

CSE 473: Artificial Intelligence

Spring 2018

Problem Spaces & Search

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With slides from :

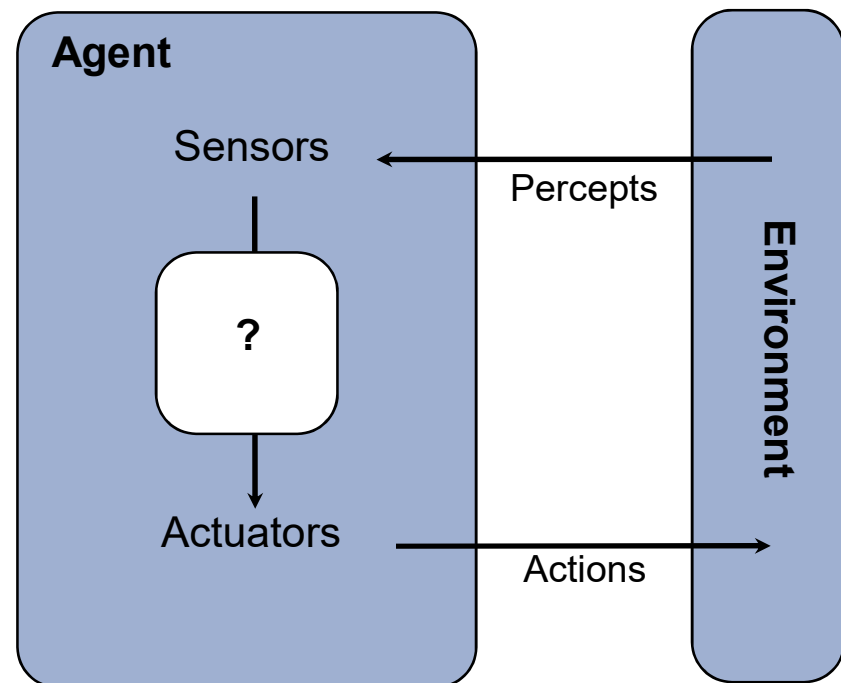
Dieter Fox, Dan Weld, Dan Klein, Stuart Russell, Andrew Moore, Luke Zettlemoyer

Outline

- Search Problems
- Uninformed Search Methods
 - Depth-First Search
 - Breadth-First Search
 - Uniform-Cost Search
- Heuristic Search Methods
 - Best-First, Greedy Search
 - A*

Agent vs. Environment

- An **agent** is an entity that *perceives* and *acts*.
- A **rational agent** selects actions that maximize its **utility function**.
- Characteristics of the **percepts**, **environment**, and **action space** dictate techniques for selecting rational actions.



Types of Agents

- Reflex



- Goal oriented

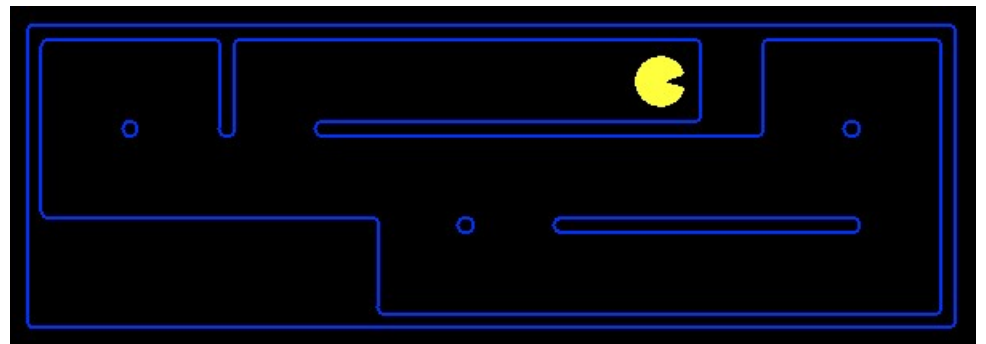
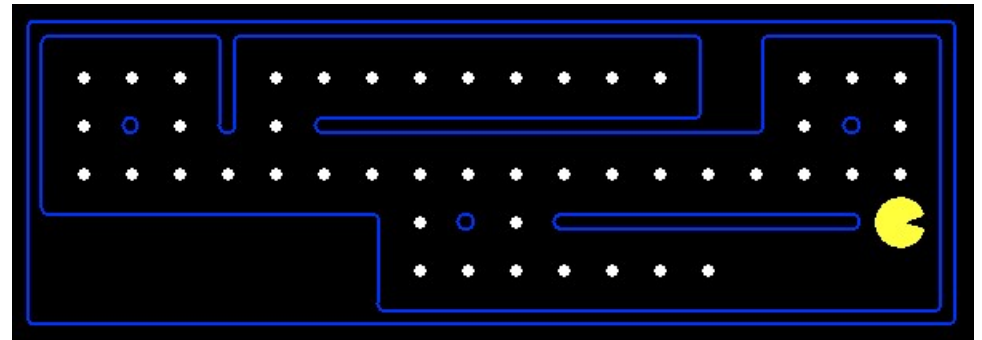


- Utility-based



Goal Based Agents

- Plan ahead
- Ask “what if”
- Decisions based on (hypothesized) consequences of actions
- Must have a model of how the world evolves in response to actions
- Act on how the world **WOULD BE**



Types of Environments


- Fully observable *vs.* partially observable
- Single agent *vs.* multiagent
- Deterministic *vs.* stochastic
- Episodic *vs.* sequential
- Discrete *vs.* continuous

Search thru a Problem Space (aka State Space)

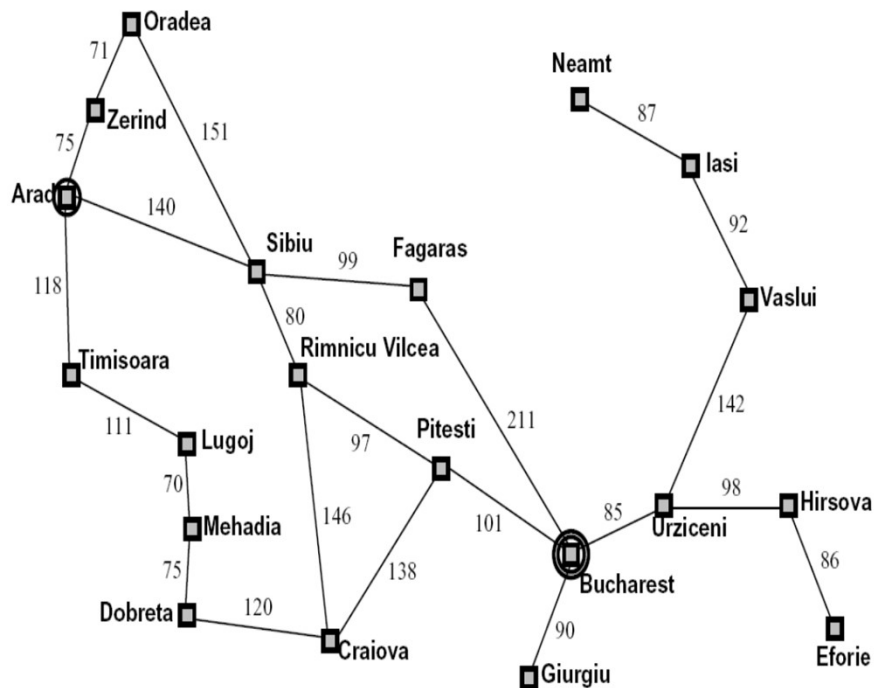
- Input:

- Set of states
- Operators [and costs]
- Start state
- Goal state [test]

- Output:

- Path: start  a state satisfying goal test
[May require shortest path]
[Sometimes just need a state that passes test]

Example: Traveling in Romania

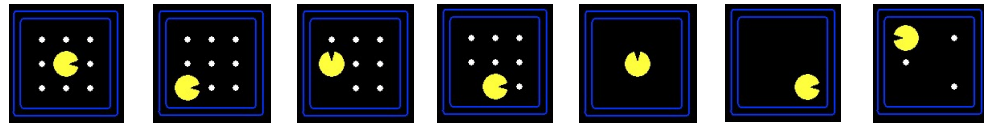


- State space:
 - Cities
- Successor function:
 - Roads: Go to adjacent city with cost = distance
- Start state:
 - Arad
- Goal test:
 - Is state == Bucharest?
- Solution?

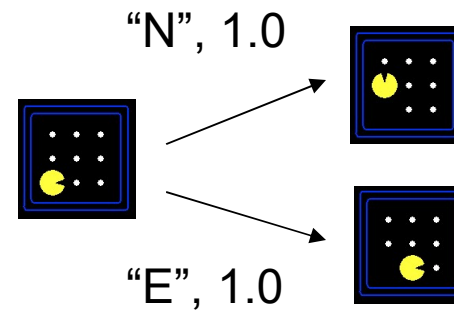
Example: Simplified Pac-Man

- Input:

- A state space



- A successor function

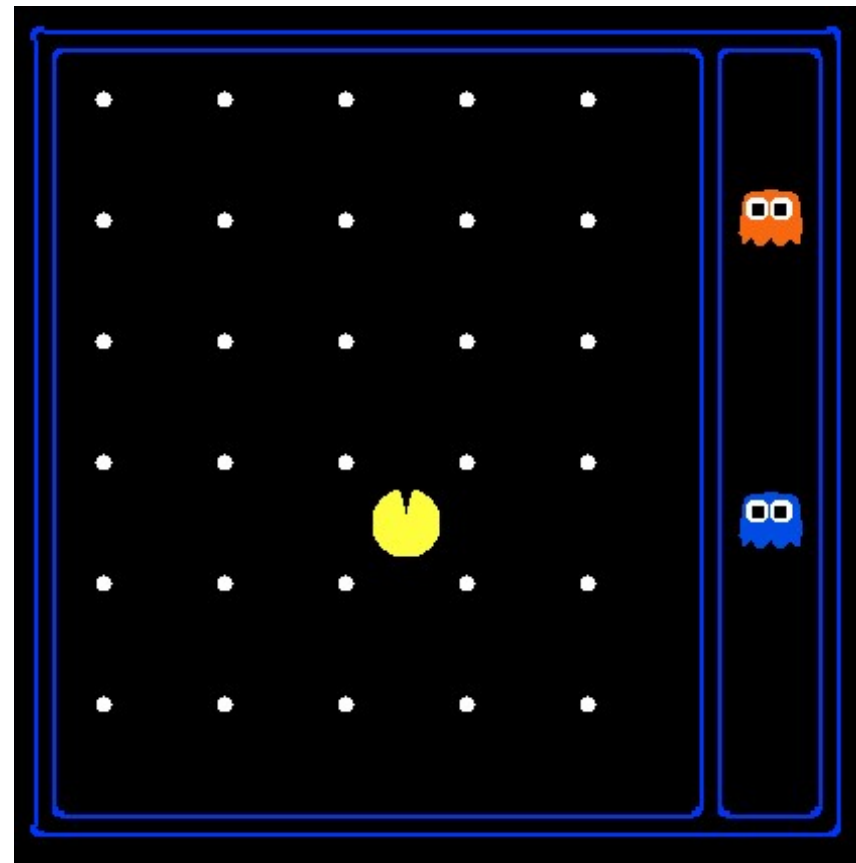


- A start state
- A goal test

- Output:

State Space Sizes?

