

CSE 484: Computer Security and Privacy

Cryptography

[Symmetric Encryption]

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...

How Cryptosystems Work Today

- **Layered approach:** **Cryptographic protocols** (like “CBC mode encryption”) built on top of **cryptographic primitives** (like “block ciphers”)
- **Flavors of cryptography:** **Symmetric** (private key) and **asymmetric** (public key)
- Public algorithms (**Kerckhoff’s Principle**)
- Security proofs based on assumptions (*not this course*)

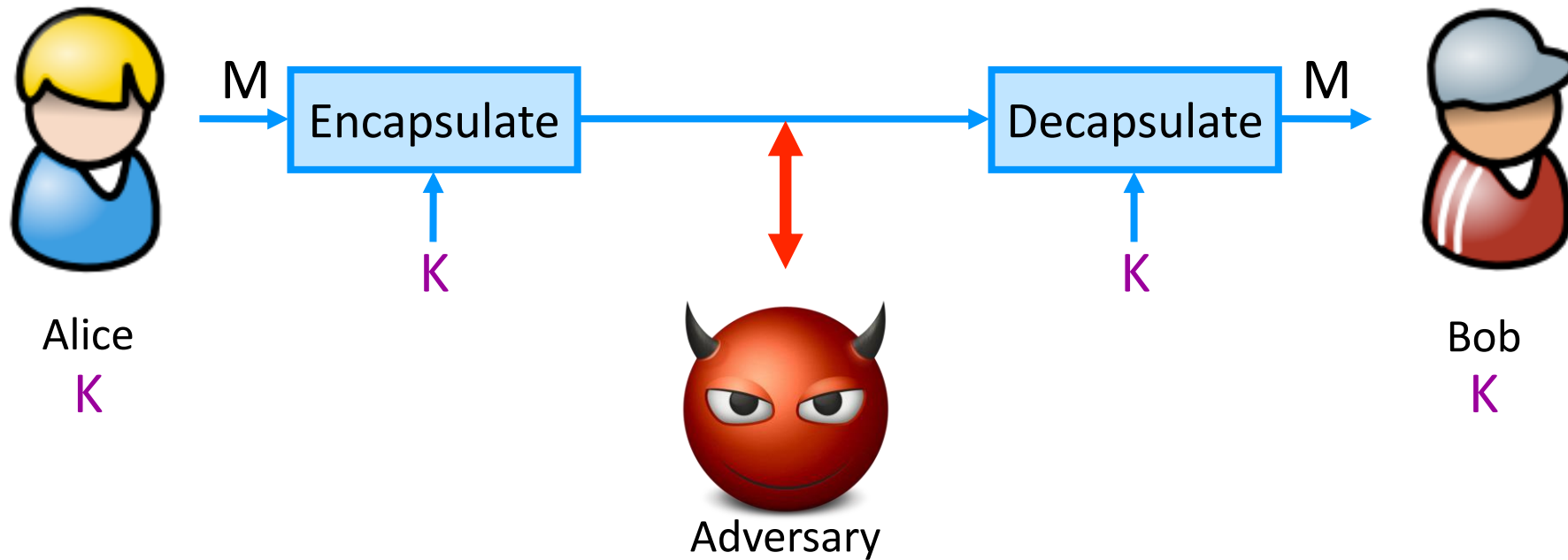
- **Be careful about inventing your own! (If you just want to use some crypto in your system, use vetted libraries!)**

Flavors of Cryptography

- Symmetric cryptography
 - Both communicating parties have access to a **shared random string K** , called the **key**.
- Asymmetric cryptography
 - Each party creates a public key **pk** and a secret key **sk**.
 - *Hard concept to understand, and revolutionary! Inventors won Turing Award*
😊

