

CSE 484: Computer Security and Privacy

Cryptography

Hashing + Integrity + Asymmetric

Fall 2021

David Kohlbrenner

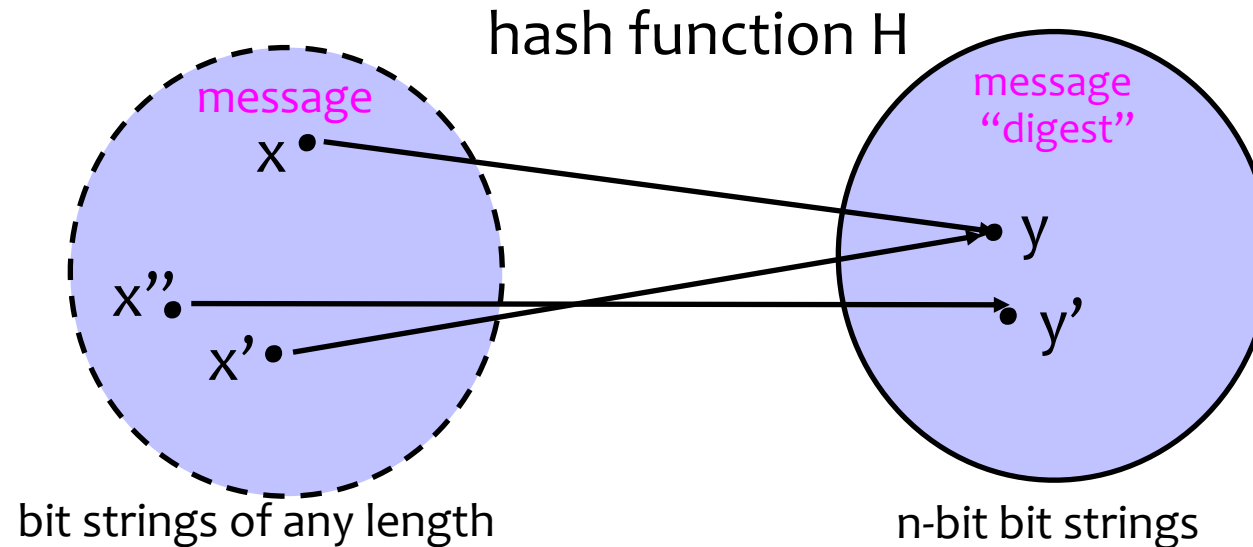
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Administrivia

- Lab 1 due on Wednesday
- HW2 is out

Hash Functions: Main Idea



- Hash function H is a lossy compression function
 - Collision: $h(x)=h(x')$ for distinct inputs x, x'
- $H(x)$ should look "random"
 - Every bit (almost) equally likely to be 0 or 1
- Cryptographic hash function needs a few properties...

One-Way vs. Collision Resistance

One-wayness does not imply collision resistance.

Collision resistance does not imply one-wayness.

You can prove this by constructing a function that has one property but not the other.

Property 3: Weak Collision Resistance

- Given randomly chosen x , hard to find x' such that $h(x)=h(x')$
 - Attacker must find collision for a specific x . By contrast, to break collision resistance it is enough to find any collision.
 - Brute-force attack requires $O(2^n)$ time
- Weak collision resistance does not imply collision resistance.

Hashing vs. Encryption

- Hashing is one-way. There is no “un-hashing”
 - A ciphertext can be decrypted with a decryption key... hashes have no equivalent of “decryption”
- Hash(x) looks “random” but can be compared for equality with Hash(x’)
 - Hash the same input twice → same hash value
 - Encrypt the same input twice → different ciphertexts
- Cryptographic hashes are also known as “cryptographic checksums” or “message digests”

Application: Password Hashing

- Instead of user password, store `hash(password)`
- When user enters a password, compute its hash and compare with the entry in the password file
- Why is hashing better than encryption here?
 - Breakout

Application: Password Hashing

- Instead of user password, store `hash(password)`
- When user enters a password, compute its hash and compare with the entry in the password file
- **Why is hashing better than encryption here?**
- System does not store actual passwords!
- Don't need to worry about where to store the key!
- Cannot go from hash to password!

Application: Password Hashing

- Which property do we need?
 - One-wayness?
 - (At least weak) Collision resistance?
 - Both?