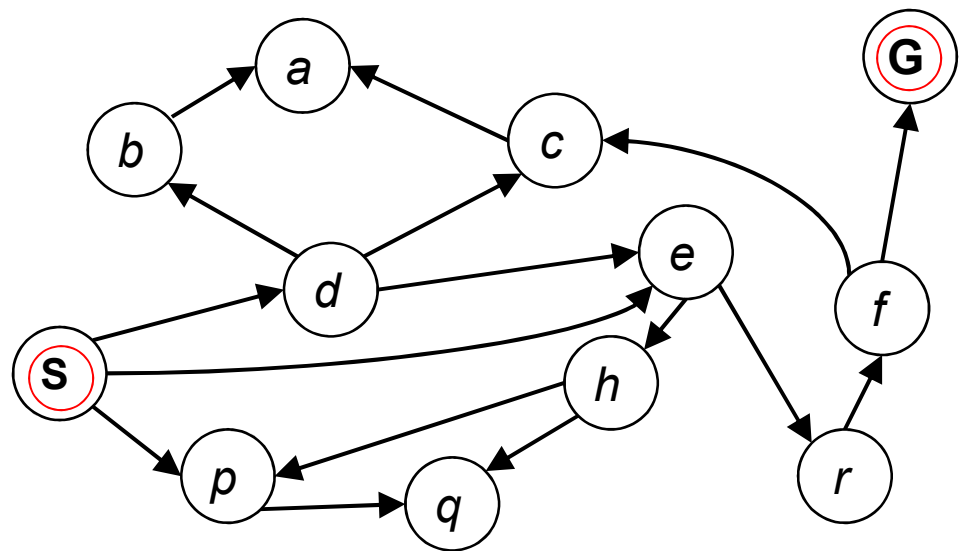
- Search Problem:
Eat all of the food
- Pacman positions:
 $10 \times 12 = 120$
- Pacman facing:
up, down, left, right
- Food configurations: 2^{30}
- Ghost1 positions: 12
- Ghost 2 positions: 11



$$120 \times 4 \times 2^{30} \times 12 \times 11 = 6.8 \times 10^{13}$$

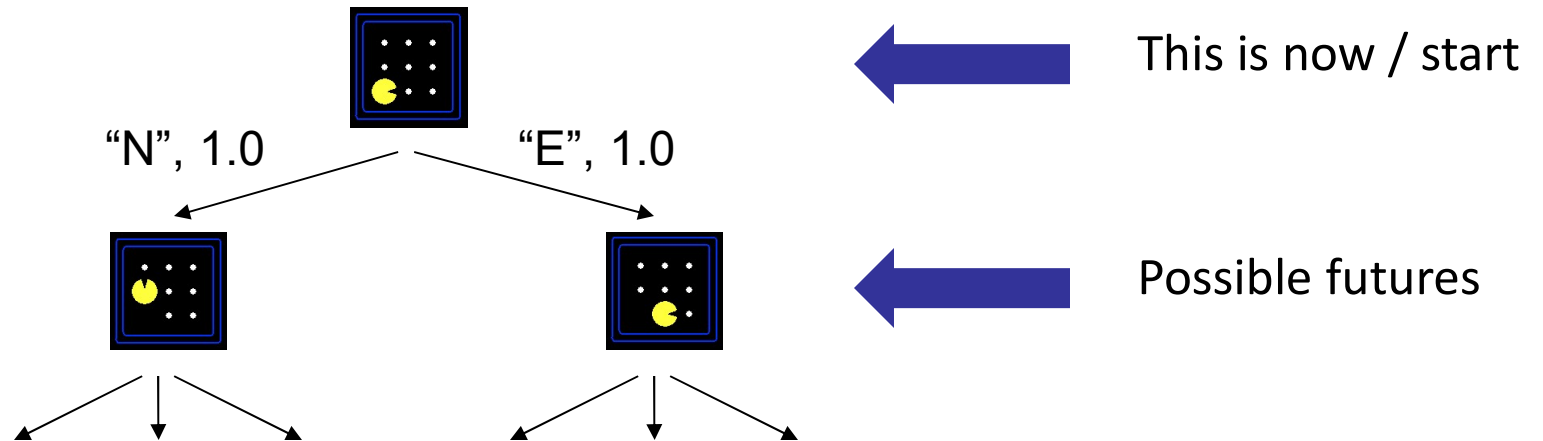
State Space Graphs

- State space graph:
 - Each node is a state
 - The successor function is represented by arcs
 - Edges may be labeled with costs
- In a search graph, each state occurs only once!
- We can rarely build this graph in memory (so we don't)



*Ridiculously tiny search graph
for a tiny search problem*

Search Trees

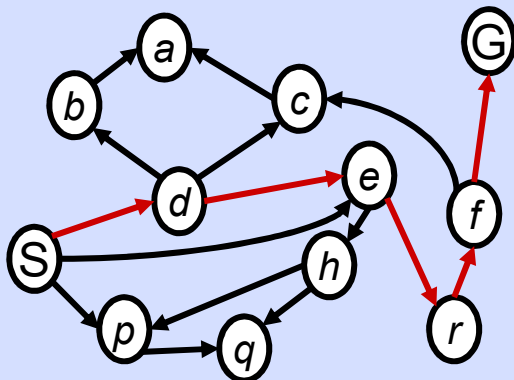


- A search tree:

- Start state at the root node
- Children correspond to successors
- Nodes contain states, correspond to PLANS to those states
- Edges are labeled with actions and costs
- For most problems, we can never actually build the whole tree

State Space Graphs vs. Search Trees

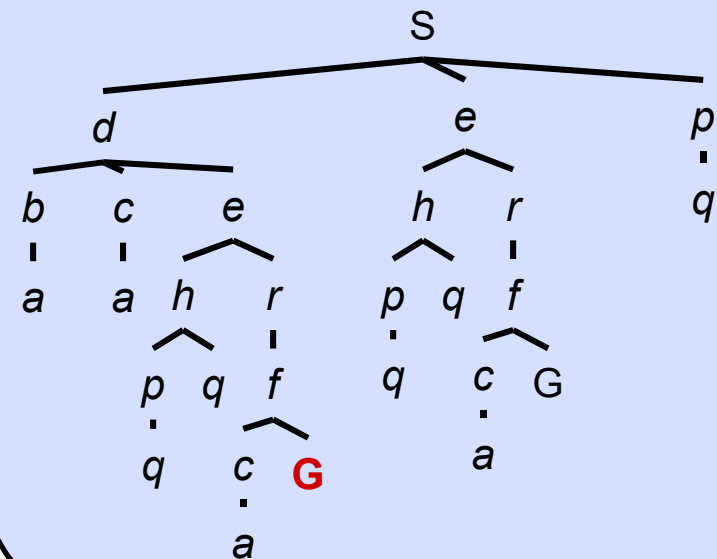
State Space Graph



*Each NODE in
in the search
tree is an
entire PATH in
the state
space graph.*

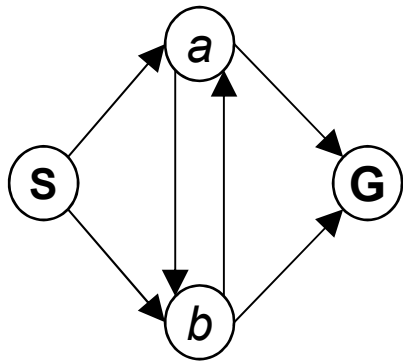
*We construct
both on
demand – and
we construct
as little as
possible.*

Search Tree



State Space Graphs vs. Search Trees

Consider this 4-state graph:

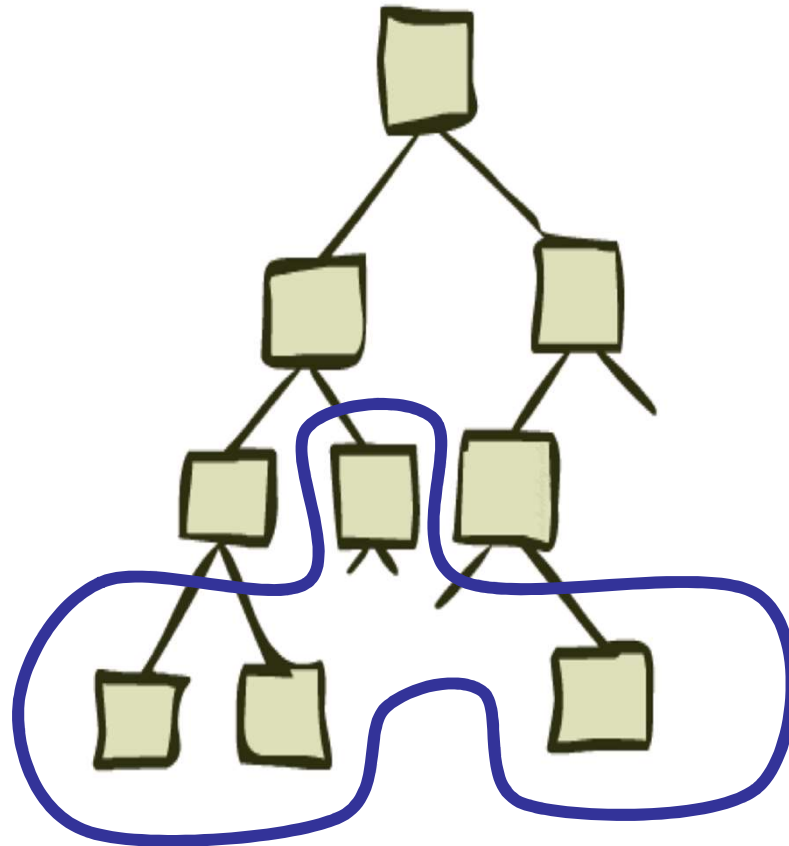


How big is its search tree (from S)?

