## Lecture 5: Convolutional Neural Networks

#### Who am I?

#### **Aditya Kusupati**

- 4th year PhD student at UW CSE
- I work with Ali Farhadi and Sham Kakade

#### My Research:

- I develop fundamental ML algorithms that are amenable to practical deployment both at edge and web-scale.
- More recently, I have been working towards rethinking search for better indexing of the world.

#### **Past Experiences:**

- Student Researcher at Google Research
- Al Resident at Microsoft Research



#### Administrative

### Assignment 1 due Friday April 14, 11:59pm

 Before submitting your work, please be sure to read the instructions on the course website carefully (Assignments Tab), and follow the steps mentioned in "Submitting your work". This will ensure Gradescope grades your work correctly.

Assignment 2 will also be released April 14th

#### Administrative

Project proposal due Monday Apr 24, 11:59pm

This Friday's discussion section will discuss how to design a project – **Sarah Pratt** 

Meet Ranjay, Sarah or me about projects initially

Benlin or Sharan about assignments

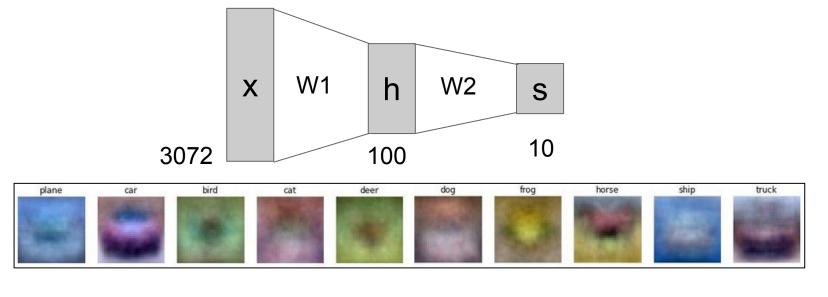
#### Last time: Neural Networks

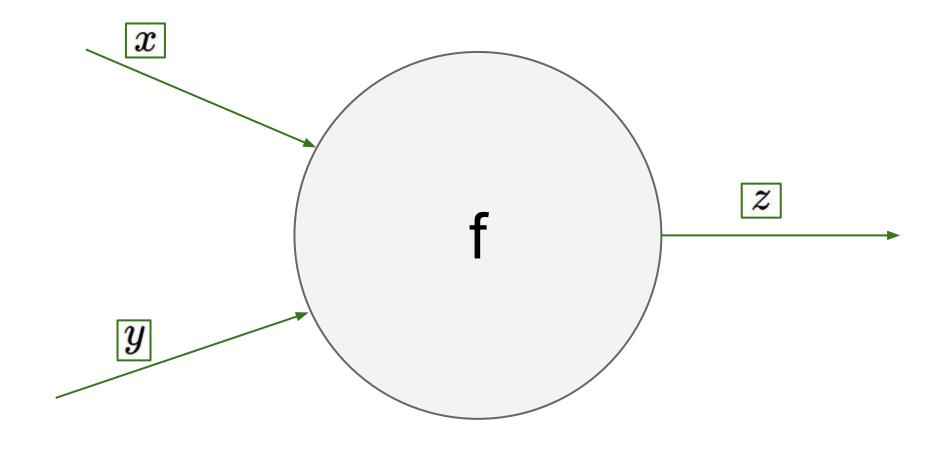
Linear score function:

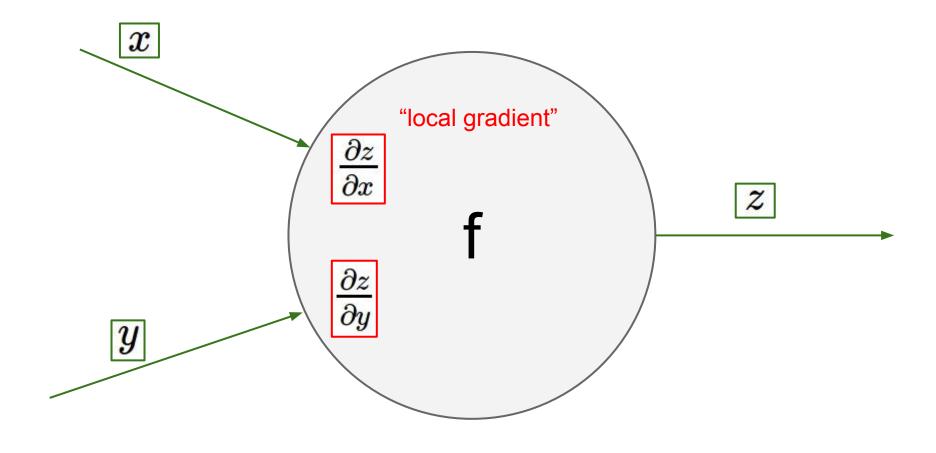
$$f = Wx$$

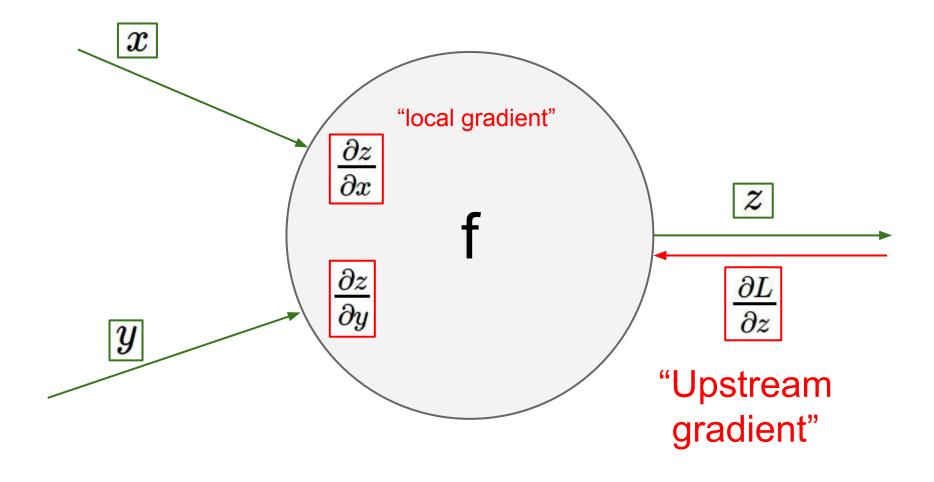
2-layer Neural Network

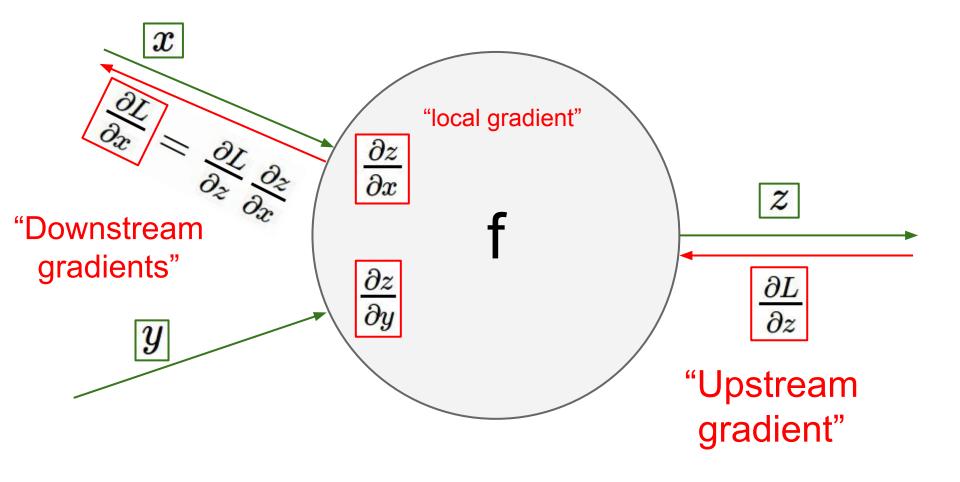
$$f = W_2 \max(0, W_1 x)$$

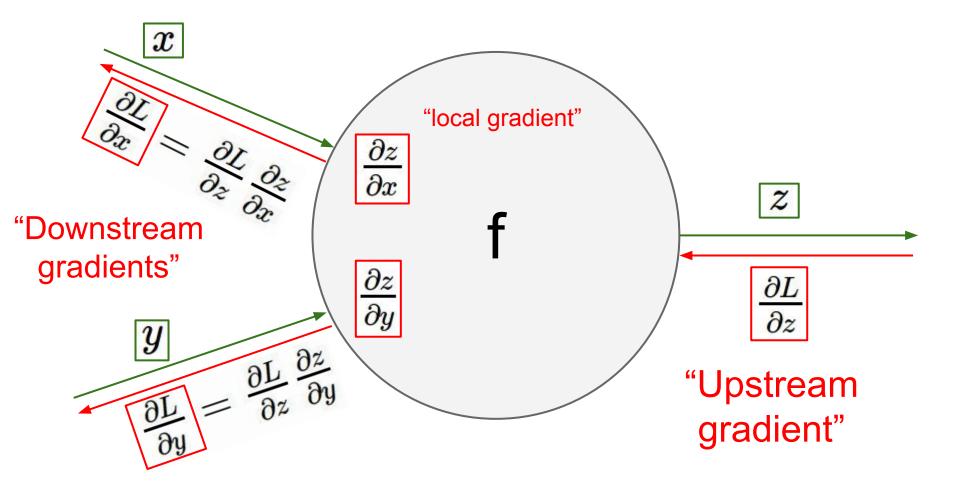


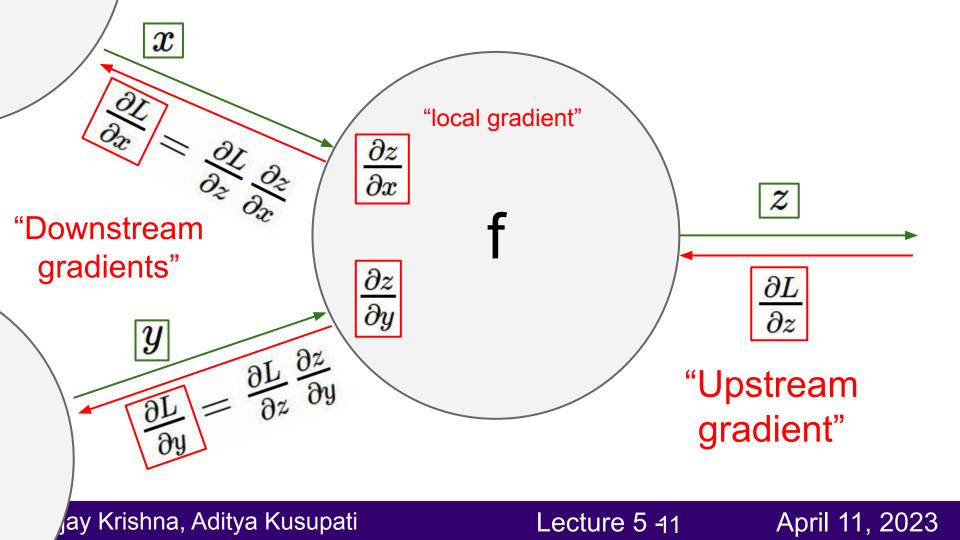












So far: backprop with scalars

What about vector-valued functions?

## Recap: Vector derivatives

#### Scalar to Scalar

$$x \in \mathbb{R}, y \in \mathbb{R}$$

Regular derivative:

$$\frac{\partial y}{\partial x} \in \mathbb{R}$$

If x changes by a small amount, how much will y change?

## Recap: Vector derivatives

#### Scalar to Scalar

$$x \in \mathbb{R}, y \in \mathbb{R}$$

$$x \in \mathbb{R}^N, y \in \mathbb{R}$$

Regular derivative:

Derivative is **Gradient**:

$$\frac{\partial y}{\partial x} \in \mathbb{R}$$

$$\frac{\partial y}{\partial x} \in \mathbb{R}^N \quad \left(\frac{\partial y}{\partial x}\right)_n = \frac{\partial y}{\partial x_n}$$

If x changes by a small amount, how much will y change?

For each element of x, if it changes by a small amount then how much will y change?

## Recap: Vector derivatives

#### Scalar to Scalar

$$x \in \mathbb{R}, y \in \mathbb{R}$$

Regular derivative:

$$\frac{\partial y}{\partial x} \in \mathbb{R}$$

If x changes by a small amount, how much will y change?

## Vector to Scalar

$$x \in \mathbb{R}^N, y \in \mathbb{R}$$

Derivative is **Gradient**:

$$\frac{\partial y}{\partial x} \in \mathbb{R}^N \quad \left(\frac{\partial y}{\partial x}\right)_n = \frac{\partial y}{\partial x_n}$$

For each element of x, if it changes by a small amount then how much will y change?

