

CSE-490DF Robotics Capstone

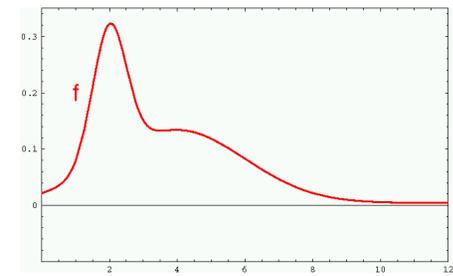
Mobile Robot Localization

Particle filters

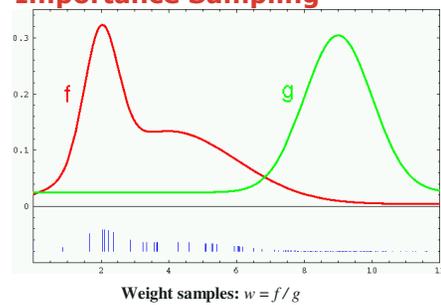
Particle Filters

- Represent belief by random **samples**
- Estimation of **non-Gaussian, nonlinear** processes
- Monte Carlo filter, Survival of the fittest, Condensation, Bootstrap filter, Particle filter
- Filtering: [Rubin, 88], [Gordon et al., 93], [Kitagawa 96]
- Computer vision: [Isard and Blake 96, 98]
- Dynamic Bayesian Networks: [Kanazawa et al., 95]d

Sample-based Density Representation



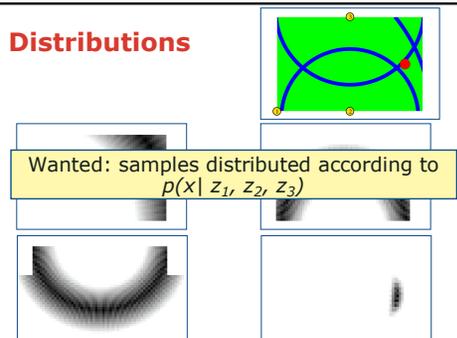
Importance Sampling



Importance Sampling with Resampling: Landmark Detection Example

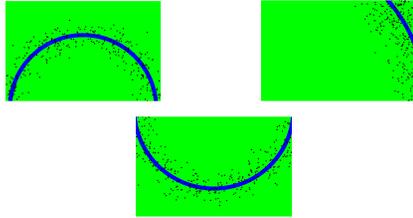


Distributions



This is Easy!

We can draw samples from $p(x|z_i)$ by adding noise to the detection parameters.



Importance Sampling with Resampling

$$\text{Target distribution } f : p(x|z_1, z_2, \dots, z_n) = \frac{\prod_{k=1}^n p(z_k|x) p(x)}{p(z_1, z_2, \dots, z_n)}$$

$$\text{Sampling distribution } g : p(x|z_i) = \frac{p(z_i|x)p(x)}{p(z_i)}$$

$$\text{Importance weights } w : \frac{f}{g} = \frac{p(x|z_1, z_2, \dots, z_n)}{p(x|z_i)} = \frac{p(z_i) \prod_{k \neq i} p(z_k|x)}{p(z_1, z_2, \dots, z_n)}$$

Weighted samples

After resampling

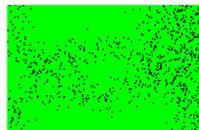
Importance Sampling with Resampling

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Importance Sampling with Resampling

