CSE 490 GZ Introduction to Data Compression Winter 2002

Arithmetic Coding: Scaling, Context, Adaptation

Scaling

- · Scaling:
 - By scaling we can keep L and R in a reasonable range of values so that W = R - L does not underflow.
 - The code can be produced progressively, not at the end.
 - Complicates decoding some.

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Scaling Principle

Lower half

If [L,R) is contained in [0,.5) then

L:= 2L; R:= 2Routput 0, followed by C 1's

C:= 0.

Upper half

If [L,R) is contained in [.5,1) then

L:= 2L-1, R:= 2R-1output 1, followed by C 0's

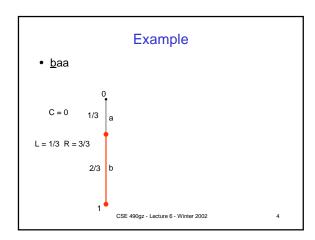
C:= 0

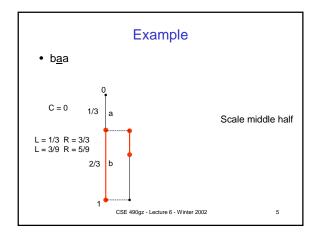
Middle Half

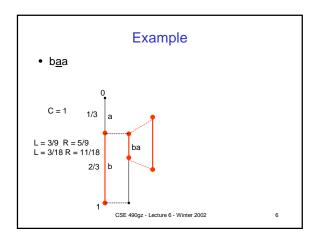
If [L,R] is contained in [.25,.75) then

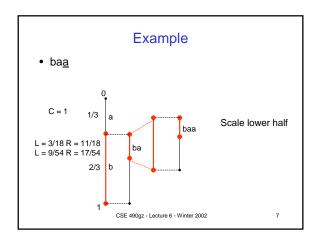
L:= 2L-.5, R:= 2R-.5C:= C+1.

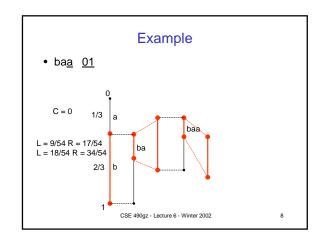
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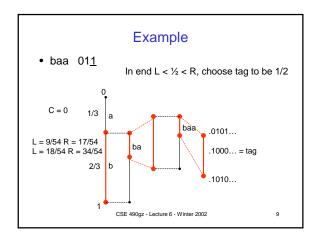


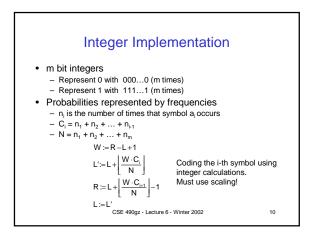


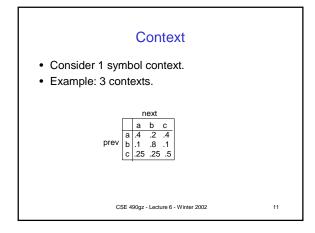


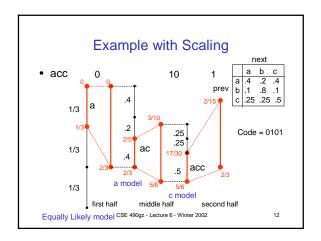












Arithmetic Coding with Context

- · Maintain the probabilities for each context.
- For the first symbol use the equal probability model
- For each successive symbol use the model for the previous symbol.

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Adaptation

- Simple solution Equally Probable Model.
 - Initially all symbols have frequency 1.
 - After symbol x is coded, increment its frequency by 1
 - Use the new model for coding the next symbol
- Example in alphabet a,b,c,d

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Zero Frequency Problem

- · How do we weight symbols that have not occurred yet.
 - Equal weights? Not so good with many symbols
 - Escape symbol, but what should its weight be?
 - When a new symbol is encountered send the <esc>, followed by the symbol in the equally probable model. (Both encoded arithmetically.)

aabaac After aabaac is encoded 1 2 2 3 4 4 The probability model is 0 0 1 1 1 1 h 0 b 1/7 a 4/7 С 000001 c 1/7 d 0 000000 <esc> 1/7 <esc> 1 1 1 1 1 1 1

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PPM

- · Prediction with Partial Matching
 - Cleary and Witten (1984)
- · State of the art arithmetic coder
 - Arbitrary order context
 - The context chosen is one that does a good prediction given the past
 - Adaptive
- Example
 - Context "the" does not predict the next symbol "a" well. Move to the context "he" which does.

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Arithmetic vs. Huffman

- · Both compress very well. For m symbol grouping.
 - Huffman is within 1/m of entropy.
 - Arithmetic is within 2/m of entropy.
- Context
 - Huffman needs a tree for every context.
 - Arithmetic needs a small table of frequencies for every context.
- Adaptation
 - Huffman has an elaborate adaptive algorithm
- Arithmetic has a simple adaptive mechanism.
- Bottom Line Arithmetic is more flexible than Huffman.

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