

CSE 484: Computer Security and Privacy

Cryptography

[MACs and Hash Functions]

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...

Admin

- Homework 2
 - Out soon™

When is an Encryption Scheme “Secure”?

- Hard to recover the key?
 - What if attacker can learn plaintext without learning the key?
- Hard to recover plaintext from ciphertext?
 - What if attacker learns some bits or some function of bits?

✓

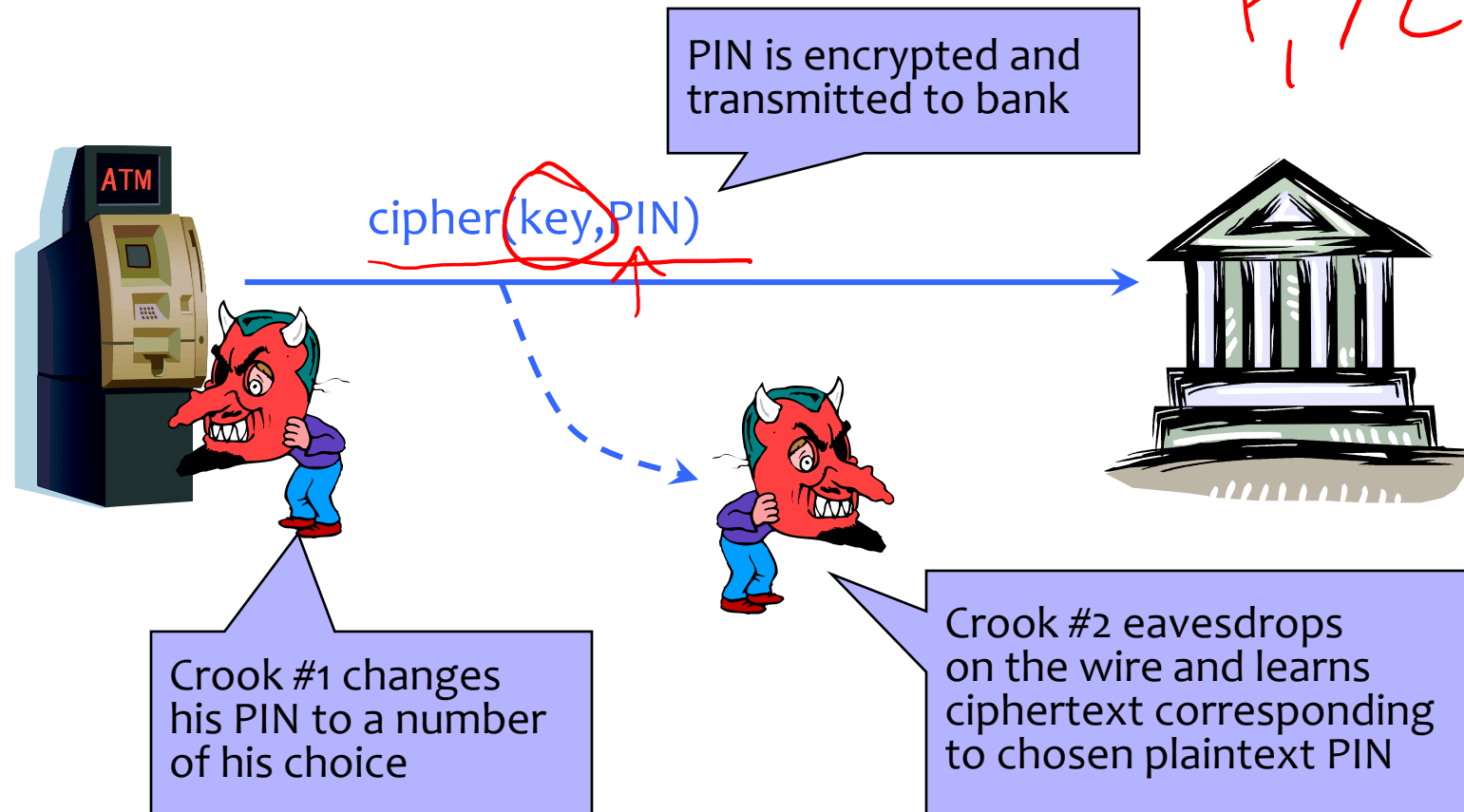
How Can a Cipher Be Attacked?

10x

- Attackers knows ciphertext and encryption algthm
 - What else does the attacker know? Depends on the application in which the cipher is used!

don't know key?

Chosen Plaintext Attack



... repeat for any PIN value

How Can a Cipher Be Attacked?

- Attackers knows ciphertext and encryption alghthm
 - What else does the attacker know? Depends on the application in which the cipher is used!
- Ciphertext-only attack ↩
- KPA: Known-plaintext attack (stronger) ↩
 - Knows some plaintext-ciphertext pairs
- CPA: Chosen-plaintext attack (even stronger) ↩
 - Can obtain ciphertext for any plaintext of his choice
- CCA: Chosen-ciphertext attack (very strong) ↩
 - Can decrypt any ciphertext except the target

CCA2

Very Informal Intuition

Minimum security requirement for a modern encryption scheme

P_{10} / C_{10}

P_{10} / C_{12}
 C_{10}

- Security against chosen-plaintext attack (CPA)
 - Ciphertext leaks no information about the plaintext
 - Even if the attacker correctly guesses the plaintext, he cannot verify his guess
 - Every ciphertext is unique, encrypting same message twice produces completely different ciphertexts
 - Implication: encryption must be randomized or stateful
- Security against chosen-ciphertext attack (CCA)
 - Integrity protection – it is not possible to change the plaintext by modifying the ciphertext

