

# CSE 484 / CSE M 584: Asymmetric Cryptography

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# Announcements

- Physical security lecture: Wednesday, March 9

# Begin Review Slides

# RSA Signatures

- Public key is  $(n,e)$ , private key is  $(n,d)$
- To **sign** message  $m$ :  $s = m^d \bmod n$ 
  - Signing & decryption are same **underlying** operation in RSA
  - It's infeasible to compute  $s$  on  $m$  if you don't know  $d$
- To **verify** signature  $s$  on message  $m$ :  
verify that  $s^e \bmod n = (m^d)^e \bmod n = m$ 
  - Just like encryption (for RSA primitive)
  - Anyone who knows  $n$  and  $e$  (public key) can verify signatures produced with  $d$  (private key)
- In practice, also need padding & hashing
  - Without padding and hashing: Consider multiplying two signatures together
  - Standard padding/hashing schemes exist for RSA signatures

# End Review Slides

- To sign message  $m$ :  $s = m^d \bmod n$
- Suppose sign  $m = 1 \rightarrow s = m^d \bmod n$  is 1
- Suppose sign  $m$  for any  $m \rightarrow s = m^d \bmod n$  is 1
  - Adversary gets  $m$  and  $s$
  - Adversary computes  $s' = s^2 \bmod n$  and  $m' = m^2 \bmod n$
  - Adversary sends  $s', m'$  to receiver
  - Signature  $s'$  on  $m'$  verifies as correct
    - $(s')^e \bmod n = (s^2)^e \bmod n = (m^{d2})^e \bmod n = m^2$
- Suppose adversary receives two message-signature pairs  $(m_1, s_1), (m_2, s_2)$ ?
- Thus, sign  $H(m)$ , not  $m$ , where  $H$  hashes to a number between 0 and  $n-1$

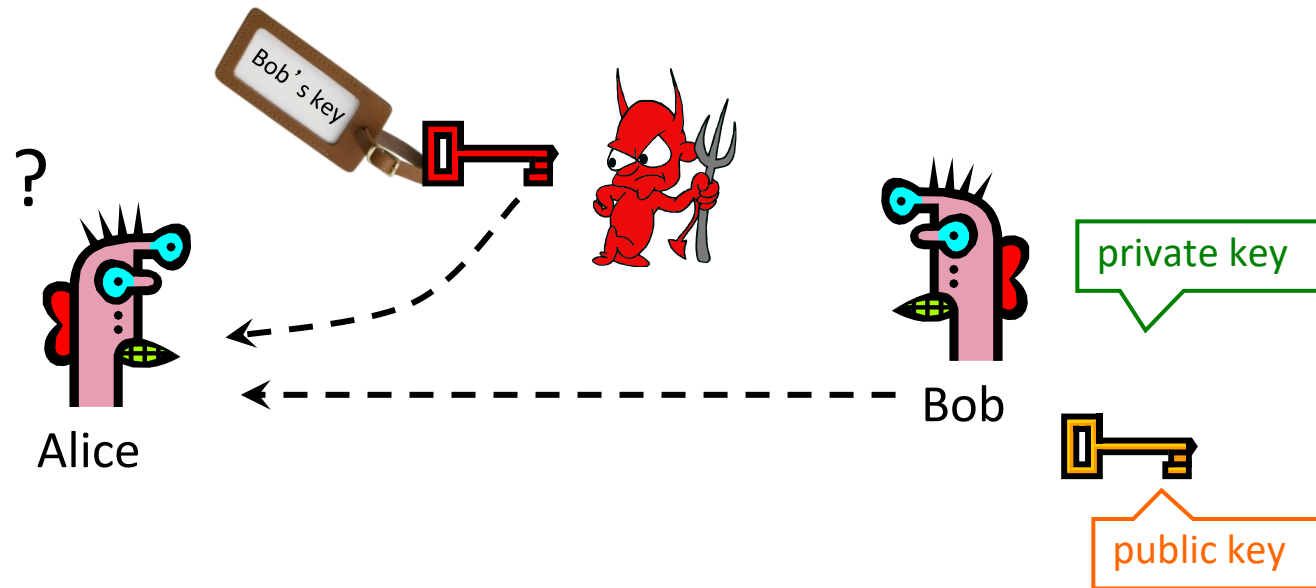
# DSS Signatures

- Digital Signature Standard (DSS)
  - U.S. government standard (1991, most recent rev. 2013)
- Public key:  $(p, q, g, y=g^x \bmod p)$ , private key:  $x$
- **Each signing operation picks a new random value**, to use during signing. Security breaks if two messages are signed with that same value.
- Security of DSS requires hardness of discrete log
  - If could solve discrete logarithm problem, would extract  $x$  (private key) from  $g^x \bmod p$  (public key)
- Again: We've discussed discrete logs modulo integers; significant advantages to using elliptic curve groups instead.