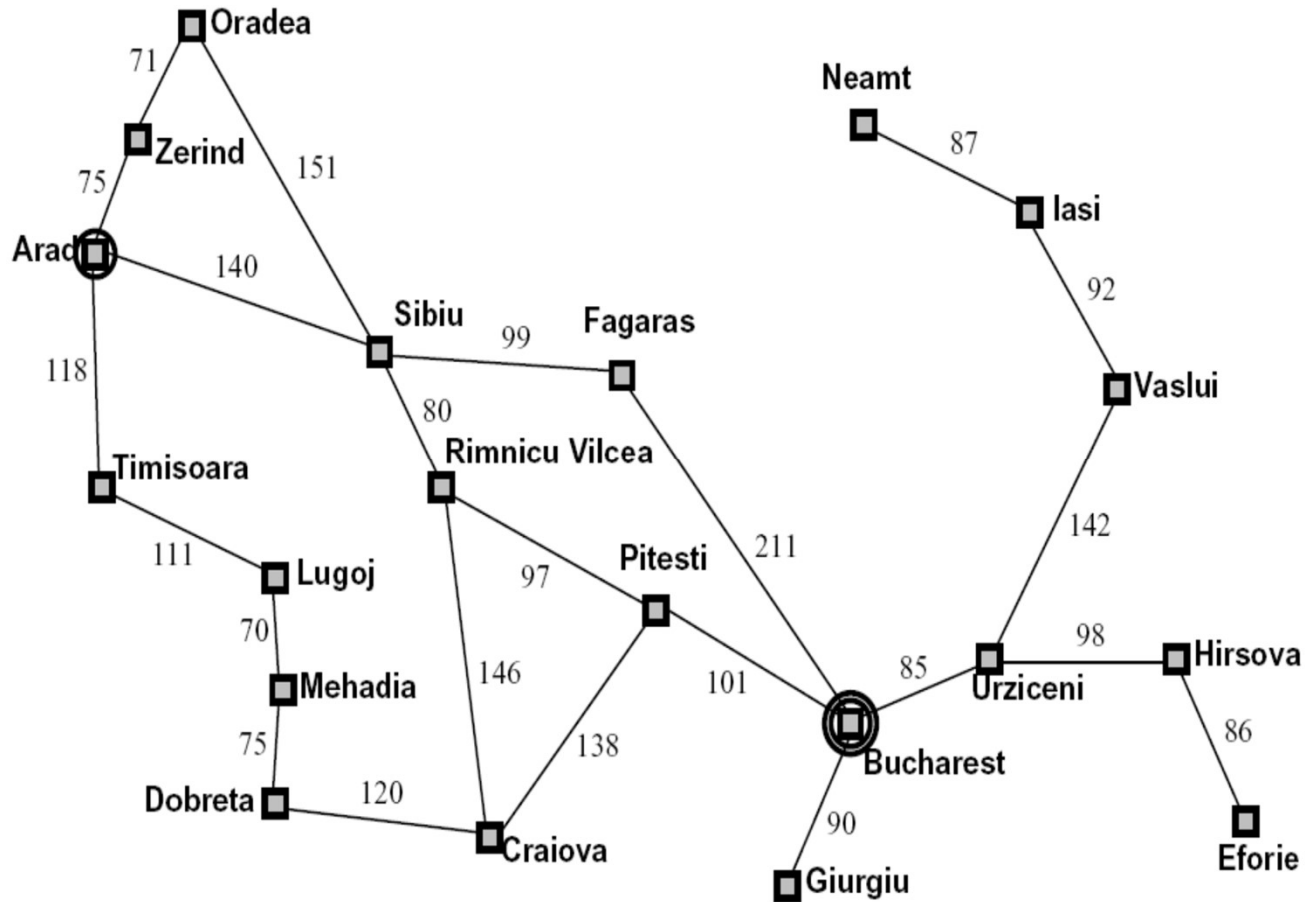


Important: Lots of repeated structure in the search tree!

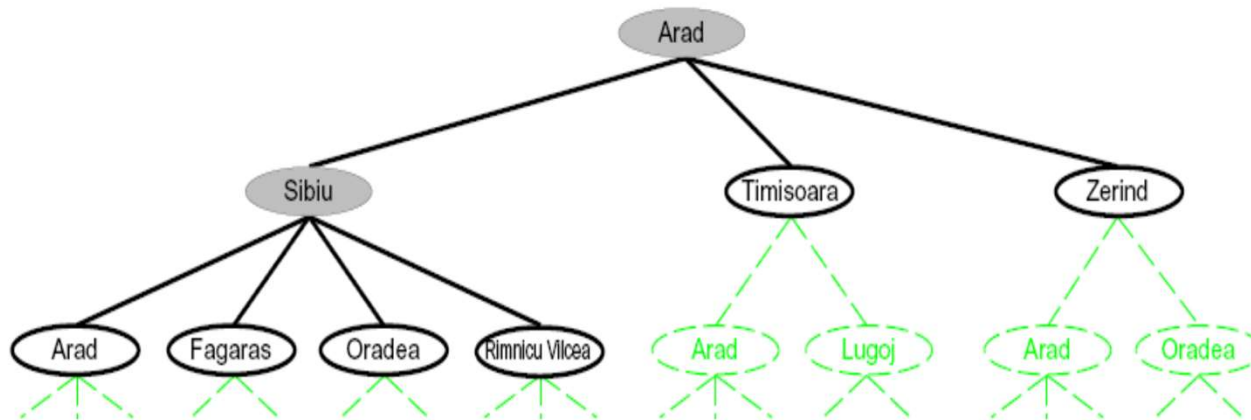
Tree Search



Search Example: Romania



Searching with a Search Tree



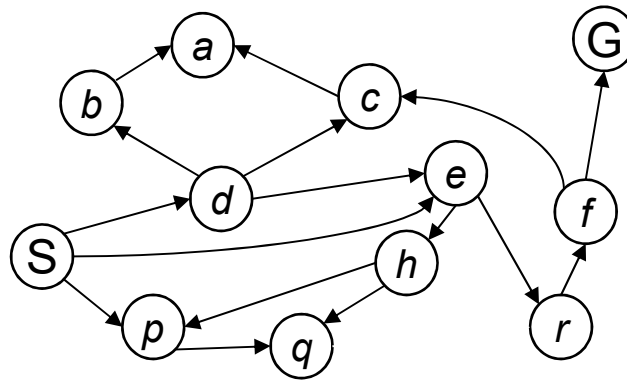
- Search:
 - Expand out potential plans (tree nodes)
 - Maintain a **fringe** of partial plans under consideration
 - Try to expand as few tree nodes as possible

General Tree Search

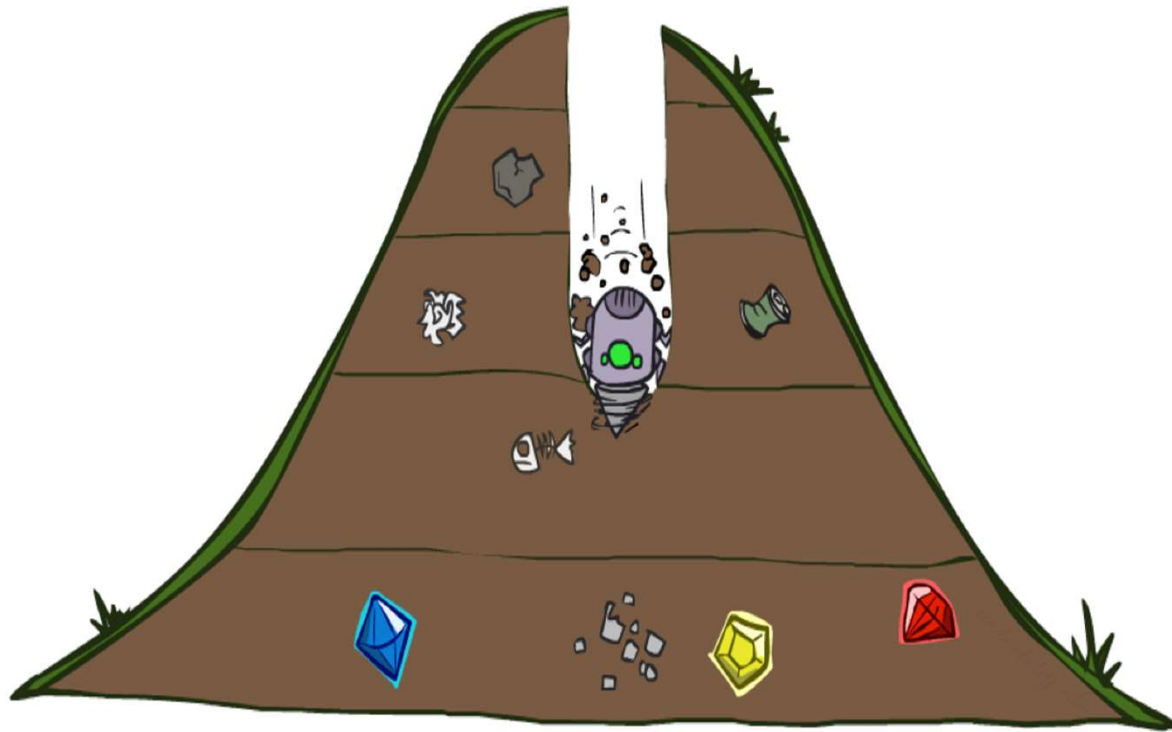
```
function TREE-SEARCH(problem, strategy) returns a solution, or failure
  initialize the search tree using the initial state of problem
  loop do
    if there are no candidates for expansion then return failure
    choose a leaf node for expansion according to strategy
    if the node contains a goal state then return the corresponding solution
    else expand the node and add the resulting nodes to the search tree
  end
```

- Important ideas:
 - Fringe
 - Expansion
 - Exploration strategy
- Main question: which fringe nodes to explore?