IND-CPA

IND-CCA

CCA2

The shape of the formal approach

- INDistinguishability under Chosen Plaintext Attack
 - IND-CPA

- Formalized *cryptographic game*

- Adversary submits pairs of plaintexts (M_a, M_b)
 - Gets back ONE of the ciphertexts (C_x)

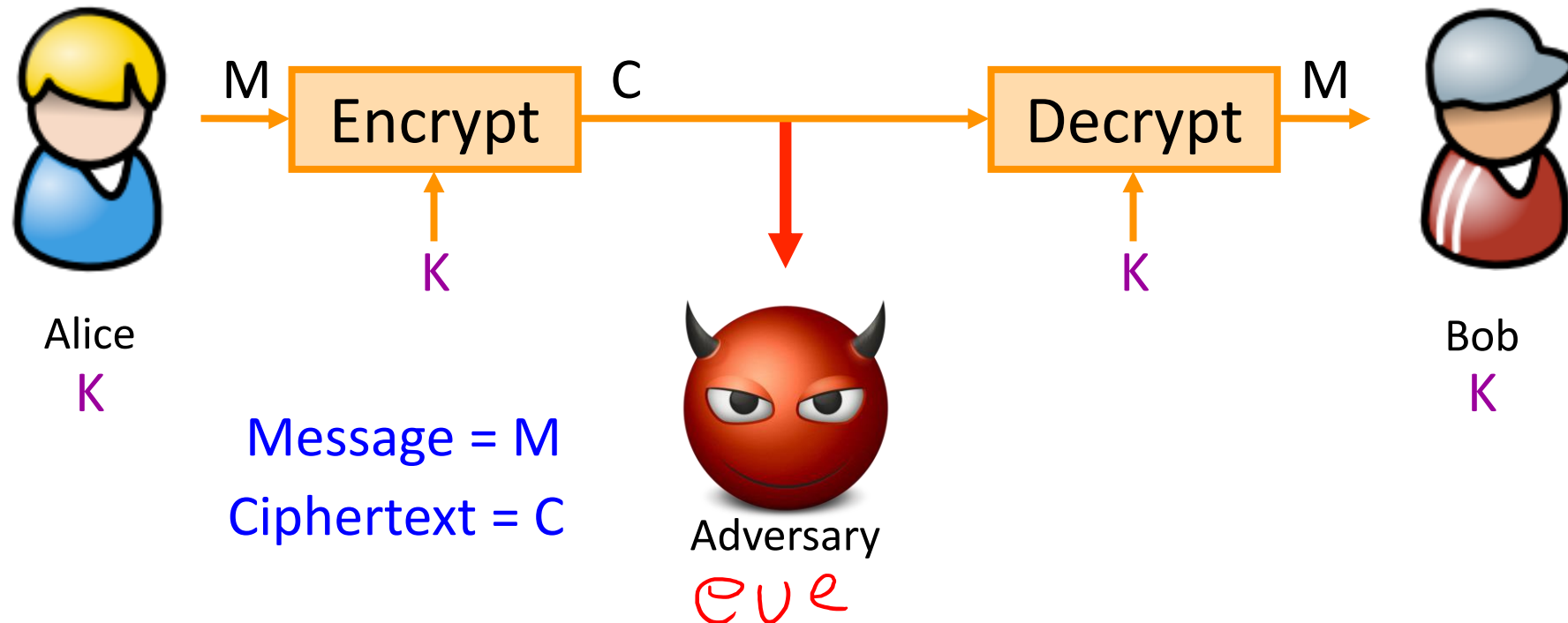
$M_a, M_b,$
 M_a, M_c
 M_a, M_d

- Adversary must guess which ciphertext this is (C_a or C_b)
 - If they can do better than 50/50, they win