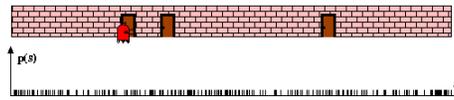


Weighted samples



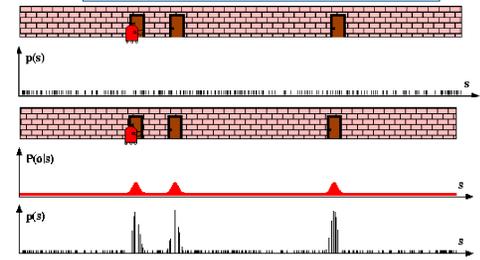
After resampling

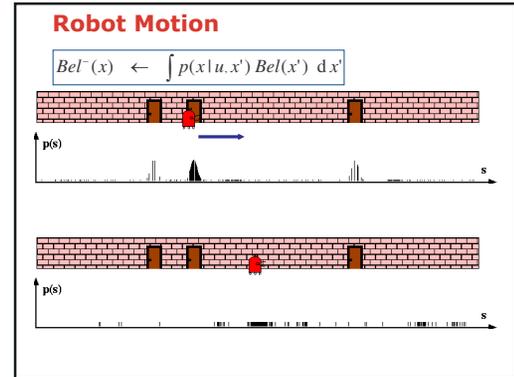
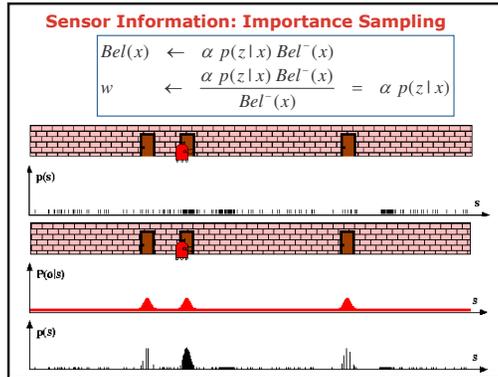
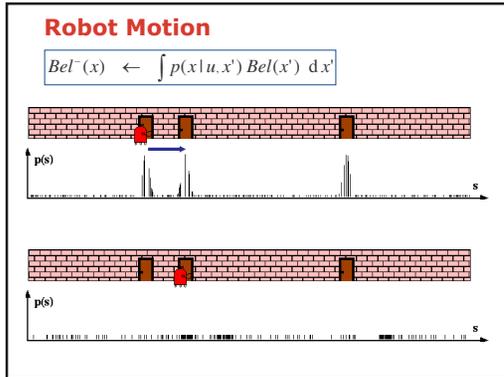
Particle Filters



Sensor Information: Importance Sampling

$$\begin{aligned} Bel(x) &\leftarrow \alpha p(z|x) Bel^-(x) \\ w &\leftarrow \frac{\alpha p(z|x) Bel^-(x)}{Bel^-(x)} = \alpha p(z|x) \end{aligned}$$





- ### Particle Filter Algorithm
1. Algorithm **particle_filter**(S_{t-1}, u_{t-1}, z_t):
 2. $S_t = \emptyset, \eta = 0$
 3. **For** $i = 1 \dots n$ *Generate new samples*
 4. Sample index $j(i)$ from the discrete distribution given by w_{t-1}
 5. Sample x_t^i from $p(x_t | x_{t-1}, u_{t-1})$ using $x_{t-1}^{j(i)}$ and u_{t-1}
 6. $w_t^i = p(z_t | x_t^i)$ *Compute importance weight*
 7. $\eta = \eta + w_t^i$ *Update normalization factor*
 8. $S_t = S_t \cup \{ \langle x_t^i, w_t^i \rangle \}$ *Insert*
 9. **For** $i = 1 \dots n$
 10. $w_t^i = w_t^i / \eta$ *Normalize weights*

Particle Filter Algorithm

$$Bel(x_t) = \eta p(z_t | x_t) \int p(x_t | x_{t-1}, u_{t-1}) Bel(x_{t-1}) dx_{t-1}$$

\swarrow draw x_{t-1}^j from $Bel(x_{t-1})$
 \searrow draw x_t^i from $p(x_t | x_{t-1}^j, u_{t-1})$
 \leftarrow Importance factor for x_t^i :