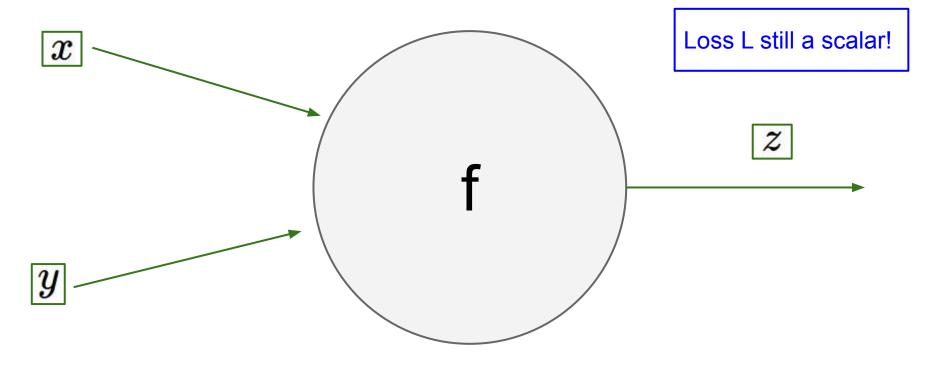
#### Vector to Vector

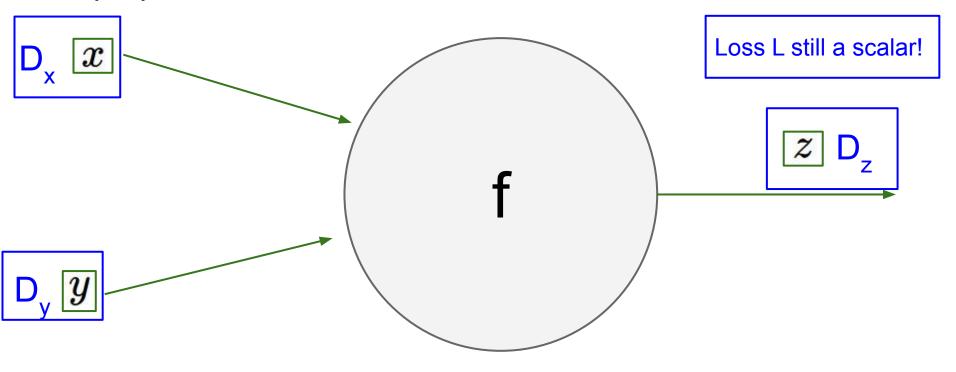
$$x \in \mathbb{R}^N, y \in \mathbb{R}^M$$

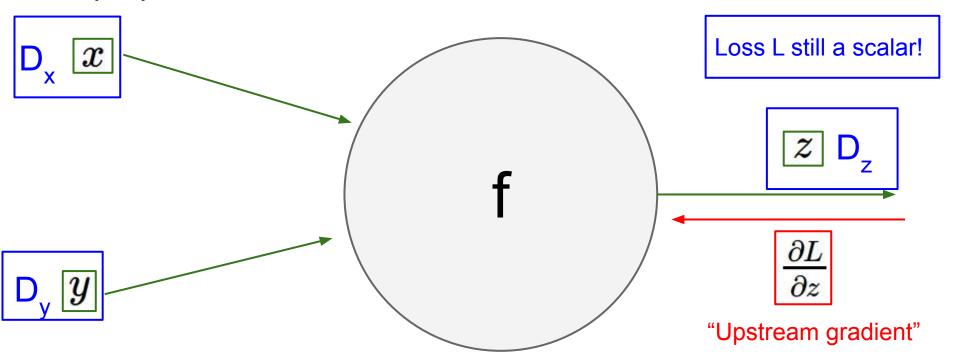
Derivative is **Jacobian**:

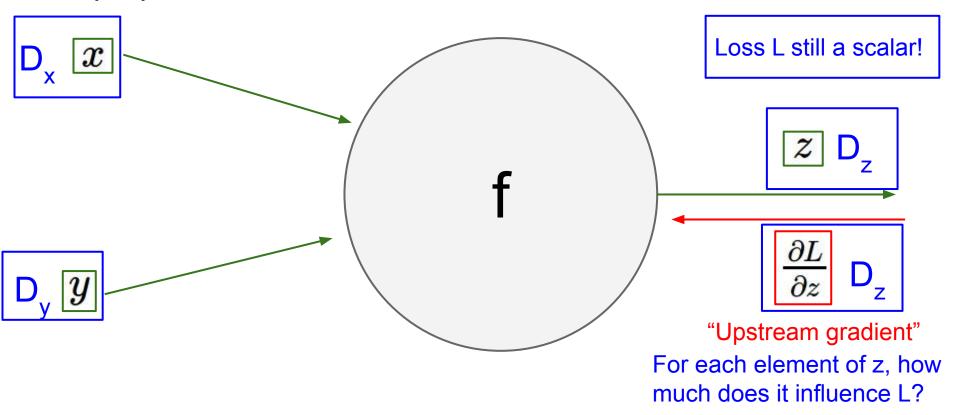
$$\frac{\partial y}{\partial x} \in \mathbb{R}^N \quad \left(\frac{\partial y}{\partial x}\right)_n = \frac{\partial y}{\partial x_n} \quad \frac{\partial y}{\partial x} \in \mathbb{R}^{N \times M} \quad \left(\frac{\partial y}{\partial x}\right)_{n,m} = \frac{\partial y_m}{\partial x_n}$$

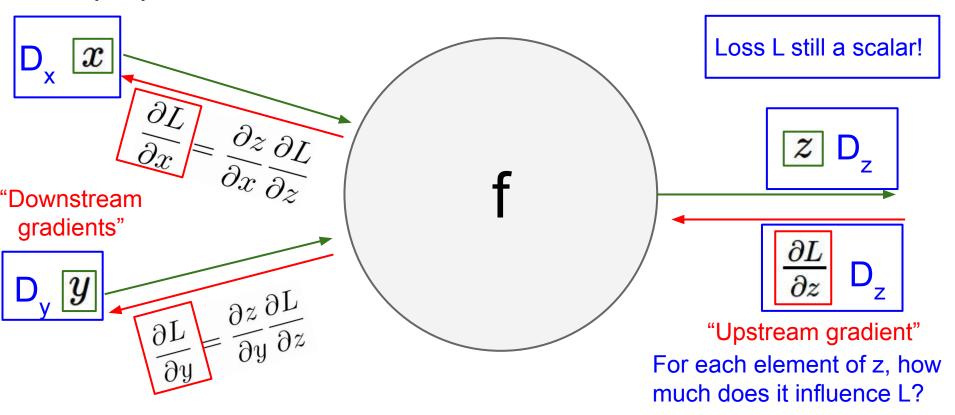
For each element of x, if it changes by a small amount then how much will each element of y change?

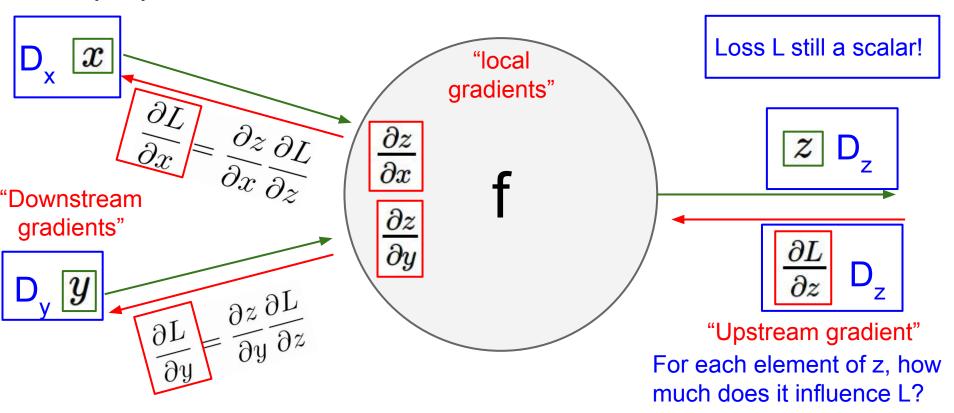


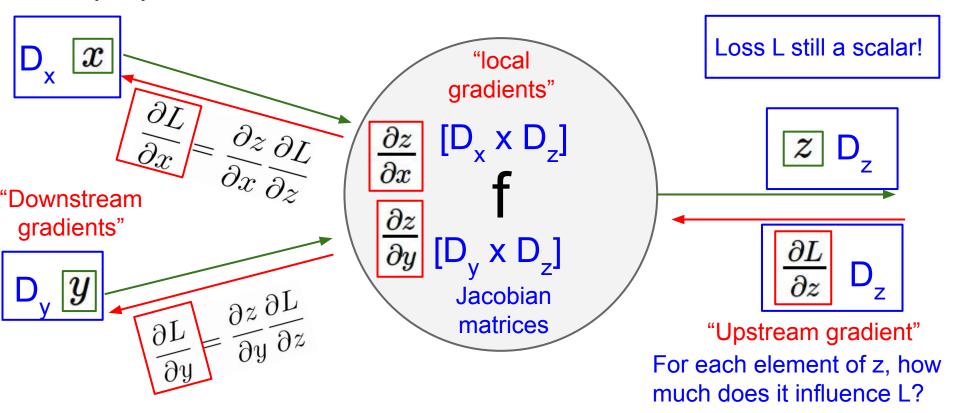


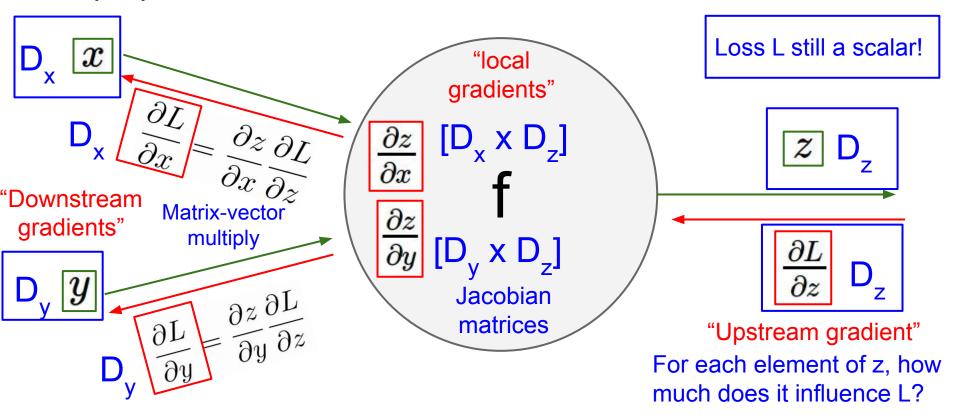




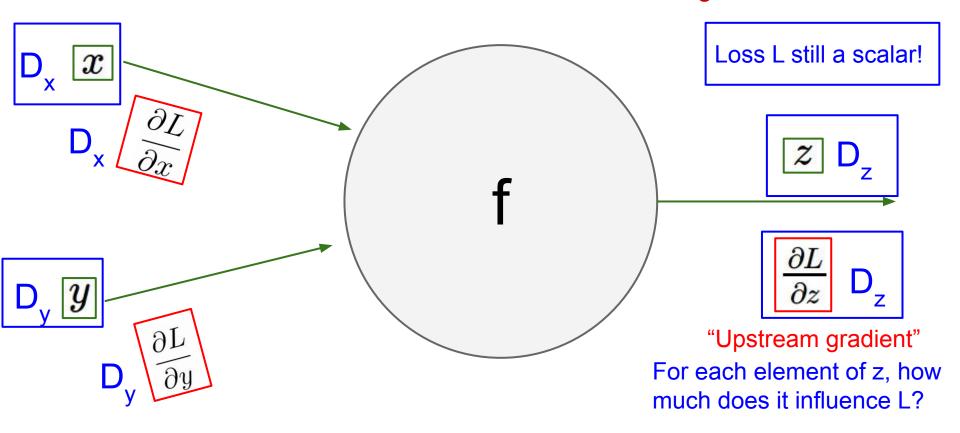




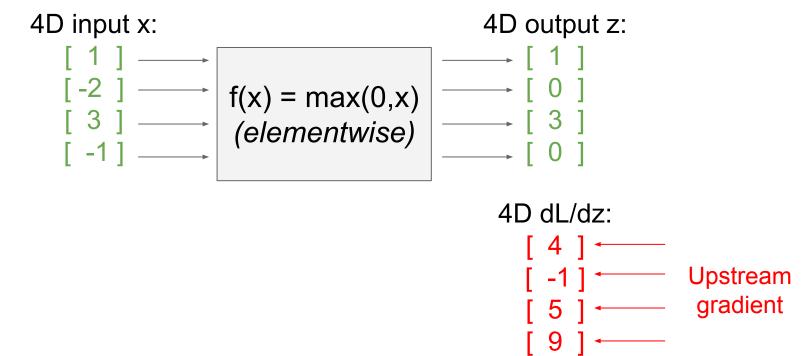




#### Gradients of variables wrt loss have same dims as the original variable



# 4D input x: 4D output z: $\begin{bmatrix} 1 \\ -2 \end{bmatrix} \longrightarrow f(x) = max(0,x) \longrightarrow \begin{bmatrix} 0 \\ 0 \end{bmatrix}$ (elementwise) $\begin{bmatrix} 3 \end{bmatrix} \longrightarrow \begin{bmatrix} 0 \end{bmatrix}$



