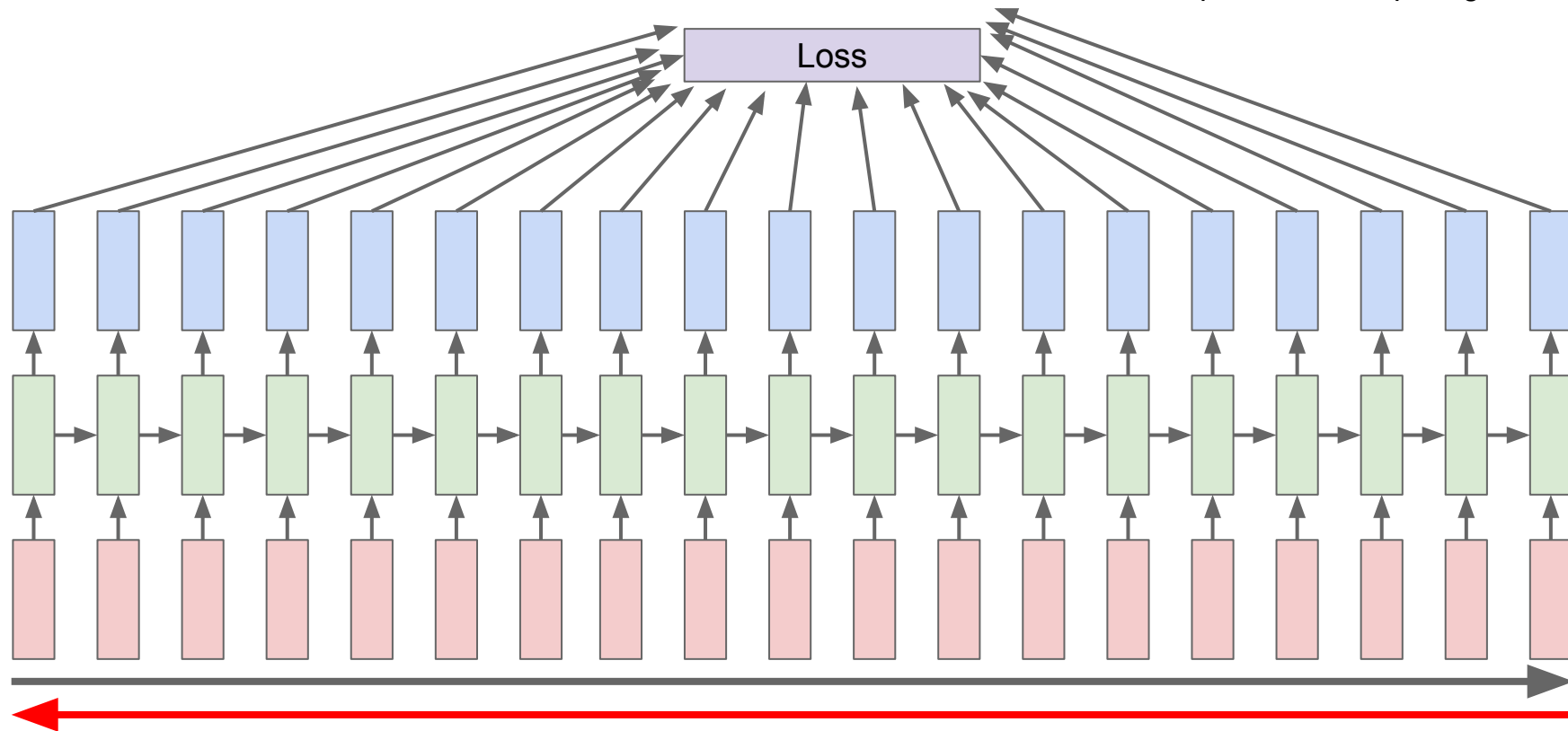
Vocabulary:  
[h,e,l,o]

At test-time sample  
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feed back to model

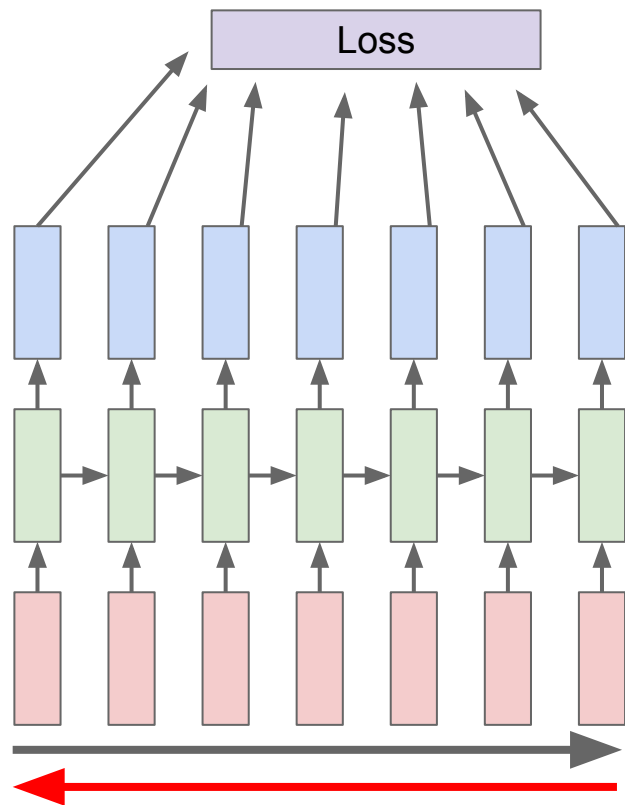


# Backpropagation through time

Forward through entire sequence to compute loss, then backward through entire sequence to compute gradient

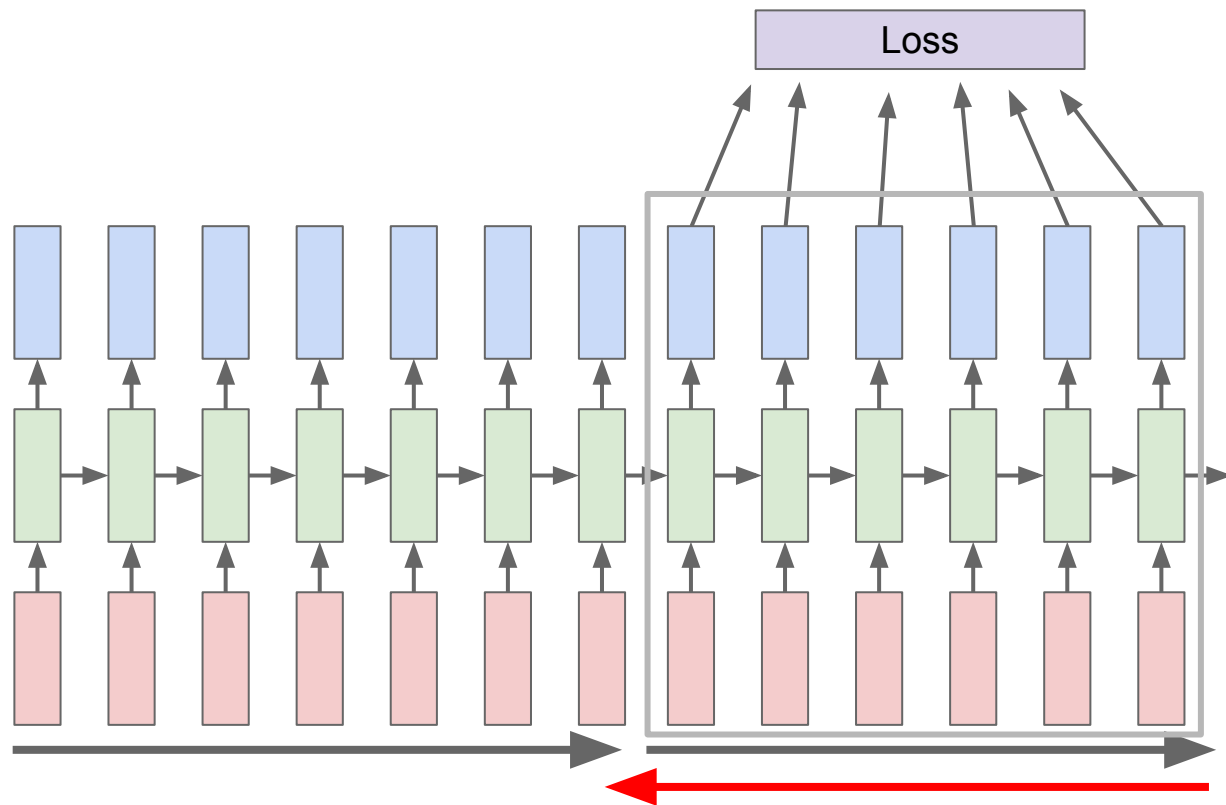


# Truncated Backpropagation through time



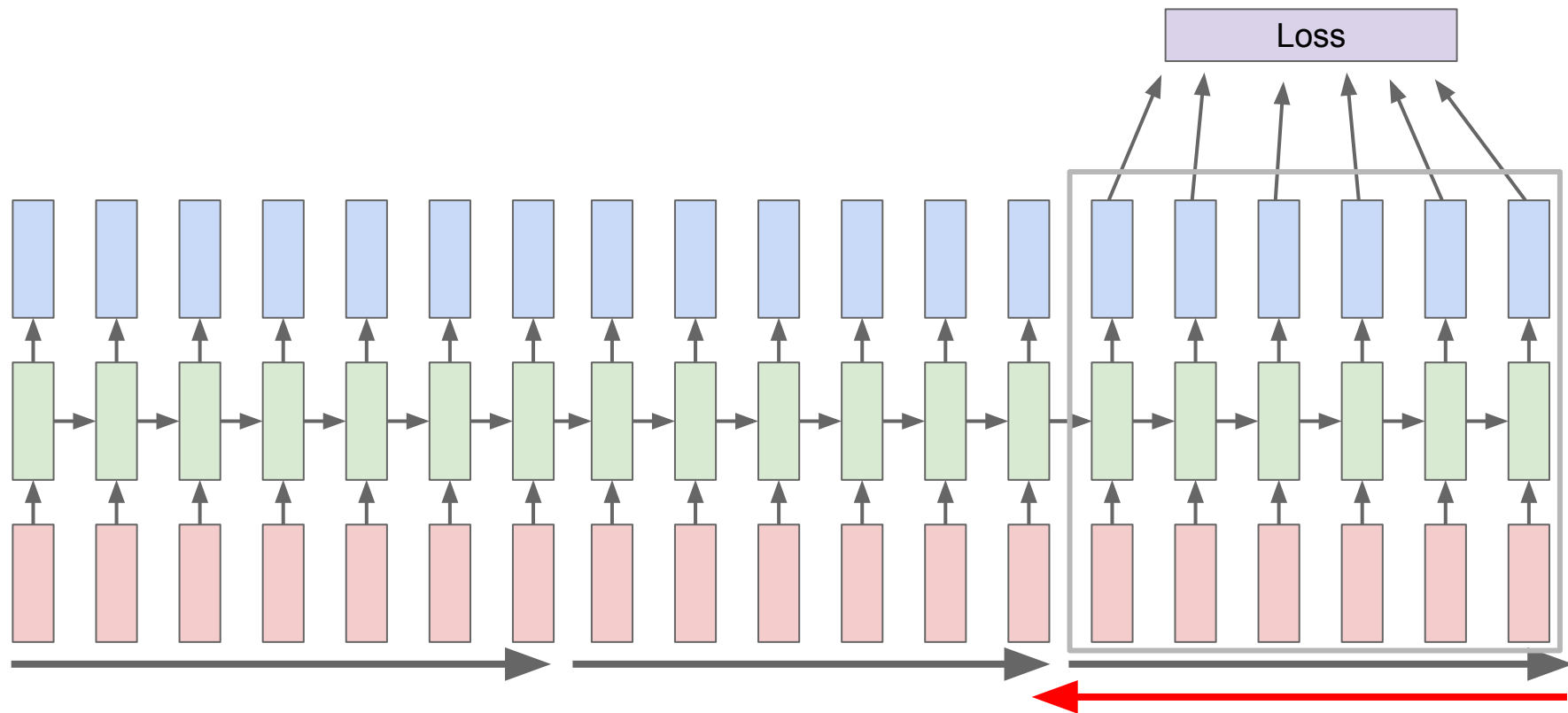
Run forward and backward through chunks of the sequence instead of whole sequence

# Truncated Backpropagation through time



Carry hidden states forward in time forever, but only backpropagate for some smaller number of steps

# Truncated Backpropagation through time



# min-char-rnn.py gist: 112 lines of Python

```
1 """
2 Minimal character-level Vanilla RNN model. Written by Andrej Karpathy (@karpathy)
3 BSD License
4 """
5 import numpy as np
6
7 # data I/O
8 data = open('input.txt', 'r').read() # should be simple plain text file
9 chars = list(set(data))
10 data_size, vocab_size = len(data), len(chars)
11 print 'data has %d characters, %d unique.' % (data_size, vocab_size)
12 char_to_ix = {ch:i for i,ch in enumerate(chars)}
13 ix_to_char = {i:ch for i,ch in enumerate(chars)}
14
15 # hyperparameters
16 hidden_size = 100 # size of hidden layer of neurons
17 seq_length = 25 # number of steps to unroll the RNN for
18 learning_rate = 1e-1
19
20 # model parameters
21 wnh = np.random.randn(hidden_size, vocab_size)*0.01 # input to hidden
22 whh = np.random.randn(hidden_size, hidden_size)*0.01 # hidden to hidden
23 why = np.random.randn(vocab_size, hidden_size)*0.01 # hidden to output
24 bh = np.zeros((hidden_size, 1)) # hidden bias
25 by = np.zeros((vocab_size, 1)) # output bias
26
27 def lossFun(inputs, targets, hprev):
28     """
29     inputs, targets are both list of integers.
30     hprev is Nx1 array of initial hidden state
31     returns the loss, gradients on model parameters, and last hidden state
32     """
33     xs, hs, ys, ps = {}, {}, {}, {}
34     hs[-1] = np.copy(hprev)
35     loss = 0
36     # forward pass
37     for t in xrange(len(inputs)):
38         xs[t] = np.zeros((vocab_size,1)) # encode in 1-of-k representation
39         xs[t][inputs[t]] = 1
40         hs[t] = np.tanh(np.dot(wnh, xs[t]) + np.dot(whh, hs[t-1]) + bh) # hidden state
41         ys[t] = np.dot(why, hs[t]) + by # unnormalized log probabilities for next chars
42         ps[t] = np.exp(ys[t]) / np.sum(np.exp(ys[t])) # probabilities for next chars
43         loss += -np.log(ps[t][targets[t],0]) # softmax (cross-entropy loss)
44     # backward pass: compute gradients going backwards
45     dwhx, dwhh, dwhy = np.zeros_like(wnh), np.zeros_like(whh), np.zeros_like(why)
46     dbh, dby = np.zeros_like(bh), np.zeros_like(by)
47     dhnext = np.zeros_like(hs[0])
48     for t in reversed(xrange(len(inputs))):
49         dy = np.copy(ps[t])
50         dy[targets[t]] -= 1 # backprop into y
51         dwhy += np.dot(dy, hs[t].T)
52         dby += dy
53         dh = np.dot(why.T, dy) + dhnext # backprop into h
54         dhrdw = (1 - hs[t] * hs[t]) * dh # backprop through tanh nonlinearity
55         dbh += dhrdw
56         dwhx += np.dot(dhrdw, xs[t].T)
57         dwhh += np.dot(dhrdw, hs[t-1].T)
58         dhnext = np.dot(whh.T, dhrdw)
59     for dparam in [dwhx, dwhh, dwhy, dbh, dby]:
60         np.clip(dparam, -5, 5, out=dparam) # clip to mitigate exploding gradients
61     return loss, dwhx, dwhh, dwhy, dbh, dby, hs[len(inputs)-1]
```

```
62 def sample(h, seed_ix, n):
63     """
64     sample a sequence of integers from the model
65     h is memory state, seed_ix is seed letter for first time step
66     """
67     x = np.zeros((vocab_size, 1))
68     x[seed_ix] = 1
69     ixes = []
70     for t in xrange(n):
71         h = np.tanh(np.dot(wnh, x) + np.dot(whh, h) + bh)
72         y = np.dot(why, h) + by
73         p = np.exp(y) / np.sum(np.exp(y))
74         ix = np.random.choice(range(vocab_size), p=p.ravel())
75         x = np.zeros((vocab_size, 1))
76         x[ix] = 1
77         ixes.append(ix)
78     return ixes
79
80 n, p = 0, 0
81 mxh, meth, mwhy = np.zeros_like(wnh), np.zeros_like(whh), np.zeros_like(why)
82 mbh, mby = np.zeros_like(bh), np.zeros_like(by) # memory variables for Adagrad
83 smooth_loss = -np.log(1.0/vocab_size)*seq_length # loss at iteration 0
84 while True:
85     # prepare inputs (we're sweeping from left to right in steps seq_length long)
86     if p+seq_length+1 >= len(data) or n == 0:
87         hprev = np.zeros((hidden_size,1)) # reset RNN memory
88         p = 0 # go from start of data
89         inputs = [char_to_ix[ch] for ch in data[p:p+seq_length]]
90         targets = [char_to_ix[ch] for ch in data[p+1:p+seq_length+1]]
91
92     # sample from the model now and then
93     if n % 100 == 0:
94         sample_ix = sample(hprev, inputs[0], 200)
95         txt = ''.join(ix_to_char[ix] for ix in sample_ix)
96         print '----\n%s\n' % (txt, )
97
98     # forward seq_length characters through the net and fetch gradient
99     loss, dwhx, dwhh, dwhy, dbh, dby, hprev = lossFun(inputs, targets, hprev)
100     smooth_loss = smooth_loss * 0.999 + loss * 0.001
101     if n % 100 == 0: print 'iter %d, loss: %f' % (n, smooth_loss) # print progress
102
103     # perform parameter update with Adagrad
104     for param, dparam, mem in zip([wnh, whh, why, bh, by],
105                                 [dwhx, dwhh, dwhy, dbh, dby],
106                                 [mxh, meth, mwhy, mbh, mby]):
107         mem += dparam * dparam
108         param += -learning_rate * dparam / np.sqrt(mem + 1e-8) # adagrad update
109
110 p += seq_length # move data pointer
111 n += 1 # iteration counter
```

[Simple python implementation](#)

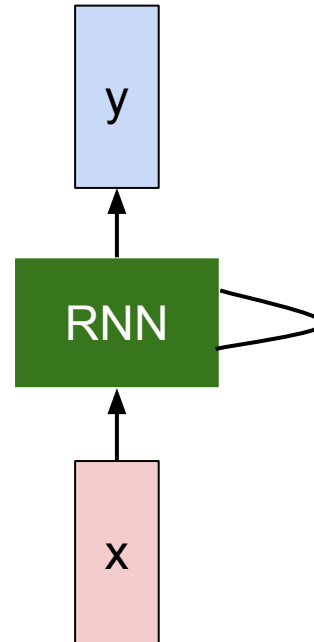


# THE SONNETS

by William Shakespeare

From fairest creatures we desire increase,  
That thereby beauty's rose might never die,  
But as the ripper should by time decease,  
His tender heir might bear his memory:  
But thou, contracted to thine own bright eyes,  
Feed'st thy light's flame with self-substantial fuel,  
Making a famine where abundance lies,  
Thyself thy foe, to thy sweet self too cruel:  
Thou that art now the world's fresh ornament,  
And only herald to the gaudy spring,  
Within thine own bud buriest thy content,  
And tender churl mak'st waste in niggarding:  
    Pity the world, or else this glutton be,  
    To eat the world's due, by the grave and thee.