# Post-Quantum

- If quantum computer become a reality
  - It becomes much more efficient to break conventional asymmetric encryption schemes (e.g., factoring becomes “easy”)
  - For block ciphers (symmetric encryption), use 256-bit keys for 128-bits of security
- There exists efforts to make quantum-resilient asymmetric encryption schemes

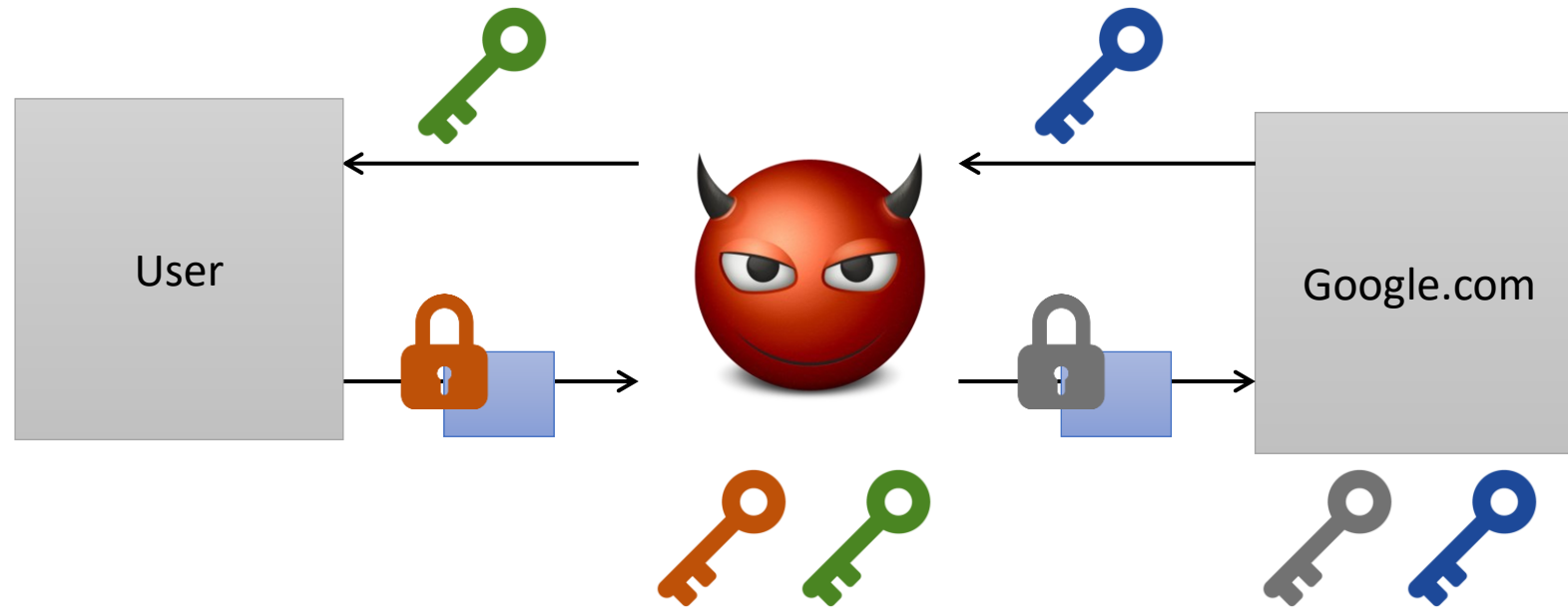
# Authenticity of Public Keys



Problem: How does Alice know that the public key they received is really Bob's public key?