4D input x:
$$\begin{bmatrix}
1 \\
-2
\end{bmatrix}$$

$$\begin{bmatrix}
(az/dx) \\
(bz/dx)
\end{bmatrix}$$

$$\begin{bmatrix}
(az/dx) \\
(bz/dz)
\end{bmatrix}$$

$$\begin{bmatrix}
(az/dx) \\
(bz/dz)
\end{bmatrix}$$

$$\begin{bmatrix}
(az/dz) \\
(cz/dz)
\end{bmatrix}$$

$$\begin{bmatrix}
(az/dz) \\
(c$$

4D input x:
$$\begin{bmatrix}
1 \\
-2 \\
-2
\end{bmatrix}$$

$$f(x) = max(0,x)$$

$$\begin{bmatrix}
3 \\
-1
\end{bmatrix}$$

$$(elementwise)$$

$$\begin{bmatrix}
4 \\
0
\end{bmatrix}$$
4D dL/dz:
$$\begin{bmatrix}
4 \\
0
\end{bmatrix}$$

$$\begin{bmatrix}
6 \\
0
\end{bmatrix}$$

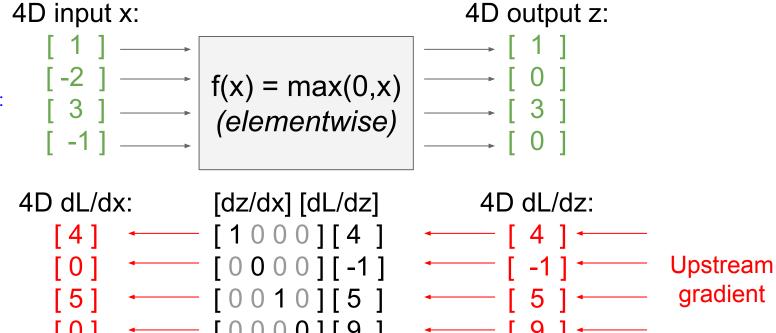
$$\begin{bmatrix}
7 \\
0
\end{bmatrix}$$

$$\begin{bmatrix}
7 \\
9
\end{bmatrix}$$

$$\begin{bmatrix}
7 \\
9
\end{bmatrix}$$

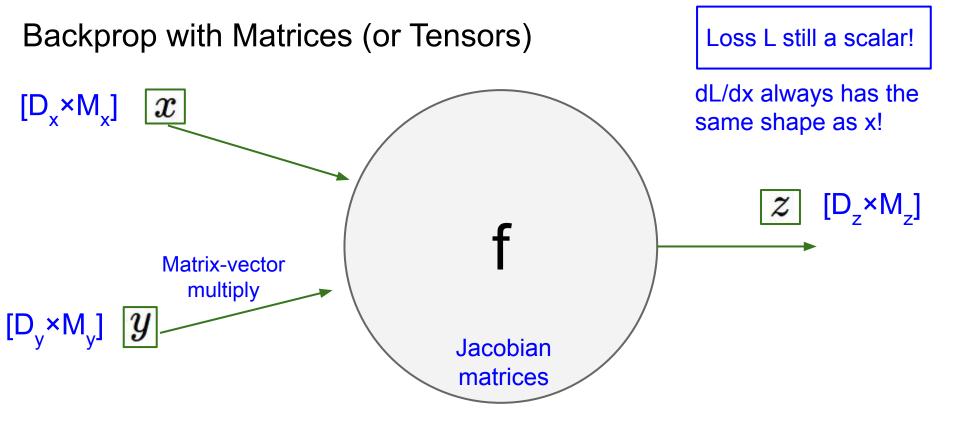
$$\begin{bmatrix}
7 \\
9
\end{bmatrix}$$

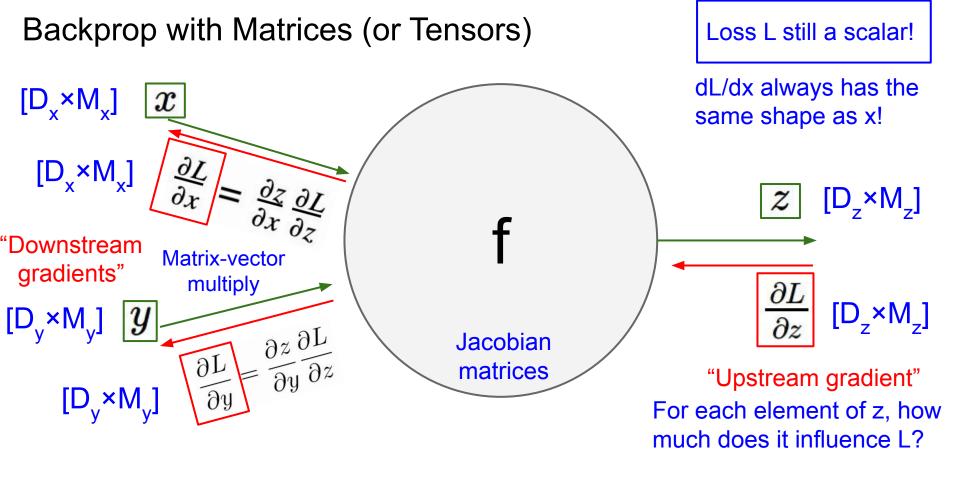
Jacobian is sparse: off-diagonal entries always zero! Never explicitly form Jacobian -- instead use implicit multiplication

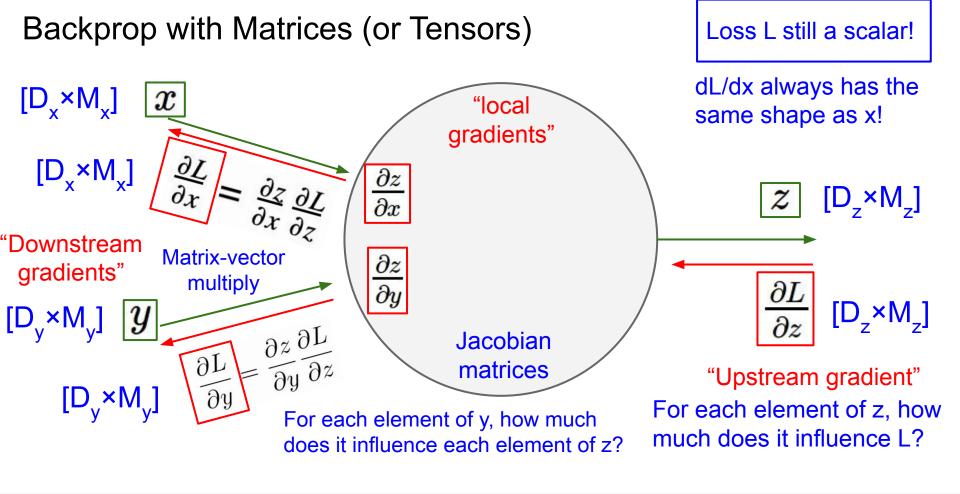


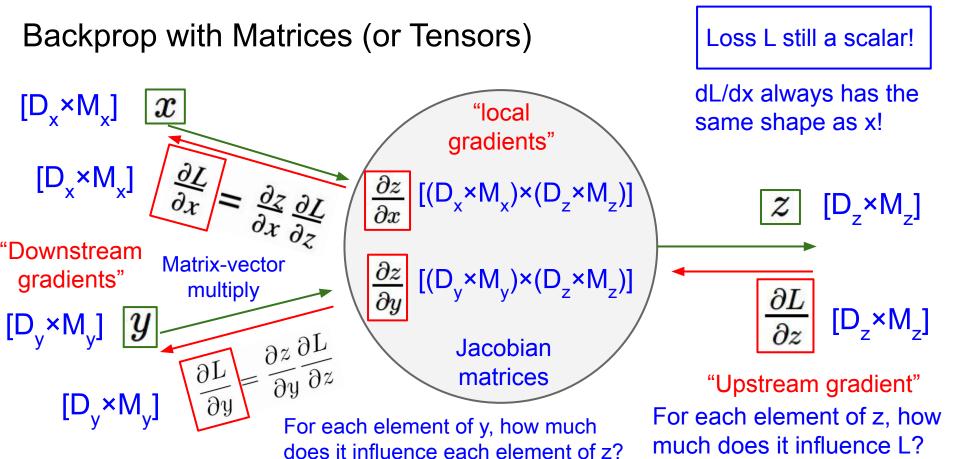
Jacobian is sparse: off-diagonal entries always zero! Never explicitly form Jacobian -- instead use implicit multiplication

4D input x: 4D output z: f(x) = max(0,x)(elementwise) 4D dL/dx: [dz/dx] [dL/dz]4D dL/dz: 









## **Backprop with Matrices**

## Matrix Multiply

$$y_{n,m} = \sum_{d} x_{n,d} w_{d,m}$$

Also see derivation by Prof. Justin Johnson: <a href="https://courses.cs.washington.edu/courses/cse493g1/23s">https://courses.cs.washington.edu/courses/cse493g1/23s</a> p/resources/linear-backprop.pdf

## Matrix Multiply

$$y_{n,m} = \sum_{d} x_{n,d} w_{d,m}$$

### Jacobians:

dy/dx:  $[(N\times D)\times (N\times M)]$ dy/dw:  $[(D\times M)\times (N\times M)]$ 

For a neural net we may have N=64, D=M=4096
Each Jacobian takes ~256 GB of memory! Must work with them implicitly!

## [13 9 -2 -6] [ 5 2 17 1]

y: [N×M]

dL/dy: [N×M] ------ [ 2 3 -3 9 ] [ -8 1 4 6 ]

## Matrix Multiply

$$y_{n,m} = \sum_{d} x_{n,d} w_{d,m}$$

**Q**: What parts of y are affected by one element of x?





## Matrix Multiply

$$y_{n,m} = \sum_{d} x_{n,d} w_{d,m}$$

**Q**: What parts of y are affected by one element of x?

**A**:  $x_{n,d}$  affects the whole row  $y_{n,\cdot}$ 

$$\frac{\partial L}{\partial x_{n,d}} = \sum_{m} \frac{\partial L}{\partial y_{n,m}} \frac{\partial y_{n,m}}{\partial x_{n,d}}$$

3 2 1 -1]

2 1 3 2]

[ 3 2 1 -2]

## Matrix Multiply

$$y_{n,m} = \sum_{d} x_{n,d} w_{d,m}$$

dL/dy: [N×M]

[ 2 3 -3 9

**Q**: What parts of y are affected by one element of x?

**A**:  $x_{n,d}$  affects the whole row  $y_{n,\cdot}$ 

 $\frac{\partial L}{\partial x_{n,d}} = \sum \frac{\partial L}{\partial y_{n,m}} \frac{\partial y_{n,m}}{\partial x_{n,d}}$ 

Q: How much

## Matrix Multiply

$$y_{n,m} = \sum_{d} x_{n,d} w_{d,m}$$

**A**:  $x_{n,d}$  affects the whole row  $y_{n,\cdot}$ 

$$\frac{\partial L}{\partial x_{n,d}} = \sum_{m} \frac{\partial L}{\partial y_{n,m}} \frac{\partial y_{n,m}}{\partial x_{n,d}} = \sum_{m} \frac{\partial L}{\partial y_{n,m}} w_{d,m}$$

Q: How much does  $x_{n,d}$ affect  $y_{n,m}$ ?

 $\mathbf{A}: w_{d,m}$ 

## $[N\times D]$ $[N\times M]$ $[M\times D]$

$$\frac{\partial L}{\partial x} = \left(\frac{\partial L}{\partial y}\right) w^T$$

## Matrix Multiply

$$y_{n,m} = \sum_{d} x_{n,d} w_{d,m}$$

**A**: 
$$x_{n,d}$$
 affects the whole row  $y_{n,\cdot}$ 

$$\frac{\partial L}{\partial x} = \sum_{n} \frac{\partial L}{\partial x_n} \frac{\partial y_{n,n}}{\partial x_n}$$

$$\frac{\partial L}{\partial x} = \left(\frac{\partial L}{\partial y}\right) w^T \qquad \frac{\partial L}{\partial x_{n,d}} = \sum_{m} \frac{\partial L}{\partial y_{n,m}} \frac{\partial y_{n,m}}{\partial x_{n,d}} = \sum_{m} \frac{\partial L}{\partial y_{n,m}} w_{d,m}$$

dL/dy: [N×M]

Q: How much

does  $x_{n,d}$ 

 $\mathbf{A}: w_{d,m}$ 

affect  $y_{n,m}$ ?

