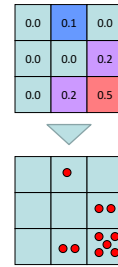


A cartoon map of the United States with arrows pointing to various locations, each with a speech bubble saying "You are here!". The locations include New York, Los Angeles, San Francisco, Chicago, Dallas, Houston, Phoenix, Salt Lake City, Denver, and San Diego. The map also shows the Great Lakes, the Gulf of Mexico, and the Pacific Ocean.

[Most slides were created by Dan Klein and Pieter Abbeel for CS188 Intro to AI at UC Berkeley. All CS188 materials are available at <http://ai.berkeley.edu>.]

- Filtering: approximate solution
- Sometimes $|X|$ is too big to use exact inference
 - $|X|$ may be too big to even store $B(X)$
 - E.g. X is continuous
 - $|X|^2$ may be too big to do updates
- Solution: approximate inference
 - Track samples of X , not all values
 - Samples are called particles
 - Time step is linear in the number of samples
 - But: number needed may be large
 - In memory: list of particles, not states
- This is how robot localization works in practice



Particles:

- (3,3)
- (2,3)
- (3,3)
- (3,2)
- (3,3)
- (3,2)
- (1,2)
- (3,3)
- (3,3)
- (2,3)

- Each particle is moved by sampling its next position from the transition model
$$x' = \text{sample}(P(X'|x))$$
 - This is like prior sampling – samples' frequencies reflect the transition probabilities
 - Here, most samples move clockwise, but some move in another direction or stay in place
- This captures the passage of time
 - If enough samples, close to exact values before and after (consistent)

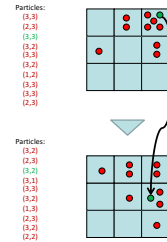
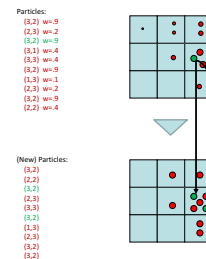


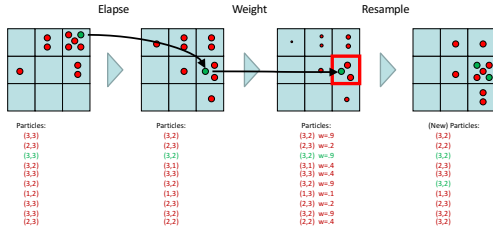
Diagram illustrating the merging of two particles into a new particle. The top part shows two 3x3 grids of particles. The left grid has particles at (1,2), (2,3), (3,2), (3,3), (3,2), (1,3), (2,3), (3,2), and (2,2). The right grid has particles at (1,2), (1,3), (2,3), (3,2), (3,3), (3,2), (3,3), (3,2), and (3,3). A blue arrow points from the right grid to a new 3x3 grid below. The new grid has particles at (1,2), (2,3), (3,2), (3,3), (3,2), (1,3), (2,3), (3,2), and (2,2). A red box highlights the particle at (3,3) in the new grid.

- Rather than tracking weighted samples, we resample
- N times, we choose from our weighted sample distribution (i.e. draw with replacement)
- This is equivalent to renormalizing the distribution
- Now the update is complete for this time step, continue with the next one



Recap: Particle Filtering

- Particles: track samples of states rather than an explicit distribution

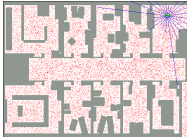


[Demos: ghostbusters particle filtering (11503.4.5)]

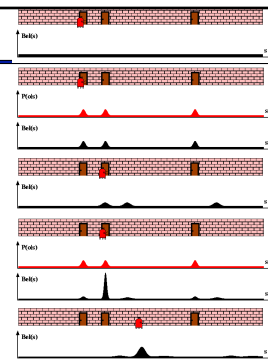
Particle Filters in Robotics

Robot Localization

- In robot localization:
 - We know the map, but not the robot's position
 - Observations may be vectors of range finder readings
 - State space and readings are typically continuous (works basically like a very fine grid) and so we cannot store $B(X)$
 - Particle filtering is a main technique