When forty winters shall besiege thy brow,  
And dig deep trenches in thy beauty's field,  
Thy youth's proud livery so gazed on now,  
Will be a tatter'd weed of small worth held:  
Then being asked, where all thy beauty lies,  
Where all the treasure of thy lusty days;  
To say, within thine own deep sunken eyes,  
Were an all-eating shame, and thriftless praise.  
How much more praise deserv'd thy beauty's use,  
If thou couldst answer 'This fair child of mine  
Shall sum my count, and make my old excuse,'  
Proving his beauty by succession thine!  
    This were to be new made when thou art old,  
    And see thy blood warm when thou feel'st it cold.



at first:

tyntd-iafhatawiaoihrdemot lytdws e ,tfti, astai f ogoh eoase rrranbyne 'nhtnee e  
plia tklrqd t o idoe ns,smtt h ne etie h,hregtrs niglike,aoaenns lng

↓  
train more

"Tmont thithey" fomesscerliund  
Keushey. Thom here  
sheulke, anmerenith ol sivh I lalterthend Bleipile shuw y fil on aseterlome  
coaniogennc Phe lism thond hon at. MeiDimorotion in ther thize."

↓  
train more

Aftair fall unsuch that the hall for Prince Velzonski's that me of  
her hearly, and behs to so arwage fiving were to it beloge, pavu say falling misfort  
how, and Gogition is so overelical and offer.

↓  
train more

"Why do what that day," replied Natasha, and wishing to himself the fact the  
princess, Princess Mary was easier, fed in had oftened him.  
Pierre aking his soul came to the packs and drove up his father-in-law women.

PANDARUS:

Alas, I think he shall be come approached and the day  
When little strain would be attain'd into being never fed,  
And who is but a chain and subjects of his death,  
I should not sleep.

Second Senator:

They are away this miseries, produced upon my soul,  
Breaking and strongly should be buried, when I perish  
The earth and thoughts of many states.

DUKE VINCENTIO:

Well, your wit is in the care of side and that.

Second Lord:

They would be ruled after this chamber, and  
my fair nudes begun out of the fact, to be conveyed,  
Whose noble souls I'll have the heart of the wars.

Clown:

Come, sir, I will make did behold your worship.

VIOLA:

I'll drink it.

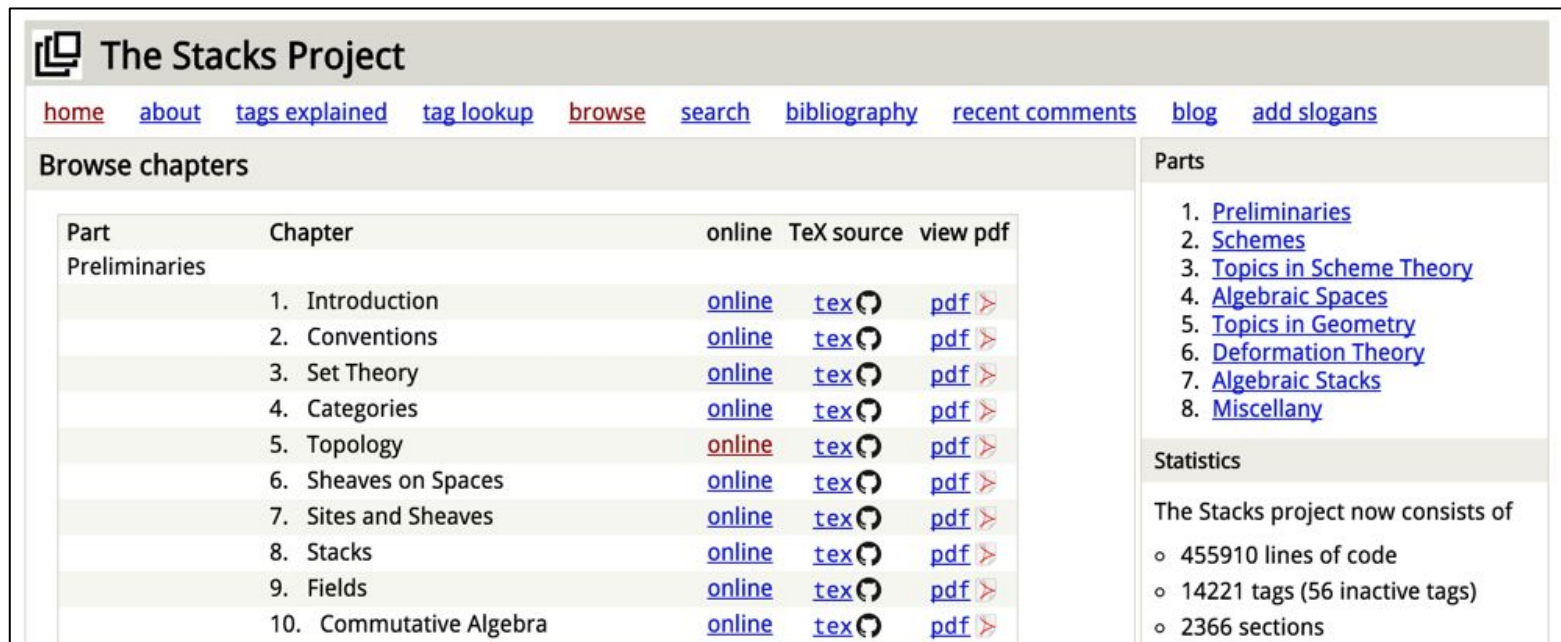
VIOLA:

Why, Salisbury must find his flesh and thought  
That which I am not apt, not a man and in fire,  
To show the reining of the raven and the wars  
To grace my hand reproach within, and not a fair are hand,  
That Caesar and my goodly father's world;  
When I was heaven of presence and our fleets,  
We spare with hours, but cut thy council I am great,  
Murdered and by thy master's ready there  
My power to give thee but so much as hell:  
Some service in the noble bondman here,  
Would show him to her wine.

KING LEAR:

O, if you were a feeble sight, the courtesy of your law,  
Your sight and several breath, will wear the gods  
With his heads, and my hands are wonder'd at the deeds,  
So drop upon your lordship's head, and your opinion  
Shall be against your honour.

# The Stacks Project: open source algebraic geometry textbook



The Stacks Project

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- 455910 lines of code
- 14221 tags (56 inactive tags)
- 2366 sections

Latex source



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For  $\bigoplus_{n=1, \dots, m}$  where  $\mathcal{L}_{m, \bullet} = 0$ , hence we can find a closed subset  $\mathcal{H}$  in  $\mathcal{H}$  and any sets  $\mathcal{F}$  on  $X$ ,  $U$  is a closed immersion of  $S$ , then  $U \rightarrow T$  is a separated algebraic space.

*Proof.* Proof of (1). It also start we get

$$S = \text{Spec}(R) = U \times_X U \times_X U$$

and the comparicoly in the fibre product covering we have to prove the lemma generated by  $\coprod Z \times_U U \rightarrow V$ . Consider the maps  $M$  along the set of points  $Sch_{fppf}$  and  $U \rightarrow U$  is the fibre category of  $S$  in  $U$  in Section, ?? and the fact that any  $U$  affine, see Morphisms, Lemma ???. Hence we obtain a scheme  $S$  and any open subset  $W \subset U$  in  $Sh(G)$  such that  $\text{Spec}(R') \rightarrow S$  is smooth or an

$$U = \bigcup U_i \times_{S_i} U_i$$

which has a nonzero morphism we may assume that  $f_i$  is of finite presentation over  $S$ . We claim that  $\mathcal{O}_{X, x}$  is a scheme where  $x, x', s'' \in S'$  such that  $\mathcal{O}_{X, x'} \rightarrow \mathcal{O}'_{X', x'}$  is separated. By Algebra, Lemma ?? we can define a map of complexes  $GL_{S'}(x'/S'')$  and we win.  $\square$

To prove study we see that  $\mathcal{F}|_U$  is a covering of  $\mathcal{X}'$ , and  $\mathcal{T}_i$  is an object of  $\mathcal{F}_{X/S}$  for  $i > 0$  and  $\mathcal{F}_p$  exists and let  $\mathcal{F}_i$  be a presheaf of  $\mathcal{O}_X$ -modules on  $\mathcal{C}$  as a  $\mathcal{F}$ -module. In particular  $\mathcal{F} = U/\mathcal{F}$  we have to show that

$$\widetilde{M}^\bullet = \mathcal{I}^\bullet \otimes_{\text{Spec}(k)} \mathcal{O}_{S, s} - i_X^{-1} \mathcal{F}$$

is a unique morphism of algebraic stacks. Note that

$$\text{Arrows} = (Sch/S)_{fppf}^{opp}, (Sch/S)_{fppf}$$

and

$$V = \Gamma(S, \mathcal{O}) \mapsto (U, \text{Spec}(A))$$

is an open subset of  $X$ . Thus  $U$  is affine. This is a continuous map of  $X$  is the inverse, the groupoid scheme  $S$ .

*Proof.* See discussion of sheaves of sets.  $\square$

The result for prove any open covering follows from the less of Example ???. It may replace  $S$  by  $X_{spaces, \acute{e}tale}$  which gives an open subspace of  $X$  and  $T$  equal to  $S_{Zar}$ , see Descent, Lemma ???. Namely, by Lemma ?? we see that  $R$  is geometrically regular over  $S$ .

**Lemma 0.1.** Assume (3) and (3) by the construction in the description.

Suppose  $X = \lim |X|$  (by the formal open covering  $X$  and a single map  $\text{Proj}_X(\mathcal{A}) = \text{Spec}(B)$  over  $U$  compatible with the complex

$$\text{Set}(\mathcal{A}) = \Gamma(X, \mathcal{O}_{X, \mathcal{O}_X}).$$

When in this case of to show that  $\mathcal{Q} \rightarrow \mathcal{C}_{Z/X}$  is stable under the following result in the second conditions of (1), and (3). This finishes the proof. By Definition ?? (without element is when the closed subschemes are catenary. If  $T$  is surjective we may assume that  $T$  is connected with residue fields of  $S$ . Moreover there exists a closed subspace  $Z \subset X$  of  $X$  where  $U$  in  $X'$  is proper (some defining as a closed subset of the uniqueness it suffices to check the fact that the following theorem

(1)  $f$  is locally of finite type. Since  $S = \text{Spec}(R)$  and  $Y = \text{Spec}(R)$ .

*Proof.* This is form all sheaves of sheaves on  $X$ . But given a scheme  $U$  and a surjective étale morphism  $U \rightarrow X$ . Let  $U \cap U = \coprod_{i=1, \dots, n} U_i$  be the scheme  $X$  over  $S$  at the schemes  $X_i \rightarrow X$  and  $U = \lim_i X_i$ .  $\square$

The following lemma surjective restrocomposes of this implies that  $\mathcal{F}_{x_0} = \mathcal{F}_{x_0} = \mathcal{F}_{\mathcal{X}, \dots, 0}$ .

**Lemma 0.2.** Let  $X$  be a locally Noetherian scheme over  $S$ ,  $E = \mathcal{F}_{X/S}$ . Set  $\mathcal{I} = \mathcal{J}_1 \subset \mathcal{I}'_n$ . Since  $\mathcal{I}^n \subset \mathcal{I}^n$  are nonzero over  $i_0 \in \mathfrak{p}$  is a subset of  $\mathcal{J}_{n,0} \circ A_2$  works.

**Lemma 0.3.** In Situation ???. Hence we may assume  $\mathfrak{q}' = 0$ .

*Proof.* We will use the property we see that  $\mathfrak{p}$  is the next functor (??). On the other hand, by Lemma ?? we see that

$$D(\mathcal{O}_{X'}) = \mathcal{O}_X(D)$$

where  $K$  is an  $F$ -algebra where  $\delta_{n+1}$  is a scheme over  $S$ .  $\square$

Proof. Omitted. □

**Lemma 0.1.** Let  $\mathcal{C}$  be a set of the construction.

Let  $\mathcal{C}$  be a gerber covering. Let  $\mathcal{F}$  be a quasi-coherent sheaves of  $\mathcal{O}$ -modules. We have to show that

$$\mathcal{O}_{\mathcal{O}_X} = \mathcal{O}_X(\mathcal{L})$$

Proof. This is an algebraic space with the composition of sheaves  $\mathcal{F}$  on  $X_{\acute{e}tale}$  we have

$$\mathcal{O}_X(\mathcal{F}) = \{\text{morph}_1 \times_{\mathcal{O}_X} (\mathcal{G}, \mathcal{F})\}$$

where  $\mathcal{G}$  defines an isomorphism  $\mathcal{F} \rightarrow \mathcal{F}$  of  $\mathcal{O}$ -modules. □

**Lemma 0.2.** This is an integer  $\mathcal{Z}$  is injective.

Proof. See Spaces, Lemma ?? □

**Lemma 0.3.** Let  $S$  be a scheme. Let  $X$  be a scheme and  $X$  is an affine open covering. Let  $U \subset X$  be a canonical and locally of finite type. Let  $X$  be a scheme. Let  $X$  be a scheme which is equal to the formal complex.

The following to the construction of the lemma follows.

Let  $X$  be a scheme. Let  $X$  be a scheme covering. Let

$$b : X \rightarrow Y' \rightarrow Y \rightarrow Y \rightarrow Y' \times_X Y \rightarrow X.$$

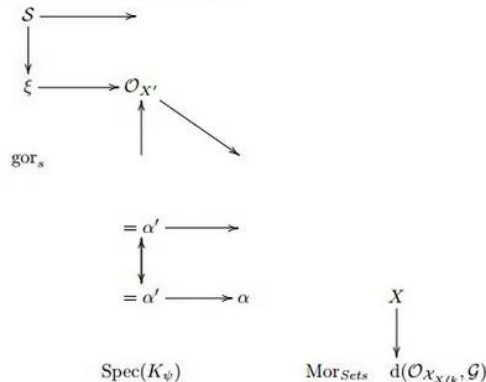
be a morphism of algebraic spaces over  $S$  and  $Y$ .

Proof. Let  $X$  be a nonzero scheme of  $X$ . Let  $X$  be an algebraic space. Let  $\mathcal{F}$  be a quasi-coherent sheaf of  $\mathcal{O}_X$ -modules. The following are equivalent

- (1)  $\mathcal{F}$  is an algebraic space over  $S$ .
- (2) If  $X$  is an affine open covering.

Consider a common structure on  $X$  and  $X$  the functor  $\mathcal{O}_X(U)$  which is locally of finite type. □

This since  $\mathcal{F} \in \mathcal{F}$  and  $x \in \mathcal{G}$  the diagram



is a limit. Then  $\mathcal{G}$  is a finite type and assume  $S$  is a flat and  $\mathcal{F}$  and  $\mathcal{G}$  is a finite type  $f_*$ . This is of finite type diagrams, and

- the composition of  $\mathcal{G}$  is a regular sequence,
- $\mathcal{O}_{X'}$  is a sheaf of rings.

□

Proof. We have see that  $X = \text{Spec}(R)$  and  $\mathcal{F}$  is a finite type representable by algebraic space. The property  $\mathcal{F}$  is a finite morphism of algebraic stacks. Then the cohomology of  $X$  is an open neighbourhood of  $U$ . □

Proof. This is clear that  $\mathcal{G}$  is a finite presentation, see Lemmas ??.

A reduced above we conclude that  $U$  is an open covering of  $\mathcal{C}$ . The functor  $\mathcal{F}$  is a "field

$$\mathcal{O}_{X,x} \rightarrow \mathcal{F}_{\bar{x}} \rightarrow -1(\mathcal{O}_{X_{\acute{e}tale}}) \rightarrow \mathcal{O}_{X_t}^{-1} \mathcal{O}_{X_\lambda}(\mathcal{O}_{X_\eta}^{\vee})$$

is an isomorphism of covering of  $\mathcal{O}_{X_t}$ . If  $\mathcal{F}$  is the unique element of  $\mathcal{F}$  such that  $X$  is an isomorphism.

The property  $\mathcal{F}$  is a disjoint union of Proposition ?? and we can filtered set of presentations of a scheme  $\mathcal{O}_X$ -algebra with  $\mathcal{F}$  are opens of finite type over  $S$ .

If  $\mathcal{F}$  is a scheme theoretic image points. □

If  $\mathcal{F}$  is a finite direct sum  $\mathcal{O}_{X_\lambda}$  is a closed immersion, see Lemma ?? . This is a sequence of  $\mathcal{F}$  is a similar morphism.