CIA

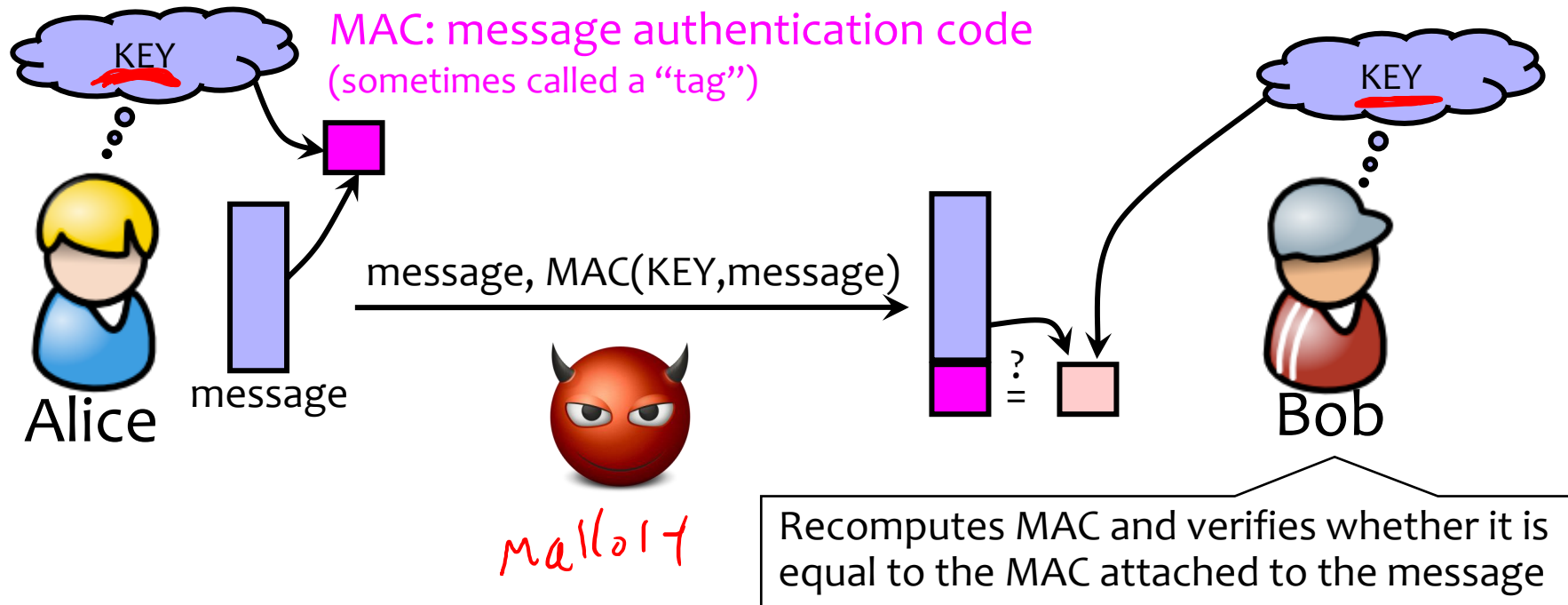
So Far: Achieving Privacy

Encryption schemes: A tool for protecting privacy.



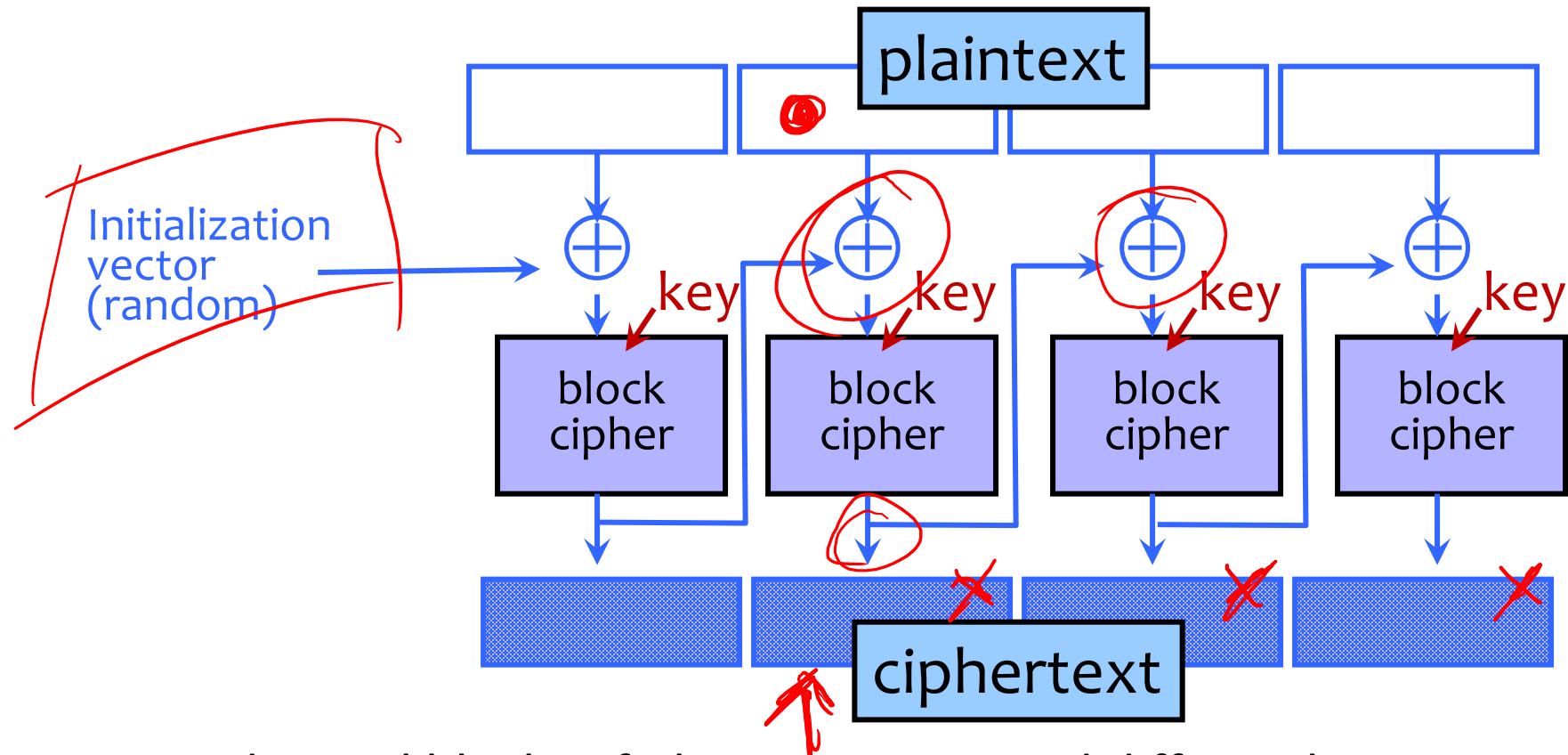
Now: Achieving Integrity

Message authentication schemes: A tool for protecting integrity.