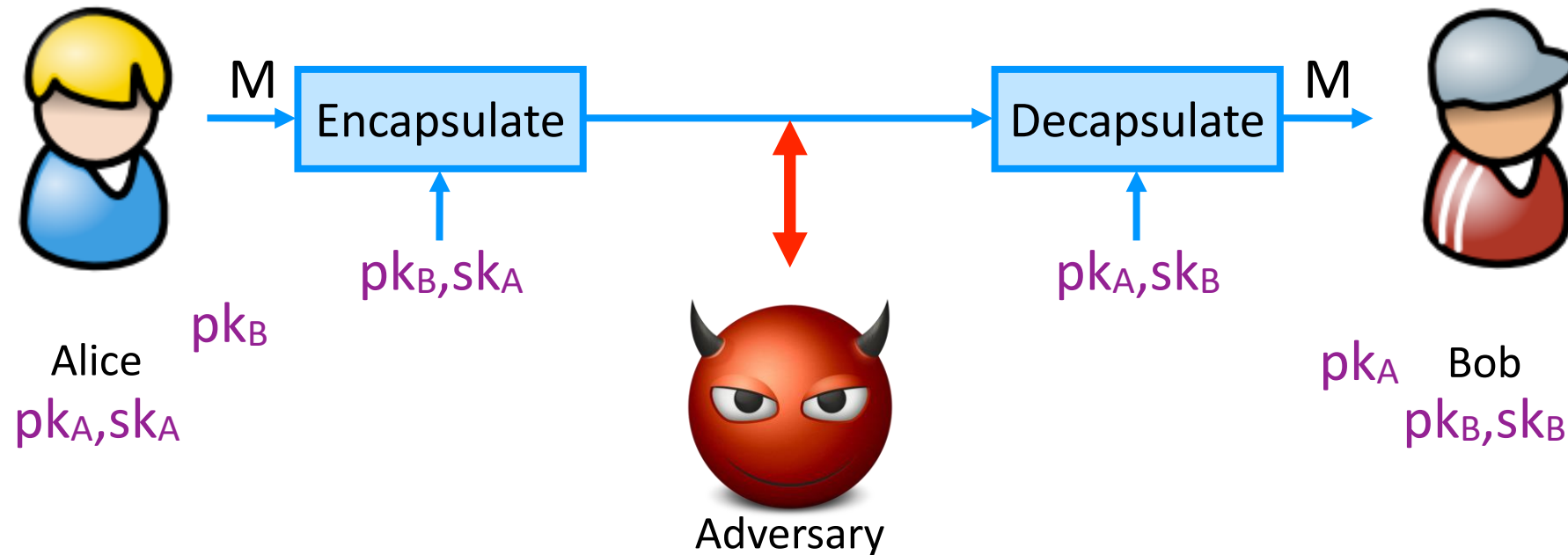
Symmetric Setting

Both communicating parties have access to a **shared random string K** , called the **key**.



Asymmetric Setting

Each party creates a public key pk and a secret key sk .



Flavors of Cryptography

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Flavors of Cryptography

- Symmetric cryptography
 - Both communicating parties have access to a **shared random string K** , called the **key**.
 - **Challenge: How do you privately share a key?**
- Asymmetric cryptography
 - Each party creates a public key **pk** and a secret key **sk** .
 - **Challenge: How do you validate a public key?**

Ingredient: Randomness

- Many applications (especially security ones) require randomness
- Explicit uses:
 - Generate secret cryptographic keys
 - Generate random initialization vectors for encryption
- Other “non-obvious” uses:
 - Generate passwords for new users
 - Shuffle the order of votes (in an electronic voting machine)
 - Shuffle cards (for an online gambling site)