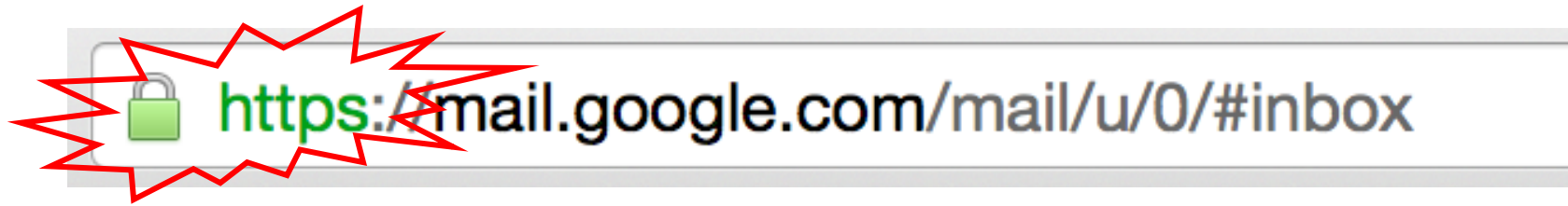
# Threat: Person-in-the Middle



# Distribution of Public Keys

- Public announcement or public directory
  - Risks: forgery and tampering
- Public-key certificate
  - Signed statement specifying the key and identity
    - $\text{sig}_{\text{CA}}(\text{"Bob"}, \text{PK}_B)$
    - Additional information often signed as well (e.g., expiration date)
- Common approach: certificate authority (CA)
  - Single agency responsible for certifying public keys
  - After generating a private/public key pair, user proves their identity and knowledge of the private key to obtain CA's certificate for the public key (offline)
  - Every computer is pre-configured with CA's public key

You encounter this every day...