Application: Password Hashing + Salting

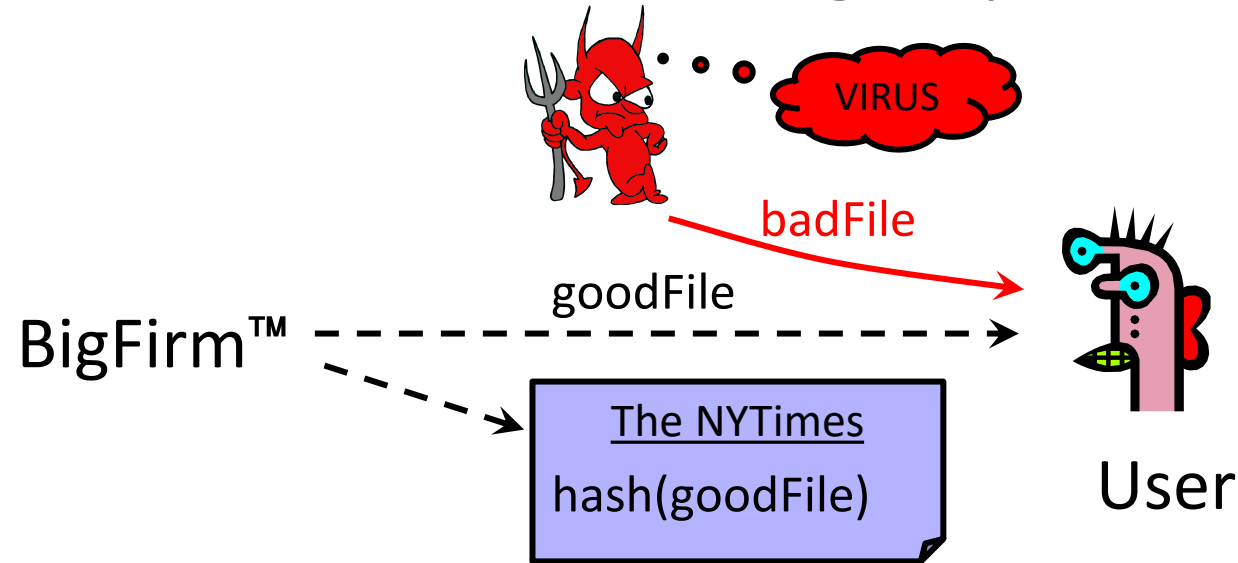
- **Salting**

- We 'salt' hashes for password by adding a randomized suffix to the password
 - E.g. Hash("coolpassword"+"35B67C2A")
 - We then store the salt with the hashed password!
 - Server generates the salt
-
- The goal is to prevent *precomputation attacks*
 - If the adversary doesn't know the salt, they can't *precompute* common passwords

Hash Functions Review

- Map large domain to small range (e.g., range of all 160- or 256-bit values)
- Properties:
 - Collision Resistance: Hard to find two distinct inputs that map to same output
 - One-wayness: Given a point in the range (that was computed as the hash of a random domain element), hard to find a preimage
 - Weak Collision Resistance: Given a point in the domain and its hash in the range, hard to find a new domain element that maps to the same range element

Application: Software Integrity



Goal: Software manufacturer wants to ensure file is received by users without modification.

Idea: given goodFile and hash(goodFile), very hard to find badFile such that hash(goodFile)=hash(badFile)

Application: Software Integrity

- Which property do we need?
 - One-wayness?
 - (At least weak) Collision resistance?
 - Both?

Which Property Do We Need?

One-wayness, Collision Resistance, Weak CR?

- UNIX passwords stored as hash(password)
 - **One-wayness**: hard to recover the/a valid password
- Integrity of software distribution
 - **Weak collision resistance**
 - But software images are not really random... may need **full collision resistance** if considering malicious developers

Which Property Do We Need?