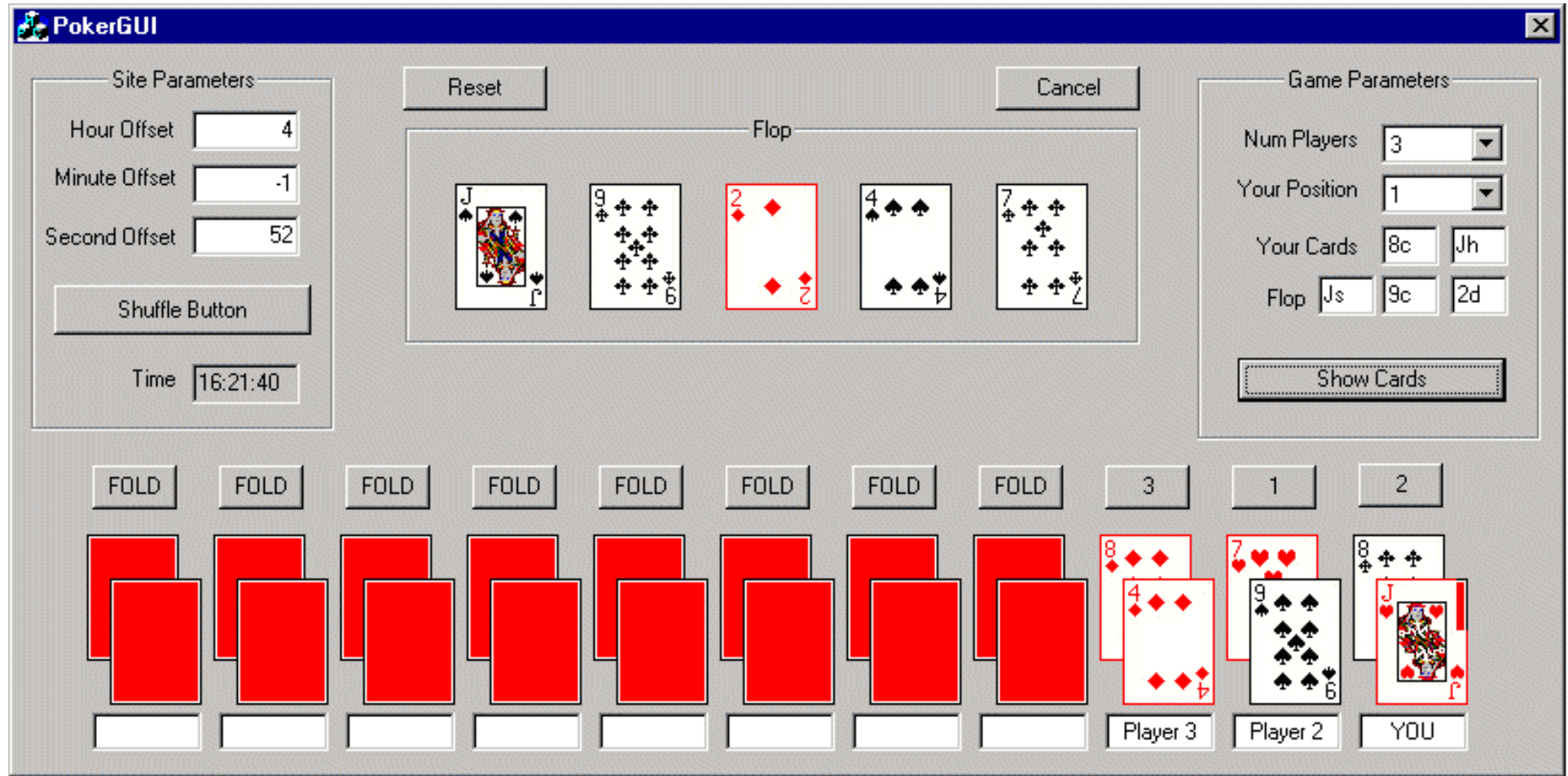
C's rand() Function

- C has a built-in random function: `rand()`

```
unsigned long int next = 1;
/* rand:  return pseudo-random integer on 0..32767 */
int rand(void) {
    next = next * 1103515245 + 12345;
    return (unsigned int)(next/65536) % 32768;
}
/* srand:  set seed for rand() */
void srand(unsigned int seed) {
    next = seed;
}
```

