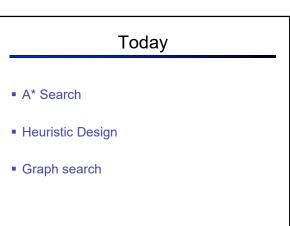
## CSE 473: Artificial Intelligence

## Spring 2018

Heuristic Search and A\* Algorithms

Steve Tanimoto

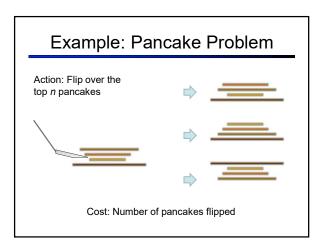
With slides from : Dieter Fox, Dan Weld, Dan Klein, Stuart Russell, Andrew Moore, Luke Zettlemoyer





#### • Search Algorithm:

- Systematically builds a search tree
- Chooses an ordering of the fringe (unexplored nodes)



### Example: Pancake Problem

#### BOUNDS FOR SORTING BY PREFIX REVERSAL

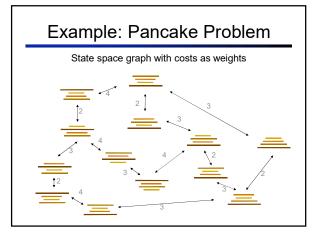
William H. GATES

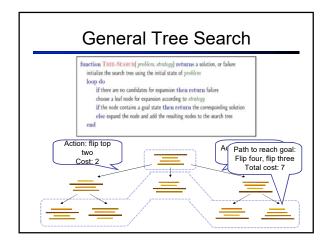
Microsoft, Albuquerque, New Mexico

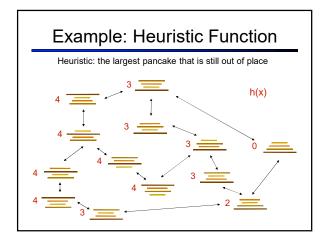
Christos H. PAPADIMITRIOU\*<sup>†</sup> Department of Electrical Engineering, University of California, Berkeley, CA 94720, U.S.A.

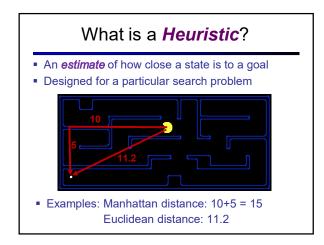
Received 18 January 1978 Revised 28 August 1978

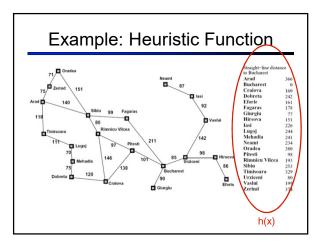
For a permutation  $\sigma$  of the integers from 1 to n, let  $f(\sigma)$  be the smallest number of prefix reversals that will transform  $\sigma$  to the identity permutation, and let f(n) be the largest such  $f(\sigma)$  for all  $\sigma$  in (the symmetric group)  $S_{\alpha}$ . We show that f(n) = (5n + 5)/3, and that  $f(n) \ge 17n/16$  for n a multiple of 16. If, furthermore, each integer is required to participate in an even number of reversed prefixes, the corresponding function g(n) is shown to obey  $3n/2 - 1 \le g(n) \le 2n + 3$ .



