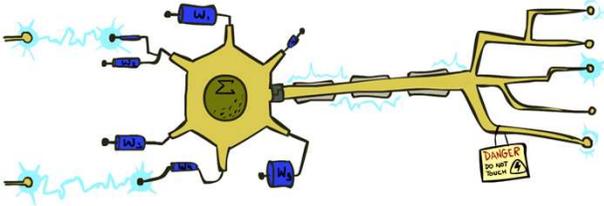


## CSE 473: Artificial Intelligence Perceptrons



Steve Tanimoto --- University of Washington

[These slides were created by Dan Klein and Pieter Abbeel for CS188 Intro to AI at UC Berkeley. All CS188 materials are available at <http://ai.berkeley.edu>.]

## Error-Driven Classification



## Errors, and What to Do

### Examples of errors

Dear GlobalSCAPE Customer,  
GlobalSCAPE has partnered with ScanSoft to offer you the latest version of OmniPage Pro, for just \$99.99\* - the regular list price is \$499! The most common question we've received about this offer is - Is this genuine? We would like to assure you that this offer is authorized by ScanSoft, is genuine and valid. You can get the . . .

. . . To receive your \$30 Amazon.com promotional certificate, click through to <http://www.amazon.com/apparel> and see the prominent link for the \$30 offer. All details are there. We hope you enjoyed receiving this message. However, if you'd rather not receive future e-mails announcing new store launches, please click . . .

## What to Do About Errors

- Problem: there's still spam in your inbox
- Need more **features** – words aren't enough!
  - Have you emailed the sender before?
  - Have 1M other people just gotten the same email?
  - Is the sending information consistent?
  - Is the email in ALL CAPS?
  - Do inline URLs point where they say they point?
  - Does the email address you by (your) name?
- Naïve Bayes models can incorporate a variety of features, but tend to do best in homogeneous cases (e.g. all features are word occurrences)

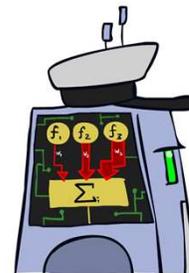
## Later On...

Web Search

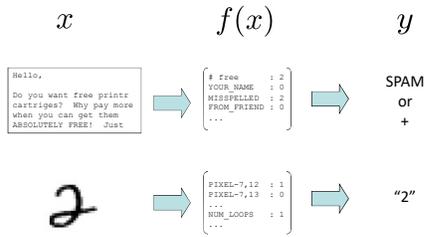


Decision Problems

## Linear Classifiers

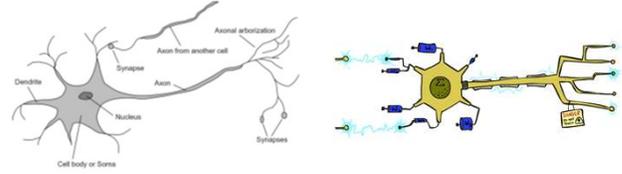


## Feature Vectors



## Some (Simplified) Biology

- Very loose inspiration: human neurons



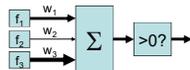
## Linear Classifiers

- Inputs are **feature values**
- Each feature has a **weight**
- Sum is the **activation**



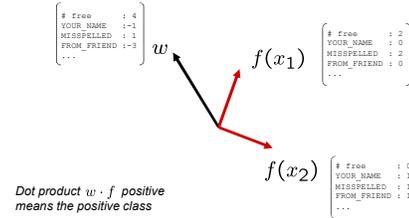
$$\text{activation}_w(x) = \sum_i w_i \cdot f_i(x) = w \cdot f(x)$$

- If the activation is:
  - Positive, output +1
  - Negative, output -1

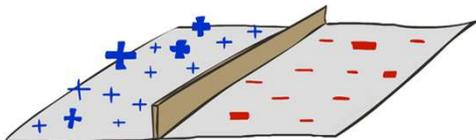


## Weights

- Binary case: compare features to a weight vector
- Learning: figure out the weight vector from examples

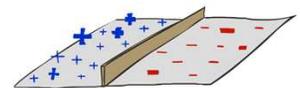


## Decision Rules



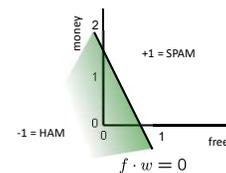
## Binary Decision Rule

- In the space of feature vectors
  - Examples are points
  - Any weight vector is a hyperplane
  - One side corresponds to  $Y=+1$
  - Other corresponds to  $Y=-1$



$w$

$\begin{bmatrix} \text{BIAS} & : -3 \\ \text{free} & : 4 \\ \text{money} & : 2 \\ \dots & \end{bmatrix}$

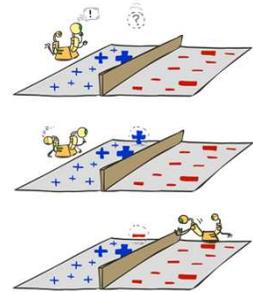


## Weight Updates



## Learning: Binary Perceptron

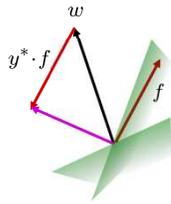
- Start with weights = 0
- For each training instance:
  - Classify with current weights
- If correct (i.e.,  $y=y^*$ ), no change!
- If wrong: adjust the weight vector



## Learning: Binary Perceptron

- Start with weights = 0
- For each training instance:
  - Classify with current weights
- If correct (i.e.,  $y=y^*$ ), no change!
- If wrong: adjust the weight vector by adding or subtracting the feature vector. Subtract if  $y^*$  is -1.

