

CSE 484 (Winter 2010)

# Symmetric Cryptography

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Thanks to Dan Boneh, Dieter Gollmann, John Manferdelli, John Mitchell, Vitaly Shmatikov, Bennet Yee, and many others for sample slides and materials ...

# Goals for Today

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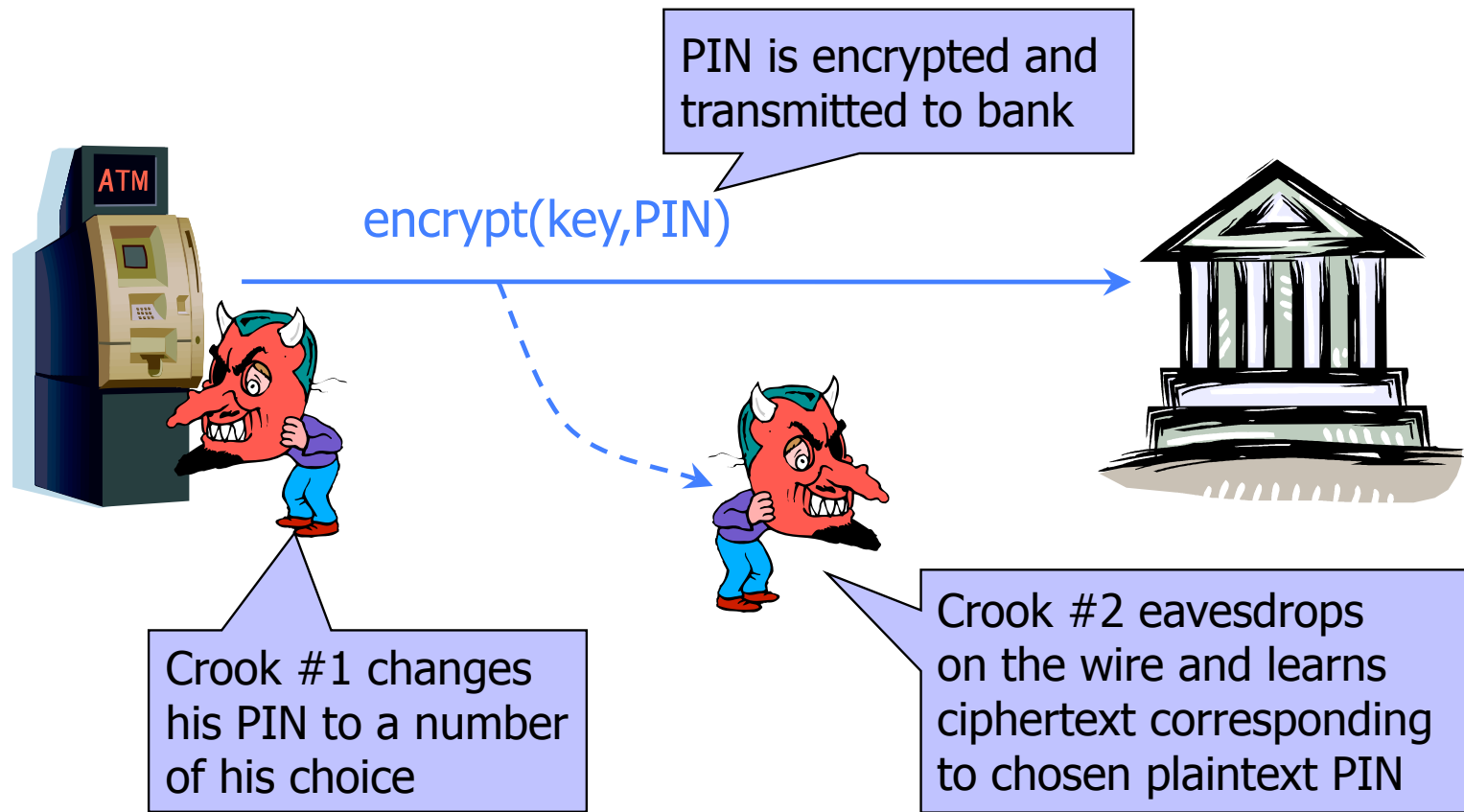
- ◆ Under the hood: Symmetric encryption

# Attack Scenarios for Encryption

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- ◆ Ciphertext-Only
- ◆ Known Plaintext
- ◆ Chosen Plaintext
- ◆ Chosen Ciphertext (and Chosen Plaintext)
  
- ◆ (General advice: Target strongest level of privacy possible -- even if not clear why -- for extra "safety")

# Chosen-Plaintext Attack



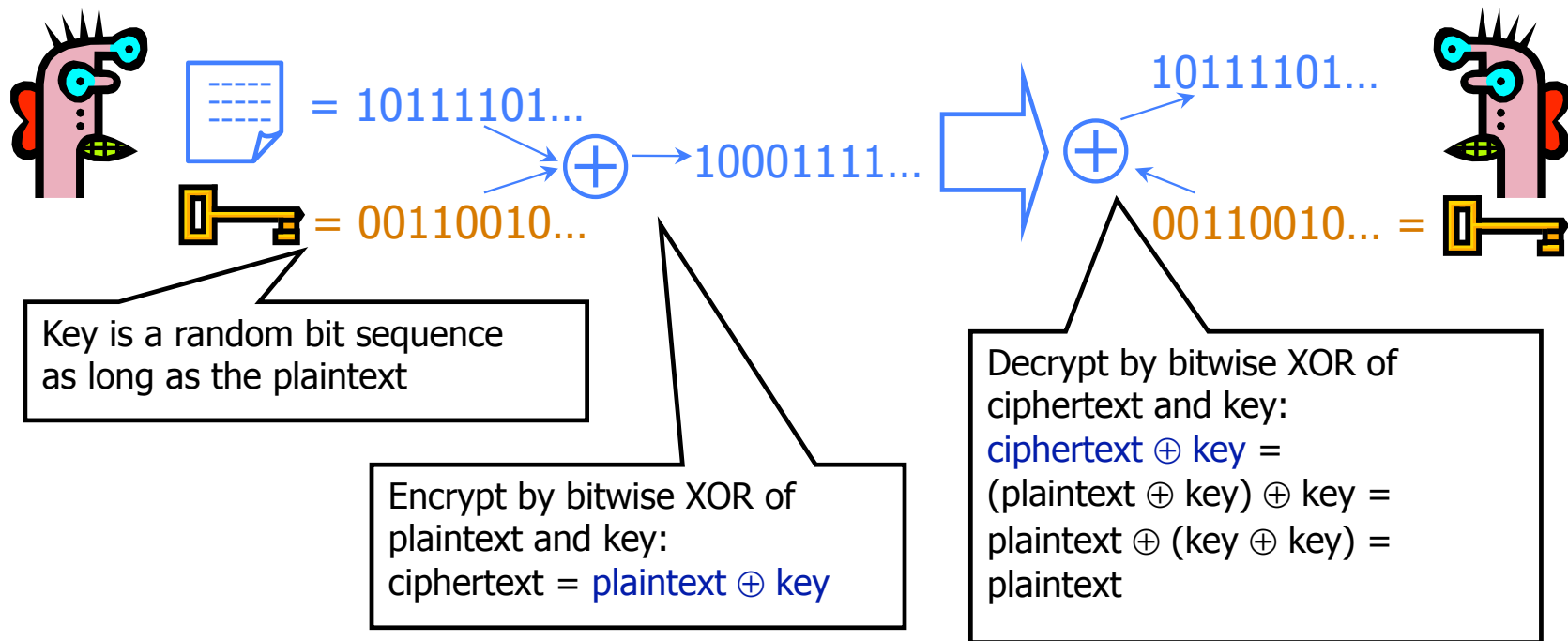
... repeat for any PIN value

# Attack Scenarios for Integrity

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- ◆ What do you think these scenarios should be?

