

# CSE 484 / CSE M 584: Cryptography

Winter 2022

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# Announcements

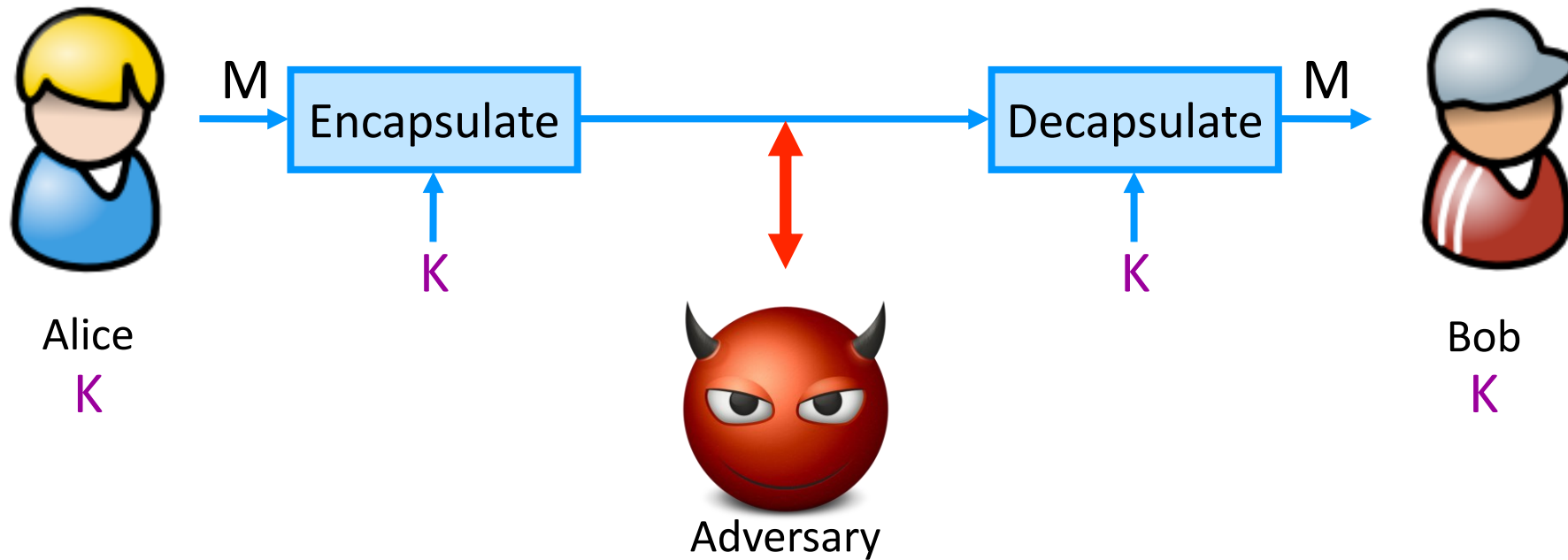
- Office Hours This Week: (Likely) all virtual as we transition to hybrid next week

# Brief Review

- Cryptography:
  - Layered approach
  - One big goal: Privacy
  - One big goal: Integrity
  - Other goals exist
- Kerckhoff's Principle
  - Algorithm public
  - Key to algorithm secret
- Randomness
  - Randomness problems can lead to security system problems

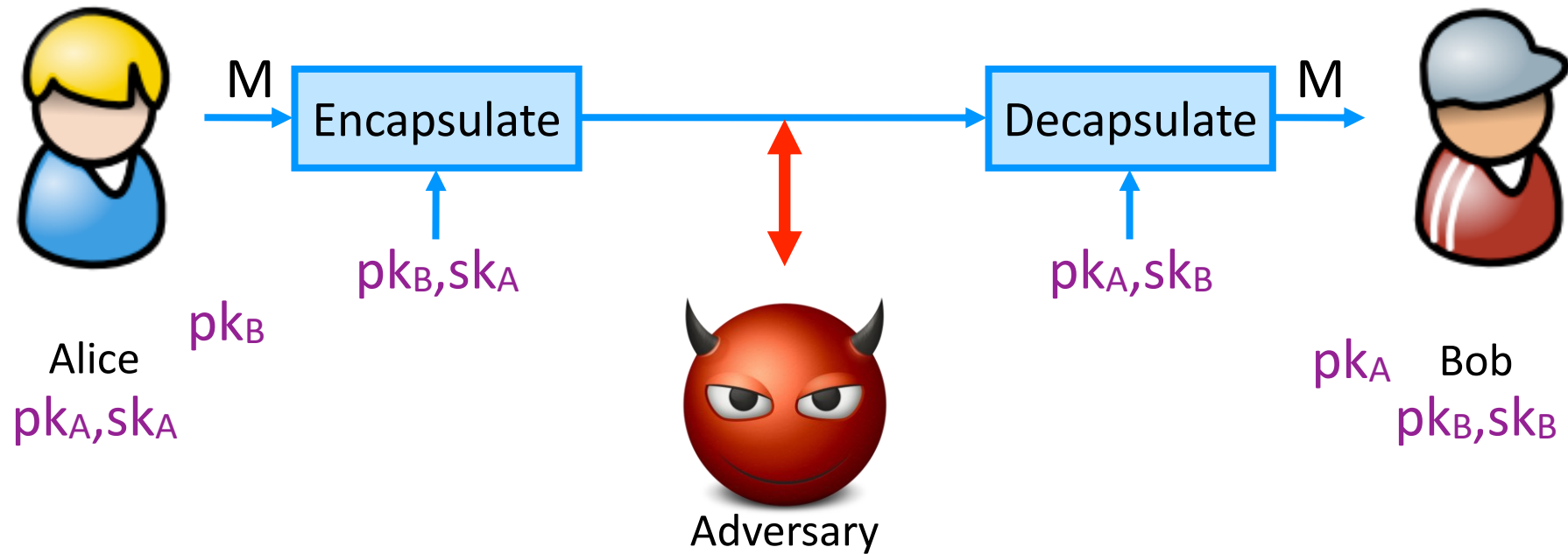
# Symmetric Setting

Both communicating parties have access to a **shared random string  $K$** , called the **key**.



# Asymmetric Setting

Each party creates a public key  $pk$  and a secret key  $sk$ .



# Flavors of Cryptography

- Symmetric cryptography
  - Both communicating parties have access to a **shared random string  $K$** , called the **key**.
  - **Challenge: How do you privately share a key?**
- Asymmetric cryptography
  - Each party creates a public key  **$pk$**  and a secret key  **$sk$** .
  - **Challenge: How do you validate a public key?**

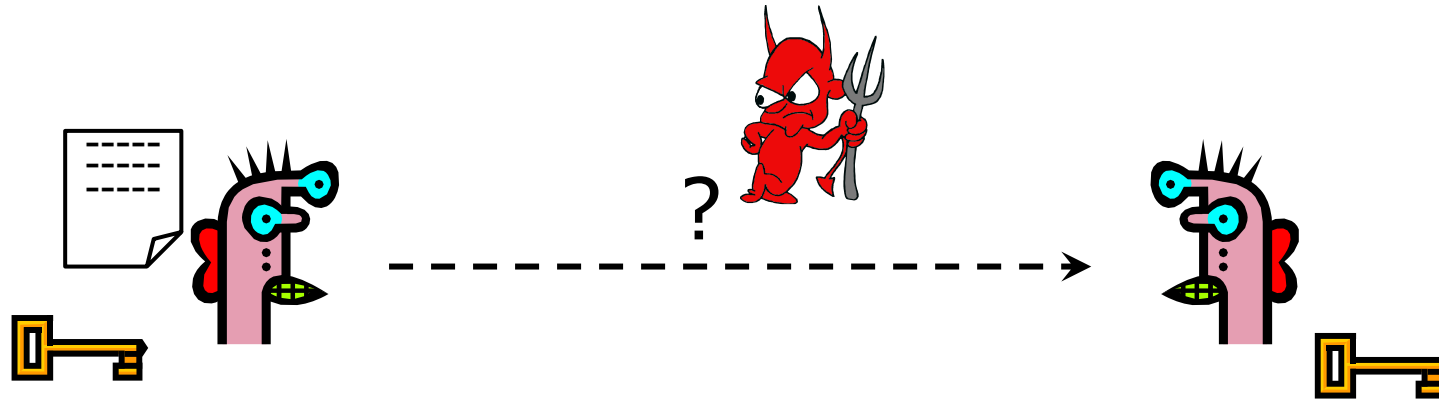
# Flavors of Cryptography

- Symmetric cryptography
  - Both communicating parties have access to a **shared random string  $K$** , called the **key**.
  - **Challenge: How do you privately share a key?**
- Asymmetric cryptography
  - Each party creates a public key  **$pk$**  and a secret key  **$sk$** .
  - **Challenge: How do you validate a public key?**
- **Key building block: Randomness** – something that the adversaries won't know and can't predict and can't figure out

# End Review



# Confidentiality: Basic Problem



Given (Symmetric Crypto): both parties know the same **secret**.