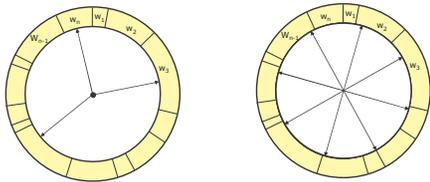
$$w_t^i = \frac{\text{target distribution}}{\text{proposal distribution}}$$

$$= \frac{\eta p(z_t | x_t^i) p(x_t | x_{t-1}^j, u_{t-1}) Bel(x_{t-1}^j)}{p(x_t | x_{t-1}^j, u_{t-1}) Bel(x_{t-1}^j)}$$

$$\propto p(z_t | x_t^i)$$

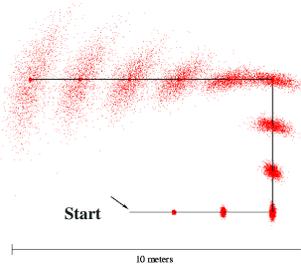
- ### Resampling
- **Given**: Set S of weighted samples.
 - **Wanted**: Random sample, where the probability of drawing x_j is given by w_j .
 - Typically done n times with replacement to generate new sample set S' .

Resampling

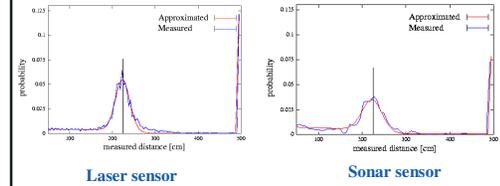


- Roulette wheel
- Binary search, $\log n$
- Stochastic universal sampling
- Systematic resampling
- Linear time complexity
- Easy to implement, low variance

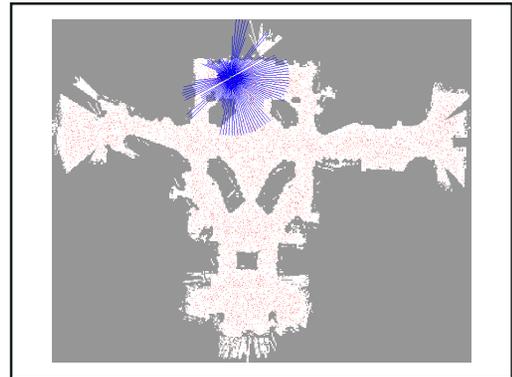
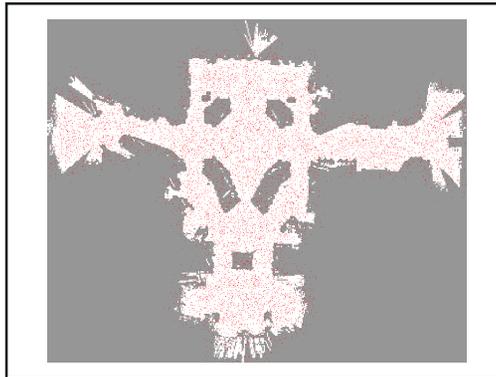
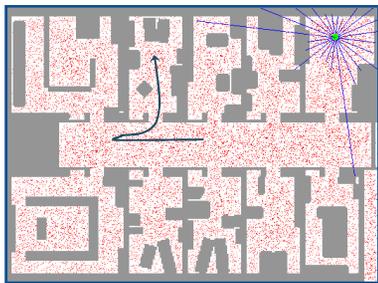
Motion Model Reminder