# One-Time Pad



Cipher achieves **perfect secrecy** if and only if there are as many possible keys as possible plaintexts, and every key is equally likely (Claude Shannon)

# Advantages of One-Time Pad

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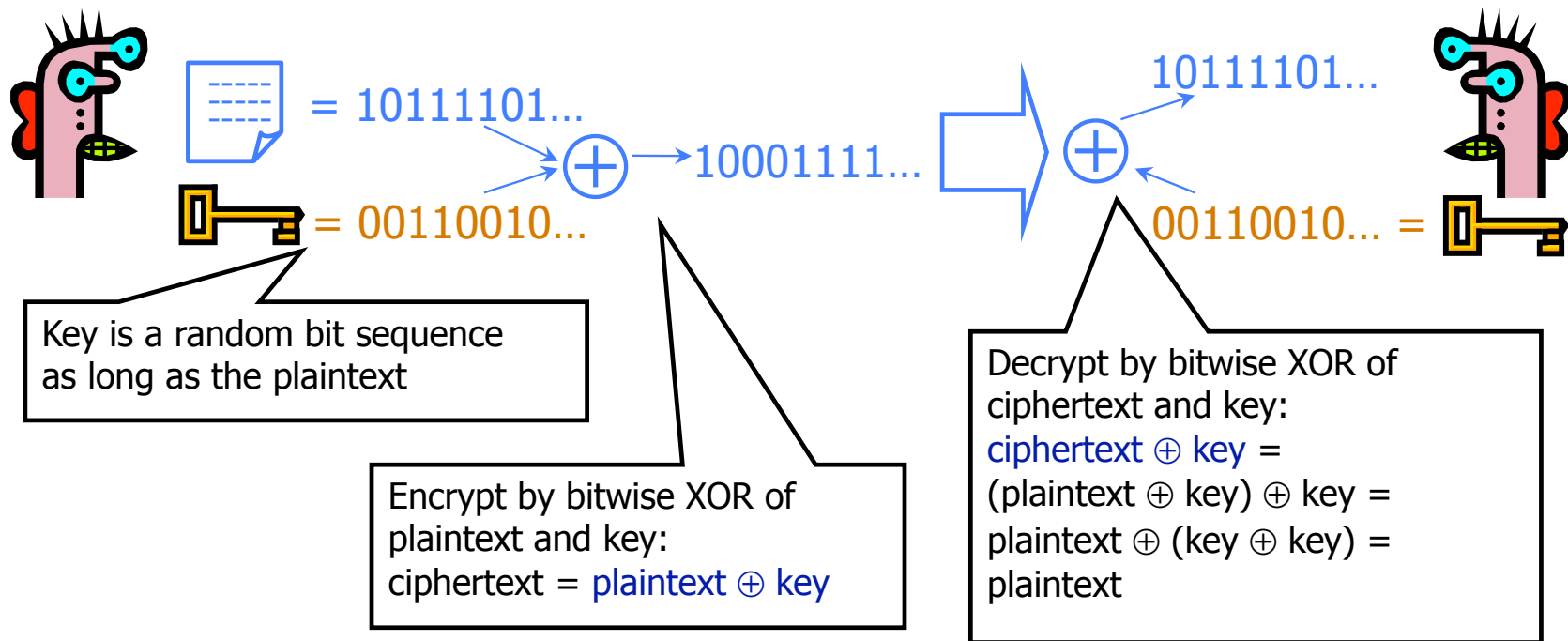
## ◆ Easy to compute

- Encryption and decryption are the same operation
- Bitwise XOR is very cheap to compute

## ◆ As secure as theoretically possible

- Given a ciphertext, all plaintexts are equally likely, regardless of attacker's computational resources
- ...as long as the key sequence is truly random
  - True randomness is expensive to obtain in large quantities
- ...as long as each key is same length as plaintext
  - But how does the sender communicate the key to receiver?

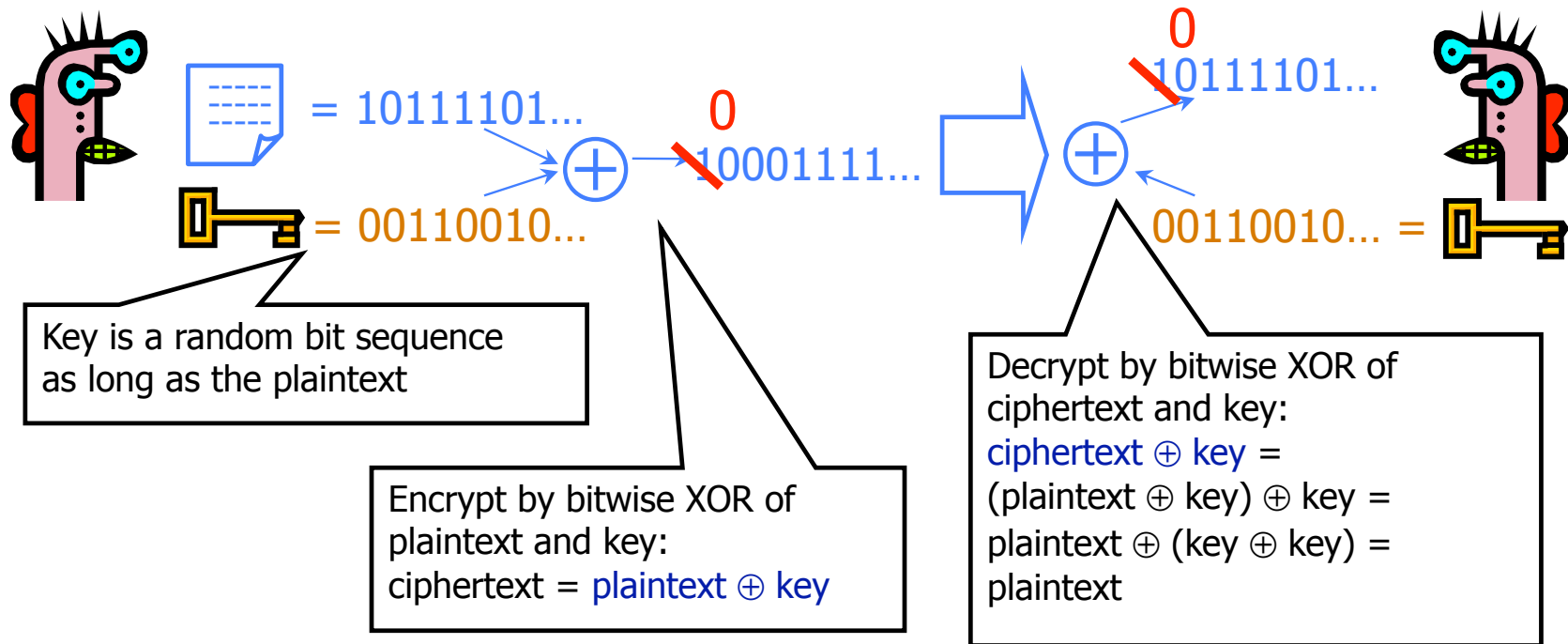
# Disadvantages



Disadvantage #1: Keys as long as messages.  
Impractical in most scenarios  
Still used by intelligence communities