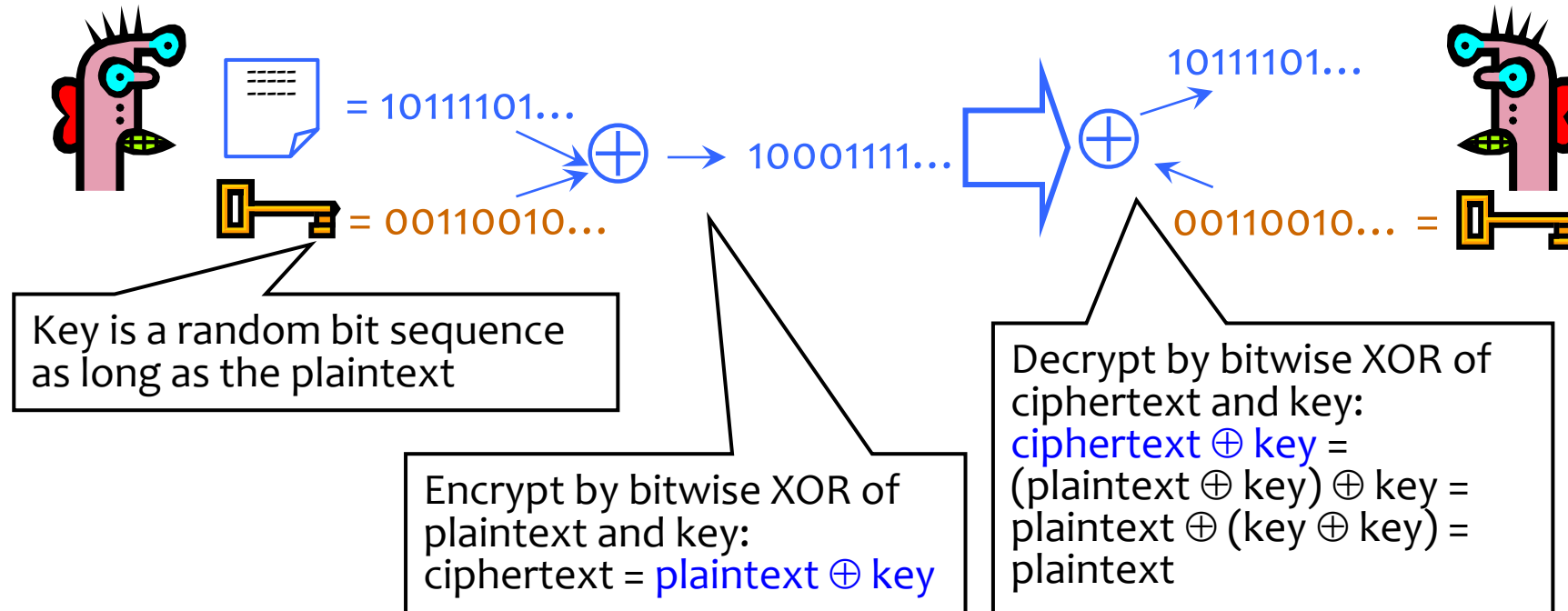
Goal: send a message confidentially.

Ignore for now: How is this achieved in practice??

# One weird bit-level trick

- XOR!
  - Just XOR with a random bit!
- Why?
  - Uniform output
  - Independent of 'message' bit

# One-Time Pad



Cipher achieves **perfect secrecy** if and only if there are **as many possible keys as possible plaintexts**, and **every key is equally likely** (Claude Shannon, 1949)

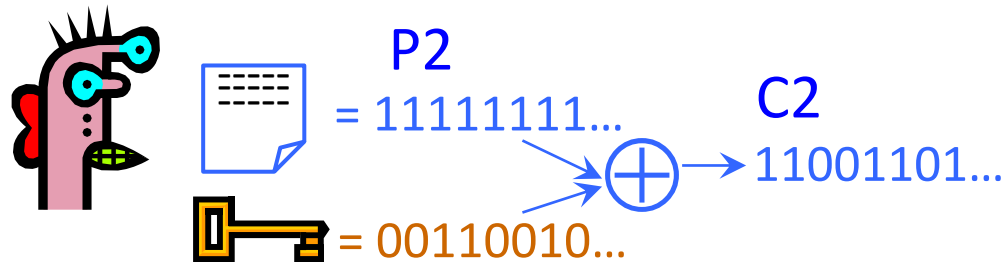
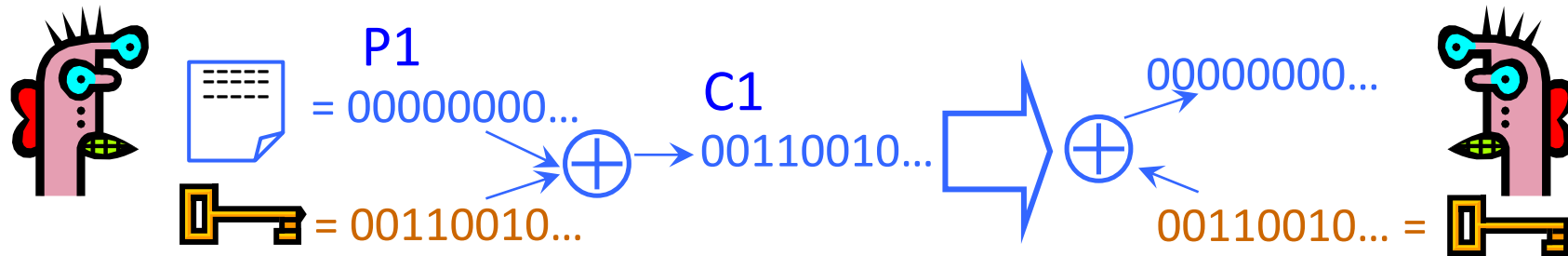
# Advantages of One-Time Pad

- Easy to compute
  - Encryption and decryption are the same operation
  - Bitwise XOR is very cheap to compute
- As secure as theoretically possible
  - Given a ciphertext, all plaintexts are equally likely, regardless of attacker's computational resources
  - ...as long as the key sequence is truly random
    - True randomness is expensive to obtain in large quantities
  - ...as long as each key is same length as plaintext
    - But how does sender communicate the key to receiver?

# Problems with the One-Time Pad?

- Breakout Discussions
- What potential security problems do you see with the one-time pad?
- (Try not to look ahead and next slides)
- Recall two key goals of cryptography: confidentiality and integrity

# Dangers of Reuse



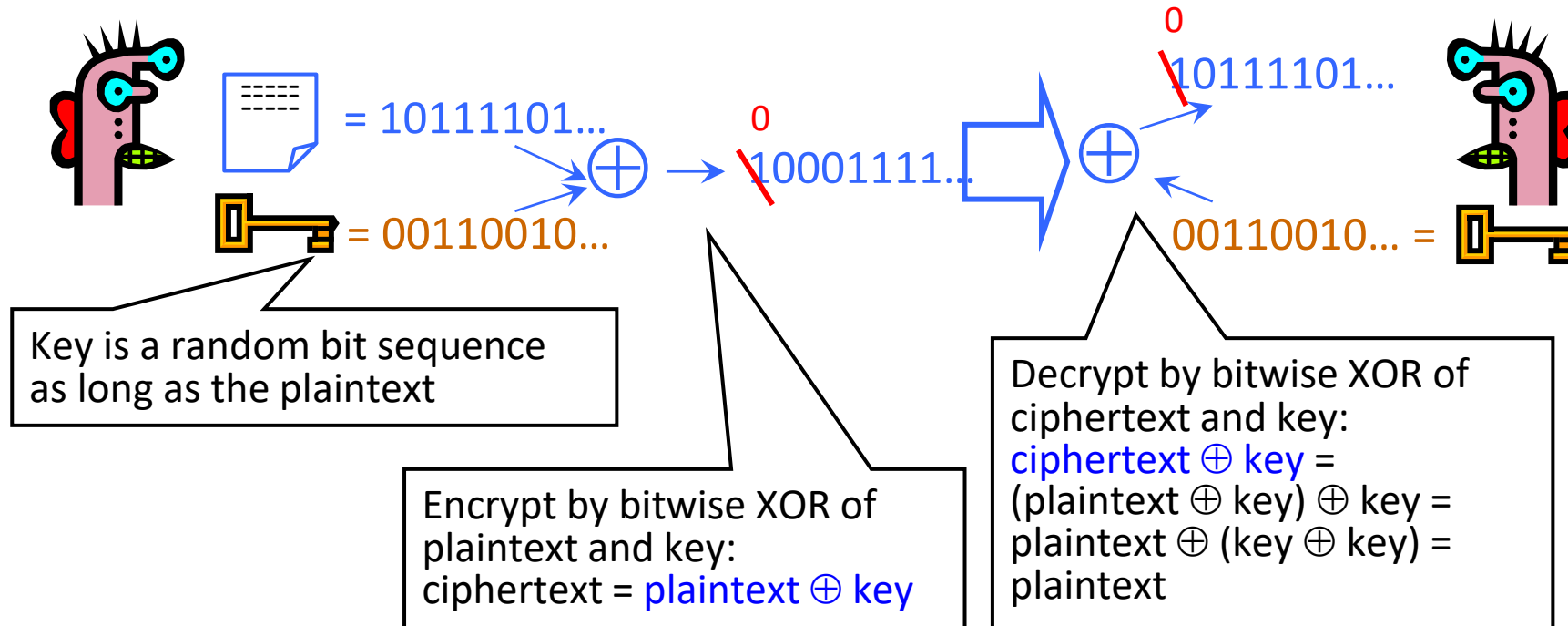
Learn relationship between plaintexts

$$\begin{aligned} C1 \oplus C2 &= (P1 \oplus K) \oplus (P2 \oplus K) = \\ &= (P1 \oplus P2) \oplus (K \oplus K) = P1 \oplus P2 \end{aligned}$$

# Problems with One-Time Pad

- (1) Key must be as long as the plaintext
  - Impractical in most realistic scenarios
  - Still used for diplomatic and intelligence traffic
- **(2) Insecure if keys are reused**
  - **Attacker can obtain XOR of plaintexts**