Bayes Filter for Robot Localization



Bayes Filters: Framework

- Given:**
 - Stream of observations z and action data u :

$$d_t = \{u_1, z_2, \dots, u_{t-1}, z_t\}$$
 - Sensor model $P(z|x)$.
 - Action model $P(x|u, x')$.
 - Prior probability of the system state $P(x)$.
- Wanted:**
 - Estimate of the state X of a **dynamical system**.
 - The posterior of the state is also called **Belief**:

$$Bel(x_t) = P(x_t | u_1, z_2, \dots, u_{t-1}, z_t)$$

11

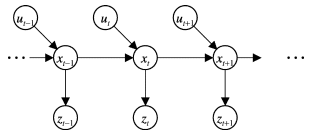
robotic
Robotics

Bayes Filters

z = observation
 u = action
 x = state

$$\begin{aligned}
 Bel(x_t) &= P(x_t | u_1, z_1, \dots, u_t, z_t) \\
 \text{Bayes} &= \eta P(z_t | x_t, u_1, z_1, \dots, u_t) P(x_t | u_1, z_1, \dots, u_t) \\
 \text{Markov} &= \eta P(z_t | x_t) P(x_t | u_1, z_1, \dots, u_t) \\
 \text{Marginal} &= \eta P(z_t | x_t) \int P(x_t | u_1, z_1, \dots, u_t, x_{t-1}) P(x_{t-1} | u_1, z_1, \dots, u_t) dx_{t-1} \\
 \text{Markov} &= \eta P(z_t | x_t) \int P(x_t | u_t, x_{t-1}) P(x_{t-1} | u_1, z_1, \dots, u_t) dx_{t-1} \\
 &= \eta P(z_t | x_t) \int P(x_t | u_t, x_{t-1}) Bel(x_{t-1}) dx_{t-1}
 \end{aligned}$$

Markov Assumption



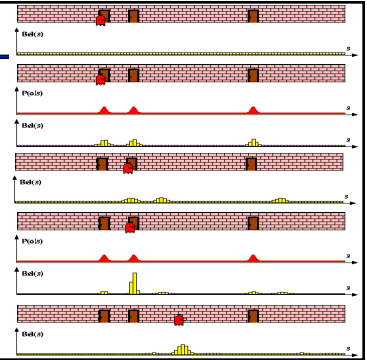
$$p(z_t | x_{0:t}, z_{1:t-1}, u_{1:t}) = p(z_t | x_t)$$

$$p(x_t | x_{1:t-1}, z_{1:t-1}, u_{1:t}) = p(x_t | x_{t-1}, u_t)$$

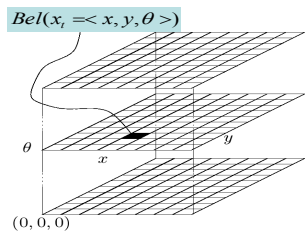
Underlying Assumptions

- Static world
- Independent noise
- Perfect model, no approximation errors

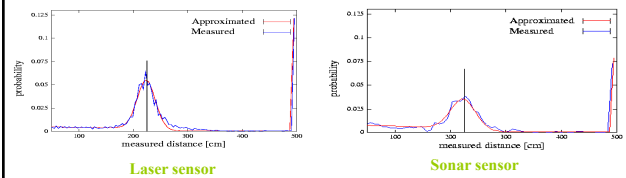
Piecewise Constant Belief



Piecewise Constant Representation



Proximity Sensor Model



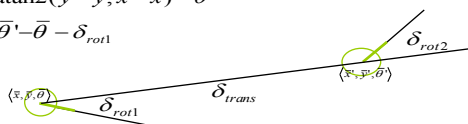
Probabilistic Kinematics

- Robot moves from $\langle \bar{x}, \bar{y}, \bar{\theta} \rangle$ to $\langle \bar{x}', \bar{y}', \bar{\theta}' \rangle$
- Odometry information $u = \langle \delta_{rot1}, \delta_{rot2}, \delta_{trans} \rangle$

