

**CSE 490 GZ**  
**Final Exam**  
**March 19, 2002**

For each problem give as brief an answer as possible. The questions can be answered in any order.

- 1) Answer each of these questions True or False.
  - a) JPEG 2000 may block the transformed image to allow for different bit allocation for different blocks.
  - b) JPEG blocks the image where each block is transformed using the wavelet transform.
  - c) In audio coding some transform coefficients can be ignored (set to zero) because the human ear cannot perceive their presence or not.
  - d) In group-of-frames video coding the previous frame is used to predict the current frame.
  - e) In image and video coding the chrominance data is sampled at a higher rate than the luminance data.
  - f) Finding the closest codeword among  $n$  codewords to an input vector requires time linear in  $n$  on average.
  - g) Blocked lapped transforms when applied to images leave *no* blocking artifacts.
  - h) In motion compensation in video coders motion vectors can be compressed using predictive coding.
  - i) Resolution scalability in image compression means that images can be shown in good fidelity, depending on the bit rate, in various sizes.
  - j) Bit-plane coding of DCT coefficients leads to a higher PSNR than does the JPEG style run-length coding.
  - k) SPIHT, GTW, and EBCOT each produce an embedded code, which can be truncated to any length to remain a valid code at a lower bit rate and fidelity.
  - l) Frame-by-frame video coding is error resilient.
  - m) In JPEG, predictive coding is used for the DC coefficient but not the AC coefficients.
  - n) Audio coding does not use the PSNR metric for fidelity.
  - o) Each B frame in MPEG-1 are predicted by the previous I or P frame and the successive I or P frame.
- 2) For each of the following methods explain briefly what happens in encoding but not in decoding that makes encoding slower than decoding.
  - a) LZ77
  - b) Burrows-Wheeler Transform
  - c) MPEG – 1
- 3) Assuming an initial dictionary
  - 0 a
  - 1 b
  - 2 c

decode the following sequence using LZW with the doubling strategy showing the decoder's dictionary at each step.

0010011100010

- 4) Decode the following using the Burrows-Wheeler Transform:  $L = \text{bbabbaa}$  and  $X = 2$ . In the process compute the mapping  $T$  and use it in the decoding.
- 5) Consider the probabilities on the symbols  $a : \frac{1}{4}$ ,  $b : \frac{3}{4}$ . Use arithmetic coding with scaling to decode the sequence 011 that encodes 4 symbols. Show the steps along the way.
- 6) Do one iteration of the Lloyd algorithm with initial codewords 2 and 3 on the data

|             |     |     |     |    |    |     |     |     |
|-------------|-----|-----|-----|----|----|-----|-----|-----|
| pixel value | 0   | 1   | 2   | 3  | 4  | 5   | 6   | 7   |
| frequency   | 200 | 100 | 100 | 50 | 50 | 100 | 200 | 200 |

Compute the before and after distortion as well as the steps in the iteration.

- 7) Consider the following symbols and their frequencies

|           |   |   |    |   |   |   |    |   |
|-----------|---|---|----|---|---|---|----|---|
| symbol    | a | b | c  | d | e | f | g  | h |
| frequency | 3 | 8 | 10 | 1 | 5 | 7 | 20 | 4 |

- a) Design an optimal Huffman tree for these symbols with their frequencies.
  - b) What is the average bit rate for the code?
- 8) Consider the Sequitur algorithm in the state after the prefix abaab of abaabaaba has been processed.

a b a a b a a b a

$S \rightarrow AaA$

$A \rightarrow ab$

Show the remaining steps in the Sequitur algorithm.

- 9)