# Integrity?





# Problems with One-Time Pad

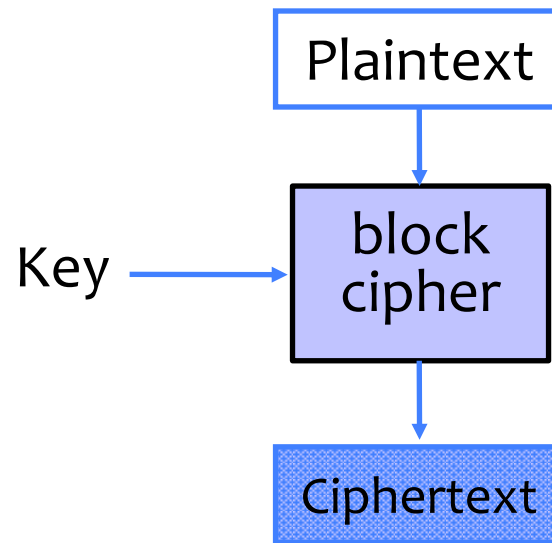
- (1) Key must be as long as the plaintext
  - Impractical in most realistic scenarios
  - Still used for diplomatic and intelligence traffic
- (2) Insecure if keys are reused
  - Attacker can obtain XOR of plaintexts
- **(3) Does not guarantee integrity**
  - One-time pad only guarantees confidentiality
  - Attacker cannot recover plaintext, but can easily change it to something else

# Reducing Key Size

- What to do when it is infeasible to pre-share huge random keys?
  - When one-time pad is unrealistic...
- Use special cryptographic primitives: block ciphers, stream ciphers
  - Single key can be re-used (with some restrictions)
  - Not as theoretically secure as one-time pad

# Block Ciphers

- Operates on a single chunk (“block”) of plaintext
  - For example, 64 bits for DES, 128 bits for AES
  - Each key defines a different permutation
  - Same key is reused for each block (can use short keys)



# Keyed Permutation

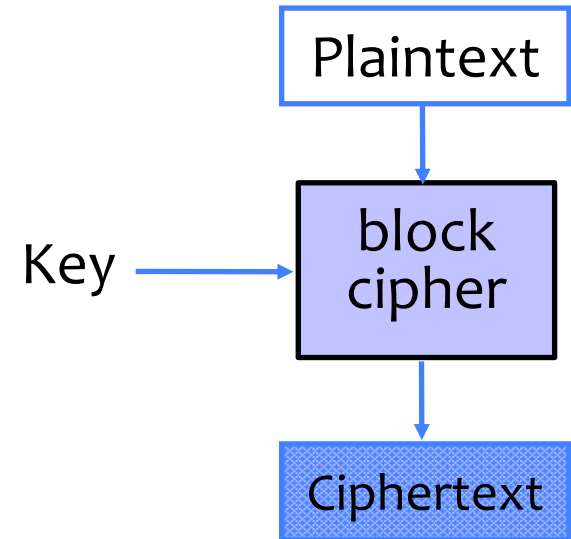
Key = 00   Key = 01

input	possible output	possible output	etc.
000	010	111	...
001	111	110	...
010	101	000	...
011	110	101	...
...	...		...
111	000	110	...

For N-bit input,  $2^N!$  possible permutations  
For K-bit key,  $2^K$  possible keys

# Keyed Permutation

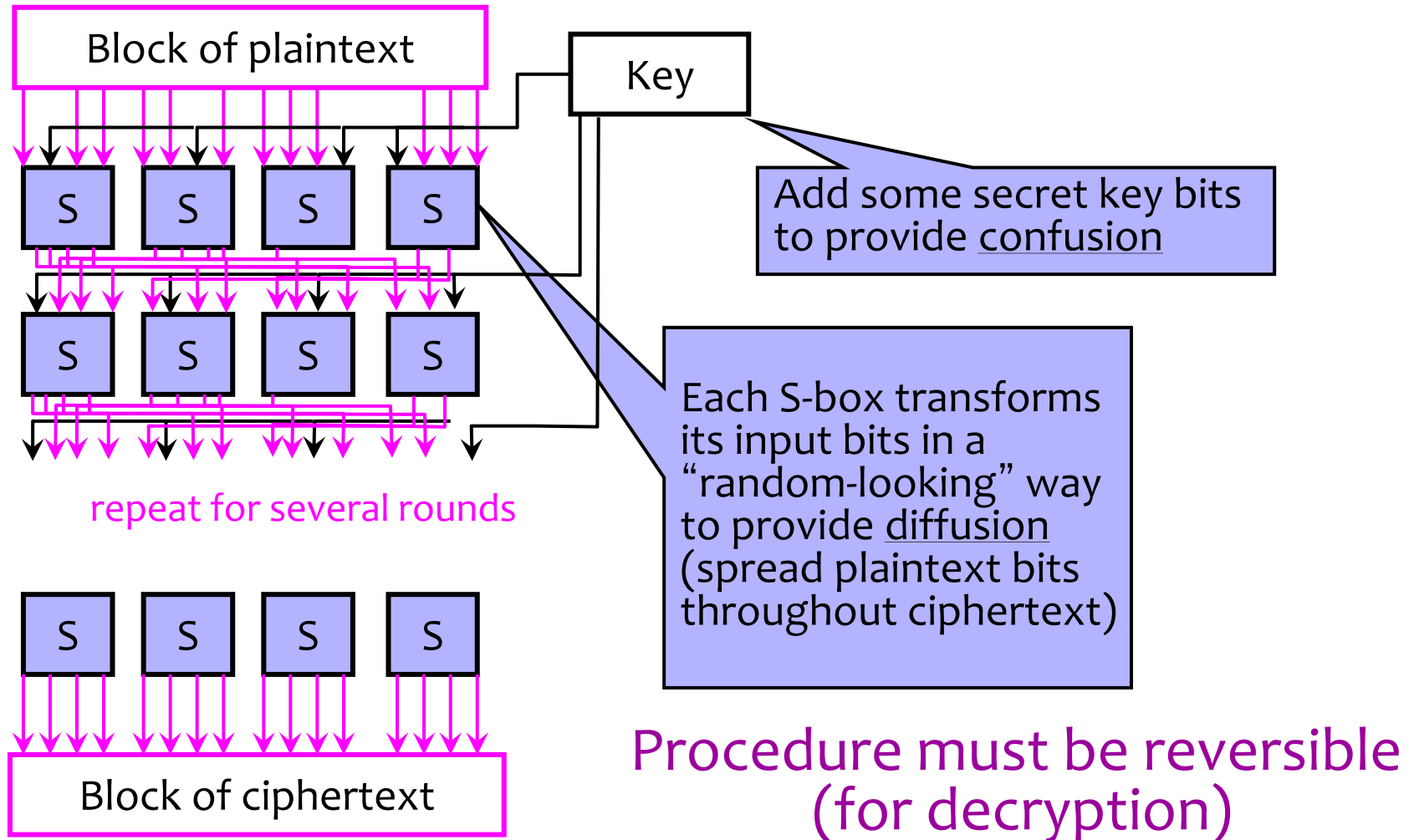
- Not just shuffling of input bits!
  - Suppose plaintext = “111”.
  - Then “111” is not the only possible ciphertext!
- Instead:
  - **Permutation of possible outputs**
  - Use secret key to pick a permutation



# Block Cipher Security

- Result should “look like” a random permutation on the inputs
  - Recall: not just shuffling bits.  $N$ -bit block cipher permutes over  $2^N$  inputs.
- Only computational guarantee of secrecy
  - Not impossible to break, just very expensive
    - If there is no efficient algorithm (unproven assumption!), then can only break by brute-force, try-every-possible-key search
  - Time and cost of breaking the cipher exceed the value and/or useful lifetime of protected information

# Block Cipher Operation (Simplified)



# Standard Block Ciphers

- **DES: Data Encryption Standard**

- Feistel structure: builds invertible function using non-invertible ones
- Invented by IBM, issued as federal standard in 1977
- 64-bit blocks, 56-bit key + 8 bits for parity



# DES and 56 bit keys

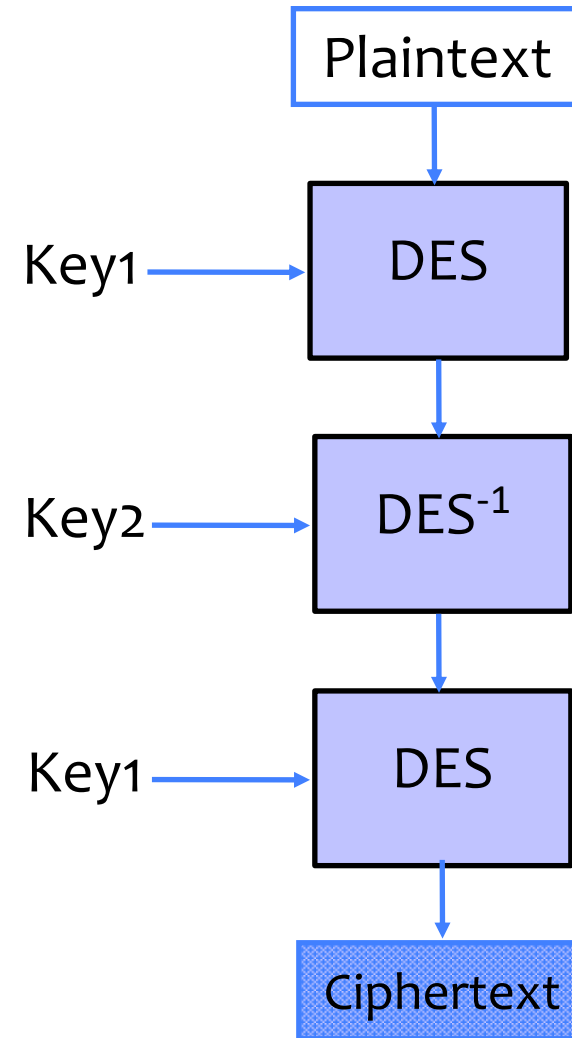
- 56 bit keys are quite short

Key Size (bits)	Number of Alternative Keys	Time required at 1 encryption/ $\mu$ s	Time required at $10^6$ encryptions/ $\mu$ s
32	$2^{32} = 4.3 \times 10^9$	$2^{31} \mu s = 35.8$ minutes	2.15 milliseconds
56	$2^{56} = 7.2 \times 10^{16}$	$2^{55} \mu s = 1142$ years	10.01 hours
128	$2^{128} = 3.4 \times 10^{38}$	$2^{127} \mu s = 5.4 \times 10^{24}$ years	$5.4 \times 10^{18}$ years
168	$2^{168} = 3.7 \times 10^{50}$	$2^{167} \mu s = 5.9 \times 10^{36}$ years	$5.9 \times 10^{30}$ years
26 characters (permutation)	$26! = 4 \times 10^{26}$	$2 \times 10^{26} \mu s = 6.4 \times 10^{12}$ years	$6.4 \times 10^6$ years