$$\delta_{trans} = \sqrt{(\bar{x}' - \bar{x})^2 + (\bar{y}' - \bar{y})^2}$$

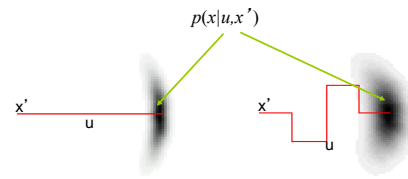
$$\delta_{rot1} = \text{atan2}(\bar{y}' - \bar{y}, \bar{x}' - \bar{x}) - \bar{\theta}$$

$$\delta_{rot2} = \bar{\theta}' - \bar{\theta} - \delta_{rot1}$$

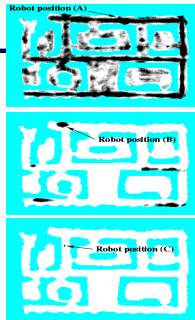
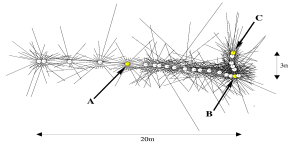


Probabilistic Kinematics

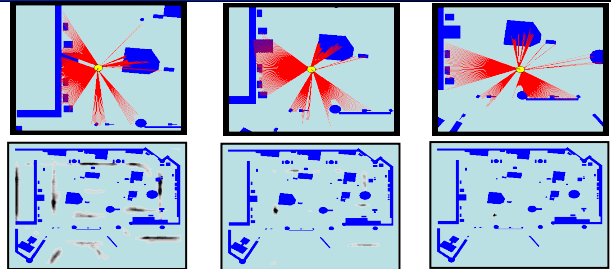
- Odometry information is inherently noisy.



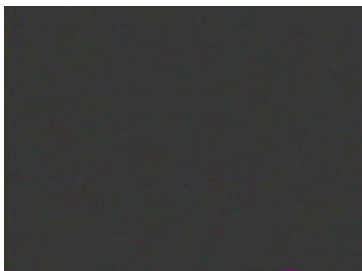
Sonars and Occupancy Grid Map



Laser-based Localization

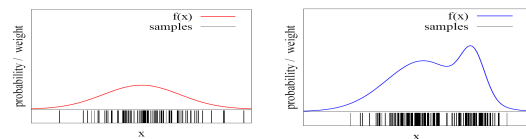


Museum Tourguide Minerva



Sample-Based Density Approximation

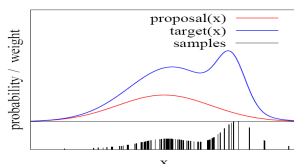
- Particle sets can be used to approximate densities



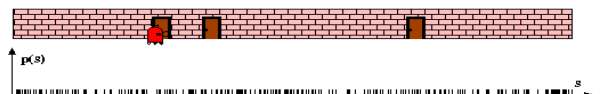
- The more particles fall into an interval, the higher the probability of that interval
- How to draw samples from a function/distribution?