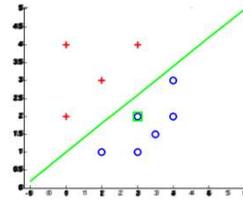
$$y = \begin{cases} +1 & \text{if } w \cdot f(x) \geq 0 \\ -1 & \text{if } w \cdot f(x) < 0 \end{cases}$$



$$w = w + y^* \cdot f$$

## Examples: Perceptron

- Separable Case



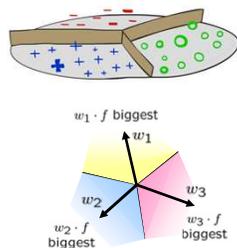
## Multiclass Decision Rule

- If we have multiple classes:
  - A weight vector for each class:  $w_y$

- Score (activation) of a class  $y$ :  $w_y \cdot f(x)$

- Prediction highest score wins

$$y = \arg \max_y w_y \cdot f(x)$$



Binary = multiclass where the negative class has weight zero

## Learning: Multiclass Perceptron

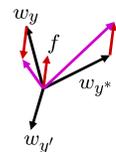
- Start with all weights = 0
- Pick up training examples one by one
- Predict with current weights

$$y = \arg \max_y w_y \cdot f(x)$$

- If correct, no change!
- If wrong: lower score of wrong answer, raise score of right answer

$$w_y = w_y - f(x)$$

$$w_{y^*} = w_{y^*} + f(x)$$



## Example: Multiclass Perceptron

“win the vote”  
 “win the election”  
 “win the game”

$w_{SPORTS}$

BIAS	: 1
win	: 0
game	: 0
vote	: 0
the	: 0
...	

$w_{POLITICS}$

BIAS	: 0
win	: 0
game	: 0
vote	: 0
the	: 0
...	

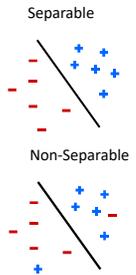
$w_{TECH}$

BIAS	: 0
win	: 0
game	: 0
vote	: 0
the	: 0
...	

## Properties of Perceptrons

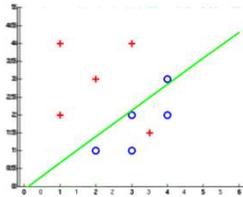
- Separability: true if some parameters get the training set perfectly correct
- Convergence: if the training is separable, perceptron will eventually converge (binary case)
- Mistake Bound: the maximum number of mistakes (binary case) related to the *margin* or degree of separability

$$\text{mistakes} < \frac{k}{\delta^2}$$

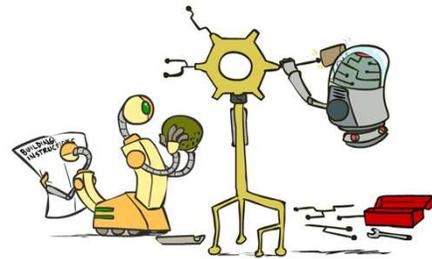


## Examples: Perceptron

- Non-Separable Case

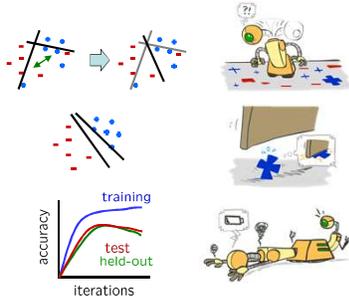


## Improving the Perceptron



## Problems with the Perceptron

- Noise: if the data isn't separable, weights might thrash
  - Averaging weight vectors over time can help (averaged perceptron)
- Mediocre generalization: finds a “barely” separating solution
- Overtraining: test / held-out accuracy usually rises, then falls
  - Overtraining is a kind of overfitting

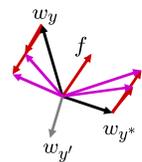


## Fixing the Perceptron

- Idea: adjust the weight update to mitigate these effects
- MIRA\*: choose an update size that fixes the current mistake...
- ... but, minimizes the change to  $w$

$$\min_w \frac{1}{2} \sum_y \|w_y - w'_y\|^2$$

$$w_{y^*} \cdot f(x) \geq w_y \cdot f(x) + 1$$



Guessed  $y$  instead of  $y^*$  on example  $x$  with features  $f(x)$

$$w_y = w'_y - \tau f(x)$$

$$w_{y^*} = w_{y^*} + \tau f(x)$$

\* Margin Infused Relaxed Algorithm

## Minimum Correcting Update

$$\min_w \frac{1}{2} \sum_y \|w_y - w'_y\|^2$$

$$w_{y^*} \cdot f \geq w_y \cdot f + 1$$

$$\min_{\tau} \|\tau f\|^2$$

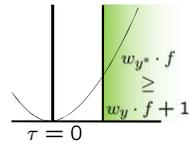
$$w_{y^*} \cdot f \geq w_y \cdot f + 1$$