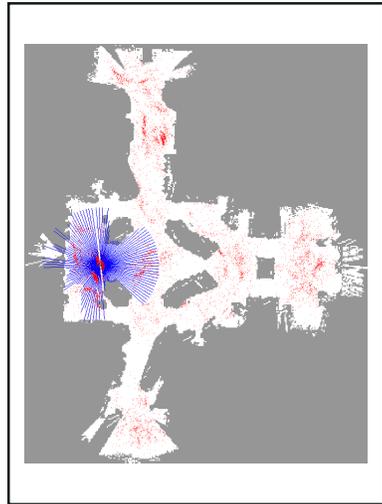
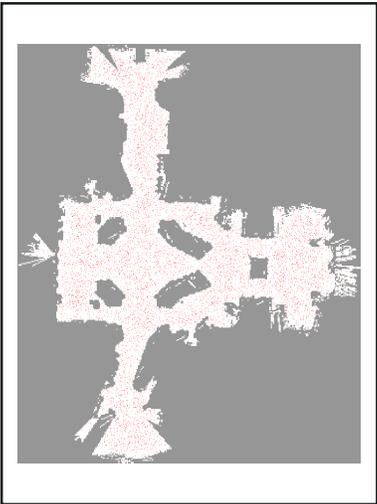
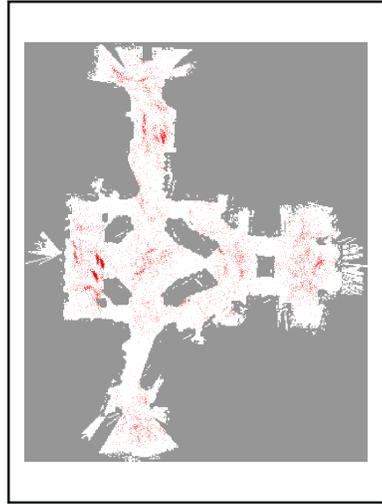
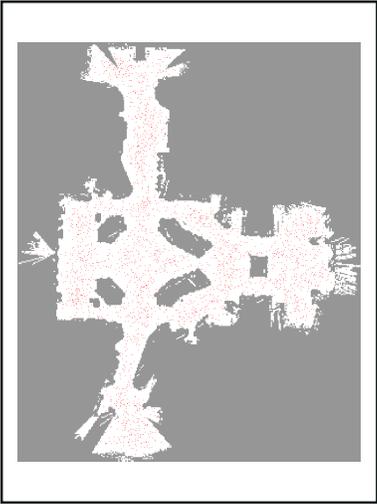
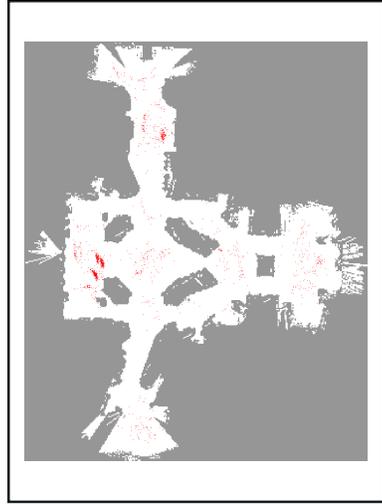
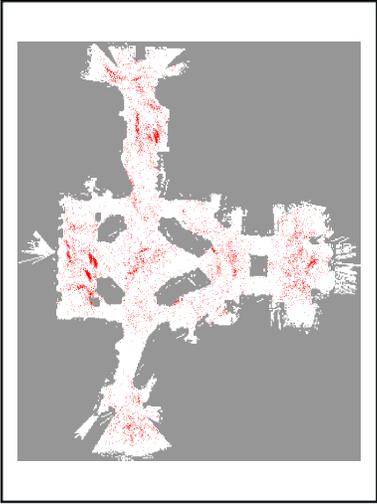