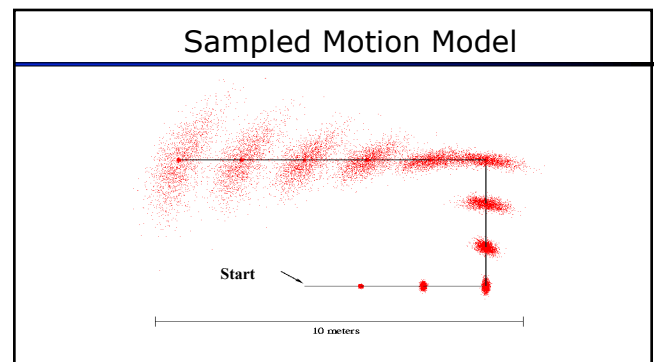
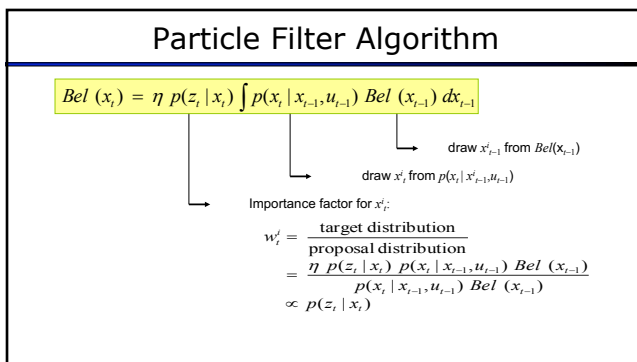
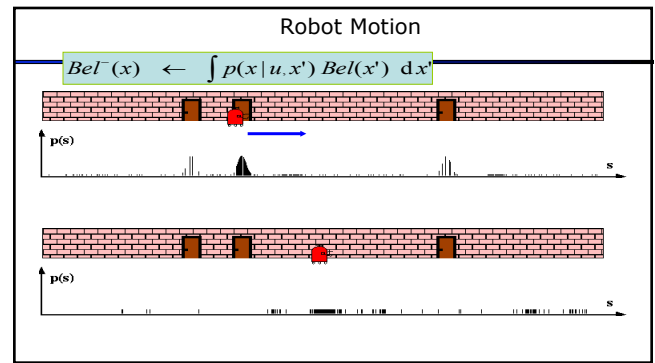
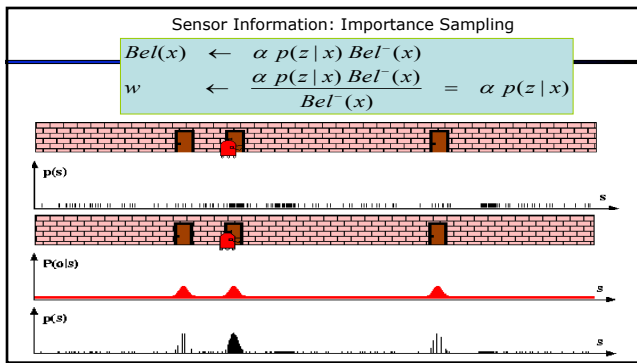
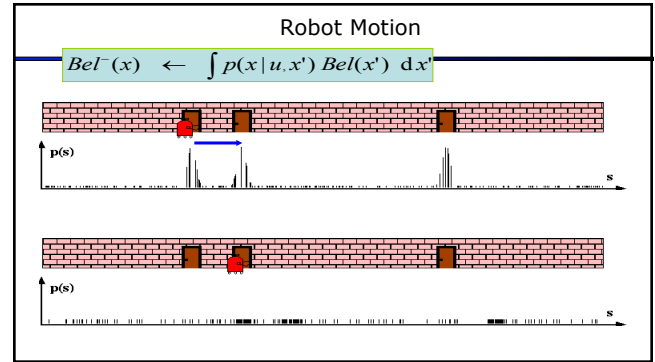
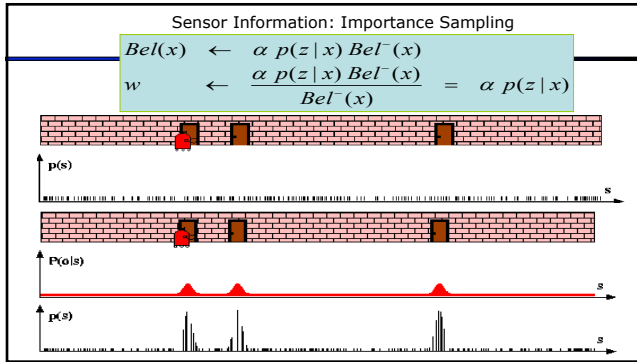
Importance Sampling Principle

