

CSE 484 In-class Worksheet #8 – Lecture 10– Fall 2017

Name: _____ UW Student #: _____ Date: _____

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Partner names for this activity: _____

Q1: For hash functions, one-wayness does not imply collision resistance. We can prove this by constructing a hash function that is one-way but *not* collision resistant.

Suppose g is one-way.

Define $h(x)$ as $g(x')$ where x' is x except the last bit.

Then h is one-way (to invert h , must invert g).

But collisions for h are easy to find. **How?**

Q2: For hash functions, collision resistance does not imply one-wayness. We can prove this by constructing a hash function that is collision resistant but *not* one-way.

Suppose g is collision-resistant.

Define $y=h(x)$ to be $0x$ if x is n -bit long, $1g(x)$ otherwise.

Then h is collision resistant: if y starts with 0 , then there are no collisions. If y starts with 1 , then must find collisions in g (which is hard by definition).

But h is not one-way. Some y 's are easy to invert! **Which ones, and how?**

Q3: What problem do you see with the “Encrypt-and-MAC” approach for authenticated encryption?