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[These slides were adapted from Dan Klein and Pieter Abbeel for CS188 Intro to AI at UC Berkeley. All CS188 materials are available at http://ai.berkeley.edu.]

Reinforcement Learning





Reinforcement Learning



- Basic idea:
 - Receive feedback in the form of rewards
 - Agent's utility is defined by the reward function
 - Must (learn to) act so as to maximize expected rewards
 - All learning is based on observed samples of outcomes!



Initial



A Learning Trial



After Learning [1K Trials]

[Kohl and Stone, ICRA 2004]



Initial

[Kohl and Stone, ICRA 2004]

[Video: AIBO WALK – initial]



Training

[Kohl and Stone, ICRA 2004]

[Video: AIBO WALK – training]



Finished

[Kohl and Stone, ICRA 2004]

[Video: AIBO WALK – finished]

Example: Sidewinding



[Andrew Ng]

[Video: SNAKE – climbStep+sidewinding]

Example: Toddler Robot



[Tedrake, Zhang and Seung, 2005]

[Video: TODDLER – 40s]

The Crawler!



[Demo: Crawler Bot (L10D1)] [You, in Project 3]

Video of Demo Crawler Bot



Reinforcement Learning

- Still assume a Markov decision process (MDP):
 - A set of states $s \in S$
 - A set of actions (per state) A
 - A model T(s,a,s')
 - A reward function R(s,a,s')
- Still looking for a policy $\pi(s)$







- New twist: don't know T or R
 - I.e. we don't know which states are good or what the actions do
 - Must actually try actions and states out to learn

Offline (MDPs) vs. Online (RL)



Offline Solution

Online Learning

Model-Based Learning



Model-Based Learning

- Model-Based Idea:
 - Learn an approximate model based on experiences
 - Solve for values as if the learned model were correct
- Step 1: Learn empirical MDP model
 - Count outcomes s' for each s, a
 - Normalize to give an estimate of $\hat{T}(s, a, s')$
 - Discover each $\widehat{R}(s, a, s')$ when we experience (s, a, s')
- Step 2: Solve the learned MDP
 - For example, use value iteration, as before





Example: Model-Based Learning



Example: Expected Age

Goal: Compute expected age of CSE 473 students



Without P(A), instead collect samples $[a_1, a_2, ..., a_N]$



Model-Free Learning



Preview: Gridworld Reinforcement Learning



Passive Reinforcement Learning



Passive Reinforcement Learning

- Simplified task: policy evaluation
 - Input: a fixed policy π(s)
 - You don't know the transitions T(s,a,s')
 - You don't know the rewards R(s,a,s')
 - Goal: learn the state values



- In this case:
 - Learner is "along for the ride"
 - No choice about what actions to take
 - Just execute the policy and learn from experience
 - This is NOT offline planning! You actually take actions in the world.

Direct Evaluation

- Goal: Compute values for each state under π
- Idea: Average together observed sample values
 - Act according to π
 - Every time you visit a state, write down what the sum of discounted rewards turned out to be
 - Average those samples
- This is called direct evaluation



Example: Direct Evaluation



Problems with Direct Evaluation

- What's good about direct evaluation?
 - It's easy to understand
 - It doesn't require any knowledge of T, R
 - It eventually computes the correct average values, using just sample transitions
- What bad about it?
 - It wastes information about state connections
 - Each state must be learned separately
 - So, it takes a long time to learn

Output Values



If B and E both go to C under this policy, how can their values be different?

Why Not Use Policy Evaluation?

π(s)

- Simplified Bellman updates calculate V for a fixed policy:
 - Each round, replace V with a one-step-look-ahead layer over V

$$V_0^{\pi}(s) = 0$$

$$V_{k+1}^{\pi}(s) \leftarrow \sum_{s'} T(s, \pi(s), s') [R(s, \pi(s), s') + \gamma V_k^{\pi}(s')] \quad (s, \pi(s), s')$$

- This approach fully exploited the connections between the states
- Unfortunately, we need T and R to do it!
- Key question: how can we do this update to V without knowing T and R?
 - In other words, how to we take a weighted average without knowing the weights?

Sample-Based Policy Evaluation?