- UNIX passwords stored as hash(password)
 - **One-wayness:** hard to recover the/a valid password
- Integrity of software distribution
 - **Weak collision resistance**
 - But software images are not really random... may need **full collision resistance** if considering malicious developers
- Commitments (e.g. auctions)
 - Alice wants to bid B, sends $H(B)$, later reveals B
 - **One-wayness:** rival bidders should not recover B (this may mean that they need to hash some randomness with B too)
 - **Collision resistance:** Alice should not be able to change their mind to bid B' such that $H(B)=H(B')$

Commitments

Common Hash Functions

- **SHA-2: SHA-256, SHA-512, SHA-224, SHA-384**
- **SHA-3: standard released by NIST in August 2015**
- MD5 – **Don't Use!**
 - 128-bit output
 - Designed by Ron Rivest, used very widely
 - Collision-resistance broken (summer of 2004)
- RIPEMD
 - 160-bit version is OK
 - 128-bit version is *not* good
- SHA-1 (Secure Hash Algorithm) – **Don't Use!**
 - 160-bit output
 - US government (NIST) standard as of 1993-95
 - Theoretically broken 2005; practical attack 2017!

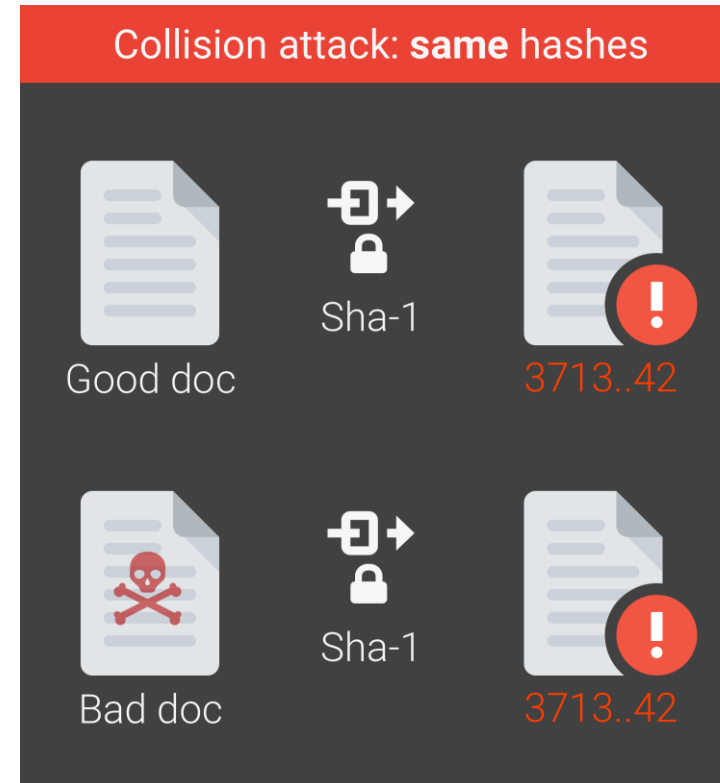
SHA-1 Broken in Practice (2017)

Google just cracked one of the building blocks of web encryption (but don't worry)