Tree Search Example



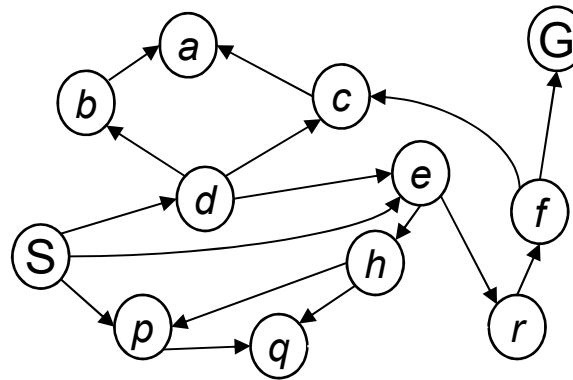
Depth-First Search



Depth-First Search

*Strategy: expand a
deepest node first*

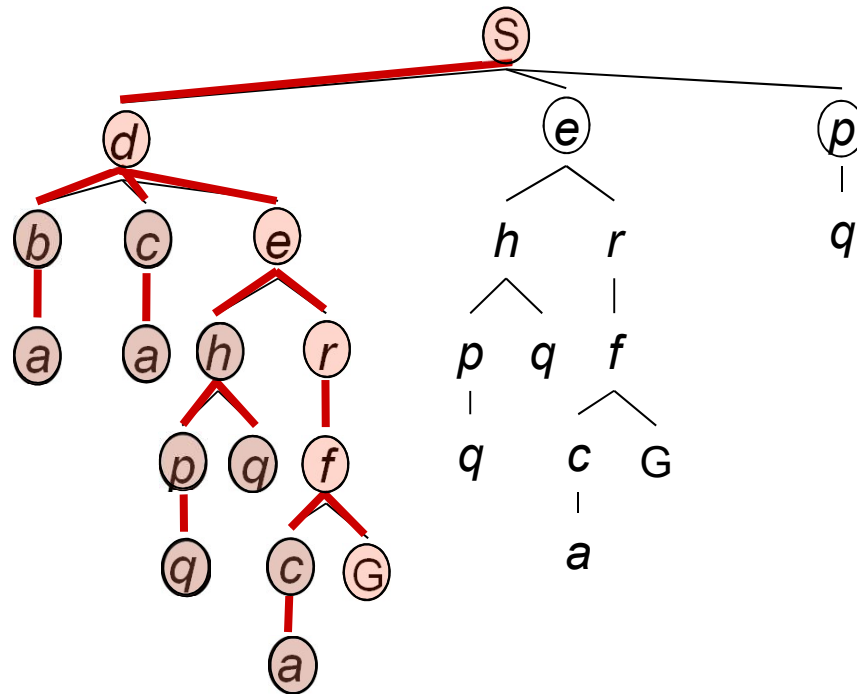
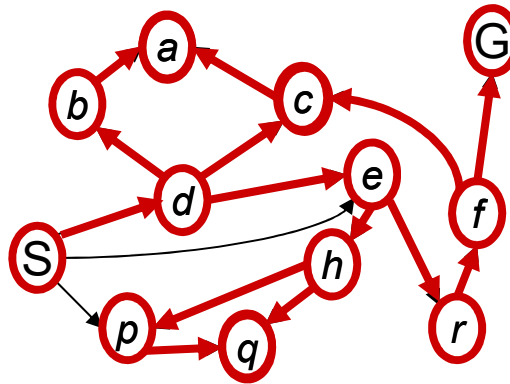
*Implementation: Fringe is
a LIFO stack*



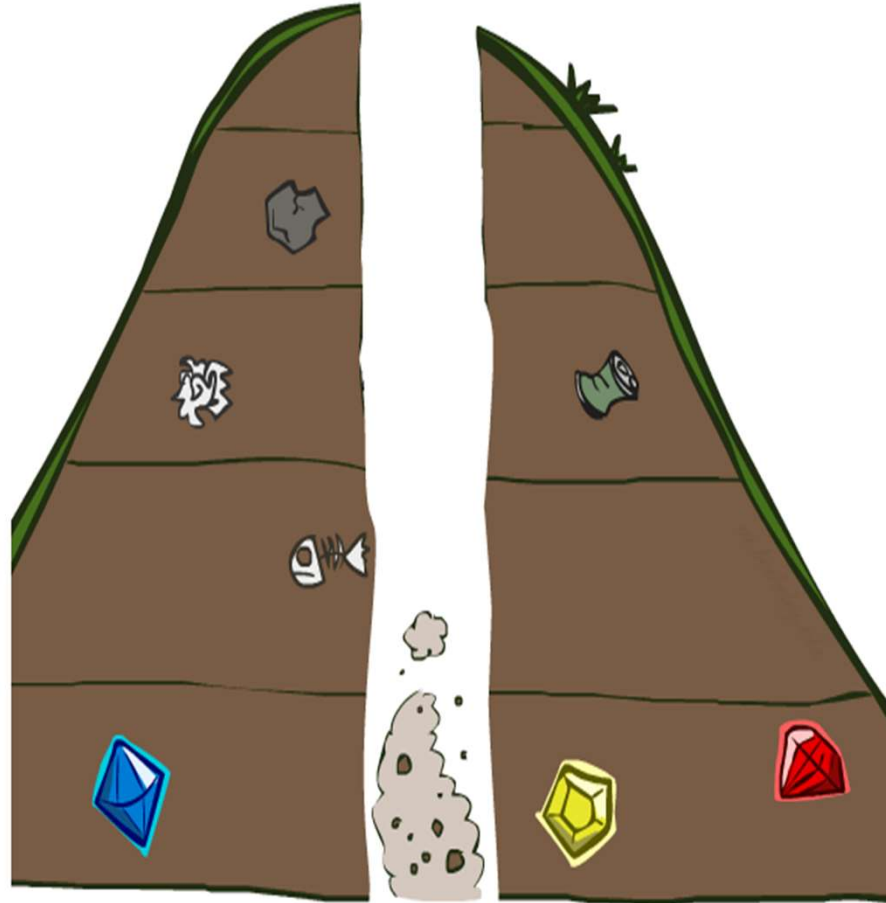
Depth-First Search

Strategy: expand a deepest node first

Implementation: Fringe is a LIFO stack



Search Algorithm Properties

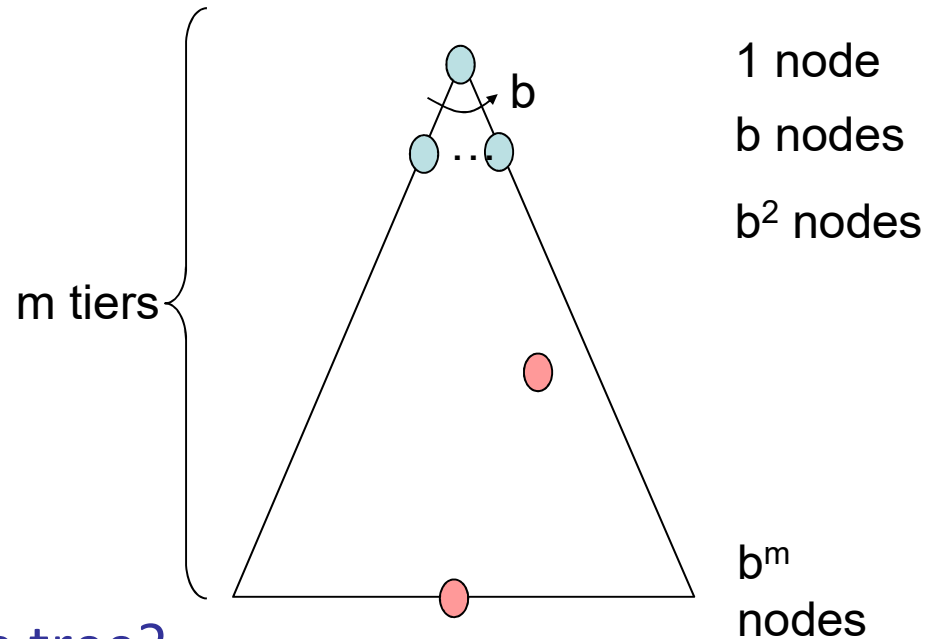


Search Algorithm Properties

- Complete: Guaranteed to find a solution if one exists?
- Optimal: Guaranteed to find the least cost path?
- Time complexity?
- Space complexity?