- 1999: EFF DES Crack + distributed machines
  - < 24 hours to find DES key
- DES ---> 3DES
  - 3DES: DES + inverse DES + DES (with 2 or 3 diff keys)

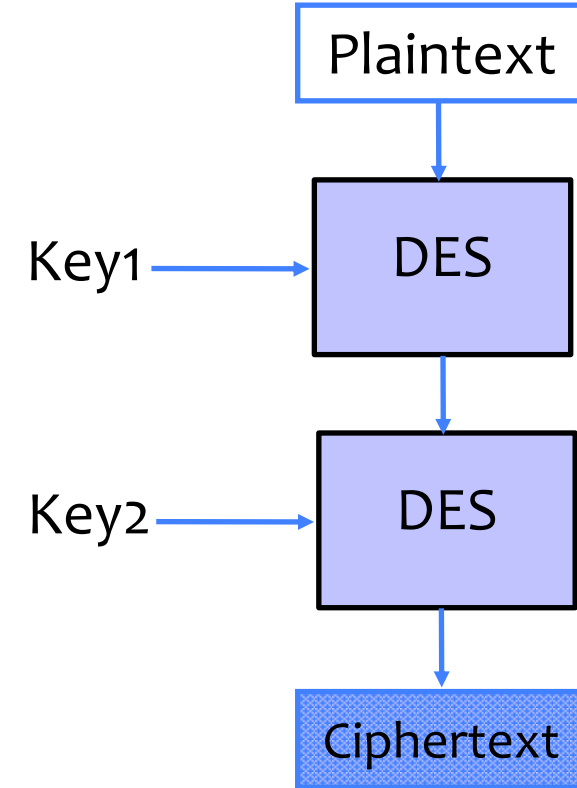
# 3DES

- Two-key 3DES increases security of DES by doubling the key length



# But wait... what about *2DES*?

- Suppose you are given plaintext-ciphertext pairs  $(P1, C1)$ ,  $(P2, C2)$ ,  $(P3, C3)$
- Suppose Key1 and Key2 are each 56-bits long
- Can you figure out Key1 and Key2 if you try all possible values for both ( $2^{112}$  possibilities) → Yes
- Can you figure out Key1 and Key2 more than that? → **Breakout**

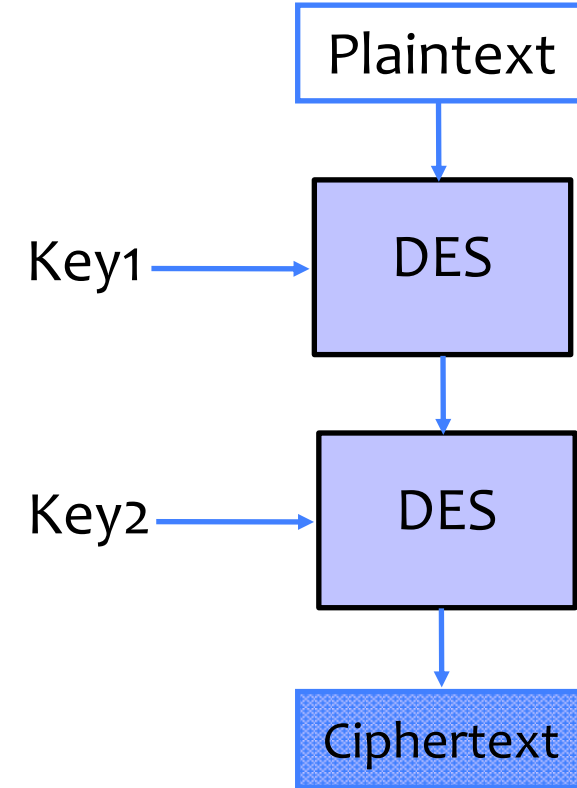


# But wait... what about *2DES*?

- Meet-in-the-middle attack

# Meet-in-the-Middle Attack

- Guess  $2^{56}$  values for Key1, and create a table from P1 to a middle value M1 for each key guess ( $M1^{G1}$ ,  $M1^{G2}$ ,  $M1^{G3}$ , ...)
- Guess  $2^{56}$  values for Key2, and create a table from C1 to a middle value M'1 for each key guess ( $M'1^{G1}$ ,  $M'1^{G2}$ ,  $M'1^{G3}$ , ...)
- Look for collision in the middle values → if only one collision, found Key1 and Key2; otherwise repeat for (P2,C2), ...

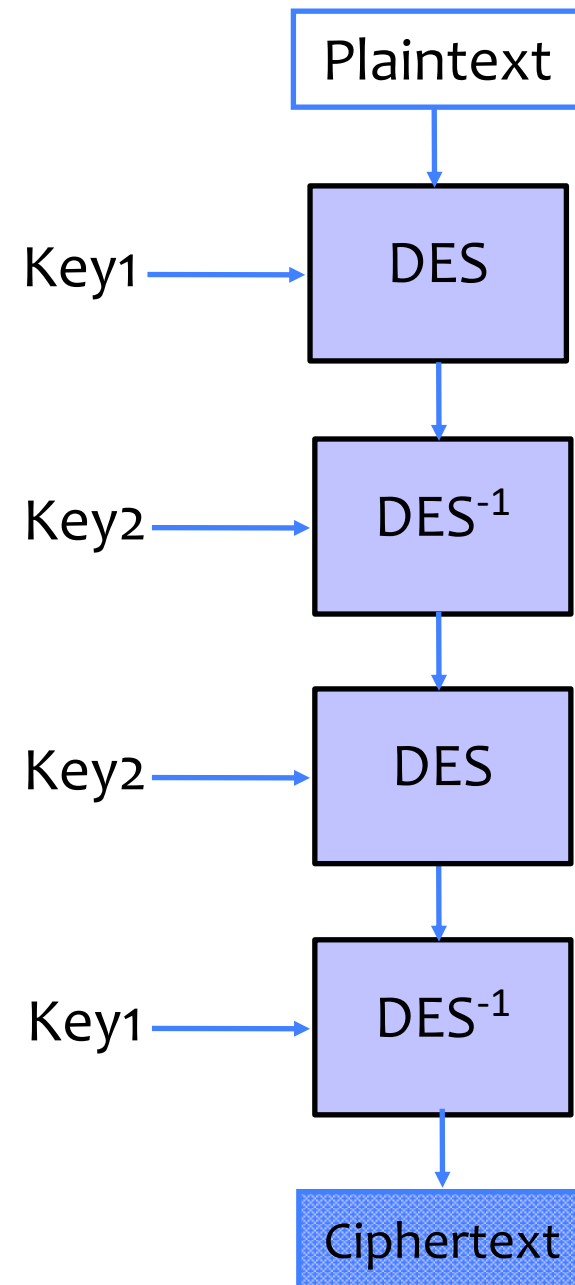


# Defining the strength of a scheme

- *Effective Key Strength*
  - Amount of 'work' the adversary needs to do
- **DES**: 56-bits
  - $2^{56}$  encryptions to try 'all keys'
- **2DES**: 57-bits
  - $2 \cdot (2^{56})$  encryptions =  $2^{57}$
- **3DES**: 112-bits (or sometimes 80-bits)
  - Meet-in-the-middle + more work =  $2^{112}$  (for 3 keys, e.g. K1, K2, K3)
  - Various attacks =  $2^{80}$  (for 2 keys, e.g. K1, K2, K1)

# 4DES

- Paul Kocher's \*JOKE\* proposal
- If two-key 3DES is good, would two-key 4DES be even better



# Standard Block Ciphers

- **DES: Data Encryption Standard**

- Feistel structure: builds invertible function using non-invertible ones
- Invented by IBM, issued as federal standard in 1977
- 64-bit blocks, 56-bit key + 8 bits for parity

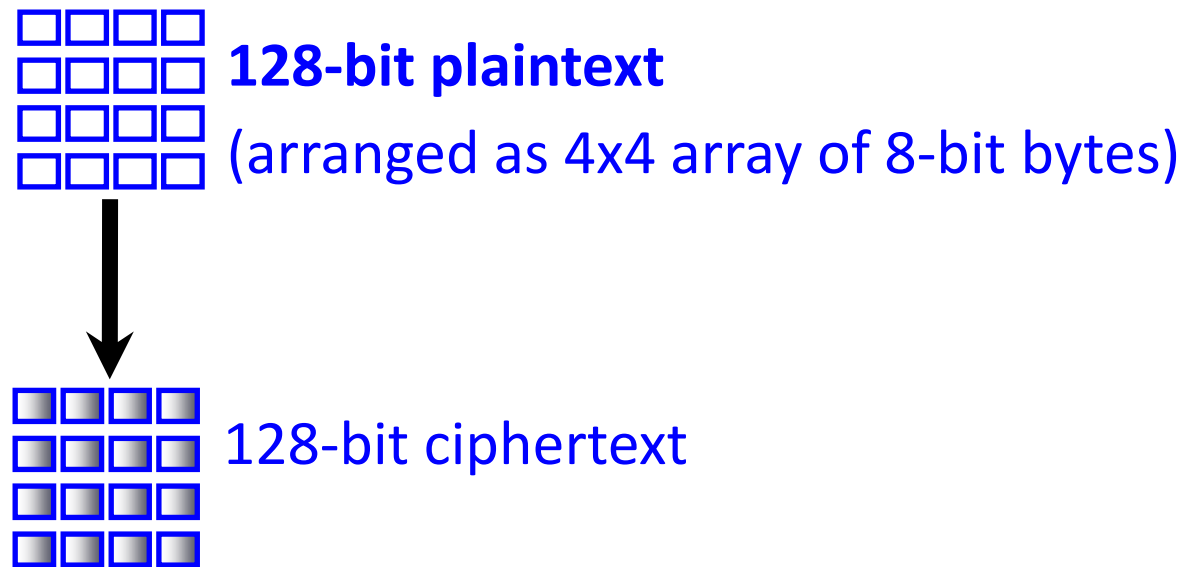
- **AES: Advanced Encryption Standard**

- Federal standard as of 2001
  - NIST: National Institute of Standards & Technology
- Based on the Rijndael algorithm
  - Selected via an open process
- 128-bit blocks, keys can be 128, 192 or 256 bits