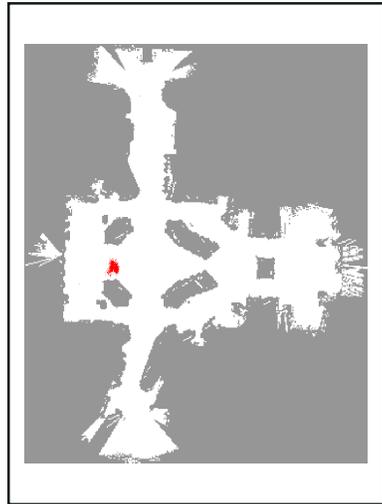
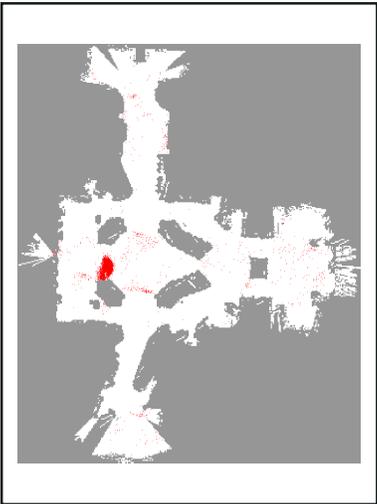
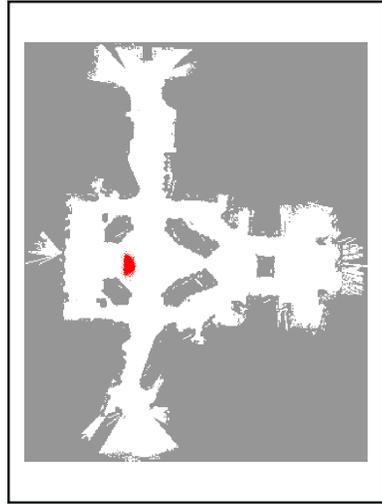
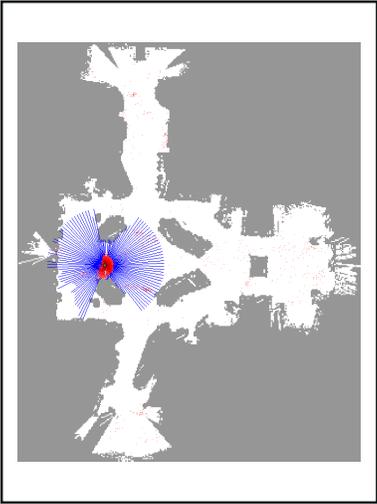
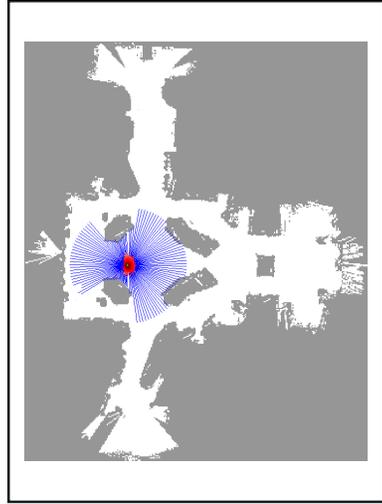
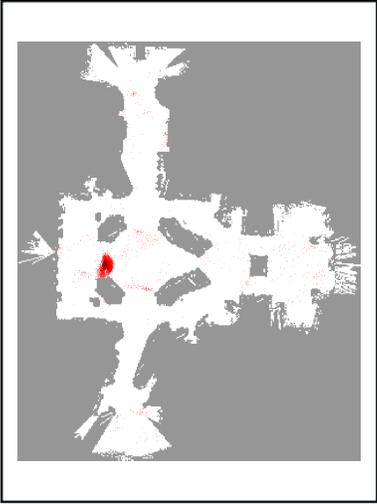
Proximity Sensor Model Reminder