## Matrix Multiply

$$y_{n,m} = \sum_{d} x_{n,d} w_{d,m}$$

$$\begin{array}{c} | [13 9 -2 -6] \\ \hline \end{array}$$

$$[5 2 17 1]$$

### By similar logic:

[ 3 2 1 -2]

$$\frac{\partial L}{\partial x} = \left(\frac{\partial L}{\partial y}\right) w^T$$

$$[D\times M] [D\times N] [N\times M]$$

$$\frac{\partial L}{\partial w} = x^T \left(\frac{\partial L}{\partial y}\right)$$

These formulas are easy to remember: they are the only way to make shapes match up!

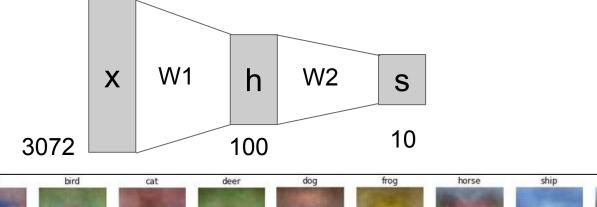
## Wrapping up: Neural Networks

Linear score function:

$$f = Wx$$

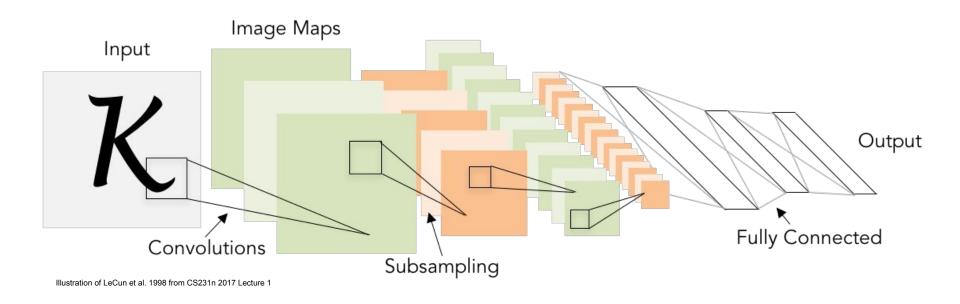
2-layer Neural Network

$$f = W_2 \max(0, W_1 x)$$





### **Next: Convolutional Neural Networks**



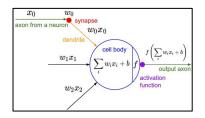
## A bit of history...

The **Mark I Perceptron** machine was the first implementation of the perceptron algorithm.

The machine was connected to a camera that used 20×20 cadmium sulfide photocells to produce a 400-pixel image.

recognized letters of the alphabet

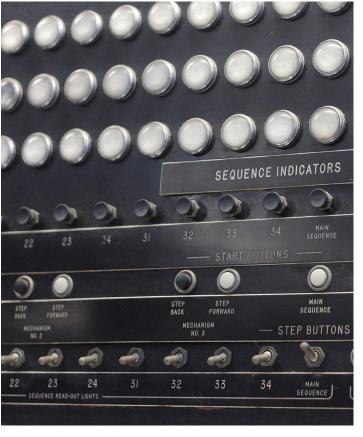
$$f(x) = \begin{cases} 1 & \text{if } w \cdot x + b > 0 \\ 0 & \text{otherwise} \end{cases}$$



#### update rule:

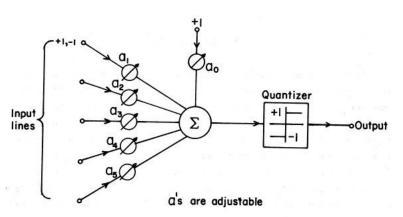
$$w_i(t+1) = w_i(t) + \alpha(d_j - y_j(t))x_{j,i}$$

Frank Rosenblatt, ~1957: Perceptron

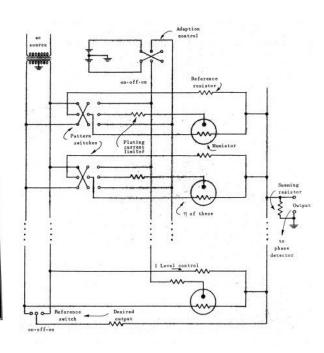


This image by Rocky Acosta is licensed under CC-BY 3.0

## A bit of history...

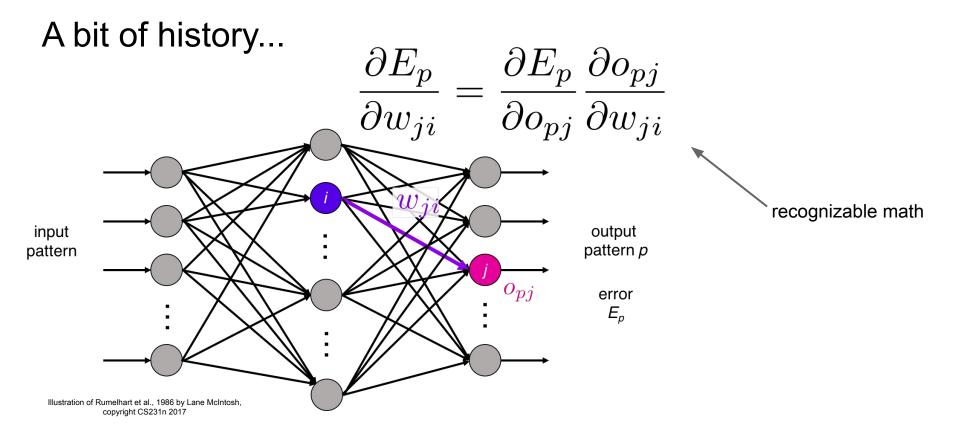






Widrow and Hoff, ~1960: Adaline/Madaline

These figures are reproduced from Widrow 1960, Stanford Electronics Laboratories Technical Report with permission from Stanford University Special Collections.



Rumelhart et al., 1986: First time back-propagation became popular

## A bit of history...

[Hinton and Salakhutdinov 2006]

Reinvigorated research in Deep Learning

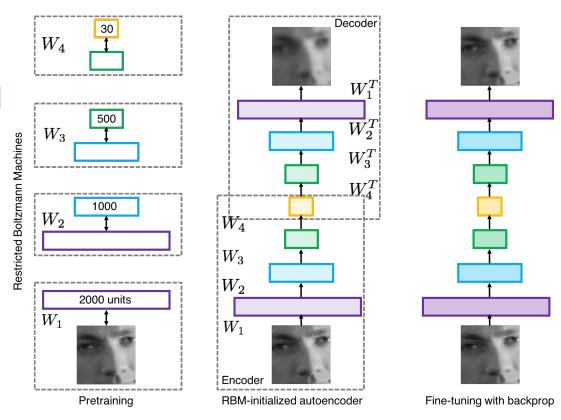


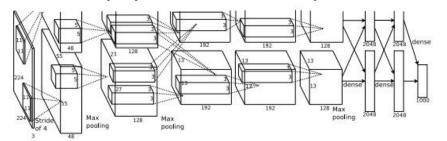
Illustration of Hinton and Salakhutdinov 2006 by Lane McIntosh, copyright CS231n 2017

### First strong results

Acoustic Modeling using Deep Belief Networks
Abdel-rahman Mohamed, George Dahl, Geoffrey Hinton, 2010
Context-Dependent Pre-trained Deep Neural Networks
for Large Vocabulary Speech Recognition
George Dahl, Dong Yu, Li Deng, Alex Acero, 2012

## Imagenet classification with deep convolutional neural networks

Alex Krizhevsky, Ilya Sutskever, Geoffrey E Hinton, 2012



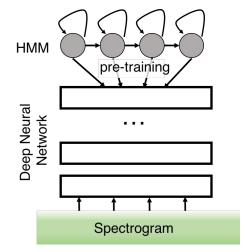
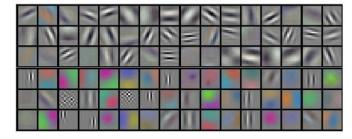


Illustration of Dahl et al. 2012 by Lane McIntosh, copyright CS231n 2017



Figures copyright Alex Krizhevsky, Ilya Sutskever, and Geoffrey Hinton, 2012. Reproduced with permission.

## A bit of history:

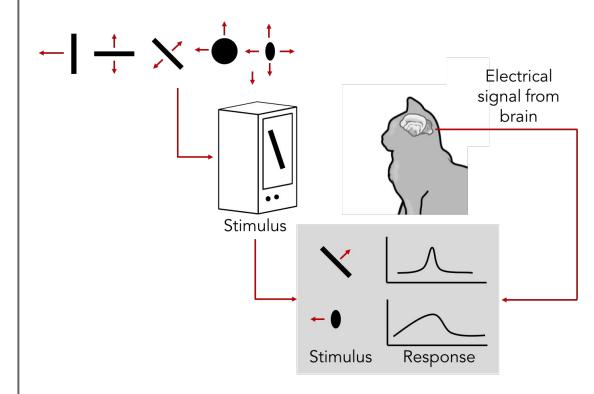
# Hubel & Wiesel, 1959

RECEPTIVE FIELDS OF SINGLE NEURONES IN THE CAT'S STRIATE CORTEX

1962

RECEPTIVE FIELDS, BINOCULAR INTERACTION AND FUNCTIONAL ARCHITECTURE IN THE CAT'S VISUAL CORTEX

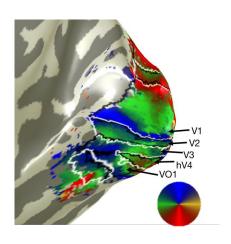
1968...

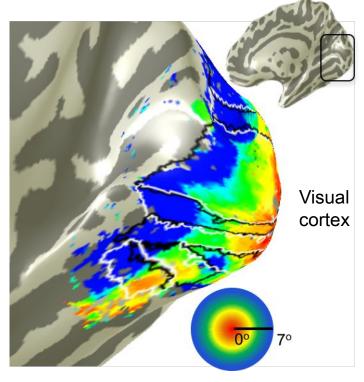


<u>Cat image</u> by CNX OpenStax is licensed under CC BY 4.0; changes made

## A bit of history

Topographical mapping in the cortex: nearby cells in cortex represent nearby regions in the visual field

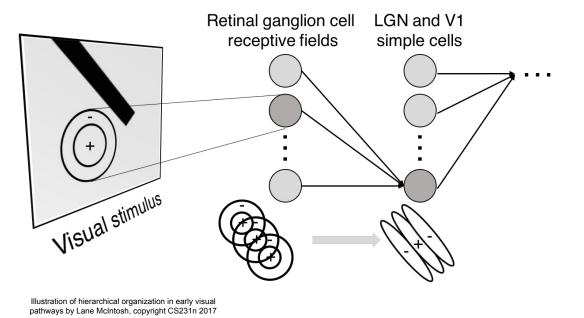




Retinotopy images courtesy of Jesse Gomez in the Stanford Vision & Perception Neuroscience Lab.

Human brain

## Hierarchical organization



## Simple cells:

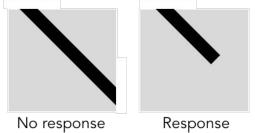
Response to light orientation

#### Complex cells:

Response to light orientation and movement

### Hypercomplex cells:

response to movement with an end point

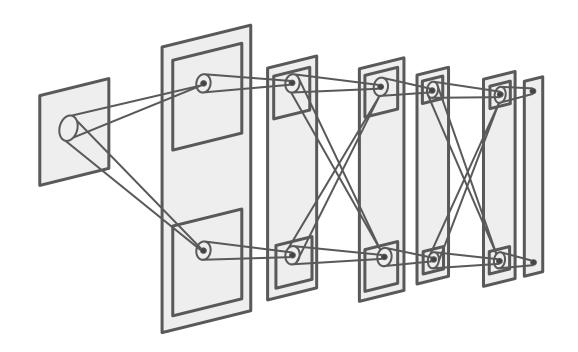


(end point)

## A bit of history:

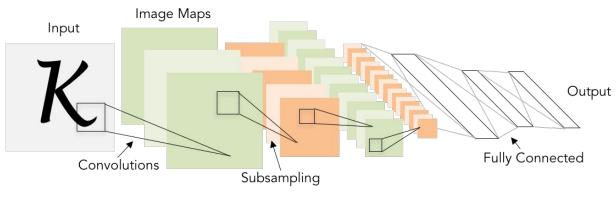
# **Neocognitron** [Fukushima 1980]

"sandwich" architecture (SCSCSC...) simple cells: modifiable parameters complex cells: perform pooling



## A bit of history: Gradient-based learning applied to document recognition

[LeCun, Bottou, Bengio, Haffner 1998]



LeNet-5

## A bit of history: ImageNet Classification with Deep Convolutional Neural Networks [Krizhevsky, Sutskever, Hinton, 2012]



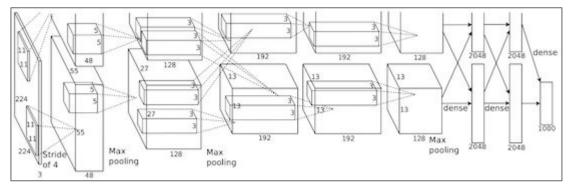
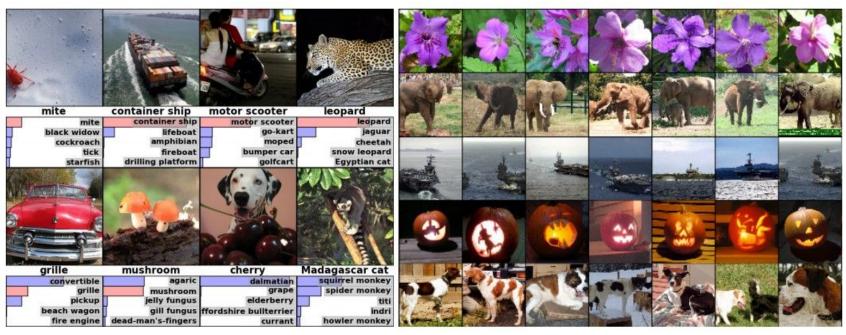


Figure copyright Alex Krizhevsky, Ilya Sutskever, and Geoffrey Hinton, 2012. Reproduced with permission.