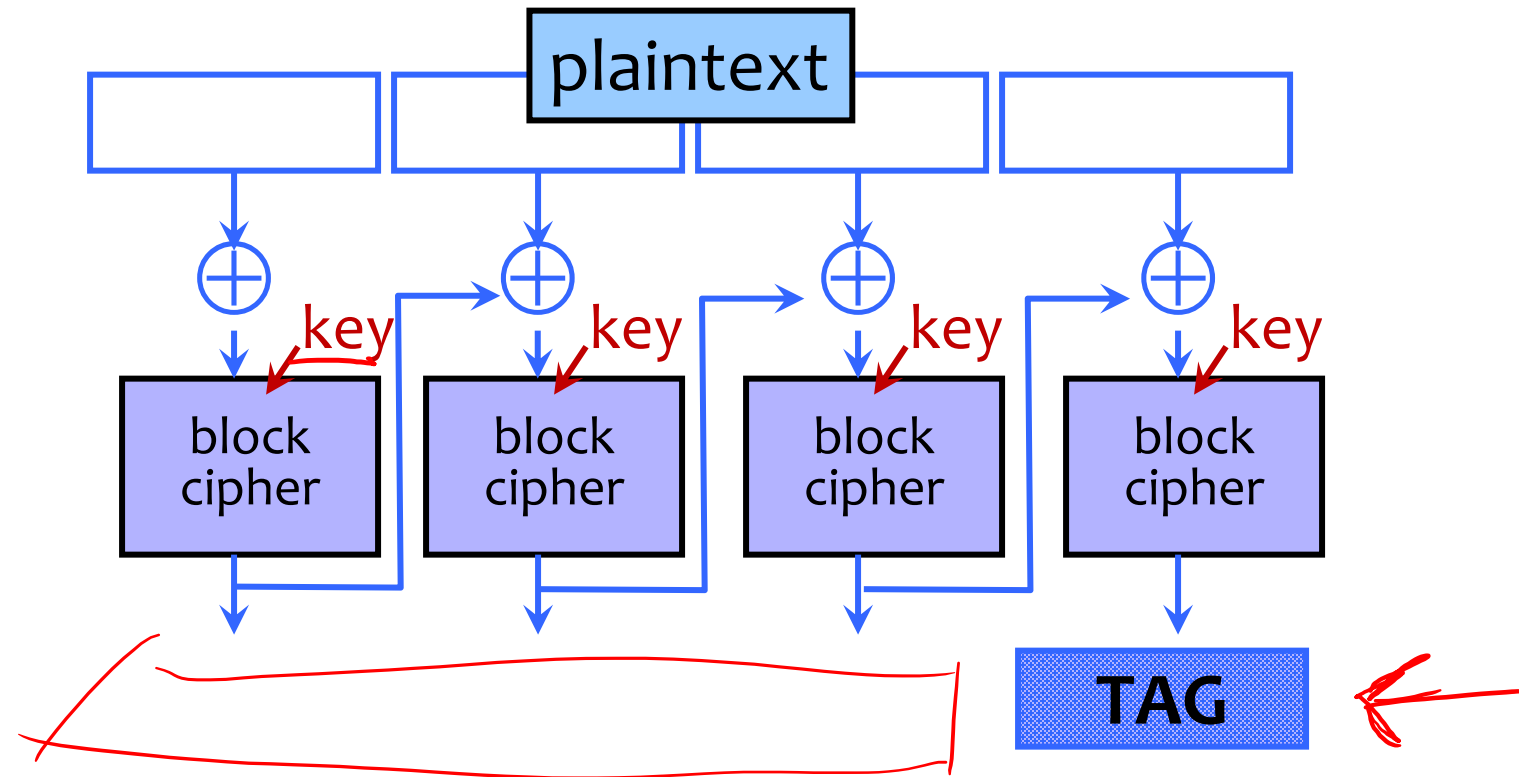
Integrity and authentication: only someone who knows KEY can compute correct MAC for a given message.

Reminder: CBC Mode Encryption



- Identical blocks of plaintext encrypted differently
- Last cipherblock depends on entire plaintext
 - Still does not guarantee integrity

CBC-MAC



- Not secure when system may MAC messages of different lengths (*more in section!*).
- NIST recommends a derivative called CMAC [FYI only]