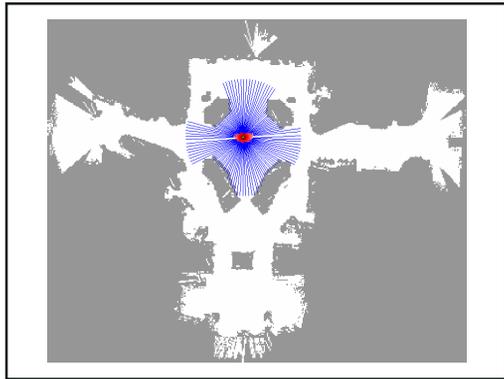
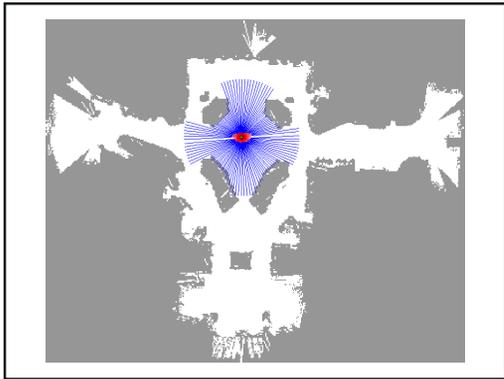
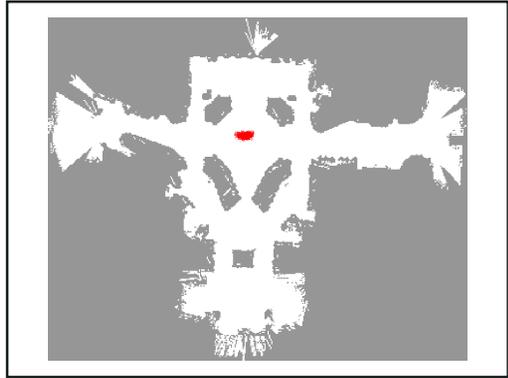
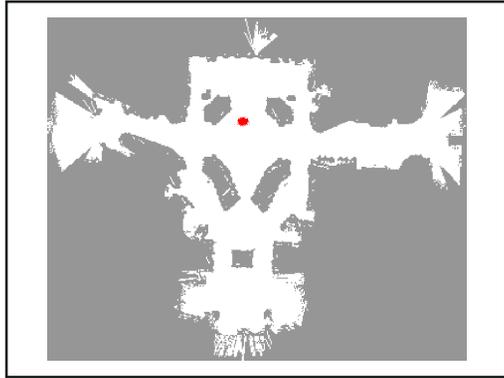
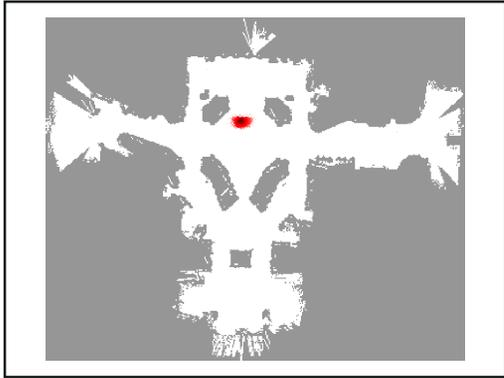


Sample-based Localization (sonar)







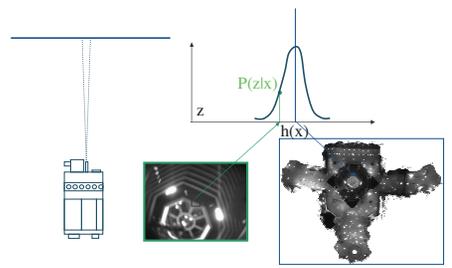


Using Ceiling Maps for Localization

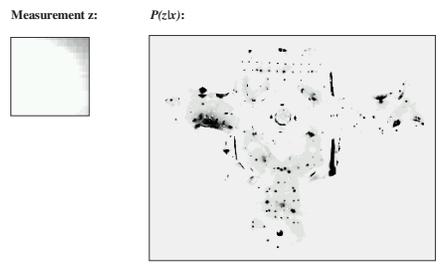
A photograph of a robot in a crowd of people. A red arrow points from the robot to a corresponding ceiling map, which is a 2D occupancy grid map of the robot's environment, rendered in a dark, textured style.