- Problem: don't use `rand()` for security-critical applications!
 - Given a few sample outputs, you can predict subsequent ones





More details: "How We Learned to Cheat at Online Poker: A Study in Software Security"

http://www.cigital.com/papers/download/developer_gambling.php

PS3 and Randomness

Hackers obtain PS3 private cryptography key due to epic programming fail? (update)

<http://www.engadget.com/2010/12/29/hackers-obtain-ps3-private-cryptography-key-due-to-epic-programm/>

- 2010/2011: Hackers **found/released private root key** for Sony's PS3
- Key used to sign software – **now can load any software on PS3** and it will execute as “trusted”
- Due to bad random number: **same “random” value used to sign all system updates**

Another real world example

```
byte buffer[256];
int index = 0;

setup(){
    for (i=0; i < 256; i++){
        buffer[i] = i;
    }
    shuffle_array(buffer);
}

random(){
    byte ret = buffer[index];
    if(index == 255){
        index = 0;
    }
    else{
        index++;
    }
}
```

Obtaining Pseudorandom Numbers

- For security applications, want “cryptographically secure pseudorandom numbers”
- Libraries include cryptographically secure pseudorandom number generators (CSPRNG)

Obtaining Pseudorandom Numbers

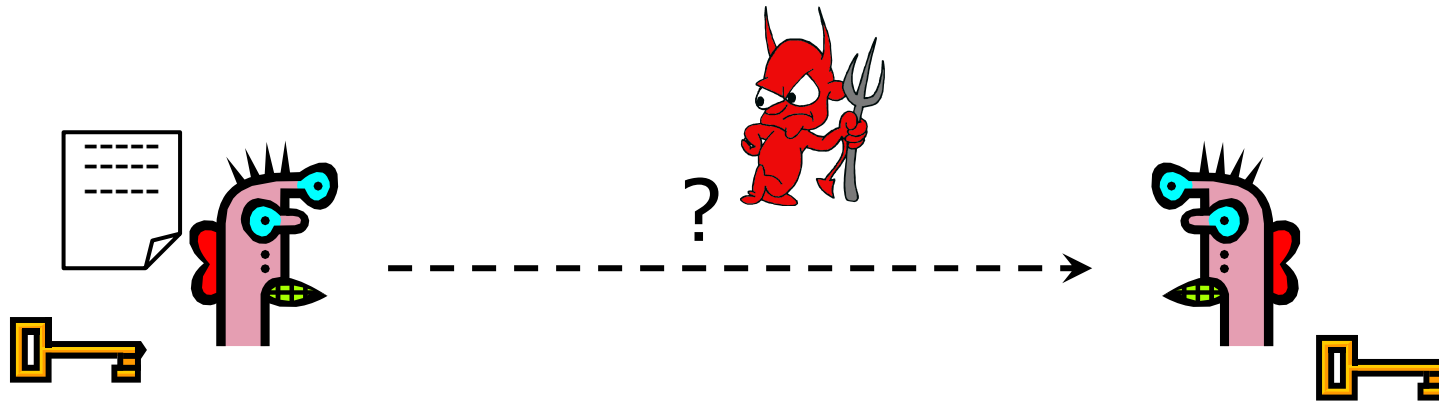
- Linux:
 - /dev/random
 - /dev/urandom - nonblocking, possibly less entropy
 - getrandom() – syscall!
- Internally:
 - Entropy pool gathered from multiple sources
 - e.g., mouse/keyboard/network timings
- Challenges with embedded systems, saved VMs

Obtaining *Random* Numbers

- Better idea:
 - AMD/Intel's [on-chip random number generator](#)
 - RDRAND
- Hopefully no hardware bugs!

Now: Symmetric Encryption

Confidentiality: Basic Problem



Given (Symmetric Crypto): both parties know the same **secret**.