We want to improve our estimate of V by computing these averages:

$$V_{k+1}^{\pi}(s) \leftarrow \sum_{s'} T(s, \pi(s), s') [R(s, \pi(s), s') + \gamma V_k^{\pi}(s')]$$

Idea: Take samples of outcomes s' (by doing the action!) and average

$$sample_{1} = R(s, \pi(s), s_{1}') + \gamma V_{k}^{\pi}(s_{1}')$$

$$sample_{2} = R(s, \pi(s), s_{2}') + \gamma V_{k}^{\pi}(s_{2}')$$

$$\dots$$

$$sample_{n} = R(s, \pi(s), s_{n}') + \gamma V_{k}^{\pi}(s_{n}')$$

$$V_{k+1}^{\pi}(s) \leftarrow \frac{1}{n} \sum_{i} sample_{i}$$





Temporal Difference Learning



Temporal Difference Learning

- Big idea: learn from every experience!
 - Update V(s) each time we experience a transition (s, a, s', r)
 - Likely outcomes s' will contribute updates more often
- Temporal difference learning of values
 - Policy still fixed, still doing evaluation!
 - Move values toward value of whatever successor occurs: running average

Sample of V(s): $sample = R(s, \pi(s), s') + \gamma V^{\pi}(s')$ Update to V(s): $V^{\pi}(s) \leftarrow (1 - \alpha)V^{\pi}(s) + (\alpha)sample$ Same update: $V^{\pi}(s) \leftarrow V^{\pi}(s) + \alpha(sample - V^{\pi}(s))$



Exponential Moving Average

- Exponential moving average
 - The running interpolation update: $\bar{x}_n = (1 \alpha) \cdot \bar{x}_{n-1} + \alpha \cdot x_n$
 - Makes recent samples more important:

$$\bar{x}_n = \frac{x_n + (1 - \alpha) \cdot x_{n-1} + (1 - \alpha)^2 \cdot x_{n-2} + \dots}{1 + (1 - \alpha) + (1 - \alpha)^2 + \dots}$$

- Forgets about the past (distant past values were wrong anyway)
- Decreasing learning rate (alpha) can give converging averages

Example: Temporal Difference Learning



 $V^{\pi}(s) \leftarrow (1-\alpha)V^{\pi}(s) + \alpha \left[R(s, \pi(s), s') + \gamma V^{\pi}(s') \right]$

Assume: $\gamma = 1$, $\alpha = 1/2$

Problems with TD Value Learning

- TD value leaning is a model-free way to do policy evaluation, mimicking Bellman updates with running sample averages
- However, if we want to turn values into a (new) policy, we're sunk:

 $\pi(s) = \arg\max_{a} Q(s, a)$ $Q(s, a) = \sum_{s'} T(s, a, s') \left[R(s, a, s') + \gamma V(s') \right]$

- Idea: learn Q-values, not values
- Makes action selection model-free too!



Active Reinforcement Learning



Active Reinforcement Learning

- Full reinforcement learning: optimal policies (like value iteration)
 - You don't know the transitions T(s,a,s')
 - You don't know the rewards R(s,a,s')
 - You choose the actions now
 - Goal: learn the optimal policy / values

In this case:

- Learner makes choices!
- Fundamental tradeoff: exploration vs. exploitation
- This is NOT offline planning! You actually take actions in the world and find out what happens...



Detour: Q-Value Iteration

- Value iteration: find successive (depth-limited) values
 - Start with V₀(s) = 0, which we know is right
 - Given V_k, calculate the depth k+1 values for all states:

$$V_{k+1}(s) \leftarrow \max_{a} \sum_{s'} T(s, a, s') \left[R(s, a, s') + \gamma V_k(s') \right]$$

- But Q-values are more useful, so compute them instead
 - Start with Q₀(s,a) = 0, which we know is right
 - Given Q_k, calculate the depth k+1 q-values for all q-states:

$$Q_{k+1}(s,a) \leftarrow \sum_{s'} T(s,a,s') \left[R(s,a,s') + \gamma \max_{a'} Q_k(s',a') \right]$$

Q-Learning

Q-Learning: sample-based Q-value iteration

$$Q_{k+1}(s,a) \leftarrow \sum_{s'} T(s,a,s') \left[R(s,a,s') + \gamma \max_{a'} Q_k(s',a') \right]$$