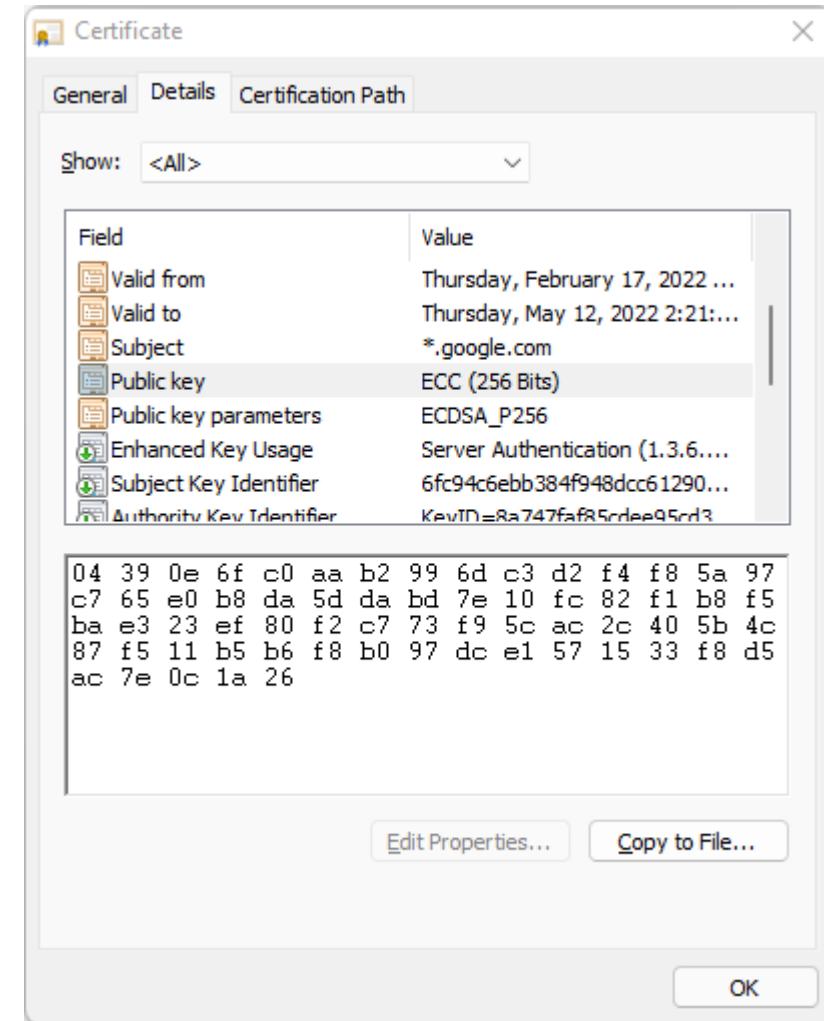
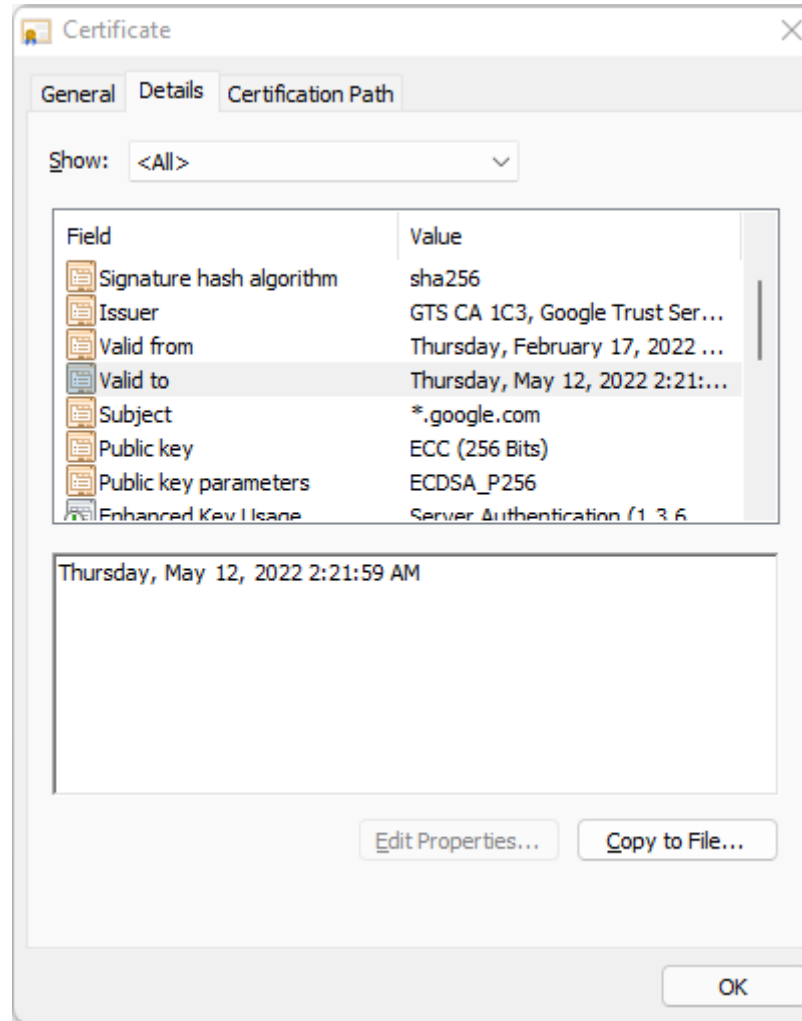
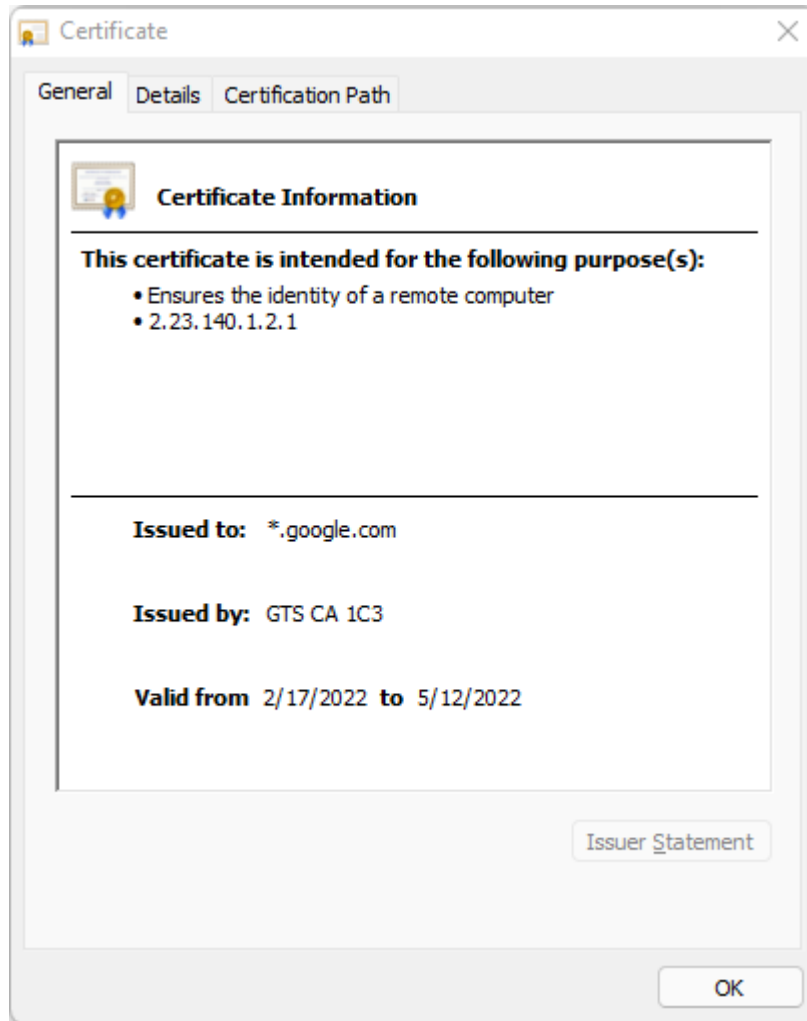