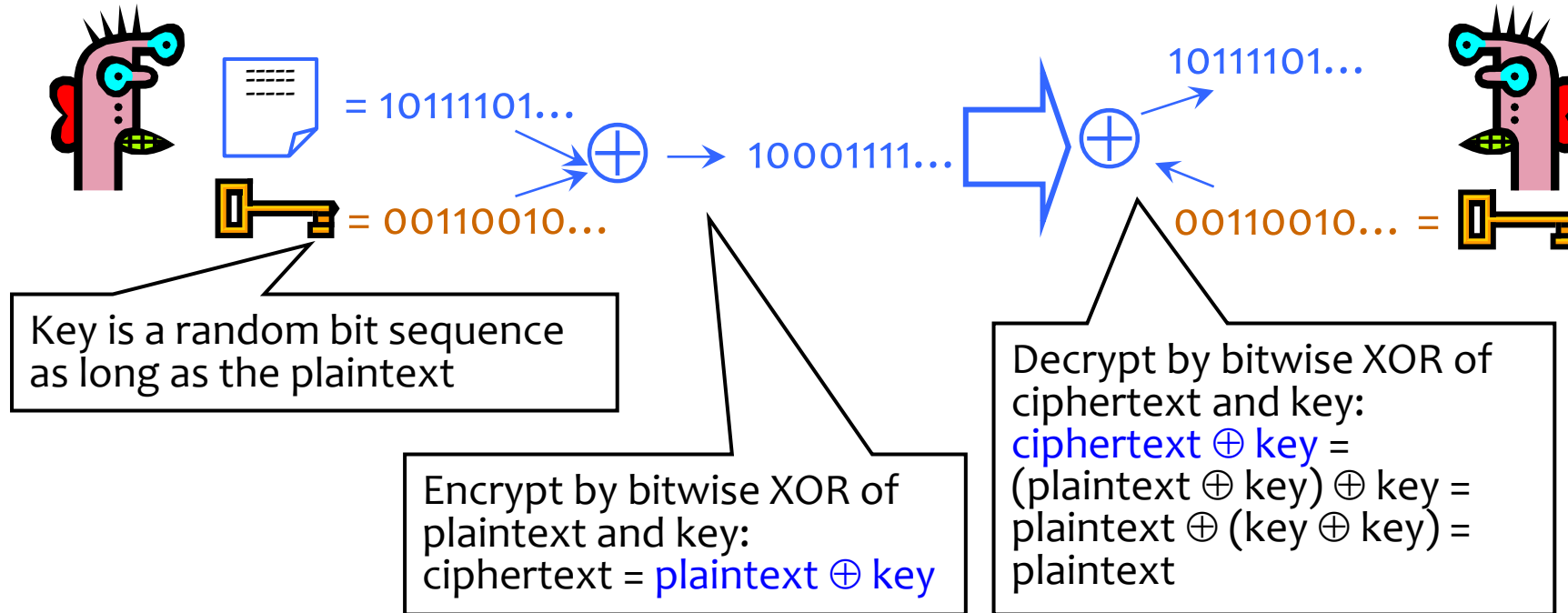
Goal: send a message confidentially.

Ignore for now: How is this achieved in practice??

One weird trick to hide your bits

- XOR!
 - Just XOR with a random bit!
- Why?
 - Uniform output
 - Independent of 'message' bit

One-Time Pad



Cipher achieves **perfect secrecy** if and only if there are **as many possible keys as possible plaintexts**, and **every key is equally likely** (Claude Shannon, 1949)

