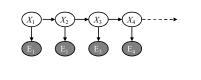
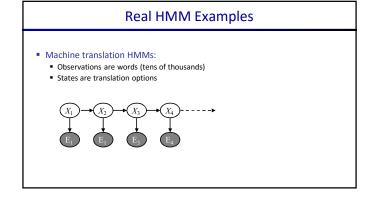
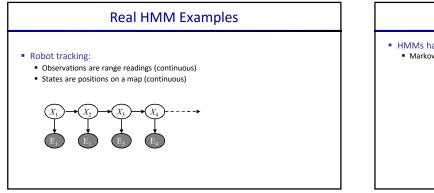


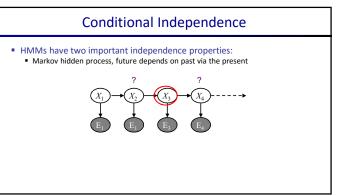
Real HMM Examples

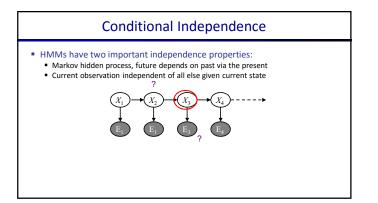
- Speech recognition HMMs:
 - Observations are acoustic signals (continuous valued)
 - States are specific positions in specific words (so, tens of thousands)

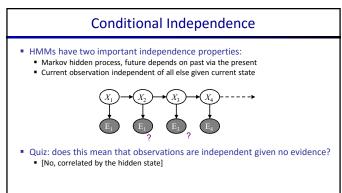






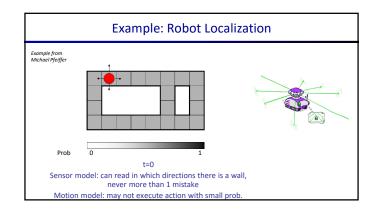


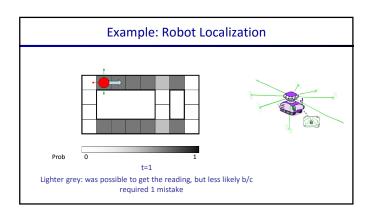


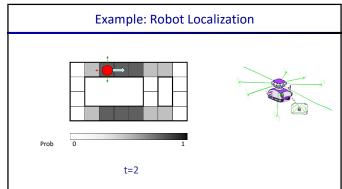


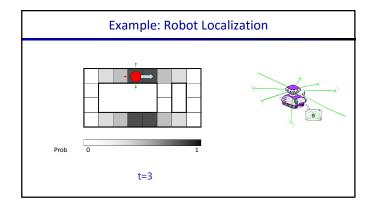
Filtering / Monitoring

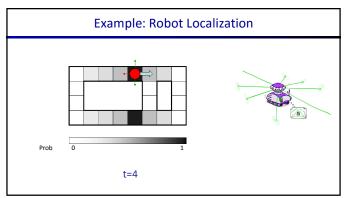
- Filtering, or monitoring, is the task of tracking the distribution B(X) (the belief state) over time
- We start with B(X) in an initial setting, usually uniform
- As time passes, or we get observations, we update B(X)
- The Kalman filter (one method Real valued values)
 invented in the 60's as a method of trajectory estimation for the Apollo program