## Linux kernel source tree

520,037 commits

1 branch

420 releases

5,039 contributors



branch: master -

linux / +



Merge branch 'drm-fixes' of git://people.freedesktop.org/~airlied/linux ...



torvalds authored 9 hours ago

latest commit 4b1706927d

Documentation	Merge git://git.kernel.org/pub/scm/linux/kernel/git/nab/target-pending	6 days ago
arch	Merge branch 'x86-urgent-for-linus' of git://git.kernel.org/pub/scm/l...	a day ago
block	block: discard bdi_unregister() in favour of bdi_destroy()	9 days ago
crypto	Merge git://git.kernel.org/pub/scm/linux/kernel/git/herbert/crypto-2.6	10 days ago
drivers	Merge branch 'drm-fixes' of git://people.freedesktop.org/~airlied/linux	9 hours ago
firmware	firmware/hex2fw.c: restore missing default in switch statement	2 months ago
fs	vfs: read file_handle only once in handle_to_path	4 days ago
include	Merge branch 'perf-urgent-for-linus' of git://git.kernel.org/pub/scm/...	a day ago
init	init: fix regression by supporting devices with major:minor:offset fo...	a month ago
ipc	Merge branch 'for-linus' of git://git.kernel.org/pub/scm/linux/kernel...	a month ago



Code



Pull requests

74



Pulse



Graphs

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```

static void do_command(struct seq_file *m, void *v)
{
    int column = 32 << (cmd[2] & 0x80);
    if (state)
        cmd = (int)(int_state ^ (in_8(&ch->ch_flags) & Cmd) ? 2 : 1);
    else
        seq = 1;
    for (i = 0; i < 16; i++) {
        if (k & (1 << i))
            pipe = (in_use & UMXTHREAD_UNCCA) +
                ((count & 0x00000000fffffff8) & 0x0000000f) << 8;
        if (count == 0)
            sub(pid, ppc_md.kexec_handle, 0x20000000);
        pipe_set_bytes(i, 0);
    }
    /* Free our user pages pointer to place camera if all dash */
    subsystem_info = &of_changes[PAGE_SIZE];
    rek_controls(offset, idx, &soffset);
    /* Now we want to deliberately put it to device */
    control_check_polarity(&context, val, 0);
    for (i = 0; i < COUNTER; i++)
        seq_puts(s, "policy ");
}

```

# Generated C code



```
/*
 * Copyright (c) 2006-2010, Intel Mobile Communications. All rights reserved.
 *
 * This program is free software; you can redistribute it and/or modify it
 * under the terms of the GNU General Public License version 2 as published by
 * the Free Software Foundation.
 *
 * This program is distributed in the hope that it will be useful,
 * but WITHOUT ANY WARRANTY; without even the implied warranty of
 * MERCHANTABILITY or FITNESS FOR A PARTICULAR PURPOSE. See the
 *
 * GNU General Public License for more details.
 *
 * You should have received a copy of the GNU General Public License
 * along with this program; if not, write to the Free Software Foundation,
 * Inc., 675 Mass Ave, Cambridge, MA 02139, USA.
 */

#include <linux/kexec.h>
#include <linux/errno.h>
#include <linux/io.h>
#include <linux/platform_device.h>
#include <linux/multi.h>
#include <linux/ckevent.h>

#include <asm/io.h>
#include <asm/prom.h>
#include <asm/e820.h>
#include <asm/system_info.h>
#include <asm/setew.h>
#include <asm/pgproto.h>
```

```

#include <asm/io.h>
#include <asm/prom.h>
#include <asm/e820.h>
#include <asm/system_info.h>
#include <asm/setew.h>
#include <asm/pgproto.h>

#define REG_PG    vesa_slot_addr_pack
#define PFM_NOCOMP  AFSR(0, load)
#define STACK_DDR(type)      (func)

#define SWAP_ALLOCATE(nr)      (e)
#define emulate_sigs()  arch_get_unaligned_child()
#define access_rw(TST)  asm volatile("movd %%esp, %0, %3" : : "r" (0)); \
    if (__type & DO_READ)

static void stat_PC_SEC __read_mostly offsetof(struct seq_argsqueue, \
    pC>[1]);