[Dellaert et al. 99]

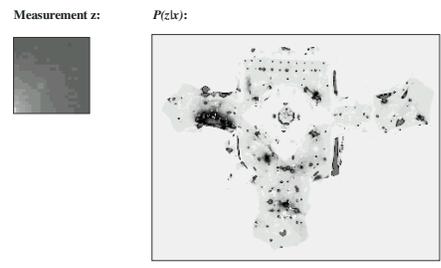
Vision-based Localization



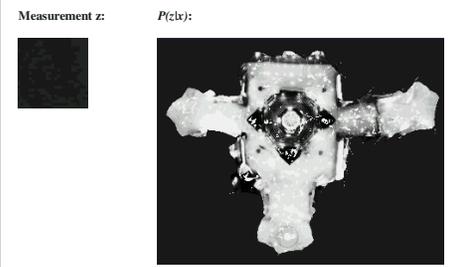
Under a Light



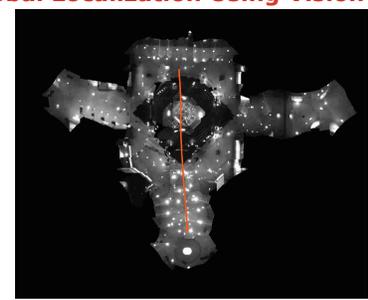
Next to a Light



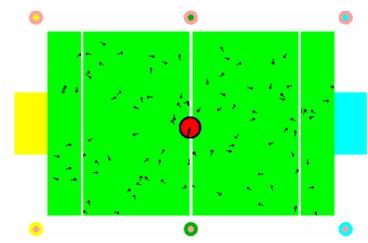
Elsewhere

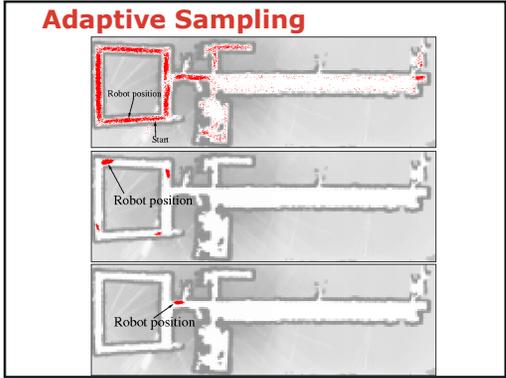


Global Localization Using Vision



Localization for AIBO robots





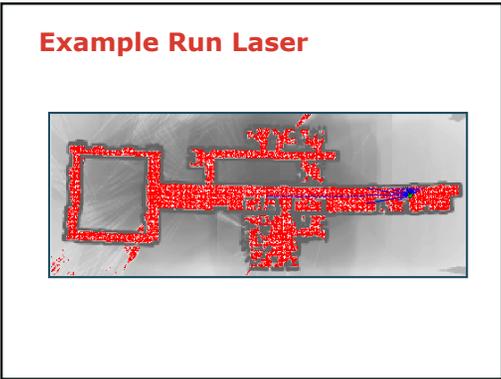
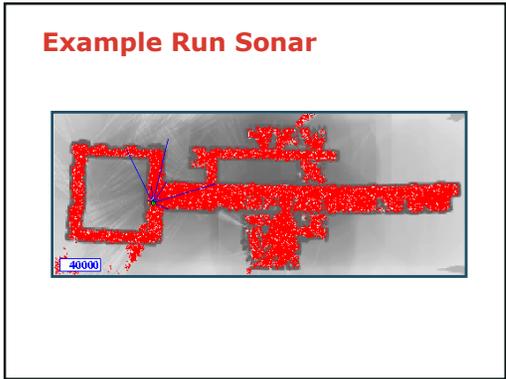
KLD-sampling

- Idea:**
 - Assume we know the true belief.
 - Represent this belief as a multinomial distribution.
 - Determine number of samples such that we can guarantee that, with probability $(1 - \delta)$, the KL-distance between the true posterior and the sample-based approximation is less than ϵ .
- Observation:**
 - For fixed δ and ϵ , number of samples only depends on number k of bins with support:

$$n = \frac{1}{2\epsilon} \chi^2(k-1, 1-\delta) \cong \frac{k-1}{2\epsilon} \left\{ 1 - \frac{2}{9(k-1)} + \sqrt{\frac{2}{9(k-1)} z_{1-\delta}} \right\}^3$$