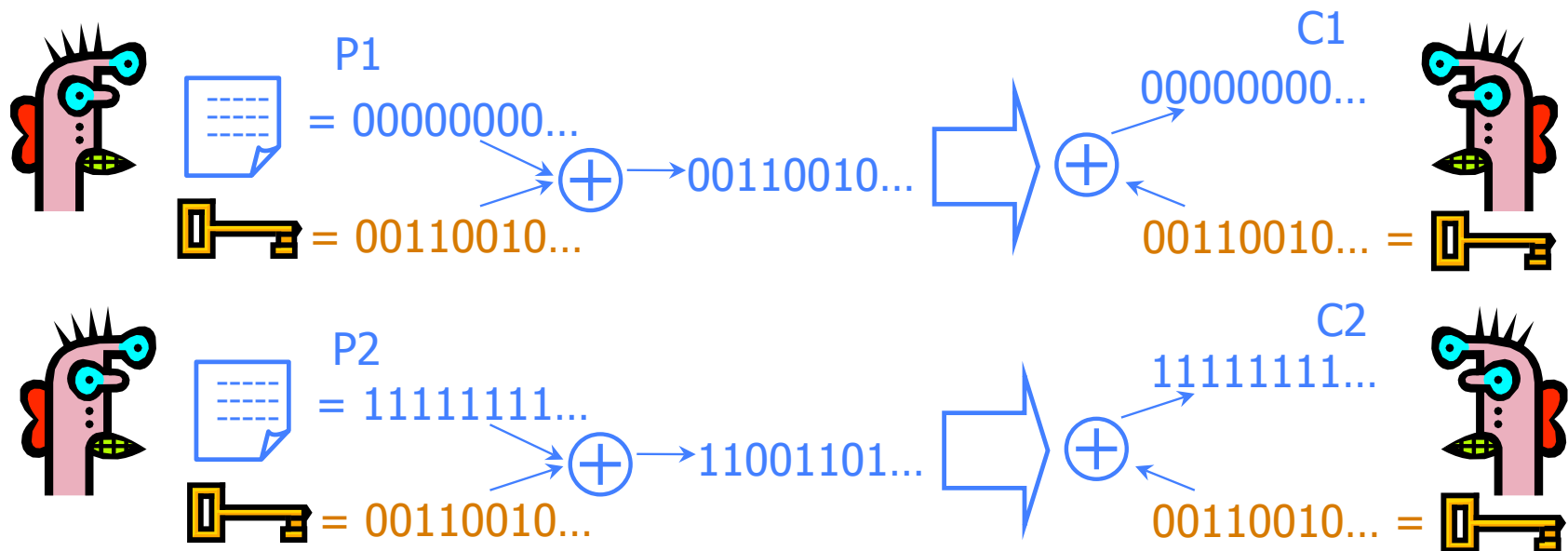
# Disadvantages



Disadvantage #2: No integrity protection

# Disadvantages

Disadvantage #3: Keys cannot be reused



Learn relationship between plaintexts:

$$C1 \oplus C2 = (P1 \oplus K) \oplus (P2 \oplus K) = (P1 \oplus P2) \oplus (K \oplus K) = P1 \oplus P2$$

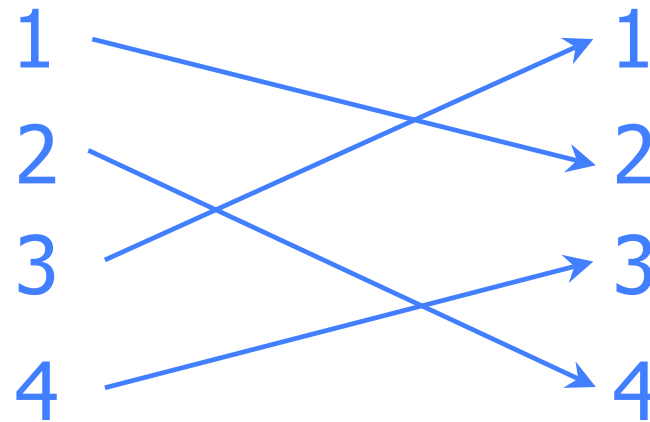
# Reducing Keysize

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- ◆ What do we do when we can't pre-share huge keys?
  - When OTP is unrealistic
- ◆ We use special cryptographic primitives
  - Single key can be reused (with some restrictions)
  - But no longer provable secure (in the sense of the OTP)
- ◆ Examples: Block ciphers, stream ciphers

# Background: Permutation

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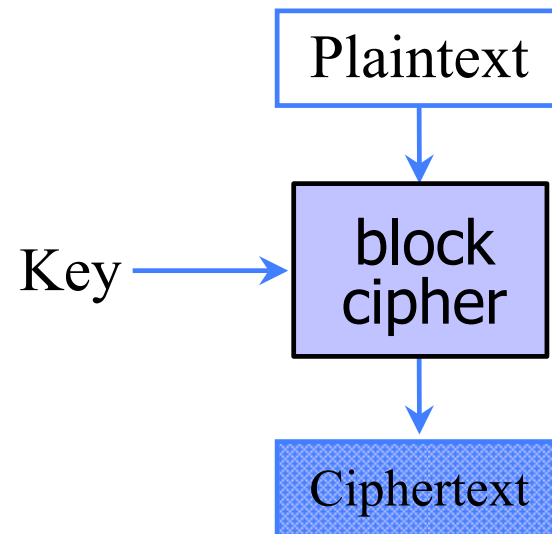
CODE becomes DCEO

- ◆ For N-bit input,  $N!$  possible permutations
- ◆ Idea: split plaintext into blocks; for each block use **secret key** to pick a permutation
  - Without the key, permutation should “look random”

# Block Ciphers

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- ◆ Operates on a single chunk (“block”) of plaintext
  - For example, 64 bits for DES, 128 bits for AES
  - Same key is reused for each block (can use short keys)