static void
os_prefix(unsigned long sys)
{
#ifdef CONFIG_PREEMPT
    PUT_PARAM_RAID(2, sel) = get_state_state();
    set_pid_sum((unsigned long)state, current_state_str(),
        (unsigned long)-1->lr_full; low;
}

```

# OpenAI GPT-2 generated text

[source](#)

**Input:** In a shocking finding, scientist discovered a herd of unicorns living in a remote, previously unexplored valley, in the Andes Mountains. Even more surprising to the researchers was the fact that the unicorns spoke perfect English.

**Output:** The scientist named the population, after their distinctive horn, Ovid's Unicorn. These four-horned, silver-white unicorns were previously unknown to science.

Now, after almost two centuries, the mystery of what sparked this odd phenomenon is finally solved.

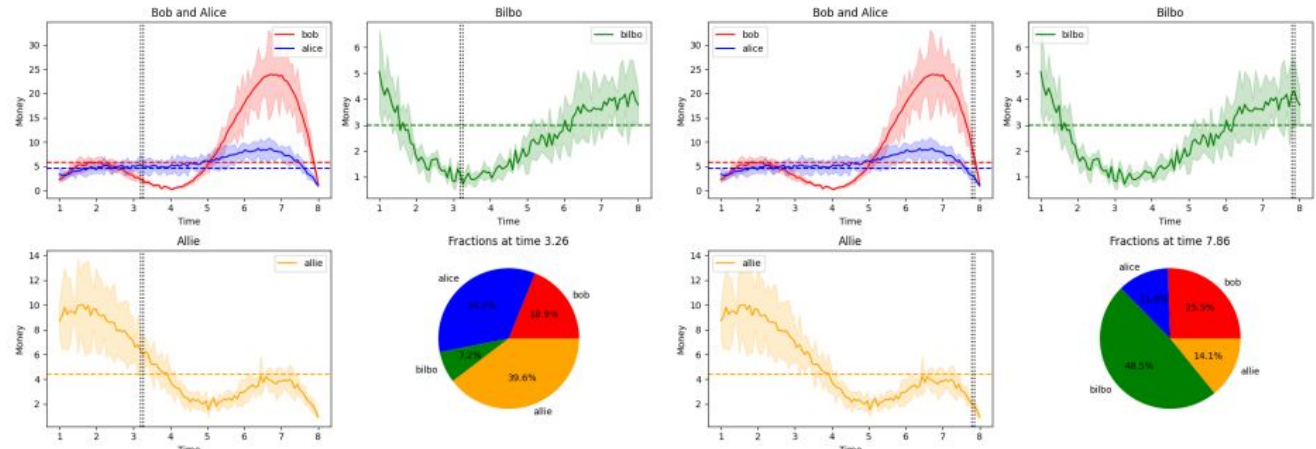
Dr. Jorge Pérez, an evolutionary biologist from the University of La Paz, and several companions, were exploring the Andes Mountains when they found a small valley, with no other animals or humans. Pérez noticed that the valley had what appeared to be a natural fountain, surrounded by two peaks of rock and silver snow.

# GPT-4

**Prompt:** Can you generate a pyplot for the following data:  $x = [1, 3, 5, 6, 8]$ ,  $y1 = [2, 3, 5, 18, 1]$ ,  $y2 = [3, 5, 6, 8, 1]$ ,  $y3 = [5, 1, 2, 3, 4]$ ,  $y4 = [9, 7, 2, 3, 1]$ . I want  $y1, y2$  to be in the same plot, but  $y3$  is in another plot next to that plot,  $y4$  is in below. I want the legend of  $y1$  to be "bob",  $y2$  to be "alice",  $y3$  to be "bilbo",  $y4$  to be "allie". I want the  $x$ -axis to be labeled with "time" and  $y$  axis to be labeled with "money". I want to add a 10 %-40% random error bar to each curve, through all times (including non-integers). I want smoothed curves to show the plot, and smoothed error bar. Do not use linear interpolation, use smooth interpolation! I want to also add some small zig-zag to the smoothed curve to make it look more real. I want to put a baseline as the mean of each line. I want to put a pie chart below indicating the fraction of the four people in each time step. I also want an animation to show how the fractions are changing in the pie chart in **\*\*continuous time\*\***. Interpolate the missing fractions! I also want vertical line animation in other three plots to match the pie chart. I want the fanciest plot. Please add as many fancy things as possible.

Here is a possible code to generate a pyplot for the following data, with some comments to explain the steps:

**GPT-4:** [We give two snapshots from the animation resulting from the produced code]



Bubek et al. Sparks of AGI. ArXiv 2023

# Language modeling leads to reasoning capabilities for GPT-4

Bubek et al. Sparks of AGI. ArXiv 2023

## GPT-4 vs ChatGPT

**Prompt:** Here we have a book, 9 eggs, a laptop, a bottle and a nail. Please tell me how to stack them onto each other in a stable manner.

### GPT-4:

One possible way to stack the objects onto each other in a stable manner is:

- Place the book flat on a level surface, such as a table or a floor. The book will serve as the base of the stack and provide a large and sturdy support.
- Arrange the 9 eggs in a 3 by 3 square on top of the book, leaving some space between them. The eggs will form a second layer and distribute the weight evenly. Make sure the eggs are not cracked or broken, and handle them gently to avoid dropping them.
- Place the laptop on top of the eggs, with the screen facing down and the keyboard facing up. The laptop will fit snugly within the boundaries of the book and the eggs, and its flat and rigid surface will provide a stable platform for the next layer. Make sure the laptop is closed and turned off, and do not press any keys or buttons.
- Place the bottle on top of the laptop, with the cap facing up and the bottom facing down. The bottle will add some height and balance to the stack, and its cylindrical shape will reduce the contact area with the laptop. Make sure the bottle is empty and closed, and do not shake or tilt it.
- Place the nail on top of the bottle cap, with the pointy end facing up and the flat end facing down. The nail will be the final and smallest object in the stack, and its sharp tip will prevent it from rolling or sliding off the bottle. Make sure the nail is clean and straight, and do not touch or move it.

### ChatGPT:

It would be difficult to stack all of these objects on top of each other in a stable manner without using any extra objects. The book and laptop are likely too large and heavy to stack on top of the eggs without damaging them. The bottle and nail may be too small to provide a stable base for the other objects.

Here is one possible way to stack the objects:

- Place the bottle on a flat surface.
- Carefully balance the nail on top of the bottle.
- Place the eggs on top of the nail, making sure they are balanced and not tilting to one side.
- Place the laptop on top of the eggs, again making sure it is balanced and not tilting to one side.
- Finally, place the book on top of the laptop.

This stack may not be very stable, so it is important to be careful when handling it. Alternatively, you could try stacking the objects in a different order or using some of the objects as supports for others to create a more stable stack.

# RNN tradeoffs

## RNN Advantages:

- Can process any length input
- Computation for step  $t$  can (in theory) use information from many steps back
- Model size doesn't increase for longer input
- Same weights applied on every timestep, so there is symmetry in how inputs are processed.

## RNN Disadvantages:

- Recurrent computation is slow
- In practice, difficult to access information from many steps back

# Image Captioning

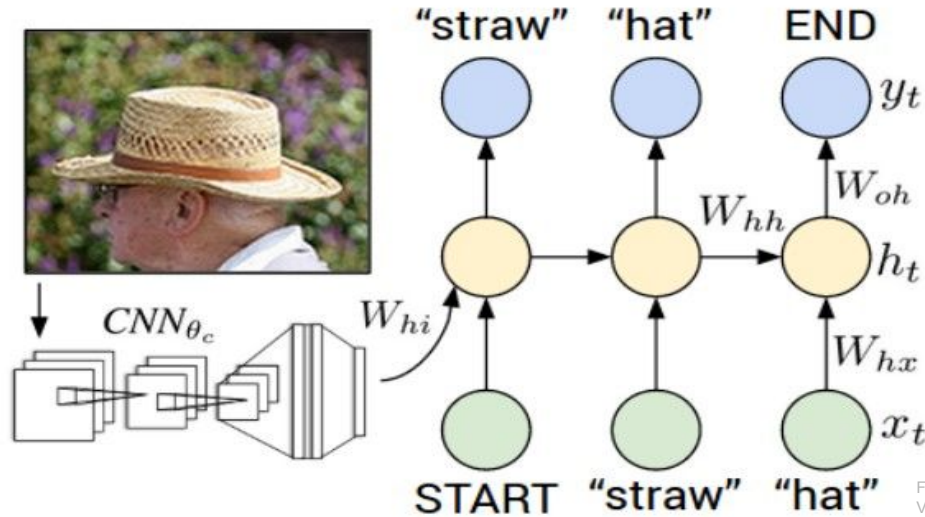


Figure from Karpathy et al, "Deep Visual-Semantic Alignments for Generating Image Descriptions", CVPR 2015; figure copyright IEEE, 2015. Reproduced for educational purposes.

Explain Images with Multimodal Recurrent Neural Networks, Mao et al.

Deep Visual-Semantic Alignments for Generating Image Descriptions, Karpathy and Fei-Fei

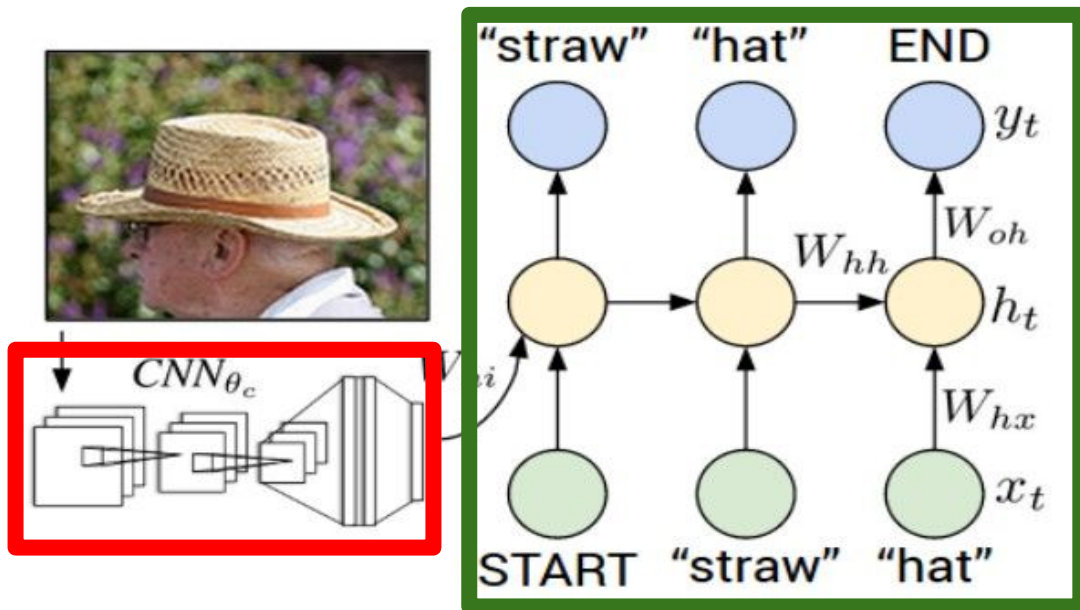
Show and Tell: A Neural Image Caption Generator, Vinyals et al.

Long-term Recurrent Convolutional Networks for Visual Recognition and Description, Donahue et al.

Learning a Recurrent Visual Representation for Image Caption Generation, Chen and Zitnick

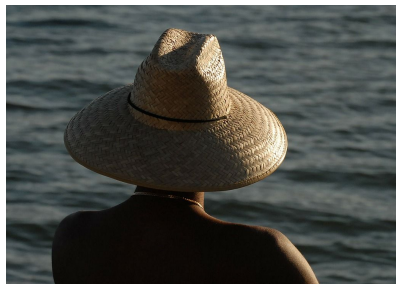


# Recurrent Neural Network



# Convolutional Neural Network





test image

[This image](#) is [CC0 public domain](#)

image

conv-64

conv-64

maxpool

conv-128

conv-128

maxpool

conv-256

conv-256

maxpool

conv-512

conv-512

maxpool

conv-512

conv-512

maxpool

FC-4096

FC-4096

FC-1000

softmax



test image

image

conv-64

conv-64

maxpool

conv-128

conv-128

maxpool

conv-256

conv-256

maxpool

conv-512

conv-512

maxpool

conv-512

conv-512

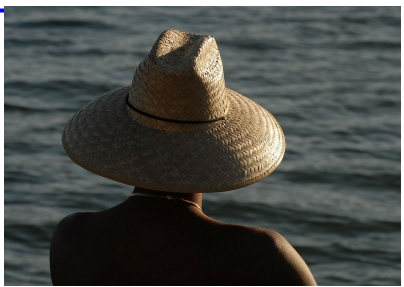
maxpool

FC-4096

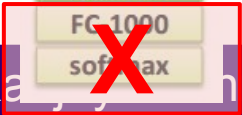
FC-4096

FC-1000

softmax



test image



image

conv-64

conv-64

maxpool

conv-128

conv-128

maxpool

conv-256

conv-256

maxpool

conv-512

conv-512

maxpool

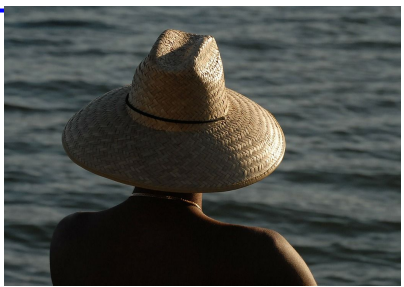
conv-512

conv-512

maxpool

FC-4096

FC-4096

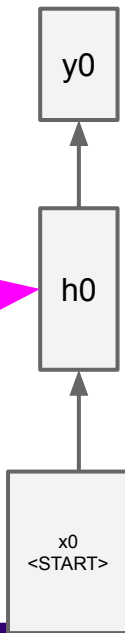


test image

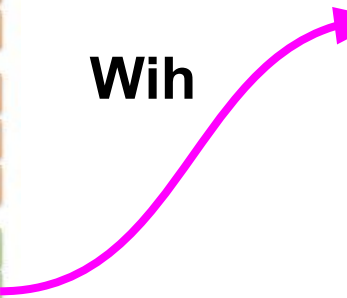
x0  
<START>



test image



**W<sub>ih</sub>**



**before:**

$$h = \tanh(W_{xh} * x + W_{hh} * h)$$

**now:**

$$h = \tanh(W_{xh} * x + W_{hh} * h + W_{ih} * v)$$

image

conv-64  
conv-64  
maxpool

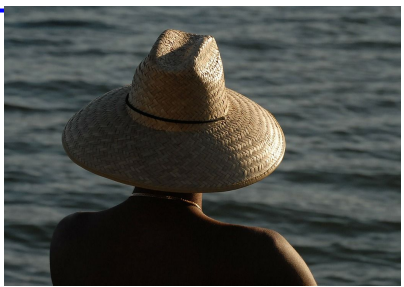
conv-128  
conv-128  
maxpool

conv-256  
conv-256  
maxpool

conv-512  
conv-512  
maxpool

conv-512  
conv-512  
maxpool

FC-4096  
FC-4096



test image

y0

h0

x0  
<START>

straw

sample!

image

conv-64

conv-64

maxpool

conv-128

conv-128

maxpool

conv-256

conv-256

maxpool

conv-512

conv-512

maxpool

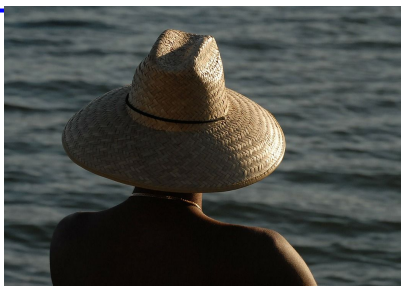
conv-512

conv-512

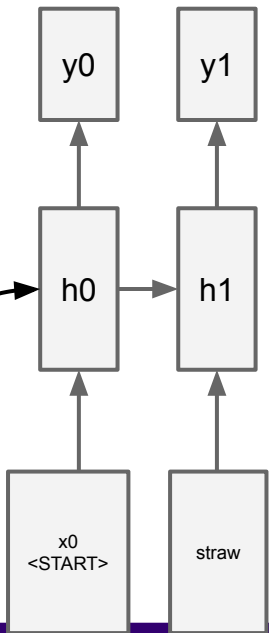
maxpool

FC-4096

FC-4096



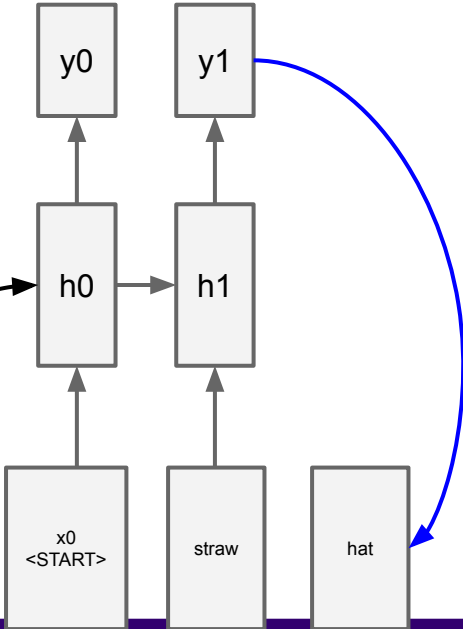
test image





test image

- image
- conv-64
- conv-64
- maxpool
- conv-128
- conv-128
- maxpool
- conv-256
- conv-256
- maxpool
- conv-512
- conv-512
- maxpool
- conv-512
- conv-512
- maxpool
- FC-4096
- FC-4096



sample!



image

conv-64  
conv-64  
maxpool

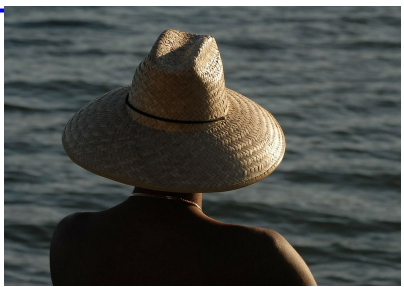
conv-128  
conv-128  
maxpool

conv-256  
conv-256  
maxpool

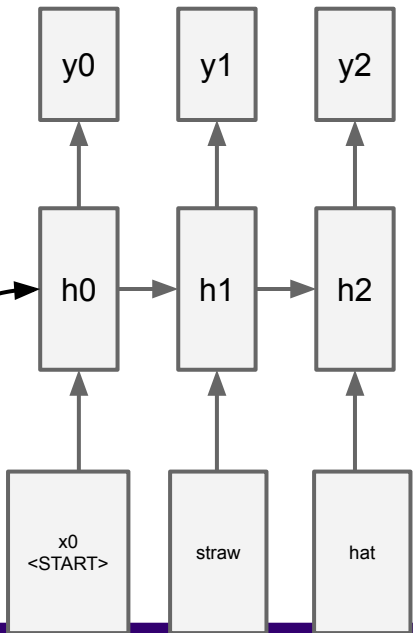
conv-512  
conv-512  
maxpool

conv-512  
conv-512  
maxpool

FC-4096  
FC-4096



test image



image

conv-64  
conv-64  
maxpool

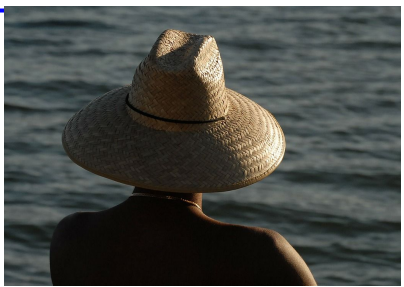
conv-128  
conv-128  
maxpool

conv-256  
conv-256  
maxpool

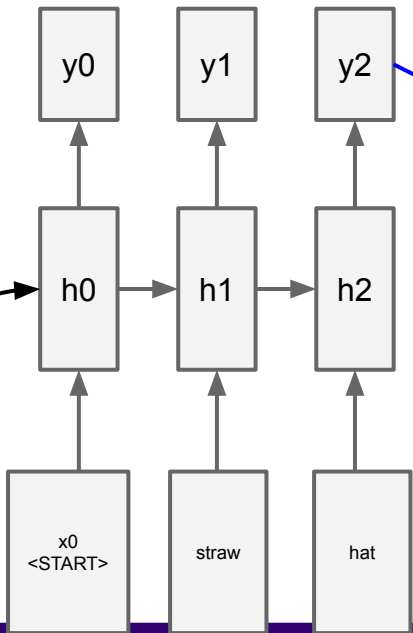
conv-512  
conv-512  
maxpool

conv-512  
conv-512  
maxpool

FC-4096  
FC-4096



test image



sample  
<END> token  
=> finish.

# Image Captioning: Example Results

Captions generated using [neuraltalk2](#)  
All images are [CC0 Public domain](#)  
[cat suitcase](#) [cat tree](#) [dog bear](#)  
[surfers tennis](#) [giraffe](#) [motorcycle](#)



*A cat sitting on a suitcase on the floor*



*A cat is sitting on a tree branch*



*A dog is running in the grass with a frisbee*



*A white teddy bear sitting in the grass*



*Two people walking on the beach with surfboards*



*A tennis player in action on the court*



*Two giraffes standing in a grassy field*



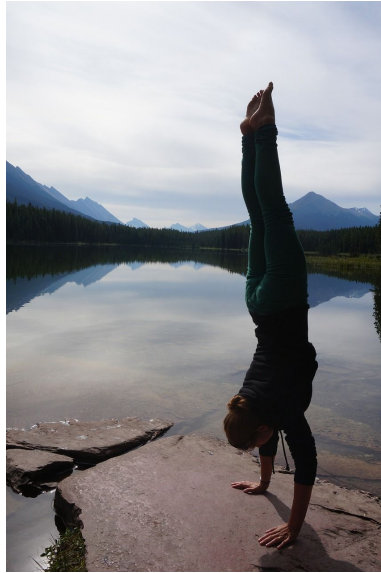
*A man riding a dirt bike on a dirt track*

# Image Captioning: Failure Cases

Captions generated using [neuraltalk2](#)  
All images are [CC0 Public domain](#): [fur coat](#), [handstand](#), [spider web](#), [baseball](#)



*A woman is holding a cat in her hand*



*A woman standing on a beach holding a surfboard*



*A bird is perched on a tree branch*



*A person holding a computer mouse on a desk*