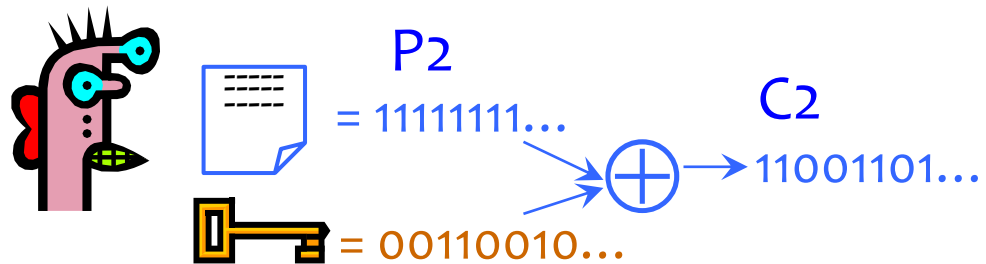
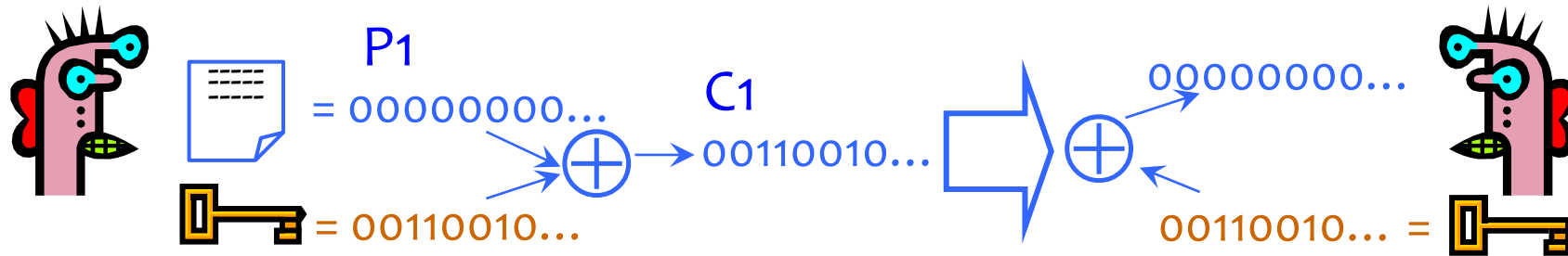
Advantages of One-Time Pad

- Easy to compute
 - Encryption and decryption are the same operation
 - Bitwise XOR is very cheap to compute
- As secure as theoretically possible
 - Given a ciphertext, all plaintexts are equally likely, regardless of attacker's computational resources
 - ...as long as the key sequence is truly random
 - True randomness is expensive to obtain in large quantities
 - ...as long as each key is same length as plaintext
 - But how does sender communicate the key to receiver?

Problems with One-Time Pad

- (1) Key must be as long as the plaintext
 - Impractical in most realistic scenarios
 - Still used for diplomatic and intelligence traffic
- (2) Insecure if keys are reused