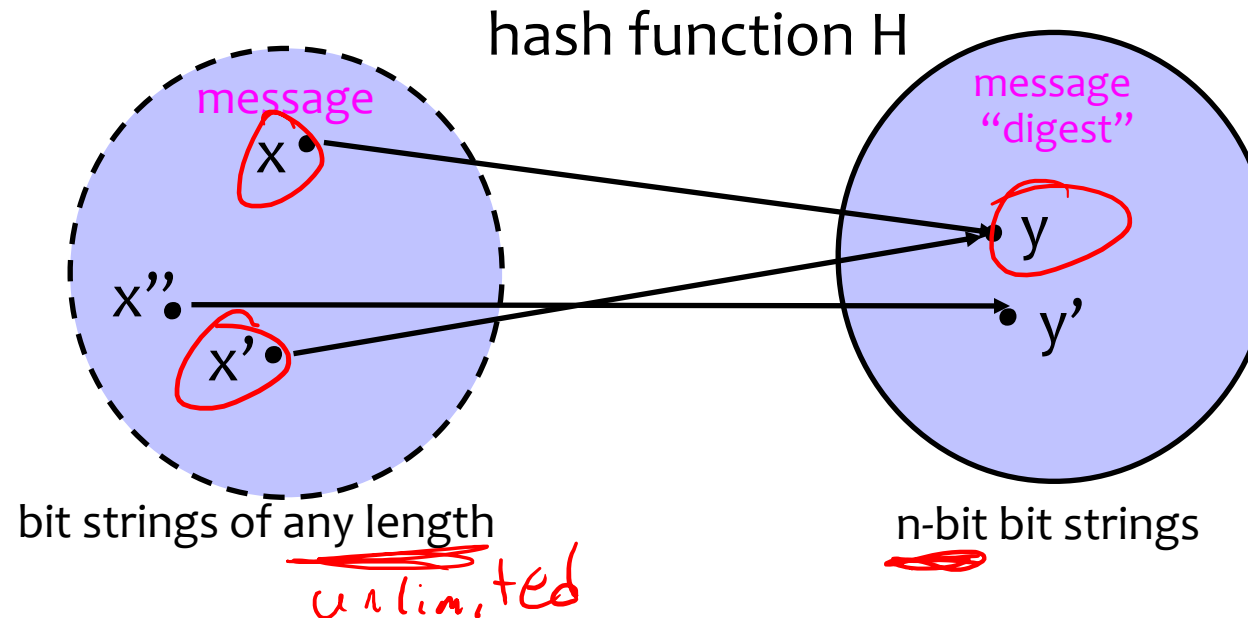
Another Tool: Hash Functions

You Just Did This

md5

```
franzi@codered:~/sploits$ md5sum sploit0.c  
3a2e6ce795bce4d06df1ff6835d25cea sploit0.c  
franzi@codered:~/sploits$
```

Hash Functions: Main Idea



- Hash function H is a lossy compression function
 - Collision: $h(x)=h(x')$ for distinct inputs x, x'
- $H(x)$ should look “random”
 - Every bit (almost) equally likely to be 0 or 1
- Cryptographic hash function needs a few properties...

Property 1: One-Way

$H(x)$ no key
?
x?
?
.

- Intuition: hash should be hard to invert
 - “Preimage resistance”
 - Let $h(x') = y \in \{0,1\}^n$ for a random x'
 - Given y , it should be hard to find any x such that $h(x)=y$
- How hard?
 - Brute-force: try every possible x , see if $h(x)=y$
 - SHA-1 (common hash function) has 160-bit output
 - Expect to try 2^{159} inputs before finding one that hashes to y .

Property 2: Collision Resistance

- Should be hard to find $x \neq x'$ such that $h(x)$ = $h(x')$

2^{159}

Birthday Paradox

- Are there two people in the first 1/8 of this class that have the same birthday?
 - 365 days in a year (366 some years)
 - Pick one person. To find another person with same birthday would take on the order of $365/2 = 182.5$ people
 - **Expect birthday “collision” with a room of only 23 people.**
 - For simplicity, approximate when we expect a collision as $\text{sqrt}(365)$.
- Why is this important for cryptography?
 - 2^{128} different 128-bit values
 - Pick one value at random. To exhaustively search for this value requires trying on average 2^{127} values.
 - **Expect “collision” after selecting approximately 2^{64} random values.**
 - **64 bits** of security against collision attacks, not 128 bits.


$x' \quad h(x') = h(x)$

Property 2: Collision Resistance

- Should be hard to find $x \neq x'$ such that $h(x) = h(x')$
- Birthday paradox means that brute-force collision search is **only** $O(2^{n/2})$, *not* $O(2^n)$
 - For SHA-1, this means $O(\underline{2^{80}})$ vs. $O(\underline{2^{160}})$

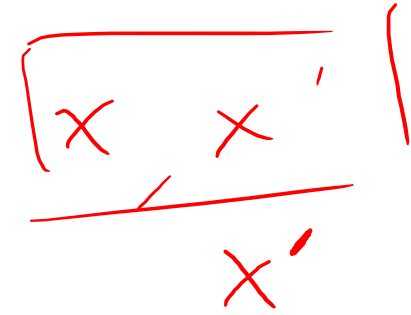
One-Way vs. Collision Resistance

One-wayness does not imply collision resistance. 

Collision resistance does not imply one-wayness. 

You can prove this by constructing a function that has one property but not the other.

Property 3: Weak Collision Resistance



- Given randomly chosen x , hard to find x' such that $h(x)=h(x')$
 - Attacker must find collision for a specific x . By contrast, to break collision resistance it is enough to find any collision.
 - Brute-force attack requires $O(2^n)$ time
- Weak collision resistance does not imply collision resistance.

Hashing vs. Encryption

- Hashing is one-way. There is no “un-hashing”
 - A ciphertext can be decrypted with a decryption key... hashes have no equivalent of “decryption”
- Hash(x) looks “random” but can be compared for equality with Hash(x')
 - Hash the same input twice → same hash value
 - Encrypt the same input twice → different ciphertexts
- Cryptographic hashes are also known as “cryptographic checksums” or “message digests”

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CIA

Application: Password Hashing

- Instead of user password, store `hash(password)`
- When user enters a password, compute its hash and compare with the entry in the password file
- Why is hashing better than encryption here?