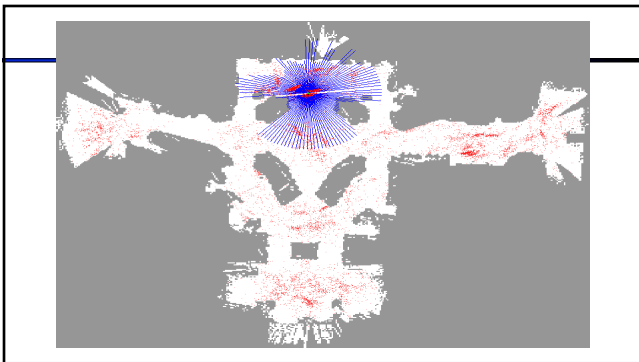
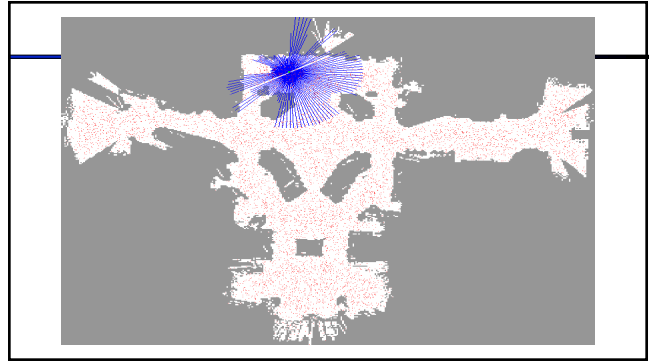
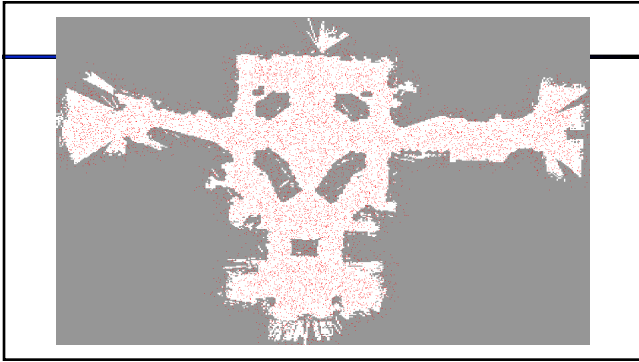
- We can use a different distribution g to generate samples from f
- By introducing an importance weight w , we can account for the "differences between g and f "
- $w = f/g$
- f is often called target
- g is often called proposal

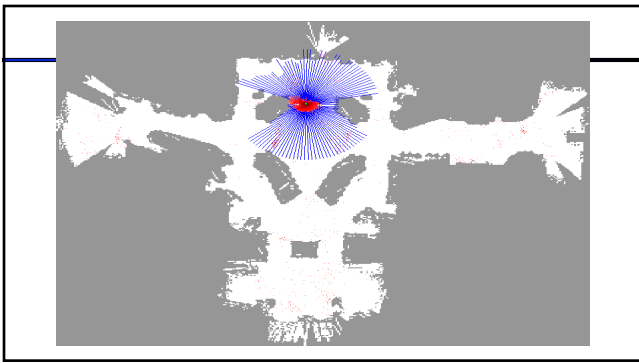
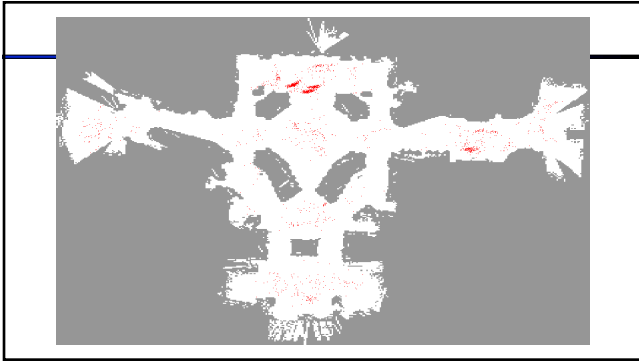