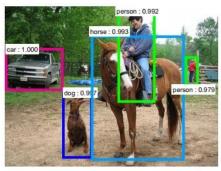
"AlexNet"

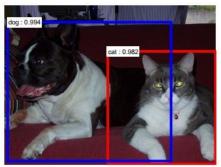
Classification Retrieval



Figures copyright Alex Krizhevsky, Ilya Sutskever, and Geoffrey Hinton, 2012. Reproduced with permission.

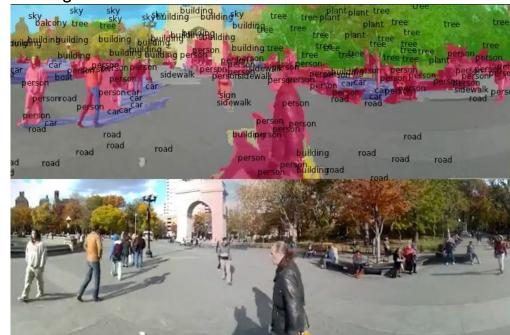
#### Detection







Segmentation

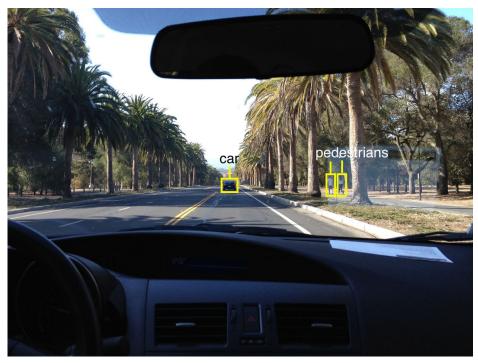


Figures copyright Clement Farabet, 2012.

Figures copyright Shaoqing Ren, Kaiming He, Ross Girschick, Jian Sun, 2015. Reproduced with permission. Reproduced with permission.

[Faster R-CNN: Ren, He, Girshick, Sun 2015]

[Farabet et al., 2012]



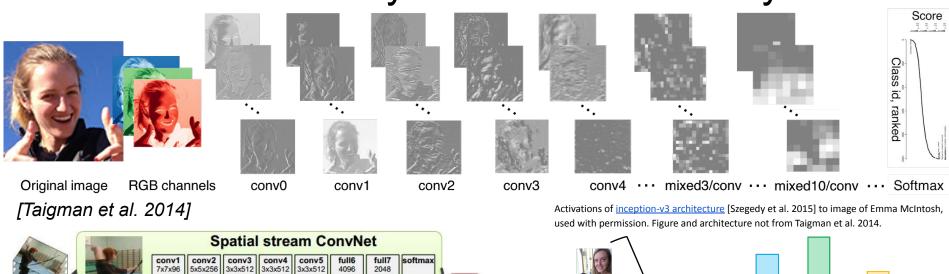
self-driving cars

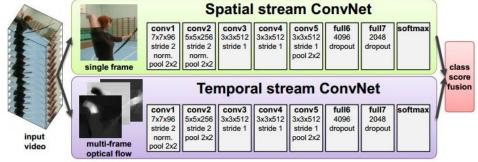
Photo by Lane McIntosh. Copyright CS231n 2017.



#### **NVIDIA** Tesla line

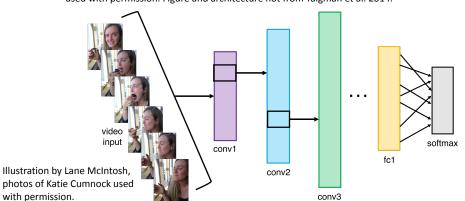
Note that for embedded systems a typical setup would involve NVIDIA Tegras, with integrated GPU and ARM-based CPU cores.





[Simonyan et al. 2014]

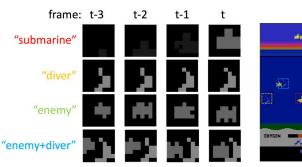
Figures copyright Simonyan et al., 2014. Reproduced with permission.





[Toshev, Szegedy 2014]

Images are examples of pose estimation, not actually from Toshev & Szegedy 2014. Copyright Lane McIntosh.



DAYGEN ARTHUR AR



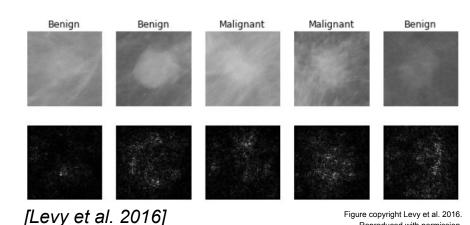
DETECTION

ATTIVISION

DETECTION

[Guo et al. 2014]

Figures copyright Xiaoxiao Guo, Satinder Singh, Honglak Lee, Richard Lewis, and Xiaoshi Wang, 2014. Reproduced with permission.





[Dieleman et al. 2014]

From left to right: public domain by NASA, usage permitted by ESA/Hubble, public domain by NASA, and public domain.

Reproduced with permission.



[Sermanet et al. 2011] [Ciresan et al.]

Photos by Lane McIntosh. Copyright CS231n 2017.



Whale recognition, Kaggle Challenge



Mnih and Hinton, 2010

#### No errors



A white teddy bear sitting in the grass



A man riding a wave on top of a surfboard

#### Minor errors



A man in a baseball uniform throwing a ball



A cat sitting on a suitcase on the floor

#### Somewhat related



A woman is holding a cat in her hand



A woman standing on a beach holding a surfboard

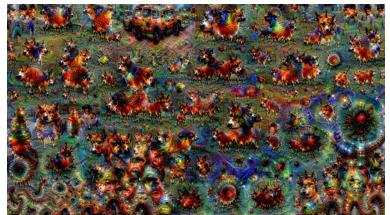
## Image Captioning

[Vinyals et al., 2015] [Karpathy and Fei-Fei, 2015]

All images are CC0 Public domain:

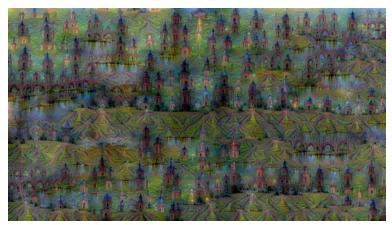
https://pixabay.com/en/lugqage-antique-cat-1643010/ https://pixabay.com/en/teddy-plush-bears-cute-teddy-bear-1623436/ https://pixabay.com/en/surf-wave-summer-sport-liforal-1668716/ https://pixabay.com/en/woman-female-model-portrait-adult-983967/ https://pixabay.com/en/handstand-lake-meditation-496008/ https://pixabay.com/en/baseball-player-shortstop-infield-1045263/

Captions generated by Justin Johnson using Neuraltalk2











Figures copyright Justin Johnson, 2015. Reproduced with permission. Generated using the Inceptionism approach from a blog post by Google Research.

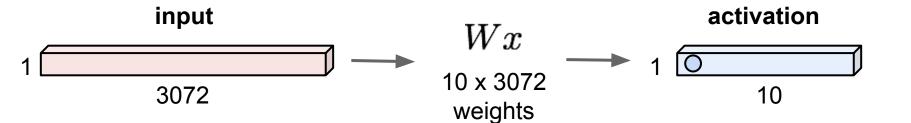
Original image is CCO public domain
Starry Niight and Tree Roots by Van Gogh are in the public domain
Bokeh image is in the public domain
Stylized images copyright Justin Johnson, 2017;
reproduced with permission

Gatys et al, "Image Style Transfer using Convolutional Neural Networks", CVPR 2016 Gatys et al, "Controlling Perceptual Factors in Neural Style Transfer", CVPR 2017

## Convolutional Neural Networks

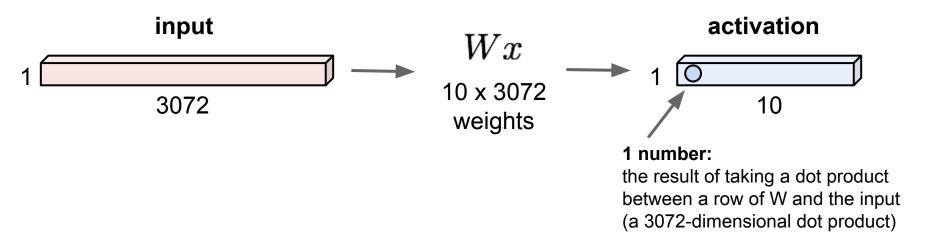
## Recap: Fully Connected Layer

32x32x3 image -> stretch to 3072 x 1

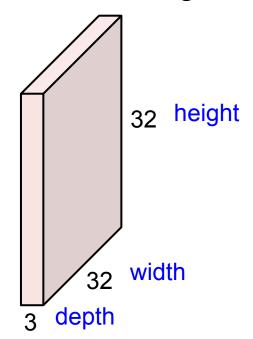


## Fully Connected Layer

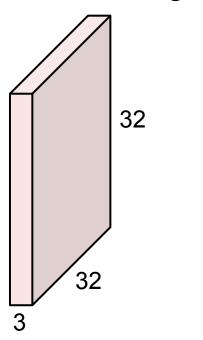
32x32x3 image -> stretch to 3072 x 1



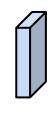
32x32x3 image -> preserve spatial structure



32x32x3 image

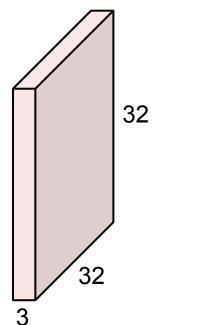


5x5x3 filter



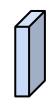
**Convolve** the filter with the image i.e. "slide over the image spatially, computing dot products"

32x32x3 image

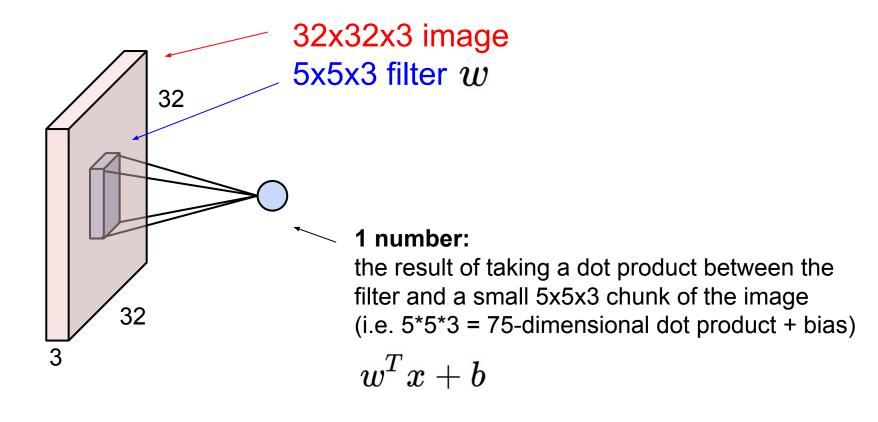


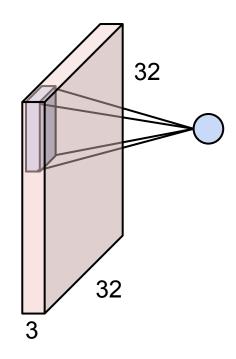
Filters always extend the full depth of the input volume