*A man in a baseball uniform throwing a ball*

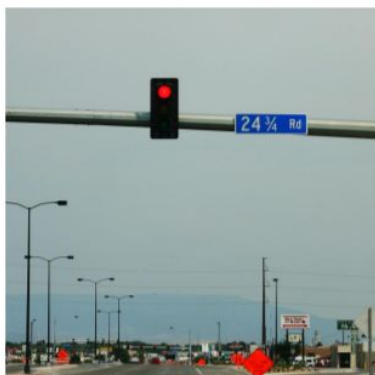


# Visual Question Answering (VQA)



**Q: What endangered animal is featured on the truck?**

- A: A bald eagle.**
- A: A sparrow.
- A: A humming bird.
- A: A raven.



**Q: Where will the driver go if turning right?**

- A: Onto 24 3/4 Rd.**
- A: Onto 25 3/4 Rd.
- A: Onto 23 3/4 Rd.
- A: Onto Main Street.



**Q: When was the picture taken?**

- A: During a wedding.**
- A: During a bar mitzvah.
- A: During a funeral.
- A: During a Sunday church service.

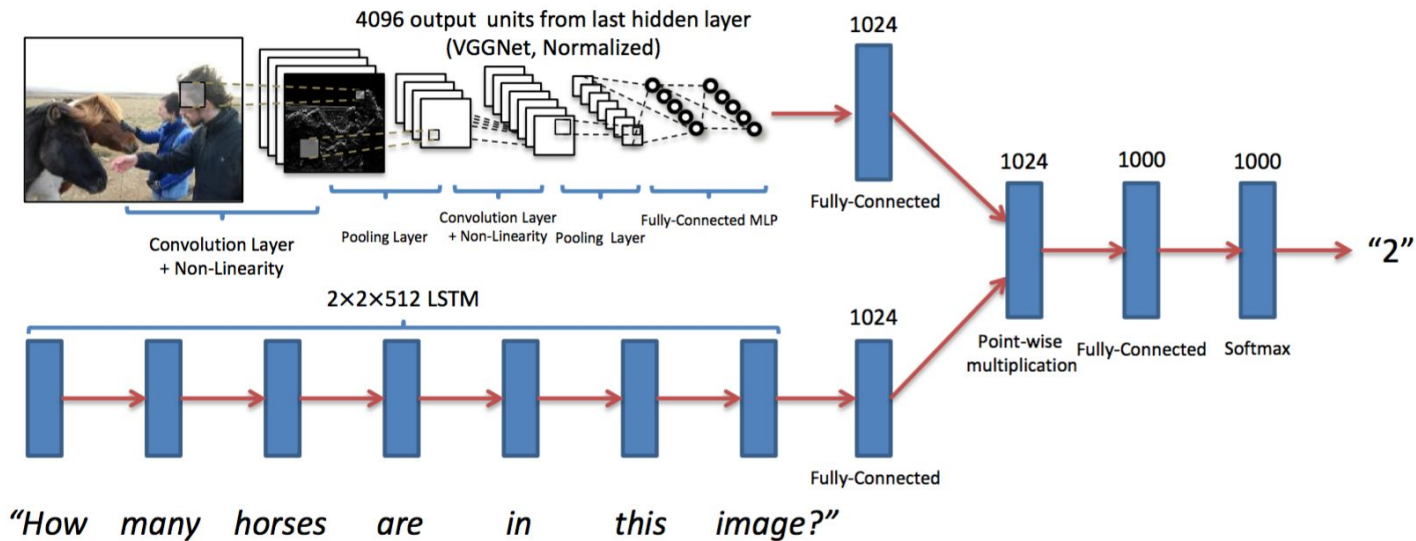


**Q: Who is under the umbrella?**

- A: Two women.**
- A: A child.
- A: An old man.
- A: A husband and a wife.

Agrawal et al, "VQA: Visual Question Answering", ICCV 2015  
Zhu et al, "Visual 7W: Grounded Question Answering in Images", CVPR 2016  
Figure from Zhu et al, copyright IEEE 2016. Reproduced for educational purposes.

# Visual Question Answering: RNNs with Attention



Agrawal et al, "Visual 7W: Grounded Question Answering in Images", CVPR 2015  
Figures from Agrawal et al, copyright IEEE 2015. Reproduced for educational purposes.

# Visual Dialog: Conversations about images

**Visual Dialog**



A cat drinking water out of a coffee mug.

What color is the mug?

White and red

Are there any pictures on it?

No, something is there can't tell what it is

Is the mug and cat on a table?

Yes, they are

Are there other items on the table?

Yes, magazines, books, toaster and basket, and a plate

Start typing question here ...

Das et al, "Visual Dialog", CVPR 2017  
Figures from Das et al, copyright IEEE 2017. Reproduced with permission.

# Visual Language Navigation: Go to the living room

Agent encodes instructions in language and uses an RNN to generate a series of movements as the visual input changes after each move.

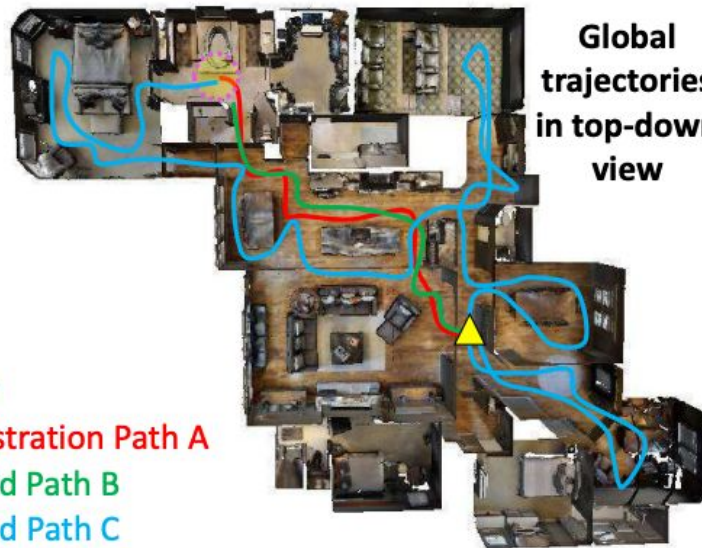
## Instruction

Turn right and head towards the *kitchen*. Then turn left, pass a *table* and enter the *hallway*. Walk down the hallway and turn into the *entry way* to your right *without doors*. Stop in front of the *toilet*.

## Local visual scene



## Global trajectories in top-down view



-  Initial Position
-  Target Position
-  Demonstration Path A
-  Executed Path B
-  Executed Path C

Wang et al, "Reinforced Cross-Modal Matching and Self-Supervised Imitation Learning for Vision-Language Navigation", CVPR 2018  
Figures from Wang et al, copyright IEEE 2017. Reproduced with permission.

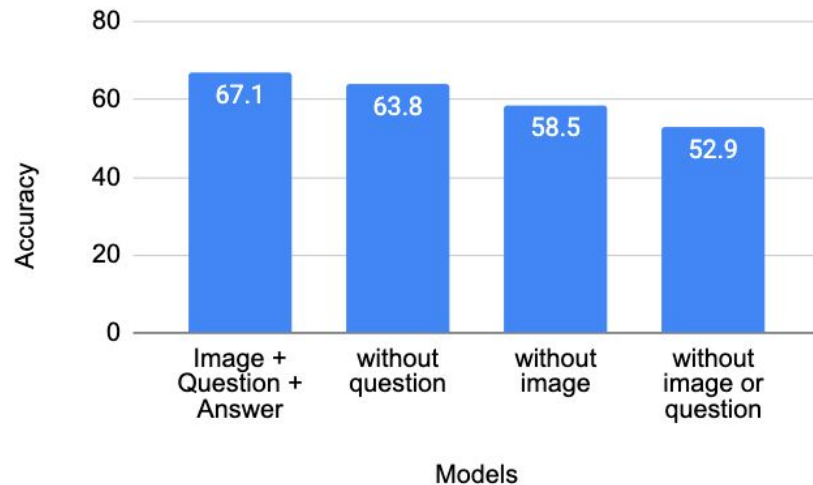
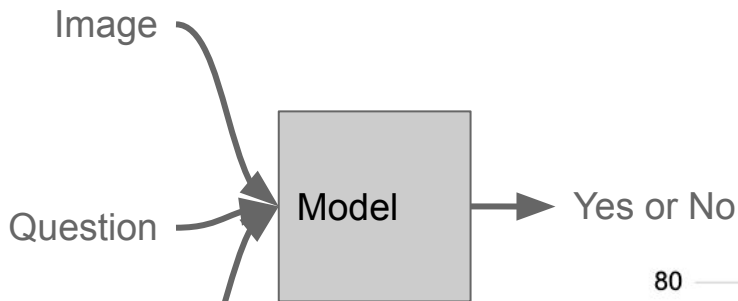


# Visual Question Answering: Dataset Bias



What is the dog playing with?

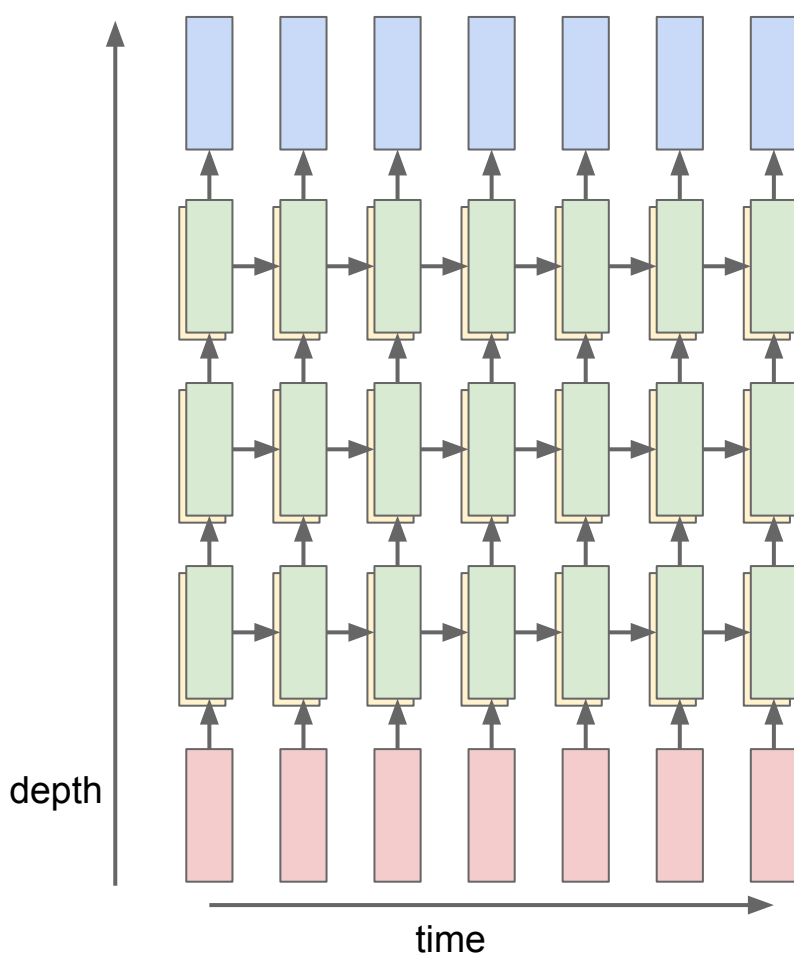
Frisbee



# Multilayer RNNs

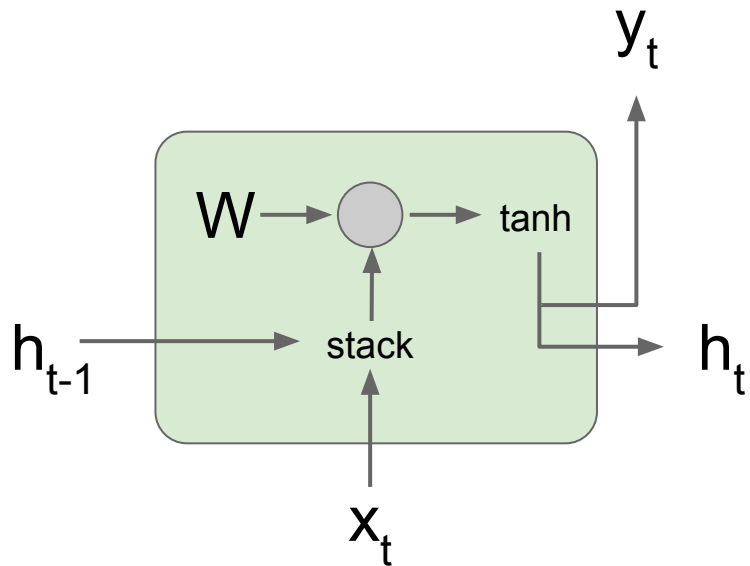
Each layer has a different set of weights

Outputs from one layer become inputs to the layer above.



# Vanilla RNN Gradient Flow

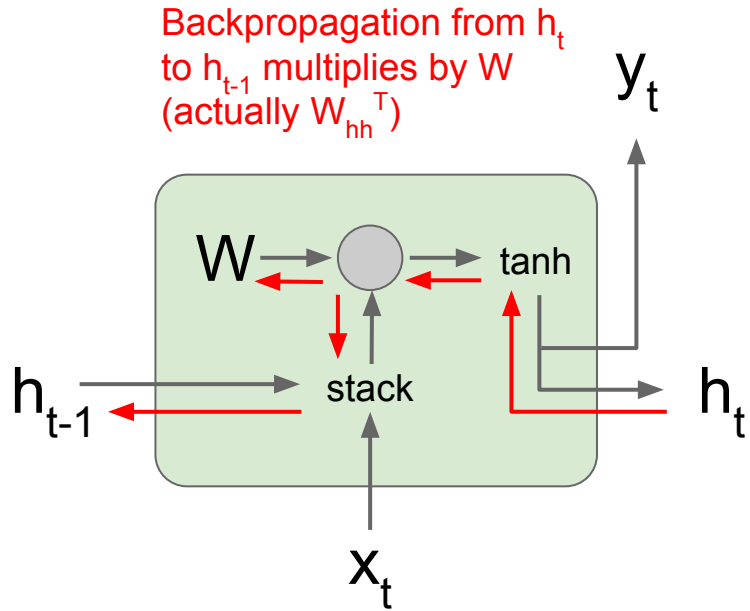
Bengio et al, "Learning long-term dependencies with gradient descent is difficult", IEEE Transactions on Neural Networks, 1994  
Pascanu et al, "On the difficulty of training recurrent neural networks", ICML 2013



$$\begin{aligned}h_t &= \tanh(W_{hh}h_{t-1} + W_{hx}x_t) \\ &= \tanh\left(\begin{pmatrix} W_{hh} & W_{hx} \end{pmatrix} \begin{pmatrix} h_{t-1} \\ x_t \end{pmatrix}\right) \\ &= \tanh\left(W \begin{pmatrix} h_{t-1} \\ x_t \end{pmatrix}\right)\end{aligned}$$

# Vanilla RNN Gradient Flow

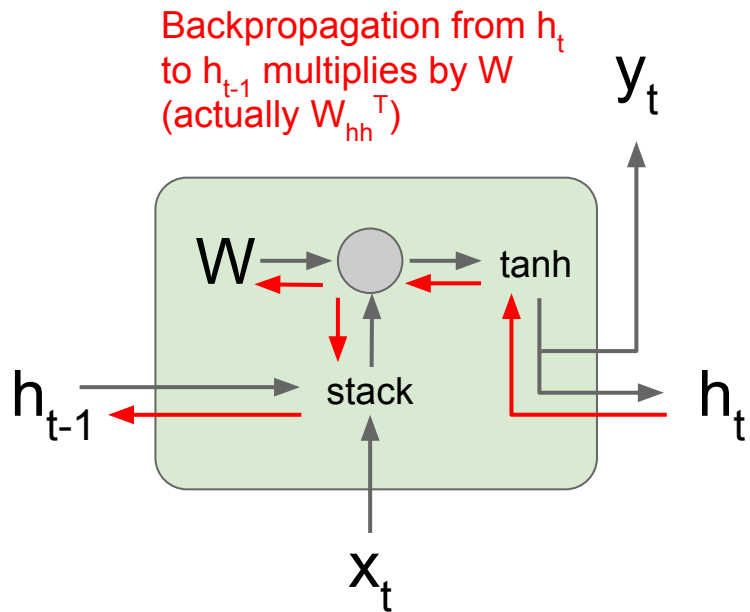
Bengio et al, "Learning long-term dependencies with gradient descent is difficult", IEEE Transactions on Neural Networks, 1994  
Pascanu et al, "On the difficulty of training recurrent neural networks", ICML 2013



$$\begin{aligned} h_t &= \tanh(W_{hh}h_{t-1} + W_{hx}x_t) \\ &= \tanh\left(\begin{pmatrix} W_{hh} & W_{hx} \end{pmatrix} \begin{pmatrix} h_{t-1} \\ x_t \end{pmatrix}\right) \\ &= \tanh\left(W \begin{pmatrix} h_{t-1} \\ x_t \end{pmatrix}\right) \end{aligned}$$

# Vanilla RNN Gradient Flow

Bengio et al, "Learning long-term dependencies with gradient descent is difficult", IEEE Transactions on Neural Networks, 1994  
Pascanu et al, "On the difficulty of training recurrent neural networks", ICML 2013

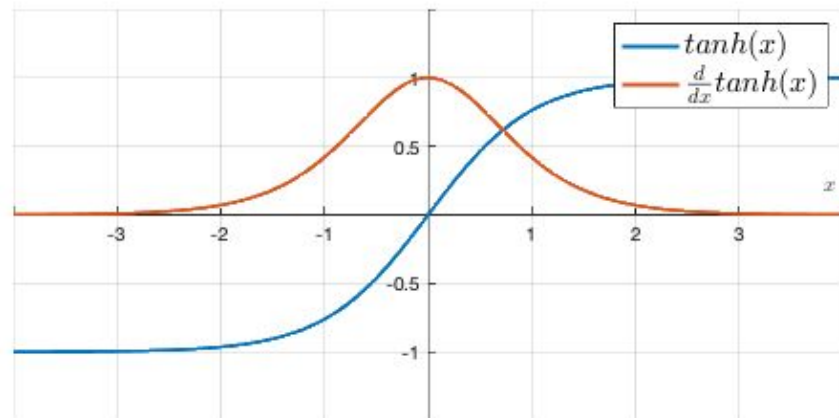
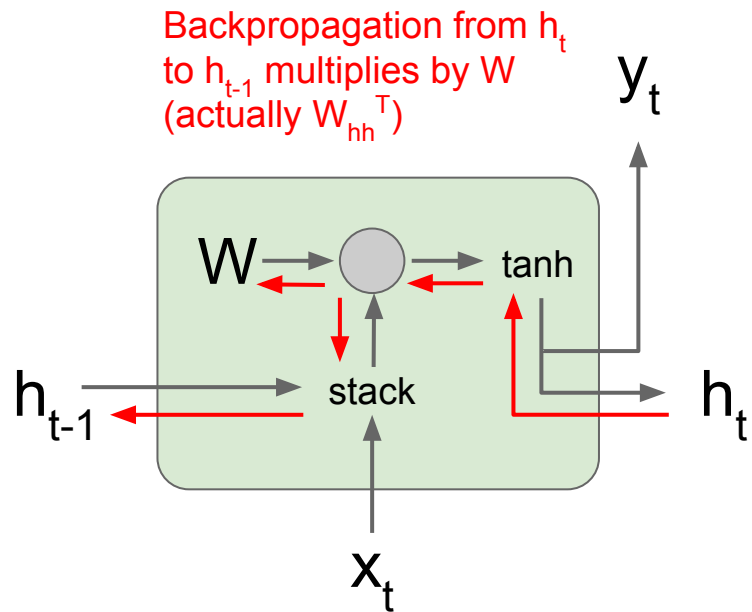


$$\begin{aligned}h_t &= \tanh(W_{hh}h_{t-1} + W_{xh}x_t) \\ &= \tanh\left(\begin{pmatrix} W_{hh} & W_{hx} \end{pmatrix} \begin{pmatrix} h_{t-1} \\ x_t \end{pmatrix}\right) \\ &= \tanh\left(W \begin{pmatrix} h_{t-1} \\ x_t \end{pmatrix}\right)\end{aligned}$$

$$\frac{\partial h_t}{\partial h_{t-1}} = \tanh'(W_{hh}h_{t-1} + W_{xh}x_t)W_{hh}$$

# Vanilla RNN Gradient Flow

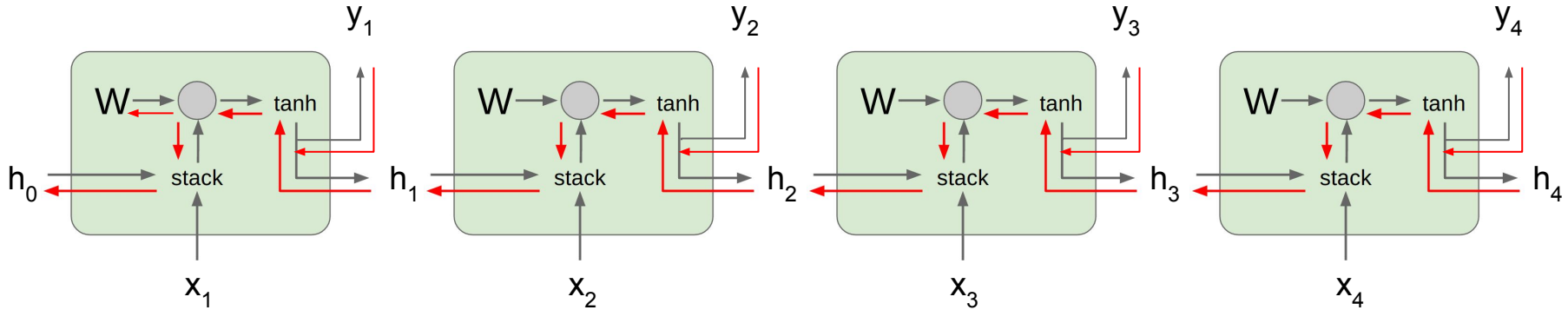
Bengio et al, "Learning long-term dependencies with gradient descent is difficult", IEEE Transactions on Neural Networks, 1994  
Pascanu et al, "On the difficulty of training recurrent neural networks", ICML 2013



$$\frac{\partial h_t}{\partial h_{t-1}} = \tanh'(W_{hh} h_{t-1} + W_{xh} x_t) W_{hh}$$

# Vanilla RNN Gradient Flow

Bengio et al, "Learning long-term dependencies with gradient descent is difficult", IEEE Transactions on Neural Networks, 1994  
Pascanu et al, "On the difficulty of training recurrent neural networks", ICML 2013

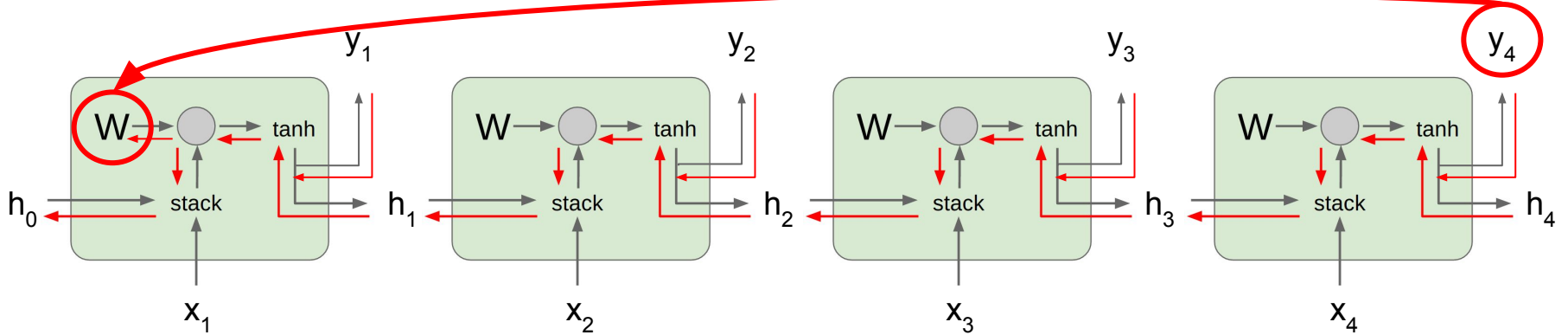


$$\frac{\partial L}{\partial W} = \sum_{t=1}^T \frac{\partial L_t}{\partial W}$$

# Vanilla RNN Gradient Flow

Gradients over multiple time steps:

Bengio et al, "Learning long-term dependencies with gradient descent is difficult", IEEE Transactions on Neural Networks, 1994  
Pascanu et al, "On the difficulty of training recurrent neural networks", ICML 2013



$$\frac{\partial L}{\partial W} = \sum_{t=1}^T \frac{\partial L_t}{\partial W}$$

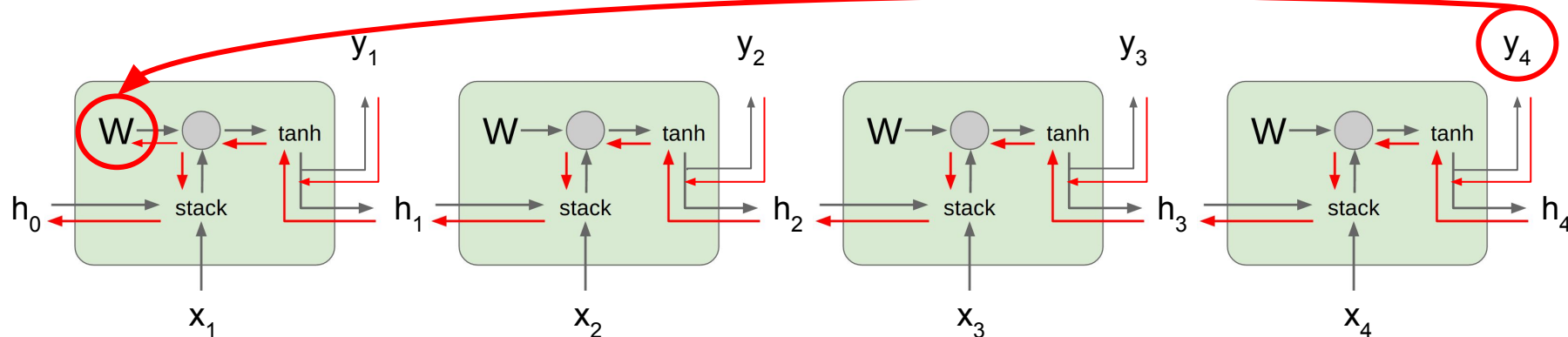
$$\frac{\partial L_T}{\partial W} = \frac{\partial L_T}{\partial h_T} \frac{\partial h_T}{\partial h_{T-1}} \cdots \frac{\partial h_1}{\partial W}$$



# Vanilla RNN Gradient Flow

Gradients over multiple time steps:

Bengio et al, "Learning long-term dependencies with gradient descent is difficult", IEEE Transactions on Neural Networks, 1994  
Pascanu et al, "On the difficulty of training recurrent neural networks", ICML 2013



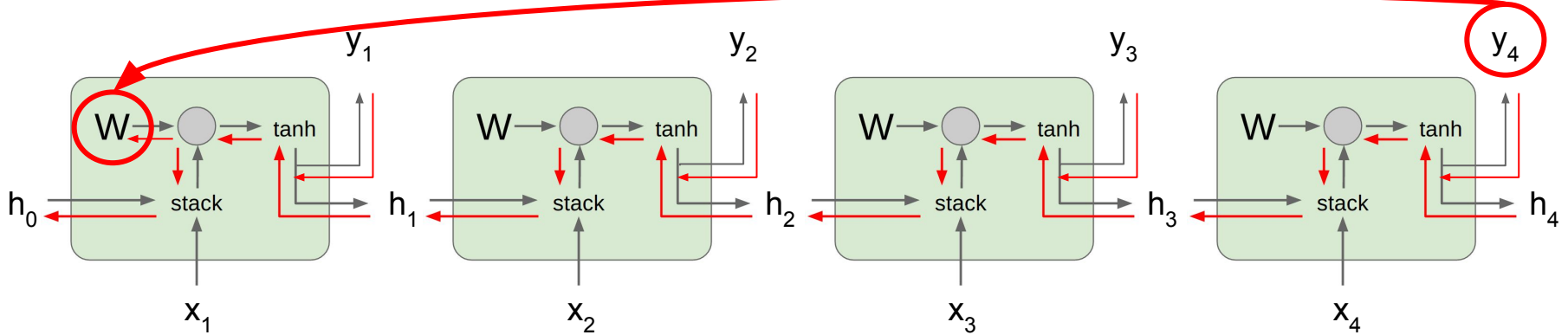
$$\frac{\partial L}{\partial W} = \sum_{t=1}^T \frac{\partial L_t}{\partial W}$$

$$\frac{\partial L_T}{\partial W} = \frac{\partial L_T}{\partial h_T} \frac{\partial h_T}{\partial h_{T-1}} \cdots \frac{\partial h_1}{\partial W} = \frac{\partial L_T}{\partial h_T} \left( \prod_{t=2}^T \frac{\partial h_t}{\partial h_{t-1}} \right) \frac{\partial h_1}{\partial W}$$

# Vanilla RNN Gradient Flow

Gradients over multiple time steps:

Bengio et al, "Learning long-term dependencies with gradient descent is difficult", IEEE Transactions on Neural Networks, 1994  
 Pascanu et al, "On the difficulty of training recurrent neural networks", ICML 2013



$$\frac{\partial L}{\partial W} = \sum_{t=1}^T \frac{\partial L_t}{\partial W}$$

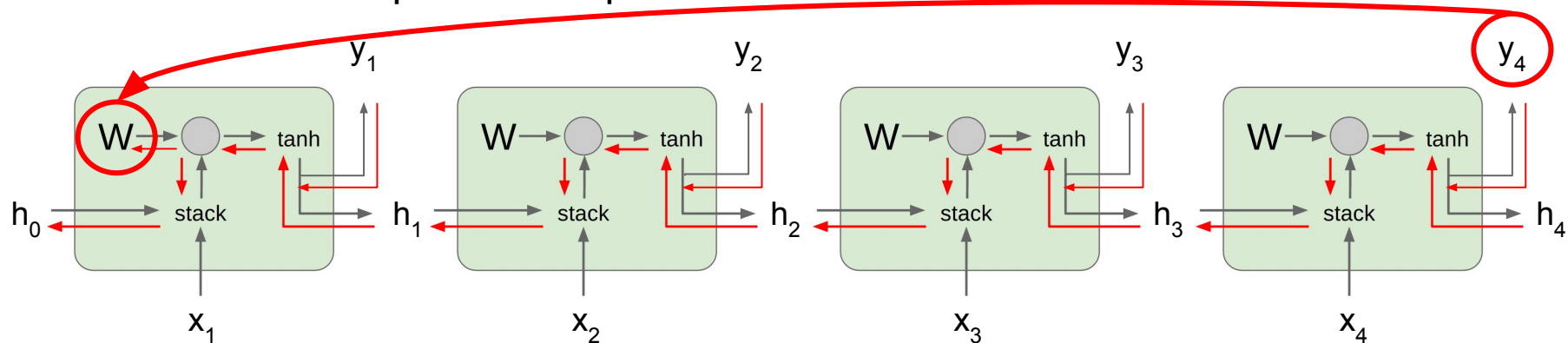
$$\frac{\partial h_t}{\partial h_{t-1}} = \tanh'(W_{hh} h_{t-1} + W_{xh} x_t) W_{hh}$$

$$\frac{\partial L_T}{\partial W} = \frac{\partial L_T}{\partial h_T} \frac{\partial h_T}{\partial h_{t-1}} \cdots \frac{\partial h_1}{\partial W} = \frac{\partial L_T}{\partial h_T} \left( \prod_{t=2}^T \frac{\partial h_t}{\partial h_{t-1}} \right) \frac{\partial h_1}{\partial W}$$

# Vanilla RNN Gradient Flow

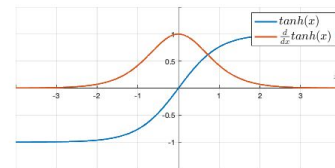
Gradients over multiple time steps:

Bengio et al, "Learning long-term dependencies with gradient descent is difficult", IEEE Transactions on Neural Networks, 1994  
 Pascanu et al, "On the difficulty of training recurrent neural networks", ICML 2013



$$\frac{\partial L}{\partial W} = \sum_{t=1}^T \frac{\partial L_t}{\partial W}$$

Almost always  $< 1$   
**Vanishing gradients**

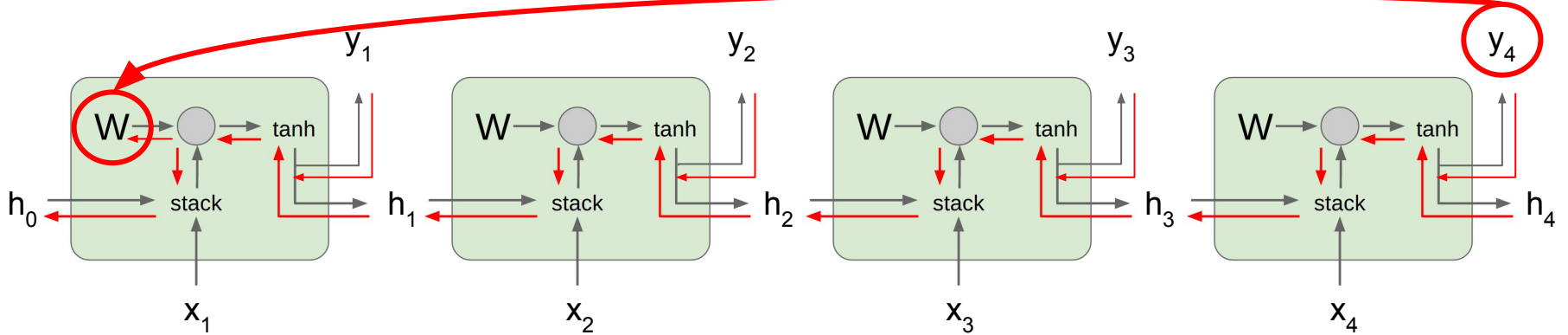


$$\frac{\partial L_T}{\partial W} = \frac{\partial L_T}{\partial h_T} \left( \prod_{t=2}^T \tanh'(W_{hh} h_{t-1} + W_{xh} x_t) \right) W_{hh}^{T-1} \frac{\partial h_1}{\partial W}$$

# Vanilla RNN Gradient Flow

Gradients over multiple time steps:

Bengio et al, "Learning long-term dependencies with gradient descent is difficult", IEEE Transactions on Neural Networks, 1994  
Pascanu et al, "On the difficulty of training recurrent neural networks", ICML 2013



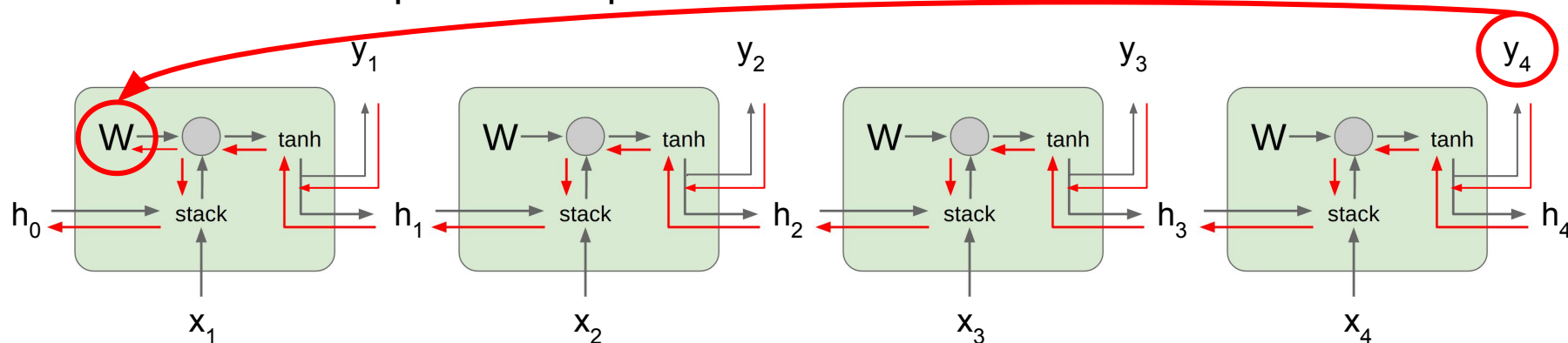
$$\frac{\partial L}{\partial W} = \sum_{t=1}^T \frac{\partial L_t}{\partial W}$$

What if we assumed no non-linearity?

# Vanilla RNN Gradient Flow

Gradients over multiple time steps:

Bengio et al, "Learning long-term dependencies with gradient descent is difficult", IEEE Transactions on Neural Networks, 1994  
 Pascanu et al, "On the difficulty of training recurrent neural networks", ICML 2013



What if we assumed no non-linearity?

$$\frac{\partial L}{\partial W} = \sum_{t=1}^T \frac{\partial L_t}{\partial W}$$

Largest singular value > 1:  
**Exploding gradients**

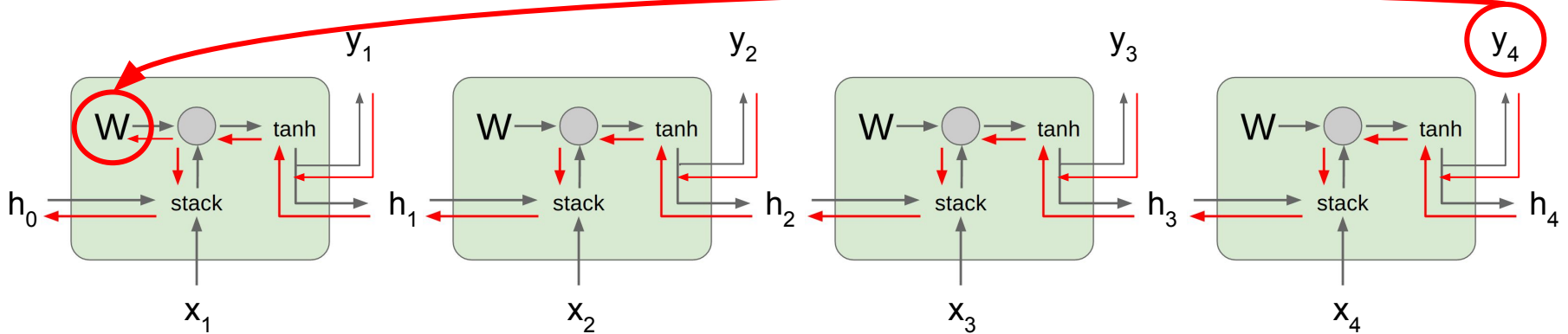
$$\frac{\partial L_T}{\partial W} = \frac{\partial L_T}{\partial h_T} \boxed{W_{hh}^{T-1}} \frac{\partial h_1}{\partial W}$$

Largest singular value < 1:  
**Vanishing gradients**

# Vanilla RNN Gradient Flow

Gradients over multiple time steps:

Bengio et al, "Learning long-term dependencies with gradient descent is difficult", IEEE Transactions on Neural Networks, 1994  
 Pascanu et al, "On the difficulty of training recurrent neural networks", ICML 2013



What if we assumed no non-linearity?

$$\frac{\partial L}{\partial W} = \sum_{t=1}^T \frac{\partial L_t}{\partial W}$$

$$\frac{\partial L_T}{\partial W} = \frac{\partial L_T}{\partial h_T} \boxed{W_{hh}^{T-1}} \frac{\partial h_1}{\partial W}$$

Largest singular value > 1:  
**Exploding gradients**

Largest singular value < 1:  
**Vanishing gradients**

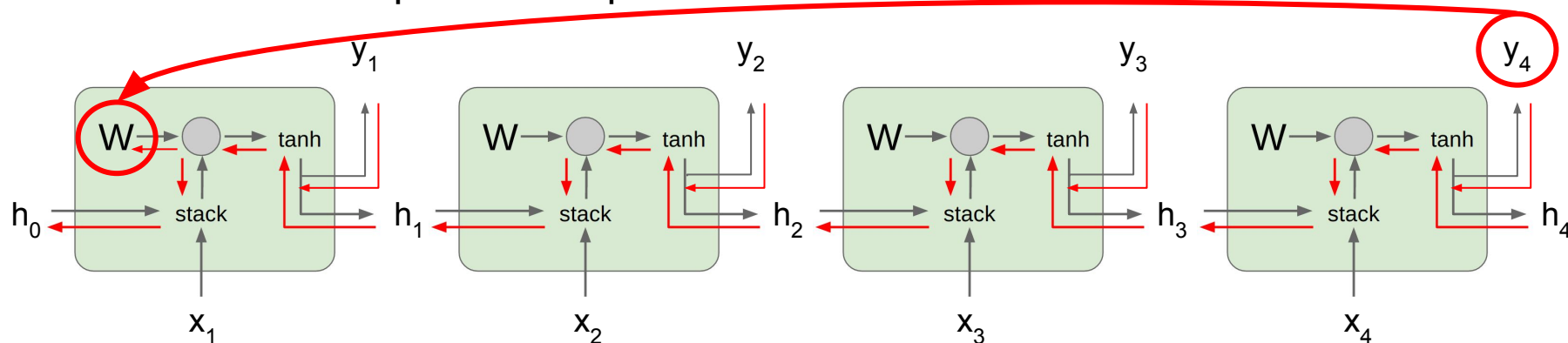
**Gradient clipping:**  
 Scale gradient if its norm is too big