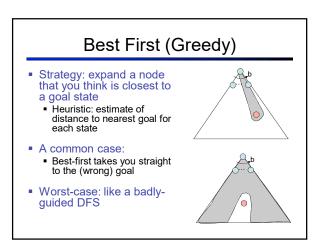


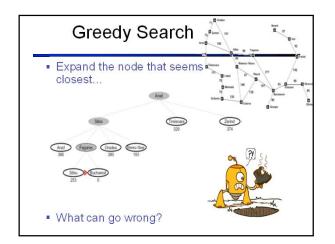


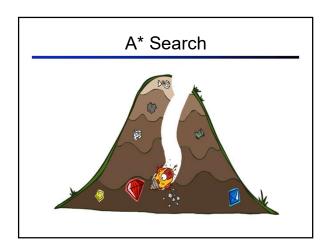


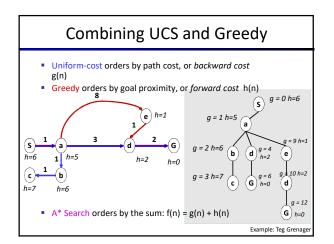


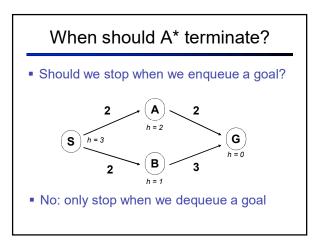


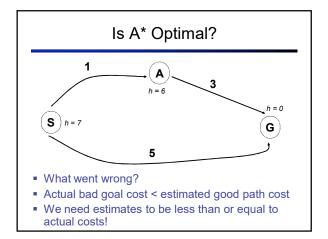


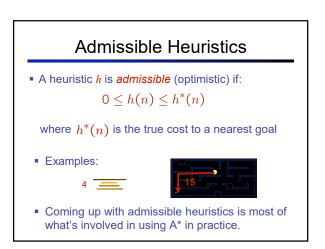


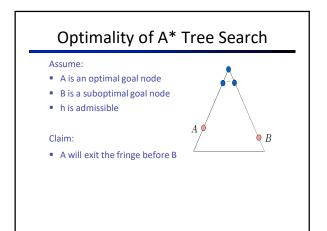


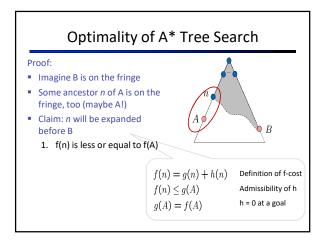


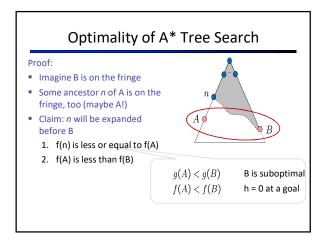


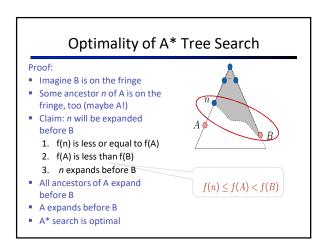


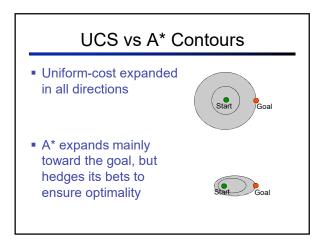


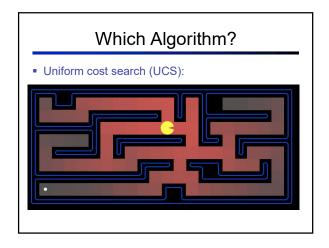


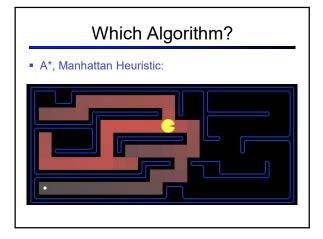


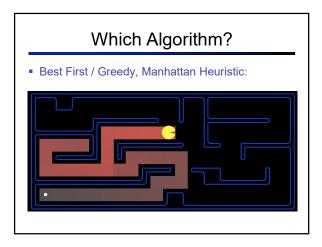


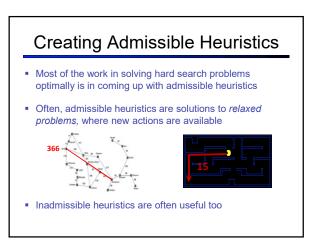


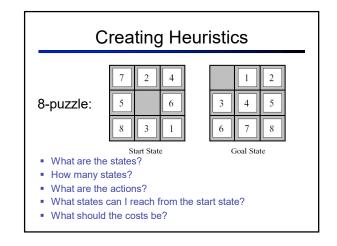


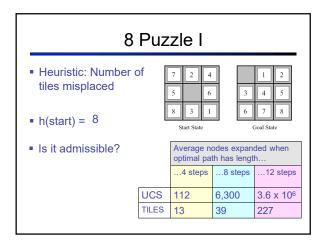


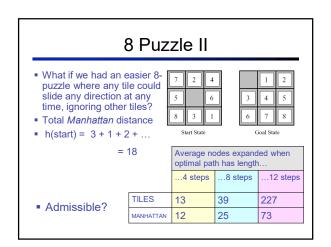






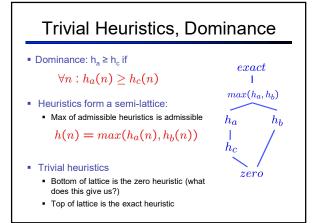






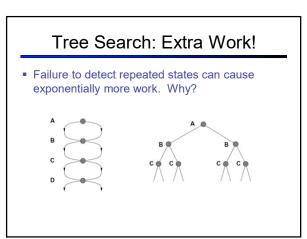
## 8 Puzzle III

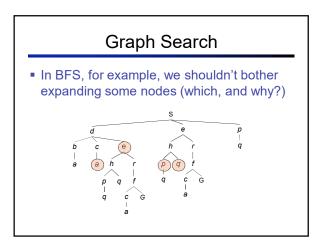
- How about using the actual cost as a heuristic?
  - Would it be admissible?
  - Would we save on nodes expanded?
  - What's wrong with it?
- With A\*: a trade-off between quality of estimate and work per node!



# A\* Applications Pathing / routing problems

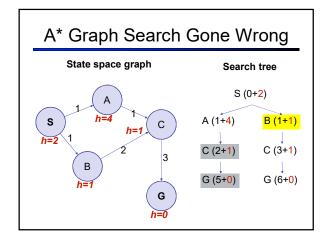
- Resource planning problems
- Robot motion planning
- Language analysis
- Machine translation
- Speech recognition
- ....

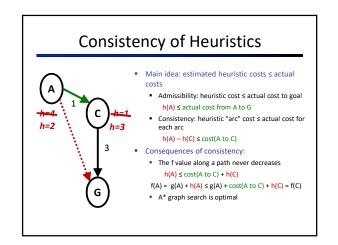


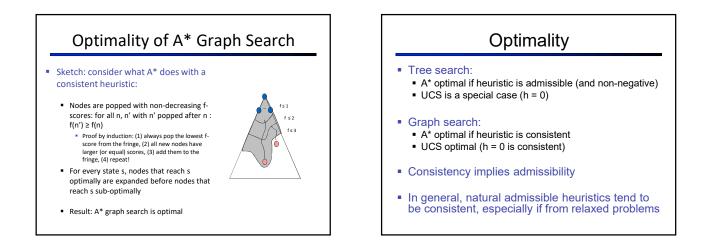


## Graph Search

- Idea: never expand a state twice
- How to implement:
  - Tree search + set of expanded states ("closed set")
  - Expand the search tree node-by-node, but...
  - Before expanding a node, check to make sure its state has never been expanded before
  - If not new, skip it, if new add to closed set
- Hint: in python, store the closed set as a set, not a list
- Can graph search wreck completeness? Why/why not?
- How about optimality?







## Summary: A\*

- A\* uses both backward costs and (estimates of) forward costs
- A\* is optimal with admissible / consistent heuristics
- Heuristic design is key: often use relaxed problems