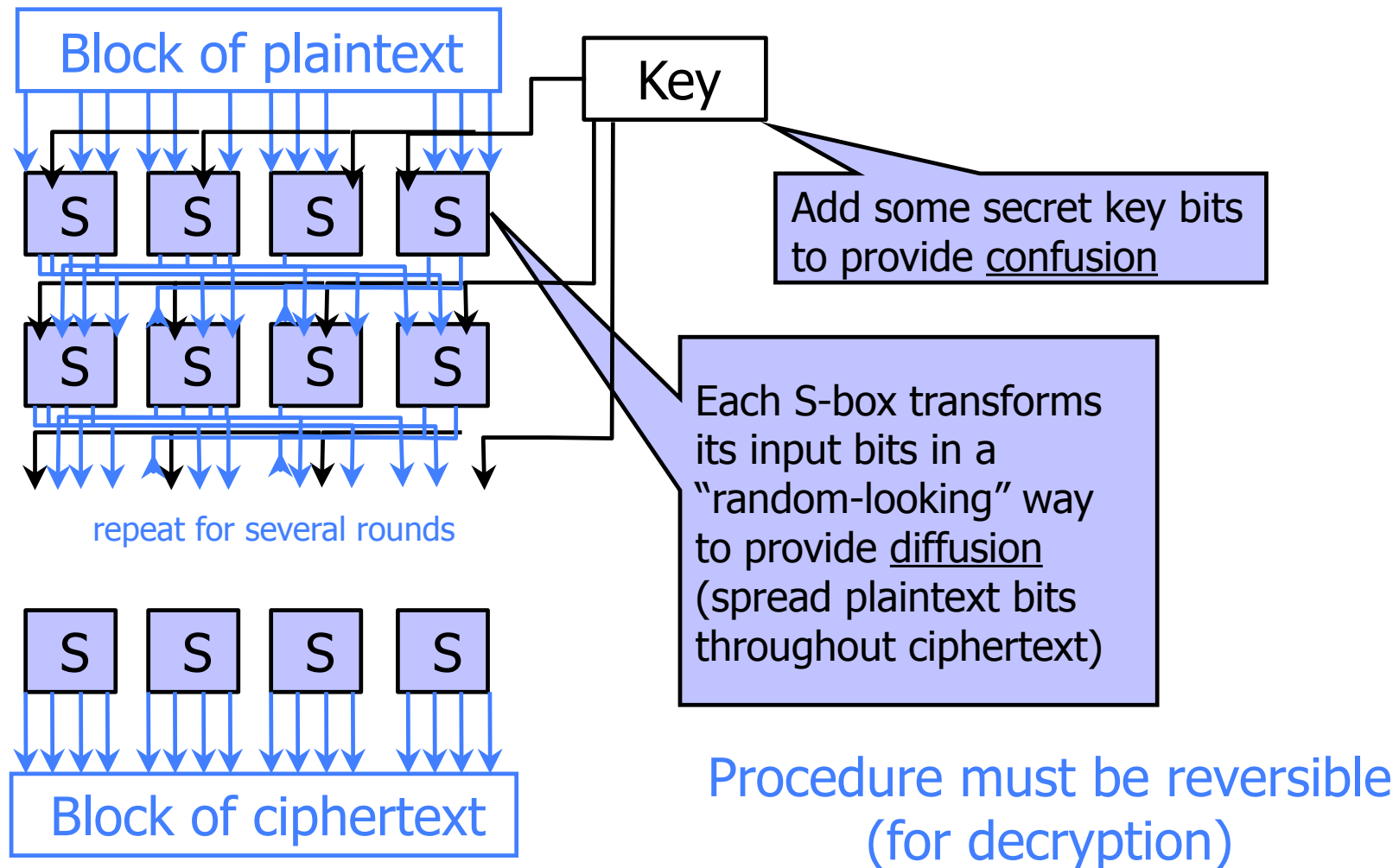


# Block Cipher Security

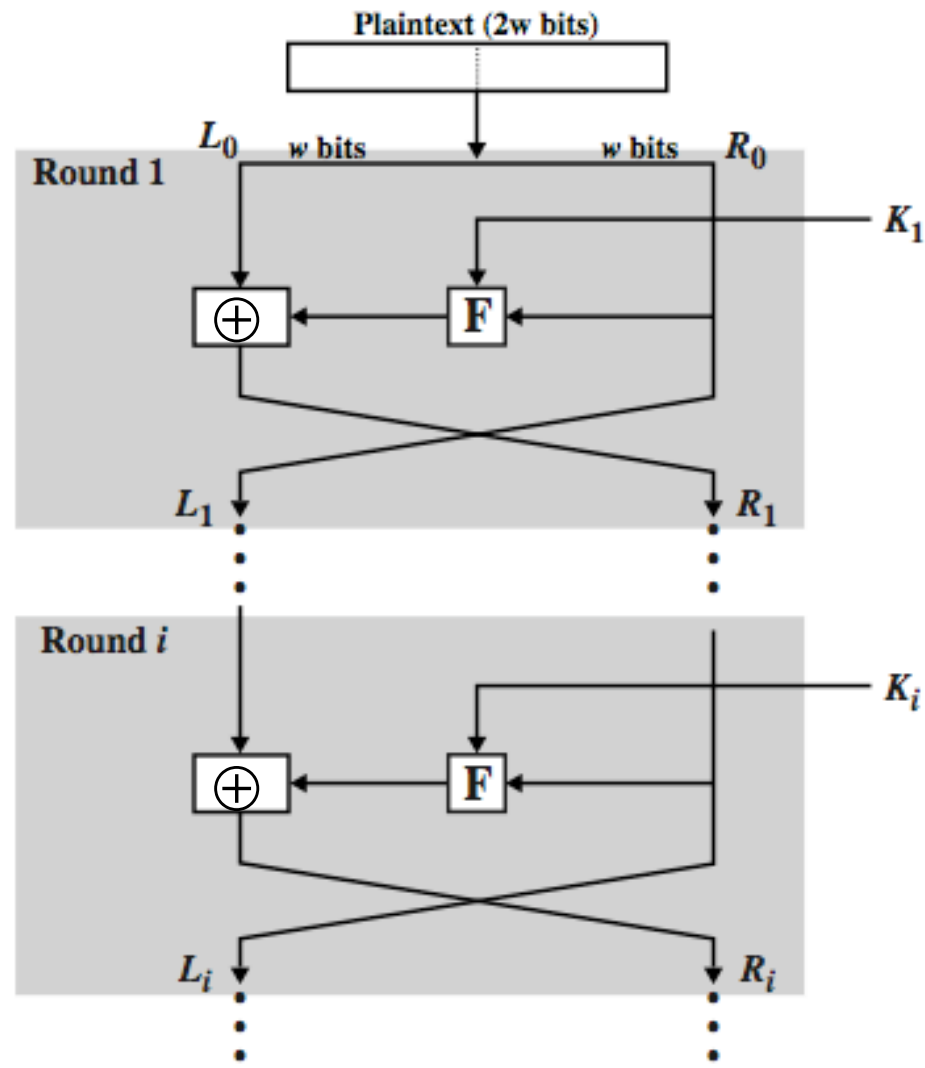
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- ◆ Result should look like a random permutation
  - “As if” plaintext bits were randomly shuffled
- ◆ Only computational guarantee of secrecy
  - Not impossible to break, just very expensive
    - If there is no efficient algorithm (unproven assumption!), then can only break by brute-force, try-every-possible-key search
  - Time and cost of breaking the cipher exceed the value and/or useful lifetime of protected information

# Block Cipher Operation (Simplified)



# Feistel Structure (Stallings Fig 2.2)





# DES

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## ◆ Feistel structure

- “Ladder” structure: split input in half, put one half through the round and XOR with the other half
- After 3 random rounds, ciphertext indistinguishable from a random permutation if internal F function is a pseudorandom function (Luby & Rackoff)

## ◆ DES: Data Encryption Standard

- Feistel structure
- Invented by IBM, issued as federal standard in 1977
- 64-bit blocks, 56-bit key + 8 bits for parity