```
grad_norm = np.sum(grad * grad)
if grad_norm > threshold:
    grad *= (threshold / grad_norm)
```

# Vanilla RNN Gradient Flow

Gradients over multiple time steps:

Bengio et al, "Learning long-term dependencies with gradient descent is difficult", IEEE Transactions on Neural Networks, 1994  
 Pascanu et al, "On the difficulty of training recurrent neural networks", ICML 2013



What if we assumed no non-linearity?

$$\frac{\partial L}{\partial W} = \sum_{t=1}^T \frac{\partial L_t}{\partial W}$$

Largest singular value > 1:  
**Exploding gradients**

$$\frac{\partial L_T}{\partial W} = \frac{\partial L_T}{\partial h_T} \boxed{W_{hh}^{T-1}} \frac{\partial h_1}{\partial W}$$

Largest singular value < 1:  
**Vanishing gradients**

→ Change RNN architecture

# Long Short Term Memory (LSTM)

## Vanilla RNN

$$h_t = \tanh \left( W \begin{pmatrix} h_{t-1} \\ x_t \end{pmatrix} \right)$$

## LSTM

$$\begin{pmatrix} i \\ f \\ o \\ g \end{pmatrix} = \begin{pmatrix} \sigma \\ \sigma \\ \sigma \\ \tanh \end{pmatrix} W \begin{pmatrix} h_{t-1} \\ x_t \end{pmatrix}$$
$$c_t = f \odot c_{t-1} + i \odot g$$
$$h_t = o \odot \tanh(c_t)$$

Hochreiter and Schmidhuber, "Long Short Term Memory", Neural Computation 1997



RNNs have a single hidden state ( $h_t$ )

LSTMs have two: **cell memory**  $c_t$  and hidden state  $h_t$

## Vanilla RNN

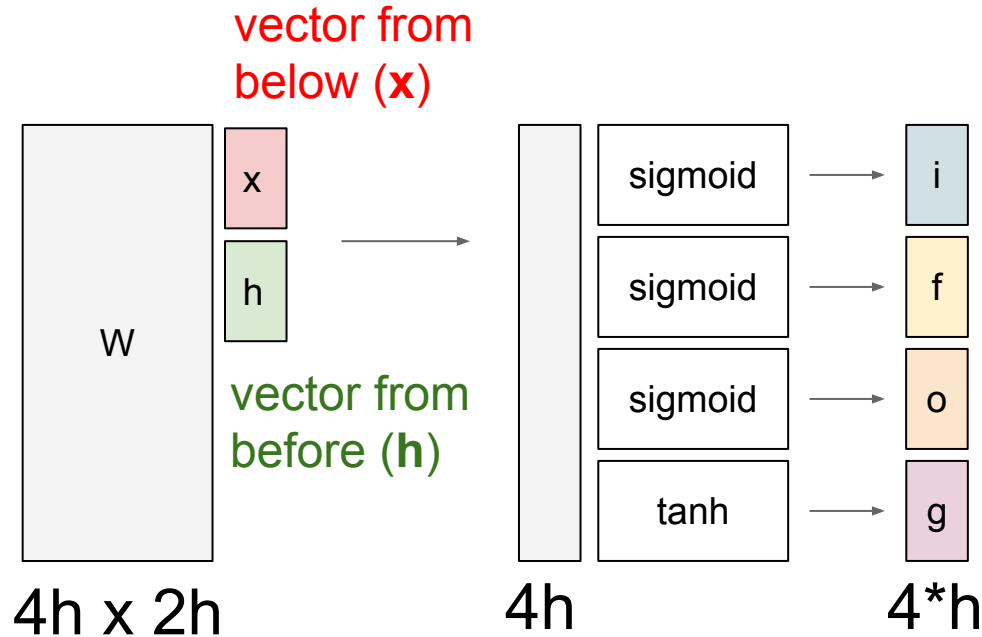
$$h_t = \tanh \left( W \begin{pmatrix} h_{t-1} \\ x_t \end{pmatrix} \right)$$

## LSTM

$$\begin{pmatrix} i \\ f \\ o \\ g \end{pmatrix} = \begin{pmatrix} \sigma \\ \sigma \\ \sigma \\ \tanh \end{pmatrix} W \begin{pmatrix} h_{t-1} \\ x_t \end{pmatrix}$$
$$c_t = f \odot c_{t-1} + i \odot g$$
$$h_t = o \odot \tanh(c_t)$$

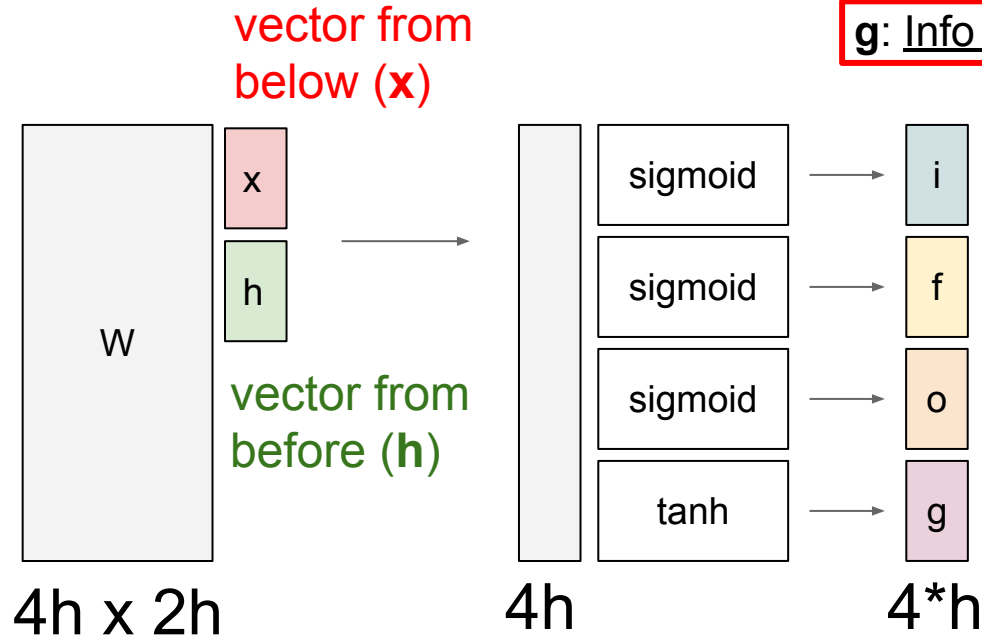
# Long Short Term Memory (LSTM)

[Hochreiter et al., 1997]



# Long Short Term Memory (LSTM)

[Hochreiter et al., 1997]



$g$ : Info gate, How much to write to cell

$$\begin{pmatrix} i \\ f \\ o \\ g \end{pmatrix} = \begin{pmatrix} \sigma \\ \sigma \\ \sigma \\ \tanh \end{pmatrix} W \begin{pmatrix} h_{t-1} \\ x_t \end{pmatrix}$$

$$c_t = f \odot c_{t-1} + i \odot g$$

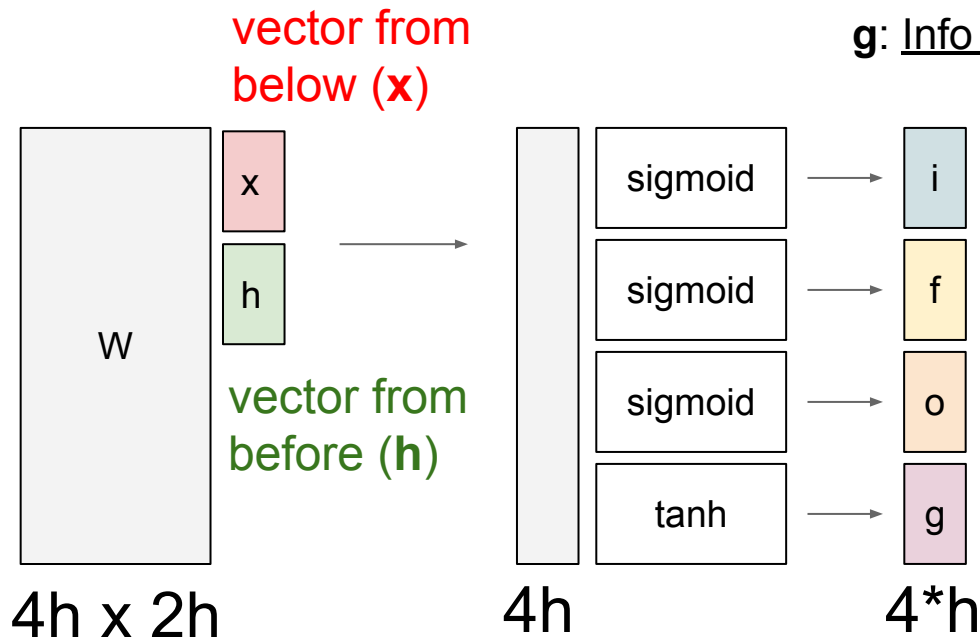
$$h_t = o \odot \tanh(c_t)$$

# Long Short Term Memory (LSTM)

[Hochreiter et al., 1997]

i: Input gate, whether to write to cell

g: Info gate, How much to write to cell



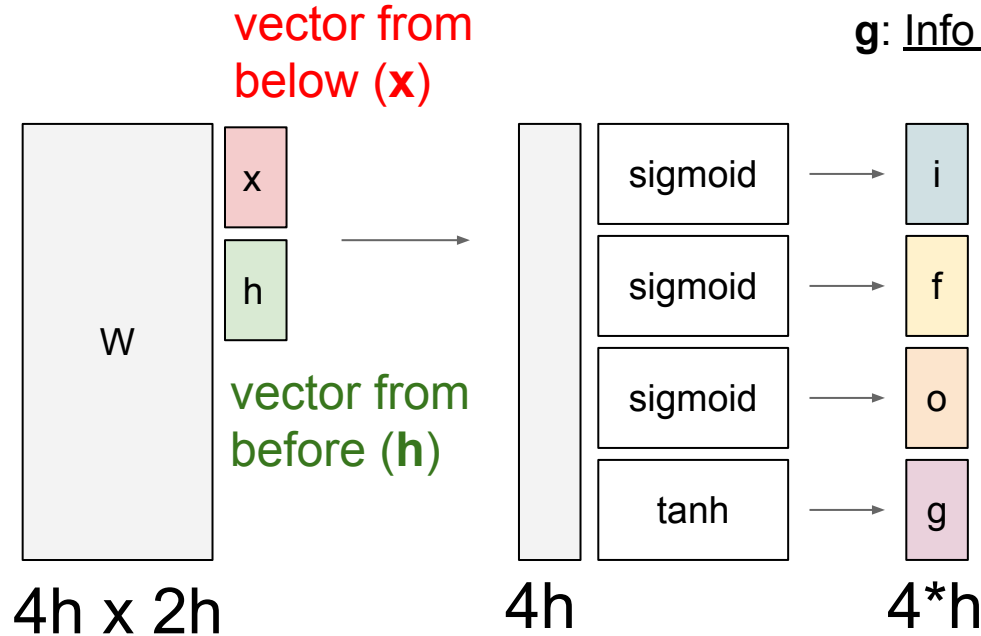
$$\begin{pmatrix} i \\ f \\ o \\ g \end{pmatrix} = \begin{pmatrix} \sigma \\ \sigma \\ \sigma \\ \tanh \end{pmatrix} W \begin{pmatrix} h_{t-1} \\ x_t \end{pmatrix}$$

$$c_t = f \odot c_{t-1} + i \odot g$$

$$h_t = o \odot \tanh(c_t)$$

# Long Short Term Memory (LSTM)

[Hochreiter et al., 1997]



$i$ : Input gate, whether to write to cell

$f$ : Forget gate, Whether to erase cell

$g$ : Info gate, How much to write to cell

$$\begin{pmatrix} i \\ f \\ o \\ g \end{pmatrix} = \begin{pmatrix} \sigma \\ \sigma \\ \sigma \\ \tanh \end{pmatrix} W \begin{pmatrix} h_{t-1} \\ x_t \end{pmatrix}$$

$$c_t = f \odot c_{t-1} + i \odot g$$

$$h_t = o \odot \tanh(c_t)$$

# Long Short Term Memory (LSTM)

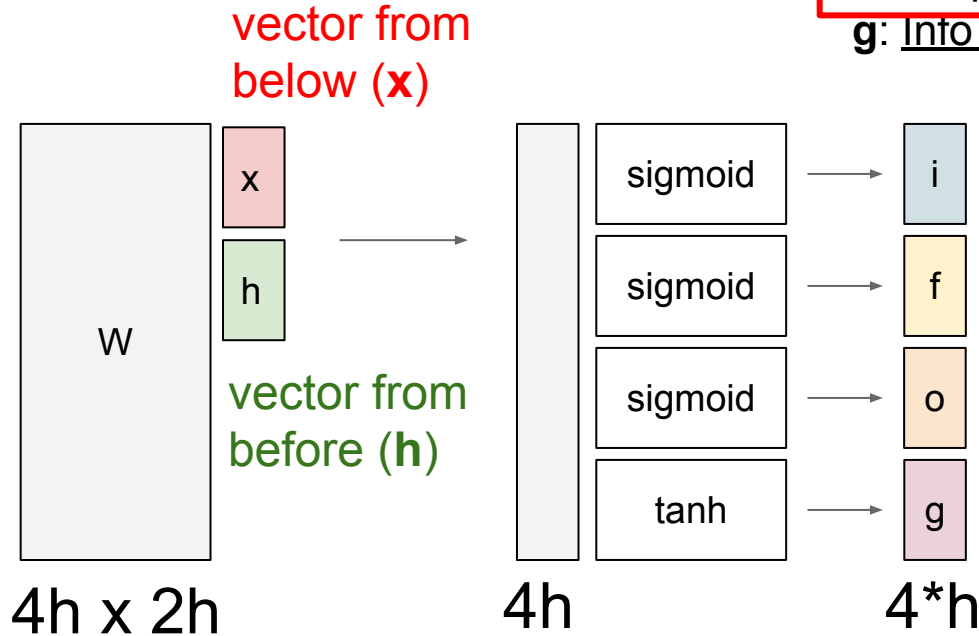
[Hochreiter et al., 1997]

i: Input gate, whether to write to cell

f: Forget gate, Whether to erase cell

o: Output gate, How much to reveal cell

g: Info gate, How much to write to cell



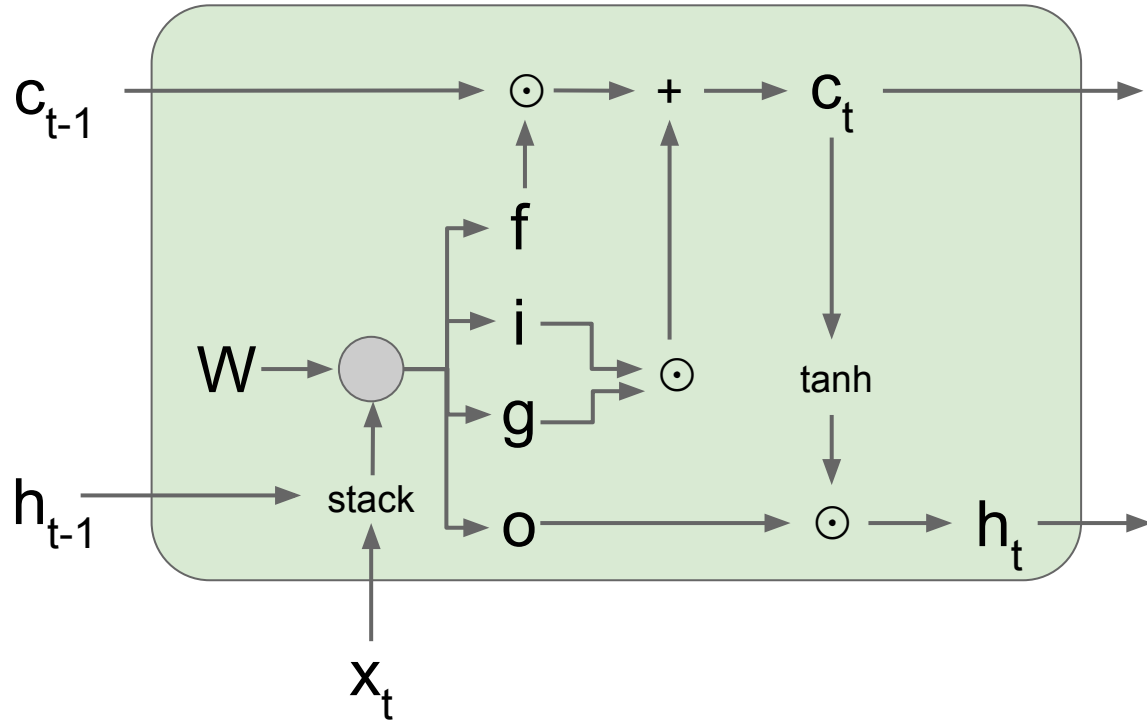
$$\begin{pmatrix} i \\ f \\ o \\ g \end{pmatrix} = \begin{pmatrix} \sigma \\ \sigma \\ \sigma \\ \tanh \end{pmatrix} W \begin{pmatrix} h_{t-1} \\ x_t \end{pmatrix}$$

$$c_t = f \odot c_{t-1} + i \odot g$$

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# Long Short Term Memory (LSTM)

[Hochreiter et al., 1997]



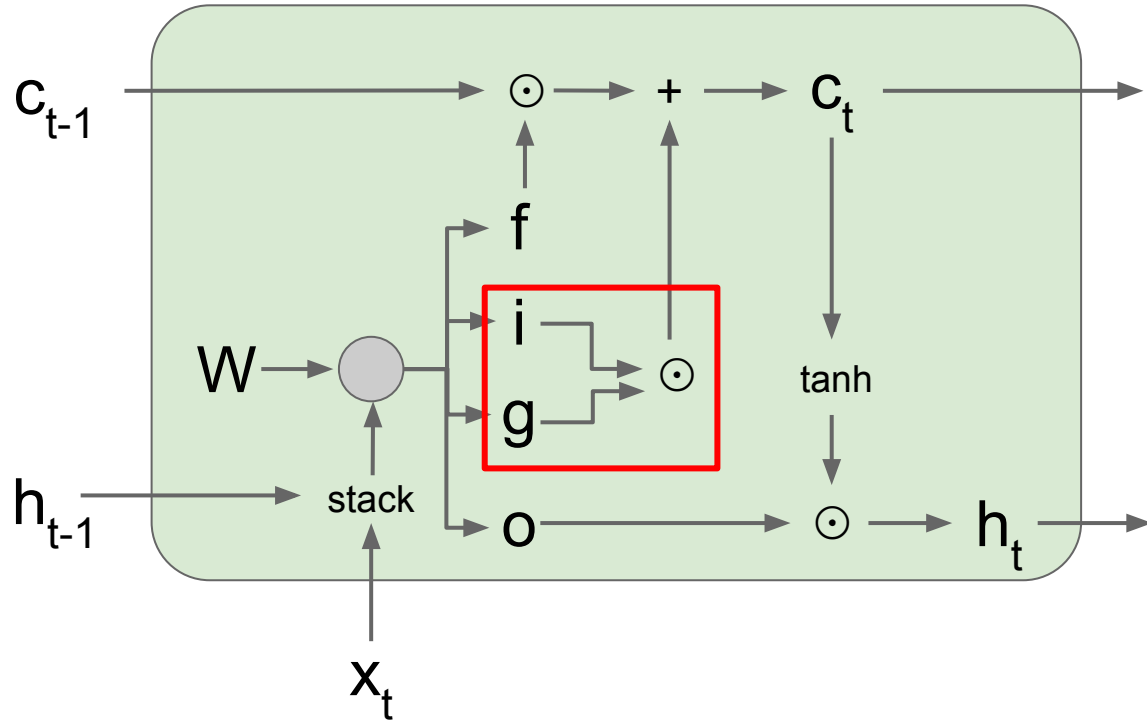
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# Long Short Term Memory (LSTM)

[Hochreiter et al., 1997]



$$\begin{pmatrix} i \\ f \\ o \\ g \end{pmatrix} = \begin{pmatrix} \sigma \\ \sigma \\ \sigma \\ \tanh \end{pmatrix} W \begin{pmatrix} h_{t-1} \\ x_t \end{pmatrix}$$

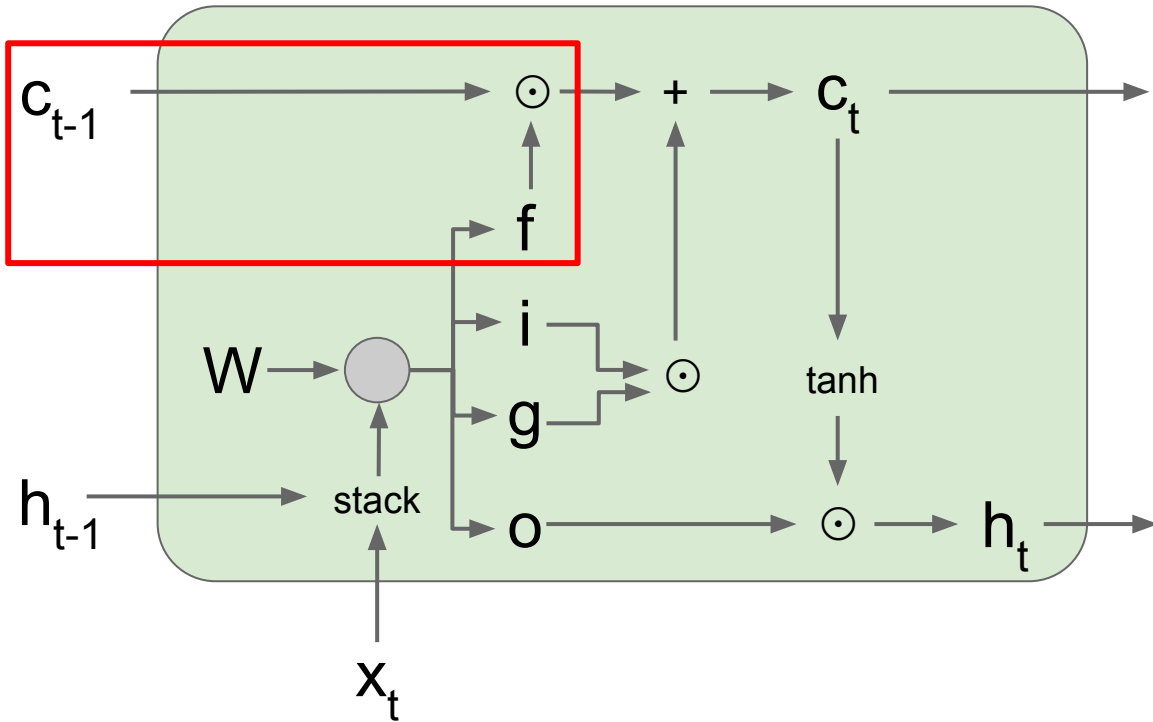
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# Long Short Term Memory (LSTM)

[Hochreiter et al., 1997]



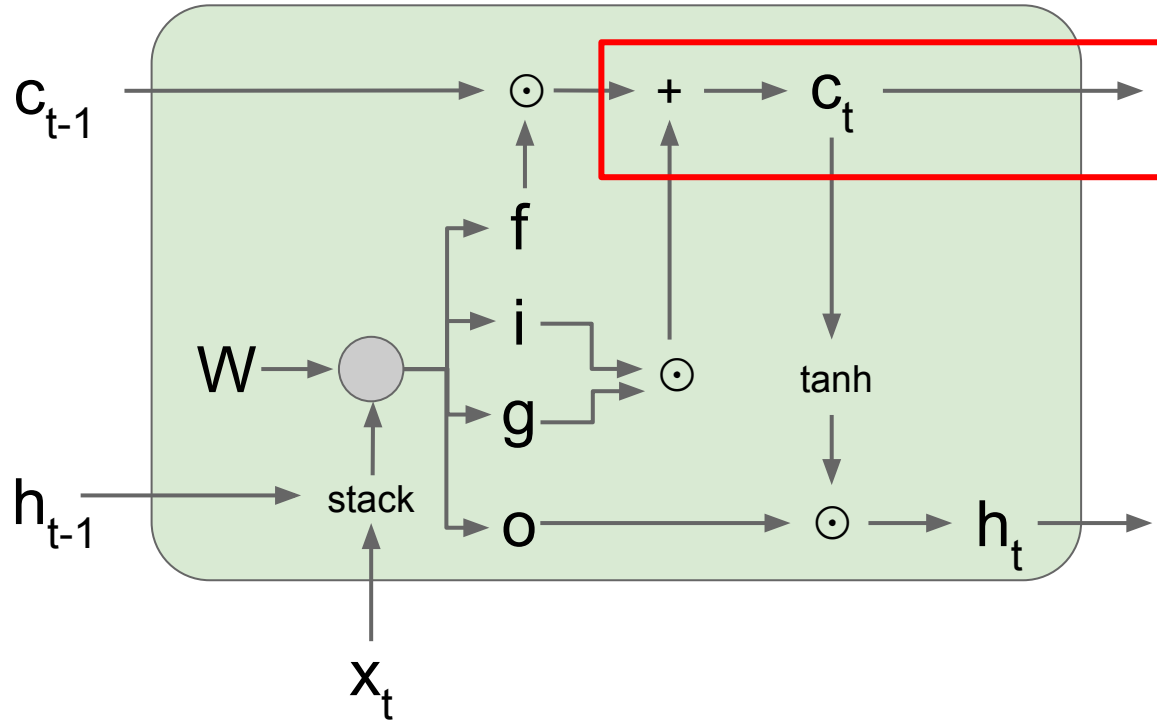
$$\begin{pmatrix} i \\ f \\ o \\ g \end{pmatrix} = \begin{pmatrix} \sigma \\ \sigma \\ \sigma \\ \tanh \end{pmatrix} W \begin{pmatrix} h_{t-1} \\ x_t \end{pmatrix}$$

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# Long Short Term Memory (LSTM)

[Hochreiter et al., 1997]



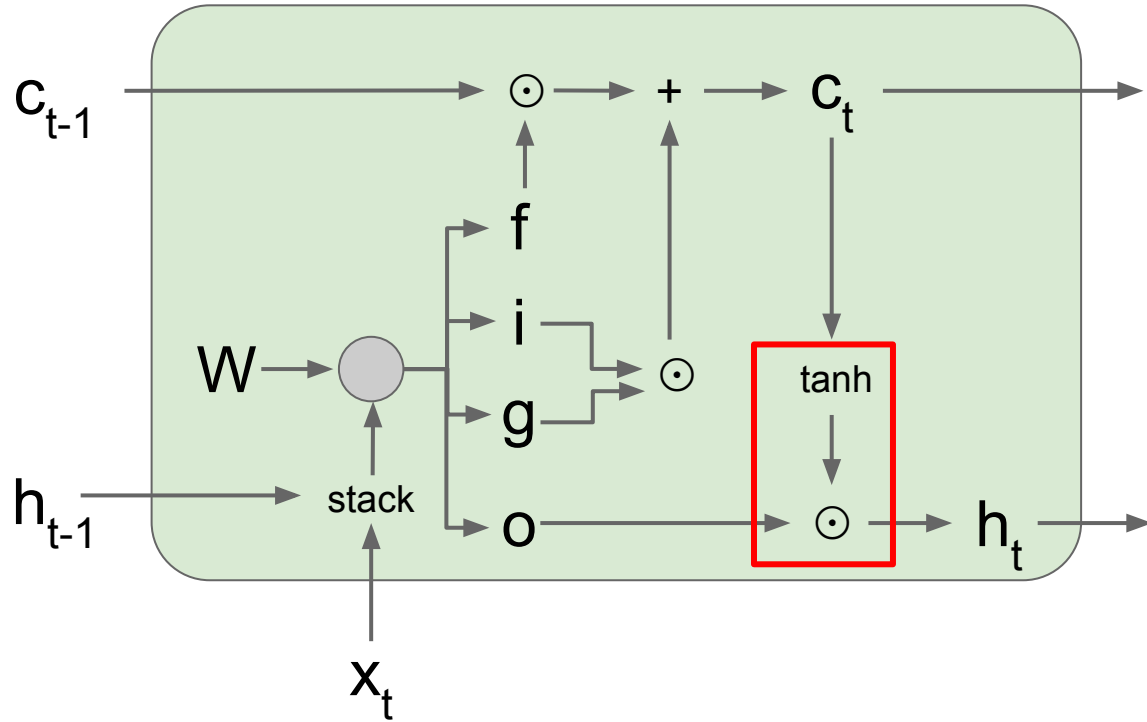
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# Long Short Term Memory (LSTM)

[Hochreiter et al., 1997]



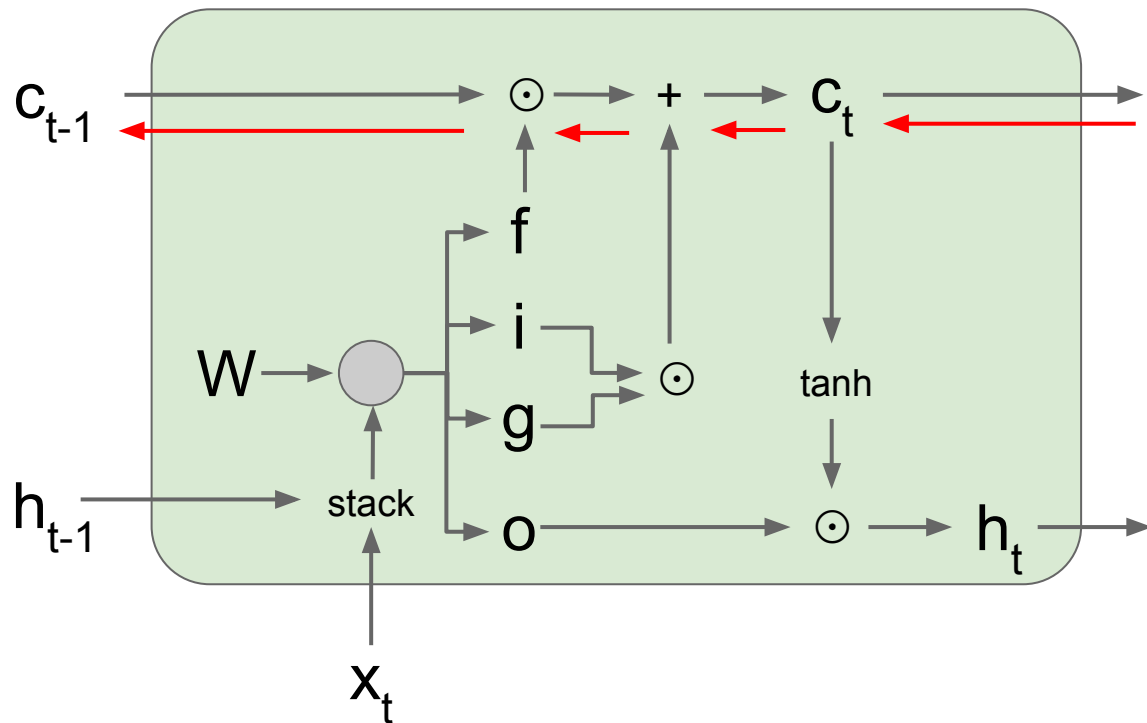
$$\begin{pmatrix} i \\ f \\ o \\ g \end{pmatrix} = \begin{pmatrix} \sigma \\ \sigma \\ \sigma \\ \tanh \end{pmatrix} W \begin{pmatrix} h_{t-1} \\ x_t \end{pmatrix}$$

$$c_t = f \odot c_{t-1} + i \odot g$$

$$h_t = o \odot \tanh(c_t)$$

# Long Short Term Memory (LSTM): Gradient Flow

[Hochreiter et al., 1997]



Backpropagation from  $c_t$  to  $c_{t-1}$  only elementwise multiplication by  $f$ , no matrix multiply by  $W$

$$\begin{pmatrix} i \\ f \\ o \\ g \end{pmatrix} = \begin{pmatrix} \sigma \\ \sigma \\ \sigma \\ \tanh \end{pmatrix} W \begin{pmatrix} h_{t-1} \\ x_t \end{pmatrix}$$

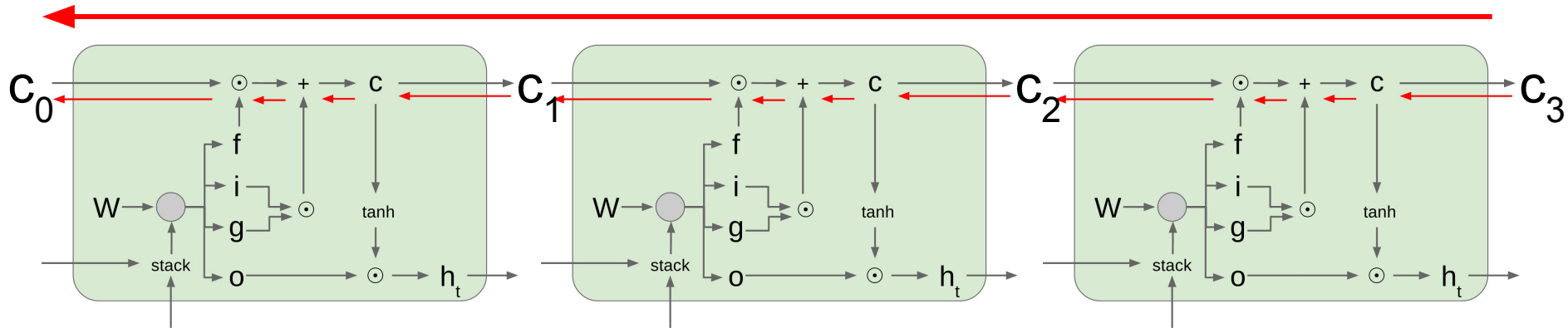
$$c_t = f \odot c_{t-1} + i \odot g$$

$$h_t = o \odot \tanh(c_t)$$

# Long Short Term Memory (LSTM): Gradient Flow

[Hochreiter et al., 1997]

Uninterrupted gradient flow!



Notice that the gradient contains the **f** gate's vector of activations

- allows better control of gradients values, using suitable parameter updates of the forget gate.

Also notice that are added through the **f**, **i**, **g**, and **o** gates

- better balancing of gradient values

# Do LSTMs solve the vanishing gradient problem?

The LSTM architecture makes it easier for the RNN to preserve information over many timesteps

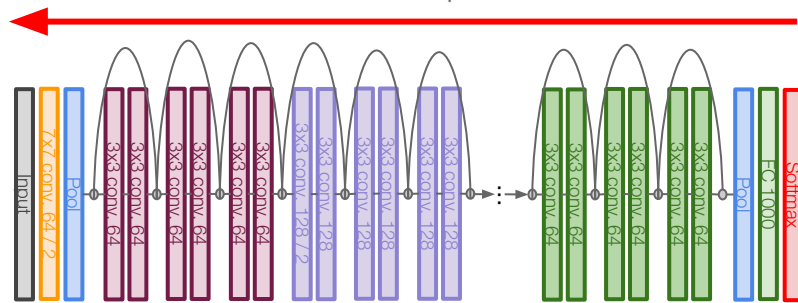
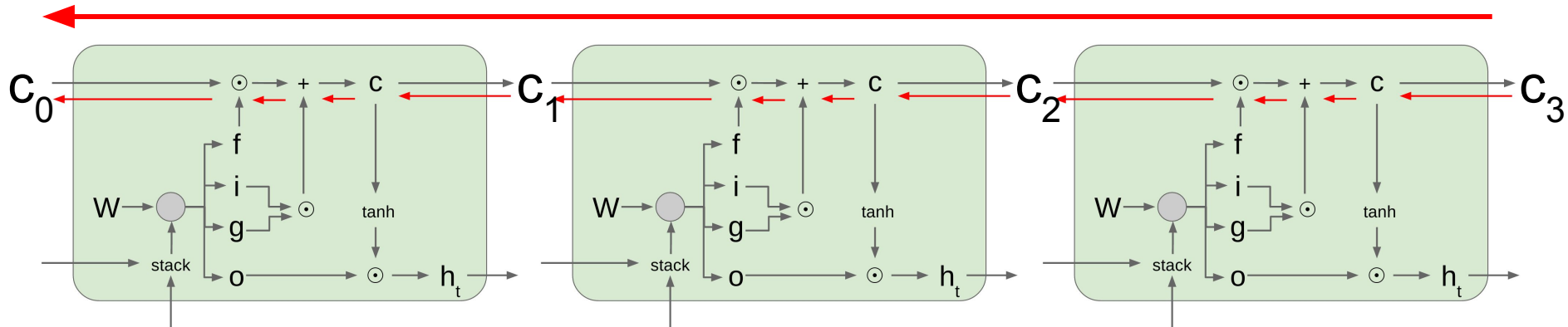
- e.g. **if the  $f = 1$  and the  $i = 0$** , then the information of that cell is preserved indefinitely.
- By contrast, it's harder for vanilla RNN to learn a recurrent weight matrix  $W_h$  that preserves info in hidden state

LSTM **doesn't guarantee** that there is no vanishing/exploding gradient, but it does provide an easier way for the model to learn long-distance dependencies

# Long Short Term Memory (LSTM): Gradient Flow

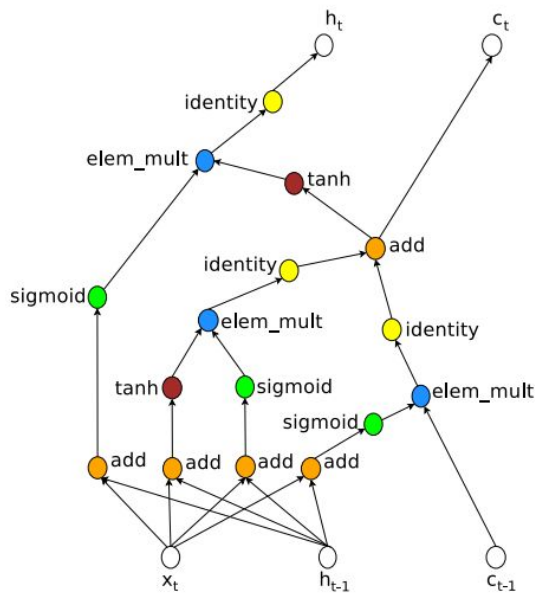
[Hochreiter et al., 1997]

## Uninterrupted gradient flow!

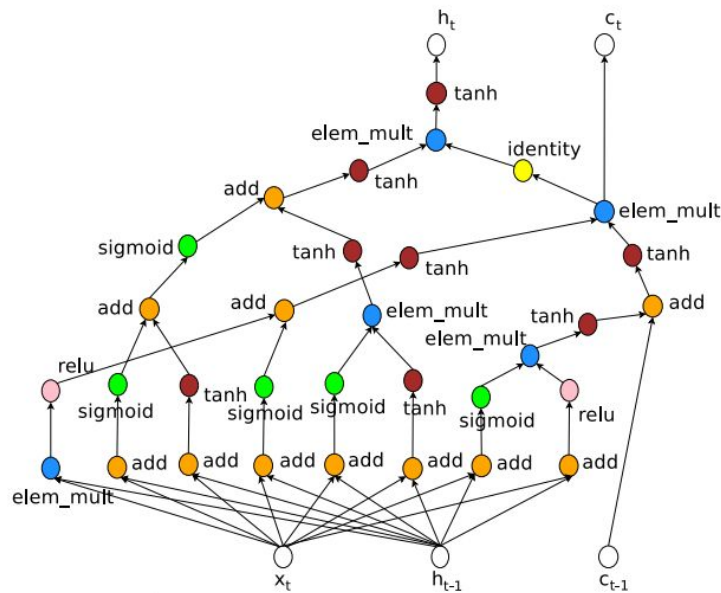


Similar to residual connections (e.g. in ResNets and Transformers), which we will learn about soon!

# Neural Architecture Search for RNN architectures



LSTM cell



Cell they found

Zoph et al, "Neural Architecture Search with Reinforcement Learning", ICLR 2017  
Figures copyright Zoph et al, 2017. Reproduced with permission.



# Other RNN Variants

**GRU** [*Learning phrase representations using rnn encoder-decoder for statistical machine translation*, Cho et al. 2014]

$$r_t = \sigma(W_{xr}x_t + W_{hr}h_{t-1} + b_r)$$

$$z_t = \sigma(W_{xz}x_t + W_{hz}h_{t-1} + b_z)$$

$$\tilde{h}_t = \tanh(W_{xh}x_t + W_{hh}(r_t \odot h_{t-1}) + b_h)$$

$$h_t = z_t \odot h_{t-1} + (1 - z_t) \odot \tilde{h}_t$$

[*LSTM: A Search Space Odyssey*, Greff et al., 2015]

[*An Empirical Exploration of Recurrent Network Architectures*, Jozefowicz et al., 2015]

MUT1:

$$z = \text{sigm}(W_{xz}x_t + b_z)$$

$$r = \text{sigm}(W_{xr}x_t + W_{hr}h_t + b_r)$$

$$h_{t+1} = \tanh(W_{hh}(r \odot h_t) + \tanh(x_t) + b_h) \odot z + h_t \odot (1 - z)$$

MUT2:

$$z = \text{sigm}(W_{xz}x_t + W_{hz}h_t + b_z)$$

$$r = \text{sigm}(x_t + W_{hr}h_t + b_r)$$

$$h_{t+1} = \tanh(W_{hh}(r \odot h_t) + W_{xh}x_t + b_h) \odot z + h_t \odot (1 - z)$$

MUT3:

$$z = \text{sigm}(W_{xz}x_t + W_{hz} \tanh(h_t) + b_z)$$

$$r = \text{sigm}(W_{xr}x_t + W_{hr}h_t + b_r)$$

$$h_{t+1} = \tanh(W_{hh}(r \odot h_t) + W_{xh}x_t + b_h) \odot z + h_t \odot (1 - z)$$

# Recurrence for Vision

- LSTM were a good default choice until this year
- Use variants like GRU if you want faster compute and less parameters
- Use transformers (next lecture) as they are dominating NLP and also vision models
  - almost everyday there is a new transformer model

Su et al. "Vi-bert: Pre-training of generic visual-linguistic representations." ICLR 2020

Lu et al. "Vilbert: Pretraining task-agnostic visiolinguistic representations for vision-and-language tasks." NeurIPS 2019

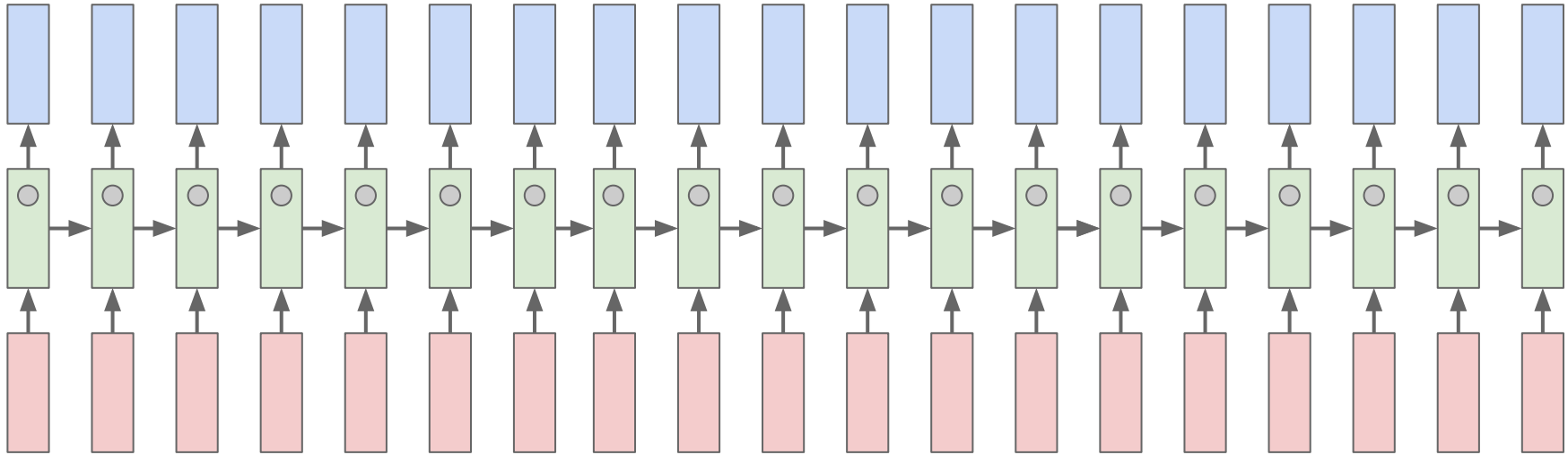
Li et al. "Visualbert: A simple and performant baseline for vision and language." *arXiv* 2019

# Summary

- RNNs allow a lot of flexibility in architecture design
- Vanilla RNNs are simple but don't work very well
- Common to use LSTM or GRU: their additive interactions improve gradient flow
- Backward flow of gradients in RNN can explode or vanish. Exploding is controlled with gradient clipping. Vanishing is controlled with additive interactions (LSTM)
- Better/simpler architectures are a hot topic of current research, as well as new paradigms for reasoning over sequences
- Better understanding (both theoretical and empirical) is needed.

Next time: Attention and transformers!

# Searching for interpretable cells



# Searching for interpretable cells