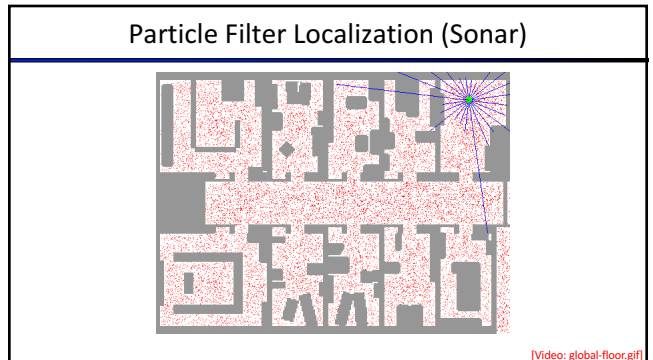
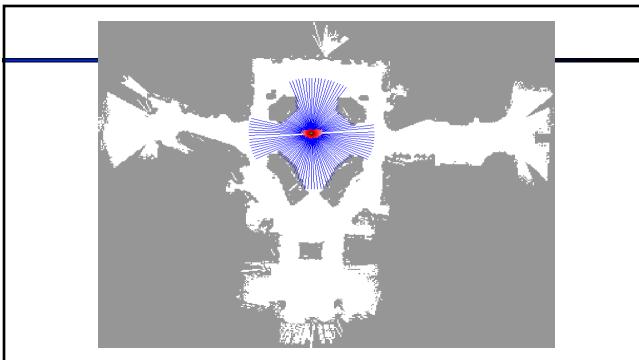
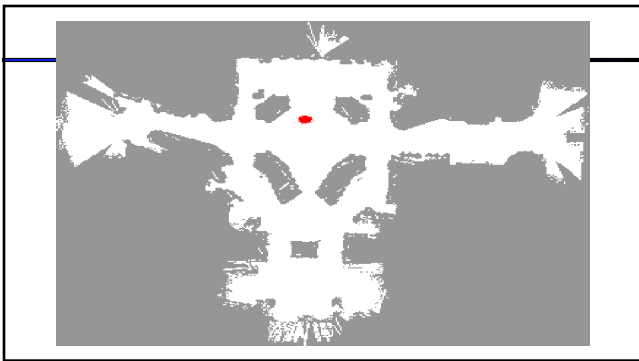
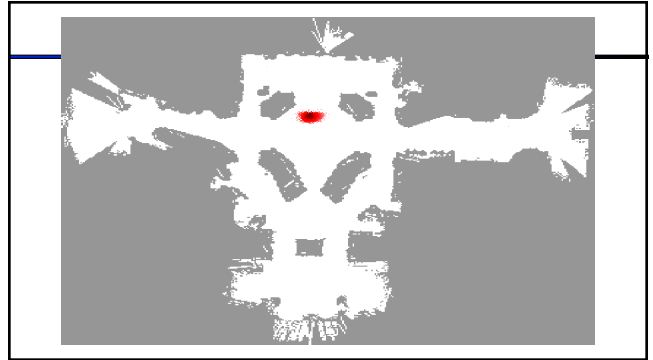
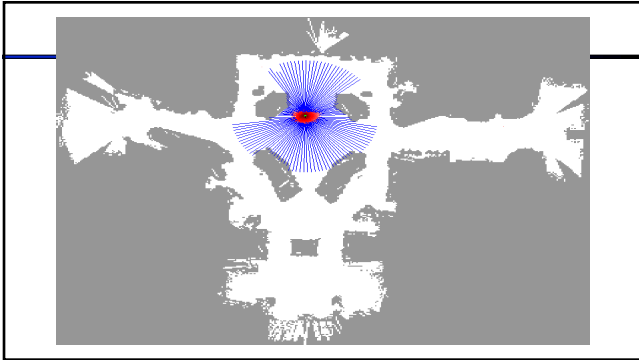
Particle Filters