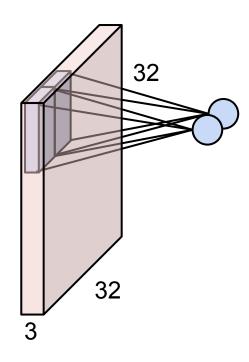
5x5x3 filter

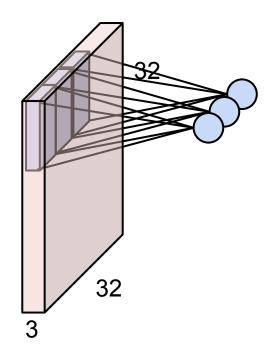


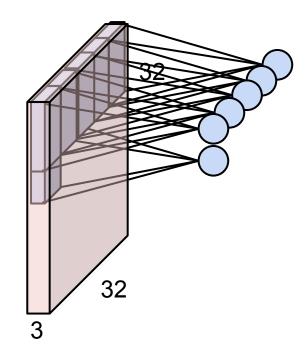
**Convolve** the filter with the image i.e. "slide over the image spatially, computing dot products"

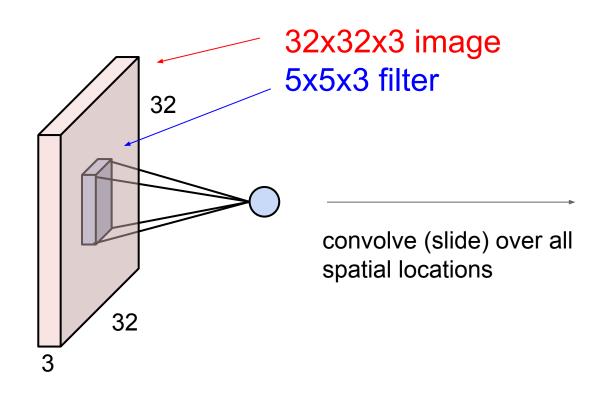




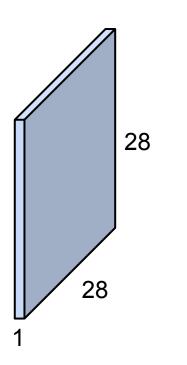




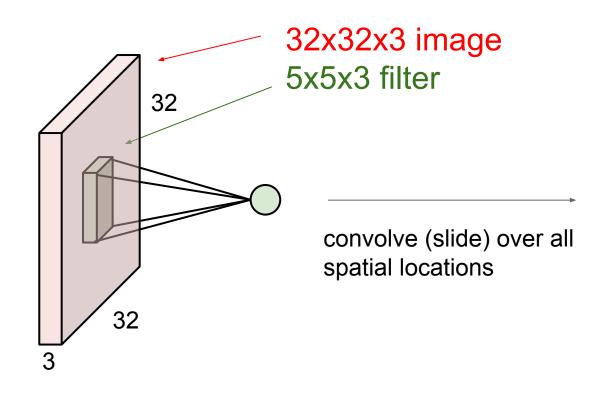


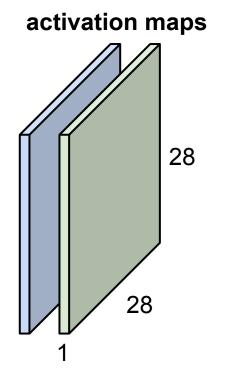


#### activation map

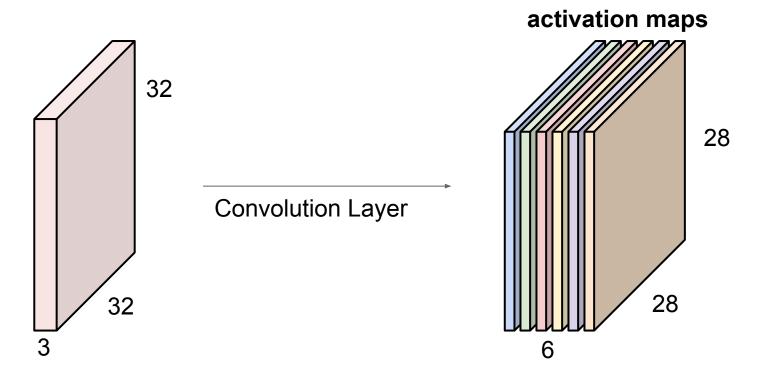


#### consider a second, green filter



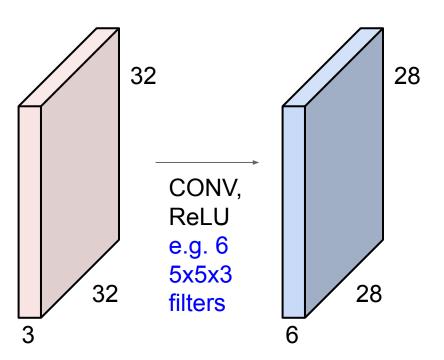


For example, if we had 6 5x5 filters, we'll get 6 separate activation maps:

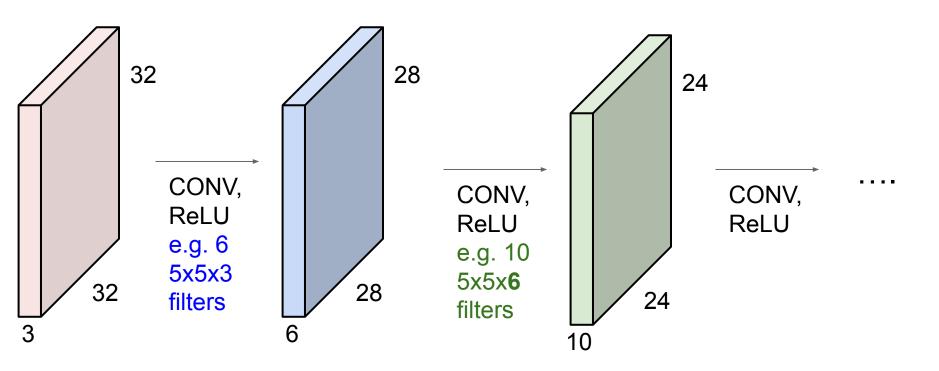


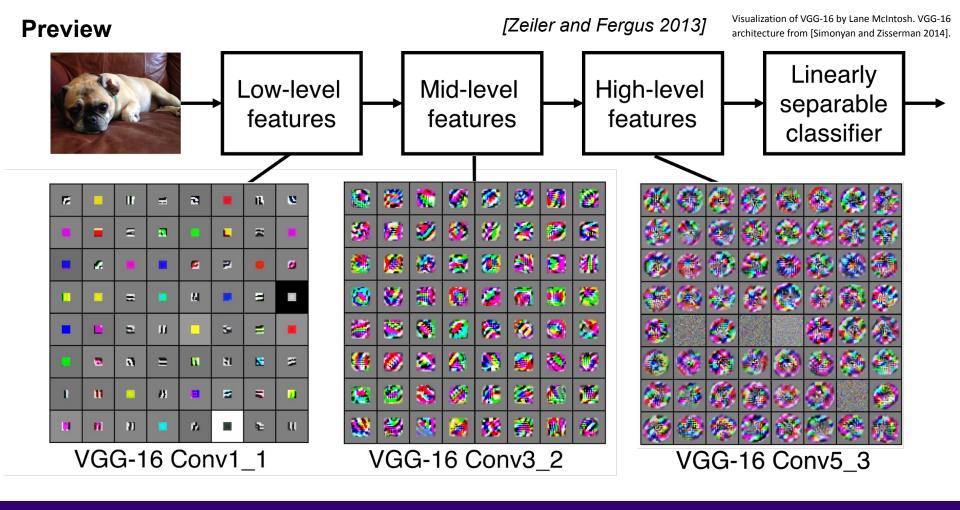
We stack these up to get a "new image" of size 28x28x6!

**Preview:** ConvNet is a sequence of Convolution Layers, interspersed with activation functions



**Preview:** ConvNet is a sequence of Convolution Layers, interspersed with activation functions

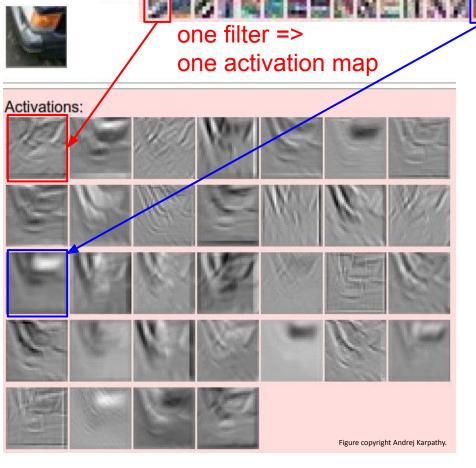




#### Linearly **Preview** Low-level Mid-level High-level separable features features features classifier 2 • 8 7 = = 34 N. H 5 VGG-16 Conv1\_1 VGG-16 Conv3 2 VGG-16 Conv5\_3 Retinal ganglion cell LGN and V1 Complex cells: receptive fields simple cells Response to light orientation and movement Hypercomplex cells: response to movement with an end point Visual stimulus

No response

Response (end point)



# example 5x5 filters (32 total)

We call the layer convolutional because it is related to convolution of two signals:

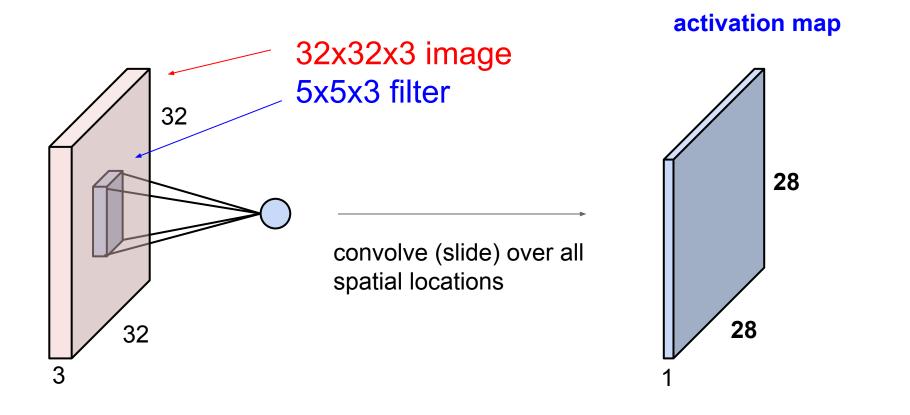
$$f[x,y] * g[x,y] = \sum_{n_1 = -\infty}^{\infty} \sum_{n_2 = -\infty}^{\infty} f[n_1, n_2] \cdot g[x - n_1, y - n_2]$$

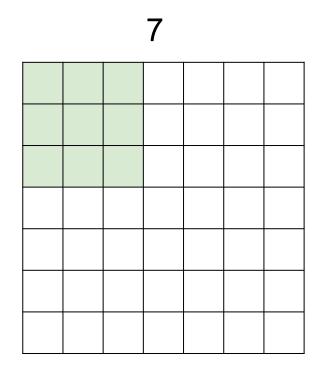
elementwise multiplication and sum of a filter and the signal (image) preview: RELU RELU RELU RELU RELU RELU CONV CONV CONV CONV CONV CONV FC car truck airplane ship horse