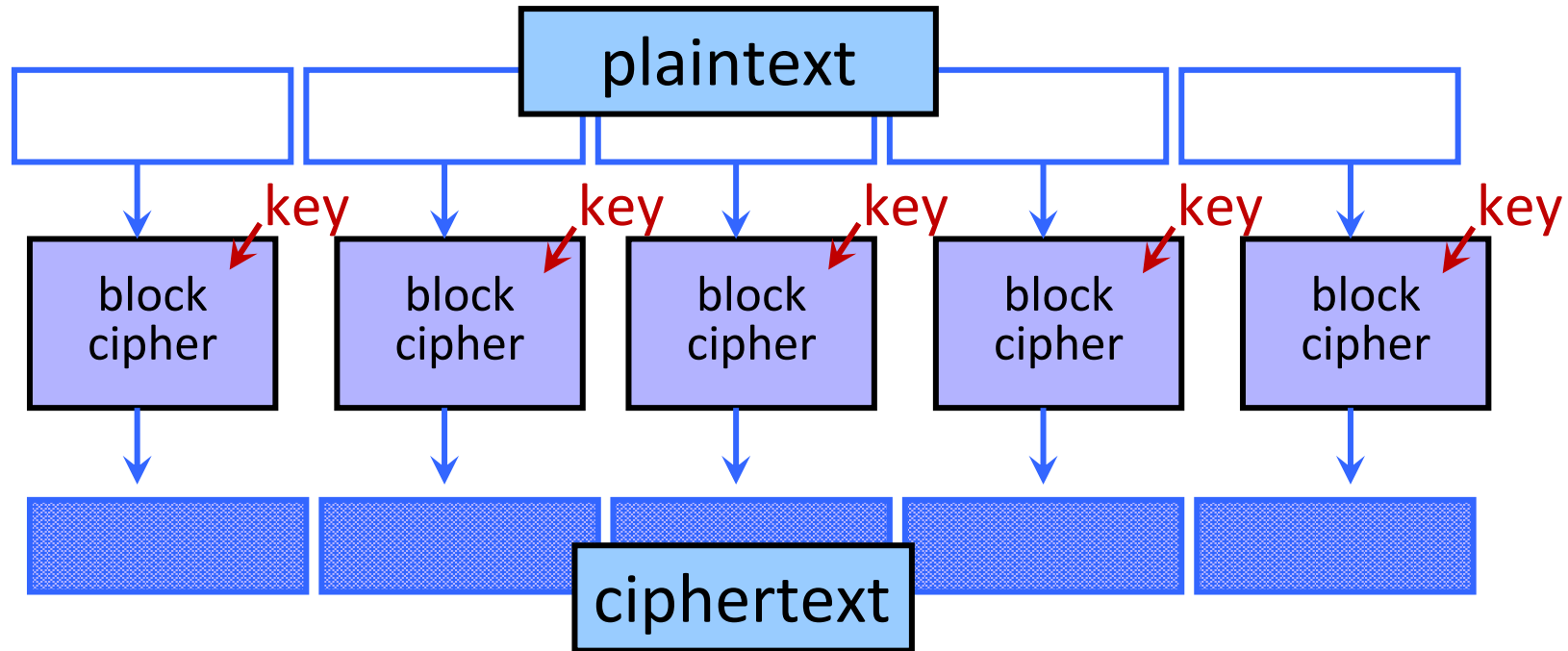
# Encrypting a Large Message

- So, we've got a good block cipher, but our plaintext is larger than 128-bit block size



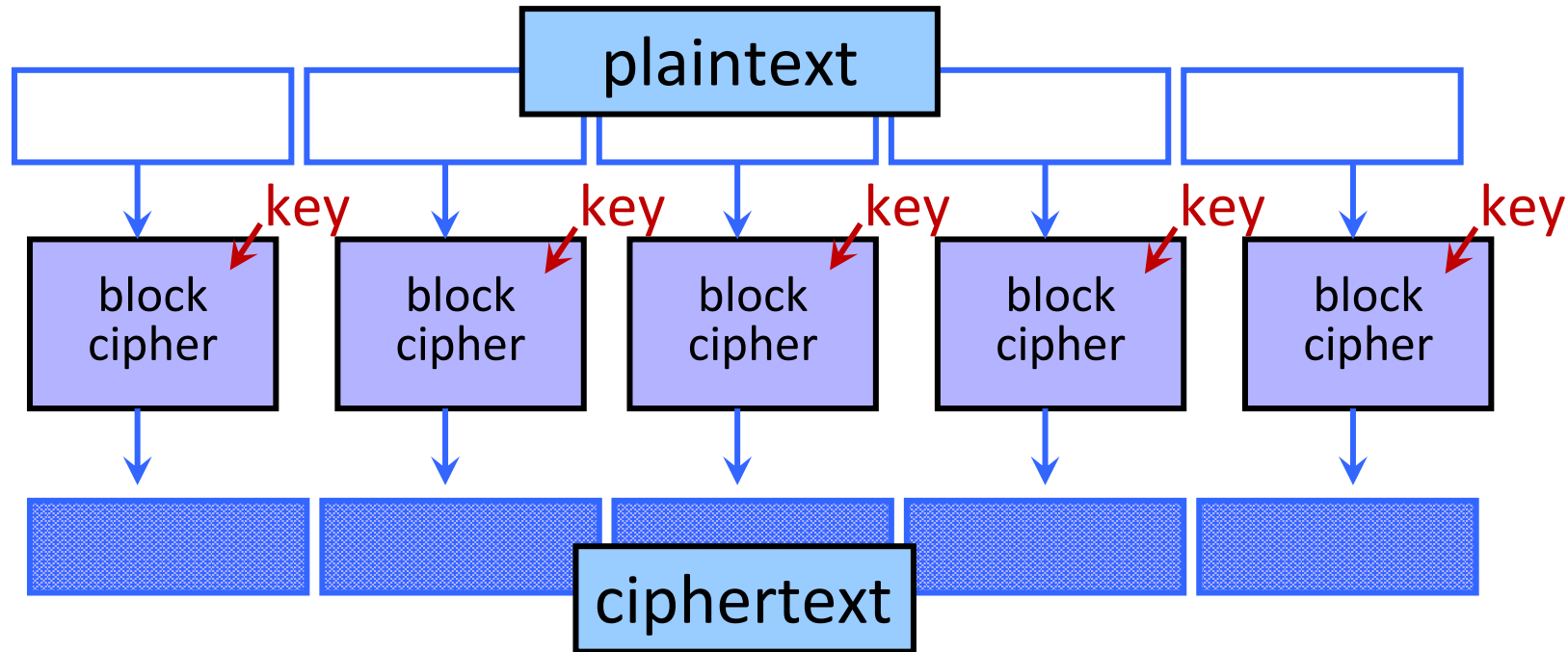
- What should we do?

# Electronic Code Book (ECB) Mode



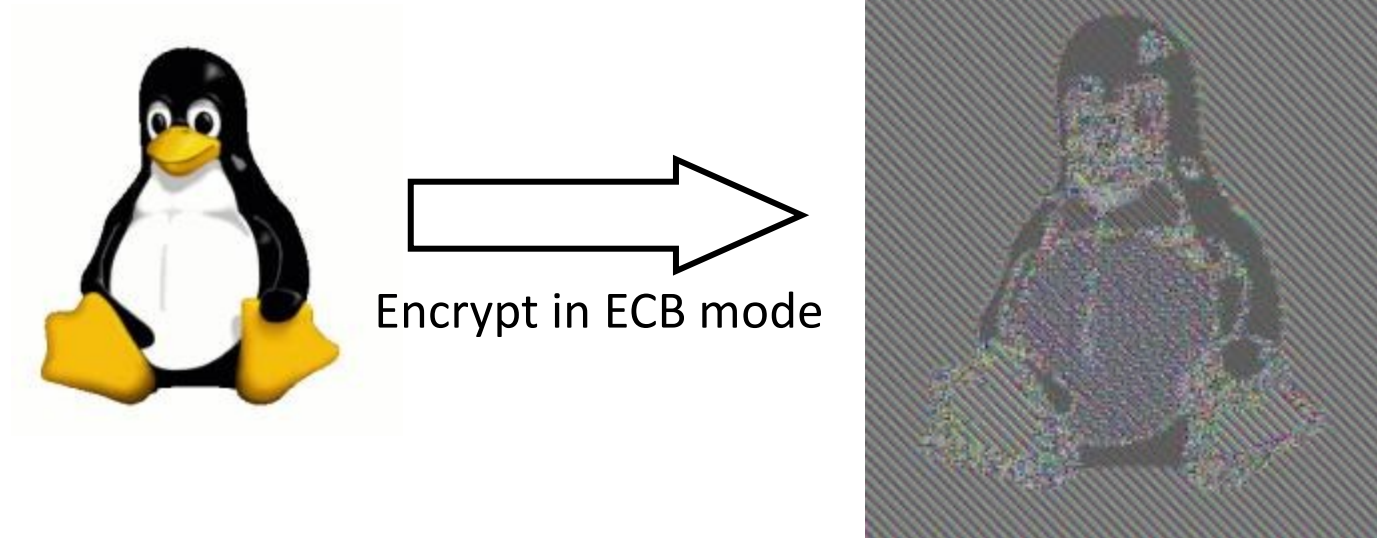
Canvas time!