```
/* Unpack a filter field's string representation from user-space
 * buffer. */
char *audit_unpack_string(void **bufp, size_t *remain, size_t len)
{
    char *str;
    if (!*bufp || (len == 0) || (len > *remain))
        return ERR_PTR(-EINVAL);
    /* Of the currently implemented string fields, PATH_MAX
     * defines the longest valid length.
     */
}
```

Karpathy, Johnson, and Fei-Fei: Visualizing and Understanding Recurrent Networks, ICLR Workshop 2016  
Figures copyright Karpathy, Johnson, and Fei-Fei, 2015; reproduced with permission

# Searching for interpretable cells

"You mean to imply that I have nothing to eat out of.... On the contrary, I can supply you with everything even if you want to give dinner parties," warmly replied Chichagov, who tried by every word he spoke to prove his own rectitude and therefore imagined Kutuzov to be animated by the same desire.

Kutuzov, shrugging his shoulders, replied with his subtle penetrating smile: "I meant merely to say what I said."

quote detection cell

Karpathy, Johnson, and Fei-Fei: Visualizing and Understanding Recurrent Networks, ICLR Workshop 2016  
Figures copyright Karpathy, Johnson, and Fei-Fei, 2015; reproduced with permission

# Searching for interpretable cells

Cell sensitive to position in line:

The sole importance of the crossing of the Berezina lies in the fact that it plainly and indubitably proved the fallacy of all the plans for cutting off the enemy's retreat and the soundness of the only possible line of action--the one Kutuzov and the general mass of the army demanded--namely, simply to follow the enemy up. The French crowd fled at a continually increasing speed and all its energy was directed to reaching its goal. It fled like a wounded animal and it was impossible to block its path. This was shown not so much by the arrangements it made for crossing as by what took place at the bridges. When the bridges broke down, unarmed soldiers, people from Moscow and women with children who were with the French transport, all--carried on by vis inertiae--pressed forward into boats and into the ice-covered water and did not, surrender.

line length tracking cell

Karpathy, Johnson, and Fei-Fei: Visualizing and Understanding Recurrent Networks, ICLR Workshop 2016  
Figures copyright Karpathy, Johnson, and Fei-Fei, 2015; reproduced with permission



# Searching for interpretable cells