- Learn Q(s,a) values as you go
 - Receive a sample (s,a,s',r)
 - Consider your old estimate: Q(s, a)
 - Consider your new sample estimate:

 $sample = R(s, a, s') + \gamma \max_{a'} Q(s', a')$

Incorporate the new estimate into a running average:

 $Q(s,a) \leftarrow (1-\alpha)Q(s,a) + (\alpha) [sample]$



[Demo: Q-learning – gridworld (L10D2)] [Demo: Q-learning – crawler (L10D3)]

Q learning with a fixed policy



Video of Demo Q-Learning -- Gridworld



CURRENT Q-VALUES

Q-Learning Properties

- Amazing result: Q-learning converges to optimal policy -- even if you're acting suboptimally!
- This is called off-policy learning
- Caveats:
 - You have to explore enough
 - You have to eventually make the learning rate small enough
 - ... but not decrease it too quickly
 - Basically, in the limit, it doesn't matter how you select actions (!)



Exploration vs. Exploitation



How to Explore?

- Several schemes for forcing exploration
 - Simplest: random actions (ε-greedy)
 - Every time step, flip a coin
 - With (small) probability ε, act randomly
 - With (large) probability 1-ε, act on current policy
 - Problems with random actions?
 - You do eventually explore the space, but keep thrashing around once learning is done
 - One solution: lower ϵ over time
 - Another solution: exploration functions



[Demo: Q-learning – manual exploration – bridge grid (L11D2)] [Demo: Q-learning – epsilon-greedy -- crawler (L11D3)]

Gridworld RL: ε-greedy



Gridworld RL: ε-greedy



CURRENT Q-VALUES

Video of Demo Q-learning – Epsilon-Greedy – Crawler



Exploration Functions

- When to explore?
 - Random actions: explore a fixed amount
 - Better idea: explore areas whose badness is not (yet) established, eventually stop exploring
- Exploration function
 - Takes a value estimate u and a visit count n, and returns an optimistic utility, e.g. f(u, n) = u + k/n



Regular Q-Update: $Q(s,a) \leftarrow_{\alpha} R(s,a,s') + \gamma \max_{a'} Q(s',a')$

Modified Q-Update: $Q(s,a) \leftarrow_{\alpha} R(s,a,s') + \gamma \max_{a'} f(Q(s',a'), N(s',a'))$

Note: this propagates the "bonus" back to states that lead to unknown states as well!

[Demo: exploration – Q-learning – crawler – exploration function (L11D4)]

Video of Demo Q-learning – Exploration Function – Crawler



Regret

- Even if you learn the optimal policy, you still make mistakes along the way
- Regret is a measure of your total mistake cost: the difference between your (expected) rewards, including youthful suboptimality, and optimal (expected) rewards
- Minimizing regret goes beyond learning to be optimal – it requires optimally learning to be optimal
- Example: random exploration and exploration functions both end up optimal, but random exploration has higher regret



Approximate Q-Learning



Generalizing Across States

- Basic Q-Learning keeps a table of all q-values
- In realistic situations, we cannot possibly learn about every single state!
 - Too many states to visit them all in training
 - Too many states to hold the q-tables in memory
- Instead, we want to generalize:
 - Learn about some small number of training states from experience
 - Generalize that experience to new, similar situations
 - This is a fundamental idea in machine learning, and we'll see it over and over again



[demo – RL pacman]

Example: Pacman

Let's say we discover through experience that this state is bad:



In naïve q-learning, we know nothing about this state:



Or even this one!



[Demo: Q-learning – pacman – tiny – watch all (L11D5)] [Demo: Q-learning – pacman – tiny – silent train (L11D6)] [Demo: Q-learning – pacman – tricky – watch all (L11D7)]

Video of Demo Q-Learning Pacman – Tiny – Watch All

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Video of Demo Q-Learning Pacman – Tiny – Silent Train



Video of Demo Q-Learning Pacman – Tricky – Watch All



Feature-Based Representations

- Solution: describe a state using a vector of features (properties)
 - Features are functions from states to real numbers (often 0/1) that capture important properties of the state
 - Example features:
 - Distance to closest ghost
 - Distance to closest dot
 - Number of ghosts
 - 1 / (dist to dot)²
 - Is Pacman in a tunnel? (0/1)
 - etc.
 - Is it the exact state on this slide?
 - Can also describe a q-state (s, a) with features (e.g. action moves closer to food)