# Electronic Code Book (ECB) Mode



- Identical blocks of plaintext produce identical blocks of ciphertext
- No integrity checks: can mix and match blocks

# Information Leakage in ECB Mode



[Wikipedia]

# Oops

## **Move Fast and Roll Your Own Crypto** **A Quick Look at the Confidentiality of Zoom Meetings**

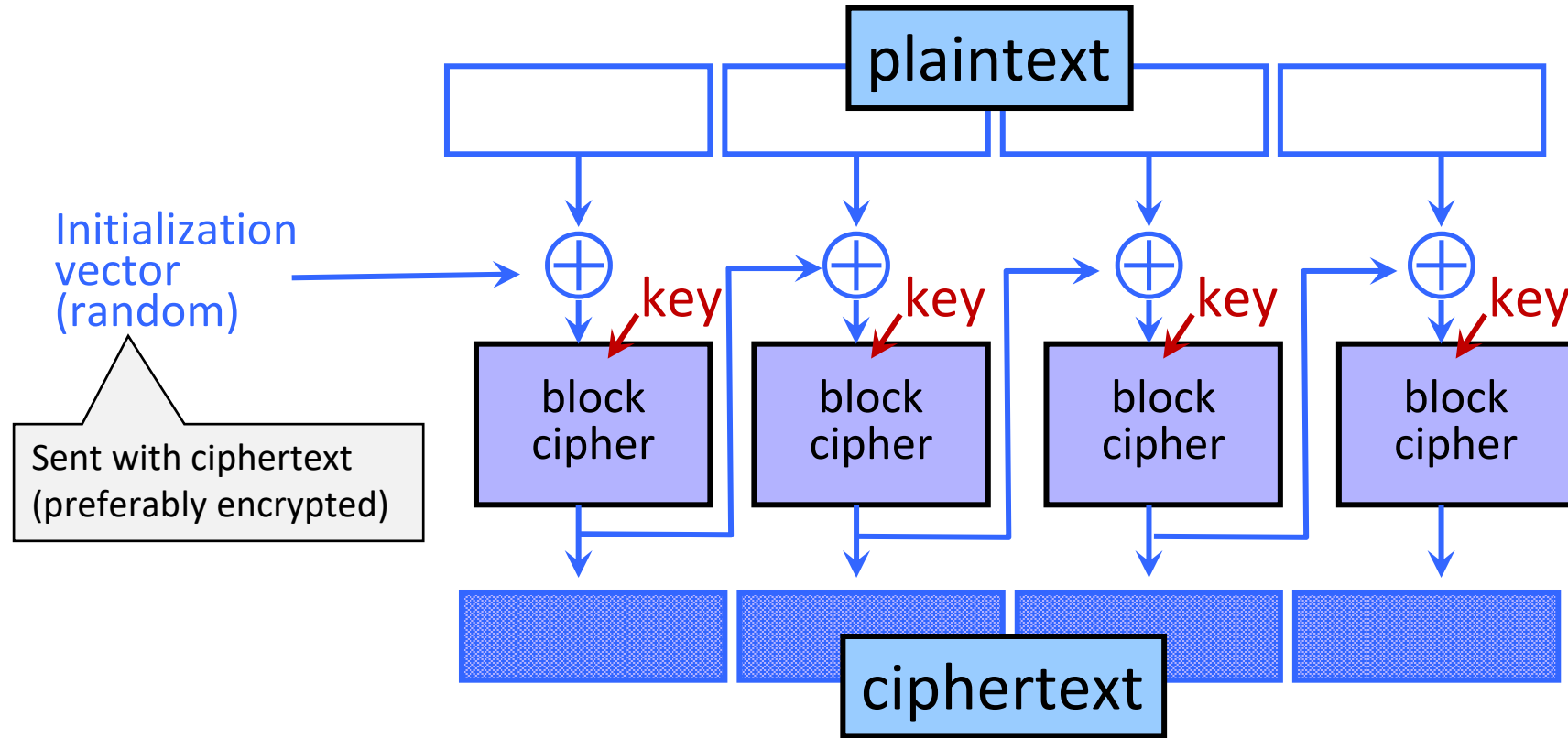
By Bill Marczak and John Scott-Railton

April 3, 2020

- Zoom [documentation](#) claims that the app uses “AES-256” encryption for meetings where possible. However, we find that in each Zoom meeting, a single AES-128 key is used in ECB mode by all participants to encrypt and decrypt audio and video. The use of ECB mode is not recommended because patterns present in the plaintext are preserved during encryption.

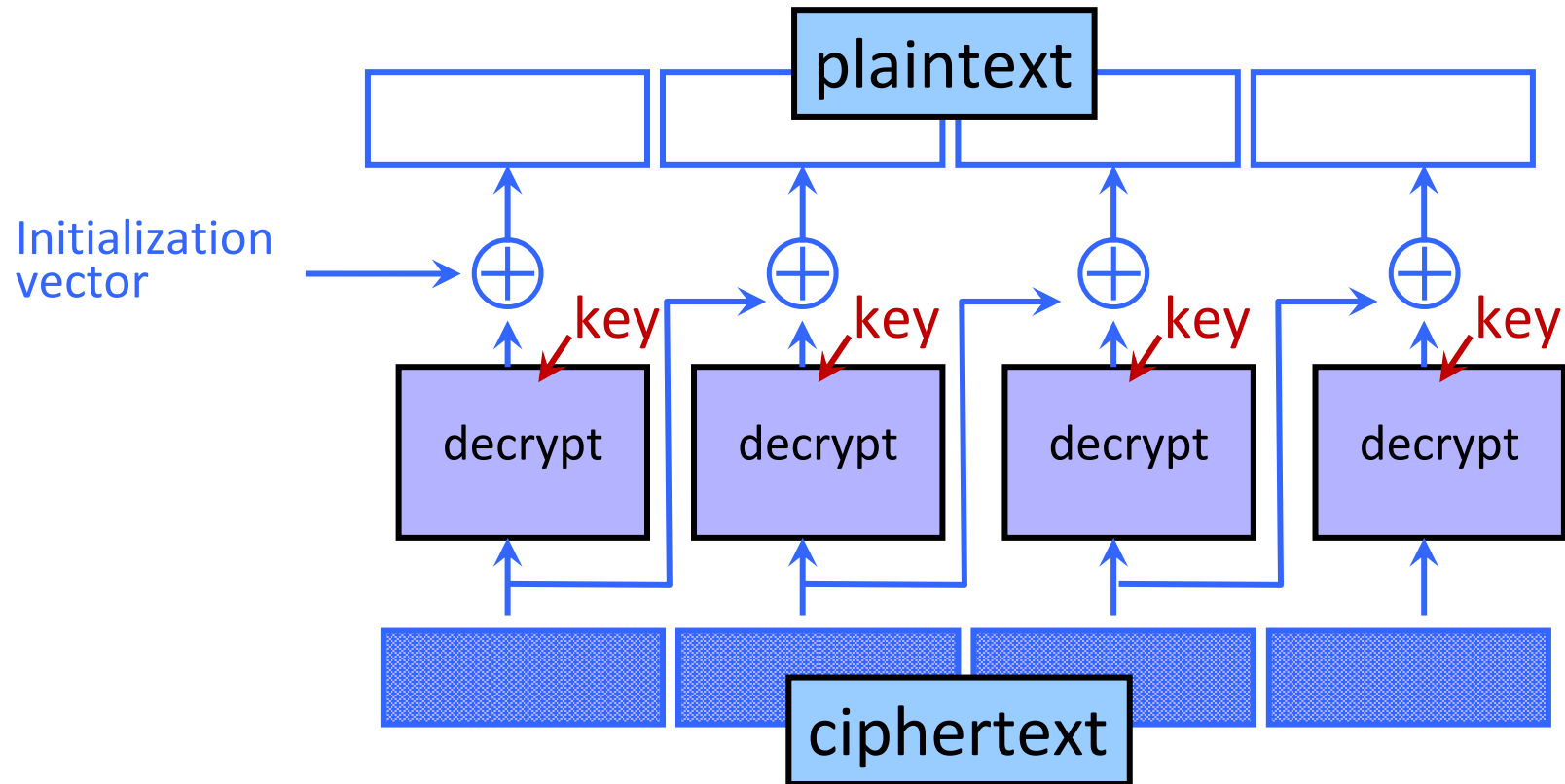
<https://citizenlab.ca/2020/04/move-fast-roll-your-own-crypto-a-quick-look-at-the-confidentiality-of-zoom-meetings/>