# DES and 56 bit keys (Stallings Tab 2.2)

◆ 56 bit keys are quite short

Key Size (bits)	Number of Alternative Keys	Time required at 1 encryption/ $\mu$ s	Time required at $10^6$ encryptions/ $\mu$ s
32	$2^{32} = 4.3 \times 10^9$	$2^{31} \mu s = 35.8$ minutes	2.15 milliseconds
56	$2^{56} = 7.2 \times 10^{16}$	$2^{55} \mu s = 1142$ years	10.01 hours
128	$2^{128} = 3.4 \times 10^{38}$	$2^{127} \mu s = 5.4 \times 10^{24}$ years	$5.4 \times 10^{18}$ years
168	$2^{168} = 3.7 \times 10^{50}$	$2^{167} \mu s = 5.9 \times 10^{36}$ years	$5.9 \times 10^{30}$ years
26 characters (permutation)	$26! = 4 \times 10^{26}$	$2 \times 10^{26} \mu s = 6.4 \times 10^{12}$ years	$6.4 \times 10^6$ years

◆ 1999: EFF DES Crack + distributed machines

- < 24 hours to find DES key

◆ DES ---> 3DES

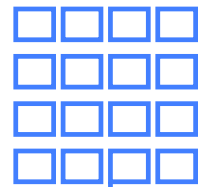
- 3DES: DES + inverse DES + DES (with 2 or 3 diff keys)

# Advanced Encryption Standard (AES)

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- ◆ New federal standard as of 2001
- ◆ Based on the **Rijndael** algorithm
- ◆ 128-bit blocks, keys can be 128, 192 or 256 bits
- ◆ Unlike DES, does not use Feistel structure
  - The entire block is processed during each round
- ◆ Design uses some very nice mathematics

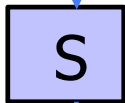
# Basic Structure of Rijndael



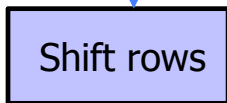
128-bit plaintext  
(arranged as 4x4 array of 8-bit bytes)



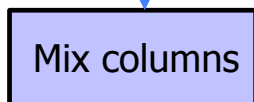
128-bit key



byte substitution



shift array rows  
(1<sup>st</sup> unchanged, 2<sup>nd</sup> left by 1, 3<sup>rd</sup> left by 2, 4<sup>th</sup> left by 3)



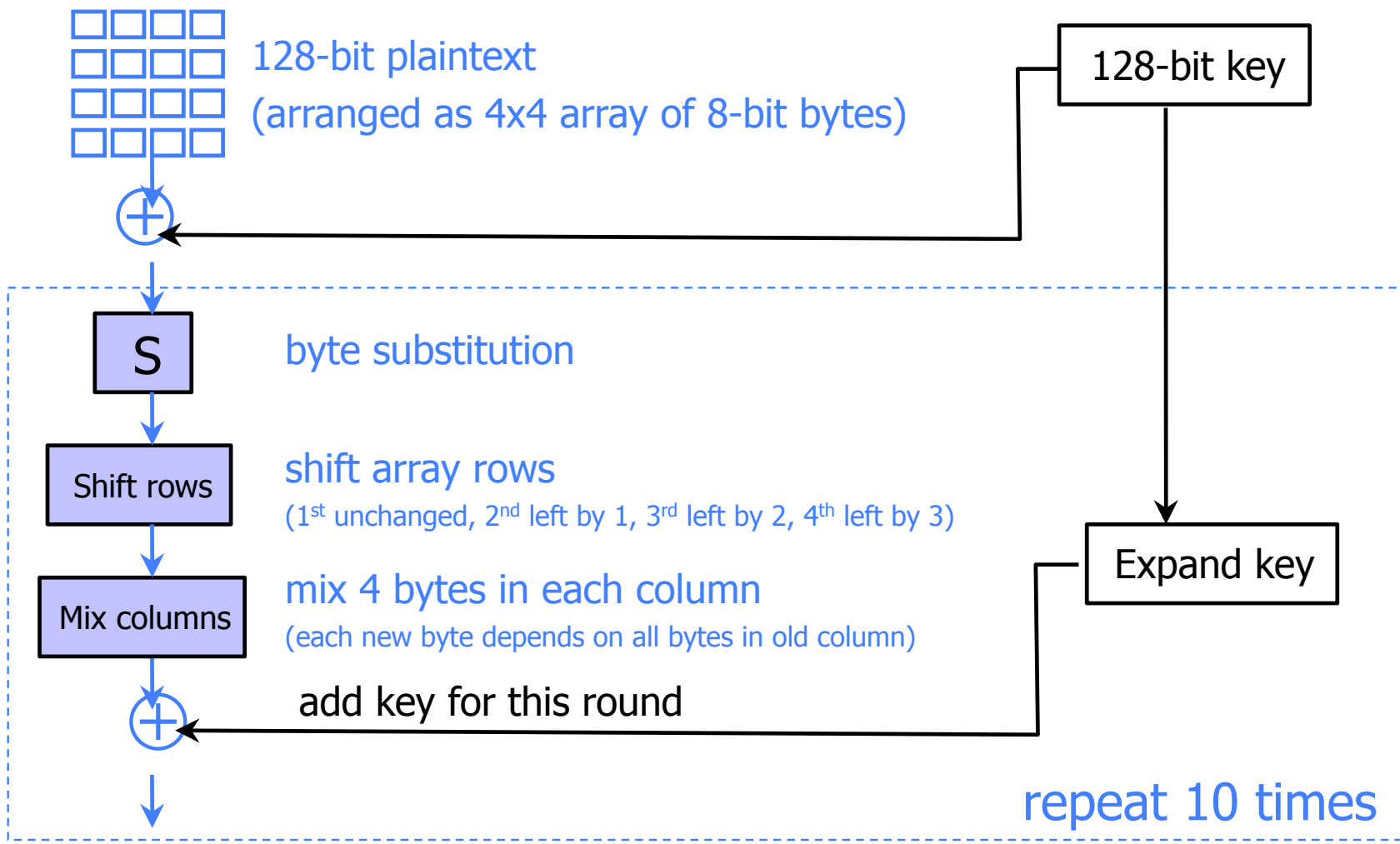
mix 4 bytes in each column  
(each new byte depends on all bytes in old column)



add key for this round

Expand key

repeat 10 times



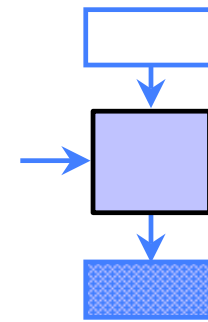
# Encrypting a Large Message

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- ◆ So, we've got a good block cipher, but our plaintext is larger than 128-bit block size

- ◆ **Electronic Code Book (ECB) mode**

- Split plaintext into blocks, encrypt each one separately using the block cipher



- ◆ **Cipher Block Chaining (CBC) mode**

- Split plaintext into blocks, XOR each block with the result of encrypting previous blocks