Adaptive Particle Filter Algorithm

- Algorithm `adaptive_particle_filter`($S_{t-1}, u_{t-1}, z_t, \Delta, \epsilon, \delta$):
- $S_t = \emptyset, \alpha = 0, n = 0, k = 0, b = \emptyset$
- Do** *Generate new samples*
- Sample index $j(n)$ from the discrete distribution given by w_{t-1}
- Sample x_t^j from $p(x_t | x_{t-1}, u_{t-1})$ using $x_{t-1}^{j(n)}$ and u_{t-1}
- $w_t^j = p(z_t | x_t^j)$ *Compute importance weight*
- $\eta = \eta + w_t^j$ *Update normalization factor*
- $S_t = S_t \cup \{x_t^j, w_t^j\}$ *Insert*
- If** (x_t^j falls into an empty bin b) *Update bins with support*
- $k = k + 1, b = \text{non-empty}$
- $n = n + 1$
- While** ($n < \frac{1}{2\epsilon} \chi^2(k-1, 1-\delta)$)
- For** $i = 1 \dots n$
- $w_i^j = w_i^j / \eta$ *Normalize weights*



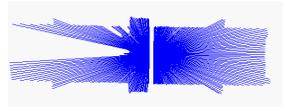
Localization Algorithms - Comparison

	Kalman filter	Multi-hypothesis tracking	Topological maps	Grid-based (fixed/variable)	Particle filter
Sensors	Gaussian	Gaussian	Features	Non-Gaussian	Non-Gaussian
Posterior	Gaussian	Multi-modal	Piecewise constant	Piecewise constant	Samples
Efficiency (memory)	++	++	++	-/+	+ / ++
Efficiency (time)	++	++	++	0 / +	+ / ++
Implementation	+	o	+	+ / o	++
Accuracy	++	++	-	+ / ++	++
Robustness	-	+	+	++	+ / ++
Global localization	No	Yes	Yes	Yes	Yes

Other Tracking Applications

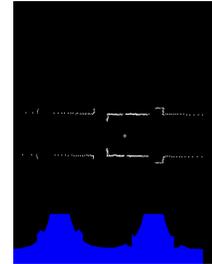
People Tracking

- **Key questions**
 - How many people are there?
 - Where do they go?
- **Requirements**
 - Real time
 - No model of the environment
 - Robot in motion



[Schulz et al. 2001]

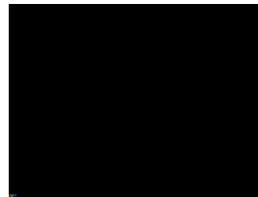
Example Run



Tracking with a Moving Robot



Condensation



[Isard et al. 96]

Mixed-State Condensation



[Isard et al. 96]

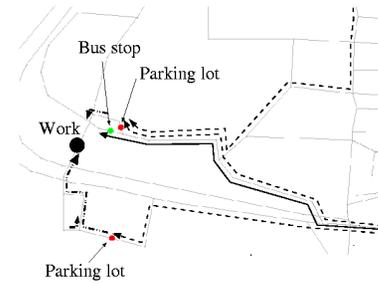
GPS Tracking



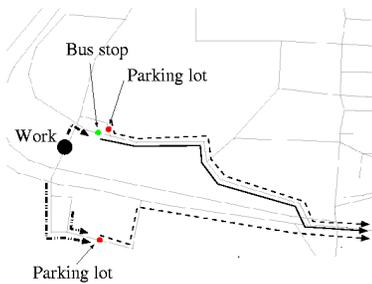
Learned Significant Locations



Path Conditioned on UW



Path Conditioned on Home



Goal and Path Prediction



Normal vs. Abnormal Activity



Normal vs. Abnormal Activity