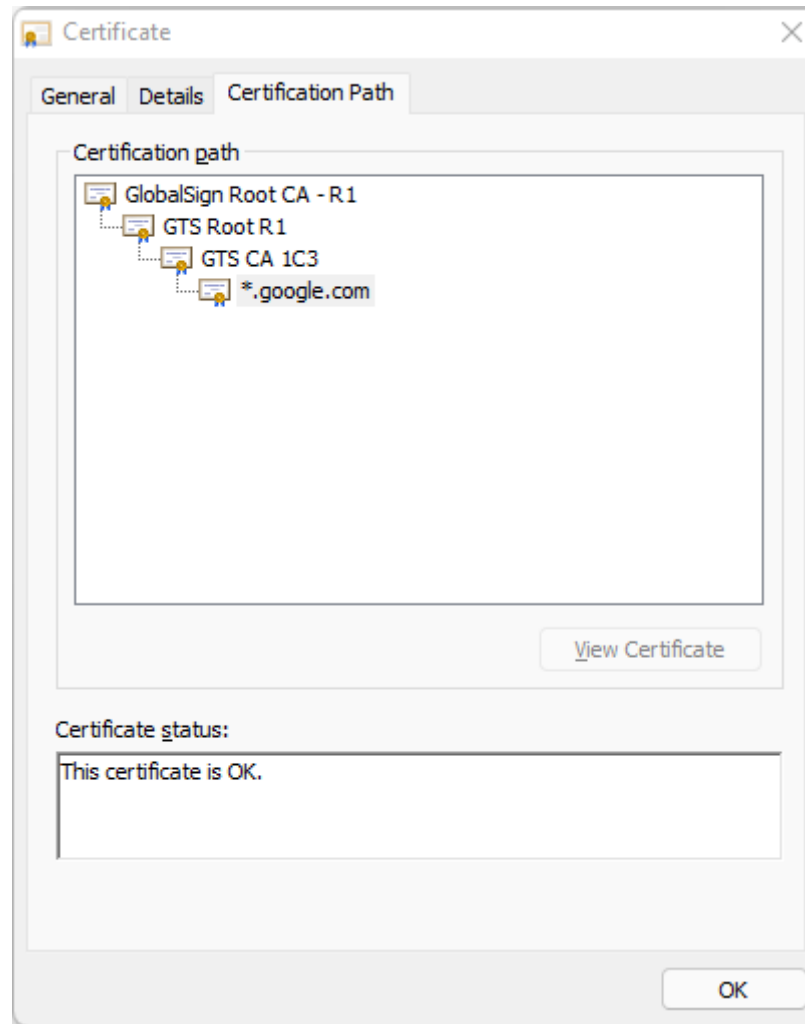
**SSL/TLS:** Encryption & authentication for connections

# SSL/TLS High Level

- SSL/TLS consists of **two** protocols
  - Familiar pattern for key exchange protocols
- Handshake protocol
  - Use **public-key cryptography** to establish a shared secret key between the client and the server
- Record protocol
  - Use the **secret symmetric key** established in the handshake protocol to protect communication between the client and the server