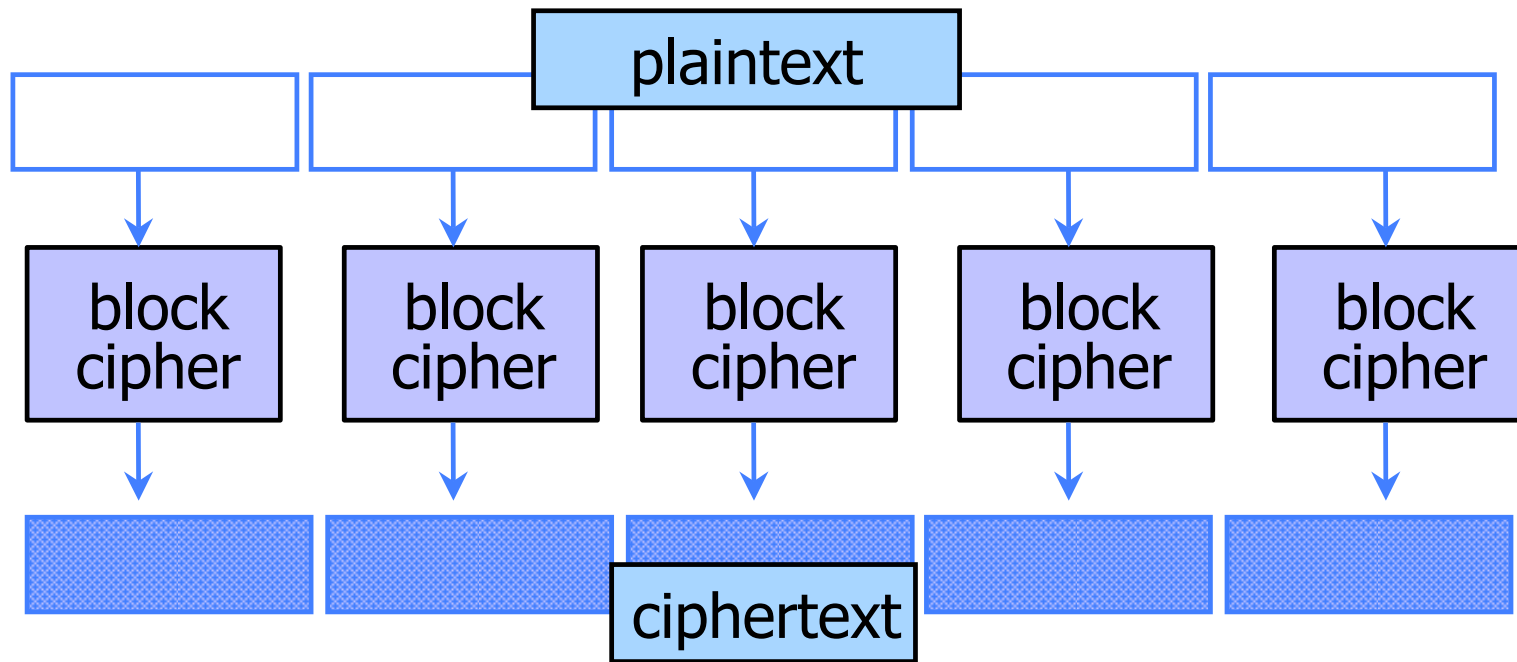
- ◆ **Counter (CTR) mode**

- Use block cipher to generate keystream, like a stream cipher

- ◆ ...