- **Cartoon of search tree:**

- b is the branching factor
- m is the maximum depth
- solutions at various depths



- **Number of nodes in entire tree?**

- $1 + b + b^2 + \dots + b^m = O(b^m)$

Depth-First Search (DFS) Properties

- What nodes does DFS expand?

- Some left prefix of the tree.
- Could process the whole tree!
- If m is finite, takes time $O(b^m)$

- How much space does the fringe take?

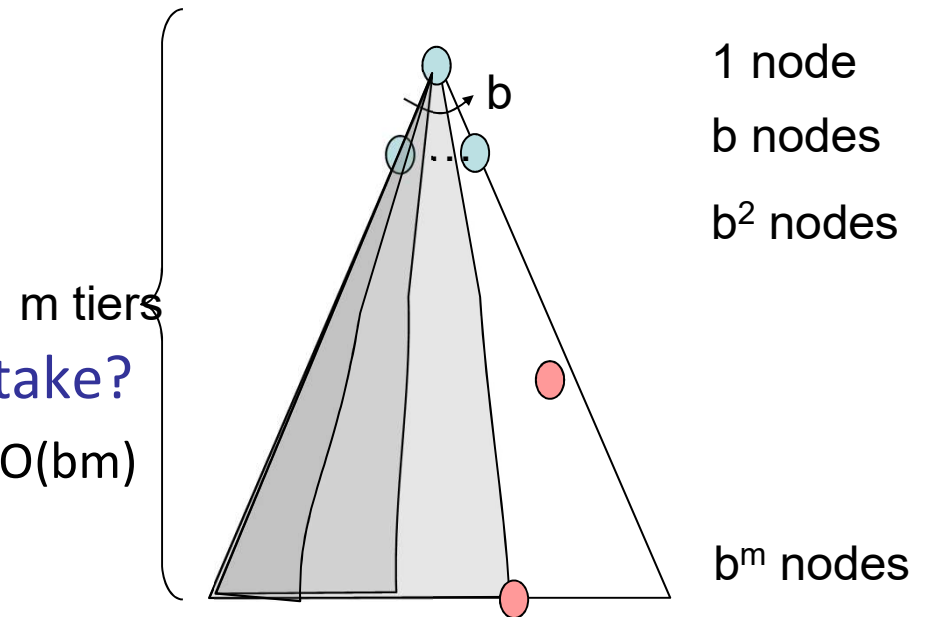
- Only has siblings on path to root, so $O(bm)$

- Is it complete?

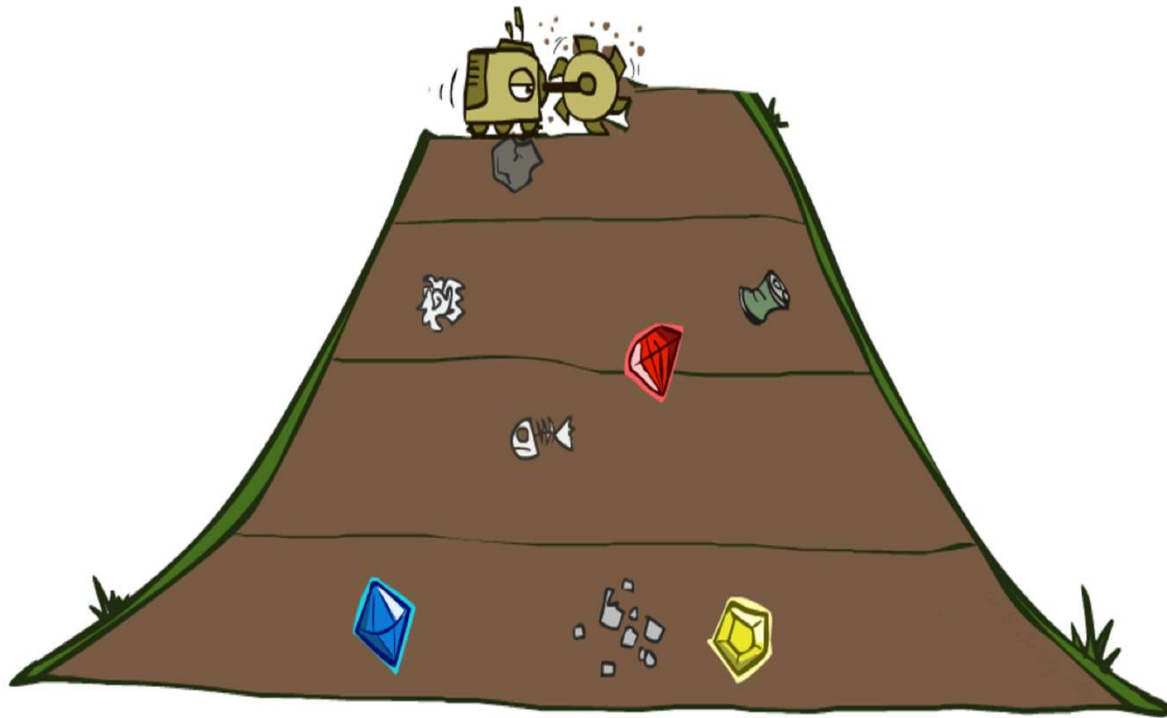
- m could be infinite, so only if we prevent cycles

- Is it optimal?

- No, it finds the “leftmost” solution, regardless of depth or cost



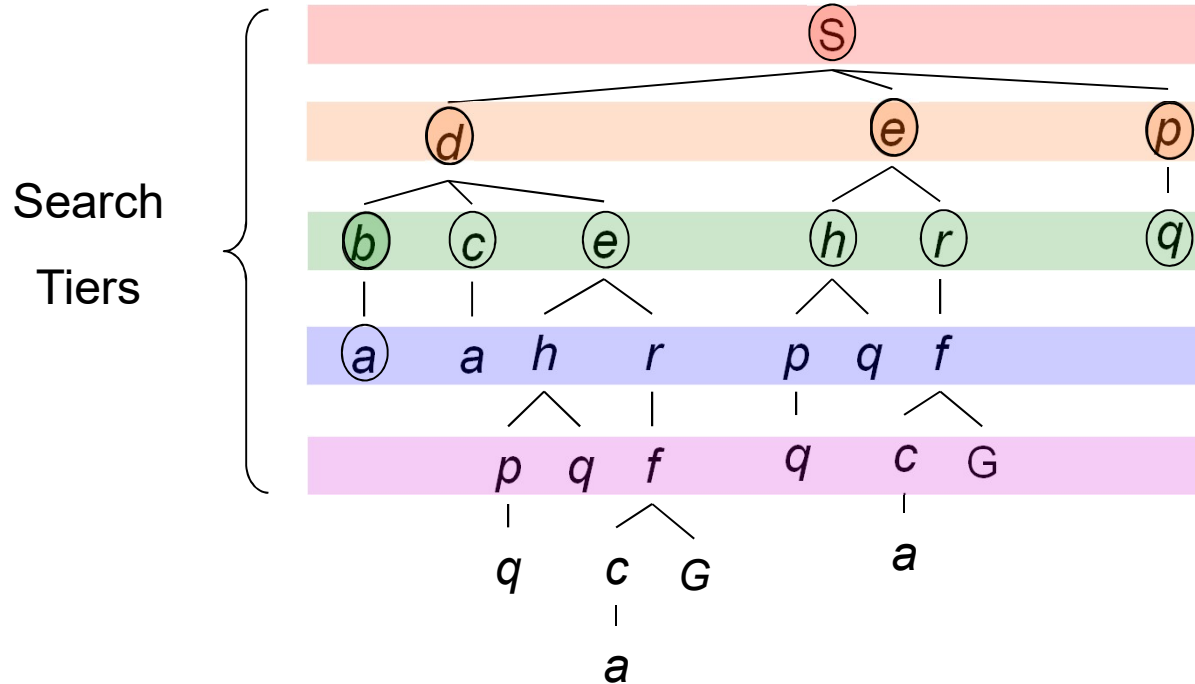
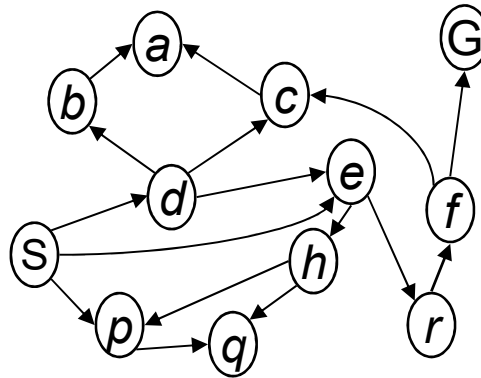
Breadth-First Search



Breadth-First Search

Strategy: expand a shallowest node first

Implementation: Fringe is a FIFO queue



Breadth-First Search (BFS) Properties

- What nodes does BFS expand?

- Processes all nodes above shallowest solution
- Let depth of shallowest solution be d
- Search takes time $O(b^d)$

- How much space does the fringe take?

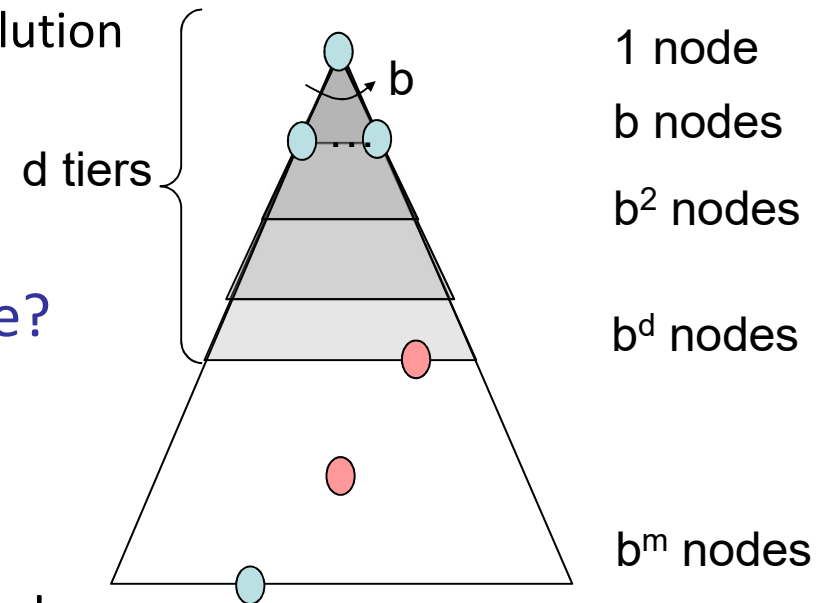
- Has roughly the last tier, so $O(b^d)$

- Is it complete?