Application: Password Hashing

- Instead of user password, store `hash(password)`
- When user enters a password, compute its hash and compare with the entry in the password file
- Why is hashing better than encryption here?
- System does not store actual passwords!
- Don't need to worry about where to store the key!
- Cannot go from hash to password!

Application: Password Hashing

- Which property do we need?
 - One-wayness?
 - (At least weak) Collision resistance?
 - Both?

~~x~~
 $h(x)$

$x'?$
 $h(x')$

password + _____

Application: Password Hashing + Salting

- **Salting**

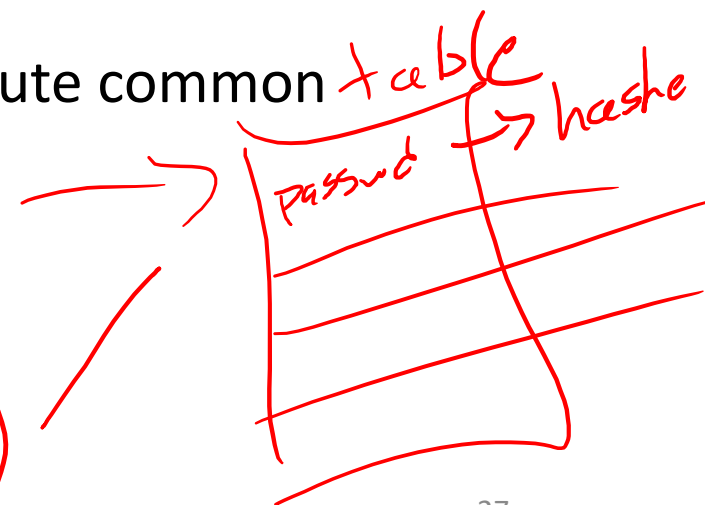
- We 'salt' hashes for password by adding a randomized suffix to the password
 - E.g. Hash("coolpassword" + "35B67C2A")
- We then store the salt with the hashed password!

- The goal is to prevent precomputation attacks

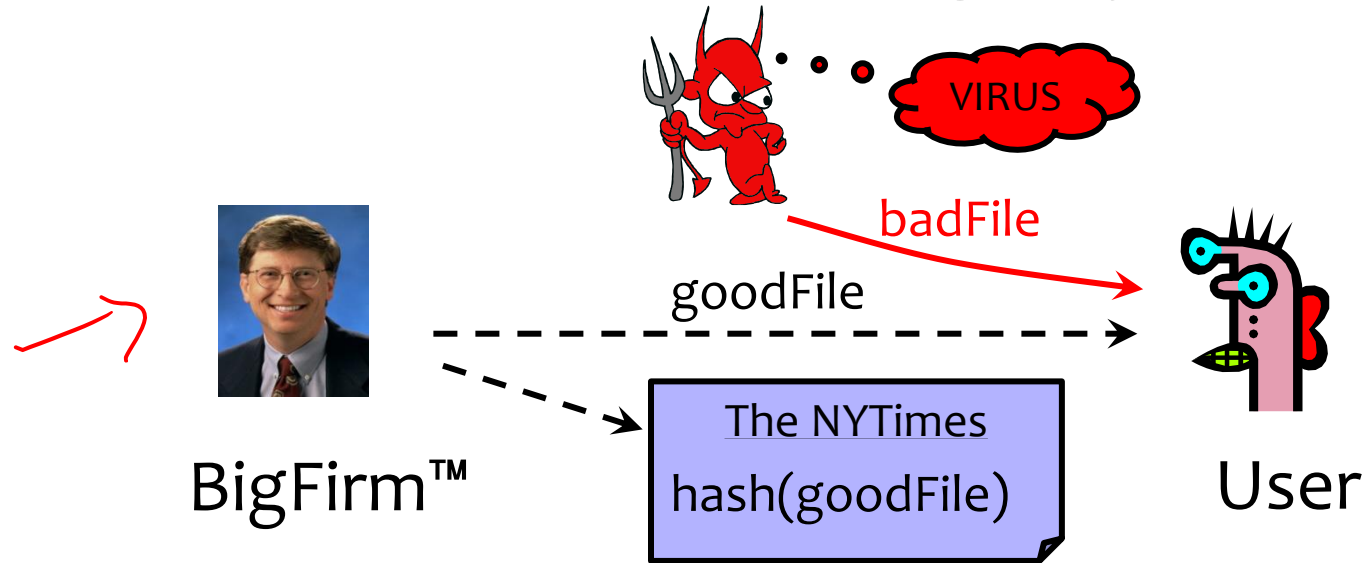
- If the adversary doesn't know the salt, they can't precompute common passwords

sha512

$h(pwd)$



Application: Software Integrity



Goal: Software manufacturer wants to ensure file is received by users without modification.

Idea: given goodFile and hash(goodFile), very hard to find badFile such that $\text{hash}(\text{goodFile}) = \text{hash}(\text{badFile})$

Application: Software Integrity

- Which property do we need?
 - One-wayness? [?]
 - (At least weak) Collision resistance?
 - Both?

Which Property Do We Need?

One-wayness, Collision Resistance, Weak CR?

- UNIX passwords stored as hash(password)
 - **One-wayness:** hard to recover the/a valid password
- Integrity of software distribution
 - **Weak collision resistance**
 - But software images are not really random... may need **full collision resistance** if considering malicious developers

Which Property Do We Need?