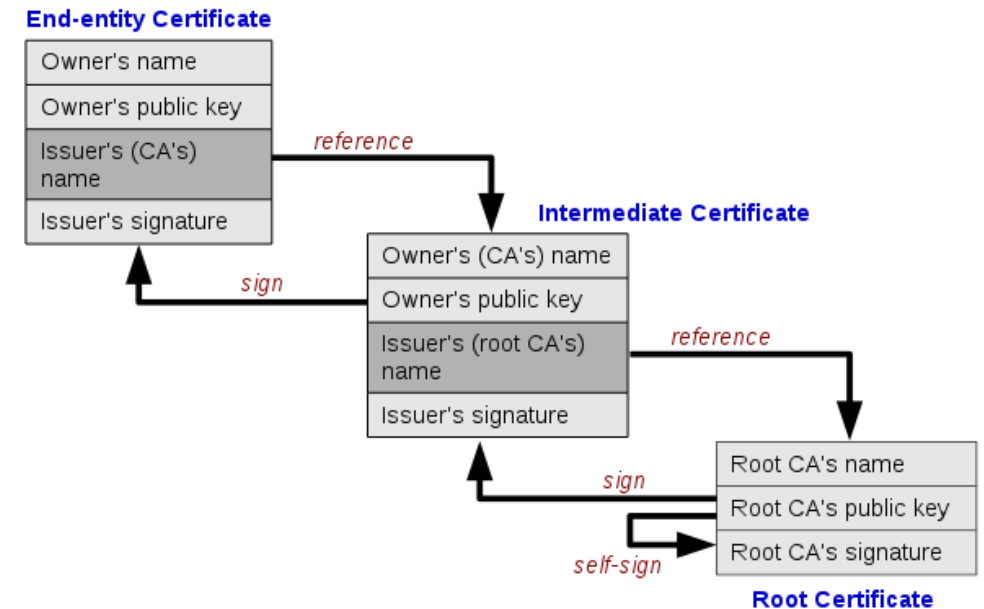
# Example of a Certificate





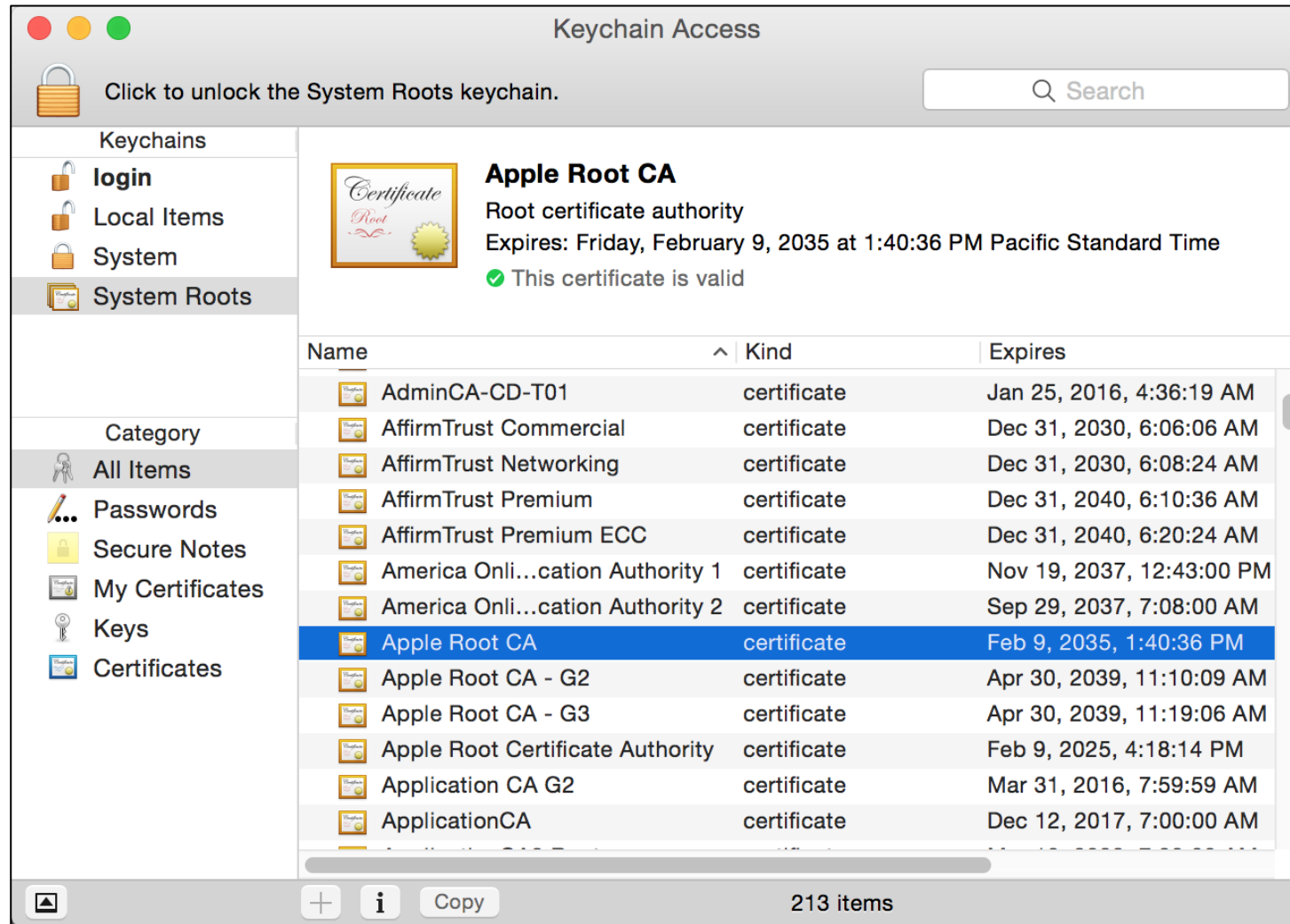
# Hierarchical Approach

- Single CA certifying every public key is impractical
- Instead, use a trusted **root authority** (e.g., Verisign)
  - Everybody must know the root's public key
  - Instead of single cert, use a **certificate chain**
    - $\text{sig}_{\text{Verisign}}(\text{"AnotherCA"}, \text{PK}_{\text{AnotherCA}})$ ,  