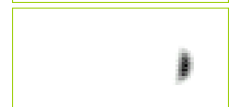
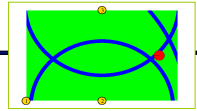




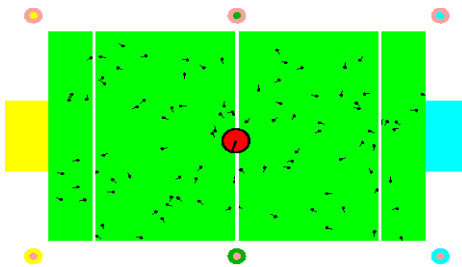
Aibo Sensor Model



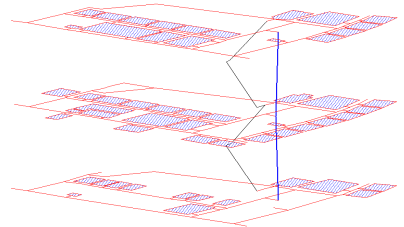
Distributions for $P(z|x)$



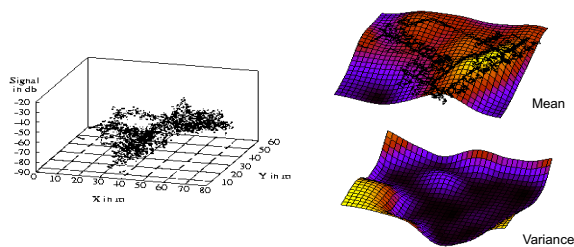
Localization for AIBO robots



WiFi-Based People Tracking

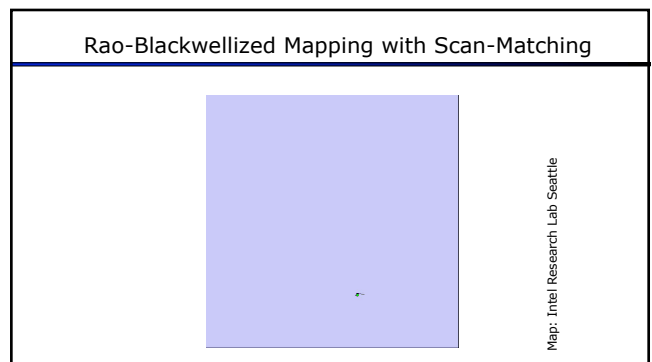
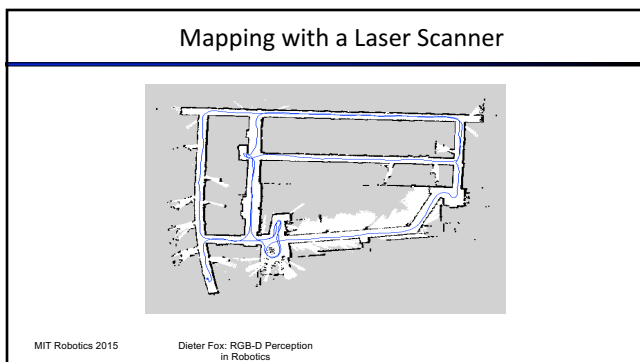
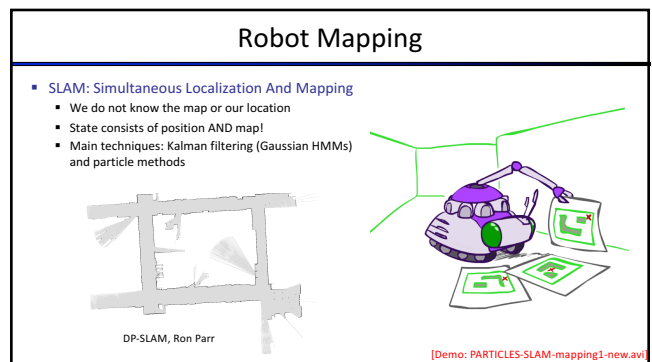
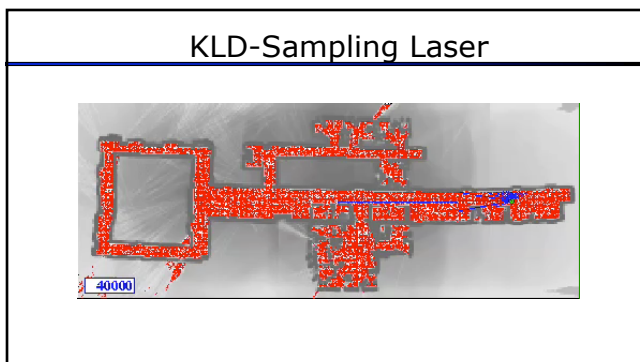
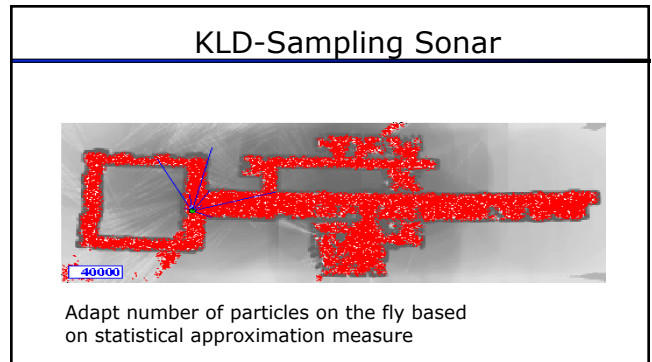
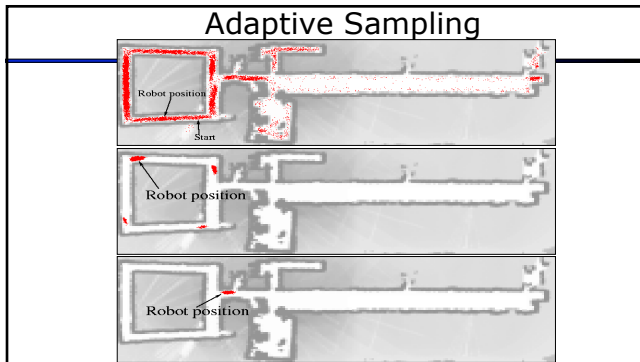


