

## **Policy Iteration**

- Alternative approach for optimal values:
  - Step 1: Policy evaluation: calculate utilities for some fixed policy (not optimal utilities!) until convergence

$$V_{k+1}^{\pi_i}(s) \leftarrow \sum_{s'} T(s, \pi_i(s), s') \left[ R(s, \pi_i(s), s') + \gamma V_k^{\pi_i}(s') \right]$$

• Step 2: Policy improvement: update policy using one-step look-ahead with resulting converged (but not optimal!) utilities as future values

$$\pi_{i+1}(s) = \arg\max_{a} \sum_{s} T(s, a, s') \left[ R(s, a, s') + \gamma V^{\pi_i}(s') \right]$$

- Repeat steps until policy converges
- This is policy iteration
  - It's still optimal! Can converge (much) faster under some conditions

## Comparison

- Both value iteration and policy iteration compute the same thing (all optimal values)

 $V_0^{\pi}(s) = 0$ 

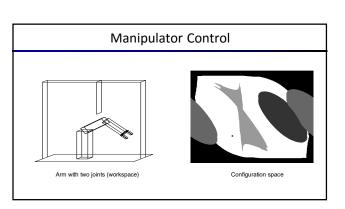
• Every iteration updates both the values and (implicitly) the policy

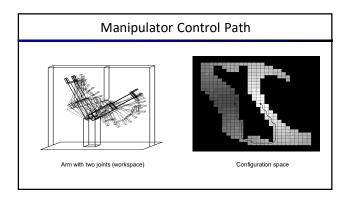
Solve with Matlab (or your favorite linear system solver)

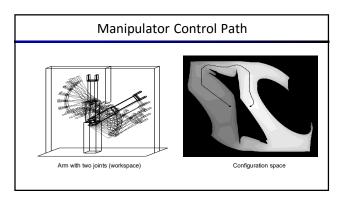
- We don't track the policy, but taking the max over actions implicitly recomputes it
- In policy iteration:
  - We do several passes that update utilities with fixed policy (each pass is fast because we consider only one action, not all of them)
  - After the policy is evaluated, a new policy is chosen (slow like a value iteration pass)
  - The new policy will be better (or we're done)
- Both are dynamic programs for solving MDPs

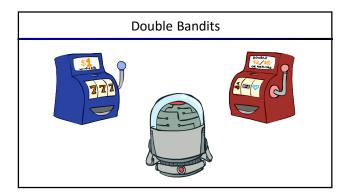
## Summary: MDP Algorithms

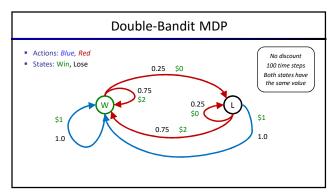
- So you want to....
  - · Compute optimal values: use value iteration or policy iteration
  - Compute values for a particular policy: use policy evaluation
  - Turn your values into a policy: use policy extraction (one-step lookahead)
- These all look the same!
  - They basically are they are all variations of Bellman updates
  - They all use one-step lookahead expectimax fragments
  - They differ only in whether we plug in a fixed policy or max over actions

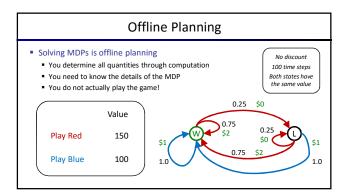


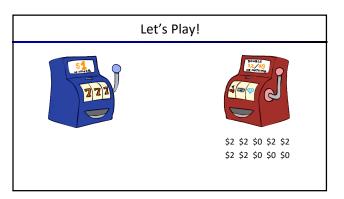


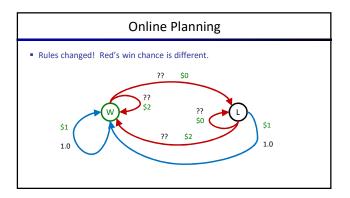


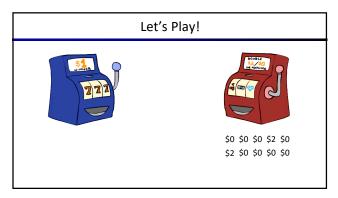












## What Just Happened?

- That wasn't planning, it was learning!
  - Specifically, reinforcement learning
  - There was an MDP, but you couldn't solve it with just computation
  - You needed to actually act to figure it out



- Exploration: you have to try unknown actions to get information
- Exploitation: eventually, you have to use what you know
- Regret: even if you learn intelligently, you make mistakes
- Sampling: because of chance, you have to try things repeatedly
- Difficulty: learning can be much harder than solving a known MDP