 $\text{sig}_{\text{AnotherCA}}(\text{"Alice"}, \text{PK}_A)$
  - Not shown in figure but important:
    - Part of each cert includes whether party is a CA or not



- What happens if root authority is ever compromised?

# Trusted(?) Certificate Authorities





# Turtles All The Way Down...



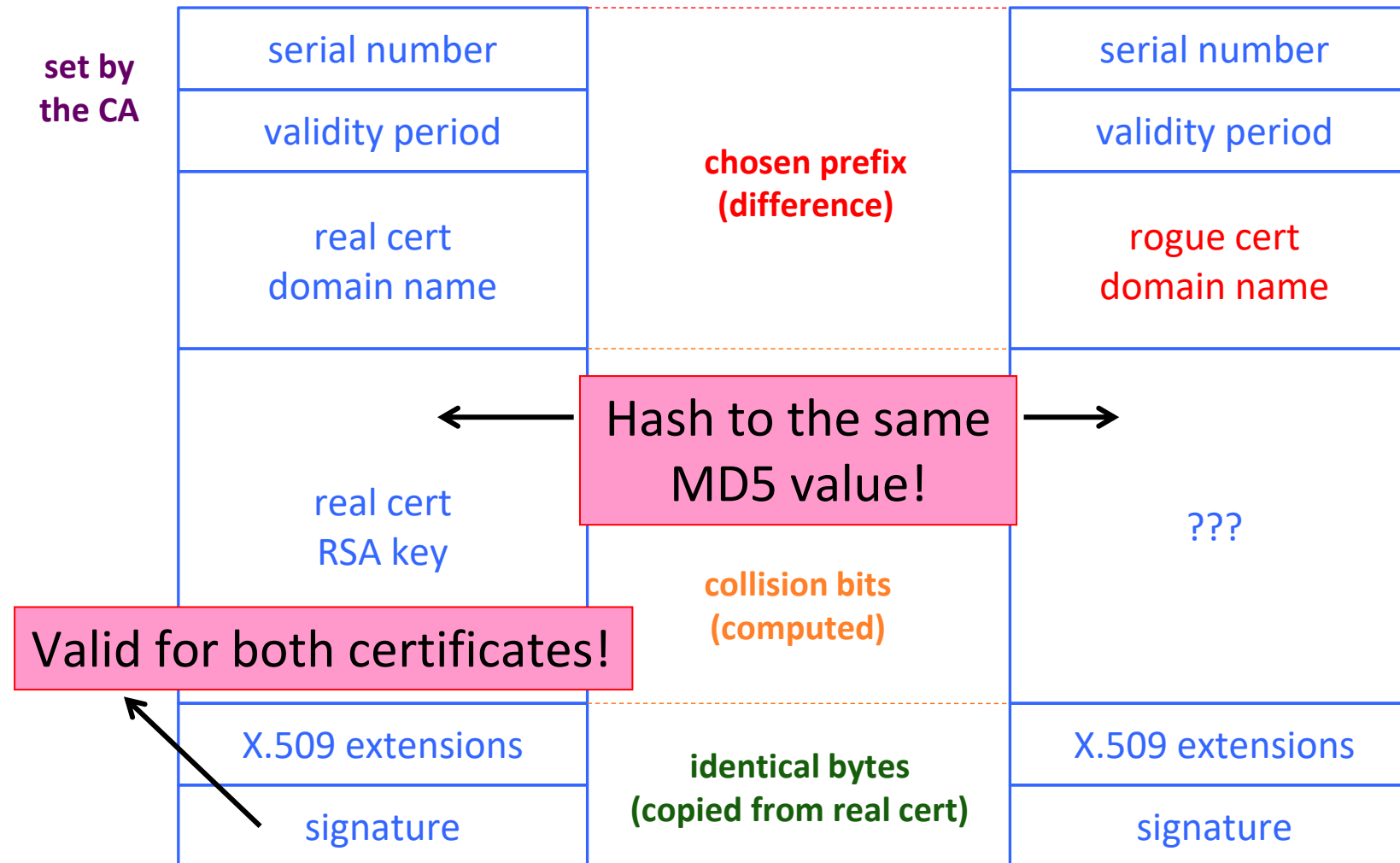
The saying holds that the world is supported by a chain of increasingly large turtles. Beneath each turtle is yet another: it is "turtles all the way down".