```
static int __dequeue_signal(struct sigpending *pending, sigset_t *mask,
                           siginfo_t *info)
{
    int sig = next_signal(pending, mask);
    if (sig) {
        if (current->notifier) {
            if (sigismember(current->notifier_mask, sig)) {
                if (!(current->notifier)(current->notifier_data)) {
                    clear_thread_flag(TIF_SIGPENDING);
                    return 0;
                }
            }
        }
        collect_signal(sig, pending, info);
    }
    return sig;
}
```

if statement cell

# Searching for interpretable cells

Cell that turns on inside comments and quotes:

```
/* Duplicate LSM field information. The lsm_rule is opaque, so
 * re-initialized. */
static inline int audit_dupe_lsm_field(struct audit_field *df,
                                     struct audit_field *sf)
{
    int ret = 0;
    char *lsm_str;
    /* our own copy of lsm_str */
    lsm_str = kstrdup(sf->lsm_str, GFP_KERNEL);
    if (unlikely(!lsm_str))
        return -ENOMEM;
    df->lsm_str = lsm_str;
    /* our own (refreshed) copy of lsm_rule */
    ret = security_audit_rule_init(df->type, df->op, df->lsm_str,
                                  (void *)&df->lsm_rule);
    /* Keep currently invalid fields around in case they
     * become valid after a policy reload. */
    if (ret == -EINVAL) {
        pr_warn("audit rule for LSM '%s' is invalid\n",
                df->lsm_str);
        ret = 0;
    }
    return ret;
}
```

quote/comment cell

Karpathy, Johnson, and Fei-Fei: Visualizing and Understanding Recurrent Networks, ICLR Workshop 2016

Figures copyright Karpathy, Johnson, and Fei-Fei, 2015; reproduced with permission

# Searching for interpretable cells

```
#ifdef CONFIG_AUDITSYSCALL
static inline int audit_match_class_bits(int class, u32 *mask)
{
    int i;
    if (classes[class]) {
        for (i = 0; i < AUDIT_BITMASK_SIZE; i++)
            if (mask[i] & classes[class][i])
                return 0;
    }
    return 1;
}
```

code depth cell