Linear Value Functions

 Using a feature representation, we can write a q function (or value function) for any state using a few weights:

$$V(s) = w_1 f_1(s) + w_2 f_2(s) + \ldots + w_n f_n(s)$$

$$Q(s,a) = w_1 f_1(s,a) + w_2 f_2(s,a) + \ldots + w_n f_n(s,a)$$

- Advantage: our experience is summed up in a few powerful numbers
- Disadvantage: states may share features but actually be very different in value!

Approximate Q-Learning

$$Q(s,a) = w_1 f_1(s,a) + w_2 f_2(s,a) + \ldots + w_n f_n(s,a)$$

Q-learning with linear Q-functions:

 $\begin{aligned} \text{transition} &= (s, a, r, s') \\ \text{difference} &= \left[r + \gamma \max_{a'} Q(s', a') \right] - Q(s, a) \\ Q(s, a) &\leftarrow Q(s, a) + \alpha \text{ [difference]} \end{aligned} \qquad \text{Exact Q's} \\ w_i &\leftarrow w_i + \alpha \text{ [difference] } f_i(s, a) \end{aligned} \qquad \text{Approximate Q's} \end{aligned}$

- Adjust weights of active features
- E.g., if something unexpectedly bad happens, blame the features that were on: disprefer all states with that state's features
- Formal justification: online least squares



Example: Q-Pacman

$$Q(s,a) = 4.0 f_{DOT}(s,a) - 1.0 f_{GST}(s,a)$$



 $Q(s,a) = 3.0 f_{DOT}(s,a) - 3.0 f_{GST}(s,a)$

[Demo: approximate Qlearning pacman (L11D10)]

Video of Demo Approximate Q-Learning -- Pacman

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Q-Learning and Least Squares



Linear Approximation: Regression*





Prediction: $\hat{y} = w_0 + w_1 f_1(x)$ Prediction: $\hat{y}_i = w_0 + w_1 f_1(x) + w_2 f_2(x)$

Optimization: Least Squares*



Minimizing Error*

Imagine we had only one point x, with features f(x), target value y, and weights w:

$$\operatorname{error}(w) = \frac{1}{2} \left(y - \sum_{k} w_{k} f_{k}(x) \right)^{2}$$
$$\frac{\partial \operatorname{error}(w)}{\partial w_{m}} = - \left(y - \sum_{k} w_{k} f_{k}(x) \right) f_{m}(x)$$
$$w_{m} \leftarrow w_{m} + \alpha \left(y - \sum_{k} w_{k} f_{k}(x) \right) f_{m}(x)$$



Approximate q update explained:

$$w_m \leftarrow w_m + \alpha \left[r + \gamma \max_a Q(s', a') - Q(s, a) \right] f_m(s, a)$$

"prediction"

"target"

Overfitting: Why Limiting Capacity Can Help*





- Problem: often the feature-based policies that work well (win games, maximize utilities) aren't the ones that approximate V / Q best
 - E.g. your value functions from project 2 were probably horrible estimates of future rewards, but they still produced good decisions
 - Q-learning's priority: get Q-values close (modeling)
 - Action selection priority: get ordering of Q-values right (prediction)
 - We'll see this distinction between modeling and prediction again later in the course
- Solution: learn policies that maximize rewards, not the values that predict them
- Policy search: start with an ok solution (e.g. Q-learning) then fine-tune by hill climbing on feature weights

- Simplest policy search:
 - Start with an initial linear value function or Q-function
 - Nudge each feature weight up and down and see if your policy is better than before

Problems:

- How do we tell the policy got better?
- Need to run many sample episodes!
- If there are a lot of features, this can be impractical
- Better methods exploit lookahead structure, sample wisely, change multiple parameters...



[Andrew Ng]

[Video: HELICOPTER]

Conclusion

- We're done with Part I: Search and Planning!
- We've seen how AI methods can solve problems in:
 - Search
 - Constraint Satisfaction Problems
 - Games
 - Markov Decision Problems
 - Reinforcement Learning
- Next up: Part II: Uncertainty and Learning!

