CSE 490 GZ Introduction to Data Compression Winter 2004

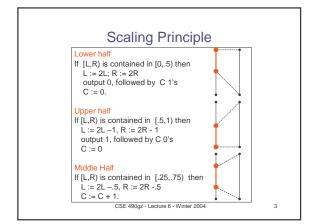
Arithmetic Coding: Scaling, Context, Adaptation

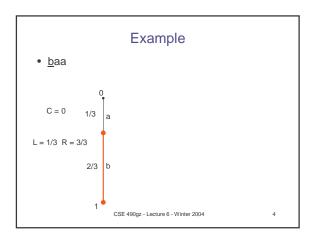
Scaling

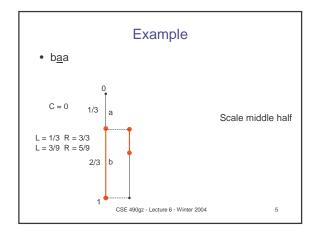
- Scaling:
 - By scaling we can keep L and R in a reasonable range of values so that W = R - L does not underflow.
 - The code can be produced progressively, not at the end
 - Complicates decoding some.

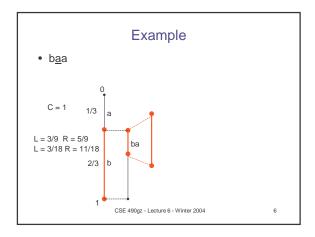
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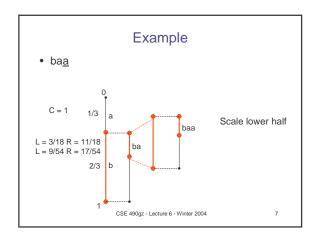
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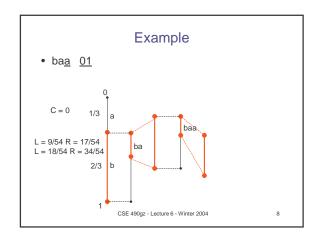


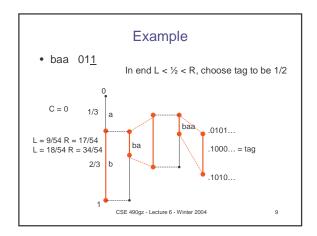


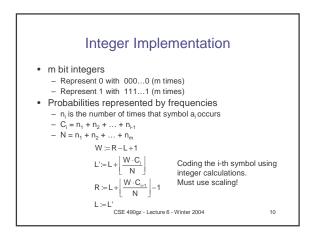


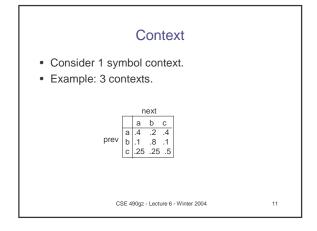


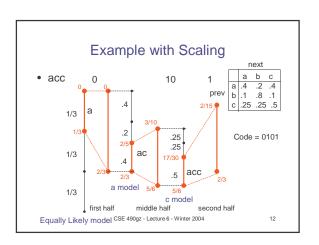












Arithmetic Coding with Context

- Maintain the probabilities for each context.
- For the first symbol use the equal probability model
- For each successive symbol use the model for the previous symbol.

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Adaptation

- Simple solution Equally Probable Model.
 - Initially all symbols have frequency 1.
 - After symbol x is coded, increment its frequency by 1
 - Use the new model for coding the next symbol
- Example in alphabet a,b,c,d

a a b a a c After aabaac is encoded The probability model is a 5/10 b 2/10 c 2/10 d 1/10

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Zero Frequency Problem

- · How do we weight symbols that have not occurred yet.
 - Equal weights? Not so good with many symbols
 - Escape symbol, but what should its weight be?
 - When a new symbol is encountered send the <esc>, followed by the symbol in the equally probable model. (Both encoded arithmetically.)

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PPM

- · Prediction with Partial Matching
 - Cleary and Witten (1984)
- · State of the art arithmetic coder
 - Arbitrary order context
 - The context chosen is one that does a good prediction given the past
 - Adaptive
- Example
 - Context "the" does not predict the next symbol "a" well. Move to the context "he" which does.

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Arithmetic vs. Huffman

- Both compress very well. For m symbol grouping.
 - Huffman is within 1/m of entropy.
- Arithmetic is within 2/m of entropy.
- Context
 - Huffman needs a tree for every context.
 - Arithmetic needs a small table of frequencies for every context.
- Adaptation
 - Huffman has an elaborate adaptive algorithm
 - Arithmetic has a simple adaptive mechanism.
- Bottom Line Arithmetic is more flexible than Huffman.

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