# Cipher Block Chaining (CBC) Mode: Encryption

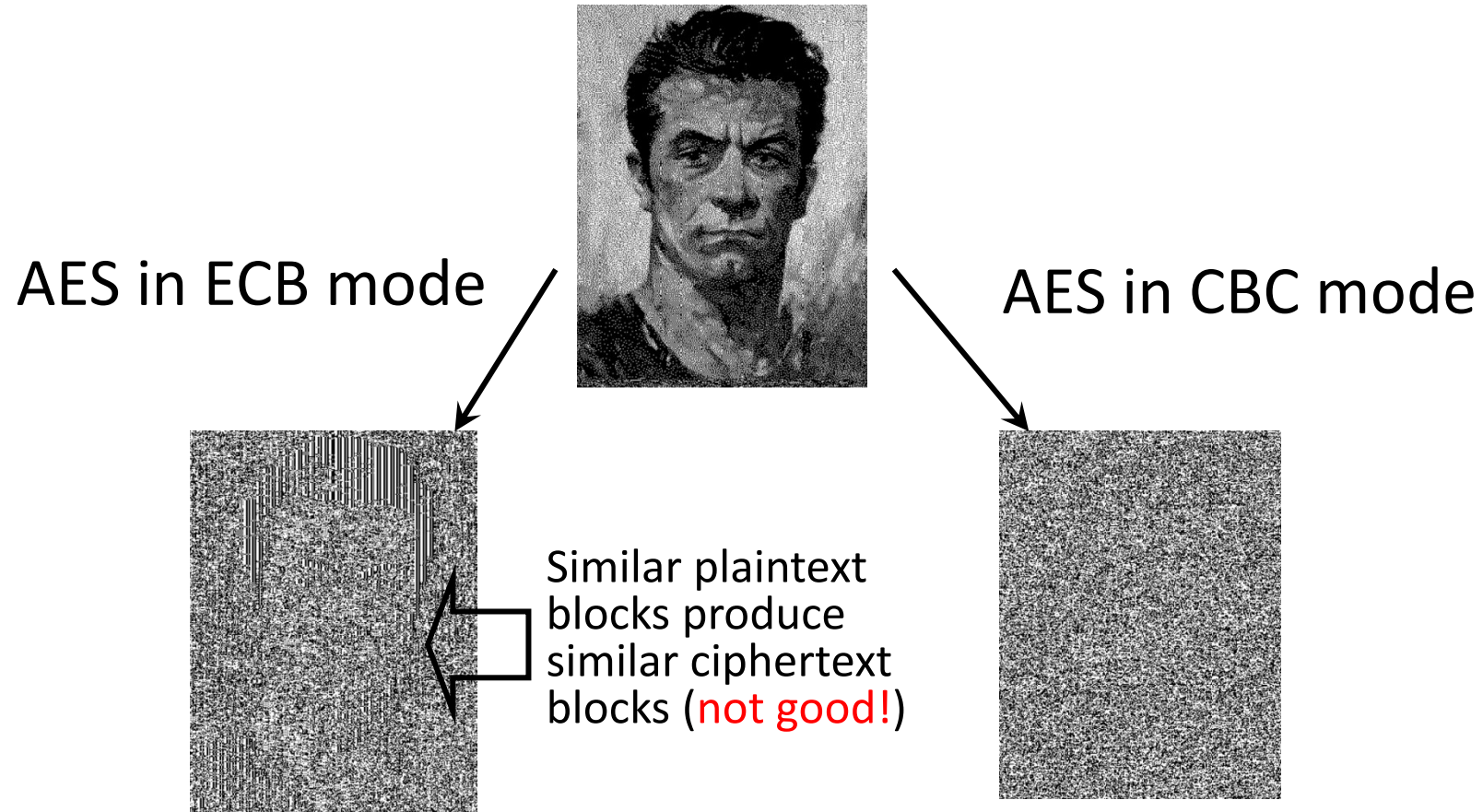


- Identical blocks of plaintext encrypted differently
- Last cipherblock depends on entire plaintext
  - Still does not guarantee integrity

# CBC Mode: Decryption



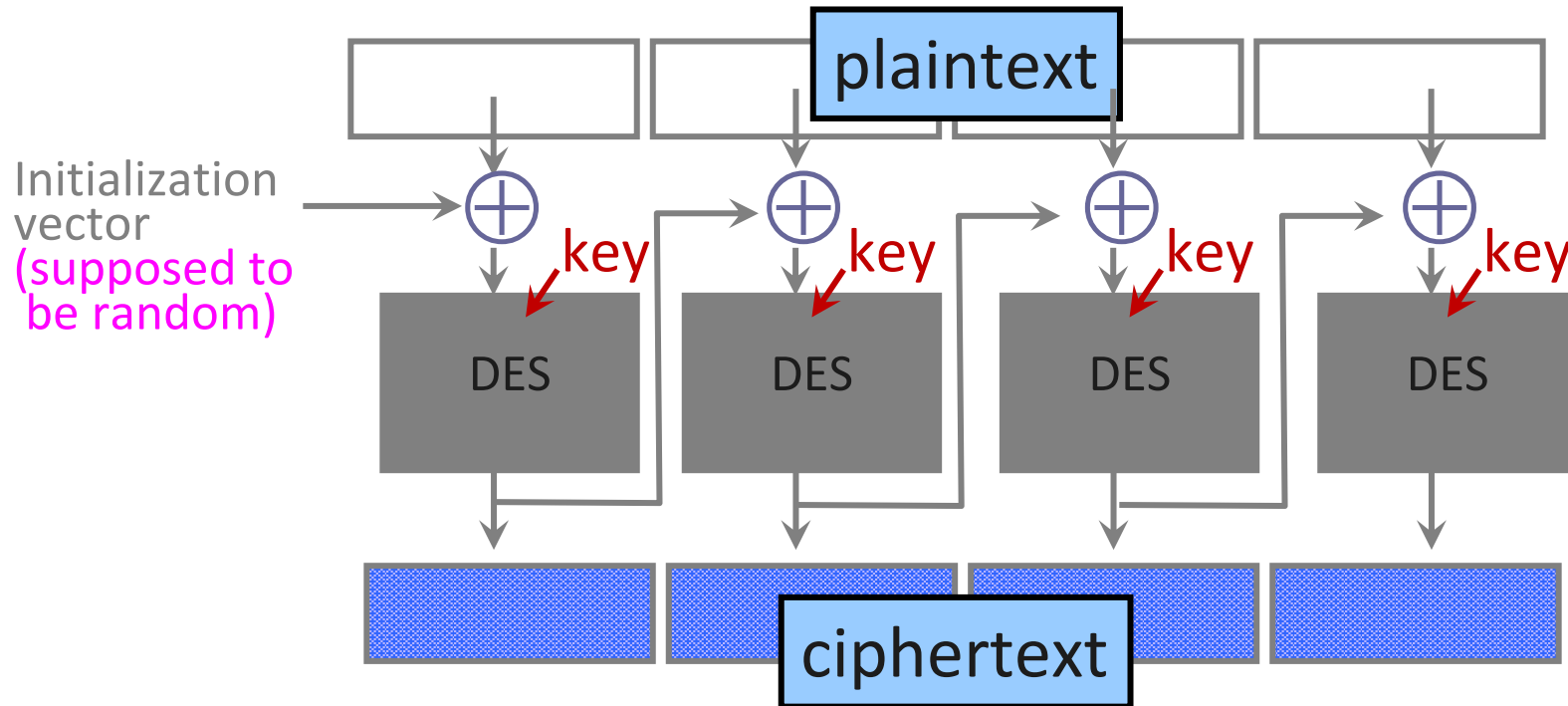
# ECB vs. CBC



[Picture due to Bart Preneel]



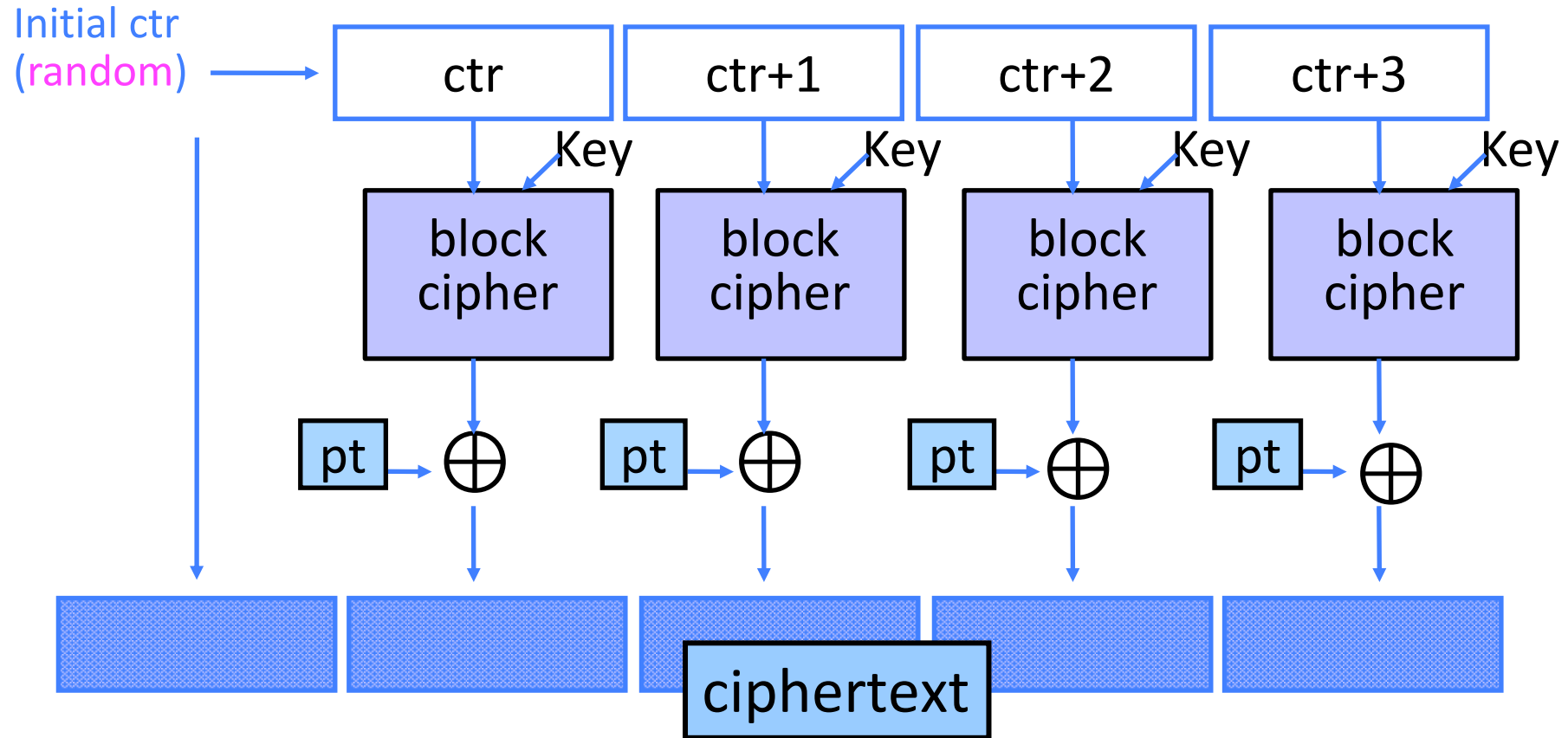
# Initialization Vector Dangers



Found in the source code for Diebold voting machines:

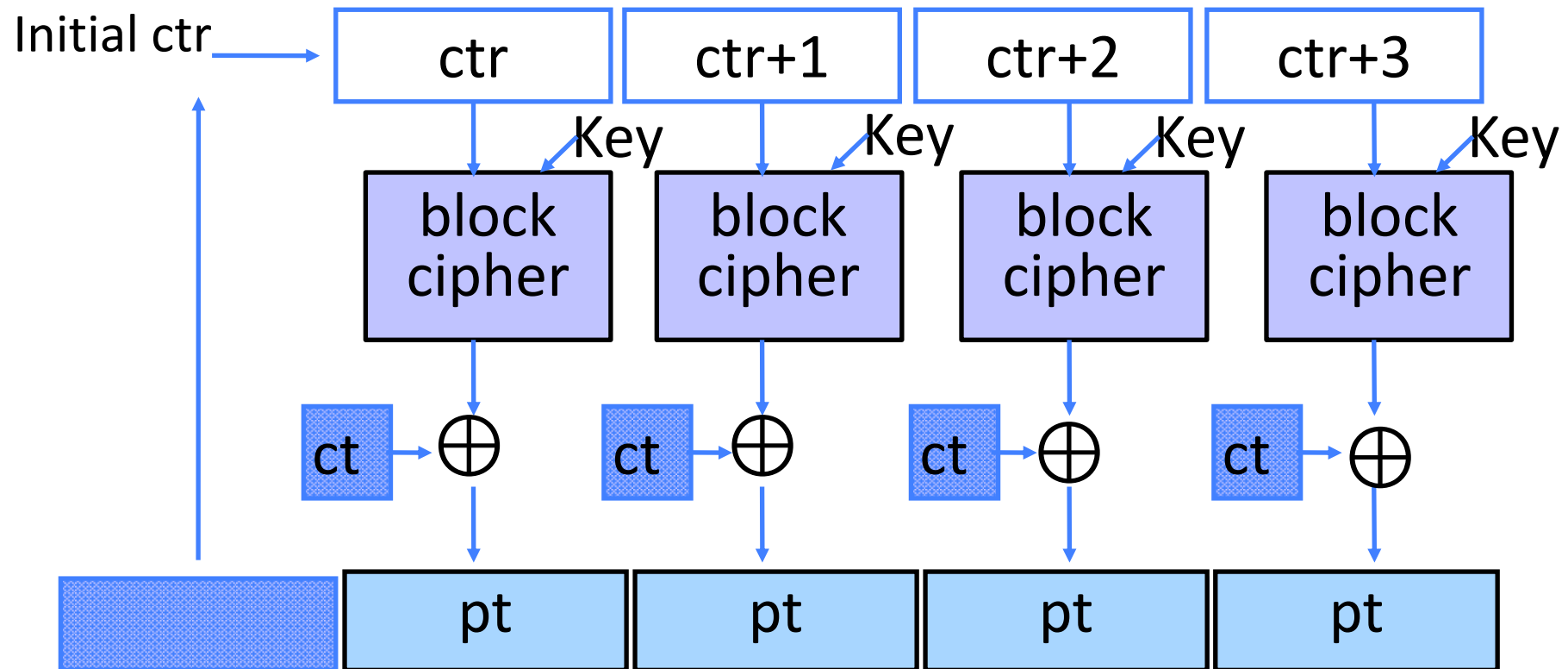
```
DesCBCEncrypt((des_c_block*)tmp, (des_c_block*)record.m_Data,  
totalSize, DESKEY, NULL, DES_ENCRYPT)
```

# Counter Mode (CTR): Encryption



- Identical blocks of plaintext encrypted differently
- Still does not guarantee integrity; Fragile if ctr repeats

# Counter Mode (CTR): Decryption



# Ok, so what mode do I use?

- Don't choose a mode, use established libraries 😊
- Good modes:
  - GCM - Galois/Counter Mode
  - CTR (sometimes)
  - Even ECB is fine in 'the right circumstance'

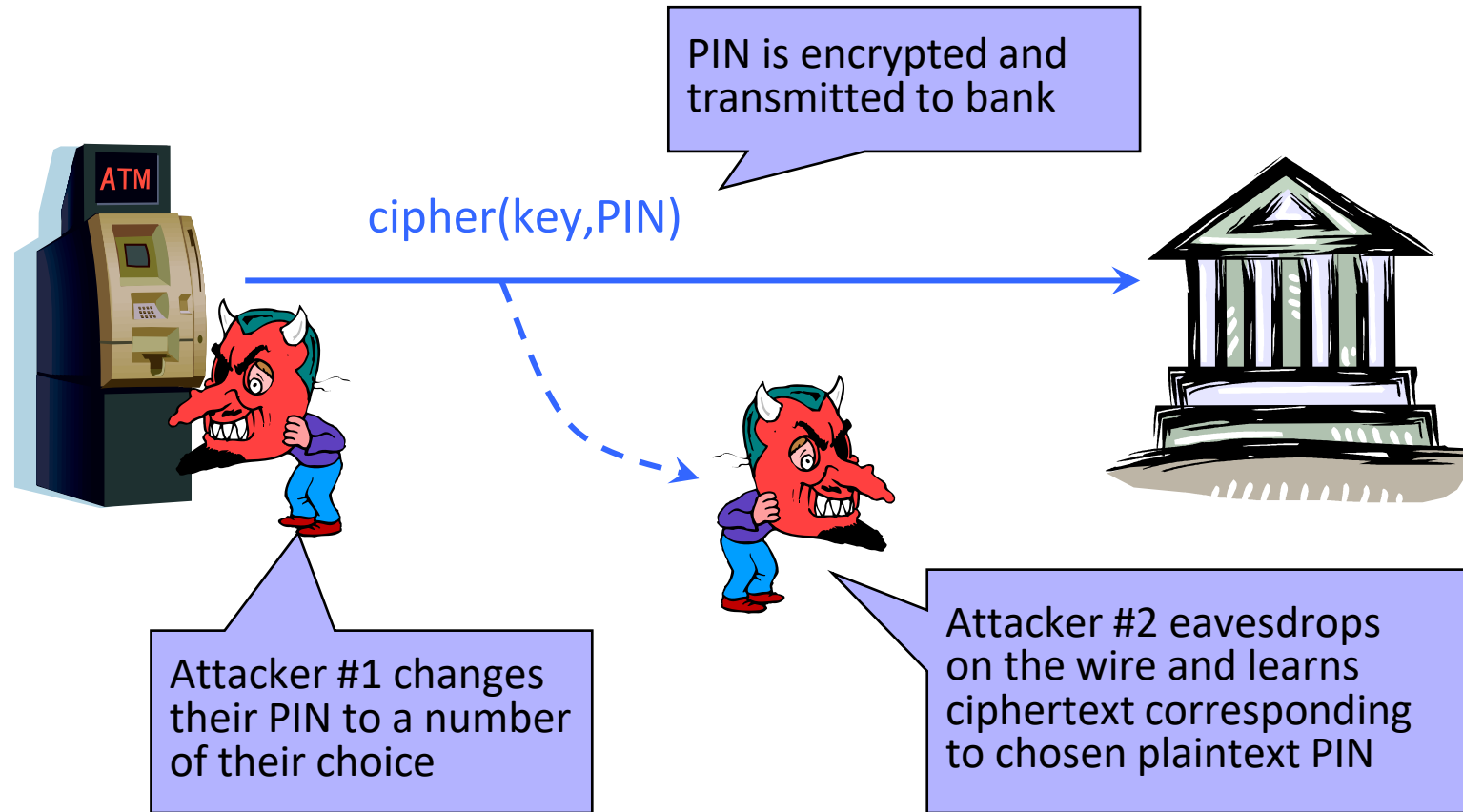
# When is an Encryption Scheme “Secure”?

- Hard to recover the key?
  - What if attacker can learn plaintext without learning the key?
- Hard to recover plaintext from ciphertext?
  - What if attacker learns some bits or some function of bits?

# How Can a Cipher Be Attacked?

- Attackers knows ciphertext and encryption algorithm
  - What else does the attacker know? Depends on the application in which the cipher is used!
- Ciphertext-only attack
- KPA: Known-plaintext attack (stronger)
  - Knows some plaintext-ciphertext pairs
- CPA: Chosen-plaintext attack (even stronger)
  - Can obtain ciphertext for any plaintext of choice
- CCA: Chosen-ciphertext attack (very strong)
  - Can decrypt any ciphertext except the target

# Chosen Plaintext Attack



... repeat for any PIN value

# Very Informal Intuition

Minimum security requirement for a modern encryption scheme



- Security against chosen-plaintext attack (CPA)
  - Ciphertext leaks no information about the plaintext
  - Even if the attacker correctly guesses the plaintext, they cannot verify their guess
  - Every ciphertext is unique, encrypting same message twice produces completely different ciphertexts
    - Implication: encryption must be randomized or stateful
- Security against chosen-ciphertext attack (CCA)
  - Integrity protection – it is not possible to change the plaintext by modifying the ciphertext