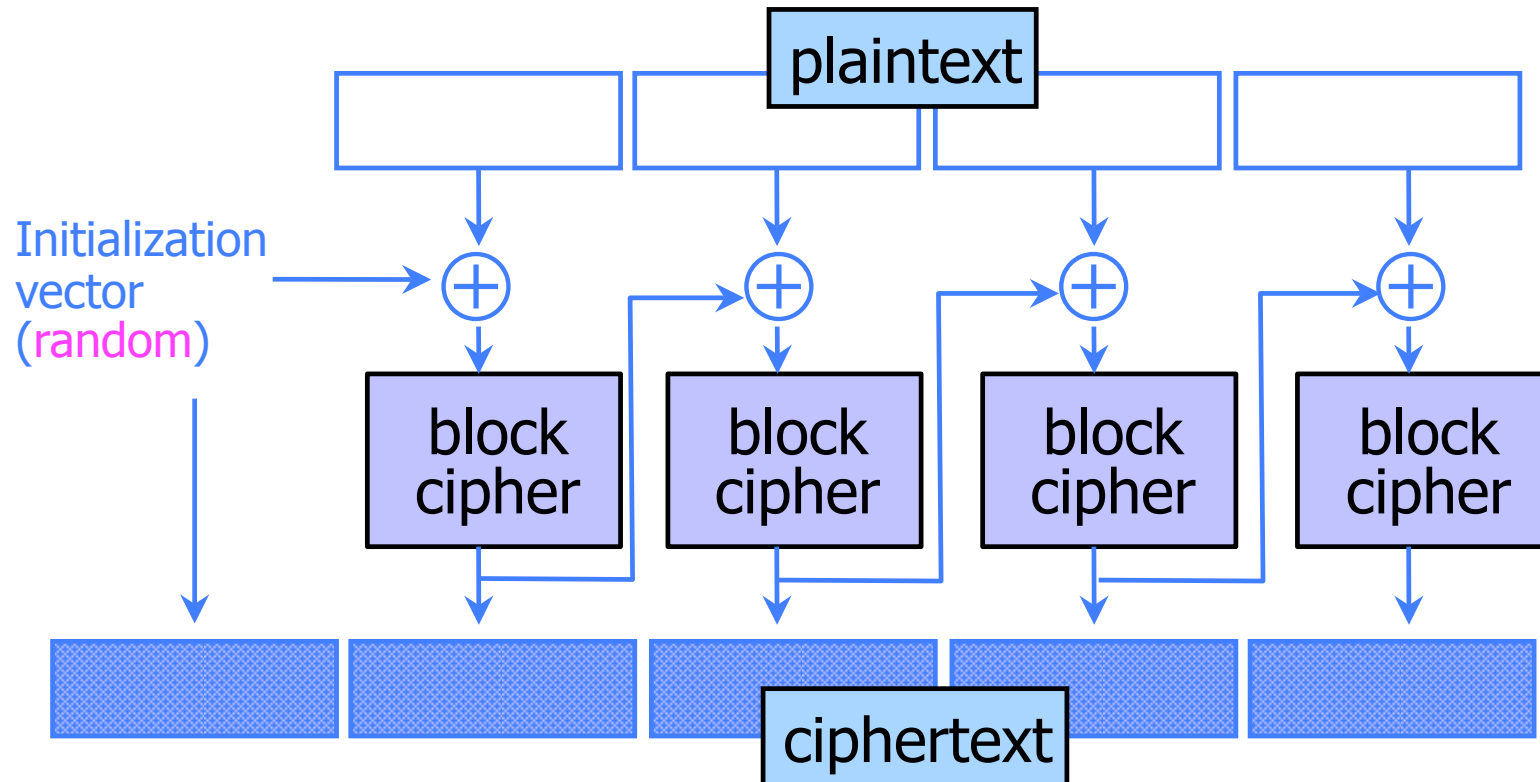
# ECB Mode

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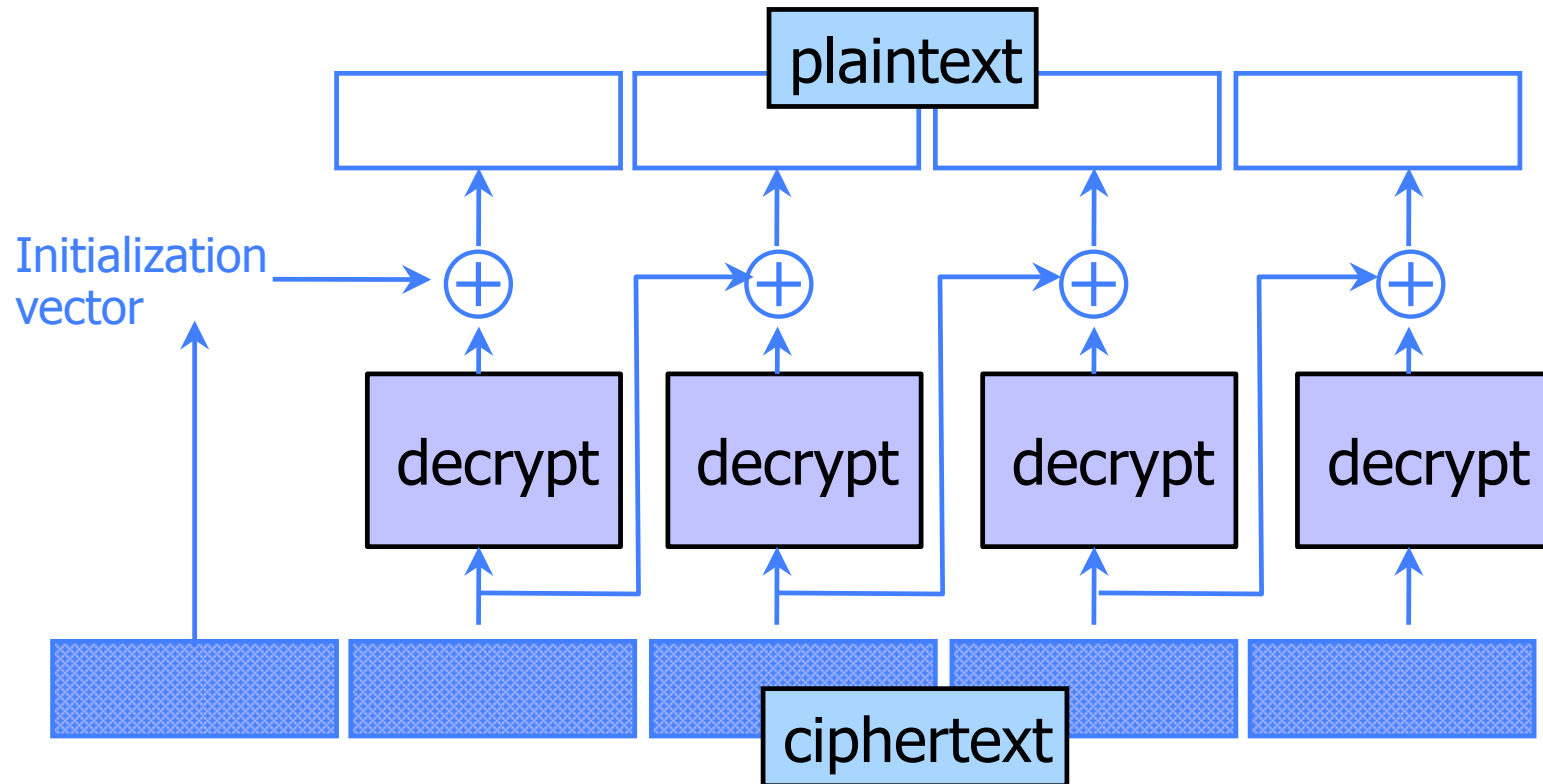
- ◆ Identical blocks of plaintext produce identical blocks of ciphertext
- ◆ No integrity checks: can mix and match blocks

# CBC Mode: Encryption



- ◆ Identical blocks of plaintext encrypted differently
- ◆ Last cipherblock depends on entire plaintext
  - Still does not guarantee integrity

# CBC Mode: Decryption

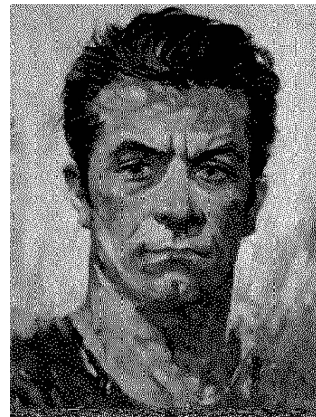




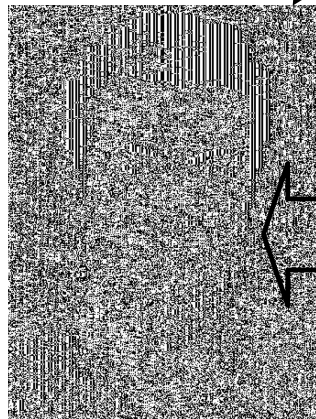
# ECB vs. CBC

[Picture due to Bart Preneel]

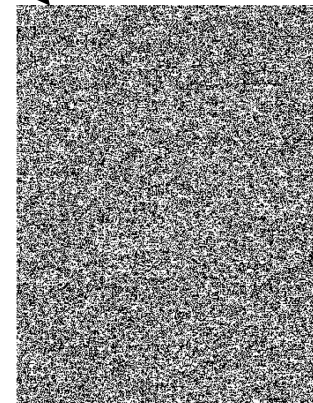
AES in ECB mode



AES in CBC mode

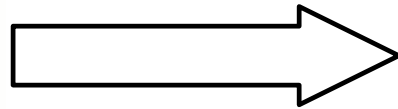
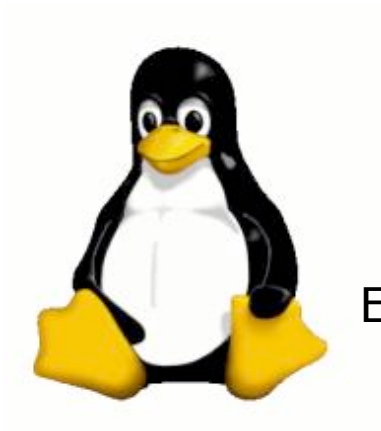


Similar plaintext blocks produce similar ciphertext blocks (not good!)