WiFi Sensor Model

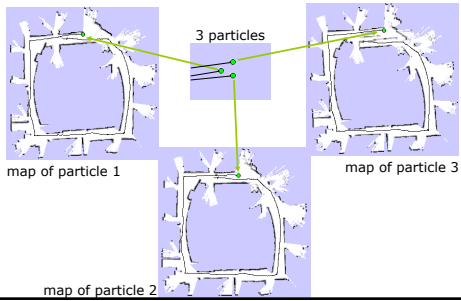


Tracking Example

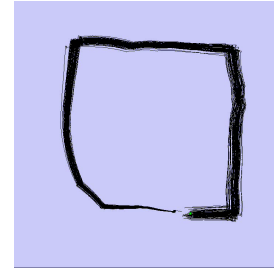




Loop Closure Example

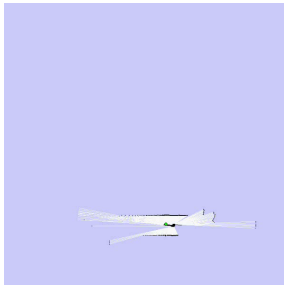


Rao-Blackwellized Mapping with Scan-Matching



Map: Intel Research Lab Seattle

Rao-Blackwellized Mapping with Scan-Matching



Map: Intel Research Lab Seattle

Example (Intel Lab)



- 15 particles
- four times faster than real-time P4, 2.8GHz
- 5cm resolution during scan matching
- 1cm resolution in final map

Work by Grisetti et al.

Outdoor Campus Map



- 30 particles
- 250x250m²
- 1.088 miles (odometry)
- 20cm resolution during scan matching
- 30cm resolution in final map

Work by Grisetti et al.