[Image from Wikipedia]

# Many Challenges...

- Hash collisions
- Weak security at CAs
  - Allows attackers to issue rogue certificates
- Users don't notice when attacks happen
  - We'll talk more about this later in the course
- How do you revoke certificates?

# Colliding Certificates



DigiNotar is a Dutch Certificate Authority. They sell SSL certificates.



Somehow, somebody managed to get a rogue SSL certificate from them on **July 10th, 2011**. This certificate was issued for domain name **.google.com**.

What can you do with such a certificate? Well, you can impersonate Google — assuming you can first reroute Internet traffic for google.com to you. This is something that can be done by a government or by a rogue ISP. Such a reroute would only affect users within that country or under that ISP.

## Attacking CAs

### Security of DigiNotar servers:

- All core certificate servers controlled by a single admin password (Pr0d@dm1n)
- Software on public-facing servers out of date, unpatched
- No anti-virus (could have detected attack)

# Consequences

- Attacker needs to first divert users to an attacker-controlled site instead of Google, Yahoo, Skype, but then...
  - For example, use DNS to poison the mapping of mail.yahoo.com to an IP address
- ... “authenticate” as the real site
- ... decrypt all data sent by users
  - Email, phone conversations, Web browsing

# More Rogue Certs



- In Jan 2013, a rogue \*.google.com certificate was issued by an intermediate CA that gained its authority from the Turkish root CA TurkTrust
  - TurkTrust accidentally issued intermediate CA certs to customers who requested regular certificates
  - Ankara transit authority used its certificate to issue a fake \*.google.com certificate in order to filter SSL traffic from its network
- This rogue \*.google.com certificate was trusted by every browser in the world

# Bad CAs

- **DarkMatter** (<https://groups.google.com/g/mozilla.dev.security.policy/c/nnLVNfqgz7g/m/TseYqDzaDAAJ> and [https://bugzilla.mozilla.org/show\\_bug.cgi?id=1427262](https://bugzilla.mozilla.org/show_bug.cgi?id=1427262))
  - Security company wanted to get CA status
  - Questionable practices
- **Symantec!** ([https://wiki.mozilla.org/CA:Symantec\\_Issues](https://wiki.mozilla.org/CA:Symantec_Issues))
  - Major company, regular participant in standards
  - Poor practices, mismanagement 2013-2017
  - CA distrusted in Oct 2018
- Recall: Turtles all the way down. How can we trust the CAs? What happens if we can't?

# Certificate Revocation

- Revocation is very important
- Many valid reasons to revoke a certificate
  - Private key corresponding to the certified public key has been compromised
  - User stopped paying their certification fee to this CA and CA no longer wishes to certify them
  - CA's private key has been compromised!
- Expiration is a form of revocation, too
  - Many deployed systems don't bother with revocation
  - Re-issuance of certificates is a big revenue source for certificate authorities



# Certificate Revocation Mechanisms

- Certificate revocation list (CRL)
  - CA periodically issues a signed list of revoked certificates
    - Credit card companies used to issue thick books of canceled credit card numbers
  - Can issue a “delta CRL” containing only updates
- Online revocation service
  - When a certificate is presented, recipient goes to a special online service to verify whether it is still valid
    - Like a merchant dialing up the credit card processor

Attempt to Fix CA Problems:

# Certificate Transparency

- **Problem:** browsers will think nothing is wrong with a rogue certificate until revoked
- **Goal:** make it impossible for a CA to issue a bad certificate for a domain *without the owner of that domain knowing*
- **Approach:** auditable certificate logs
  - Certificates published in public logs
  - Public logs checked for unexpected certificates

[www.certificate-transparency.org](http://www.certificate-transparency.org)

Attempt to Fix CA Problems:

# Certificate Pinning

- **Trust on first access:** tells browser how to act on subsequent connections
- HPKP – HTTP Public Key Pinning
  - Use these keys!
  - HTTP response header field `"Public-Key-Pins"`
- HSTS – HTTP Strict Transport Security
  - Only access server via HTTPS
  - HTTP response header field `"Strict-Transport-Security"`