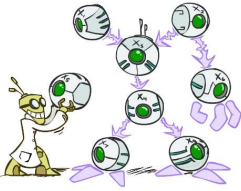


## CSE 473: Artificial Intelligence

### Bayes' Nets



Steve Tanimoto --- University of Washington

[These slides were created by Dan Klein and Pieter Abbeel for CS188 Intro to AI at UC Berkeley. All CS188 materials are available at <http://ai.berkeley.edu>.]

## Probabilistic Models

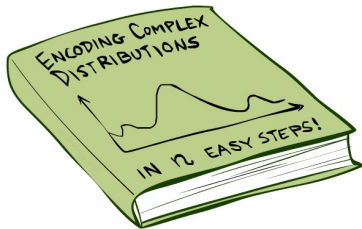
- Models describe how (a portion of) the world works

- Models are always simplifications
  - May not account for every variable
  - May not account for all interactions between variables
  - "All models are wrong; but some are useful."
    - George E. P. Box



- What do we do with probabilistic models?
  - We (or our agents) need to reason about unknown variables, given evidence
  - Example: explanation (diagnostic reasoning)
  - Example: prediction (causal reasoning)
  - Example: value of information

## Bayes' Nets: Big Picture



## Bayes' Nets: Big Picture

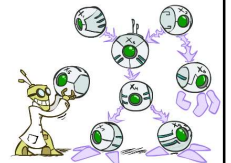
- Two problems with using full joint distribution tables as our probabilistic models:

- Unless there are only a few variables, the joint is WAY too big to represent explicitly
- Hard to learn (estimate) anything empirically about more than a few variables at a time

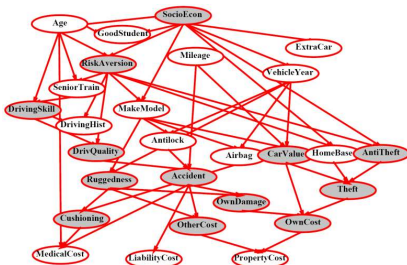


- Bayes' nets: a technique for describing complex joint distributions (models) using simple, local distributions (conditional probabilities)

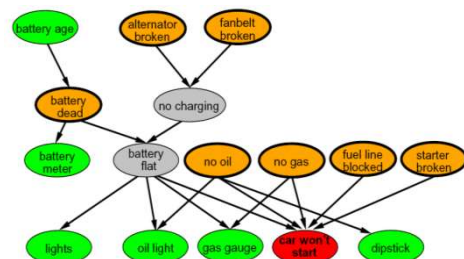
- More properly called graphical models
- We describe how variables locally interact
- Local interactions chain together to give global, indirect interactions
- For about 10 min, we'll be vague about how these interactions are specified



## Example Bayes' Net: Insurance

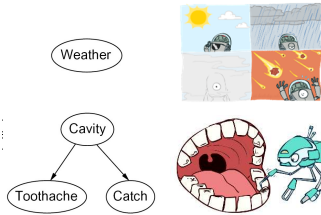


## Example Bayes' Net: Car



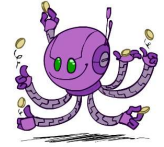
## Graphical Model Notation

- Nodes: variables (with domains)
  - Can be assigned (observed) or unassigned (unobserved)
- Arcs: interactions
  - Similar to CSP constraints
  - Indicate "direct influence" between variables.
  - Formally: encode conditional independence (more later)
- For now: imagine that arrows mean direct causation (in general, they don't!)



## Example: Coin Flips

- N independent coin flips



- No interactions between variables: absolute independence

## Example: Traffic

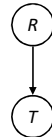
- Variables:
  - R: It rains
  - T: There is traffic



- Model 1: independence



- Model 2: rain causes traffic



- Why is an agent using model 2 better?

## Example: Traffic II

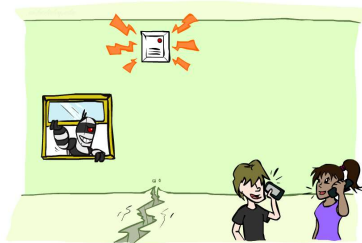
- Let's build a causal graphical model!

- Variables
  - T: Traffic
  - R: It rains
  - L: Low pressure
  - D: Roof drips
  - B: Ballgame
  - C: Cavity



## Example: Alarm Network

- Variables
  - B: Burglary
  - A: Alarm goes off
  - M: Mary calls
  - J: John calls
  - E: Earthquake!