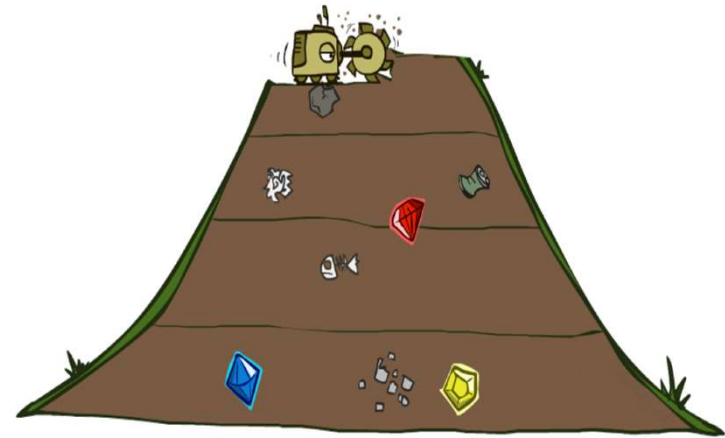
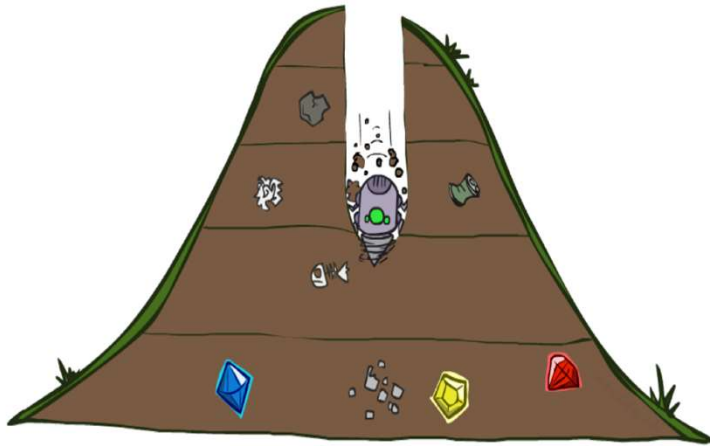
- d must be finite if a solution exists, so yes!

- Is it optimal?

- Only if costs are all 1 (more on costs later)



DFS vs BFS



Algorithm		Complete	Optimal	Time	Space
DFS	w/ Path Checking	N unless finite	N	$O(b^m)$	$O(bm)$
BFS		Y	Y	$O(b^d)$	$O(b^d)$

Memory a Limitation?

- **Suppose:**

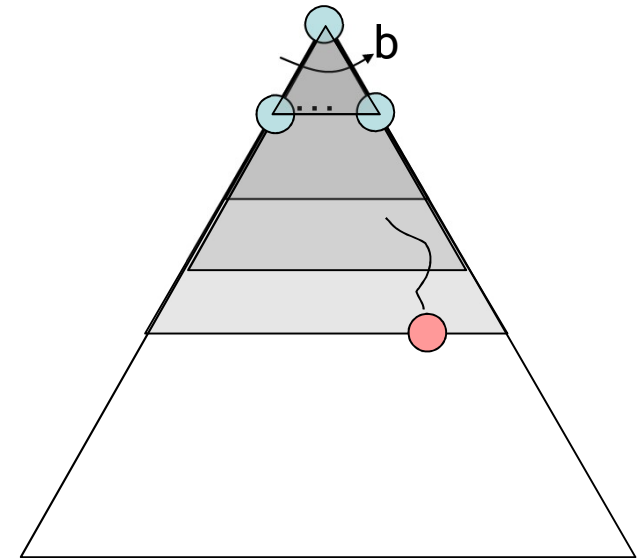
- 4 GHz CPU
 - 32 GB main memory
 - 100 instructions / expansion
 - 5 bytes / node
-
- 40 M expansions / sec
 - Memory filled in 160 sec ... 3 min

Iterative Deepening

Iterative deepening uses DFS as a subroutine:

1. Do a DFS which only searches for paths of length 1 or less.
2. If “1” failed, do a DFS which only searches paths of length 2 or less.
3. If “2” failed, do a DFS which only searches paths of length 3 or less.

....and so on.

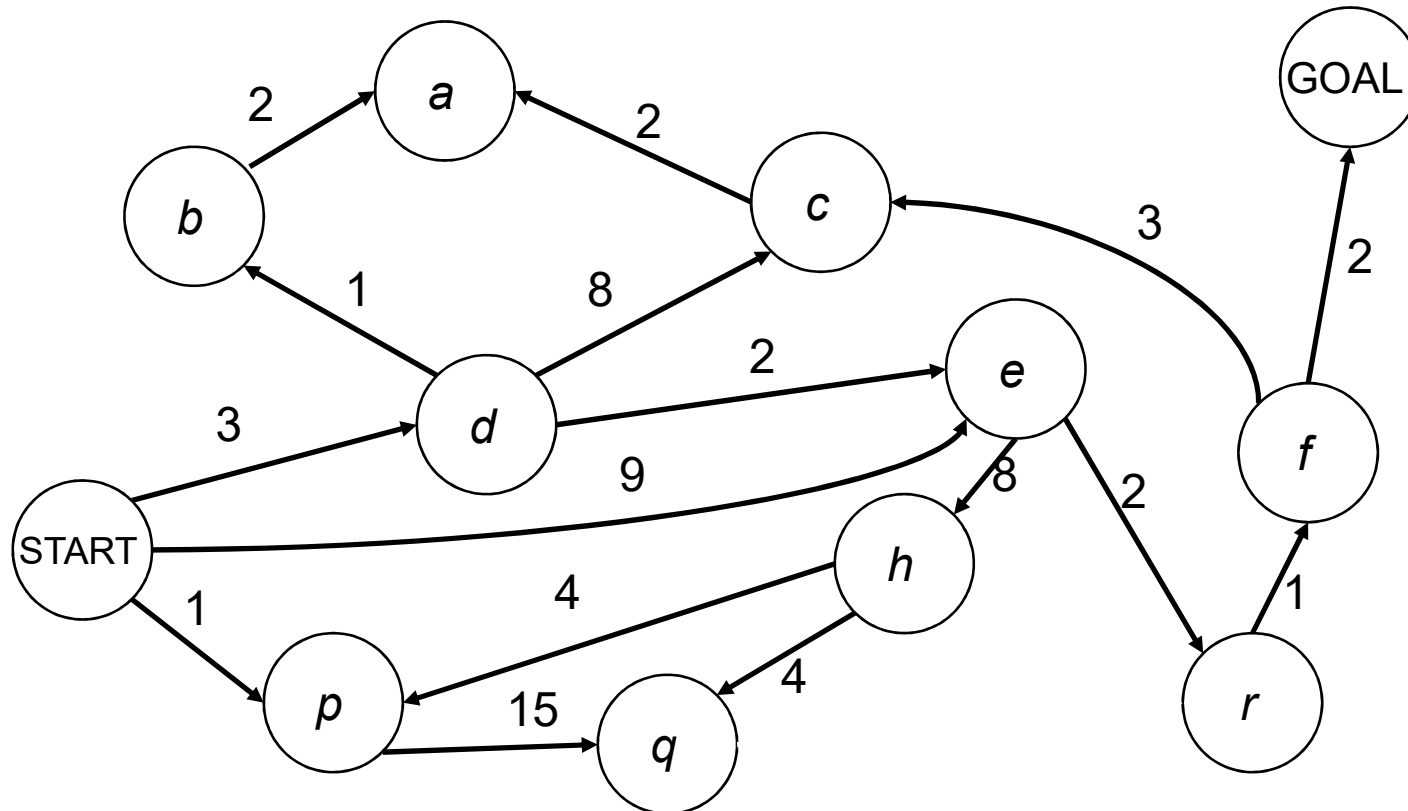


Algorithm		Complete	Optimal	Time	Space
DFS	w/ Path Checking	Y	N	$O(b^m)$	$O(bm)$
BFS		Y	Y	$O(b^d)$	$O(b^d)$
ID		Y	Y	$O(b^d)$	$O(bd)$

BFS vs. Iterative Deepening

- For $b = 10$, $d = 5$:
- $\text{BFS} = 1 + 10 + 100 + 1,000 + 10,000 + 100,000 = 111,111$
- $\text{IDS} = 6 + 50 + 400 + 3,000 + 20,000 + 100,000 = 123,456$
- $\text{Overhead} = (123,456 - 111,111) / 111,111 = 11\%$
- Memory BFS: 100,000; IDS: 50