It's all over for SHA-1

by [Russell Brandom](#) | [@russellbrandom](#) | Feb 23, 2017, 11:49am EST

<https://shattered.io>

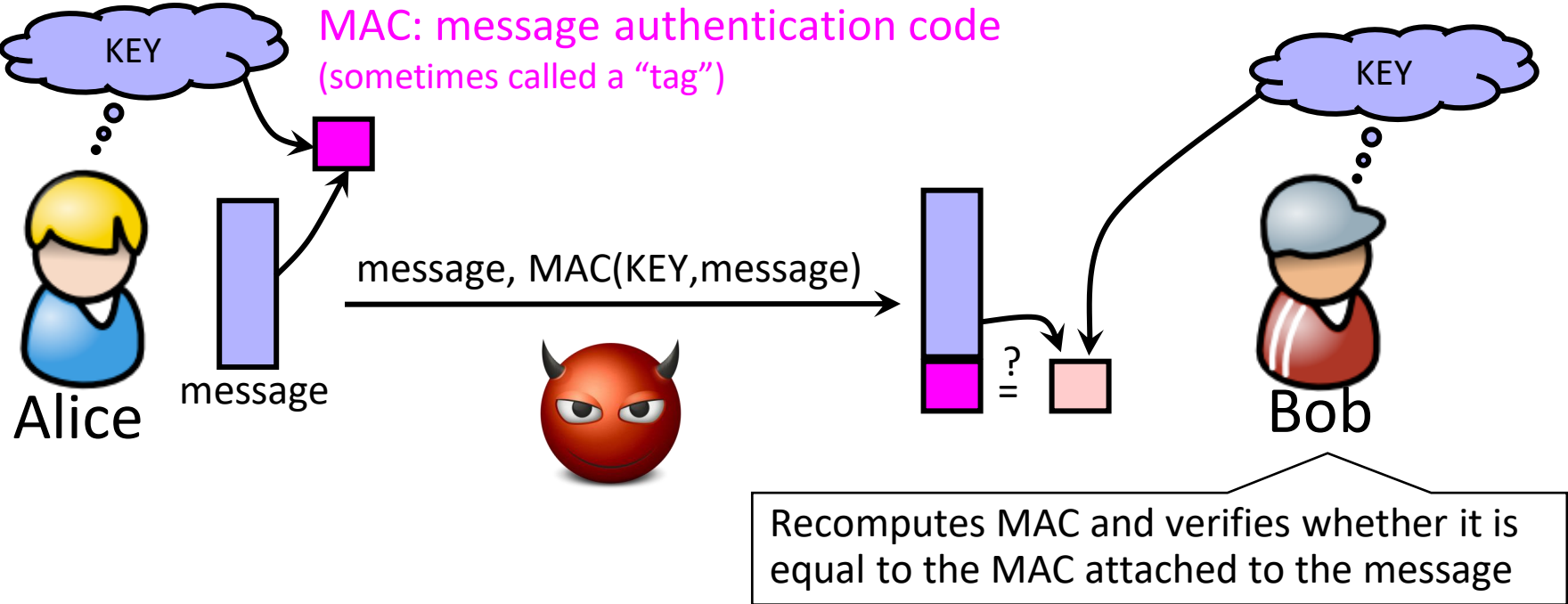


Aside: How we evaluate hash functions

- Speed
 - Is it amenable to hardware implementations?
- Diffusion
 - Does changing 1 bit in the input affect all output bits?
- Resistance to attack approaches
 - Collisions?
 - Length extensions?
 - etc

Recall: Achieving Integrity

Message authentication schemes: A tool for protecting integrity.



Integrity and authentication: only someone who knows KEY can compute correct MAC for a given message.

HMAC

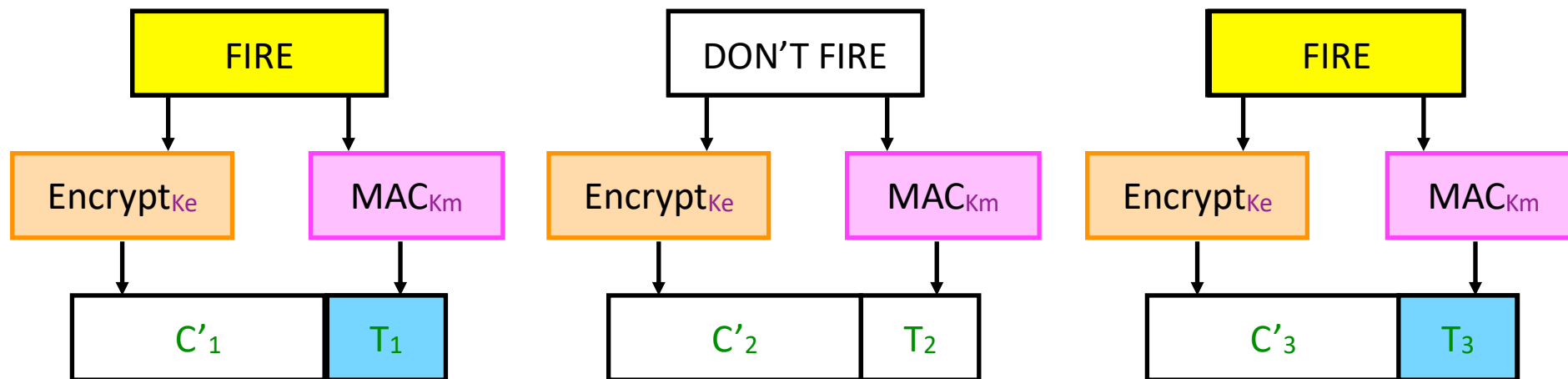
- Construct MAC from a cryptographic hash function
 - Invented by Bellare, Canetti, and Krawczyk (1996)
 - Used in SSL/TLS, mandatory for IPsec
- Why not encryption? (Historical reasons)
 - Hashing is faster than block ciphers in software
 - Can easily replace one hash function with another
 - There used to be US export restrictions on encryption