Ranjay Krishna, Aditya Kusupati

Lecture 5 - 85

April 11, 2023

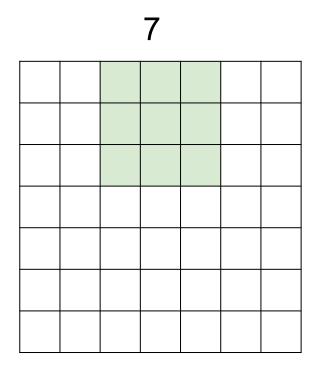




7x7 input (spatially) assume 3x3 filter

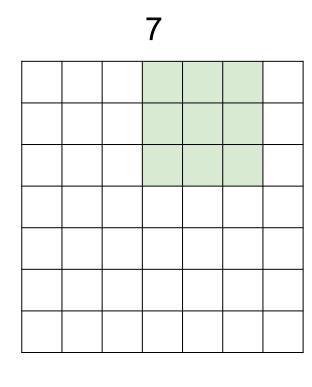
7x7 input (spatially) assume 3x3 filter

7



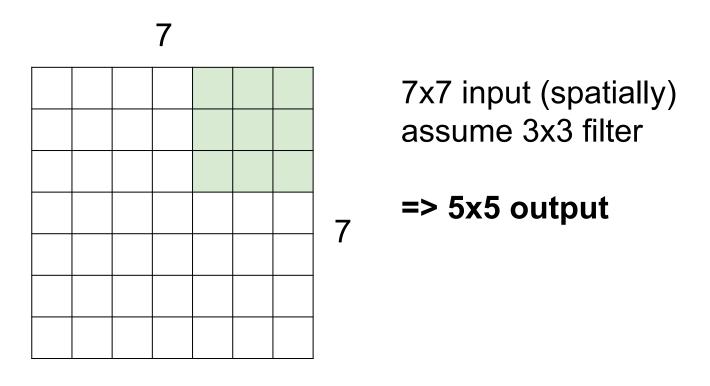
7x7 input (spatially) assume 3x3 filter

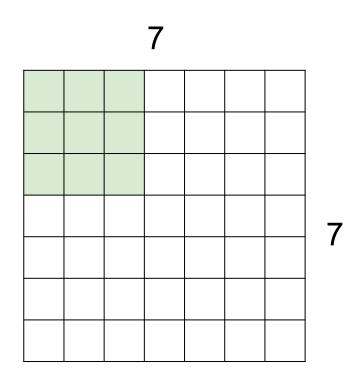
7



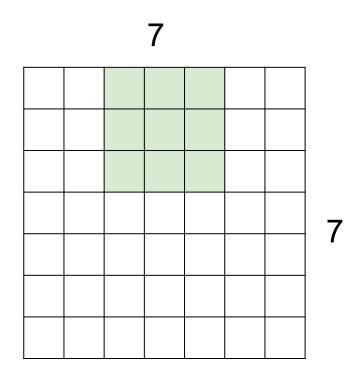
7x7 input (spatially) assume 3x3 filter

7

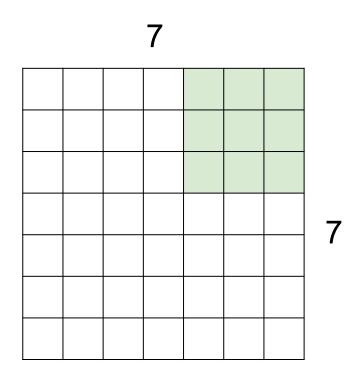




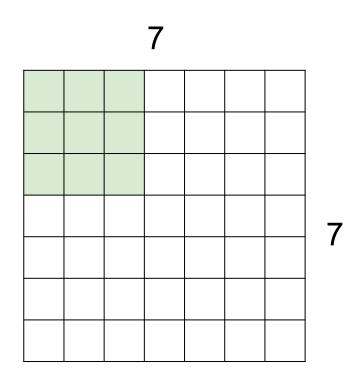
7x7 input (spatially) assume 3x3 filter applied with stride 2



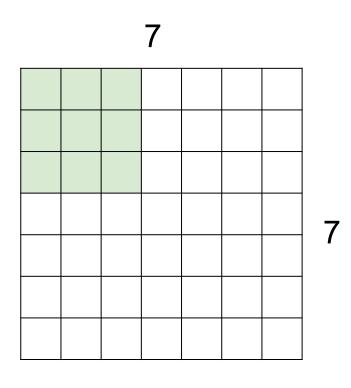
7x7 input (spatially) assume 3x3 filter applied with stride 2



7x7 input (spatially) assume 3x3 filter applied with stride 2 => 3x3 output!



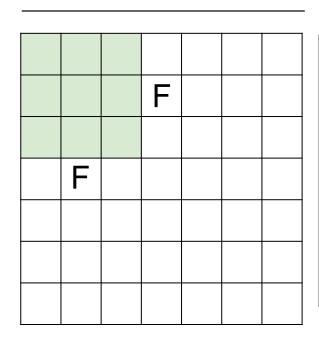
7x7 input (spatially) assume 3x3 filter applied with stride 3?



7x7 input (spatially) assume 3x3 filter applied with stride 3?

doesn't fit! cannot apply 3x3 filter on 7x7 input with stride 3.

N
---



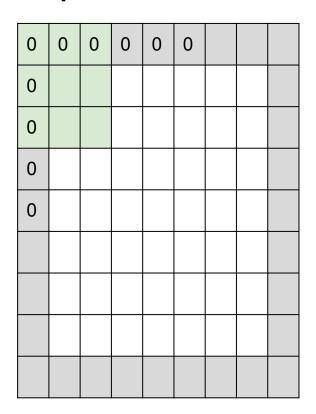
Ν

Output size:

(N - F) / stride + 1

e.g. N = 7, F = 3:  
stride 1 => 
$$(7 - 3)/1 + 1 = 5$$
  
stride 2 =>  $(7 - 3)/2 + 1 = 3$   
stride 3 =>  $(7 - 3)/3 + 1 = 2.33$  :\

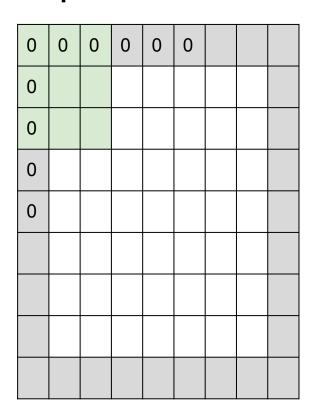
#### In practice: Common to zero pad the border



e.g. input 7x7
3x3 filter, applied with stride 1
pad with 1 pixel border => what is the output?

```
(recall:)
(N - F) / stride + 1
```

#### In practice: Common to zero pad the border

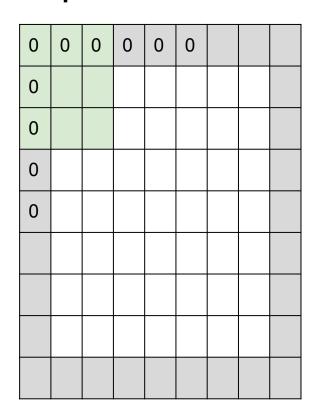


e.g. input 7x7
3x3 filter, applied with stride 1
pad with 1 pixel border => what is the output?

7x7 output!

```
(recall:)
(N + 2P - F) / stride + 1
```

#### In practice: Common to zero pad the border



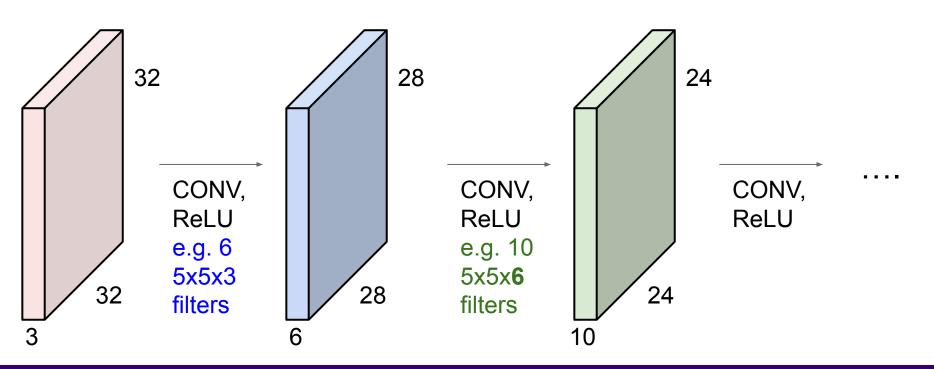
e.g. input 7x7
3x3 filter, applied with stride 1
pad with 1 pixel border => what is the output?

#### 7x7 output!

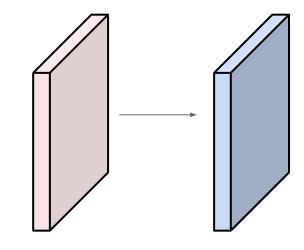
in general, common to see CONV layers with stride 1, filters of size FxF, and zero-padding with (F-1)/2. (will preserve size spatially)

#### Remember back to...

E.g. 32x32 input convolved repeatedly with 5x5 filters shrinks volumes spatially! (32 -> 28 -> 24 ...). Shrinking too fast is not good, doesn't work well.



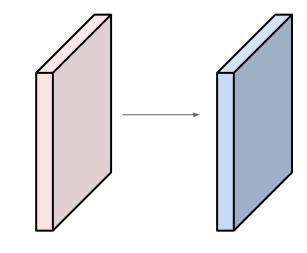
Input volume: **32x32x3** 10 5x5 filters with stride 1, pad 2



Output volume size: ?

Input volume: 32x32x3

10 5x5 filters with stride 1, pad 2



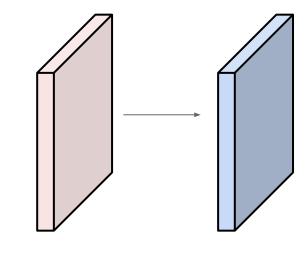
Output volume size:

$$(32+2*2-5)/1+1 = 32$$
 spatially, so

32x32x10

Input volume: 32x32x3

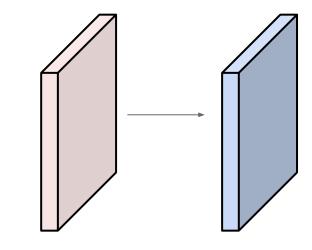
10 5x5 filters with stride 1, pad 2



Number of parameters in this layer?

Input volume: 32x32x3

10 5x5 filters with stride 1, pad 2



Number of parameters in this layer? each filter has 5\*5\*3 + 1 = 76 params

(+1 for bias)

#### Convolution layer: summary

Let's assume input is W<sub>1</sub> x H<sub>1</sub> x C Conv layer needs 4 hyperparameters:

- Number of filters **K**
- The filter size **F**
- The stride S
- The zero padding **P**

This will produce an output of W<sub>2</sub> x H<sub>2</sub> x K where:

- $-W_2 = (W_1 F + 2P)/S + 1$
- $H_2 = (H_1 F + 2P)/S + 1$

Number of parameters: F<sup>2</sup>CK and K biases

#### Convolution layer: summary

Common settings:

Let's assume input is  $W_1 \times H_1 \times C$ 

Conv layer needs 4 hyperparameters:

- Number of filters **K**
- The filter size **F**
- The stride **S**
- The zero padding **P**

This will produce an output of W<sub>2</sub> x H<sub>2</sub> x K where:

- $W_2 = (W_1 F + 2P)/S + 1$
- $H_2 = (H_1 F + 2P)/S + 1$

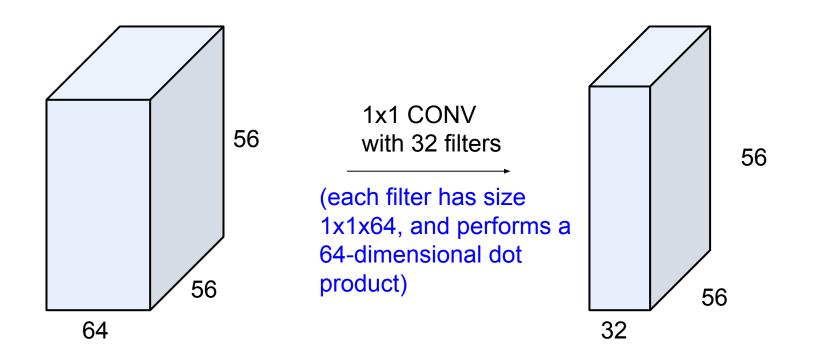
Number of parameters: F<sup>2</sup>CK and K biases

K = (powers of 2, e.g. 32, 64, 128, 512)
- F = 3, S = 1, P = 1

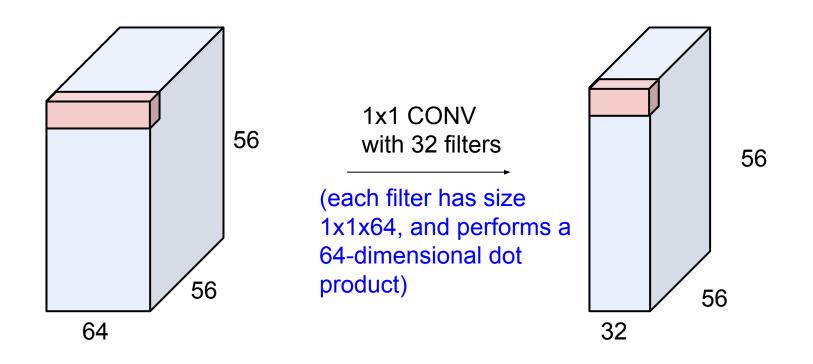
F = 5, S = 1, P = 2
F = 5, S = 2, P = ? (whatever fits)

- F = 1, S = 1, P = 0

#### (btw, 1x1 convolution layers make perfect sense)



### (btw, 1x1 convolution layers make perfect sense)



# Example: CONV layer in PyTorch

### Conv layer needs 4 hyperparameters:

- Number of filters K
- The filter size F
- The stride S
- The zero padding P

#### Conv2d

CLASS torch.nn.Conv2d(in\_channels, out\_channels, kernel\_size, stride=1, padding=0,
 dilation=1, groups=1, bias=True)

[SOURCE]

Applies a 2D convolution over an input signal composed of several input planes.