Costs on Actions

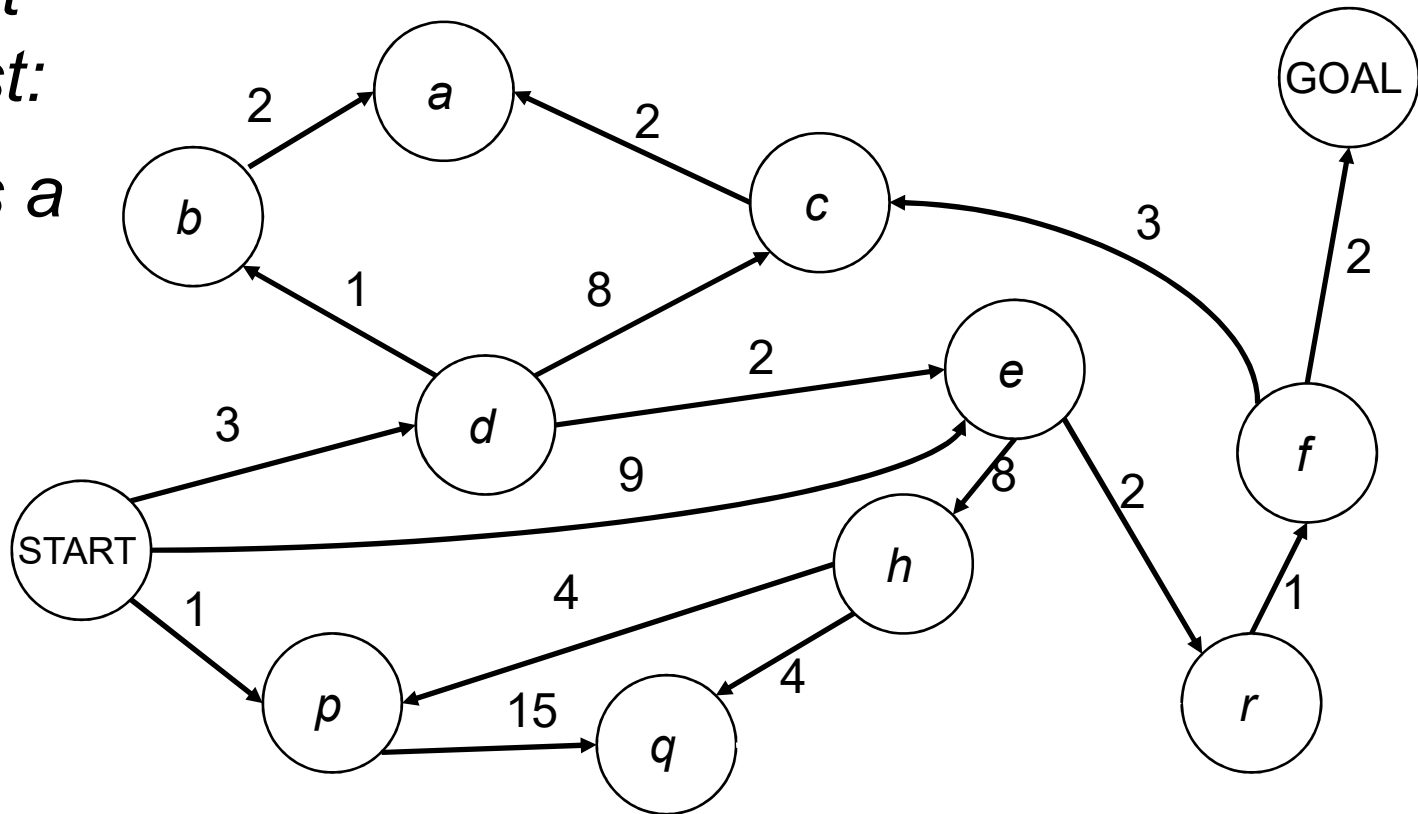


Notice that BFS finds the shortest path in terms of number of transitions. It does not find the least-cost path.

Uniform Cost Search

*Expand
cheapest
node first:*

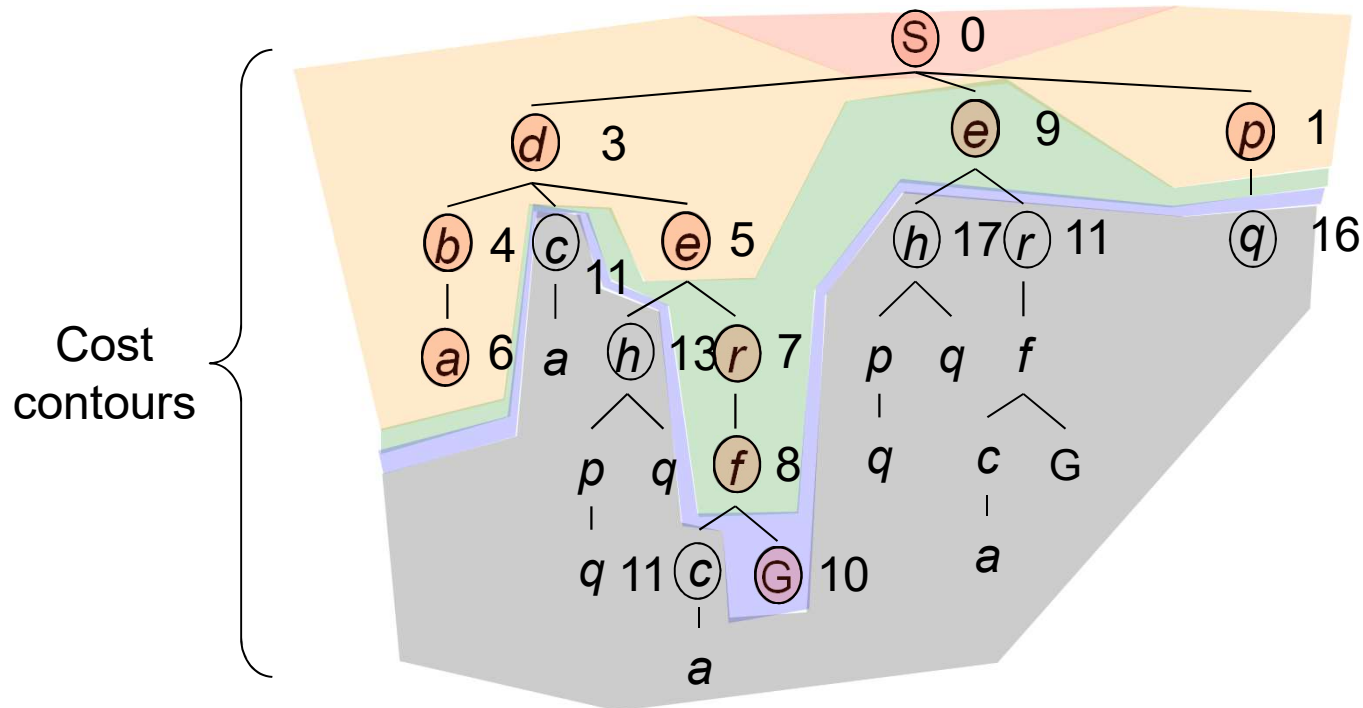
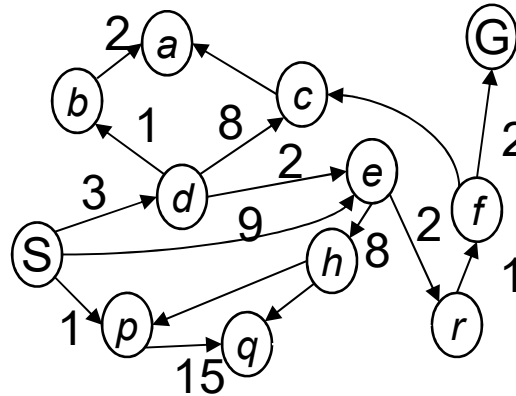
*Fringe is a
priority
queue*



Uniform Cost Search

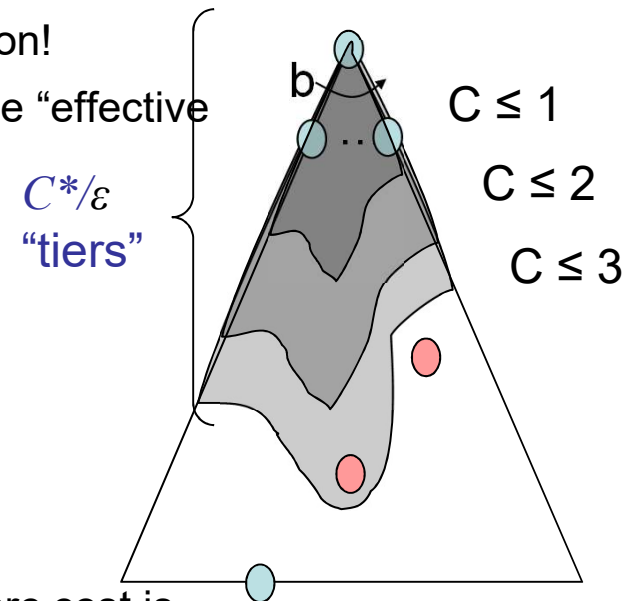
Strategy: expand a cheapest node first:

Fringe is a priority queue (priority: cumulative cost)



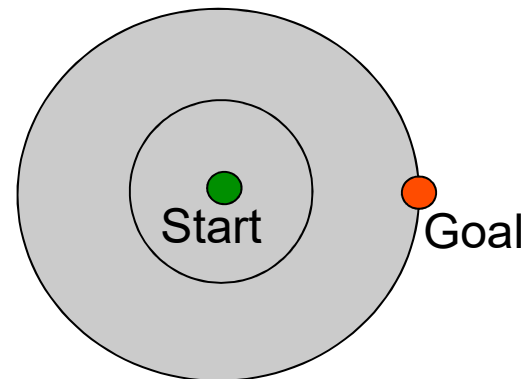
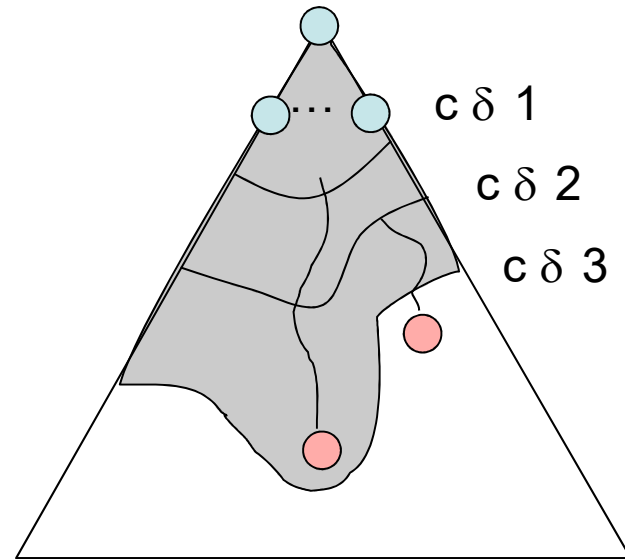
Uniform Cost Search (UCS) Properties

- What nodes does UCS expand?
 - Processes all nodes with cost less than cheapest solution!
 - If that solution costs C^* and arcs cost at least ϵ , then the “effective depth” is roughly C^*/ϵ
 - Takes time $O(b^{C^*/\epsilon})$ (exponential in effective depth)
- How much space does the fringe take?
 - Has roughly the last tier, so $O(b^{C^*/\epsilon})$
- Is it complete?
 - Assuming best solution has a finite cost and minimum arc cost is positive, yes!
- Is it optimal?
 - Yes!