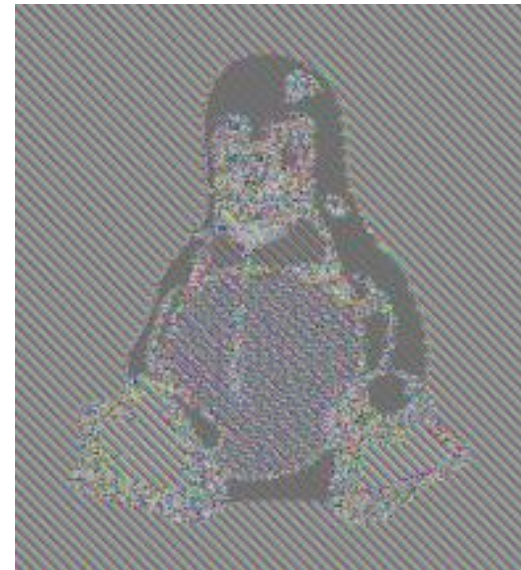


# Information Leakage in ECB Mode

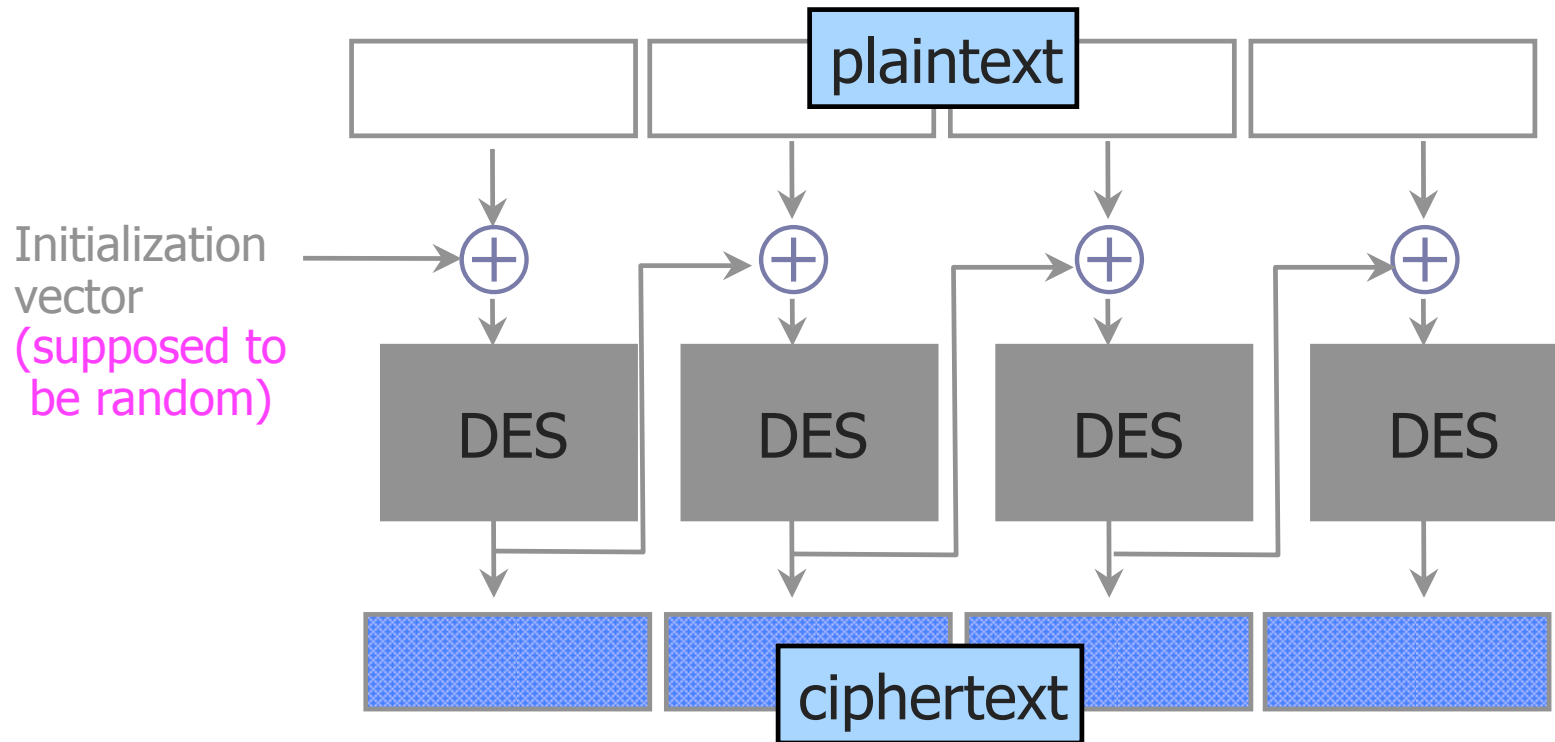
[Wikipedia]



Encrypt in ECB mode



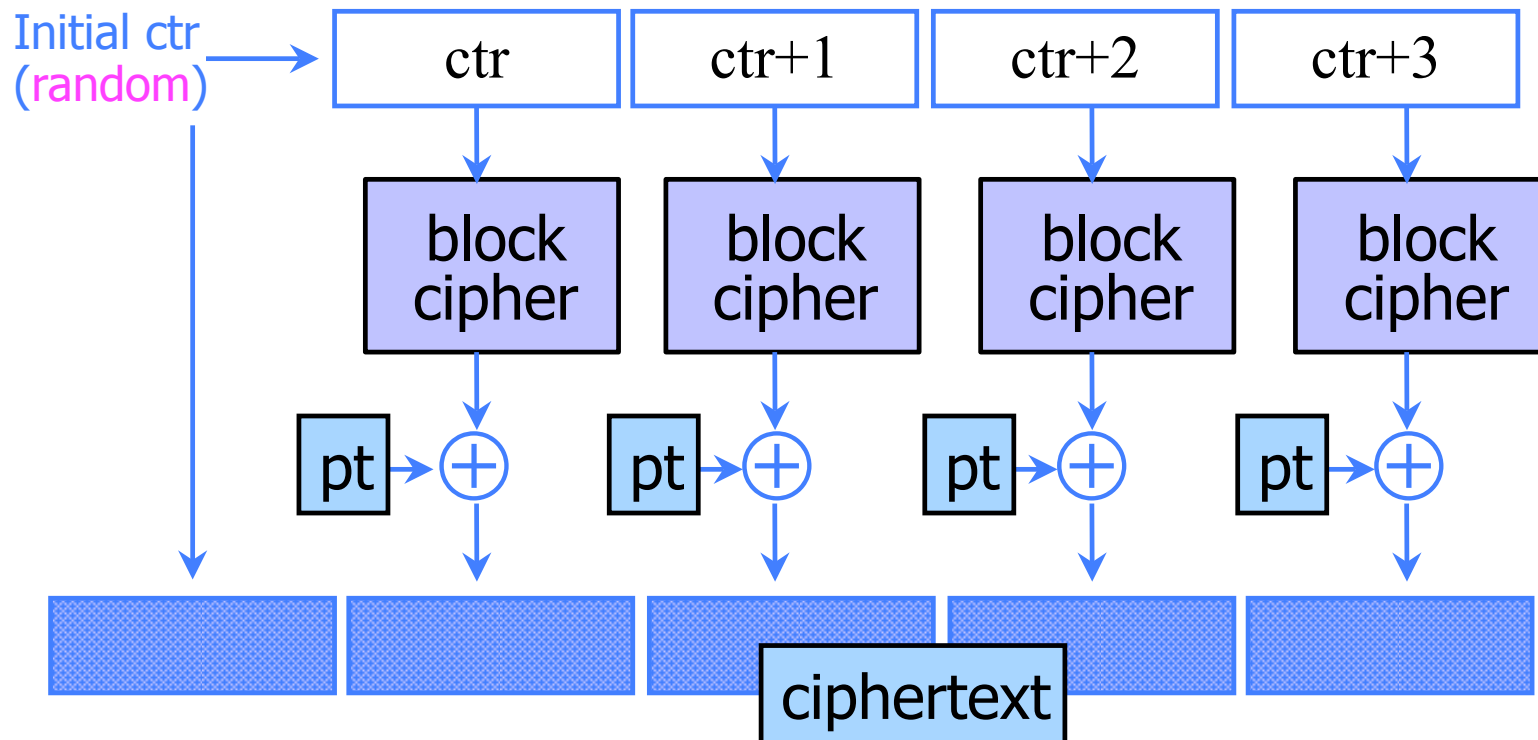
# CBC and Electronic Voting



Found in the source code for Diebold voting machines:

```
DesCBCEncrypt((des_c_block*)tmp, (des_c_block*)record.m_Data,  
totalSize, DESKEY, NULL, DES_ENCRYPT)
```

# CTR Mode: Encryption



- ◆ Identical blocks of plaintext encrypted differently
- ◆ Still does not guarantee integrity
- ◆ Fragile if ctr repeats

# CTR Mode: Decryption

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