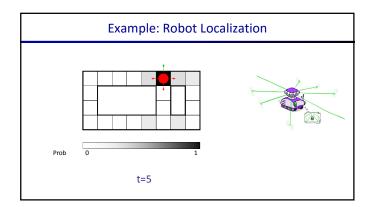


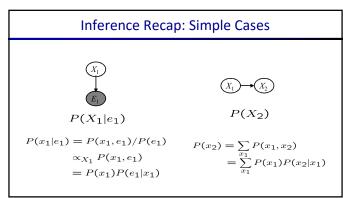


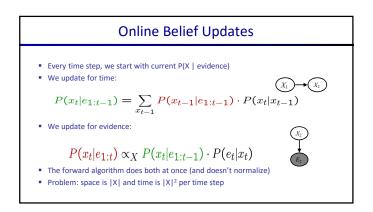


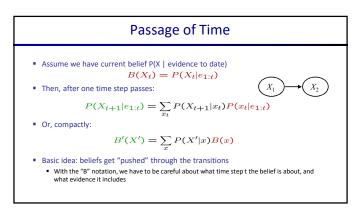


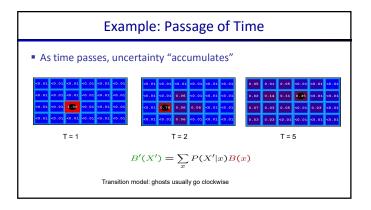


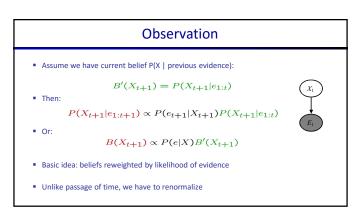


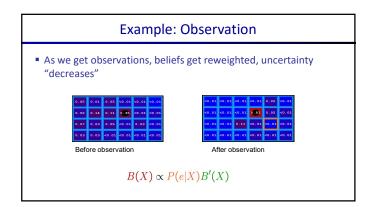


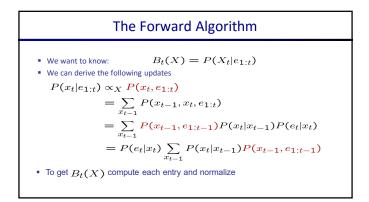


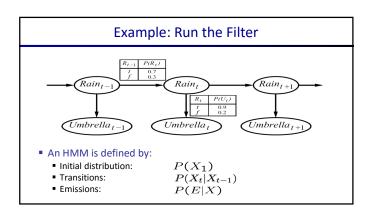


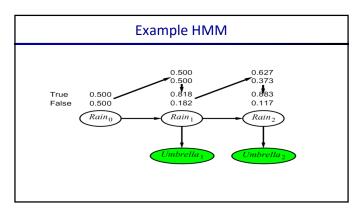


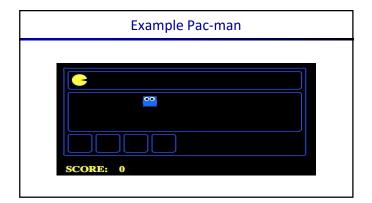


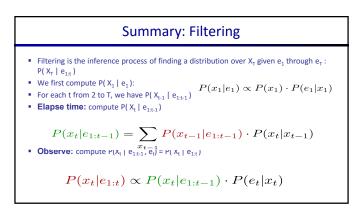


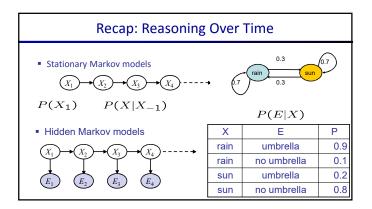




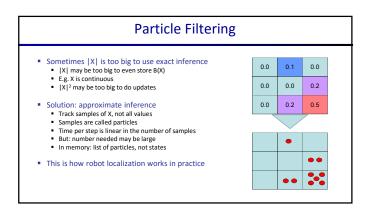


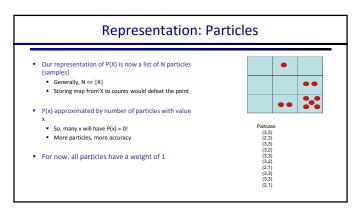


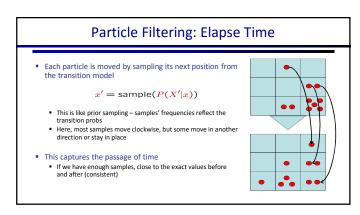


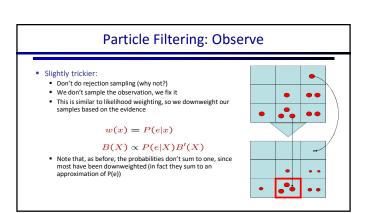


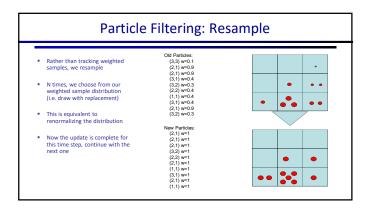
Recap: Filtering		
Elapse time: compute P(X _t e _{1:t-1}) $P(x_t e_{1:t-1}) = \sum_{x_{t-1}} P(x_{t-1} e_{1:t-1}) \cdot P(x_t x_{t-1})$ Observe: compute P(X _t e _{1:t}) $P(x_t e_{1:t}) \propto P(x_t e_{1:t-1}) \cdot P(e_t x_t)$		
Belief: <p(rain), p(sun)=""></p(rain),>		
$\begin{pmatrix} X_{1} \end{pmatrix}$ $\begin{pmatrix} X_{2} \end{pmatrix}$ $P(X_{1})$	<0.5, 0.5>	Prior on X_1
$P(X_1 \mid E_1 = umbrella)$	<0.82, 0.18>	Observe
(\underline{E}_1) (\underline{E}_2) $P(X_2 \mid E_1 = umbrella)$	<0.63, 0.37>	Elapse time
$P(X_2 \mid E_1 = umb, E_2 = umb)$	<0.88, 0.12>	Observe

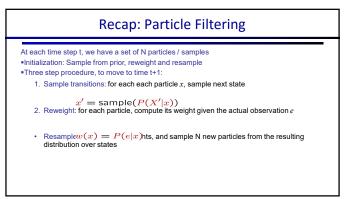












Particle Filtering Summary

- Represent current belief P(X | evidence to date) as set of n samples (actual assignments X=x)
- For each new observation e:
 - 1. Sample transition, once for each current particle \boldsymbol{x}
 - x' = sample(P(X'|x))2. For each new sample x', compute importance weights for the new evidence e:

$$w(x') = P(e|x')$$

3. Finally, normalize the importance weights and resample N new particles