- UNIX passwords stored as $\text{hash}(\text{password})$
 - **One-wayness:** hard to recover the/a valid password
- Integrity of software distribution
 - **Weak collision resistance**
 - But software images are not really random... may need **full collision resistance** if considering malicious developers
- Commitments (e.g. auctions)
 - Alice wants to bid B, sends $H(B)$, later reveals B
 - **One-wayness:** rival bidders should not recover B (this may mean that she needs to hash some randomness with B too)
 - **Collision resistance:** Alice should not be able to change her mind to bid B' such that $H(B)=H(B')$

Common Hash Functions

- MD5 – Don't Use!
 - 128-bit output
 - Designed by Ron Rivest, used very widely
 - Collision-resistance broken (summer of 2004)
- RIPEMD
 - 160-bit version is OK
 - 128-bit version is *not* good
- SHA-1 (Secure Hash Algorithm) – Don't Use!
 - 160-bit output
 - US government (NIST) standard as of 1993-95
 - Theoretically broken 2005; practical attack 2017!
- SHA-2: SHA-256, SHA-512, SHA-224, SHA-384
- SHA-3: standard released by NIST in August 2015

2^{64}

80

Keccak

SHA-1 Broken in Practice (2017)

100,000x

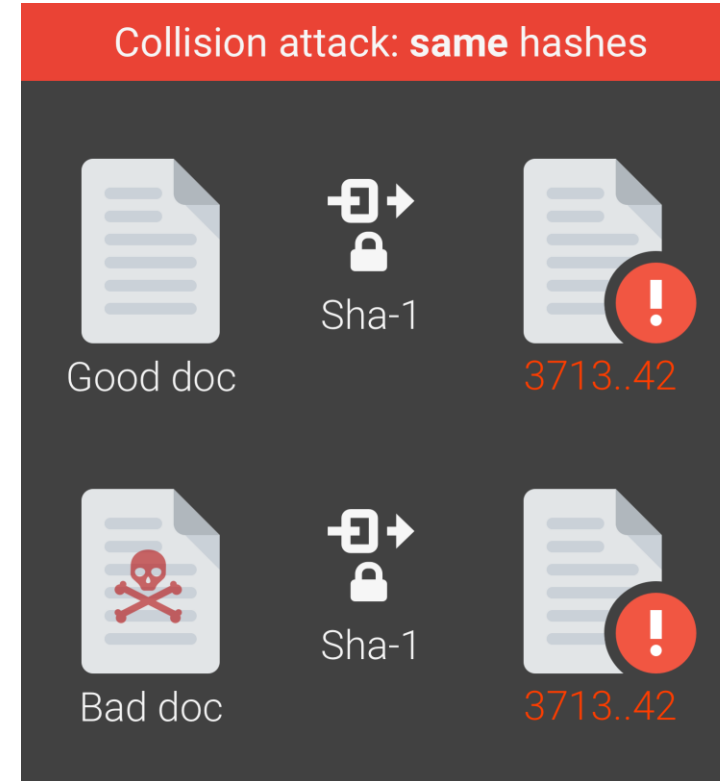
Google just cracked one of the building blocks of web encryption (but don't worry)