$$(w'_{y^*} + \tau f) \cdot f = (w'_y - \tau f) \cdot f + 1$$

$$\tau = \frac{(w'_y - w'_{y^*}) \cdot f + 1}{2f \cdot f}$$

$$w_y = w'_y - \tau f(x)$$

$$w_{y^*} = w'_{y^*} + \tau f(x)$$

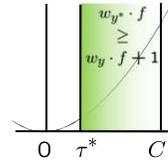


min not  $\tau=0$ , or would not have made an error, so min will be where equality holds

## Maximum Step Size

- In practice, it's also bad to make updates that are too large
  - Example may be labeled incorrectly
  - You may not have enough features
- Solution: cap the maximum possible value of  $\tau$  with some constant  $C$

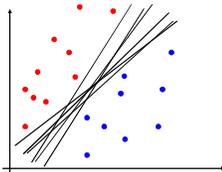
$$\tau^* = \min \left( \frac{(w'_y - w'_{y^*}) \cdot f + 1}{2f \cdot f}, C \right)$$



- Corresponds to an optimization that assumes non-separable data
- Usually converges faster than perceptron
- Usually better, especially on noisy data

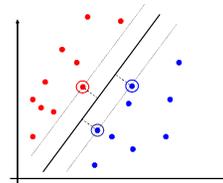
## Linear Separators

- Which of these linear separators is optimal?



## Support Vector Machines

- Maximizing the margin: good according to intuition, theory, practice
- Only support vectors matter; other training examples are ignorable
- Support vector machines (SVMs) find the separator with max margin
- Basically, SVMs are MIRA where you optimize over all examples at once



MIRA

$$\min_w \frac{1}{2} \|w - w'\|^2$$

$$w_{y^*} \cdot f(x_i) \geq w_y \cdot f(x_i) + 1$$

SVM

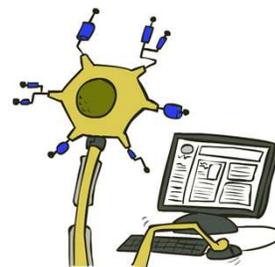
$$\min_w \frac{1}{2} \|w\|^2$$

$$\forall i, y \quad w_{y^*} \cdot f(x_i) \geq w_y \cdot f(x_i) + 1$$

## Classification: Comparison

- Naïve Bayes
  - Builds a model training data
  - Gives prediction probabilities
  - Strong assumptions about feature independence
  - One pass through data (counting)
- Perceptrons / MIRA:
  - Makes less assumptions about data
  - Mistake-driven learning
  - Multiple passes through data (prediction)
  - Often more accurate

## Web Search



## Extension: Web Search

- Information retrieval:
  - Given information needs, produce information
  - Includes, e.g. web search, question answering, and classic IR
- Web search: not exactly classification, but rather ranking

$x = \text{"Apple Computers"}$



## Feature-Based Ranking

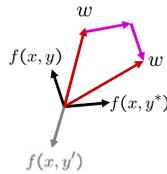
$x = \text{"Apple Computer"}$

$$f(x, \text{Apple Inc.}) = [0.3 \ 5 \ 0 \ 0 \ \dots]$$

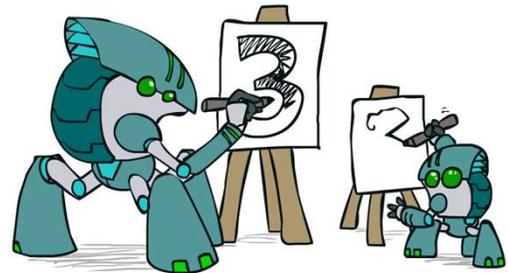
$$f(x, \text{Apple}) = [0.8 \ 4 \ 2 \ 1 \ \dots]$$

## Perceptron for Ranking

- Inputs  $x$
- Candidates  $y$
- Many feature vectors:  $f(x, y)$
- One weight vector:  $w$ 
  - Prediction:
 
$$y = \arg \max_y w \cdot f(x, y)$$
  - Update (if wrong):
 
$$w = w + f(x, y^*) - f(x, y)$$



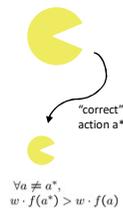
## Apprenticeship



## Pacman Apprenticeship!

- Examples are states  $s$ 

- Candidates are pairs  $(s, a)$
- "Correct" actions: those taken by expert
- Features defined over  $(s, a)$  pairs:  $f(s, a)$
- Score of a  $q$ -state  $(s, a)$  given by:
 
$$w \cdot f(s, a)$$



- How is this VERY different from reinforcement learning?

[Demo: Pacman Apprentice (L22D1.2.3)]

## Video of Demo Pacman Apprentice