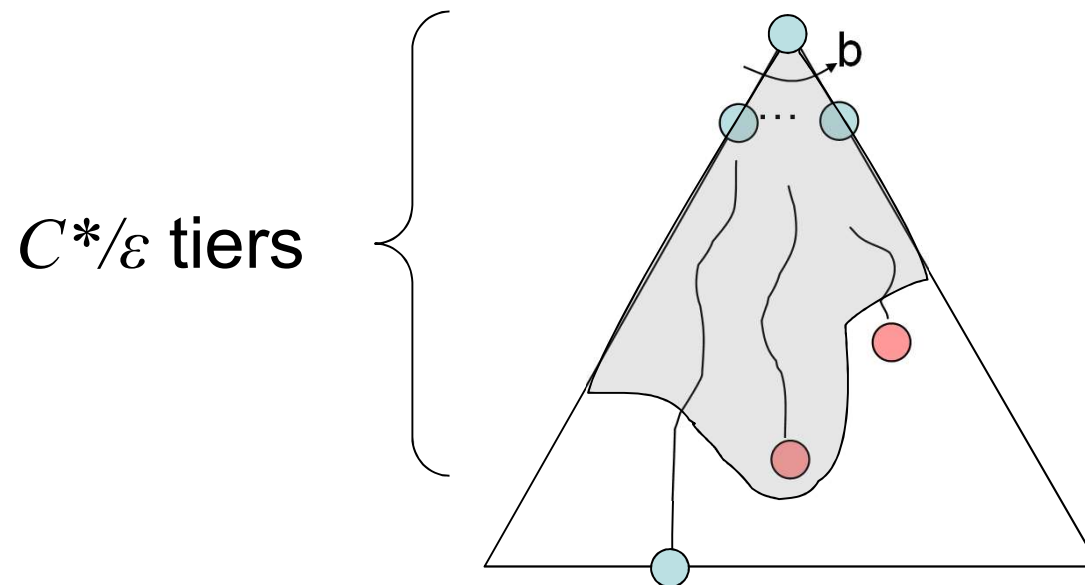
Uniform Cost Search

- Strategy: expand lowest path cost
- The good: UCS is complete and optimal!
- The bad:
 - Explores options in every “direction”
 - No information about goal location



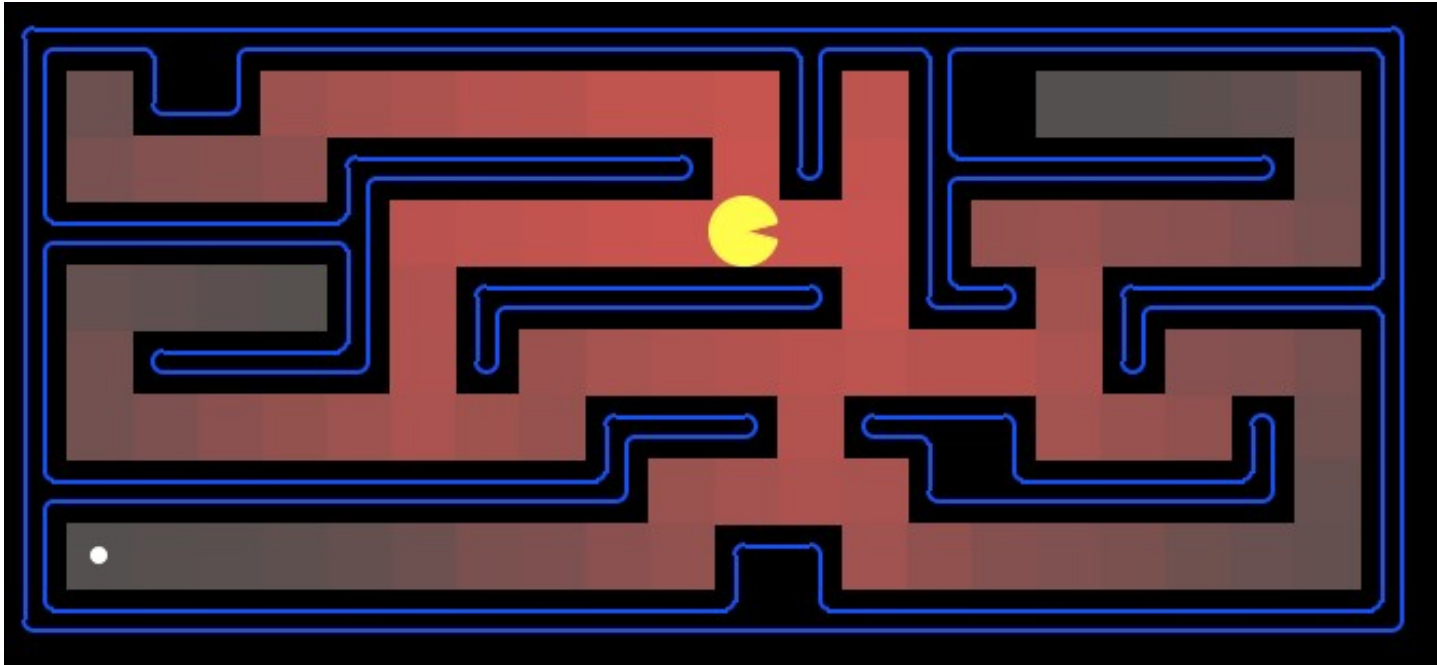
Uniform Cost Search

Algorithm		Complete	Optimal	Time	Space
DFS	w/ Path Checking	Y	N	$O(b^m)$	$O(bm)$
BFS		Y	Y	$O(b^d)$	$O(b^d)$
UCS		Y*	Y	$O(b^{C^*/\epsilon})$	$O(b^{C^*/\epsilon})$



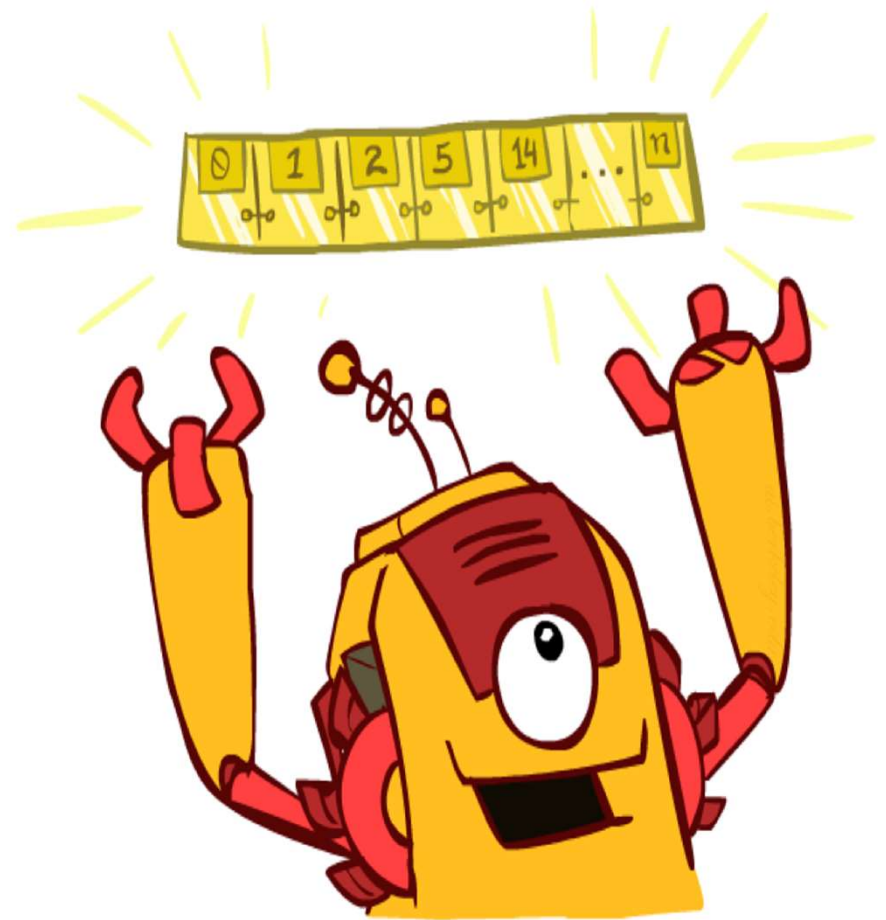
Uniform Cost: Pac-Man

- Cost of 1 for each action
- Explores all of the states, but one



The One Queue

- All these search algorithms are the same except for fringe strategies
 - Conceptually, all fringes are priority queues (i.e. collections of nodes with attached priorities)
 - Practically, for DFS and BFS, you can avoid the $\log(n)$ overhead from an actual priority queue, by using stacks and queues
 - Can even code one implementation that takes a variable queuing object



To Do:

- Look at the course website:
 - <http://http://courses.cs.washington.edu/courses/cse473/18sp/>
- Do the readings (Ch 3)
- Do Project 0 if new to Python
- Start Project 1.