MAC with SHA3

- $\text{SHA3}(\text{Key} || \text{Message})$
- SHA3 has some nice features that prevent the class of attacks HMAC prevents

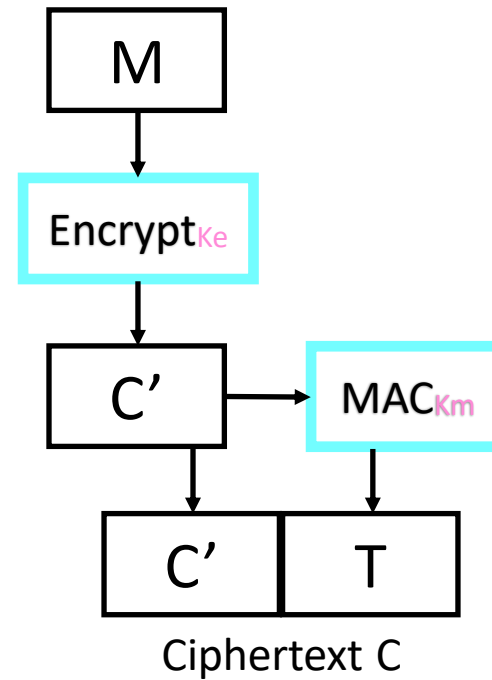
Authenticated Encryption

- What if we want both privacy and integrity?
- Natural approach: combine **encryption scheme** and a **MAC**.
- **But be careful!**
 - Obvious approach: **Encrypt-and-MAC**
 - Problem: **MAC is deterministic! same plaintext \rightarrow same MAC**



Authenticated Encryption

- Instead:
Encrypt *then* MAC.
- (Not as good:
MAC-then-Encrypt)