In the simplest case, the output value of the layer with input size  $(N,C_{\rm in},H,W)$  and output  $(N,C_{\rm out},H_{\rm out},W_{\rm out})$  can be precisely described as:

$$\mathrm{out}(N_i, C_{\mathrm{out}_j}) = \mathrm{bias}(C_{\mathrm{out}_j}) + \sum_{k=0}^{C_{\mathrm{in}}-1} \mathrm{weight}(C_{\mathrm{out}_j}, k) \star \mathrm{input}(N_i, k)$$

where  $\star$  is the valid 2D cross-correlation operator, N is a batch size, C denotes a number of channels, H is a height of input planes in pixels, and W is width in pixels.

- stride controls the stride for the cross-correlation, a single number or a tuple.
- padding controls the amount of implicit zero-paddings on both sides for padding number of points for each dimension.
- dilation controls the spacing between the kernel points; also known as the à trous algorithm. It is harder to
  describe, but this link has a nice visualization of what dilation does.
- groups controls the connections between inputs and outputs. in\_channels and out\_channels must both be divisible by groups. For example,
  - o At groups=1, all inputs are convolved to all outputs.
  - At groups=2, the operation becomes equivalent to having two conv layers side by side, each seeing half the input channels, and producing half the output channels, and both subsequently concatenated.
  - At groups= in\_channels , each input channel is convolved with its own set of filters, of size:  $\left| \frac{C_{\rm out}}{C_{\rm in}} \right|$ .

The parameters kernel\_size, stride, padding, dilation can either be:

- a single int in which case the same value is used for the height and width dimension
- a tuple of two ints in which case, the first int is used for the height dimension, and the second int for the width dimension

PyTorch is licensed under BSD 3-clause.

# Example: CONV layer in Keras

#### Conv layer needs 4 hyperparameters:

- Number of filters K
- The filter size F
- The stride S
- The zero padding P

Conv2D [source]

keras.layers.Conv2D(filters, kernel\_size, strides=(1, 1), padding='valid', data\_format=None, d

2D convolution layer (e.g. spatial convolution over images).

This layer creates a convolution kernel that is convolved with the layer input to produce a tensor of outputs. If use\_bias is True, a bias vector is created and added to the outputs. Finally, if activation is not None, it is applied to the outputs as well.

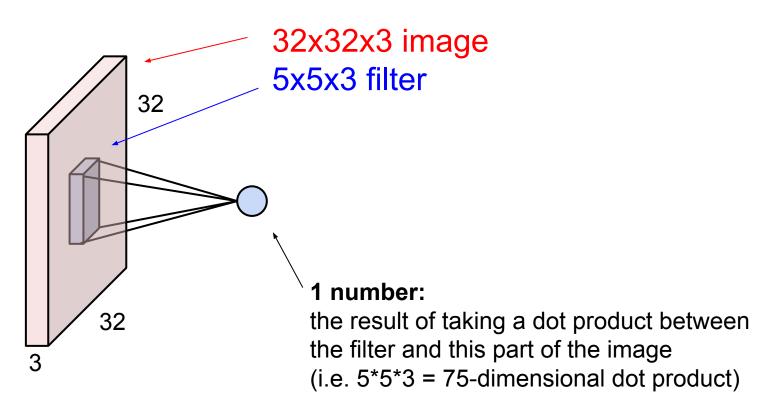
When using this layer as the first layer in a model, provide the keyword argument input\_shape (tuple of integers, does not include the batch axis), e.g. input\_shape=(128, 128, 3) for 128x128 RGB pictures in | data format="channels last" |

#### Arguments

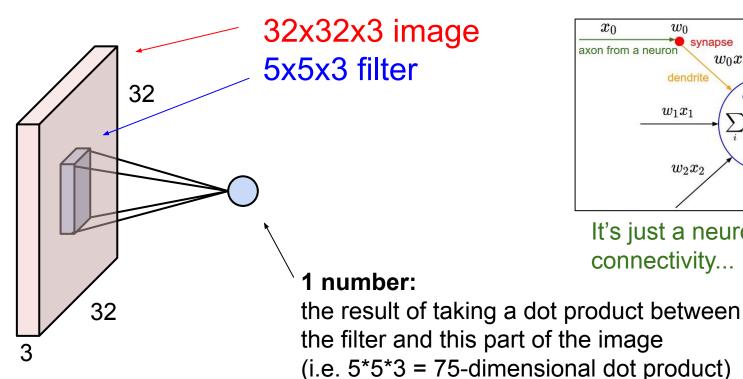
- filters: Integer, the dimensionality of the output space (i.e. the number of output filters in the convolution).
- kernel\_size: An integer or tuple/list of 2 integers, specifying the height and width of the 2D convolution window. Can be a single integer to specify the same value for all spatial dimensions.
- strides: An integer or tuple/list of 2 integers, specifying the strides of the convolution along the
  height and width. Can be a single integer to specify the same value for all spatial dimensions.
   Specifying any stride value != 1 is incompatible with specifying any dilation\_rate value != 1.
- padding: one of "valid" or "same" (case-insensitive). Note that "same" is slightly inconsistent across backends with strides != 1. as described here
- data\_format: A string, one of "channels\_last" or "channels\_first". The ordering of the dimensions in the inputs. "channels\_last" corresponds to inputs with shape (batch, height, width, channels) while "channels\_first" corresponds to inputs with shape (batch, channels, height, width). It defaults to the image\_data\_format value found in your Keras config file at ~/.keras/keras.json. If you never set it, then it will be "channels\_last".

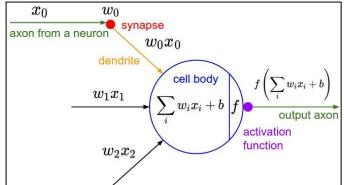
Keras is licensed under the MIT license.

### The brain/neuron view of CONV Layer



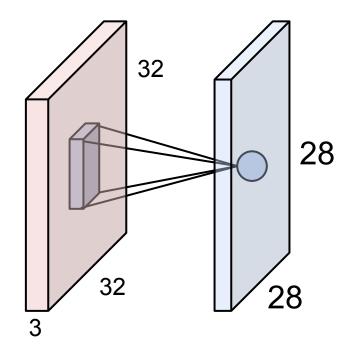
### The brain/neuron view of CONV Layer

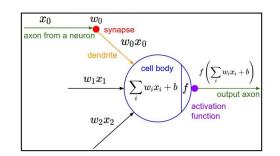




It's just a neuron with local

### Receptive field



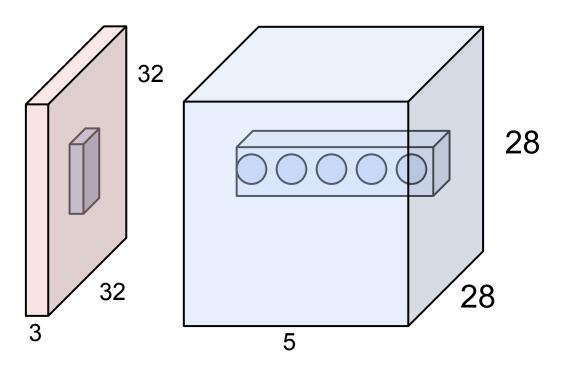


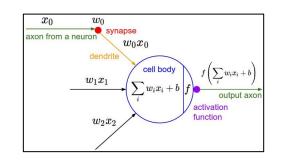
An activation map is a 28x28 sheet of neuron outputs:

- 1. Each is connected to a small region in the input
- 2. All of them share parameters

"5x5 filter" -> "5x5 receptive field for each neuron"

## The brain/neuron view of CONV Layer





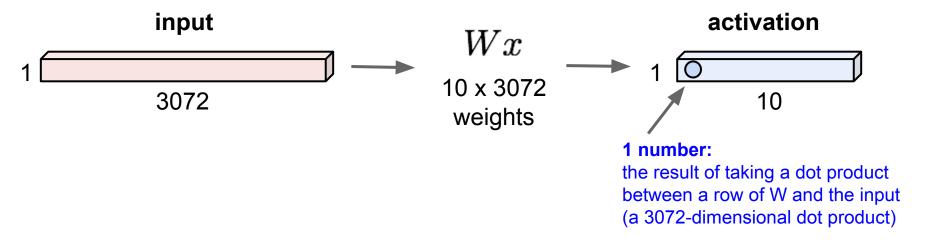
E.g. with 5 filters, CONV layer consists of neurons arranged in a 3D grid (28x28x5)

There will be 5 different neurons all looking at the same region in the input volume

# Reminder: Fully Connected Layer

32x32x3 image -> stretch to 3072 x 1

Each neuron looks at the full input volume



two more layers to go: POOL/FC RELU RELU RELU RELU RELU RELU CONV CONV CONV CONV CONV CONV FC car truck airplane ship horse

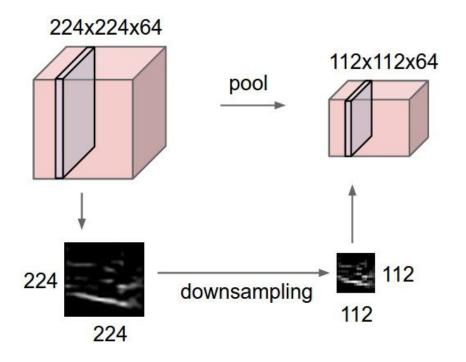
Ranjay Krishna, Aditya Kusupati

Lecture 5 - 117

April 11, 2023

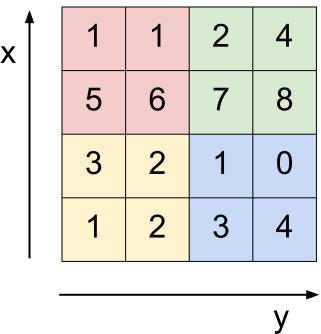
# Pooling layer

- makes the representations smaller and more manageable
- operates over each activation map independently:



## MAX POOLING

# Single depth slice



max pool with 2x2 filters and stride 2

6	8
3	4

# Pooling layer: summary

Let's assume input is W<sub>1</sub> x H<sub>1</sub> x C Conv layer needs 2 hyperparameters:

- The spatial extent **F**
- The stride S

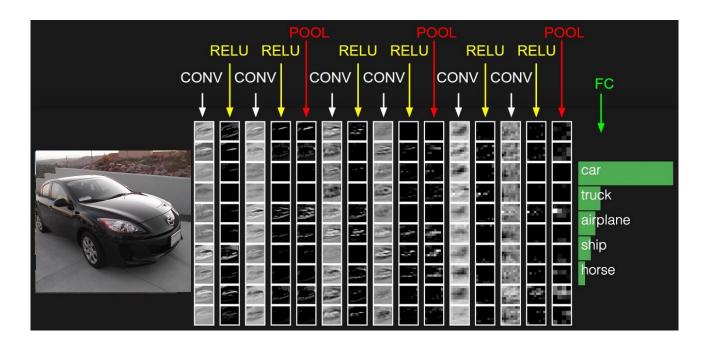
This will produce an output of  $W_2 \times H_2 \times C$  where:

- $W_2 = (W_1 F)/S + 1$
- $H_2^- = (H_1 F)/S + 1$

Number of parameters: 0

# Fully Connected Layer (FC layer)

 Contains neurons that connect to the entire input volume, as in ordinary Neural Networks



### [ConvNetJS demo: training on CIFAR-10]

#### ConvNetJS CIFAR-10 demo

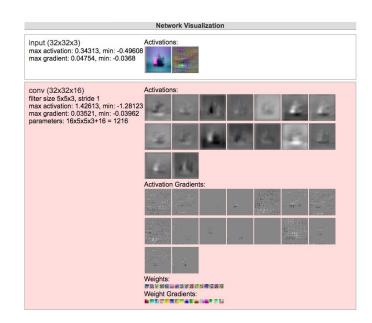
#### Description

This demo trains a Convolutional Neural Network on the <u>CIFAR-10 dataset</u> in your browser, with nothing but Javascript. The state of the art on this dataset is about 90% accuracy and human performance is at about 94% (not perfect as the dataset can be a bit ambiguous). I used <u>this python script</u> to parse the <u>original files</u> (python version) into batches of images that can be easily loaded into page DOM with img tags.

This dataset is more difficult and it takes longer to train a network. Data augmentation includes random flipping and random image shifts by up to 2px horizontally and verically.

By default, in this demo we're using Adadelta which is one of per-parameter adaptive step size methods, so we don't have to worry about changing learning rates or momentum over time. However, I still included the text fields for changing these if you'd like to play around with SGD+Momentum trainer.

Report questions/bugs/suggestions to @karpathy.



http://cs.stanford.edu/people/karpathy/convnetjs/demo/cifar10.html

# Summary

- ConvNets stack CONV,POOL,FC layers
- Trend towards smaller filters and deeper architectures
- Trend towards getting rid of POOL/FC layers (just CONV)
- Historically architectures looked like [(CONV-RELU)\*N-POOL?]\*M-(FC-RELU)\*K,SOFTMAX
  - where N is usually up to  $\sim$ 5, M is large, 0 <= K <= 2.
  - but recent advances such as ResNet/GoogLeNet have challenged this paradigm