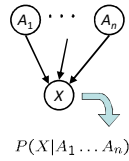
## Bayes' Net Semantics



## Bayes' Net Semantics



- A set of nodes, one per variable  $X$
- A directed, acyclic graph
- A conditional distribution for each node
  - A collection of distributions over  $X$ , one for each combination of parents' values
- CPT: conditional probability table
- Description of a noisy "causal" process



*A Bayes net = Topology (graph) + Local Conditional Probabilities*

## Probabilities in BNs



- Bayes' nets **implicitly** encode joint distributions
  - As a product of local conditional distributions
  - To see what probability a BN gives to a full assignment, multiply all the relevant conditionals together:

$$P(x_1, x_2, \dots, x_n) = \prod_{i=1}^n P(x_i | \text{parents}(X_i))$$

▪ Example:



$$P(+cavity, +catch, -toothache)$$

## Probabilities in BNs



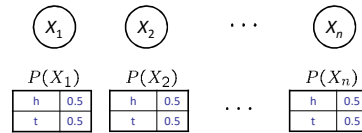
- Why are we guaranteed that setting

$$P(x_1, x_2, \dots, x_n) = \prod_{i=1}^n P(x_i | \text{parents}(X_i))$$

results in a proper joint distribution?

- Chain rule (valid for all distributions):  $P(x_1, x_2, \dots, x_n) = \prod_{i=1}^n P(x_i | x_1 \dots x_{i-1})$
- Assume conditional independences:  $P(x_i | x_1, \dots, x_{i-1}) = P(x_i | \text{parents}(X_i))$ 
  - Consequence:  $P(x_1, x_2, \dots, x_n) = \prod_{i=1}^n P(x_i | \text{parents}(X_i))$
- Not every BN can represent every joint distribution
  - The topology enforces certain conditional independencies

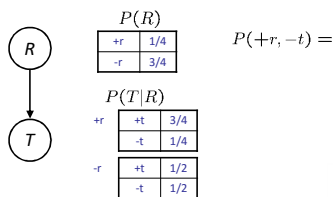
## Example: Coin Flips



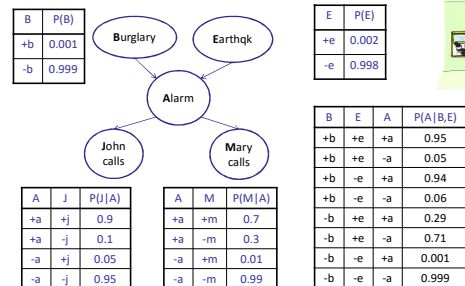
$$P(h, h, t, h) =$$

*Only distributions whose variables are absolutely independent can be represented by a Bayes' net with no arcs.*

## Example: Traffic

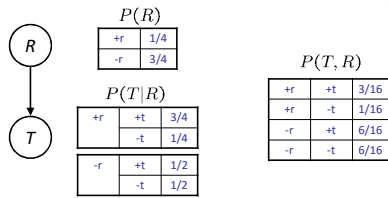


## Example: Alarm Network



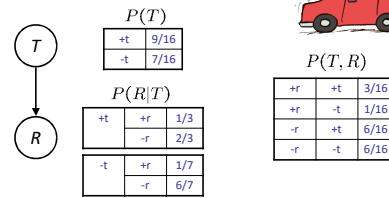
## Example: Traffic

### ▪ Causal direction



## Example: Reverse Traffic

### ▪ Reverse causality?



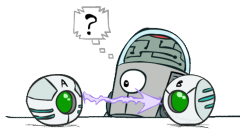
## Causality?

### ▪ When Bayes' nets reflect the true causal patterns:

- Often simpler (nodes have fewer parents)
- Often easier to think about
- Often easier to elicit from experts

### ▪ BNs need not actually be causal

- Sometimes no causal net exists over the domain (especially if variables are missing)
- E.g. consider the variables *Traffic* and *Drips*
- End up with arrows that reflect correlation, not causation



### ▪ What do the arrows really mean?

- Topology may happen to encode causal structure
- Topology really encodes conditional independence

$$P(x_i|x_1, \dots, x_{i-1}) = P(x_i|\text{parents}(X_i))$$