Encrypt-then-MAC

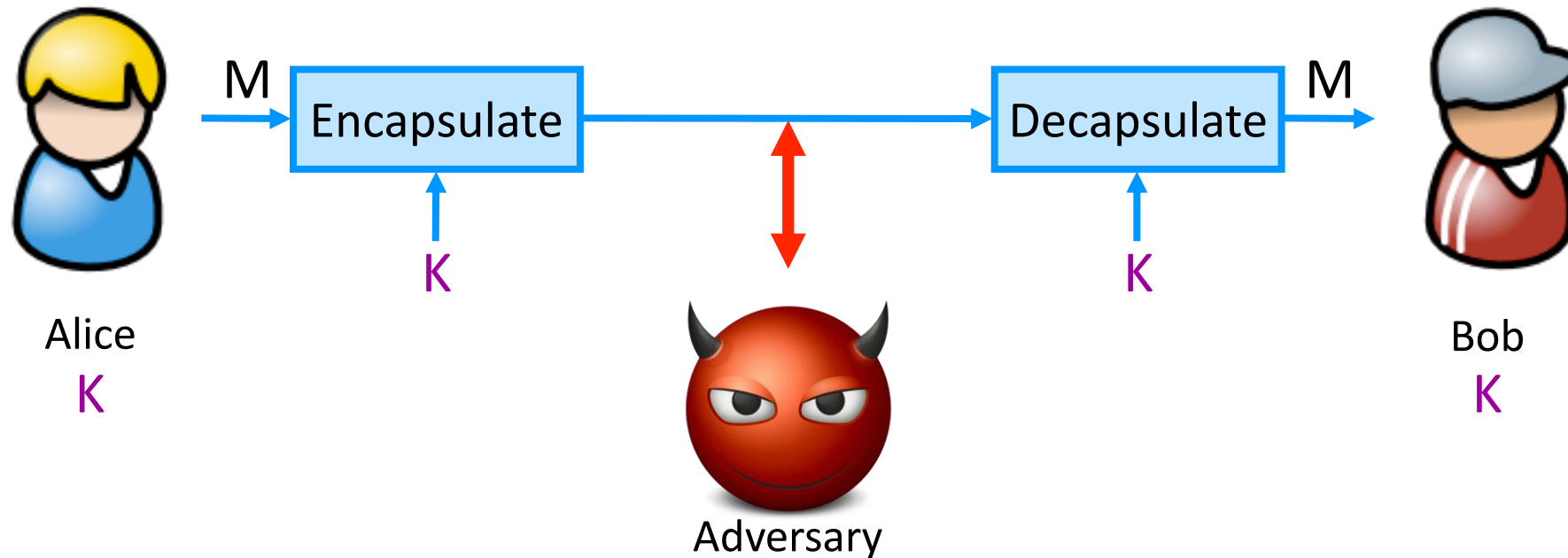
Back to cryptography land

Stepping Back: Flavors of Cryptography

- Symmetric cryptography
 - Both communicating parties have access to a **shared random string K** , called the **key**.
- Asymmetric cryptography
 - Each party creates a public key **pk** and a secret key **sk** .

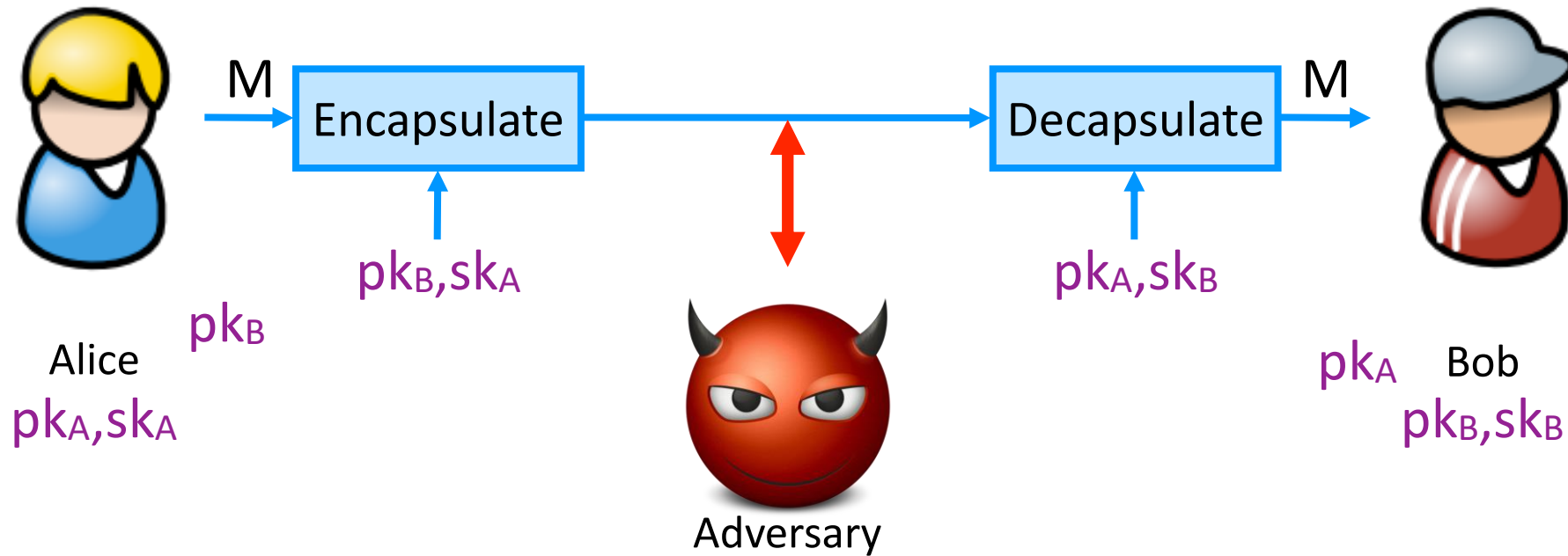
Symmetric Setting

Both communicating parties have access to a **shared random string K** , called the **key**.