Dangers of Reuse



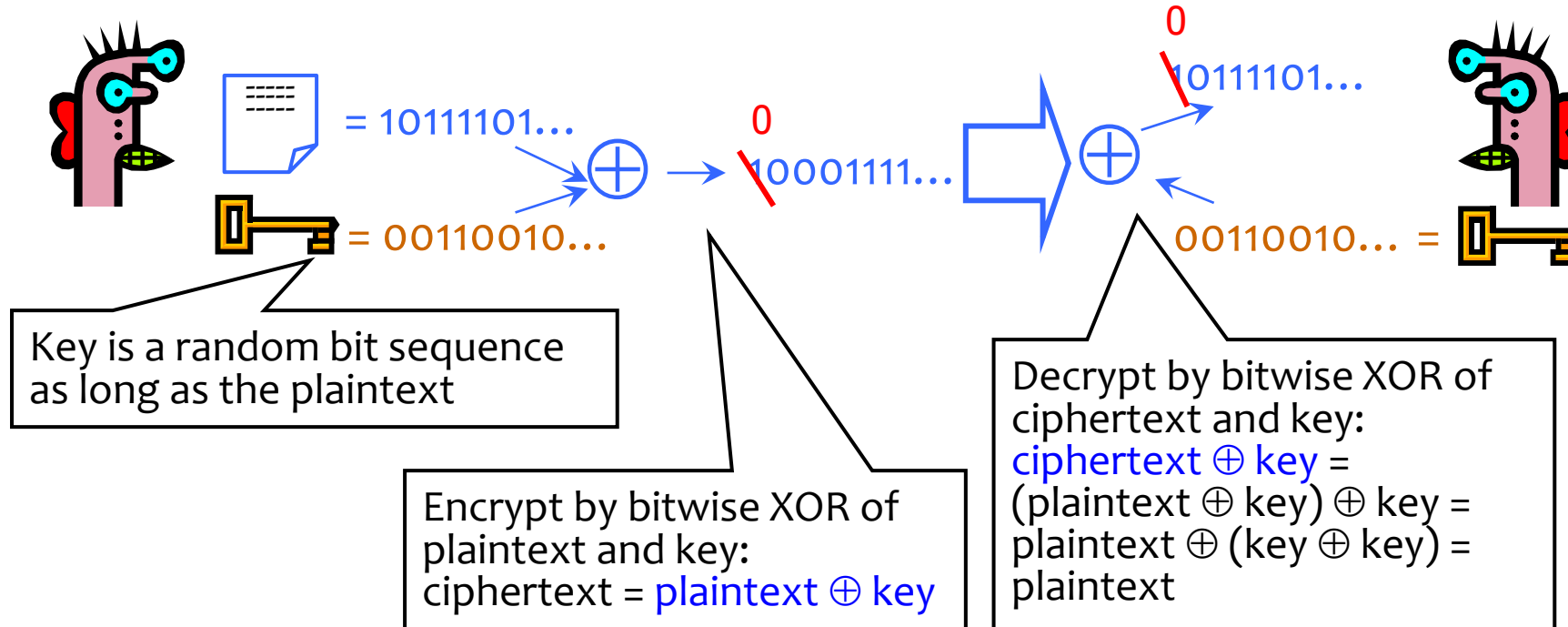
Learn relationship between plaintexts

$$\begin{aligned} C_1 \oplus C_2 &= (P_1 \oplus K) \oplus (P_2 \oplus K) = \\ &= (P_1 \oplus P_2) \oplus (K \oplus K) = P_1 \oplus P_2 \end{aligned}$$

Problems with One-Time Pad

- (1) Key must be as long as the plaintext
 - Impractical in most realistic scenarios
 - Still used for diplomatic and intelligence traffic
- (2) Insecure if keys are reused
 - Attacker can obtain XOR of plaintexts

Integrity?



Problems with One-Time Pad

- (1) Key must be as long as the plaintext
 - Impractical in most realistic scenarios
 - Still used for diplomatic and intelligence traffic
- (2) Insecure if keys are reused
 - Attacker can obtain XOR of plaintexts
- **(3) Does not guarantee integrity**
 - **One-time pad only guarantees confidentiality**
 - **Attacker cannot recover plaintext, but can easily change it to something else**

Reducing Key Size

- What to do when it is infeasible to pre-share huge random keys?
 - When one-time pad is unrealistic...
- Use special cryptographic primitives: block ciphers,
stream ciphers
 - Single key can be re-used (with some restrictions)
 - Not as theoretically secure as one-time pad

Stream Ciphers

- **One-time pad:** $\text{Ciphertext}(\text{Key}, \text{Message}) = \text{Message} \oplus \text{Key}$
 - Key must be a random bit sequence as long as message
- Idea: replace “random” with “pseudo-random”
 - Use a pseudo-random number generator (PRNG)
 - PRNG takes a short, truly random secret seed and expands it into a long “random-looking” sequence
 - E.g., 128-bit seed into a 10^6 -bit pseudo-random sequence
- $\text{Ciphertext}(\text{Key}, \text{Msg}) = \text{Msg} \oplus \text{PRNG}(\text{Key})$
 - Message processed bit by bit (like one-time pad)

No efficient algorithm can tell this sequence from truly random

Block Ciphers

- Operates on a single chunk (“block”) of plaintext
 - For example, 64 bits for DES, 128 bits for AES
 - Each key defines a different permutation
 - Same key is reused for each block (can use short keys)