It's all over for SHA-1

by Russell Brandom | @russellbrandom | Feb 23, 2017, 11:49am EST

<https://shattered.io>

110 years CPU



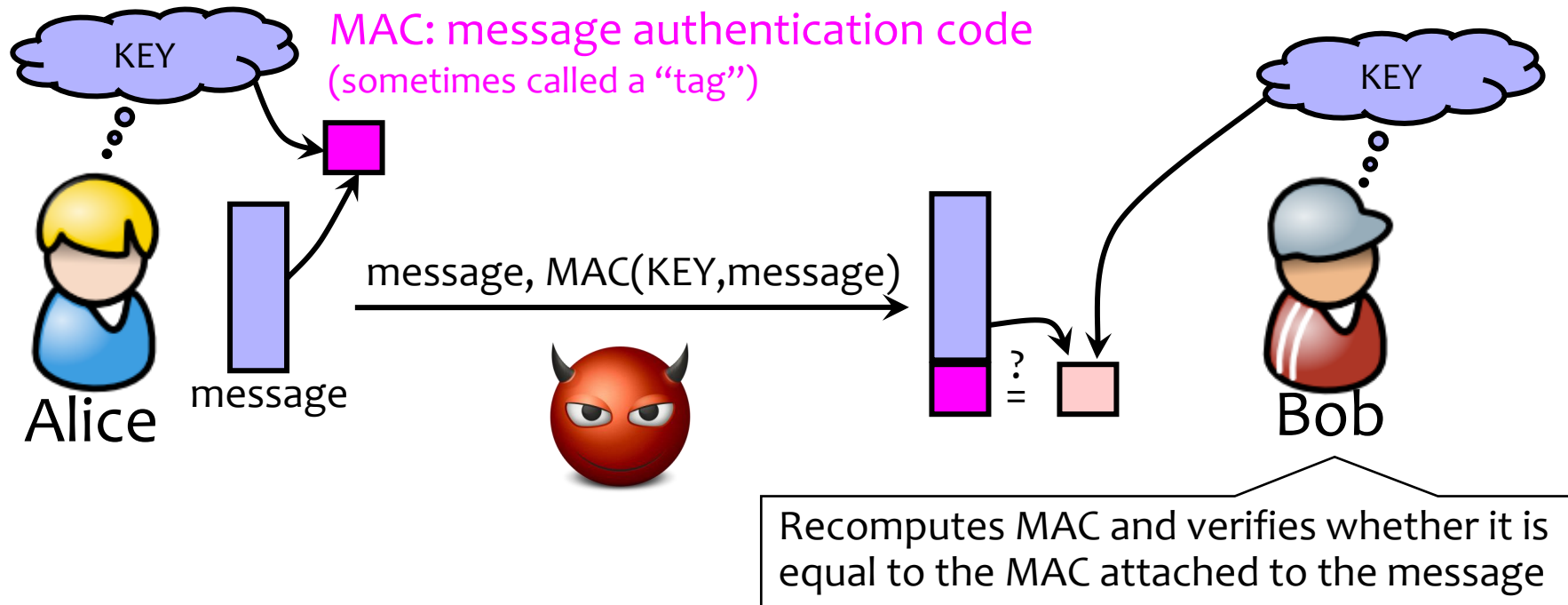
Aside: How we evaluate hash functions

- Speed
 - Is it amenable to hardware implementations?
- Diffusion
 - Does changing 1 bit in the input affect all output bits?
- Resistance to attack approaches
 - Collisions?
 - Length extensions?
 - etc

sha-2
sha-3

Recall: Achieving Integrity

Message authentication schemes: A tool for protecting integrity.



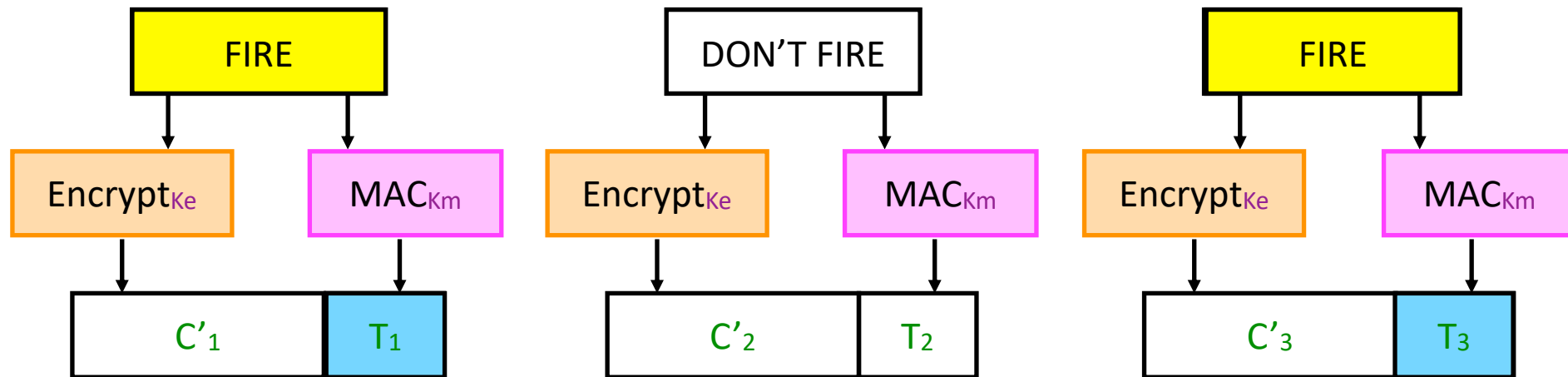
Integrity and authentication: only someone who knows KEY can compute correct MAC for a given message.

HMAC

- Construct MAC from a cryptographic hash function
 - Invented by Bellare, Canetti, and Krawczyk (1996)
 - Used in SSL/TLS, mandatory for IPsec
- Why not encryption?
 - Hashing is faster than block ciphers in software
 - Can easily replace one hash function with another
 - There used to be US export restrictions on encryption

Authenticated Encryption

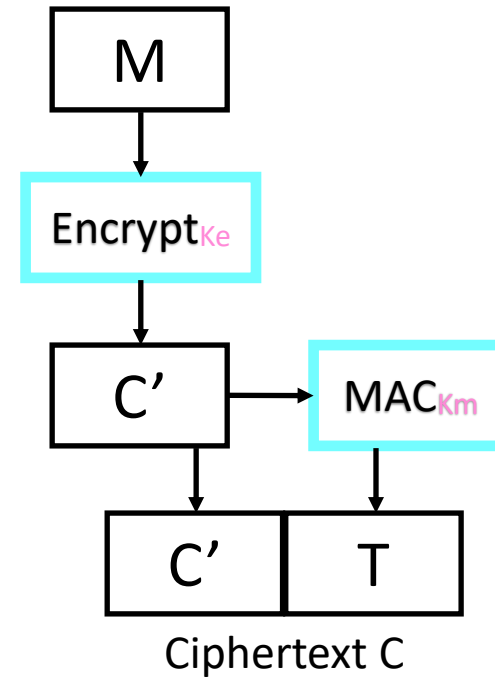
- What if we want both privacy and integrity?
- Natural approach: combine **encryption scheme** and a **MAC**.
- **But be careful!**
 - Obvious approach: Encrypt-and-MAC
 - Problem: MAC is deterministic! same plaintext \rightarrow same MAC



Authenticated Encryption

- Instead:

Encrypt *then* MAC.
- (Not as good:
MAC-then-Encrypt)



Encrypt-then-MAC