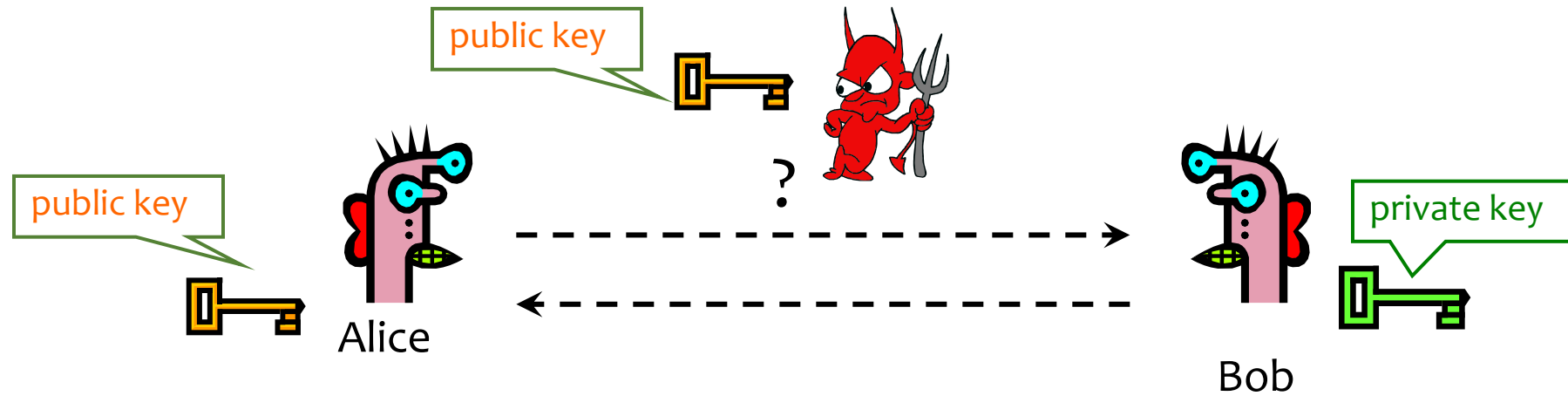


Asymmetric Setting

Each party creates a public key pk and a secret key sk .



Public Key Crypto: Basic Problem



Given: Everybody knows Bob's **public key**
Only Bob knows the corresponding **private key**

Ignore for now: How do we know it's REALLY Bob's??

Goals: 1. Alice wants to send a secret message to Bob
2. Bob wants to authenticate themselves

Applications of Public Key Crypto

- Encryption for confidentiality
 - Anyone can encrypt a message
 - With symmetric crypto, must know secret key to encrypt
 - Only someone who knows private key can decrypt
 - Key management is simpler (or at least different)
 - Secret is stored only at one site: good for open environments
- Digital signatures for authentication
 - Can “sign” a message with your private key
- Session key establishment
 - Exchange messages to create a secret session key
 - Then switch to symmetric cryptography (why?)

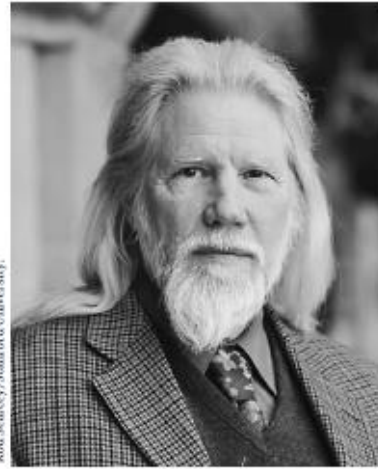
Session Key Establishment

Modular Arithmetic

- Given g and prime p , compute: $g^1 \bmod p, g^2 \bmod p, \dots, g^{100} \bmod p$
 - For $p=11, g=10$
 - $10^1 \bmod 11 = 10, 10^2 \bmod 11 = 1, 10^3 \bmod 11 = 10, \dots$
 - Produces cyclic group $\{10, 1\}$ (order=2)
 - For $p=11, g=7$
 - $7^1 \bmod 11 = 7, 7^2 \bmod 11 = 5, 7^3 \bmod 11 = 2, \dots$
 - Produces cyclic group $\{7, 5, 2, 3, 10, 4, 6, 9, 8, 1\}$ (order = 10)
 - $g=7$ is a “generator” of Z_{11}^*

Diffie-Hellman Protocol (1976)

Diffie and Hellman Receive 2015 Turing Award



Rod Seaman/Stanford University

Whitfield Diffie



Linda A. Ciervo/Stanford News Service

Martin E. Hellman

Diffie-Hellman Protocol (1976)

- Alice and Bob never met and share no secrets
- Public info: p and g
 - p is a large prime, g is a **generator** of Z_p^*
 - $Z_p^* = \{1, 2 \dots p-1\}$; a Z_p^* i such that $a = g^i \pmod p$
 - Modular arithmetic: numbers “wrap around” after they reach p

